

Computer algebra independent integration tests

4-Trig-functions/4.7-Miscellaneous/4.7.6-f^{-a+b-x+c-x²-trig-d+e-x+f-x²-ⁿ}

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Contents

1	Introduction	3
1.1	Listing of CAS systems tested	3
1.2	Results	3
1.3	Performance	7
1.4	list of integrals that has no closed form antiderivative	8
1.5	list of integrals solved by CAS but has no known antiderivative	8
1.6	list of integrals solved by CAS but failed verification	8
1.7	Timing	9
1.8	Verification	9
1.9	Important notes about some of the results	9
1.9.1	Important note about Maxima results	9
1.9.2	Important note about FriCAS and Giac/XCAS results	10
1.9.3	Important note about finding leaf size of antiderivative	10
1.9.4	Important note about Mupad results	11
1.10	Design of the test system	11
2	detailed summary tables of results	13
2.1	List of integrals sorted by grade for each CAS	13
2.1.1	Rubi	13
2.1.2	Mathematica	13
2.1.3	Maple	13
2.1.4	Maxima	14
2.1.5	FriCAS	14
2.1.6	Sympy	14
2.1.7	Giac	14
2.1.8	Mupad	14
2.2	Detailed conclusion table per each integral for all CAS systems	16
2.3	Detailed conclusion table specific for Rubi results	39
3	Listing of integrals	45
3.1	$\int F^{c(a+bx)} \sin^n(d+ex) dx$	45
3.2	$\int F^{c(a+bx)} \sin^3(d+ex) dx$	48
3.3	$\int F^{c(a+bx)} \sin^2(d+ex) dx$	52
3.4	$\int F^{c(a+bx)} \sin(d+ex) dx$	56
3.5	$\int F^{c(a+bx)} \csc(d+ex) dx$	59
3.6	$\int F^{c(a+bx)} \csc^2(d+ex) dx$	61

3.7	$\int F^{c(a+bx)} \csc^3(d+ex) dx$	63
3.8	$\int F^{c(a+bx)} \csc^4(d+ex) dx$	66
3.9	$\int e^x \sin^4(x) dx$	69
3.10	$\int F^{c(a+bx)} \cos^n(d+ex) dx$	72
3.11	$\int F^{c(a+bx)} \cos^3(d+ex) dx$	74
3.12	$\int F^{c(a+bx)} \cos^2(d+ex) dx$	78
3.13	$\int F^{c(a+bx)} \cos(d+ex) dx$	82
3.14	$\int F^{c(a+bx)} \sec(d+ex) dx$	85
3.15	$\int F^{c(a+bx)} \sec^2(d+ex) dx$	87
3.16	$\int F^{c(a+bx)} \sec^3(d+ex) dx$	89
3.17	$\int F^{c(a+bx)} \sec^4(d+ex) dx$	91
3.18	$\int e^x \cos^4(x) dx$	93
3.19	$\int e^{c(a+bx)} \tan^3(d+ex) dx$	96
3.20	$\int e^{c(a+bx)} \tan^2(d+ex) dx$	99
3.21	$\int e^{c(a+bx)} \tan(d+ex) dx$	102
3.22	$\int e^{c(a+bx)} \cot(d+ex) dx$	105
3.23	$\int e^{c(a+bx)} \cot^2(d+ex) dx$	108
3.24	$\int e^{c(a+bx)} \cot^3(d+ex) dx$	111
3.25	$\int F^{a+bx} \tan\left(\frac{\pi}{4} + \frac{1}{2}(-c-dx)\right) dx$	114
3.26	$\int F^{c(a+bx)} \sec^n(d+ex) dx$	117
3.27	$\int F^{c(a+bx)} \csc^n(d+ex) dx$	120
3.28	$\int F^{c(a+bx)} (fx)^m \sin(d+ex) dx$	123
3.29	$\int F^{c(a+bx)} (fx)^m \csc(d+ex) dx$	125
3.30	$\int F^{c(a+bx)} (fx)^m \csc^2(d+ex) dx$	127
3.31	$\int f F^{c(a+bx)} (fx)^{-2+m} (ex \cos(d+ex) + (-1+m+bcx \log(F)) \sin(d+ex)) dx$	129
3.32	$\int f F^{c(a+bx)} (fx)^m (ex \cos(d+ex) + (1+m+bcx \log(F)) \sin(d+ex)) dx$	136
3.33	$\int \frac{F^{c(a+bx)} (fx)^m (ex \cos(d+ex) + (m+bcx \log(F)) \sin(d+ex))}{x} dx$	141
3.34	$\int F^{c(a+bx)} (ex \cos(d+ex) + (1+bcx \log(F)) \sin(d+ex)) dx$	144
3.35	$\int F^{c(a+bx)} (e \cos(d+ex) + bc \log(F) \sin(d+ex)) dx$	150
3.36	$\int \frac{F^{c(a+bx)} (ex \cos(d+ex) + (-1+bcx \log(F)) \sin(d+ex))}{x^2} dx$	153
3.37	$\int \frac{F^{c(a+bx)} (ex \cos(d+ex) + (-2+bcx \log(F)) \sin(d+ex))}{x^3} dx$	156
3.38	$\int e^{a+bx} \cos(c+dx) \sin(c+dx) dx$	160
3.39	$\int e^{a+bx} \cos(c+dx) \sin^2(c+dx) dx$	163
3.40	$\int e^{a+bx} \cos(c+dx) \sin^3(c+dx) dx$	166
3.41	$\int e^{a+bx} \cos^2(c+dx) \sin(c+dx) dx$	170
3.42	$\int e^{a+bx} \cos^2(c+dx) \sin^2(c+dx) dx$	173
3.43	$\int e^{a+bx} \cos^2(c+dx) \sin^3(c+dx) dx$	176
3.44	$\int e^{a+bx} \cos^3(c+dx) \sin(c+dx) dx$	179
3.45	$\int e^{a+bx} \cos^3(c+dx) \sin^2(c+dx) dx$	183
3.46	$\int e^{a+bx} \cos^3(c+dx) \sin^3(c+dx) dx$	186
3.47	$\int e^x x \sin(x) dx$	189
3.48	$\int e^x x^2 \sin(x) dx$	191
3.49	$\int e^x x \cos(x) dx$	194
3.50	$\int e^x x^2 \cos(x) dx$	196
3.51	$\int e^{3x} (-5 \cos(4x) + 2 \sin(4x)) dx$	199
3.52	$\int (e^{-x} \sin(x) + e^x \sin(x)) dx$	201
3.53	$\int \frac{F^{a+bx} \cos(c+dx)}{e+e \sin(c+dx)} dx$	203
3.54	$\int \frac{F^{a+bx} \cos(c+dx)}{e-e \sin(c+dx)} dx$	206

3.55	$\int \frac{f^{a+bx} \sin(c+dx)}{e+e \cos(c+dx)} dx$	209
3.56	$\int \frac{f^{a+bx} \sin(c+dx)}{e-e \cos(c+dx)} dx$	212
3.57	$\int e^{x^2} \sin(bx) dx$	215
3.58	$\int e^{x^2} \cos(bx) dx$	218
3.59	$\int e^{x^2} \sin(a+bx) dx$	221
3.60	$\int e^{x^2} \cos(a+bx) dx$	224
3.61	$\int e^{2x^2} x \cos(2x^2) dx$	227
3.62	$\int e^x \sin(e^x) dx$	229
3.63	$\int e^x \csc(e^x) \sec(e^x) dx$	231
3.64	$\int e^x \cos(e^x) dx$	233
3.65	$\int e^{2x} \cos(e^{2x}) dx$	235
3.66	$\int e^{-2x} \cos(e^{-2x}) dx$	237
3.67	$\int e^{2x} \cos(e^x) dx$	239
3.68	$\int e^{-1+3x} \cos(e^{-1+3x}) \sin(1+e^{-1+3x}) dx$	241
3.69	$\int e^x \tan(e^x) dx$	244
3.70	$\int e^x \sec(e^x) dx$	246
3.71	$\int e^x \sec(e^x) \tan(e^x) dx$	248
3.72	$\int e^x \csc^2(e^x) dx$	250
3.73	$\int e^x \sin(a+bx) dx$	252
3.74	$\int e^x \sin(a+cx^2) dx$	254
3.75	$\int e^x \sin(a+bx+cx^2) dx$	257
3.76	$\int e^{x^2} \sin(a+bx) dx$	260
3.77	$\int e^{x^2} \sin(a+cx^2) dx$	263
3.78	$\int e^{x^2} \sin(a+bx+cx^2) dx$	266
3.79	$\int f^{a+bx} \sin(d+fx^2) dx$	269
3.80	$\int f^{a+bx} \sin^2(d+fx^2) dx$	272
3.81	$\int f^{a+bx} \sin^3(d+fx^2) dx$	276
3.82	$\int f^{a+bx} \sin(d+ex+fx^2) dx$	280
3.83	$\int f^{a+bx} \sin^2(d+ex+fx^2) dx$	284
3.84	$\int f^{a+bx} \sin^3(d+ex+fx^2) dx$	288
3.85	$\int f^{a+cx^2} \sin(d+ex) dx$	292
3.86	$\int f^{a+cx^2} \sin^2(d+ex) dx$	295
3.87	$\int f^{a+cx^2} \sin^3(d+ex) dx$	298
3.88	$\int f^{a+cx^2} \sin(d+fx^2) dx$	302
3.89	$\int f^{a+cx^2} \sin^2(d+fx^2) dx$	305
3.90	$\int f^{a+cx^2} \sin^3(d+fx^2) dx$	308
3.91	$\int f^{a+cx^2} \sin(d+ex+fx^2) dx$	312
3.92	$\int f^{a+cx^2} \sin^2(d+ex+fx^2) dx$	316
3.93	$\int f^{a+cx^2} \sin^3(d+ex+fx^2) dx$	320
3.94	$\int f^{a+bx+cx^2} \sin(d+ex) dx$	325
3.95	$\int f^{a+bx+cx^2} \sin^2(d+ex) dx$	328
3.96	$\int f^{a+bx+cx^2} \sin^3(d+ex) dx$	331
3.97	$\int f^{a+bx+cx^2} \sin(d+fx^2) dx$	335
3.98	$\int f^{a+bx+cx^2} \sin^2(d+fx^2) dx$	339
3.99	$\int f^{a+bx+cx^2} \sin^3(d+fx^2) dx$	343
3.100	$\int f^{a+bx+cx^2} \sin(d+ex+fx^2) dx$	349
3.101	$\int f^{a+bx+cx^2} \sin^2(d+ex+fx^2) dx$	353

3.102	$\int f^{a+bx+cx^2} \sin^3(d+ex+fx^2) dx$	357
3.103	$\int f^{a+bx+cx^2} \sin(a+bx+ex^2) dx$	364
3.104	$\int e^x \cos(a+bx) dx$	368
3.105	$\int e^x \cos(a+cx^2) dx$	370
3.106	$\int e^x \cos(a+bx+cx^2) dx$	373
3.107	$\int e^{x^2} \cos(a+bx) dx$	376
3.108	$\int e^{x^2} \cos(a+cx^2) dx$	379
3.109	$\int e^{x^2} \cos(a+bx+cx^2) dx$	382
3.110	$\int f^{a+bx} \cos(d+fx^2) dx$	385
3.111	$\int f^{a+bx} \cos^2(d+fx^2) dx$	388
3.112	$\int f^{a+bx} \cos^3(d+fx^2) dx$	392
3.113	$\int f^{a+bx} \cos(d+ex+fx^2) dx$	396
3.114	$\int f^{a+bx} \cos^2(d+ex+fx^2) dx$	400
3.115	$\int f^{a+bx} \cos^3(d+ex+fx^2) dx$	404
3.116	$\int f^{a+cx^2} \cos(d+ex) dx$	408
3.117	$\int f^{a+cx^2} \cos^2(d+ex) dx$	411
3.118	$\int f^{a+cx^2} \cos^3(d+ex) dx$	414
3.119	$\int f^{a+cx^2} \cos(d+fx^2) dx$	418
3.120	$\int f^{a+cx^2} \cos^2(d+fx^2) dx$	421
3.121	$\int f^{a+cx^2} \cos^3(d+fx^2) dx$	424
3.122	$\int f^{a+cx^2} \cos(d+ex+fx^2) dx$	427
3.123	$\int f^{a+cx^2} \cos^2(d+ex+fx^2) dx$	431
3.124	$\int f^{a+cx^2} \cos^3(d+ex+fx^2) dx$	435
3.125	$\int f^{a+bx+cx^2} \cos(d+ex) dx$	441
3.126	$\int f^{a+bx+cx^2} \cos^2(d+ex) dx$	444
3.127	$\int f^{a+bx+cx^2} \cos^3(d+ex) dx$	447
3.128	$\int f^{a+bx+cx^2} \cos(d+fx^2) dx$	451
3.129	$\int f^{a+bx+cx^2} \cos^2(d+fx^2) dx$	455
3.130	$\int f^{a+bx+cx^2} \cos^3(d+fx^2) dx$	459
3.131	$\int f^{a+bx+cx^2} \cos(d+ex+fx^2) dx$	465
3.132	$\int f^{a+bx+cx^2} \cos^2(d+ex+fx^2) dx$	469
3.133	$\int f^{a+bx+cx^2} \cos^3(d+ex+fx^2) dx$	473
3.134	$\int f^{a+bx+cx^2} \cos(a+bx+ex^2) dx$	480
3.135	$\int F^{c(a+bx)}(f+f \sin(d+ex))^2 dx$	484
3.136	$\int F^{c(a+bx)}(f+f \sin(d+ex)) dx$	489
3.137	$\int \frac{F^{c(a+bx)}}{f+f \sin(d+ex)} dx$	493
3.138	$\int \frac{F^{c(a+bx)}}{(f+f \sin(d+ex))^2} dx$	496
3.139	$\int F^{c(a+bx)}(f+f \cos(d+ex))^2 dx$	499
3.140	$\int F^{c(a+bx)}(f+f \cos(d+ex)) dx$	504
3.141	$\int \frac{F^{c(a+bx)}}{f+f \cos(d+ex)} dx$	508
3.142	$\int \frac{F^{c(a+bx)}}{(f+f \cos(d+ex))^2} dx$	510
4	Listing of Grading functions	513
4.0.1	Mathematica and Rubi grading function	513
4.0.2	Maple grading function	515
4.0.3	Sympy grading function	518
4.0.4	SageMath grading function	520

Chapter 1

Introduction

This report gives the result of running the computer algebra independent integration problems. The listing of the problems are maintained by and can be downloaded from <https://rulebasedintegration.org>

The number of integrals in this report is [142]. This is test number [140].

1.1 Listing of CAS systems tested

The following systems were tested at this time.

1. Mathematica 12.3 (64 bit) on windows 10.
2. Rubi 4.16.1 in Mathematica 12.1 on windows 10.
3. Maple 2021.1 (64 bit) on windows 10.
4. Maxima 5.44 on Linux. (via sagemath 9.3)
5. Fricas 1.3.7 on Linux (via sagemath 9.3)
6. Giac/Xcas 1.7 on Linux. (via sagemath 9.3)
7. Sympy 1.8 under Python 3.8.8 using Anaconda distribution on Ubuntu.
8. Mupad using Matlab 2021a with Symbolic Math Toolbox Version 8.7 under windows 10 (64 bit)

Maxima, Fricas and Giac/Xcas were called from inside SageMath. This was done using SageMath integrate command by changing the name of the algorithm to use the different CAS systems.

Sympy was called directly using Python.

1.2 Results

Important note: A number of problems in this test suite have no antiderivative in closed form. This means the antiderivative of these integrals can not be expressed in terms of elementary, special functions or Hypergeometric $2F1$ functions. RootSum and RootOf are not allowed.

If a CAS returns the above integral unevaluated within the time limit, then the result is counted as passed and assigned an A grade.

However, if CAS times out, then it is assigned an F grade even if the integral is not integrable, as this implies CAS could not determine that the integral is not integrable in the time limit.

If a CAS returns an antiderivative to such an integral, it is assigned an A grade automatically and this special result is listed in the introduction section of each individual test report to make it easy to identify as this can be important result to investigate.

The results given in in the table below reflects the above.

System	solved	Failed
Rubi	% 98.59 (140)	% 1.41 (2)
Mathematica	% 100.00 (142)	% 0.00 (0)
Maple	% 80.28 (114)	% 19.72 (28)
Maxima	% 80.28 (114)	% 19.72 (28)
Fricas	% 80.99 (115)	% 19.01 (27)
Sympy	% 26.76 (38)	% 73.24 (104)
Giac	% 44.37 (63)	% 55.63 (79)
Mupad	% 35.21 (50)	% 64.79 (92)

Table 1.1: Percentage solved for each CAS

The table below gives additional break down of the grading of quality of the antiderivatives generated by each CAS. The grading is given using the letters A,B,C and F with A being the best quality. The grading is accomplished by comparing the antiderivative generated with the optimal antiderivatives included in the test suite. The following table describes the meaning of these grades.

grade	description
A	Integral was solved and antiderivative is optimal in quality and leaf size.
B	Integral was solved and antiderivative is optimal in quality but leaf size is larger than twice the optimal antiderivatives leaf size.
C	Integral was solved and antiderivative is non-optimal in quality. This can be due to one or more of the following reasons <ol style="list-style-type: none"> 1. antiderivative contains a hypergeometric function and the optimal antiderivative does not. 2. antiderivative contains a special function and the optimal antiderivative does not. 3. antiderivative contains the imaginary unit and the optimal antiderivative does not.
F	Integral was not solved. Either the integral was returned unevaluated within the time limit, or it timed out, or CAS hanged or crashed or an exception was raised.

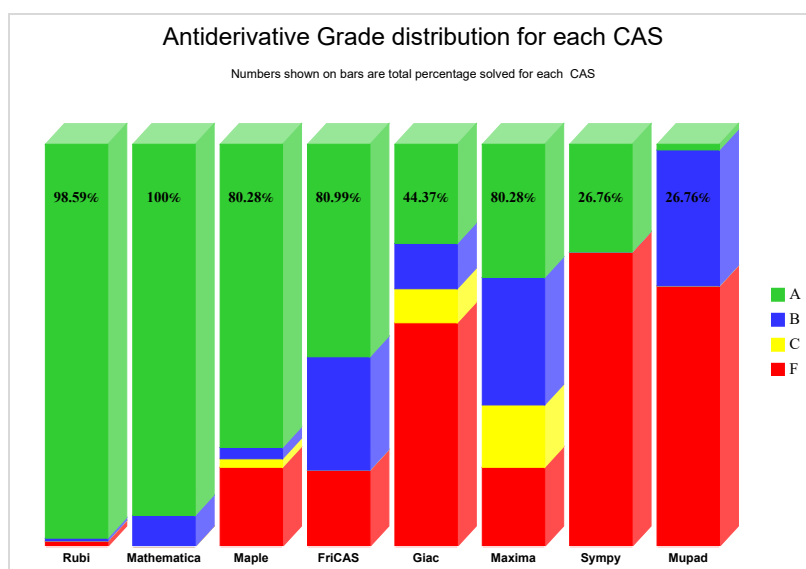
Table 1.2: Description of grading applied to integration result

Grading is implemented for all CAS systems. Based on the above, the following table summarizes the grading for this test suite.

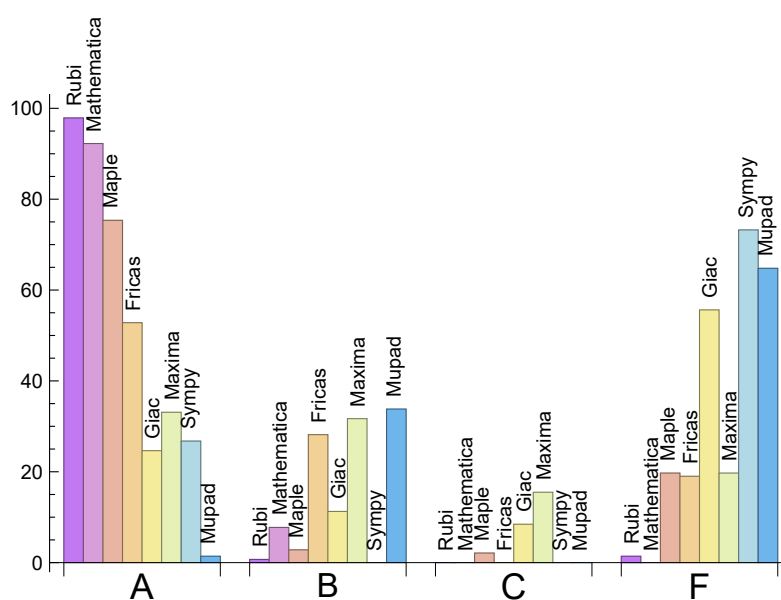
System	% A grade	% B grade	% C grade	% F grade
Rubi	97.89	0.70	0.00	1.41
Mathematica	92.25	7.75	0.00	0.00
Maple	75.35	2.82	2.11	19.72
Maxima	33.10	31.69	15.49	19.72
Fricas	52.82	28.17	0.00	19.01
Sympy	26.76	0.00	0.00	73.24
Giac	24.65	11.27	8.45	55.63
Mupad	1.41	33.80	0.00	64.79

Table 1.3: Antiderivative Grade distribution of each CAS

The following is a Bar chart illustration of the data in the above table.



The figure below compares the CAS systems for each grade level.



The following table shows the distribution of the different types of failure for each CAS. There are 3 types of reasons why it can fail. The first is when CAS returns back the input

within the time limit, which means it could not solve it. This the typical normal failure F .

The second is due to time out. CAS could not solve the integral within the 3 minutes time limit which is assigned F(-1).

The third is due to an exception generated. Assigned F(-2). This most likely indicates an interface problem between sagemath and the CAS (applicable only to FriCAS, Maxima and Giac) or it could be an indication of an internal error in CAS. This type of error requires more investigations to determine the cause.

System	Number failed	Percentage normal failure	Percentage time-out failure	Percentage exception failure
Rubi	2	100.00 %	0.00 %	0.00 %
Mathematica	0	0.00 %	0.00 %	0.00 %
Maple	28	100.00 %	0.00 %	0.00 %
Maxima	28	50.00 %	50.00 %	0.00 %
Fricas	27	100.00 %	0.00 %	0.00 %
Sympy	104	77.88 %	22.12 %	0.00 %
Giac	79	100.00 %	0.00 %	0.00 %
Mupad	92	100.00 %	0.00 %	0.00 %

Table 1.4: Time and leaf size performance for each CAS

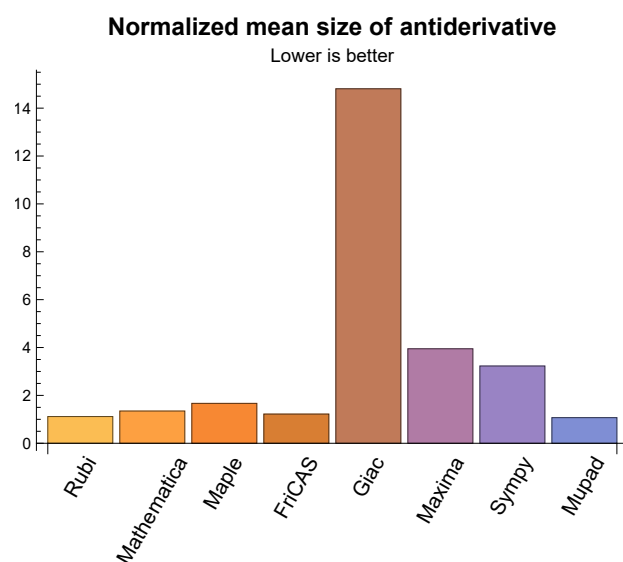
1.3 Performance

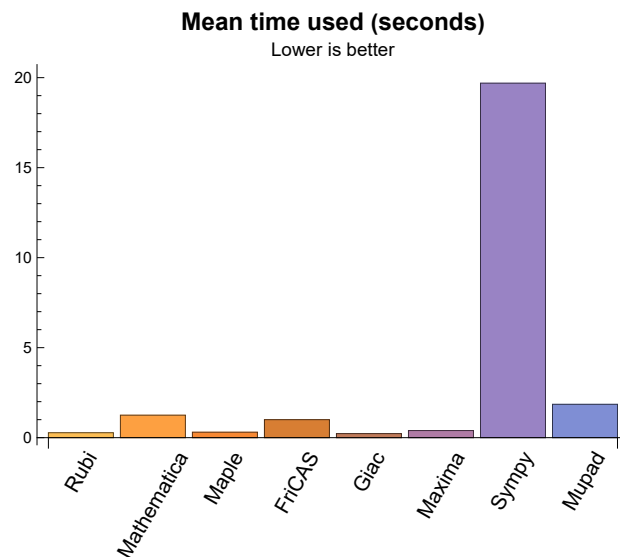
The table below summarizes the performance of each CAS system in terms of CPU time and leaf size of results.

System	Mean time (sec)	Mean size	Normalized mean	Median size	Normalized median
Rubi	0.27	140.37	1.12	129.00	1.00
Mathematica	1.25	263.82	1.35	117.50	1.00
Maple	0.30	150.31	1.67	136.00	0.91
Maxima	0.40	498.75	3.95	238.00	1.66
Fricas	1.00	199.41	1.22	156.00	1.04
Sympy	19.69	340.26	3.23	48.00	1.30
Giac	0.23	569.51	14.81	127.00	1.10
Mupad	1.85	67.46	1.07	25.50	0.84

Table 1.5: Time and leaf size performance for each CAS

The following are bar charts for the normalized leafsize and time used columns from the above table.





1.4 list of integrals that has no closed form antiderivative

{29,30}

1.5 list of integrals solved by CAS but has no known antiderivative

Rubi {}

Mathematica {}

Maple {}

Maxima {}

Fricas {}

Sympy {}

Giac {}

Mupad {}

1.6 list of integrals solved by CAS but failed verification

The following are integrals solved by CAS but the verification phase failed to verify the anti-derivative produced is correct. This does not mean necessarily that the anti-derivative is wrong, as additional methods of verification might be needed, or more time is needed (3 minutes time limit was used). These integrals are listed here to make it easier to do further investigation to determine why it was not possible to verify the result produced.

Rubi {}

Mathematica {91, 92, 93, 98, 100, 101, 102, 103, 122, 123, 124, 129, 131, 132, 133, 134}

Maple Verification phase not implemented yet.

Maxima Verification phase not implemented yet.

Fricas Verification phase not implemented yet.

Sympy Verification phase not implemented yet.

Giac Verification phase not implemented yet.

Mupad Verification phase not implemented yet.

1.7 Timing

The command `AbsoluteTiming[]` was used in Mathematica to obtain the elapsed time for each integrate call. In Maple, the command `Usage` was used as in the following example

```
cpu_time := Usage(assign ('result_of _int',int(expr,x)),output='realtime')
```

For all other CAS systems, the elapsed time to complete each integral was found by taking the difference between the time after the call has completed from the time before the call was made. This was done using Python's `time.time()` call.

All elapsed times shown are in seconds. A time limit of 3 minutes was used for each integral. If the integrate command did not complete within this time limit, the integral was aborted and considered to have failed and assigned an F grade. The time used by failed integrals due to time out is not counted in the final statistics.

1.8 Verification

A verification phase was applied on the result of integration for Rubi and Mathematica. Future version of this report will implement verification for the other CAS systems. For the integrals whose result was not run through a verification phase, it is assumed that the antiderivative produced was correct.

Verification phase has 3 minutes time out. An integral whose result was not verified could still be correct. Further investigation is needed on those integrals which failed verifications. Such integrals are marked in the summary table below and also in each integral separate section so they are easy to identify and locate.

1.9 Important notes about some of the results

1.9.1 Important note about Maxima results

Since these integrals are run in a batch mode, using an automated script, and by using `sagemath` (SageMath uses Maxima), then any integral where Maxima needs an interactive response from the user to answer a question during evaluation of the integral in order to complete the integration, will fail and is counted as failed.

The exception raised is `ValueError`. Therefore Maxima result below is lower than what could result if Maxima was run directly and each question Maxima asks was answered correctly.

The percentage of such failures were not counted for each test file, but for an example, for the Timofeev test file, there were about 14 such integrals out of total 705, or about 2 percent. This percentage can be higher or lower depending on the specific input test file.

Such integrals can be identified by looking at the output of the integration in each section for Maxima. The exception message will indicate of the error is due to the interactive question being asked or not.

Maxima integrate was run using SageMath with the following settings set by default

```
'besselexpand : true'
'display2d : false'
'domain : complex'
'keepfloat : true'
```

```
'load(to_poly_solve)'
'load(simplify_sum)'
'load(abs_integrate)' 'load(diag)'
```

SageMath loading of Maxima `abs_integrate` was found to cause some problem. So the following code was added to disable this effect.

```
from sage.interfaces.maxima_lib import maxima_lib
maxima_lib.set('extra_definite_integration_methods', '[]')
maxima_lib.set('extra_integration_methods', '[]')
```

See <https://ask.sagemath.org/question/43088/integrate-results-that-are-different-from-using-maxima/> for reference.

1.9.2 Important note about FriCAS and Giac/X-CAS results

There are Few integrals which failed due to SageMath not able to translate the result back to SageMath syntax and not because these CAS system were not able to do the integrations.

These will fail With error `Exception raised: NotImplementedError`

The number of such cases seems to be very small. About 1 or 2 percent of all integrals.

Hopefully the next version of SageMath will have complete translation of FriCAS and XCAS syntax and I will re-run all the tests again when this happens.

1.9.3 Important note about finding leaf size of antiderivative

For Mathematica, Rubi and Maple, the buildin system function `LeafSize` is used to find the leaf size of each antiderivative.

The other CAS systems (SageMath and Sympy) do not have special buildin function for this purpose at this time. Therefore the leaf size for Fricas and Sympy and Giac antiderivatives is determined using the following function, thanks to user `slelievre` at https://ask.sagemath.org/question/57123/could-we-have-a-leaf_count-function-in-base-sagemath/

```
def tree_size(expr):
    r"""
    Return the tree size of this expression.
    """
    if expr not in SR:
        # deal with lists, tuples, vectors
        return 1 + sum(tree_size(a) for a in expr)
    expr = SR(expr)
    x, aa = expr.operator(), expr.operands()
    if x is None:
        return 1
    else:
        return 1 + sum(tree_size(a) for a in aa)
```

For Sympy, which is called directly from Python, the following code is used to obtain the leafsize of its result

```
try:
    # 1.7 is a fudge factor since it is low side from actual leaf count
    leafCount = round(1.7*count_ops(anti))

except Exception as ee:
    leafCount = 1
```

1.9.4 Important note about Mupad results

Matlab's symbolic toolbox does not have a leaf count function to measure the size of the antiderivative, Maple was used to determine the leaf size of Mupad output by post processing.

Currently no grading of the antiderivative for Mupad is implemented. If it can integrate the problem, it was assigned a B grade automatically as a placeholder. In the future, when grading function is implemented for Mupad, the tests will be rerun again.

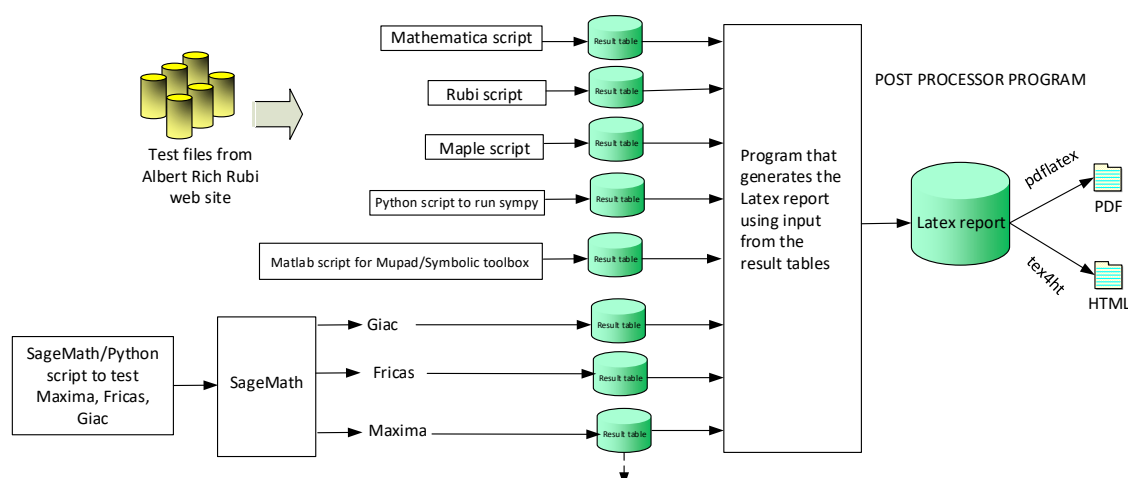
The following is an example of using Matlab's symbolic toolbox (Mupad) to solve an integral

```
integrand = evalin(symengine, 'cos(x)*sin(x)')
the_variable = evalin(symengine, 'x')
anti = int(integrand, the_variable)
```

Which gives $\sin(x)^2/2$

1.10 Design of the test system

The following diagram gives a high level view of the current test build system.



One record (line) per one integral result. The line is CSV comma separated. This is description of each record

1. integer. the problem number.
2. integer. 0 for failed, 1 for passed, -1 for timeout, -2 for CAS specific exception. (this is not the grade field)
3. integer. Leaf size of result.
4. integer. Leaf size of the optimal antiderivative.
5. number. CPU time used to solve this integral. 0 if failed.
6. string. The integral in Latex format
7. string. The input used in CAS own syntax.
8. string. The result (antiderivative) produced by CAS in Latex format
9. string. The optimal antiderivative in Latex format.
10. integer. 0 or 1. Indicates if problem has known antiderivative or not
11. String. The result (antiderivative) in CAS own syntax.
12. String. The grade of the antiderivative. Can be "A", "B", "C", or "F"
- The following field present only in Rubi and Mathematica Tables*
13. integer. 1 if result was verified or 0 if not verified.
- The following fields present only in Rubi Tables*
14. integer. Number of rules used.
15. integer. Integrand leaf size.
16. real number. Ratio of field 14 over field 15
17. integer. 1 if result was verified or 0 if not verified.
18. String of form "{n,n,..}" which is list of the rules used by Rubi

High level overview of the CAS independent integration test build system

Chapter 2

detailed summary tables of results

2.1 List of integrals sorted by grade for each CAS

2.1.1 Rubi

A grade: { 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21, 22, 23, 24, 25, 26, 27, 29, 30, 31, 33, 35, 36, 37, 38, 39, 40, 41, 42, 43, 44, 45, 46, 47, 48, 49, 50, 51, 52, 53, 54, 55, 56, 57, 58, 59, 60, 61, 62, 63, 64, 65, 66, 67, 68, 69, 70, 71, 72, 73, 74, 75, 76, 77, 78, 79, 80, 81, 82, 83, 84, 85, 86, 87, 88, 89, 90, 91, 92, 93, 94, 95, 96, 97, 98, 99, 100, 101, 102, 103, 104, 105, 106, 107, 108, 109, 110, 111, 112, 113, 114, 115, 116, 117, 118, 119, 120, 121, 122, 123, 124, 125, 126, 127, 128, 129, 130, 131, 132, 133, 134, 135, 136, 137, 138, 139, 140, 141, 142 }

B grade: { 34 }

C grade: { }

F grade: { 28, 32 }

2.1.2 Mathematica

A grade: { 1, 2, 3, 4, 5, 6, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 23, 24, 25, 26, 27, 28, 29, 30, 31, 32, 33, 34, 35, 36, 37, 38, 39, 40, 41, 42, 43, 44, 45, 46, 47, 48, 49, 50, 51, 52, 53, 54, 55, 56, 57, 58, 59, 60, 61, 62, 64, 65, 66, 67, 68, 69, 70, 71, 72, 73, 74, 75, 76, 77, 78, 79, 80, 81, 82, 83, 84, 85, 86, 87, 88, 89, 90, 91, 92, 93, 94, 95, 96, 97, 98, 100, 103, 104, 105, 106, 107, 108, 109, 110, 111, 112, 113, 114, 115, 116, 117, 118, 119, 120, 121, 122, 123, 125, 126, 127, 128, 129, 131, 134, 135, 136, 137, 138, 139, 140, 141, 142 }

B grade: { 7, 21, 22, 63, 99, 101, 102, 124, 130, 132, 133 }

C grade: { }

F grade: { }

2.1.3 Maple

A grade: { 2, 3, 4, 9, 11, 12, 13, 18, 29, 30, 36, 37, 38, 39, 40, 41, 42, 43, 44, 45, 46, 47, 48, 49, 50, 52, 57, 58, 59, 60, 61, 62, 63, 64, 65, 66, 68, 69, 70, 71, 72, 73, 74, 75, 76, 77, 78, 79, 80, 81, 82, 83, 84, 85, 86, 87, 88, 89, 90, 91, 92, 93, 94, 95, 96, 97, 98, 99, 100, 101, 102, 103, 104, 105, 106, 107, 108, 109, 110, 111, 112, 113, 114, 115, 116, 117, 118, 119, 120, 121, 122, 123, 124, 125, 126, 127, 128, 129, 130, 131, 132, 133, 134, 135, 136, 139, 140 }

B grade: { 34, 35, 51, 67 }

C grade: { 31, 32, 33 }

F grade: { 1, 5, 6, 7, 8, 10, 14, 15, 16, 17, 19, 20, 21, 22, 23, 24, 25, 26, 27, 28, 53, 54, 55, 56, 137, 138, 141, 142 }

2.1.4 Maxima

A grade: { 9, 18, 29, 30, 31, 32, 33, 38, 47, 48, 49, 50, 51, 52, 57, 58, 59, 60, 61, 62, 64, 65, 66, 67, 68, 69, 70, 71, 72, 73, 74, 75, 76, 79, 80, 81, 82, 84, 104, 105, 106, 107, 110, 111, 112, 113, 115 }

B grade: { 2, 3, 4, 11, 12, 13, 34, 35, 39, 40, 41, 42, 43, 44, 45, 46, 63, 77, 78, 83, 88, 90, 91, 93, 97, 99, 100, 102, 103, 108, 109, 114, 119, 121, 122, 124, 128, 130, 131, 133, 134, 135, 136, 139, 140 }

C grade: { 36, 37, 85, 86, 87, 89, 92, 94, 95, 96, 98, 101, 116, 117, 118, 120, 123, 125, 126, 127, 129, 132 }

F grade: { 1, 5, 6, 7, 8, 10, 14, 15, 16, 17, 19, 20, 21, 22, 23, 24, 25, 26, 27, 28, 53, 54, 55, 56, 137, 138, 141, 142 }

2.1.5 FriCAS

A grade: { 2, 3, 4, 9, 11, 12, 13, 18, 28, 29, 30, 31, 32, 33, 34, 35, 36, 37, 38, 39, 40, 41, 42, 43, 44, 45, 46, 47, 48, 49, 50, 51, 52, 57, 58, 59, 60, 61, 62, 64, 65, 66, 67, 68, 69, 71, 72, 73, 76, 77, 78, 85, 86, 87, 88, 89, 94, 95, 96, 104, 107, 108, 109, 116, 117, 118, 119, 120, 125, 126, 127, 135, 136, 139, 140 }

B grade: { 63, 70, 74, 75, 79, 80, 81, 82, 83, 84, 90, 91, 92, 93, 97, 98, 99, 100, 101, 102, 103, 105, 106, 110, 111, 112, 113, 114, 115, 121, 122, 123, 124, 128, 129, 130, 131, 132, 133, 134 }

C grade: { }

F grade: { 1, 5, 6, 7, 8, 10, 14, 15, 16, 17, 19, 20, 21, 22, 23, 24, 25, 26, 27, 53, 54, 55, 56, 137, 138, 141, 142 }

2.1.6 Sympy

A grade: { 3, 4, 9, 12, 13, 18, 29, 30, 34, 35, 38, 39, 40, 41, 42, 44, 47, 48, 49, 50, 51, 52, 61, 62, 64, 65, 66, 67, 69, 70, 71, 72, 73, 104, 135, 136, 139, 140 }

B grade: { }

C grade: { }

F grade: { 1, 2, 5, 6, 7, 8, 10, 11, 14, 15, 16, 17, 19, 20, 21, 22, 23, 24, 25, 26, 27, 28, 31, 32, 33, 36, 37, 43, 45, 46, 53, 54, 55, 56, 57, 58, 59, 60, 63, 68, 74, 75, 76, 77, 78, 79, 80, 81, 82, 83, 84, 85, 86, 87, 88, 89, 90, 91, 92, 93, 94, 95, 96, 97, 98, 99, 100, 101, 102, 103, 105, 106, 107, 108, 109, 110, 111, 112, 113, 114, 115, 116, 117, 118, 119, 120, 121, 122, 123, 124, 125, 126, 127, 128, 129, 130, 131, 132, 133, 134, 137, 138, 141, 142 }

2.1.7 Giac

A grade: { 9, 18, 29, 30, 38, 39, 40, 41, 42, 43, 44, 45, 46, 47, 48, 49, 50, 51, 52, 61, 62, 64, 65, 66, 67, 68, 69, 71, 72, 73, 74, 75, 104, 105, 106 }

B grade: { 31, 32, 63, 70, 79, 80, 81, 82, 83, 84, 110, 111, 112, 113, 114, 115 }

C grade: { 2, 3, 4, 11, 12, 13, 34, 35, 135, 136, 139, 140 }

F grade: { 1, 5, 6, 7, 8, 10, 14, 15, 16, 17, 19, 20, 21, 22, 23, 24, 25, 26, 27, 28, 33, 36, 37, 53, 54, 55, 56, 57, 58, 59, 60, 76, 77, 78, 85, 86, 87, 88, 89, 90, 91, 92, 93, 94, 95, 96, 97, 98, 99, 100, 101, 102, 103, 107, 108, 109, 116, 117, 118, 119, 120, 121, 122, 123, 124, 125, 126, 127, 128, 129, 130, 131, 132, 133, 134, 137, 138, 141, 142 }

2.1.8 Mupad

A grade: { 29, 30 }

B grade: { 2, 3, 4, 9, 11, 12, 13, 18, 31, 32, 33, 34, 35, 36, 37, 38, 39, 40, 41, 42, 43, 44, 45, 46, 47, 48, 49, 50, 51, 52, 61, 62, 63, 64, 65, 66, 67, 68, 69, 70, 71, 72, 73, 104, 135, 136, 139, 140 }

C grade: { }

F grade: { 1, 5, 6, 7, 8, 10, 14, 15, 16, 17, 19, 20, 21, 22, 23, 24, 25, 26, 27, 28, 53, 54, 55, 56, 57, 58, 59, 60, 74, 75, 76, 77, 78, 79, 80, 81, 82, 83, 84, 85, 86, 87, 88, 89, 90, 91, 92, 93, 94, 95, 96, 97, 98, 99, 100, 101, 102, 103, 105, 106, 107, 108, 109, 110, 111, 112, 113, 114, 115, 116, 117, 118, 119, 120, 121, 122, 123, 124, 125, 126, 127, 128, 129, 130, 131, 132, 133, 134, 137, 138, 141, 142 }

2.2 Detailed conclusion table per each integral for all CAS systems

Detailed conclusion table per each integral is given by table below. The elapsed time is in seconds. For failed result it is given as F(-1) if the failure was due to timeout. It is given as F(-2) if the failure was due to an exception being raised, which could indicate a bug in the system. If the failure was due to integral not being evaluated within the time limit, then it is given just an F.

In this table, the column **normalized size** is defined as $\frac{\text{antiderivative leaf size}}{\text{optimal antiderivative leaf size}}$

Problem 1	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	107	107	110	0	0	0	0	0	-1
normalized size	1	1.00	1.03	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.138	0.060	1.017	0.000	0.566	0.000	0.000	0.000
Problem 2	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	A	F(-1)	C	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	199	199	154	336	813	171	0	1311	190
normalized size	1	1.00	0.77	1.69	4.09	0.86	0.00	6.59	0.95
time (sec)	N/A	0.070	0.703	0.441	0.487	0.623	0.000	0.281	3.217
Problem 3	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	A	A	C	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	128	128	86	153	356	89	627	933	95
normalized size	1	1.00	0.67	1.20	2.78	0.70	4.90	7.29	0.74
time (sec)	N/A	0.052	0.225	0.174	0.413	1.864	34.889	0.237	3.023
Problem 4	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	A	A	C	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	73	73	48	130	194	49	326	652	50
normalized size	1	1.00	0.66	1.78	2.66	0.67	4.47	8.93	0.68
time (sec)	N/A	0.016	0.125	0.040	1.131	0.925	7.837	0.212	2.395
Problem 5	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F(-1)	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	81	81	114	0	0	0	0	0	-1
normalized size	1	1.00	1.41	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.022	1.748	0.090	0.000	0.847	0.000	0.000	0.000

Problem 6	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F(-1)	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	78	78	101	0	0	0	0	0	-1
normalized size	1	1.00	1.29	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.029	1.482	0.165	0.000	0.952	0.000	0.000	0.000
Problem 7	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	B	F	F(-1)	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	137	137	334	0	0	0	0	0	-1
normalized size	1	1.00	2.44	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.049	7.670	0.221	0.000	0.644	0.000	0.000	0.000
Problem 8	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F(-1)	F	F(-1)	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	141	141	173	0	0	0	0	0	-1
normalized size	1	1.00	1.23	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.055	2.957	0.241	0.000	3.497	0.000	0.000	0.000
Problem 9	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	54	54	33	34	37	36	70	35	41
normalized size	1	1.00	0.61	0.63	0.69	0.67	1.30	0.65	0.76
time (sec)	N/A	0.026	0.042	0.032	0.318	0.644	3.739	0.143	0.046
Problem 10	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	107	107	110	0	0	0	0	0	-1
normalized size	1	1.00	1.03	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.112	0.056	0.802	0.000	0.669	0.000	0.000	0.000
Problem 11	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	A	F(-1)	C	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	199	199	155	274	813	142	0	1307	191
normalized size	1	1.00	0.78	1.38	4.09	0.71	0.00	6.57	0.96
time (sec)	N/A	0.053	0.667	0.427	0.387	2.091	0.000	0.292	3.143

Problem 12	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	A	A	C	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	128	128	85	153	356	78	627	933	98
normalized size	1	1.00	0.66	1.20	2.78	0.61	4.90	7.29	0.77
time (sec)	N/A	0.037	0.214	0.131	0.348	0.711	34.783	0.234	2.976
Problem 13	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	A	A	C	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	72	72	47	133	192	48	352	649	48
normalized size	1	1.00	0.65	1.85	2.67	0.67	4.89	9.01	0.67
time (sec)	N/A	0.016	0.109	0.035	0.338	0.727	7.858	0.265	2.357
Problem 14	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F(-1)	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	84	84	84	0	0	0	0	0	-1
normalized size	1	1.00	1.00	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.018	0.019	0.101	0.000	0.586	0.000	0.000	0.000
Problem 15	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F(-1)	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	80	80	80	0	0	0	0	0	-1
normalized size	1	1.00	1.00	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.024	0.015	0.162	0.000	1.270	0.000	0.000	0.000
Problem 16	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F(-1)	F	F(-1)	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	141	141	112	0	0	0	0	0	-1
normalized size	1	1.00	0.79	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.049	0.291	0.302	0.000	0.645	0.000	0.000	0.000
Problem 17	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F(-1)	F	F(-1)	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	143	143	111	0	0	0	0	0	-1
normalized size	1	1.00	0.78	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.053	0.215	0.354	0.000	3.196	0.000	0.000	0.000

Problem 18	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	54	54	33	34	37	36	70	35	41
normalized size	1	1.00	0.61	0.63	0.69	0.67	1.30	0.65	0.76
time (sec)	N/A	0.029	0.027	0.034	0.327	0.643	3.712	0.131	0.042
Problem 19	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	194	194	212	0	0	0	0	0	-1
normalized size	1	1.00	1.09	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.199	2.136	0.246	0.000	0.721	0.000	0.000	0.000
Problem 20	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	130	130	174	0	0	0	0	0	-1
normalized size	1	1.00	1.34	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.126	1.674	0.142	0.000	0.736	0.000	0.000	0.000
Problem 21	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	B	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	78	78	166	0	0	0	0	0	-1
normalized size	1	1.00	2.13	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.076	0.470	0.127	0.000	1.022	0.000	0.000	0.000
Problem 22	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	B	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	76	76	163	0	0	0	0	0	-1
normalized size	1	1.00	2.14	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.078	1.232	0.179	0.000	0.578	0.000	0.000	0.000
Problem 23	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F(-1)	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	126	126	170	0	0	0	0	0	-1
normalized size	1	1.00	1.35	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.125	1.648	0.190	0.000	0.402	0.000	0.000	0.000

Problem 24	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	188	188	210	0	0	0	0	0	-1
normalized size	1	1.00	1.12	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.191	2.176	0.278	0.000	0.417	0.000	0.000	0.000
Problem 25	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	76	76	133	0	0	0	0	0	-1
normalized size	1	1.00	1.75	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.094	0.313	0.225	0.000	0.758	0.000	0.000	0.000
Problem 26	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	100	100	102	0	0	0	0	0	-1
normalized size	1	1.00	1.02	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.140	0.088	0.882	0.000	1.552	0.000	0.000	0.000
Problem 27	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	102	102	102	0	0	0	0	0	-1
normalized size	1	1.00	1.00	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.157	0.098	0.984	0.000	0.585	0.000	0.000	0.000
Problem 28	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	F	A	F	F	A	F	F	F
verified	N/A	N/A	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	139	0	143	0	0	130	0	0	-1
normalized size	1	0.00	1.03	0.00	0.00	0.94	0.00	0.00	-0.01
time (sec)	N/A	0.491	0.615	0.433	0.000	0.897	0.000	0.000	0.000
Problem 29	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD	TBD
size	25	0	0	0	0	0	0	0	-1
normalized size	1	0.00	0.00	0.00	0.00	0.00	0.00	0.00	-0.04
time (sec)	N/A	0.623	9.202	0.149	0.000	1.478	0.000	0.000	0.000

Problem 30	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD	TBD
size	27	0	0	0	0	0	0	0	-1
normalized size	1	0.00	0.00	0.00	0.00	0.00	0.00	0.00	-0.04
time (sec)	N/A	0.951	10.724	0.182	0.000	0.597	0.000	0.000	0.000
Problem 31	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	C	A	A	F(-1)	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	24	24	26	213	32	26	0	6402	27
normalized size	1	1.00	1.08	8.88	1.33	1.08	0.00	266.75	1.12
time (sec)	N/A	3.975	1.354	0.371	0.733	0.564	0.000	0.916	2.902
Problem 32	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	F	A	C	A	A	F(-1)	B	B
verified	N/A	N/A	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	23	0	23	201	30	24	0	4802	23
normalized size	1	0.00	1.00	8.74	1.30	1.04	0.00	208.78	1.00
time (sec)	N/A	2.340	0.926	0.256	0.702	0.804	0.000	0.638	2.861
Problem 33	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	C	A	A	F(-1)	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	22	22	22	199	27	22	0	0	21
normalized size	1	1.00	1.00	9.05	1.23	1.00	0.00	0.00	0.95
time (sec)	N/A	2.563	0.871	0.233	0.712	0.654	0.000	0.000	2.803
Problem 34	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	B	A	B	B	A	A	C	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	17	327	17	682	1382	18	19	3933	17
normalized size	1	19.24	1.00	40.12	81.29	1.06	1.12	231.35	1.00
time (sec)	N/A	0.766	0.406	0.162	0.462	3.998	7.557	0.382	2.872
Problem 35	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	B	A	A	C	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	16	16	16	268	392	17	17	1267	16
normalized size	1	1.00	1.00	16.75	24.50	1.06	1.06	79.19	1.00
time (sec)	N/A	0.029	0.027	0.038	0.350	0.790	1.632	0.337	2.348

Problem 36	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	C	A	F	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	20	20	19	40	564	20	0	0	19
normalized size	1	1.00	0.95	2.00	28.20	1.00	0.00	0.00	0.95
time (sec)	N/A	1.732	0.612	0.132	1.026	0.938	0.000	0.000	2.736
Problem 37	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	C	A	F	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	20	20	19	40	1072	20	0	0	19
normalized size	1	1.00	0.95	2.00	53.60	1.00	0.00	0.00	0.95
time (sec)	N/A	1.950	0.649	0.157	1.444	0.579	0.000	0.000	2.751
Problem 38	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	63	63	44	60	44	56	325	55	46
normalized size	1	1.00	0.70	0.95	0.70	0.89	5.16	0.87	0.73
time (sec)	N/A	0.047	0.155	0.059	0.315	0.607	8.519	0.130	0.502
Problem 39	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	119	119	74	108	538	109	1030	98	166
normalized size	1	1.00	0.62	0.91	4.52	0.92	8.66	0.82	1.39
time (sec)	N/A	0.093	0.663	0.160	0.351	0.573	44.426	0.125	3.012
Problem 40	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	129	129	82	118	550	135	1353	111	178
normalized size	1	1.00	0.64	0.91	4.26	1.05	10.49	0.86	1.38
time (sec)	N/A	0.088	0.896	0.097	0.347	0.648	147.998	0.144	3.029
Problem 41	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	119	119	74	108	538	98	1040	100	167
normalized size	1	1.00	0.62	0.91	4.52	0.82	8.74	0.84	1.40
time (sec)	N/A	0.083	0.672	0.095	0.364	0.895	44.752	0.144	0.857

Problem 42	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	79	79	57	71	236	90	850	66	58
normalized size	1	1.00	0.72	0.90	2.99	1.14	10.76	0.84	0.73
time (sec)	N/A	0.076	0.378	0.120	0.345	0.466	94.597	0.154	0.375
Problem 43	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	A	F(-1)	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	183	183	110	166	1148	201	0	155	255
normalized size	1	1.00	0.60	0.91	6.27	1.10	0.00	0.85	1.39
time (sec)	N/A	0.126	0.922	0.079	0.412	0.570	0.000	0.155	3.741
Problem 44	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	129	129	81	118	550	114	1357	111	179
normalized size	1	1.00	0.63	0.91	4.26	0.88	10.52	0.86	1.39
time (sec)	N/A	0.089	0.677	0.091	0.355	0.585	146.899	0.134	0.822
Problem 45	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	A	F(-1)	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	183	183	110	166	1144	200	0	152	255
normalized size	1	1.00	0.60	0.91	6.25	1.09	0.00	0.83	1.39
time (sec)	N/A	0.125	0.779	0.135	0.393	0.660	0.000	0.158	3.713
Problem 46	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	A	F(-1)	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	129	129	111	118	550	156	0	111	178
normalized size	1	1.00	0.86	0.91	4.26	1.21	0.00	0.86	1.38
time (sec)	N/A	0.101	0.943	0.105	0.357	1.456	0.000	0.161	1.006
Problem 47	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	30	30	19	19	17	17	27	16	16
normalized size	1	1.00	0.63	0.63	0.57	0.57	0.90	0.53	0.53
time (sec)	N/A	0.039	0.038	0.031	0.322	0.839	0.638	0.134	0.076

Problem 48	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	50	50	25	27	26	26	48	25	21
normalized size	1	1.00	0.50	0.54	0.52	0.52	0.96	0.50	0.42
time (sec)	N/A	0.118	0.037	0.025	0.327	1.579	1.556	0.118	2.377
Problem 49	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	30	30	18	20	17	17	27	15	17
normalized size	1	1.00	0.60	0.67	0.57	0.57	0.90	0.50	0.57
time (sec)	N/A	0.040	0.027	0.027	0.317	0.627	0.625	0.135	2.349
Problem 50	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	51	51	23	28	26	26	48	24	22
normalized size	1	1.00	0.45	0.55	0.51	0.51	0.94	0.47	0.43
time (sec)	N/A	0.117	0.034	0.028	0.319	0.657	1.557	0.135	2.364
Problem 51	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	27	27	22	103	39	21	27	39	19
normalized size	1	1.00	0.81	3.81	1.44	0.78	1.00	1.44	0.70
time (sec)	N/A	0.080	0.092	0.054	0.313	1.965	0.248	0.143	0.059
Problem 52	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	41	41	33	30	23	26	32	23	31
normalized size	1	1.00	0.80	0.73	0.56	0.63	0.78	0.56	0.76
time (sec)	N/A	0.025	0.065	0.027	0.318	0.575	0.466	0.124	2.411
Problem 53	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	82	82	64	0	0	0	0	0	-1
normalized size	1	1.00	0.78	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.136	2.546	0.369	0.000	0.772	0.000	0.000	0.000

Problem 54	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	82	82	64	0	0	0	0	0	-1
normalized size	1	1.00	0.78	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.128	2.635	0.370	0.000	0.753	0.000	0.000	0.000
Problem 55	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F(-1)	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	80	80	68	0	0	0	0	0	-1
normalized size	1	1.00	0.85	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.116	0.672	0.162	0.000	0.679	0.000	0.000	0.000
Problem 56	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F(-1)	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	78	78	66	0	0	0	0	0	-1
normalized size	1	1.00	0.85	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.118	0.634	0.188	0.000	0.707	0.000	0.000	0.000
Problem 57	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	69	69	43	42	37	30	0	0	-1
normalized size	1	1.00	0.62	0.61	0.54	0.43	0.00	0.00	-0.01
time (sec)	N/A	0.053	0.025	0.124	0.355	0.670	0.000	0.000	0.000
Problem 58	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	65	65	47	44	38	32	0	0	-1
normalized size	1	1.00	0.72	0.68	0.58	0.49	0.00	0.00	-0.02
time (sec)	N/A	0.047	0.018	0.085	0.357	0.766	0.000	0.000	0.000
Problem 59	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	81	81	81	52	51	45	0	0	-1
normalized size	1	1.00	1.00	0.64	0.63	0.56	0.00	0.00	-0.01
time (sec)	N/A	0.070	0.082	0.082	0.330	0.641	0.000	0.000	0.000

Problem 60	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	77	77	82	54	52	46	0	0	-1
normalized size	1	1.00	1.06	0.70	0.68	0.60	0.00	0.00	-0.01
time (sec)	N/A	0.051	0.083	0.075	0.340	0.613	0.000	0.000	0.000
Problem 61	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	35	35	24	30	29	29	29	21	21
normalized size	1	1.00	0.69	0.86	0.83	0.83	0.83	0.60	0.60
time (sec)	N/A	0.077	0.037	0.062	0.360	0.732	6.225	0.139	0.084
Problem 62	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	6	6	6	6	5	5	5	5	5
normalized size	1	1.00	1.00	1.00	0.83	0.83	0.83	0.83	0.83
time (sec)	N/A	0.008	0.009	0.004	0.338	2.288	0.230	0.136	2.211
Problem 63	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	B	A	B	B	F	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	5	5	21	5	19	21	0	17	43
normalized size	1	1.00	4.20	1.00	3.80	4.20	0.00	3.40	8.60
time (sec)	N/A	0.022	0.017	0.080	0.315	0.567	0.000	0.138	2.508
Problem 64	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	4	4	4	4	3	3	3	3	3
normalized size	1	1.00	1.00	1.00	0.75	0.75	0.75	0.75	0.75
time (sec)	N/A	0.008	0.010	0.038	0.308	0.762	0.226	0.124	0.037
Problem 65	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	10	10	10	8	7	7	7	7	7
normalized size	1	1.00	1.00	0.80	0.70	0.70	0.70	0.70	0.70
time (sec)	N/A	0.011	0.010	0.039	0.313	0.633	0.237	0.136	0.049

Problem 66	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	10	10	10	8	7	7	10	7	7
normalized size	1	1.00	1.00	0.80	0.70	0.70	1.00	0.70	0.70
time (sec)	N/A	0.010	0.011	0.046	0.316	0.681	0.373	0.121	2.204
Problem 67	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	13	13	13	24	10	10	12	10	10
normalized size	1	1.00	1.00	1.85	0.77	0.77	0.92	0.77	0.77
time (sec)	N/A	0.017	0.016	0.050	0.321	0.601	10.678	0.116	2.231
Problem 68	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F(-1)	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	30	30	30	25	24	42	0	24	24
normalized size	1	1.00	1.00	0.83	0.80	1.40	0.00	0.80	0.80
time (sec)	N/A	0.036	0.063	0.258	0.319	0.992	0.000	0.126	0.313
Problem 69	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	7	7	7	7	4	12	10	7	10
normalized size	1	1.00	1.00	1.00	0.57	1.71	1.43	1.00	1.43
time (sec)	N/A	0.010	0.008	0.003	0.309	1.104	0.164	0.122	2.654
Problem 70	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	B	A	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	5	5	5	9	8	19	10	29	10
normalized size	1	1.00	1.00	1.80	1.60	3.80	2.00	5.80	2.00
time (sec)	N/A	0.010	0.005	0.003	0.313	0.526	1.021	0.123	2.790
Problem 71	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	4	4	4	4	5	5	3	5	5
normalized size	1	1.00	1.00	1.00	1.25	1.25	0.75	1.25	1.25
time (sec)	N/A	0.020	0.010	0.029	0.310	1.097	0.603	0.127	0.085

Problem 72	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	6	6	6	6	7	10	5	7	13
normalized size	1	1.00	1.00	1.00	1.17	1.67	0.83	1.17	2.17
time (sec)	N/A	0.017	0.017	0.027	0.311	0.756	0.805	0.122	2.271
Problem 73	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	37	37	27	36	28	30	116	35	26
normalized size	1	1.00	0.73	0.97	0.76	0.81	3.14	0.95	0.70
time (sec)	N/A	0.013	0.062	0.006	0.315	1.193	0.785	0.120	0.101
Problem 74	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	B	F	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	115	115	108	88	100	193	0	127	-1
normalized size	1	1.00	0.94	0.77	0.87	1.68	0.00	1.10	-0.01
time (sec)	N/A	0.123	0.162	0.158	0.344	0.566	0.000	0.164	0.000
Problem 75	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	B	F	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	144	144	134	119	131	229	0	147	-1
normalized size	1	1.00	0.93	0.83	0.91	1.59	0.00	1.02	-0.01
time (sec)	N/A	0.216	0.258	0.158	0.353	0.871	0.000	0.157	0.000
Problem 76	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	81	81	81	52	51	45	0	0	-1
normalized size	1	1.00	1.00	0.64	0.63	0.56	0.00	0.00	-0.01
time (sec)	N/A	0.055	0.021	0.000	0.329	0.702	0.000	0.000	0.000
Problem 77	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	A	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	87	87	129	62	137	66	0	0	-1
normalized size	1	1.00	1.48	0.71	1.57	0.76	0.00	0.00	-0.01
time (sec)	N/A	0.098	0.236	0.092	0.336	0.711	0.000	0.000	0.000

Problem 78	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	A	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	155	155	165	129	475	161	0	0	-1
normalized size	1	1.00	1.06	0.83	3.06	1.04	0.00	0.00	-0.01
time (sec)	N/A	0.202	0.582	0.193	0.398	2.071	0.000	0.000	0.000
Problem 79	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	B	F	B	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	142	142	132	116	147	265	0	300	-1
normalized size	1	1.00	0.93	0.82	1.04	1.87	0.00	2.11	-0.01
time (sec)	N/A	0.210	0.227	0.500	0.343	0.729	0.000	0.269	0.000
Problem 80	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	B	F	B	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	157	157	156	139	186	271	0	521	-1
normalized size	1	1.00	0.99	0.89	1.18	1.73	0.00	3.32	-0.01
time (sec)	N/A	0.203	1.036	0.669	0.446	1.254	0.000	0.279	0.000
Problem 81	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	B	F	B	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	298	298	268	239	302	525	0	595	-1
normalized size	1	1.00	0.90	0.80	1.01	1.76	0.00	2.00	-0.00
time (sec)	N/A	0.367	0.812	1.002	0.460	0.716	0.000	0.404	0.000
Problem 82	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	B	F	B	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	162	162	162	152	190	313	0	384	-1
normalized size	1	1.00	1.00	0.94	1.17	1.93	0.00	2.37	-0.01
time (sec)	N/A	0.334	0.378	0.434	0.364	1.357	0.000	0.286	0.000
Problem 83	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	B	F	B	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	179	179	244	175	240	327	0	605	-1
normalized size	1	1.00	1.36	0.98	1.34	1.83	0.00	3.38	-0.01
time (sec)	N/A	0.352	1.081	0.694	0.457	0.801	0.000	0.354	0.000

Problem 84	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	B	F(-1)	B	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	340	340	323	311	377	629	0	763	-1
normalized size	1	1.00	0.95	0.91	1.11	1.85	0.00	2.24	-0.00
time (sec)	N/A	0.602	1.497	1.099	0.489	1.564	0.000	0.555	0.000
Problem 85	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	C	A	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	151	151	119	123	206	144	0	0	-1
normalized size	1	1.00	0.79	0.81	1.36	0.95	0.00	0.00	-0.01
time (sec)	N/A	0.207	0.153	0.421	0.362	0.941	0.000	0.000	0.000
Problem 86	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	C	A	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	171	171	132	145	236	161	0	0	-1
normalized size	1	1.00	0.77	0.85	1.38	0.94	0.00	0.00	-0.01
time (sec)	N/A	0.218	0.247	0.415	0.378	0.482	0.000	0.000	0.000
Problem 87	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	C	A	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	301	301	224	246	412	282	0	0	-1
normalized size	1	1.00	0.74	0.82	1.37	0.94	0.00	0.00	-0.00
time (sec)	N/A	0.346	0.424	0.842	0.420	0.623	0.000	0.000	0.000
Problem 88	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	A	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	107	107	170	84	209	107	0	0	-1
normalized size	1	1.00	1.59	0.79	1.95	1.00	0.00	0.00	-0.01
time (sec)	N/A	0.198	0.477	0.319	0.357	0.762	0.000	0.000	0.000
Problem 89	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	C	A	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	140	140	188	107	315	169	0	0	-1
normalized size	1	1.00	1.34	0.76	2.25	1.21	0.00	0.00	-0.01
time (sec)	N/A	0.228	0.817	0.405	0.381	0.719	0.000	0.000	0.000

Problem 90	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	B	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	213	213	386	166	671	315	0	0	-1
normalized size	1	1.00	1.81	0.78	3.15	1.48	0.00	0.00	-0.00
time (sec)	N/A	0.332	2.315	0.764	0.397	0.595	0.000	0.000	0.000
Problem 91	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	B	F	F	F
verified	N/A	Yes	NO	TBD	TBD	TBD	TBD	TBD	TBD
size	187	187	216	169	760	299	0	0	-1
normalized size	1	1.00	1.16	0.90	4.06	1.60	0.00	0.00	-0.01
time (sec)	N/A	0.367	0.957	0.718	0.364	0.738	0.000	0.000	0.000
Problem 92	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	C	B	F	F	F
verified	N/A	Yes	NO	TBD	TBD	TBD	TBD	TBD	TBD
size	211	211	251	191	863	363	0	0	-1
normalized size	1	1.00	1.19	0.91	4.09	1.72	0.00	0.00	-0.00
time (sec)	N/A	0.419	2.249	0.647	0.383	0.698	0.000	0.000	0.000
Problem 93	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	B	F(-1)	F	F
verified	N/A	Yes	NO	TBD	TBD	TBD	TBD	TBD	TBD
size	377	377	490	338	2180	711	0	0	-1
normalized size	1	1.00	1.30	0.90	5.78	1.89	0.00	0.00	-0.00
time (sec)	N/A	0.655	6.684	1.168	0.443	0.757	0.000	0.000	0.000
Problem 94	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	C	A	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	176	176	155	170	354	178	0	0	-1
normalized size	1	1.00	0.88	0.97	2.01	1.01	0.00	0.00	-0.01
time (sec)	N/A	0.335	0.338	0.521	0.395	1.316	0.000	0.000	0.000
Problem 95	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	C	A	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	231	231	204	217	399	224	0	0	-1
normalized size	1	1.00	0.88	0.94	1.73	0.97	0.00	0.00	-0.00
time (sec)	N/A	0.383	0.694	0.589	0.392	0.716	0.000	0.000	0.000

Problem 96	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	C	A	F(-1)	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	354	354	391	338	684	346	0	0	-1
normalized size	1	1.00	1.10	0.95	1.93	0.98	0.00	0.00	-0.00
time (sec)	N/A	0.490	0.985	0.929	0.413	1.039	0.000	0.000	0.000
Problem 97	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	B	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	193	193	230	180	647	309	0	0	-1
normalized size	1	1.00	1.19	0.93	3.35	1.60	0.00	0.00	-0.01
time (sec)	N/A	0.385	0.988	0.632	0.367	0.821	0.000	0.000	0.000
Problem 98	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	C	B	F	F	F
verified	N/A	Yes	NO	TBD	TBD	TBD	TBD	TBD	TBD
size	245	245	299	227	997	400	0	0	-1
normalized size	1	1.00	1.22	0.93	4.07	1.63	0.00	0.00	-0.00
time (sec)	N/A	0.462	3.091	0.652	0.376	0.961	0.000	0.000	0.000
Problem 99	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	B	A	B	B	F(-1)	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	386	386	3291	358	2456	727	0	0	-1
normalized size	1	1.00	8.53	0.93	6.36	1.88	0.00	0.00	-0.00
time (sec)	N/A	0.573	7.038	1.172	0.418	1.996	0.000	0.000	0.000
Problem 100	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	B	F	F	F
verified	N/A	Yes	NO	TBD	TBD	TBD	TBD	TBD	TBD
size	212	212	347	216	1007	375	0	0	-1
normalized size	1	1.00	1.64	1.02	4.75	1.77	0.00	0.00	-0.00
time (sec)	N/A	0.566	2.203	0.621	0.390	1.035	0.000	0.000	0.000
Problem 101	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	B	A	C	B	F(-1)	F	F
verified	N/A	Yes	NO	TBD	TBD	TBD	TBD	TBD	TBD
size	268	268	1120	263	1487	468	0	0	-1
normalized size	1	1.00	4.18	0.98	5.55	1.75	0.00	0.00	-0.00
time (sec)	N/A	0.646	6.728	0.695	0.416	1.645	0.000	0.000	0.000

Problem 102	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	B	A	B	B	F(-1)	F	F
verified	N/A	Yes	NO	TBD	TBD	TBD	TBD	TBD	TBD
size	430	430	3835	430	4348	861	0	0	-1
normalized size	1	1.00	8.92	1.00	10.11	2.00	0.00	0.00	-0.00
time (sec)	N/A	0.911	7.261	1.251	0.493	0.870	0.000	0.000	0.000
Problem 103	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	B	F	F	F
verified	N/A	Yes	NO	TBD	TBD	TBD	TBD	TBD	TBD
size	213	213	324	217	1017	379	0	0	-1
normalized size	1	1.00	1.52	1.02	4.77	1.78	0.00	0.00	-0.00
time (sec)	N/A	0.795	1.847	1.038	0.395	0.637	0.000	0.000	0.000
Problem 104	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	36	36	26	35	25	28	112	33	25
normalized size	1	1.00	0.72	0.97	0.69	0.78	3.11	0.92	0.69
time (sec)	N/A	0.012	0.058	0.030	0.314	0.942	0.774	0.129	0.093
Problem 105	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	B	F	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	115	115	109	86	100	193	0	127	-1
normalized size	1	1.00	0.95	0.75	0.87	1.68	0.00	1.10	-0.01
time (sec)	N/A	0.099	0.166	0.127	0.341	2.090	0.000	0.145	0.000
Problem 106	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	B	F	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	144	144	135	117	131	229	0	147	-1
normalized size	1	1.00	0.94	0.81	0.91	1.59	0.00	1.02	-0.01
time (sec)	N/A	0.169	0.258	0.128	0.346	2.074	0.000	0.179	0.000
Problem 107	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	77	77	82	54	52	46	0	0	-1
normalized size	1	1.00	1.06	0.70	0.68	0.60	0.00	0.00	-0.01
time (sec)	N/A	0.057	0.083	0.043	0.326	1.689	0.000	0.000	0.000

Problem 108	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	A	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	83	83	107	60	133	70	0	0	-1
normalized size	1	1.00	1.29	0.72	1.60	0.84	0.00	0.00	-0.01
time (sec)	N/A	0.079	0.203	0.096	0.325	0.901	0.000	0.000	0.000
Problem 109	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	A	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	151	151	166	127	474	164	0	0	-1
normalized size	1	1.00	1.10	0.84	3.14	1.09	0.00	0.00	-0.01
time (sec)	N/A	0.172	0.604	0.125	0.339	1.854	0.000	0.000	0.000
Problem 110	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	B	F	B	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	142	142	133	114	147	265	0	300	-1
normalized size	1	1.00	0.94	0.80	1.04	1.87	0.00	2.11	-0.01
time (sec)	N/A	0.169	0.232	0.166	0.342	0.689	0.000	0.259	0.000
Problem 111	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	B	F	B	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	157	157	158	139	186	271	0	521	-1
normalized size	1	1.00	1.01	0.89	1.18	1.73	0.00	3.32	-0.01
time (sec)	N/A	0.173	1.035	0.328	0.437	0.865	0.000	0.304	0.000
Problem 112	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	B	F	B	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	298	298	267	235	302	525	0	595	-1
normalized size	1	1.00	0.90	0.79	1.01	1.76	0.00	2.00	-0.00
time (sec)	N/A	0.330	0.877	0.630	0.447	1.025	0.000	0.401	0.000
Problem 113	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	B	F	B	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	162	162	163	150	190	313	0	384	-1
normalized size	1	1.00	1.01	0.93	1.17	1.93	0.00	2.37	-0.01
time (sec)	N/A	0.255	0.386	0.177	0.361	1.723	0.000	0.309	0.000

Problem 114	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	B	F	B	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	179	179	245	175	240	327	0	605	-1
normalized size	1	1.00	1.37	0.98	1.34	1.83	0.00	3.38	-0.01
time (sec)	N/A	0.284	1.085	0.338	0.454	0.762	0.000	0.362	0.000
Problem 115	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	B	F	B	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	340	340	322	307	377	629	0	763	-1
normalized size	1	1.00	0.95	0.90	1.11	1.85	0.00	2.24	-0.00
time (sec)	N/A	0.520	1.573	0.730	0.469	1.558	0.000	0.589	0.000
Problem 116	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	C	A	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	147	147	116	121	204	142	0	0	-1
normalized size	1	1.00	0.79	0.82	1.39	0.97	0.00	0.00	-0.01
time (sec)	N/A	0.168	0.156	0.167	0.349	0.816	0.000	0.000	0.000
Problem 117	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	C	A	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	171	171	131	145	236	159	0	0	-1
normalized size	1	1.00	0.77	0.85	1.38	0.93	0.00	0.00	-0.01
time (sec)	N/A	0.200	0.251	0.239	0.356	0.619	0.000	0.000	0.000
Problem 118	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	C	A	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	293	293	218	242	406	280	0	0	-1
normalized size	1	1.00	0.74	0.83	1.39	0.96	0.00	0.00	-0.00
time (sec)	N/A	0.331	0.418	0.575	0.377	1.363	0.000	0.000	0.000
Problem 119	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	A	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	103	103	170	82	205	109	0	0	-1
normalized size	1	1.00	1.65	0.80	1.99	1.06	0.00	0.00	-0.01
time (sec)	N/A	0.154	0.485	0.153	0.346	2.293	0.000	0.000	0.000

Problem 120	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	C	A	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	140	140	189	107	315	167	0	0	-1
normalized size	1	1.00	1.35	0.76	2.25	1.19	0.00	0.00	-0.01
time (sec)	N/A	0.188	0.826	0.251	0.346	1.707	0.000	0.000	0.000
Problem 121	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	B	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	205	205	389	162	673	311	0	0	-1
normalized size	1	1.00	1.90	0.79	3.28	1.52	0.00	0.00	-0.00
time (sec)	N/A	0.288	2.187	0.552	0.351	0.631	0.000	0.000	0.000
Problem 122	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	B	F	F	F
verified	N/A	Yes	NO	TBD	TBD	TBD	TBD	TBD	TBD
size	183	183	217	167	761	301	0	0	-1
normalized size	1	1.00	1.19	0.91	4.16	1.64	0.00	0.00	-0.01
time (sec)	N/A	0.304	0.955	0.172	0.371	0.817	0.000	0.000	0.000
Problem 123	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	C	B	F	F	F
verified	N/A	Yes	NO	TBD	TBD	TBD	TBD	TBD	TBD
size	211	211	252	191	863	361	0	0	-1
normalized size	1	1.00	1.19	0.91	4.09	1.71	0.00	0.00	-0.00
time (sec)	N/A	0.358	2.321	0.314	0.359	1.508	0.000	0.000	0.000
Problem 124	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	B	A	B	B	F(-1)	F	F
verified	N/A	Yes	NO	TBD	TBD	TBD	TBD	TBD	TBD
size	369	369	2997	334	2183	707	0	0	-1
normalized size	1	1.00	8.12	0.91	5.92	1.92	0.00	0.00	-0.00
time (sec)	N/A	0.583	6.954	0.702	0.407	0.933	0.000	0.000	0.000
Problem 125	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	C	A	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	172	172	151	168	354	176	0	0	-1
normalized size	1	1.00	0.88	0.98	2.06	1.02	0.00	0.00	-0.01
time (sec)	N/A	0.258	0.325	0.174	0.378	0.725	0.000	0.000	0.000

Problem 126	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	C	A	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	231	231	204	217	399	224	0	0	-1
normalized size	1	1.00	0.88	0.94	1.73	0.97	0.00	0.00	-0.00
time (sec)	N/A	0.282	0.612	0.256	0.381	0.780	0.000	0.000	0.000
Problem 127	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	C	A	F(-1)	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	346	346	386	334	680	344	0	0	-1
normalized size	1	1.00	1.12	0.97	1.97	0.99	0.00	0.00	-0.00
time (sec)	N/A	0.416	0.947	0.645	0.411	0.773	0.000	0.000	0.000
Problem 128	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	B	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	189	189	231	178	648	311	0	0	-1
normalized size	1	1.00	1.22	0.94	3.43	1.65	0.00	0.00	-0.01
time (sec)	N/A	0.265	1.004	0.184	0.361	0.722	0.000	0.000	0.000
Problem 129	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	C	B	F	F	F
verified	N/A	Yes	NO	TBD	TBD	TBD	TBD	TBD	TBD
size	245	245	301	227	997	400	0	0	-1
normalized size	1	1.00	1.23	0.93	4.07	1.63	0.00	0.00	-0.00
time (sec)	N/A	0.406	3.097	0.309	0.379	0.722	0.000	0.000	0.000
Problem 130	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	B	A	B	B	F(-1)	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	378	378	3285	354	2459	723	0	0	-1
normalized size	1	1.00	8.69	0.94	6.51	1.91	0.00	0.00	-0.00
time (sec)	N/A	0.522	7.002	0.697	0.423	0.926	0.000	0.000	0.000
Problem 131	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	B	F	F	F
verified	N/A	Yes	NO	TBD	TBD	TBD	TBD	TBD	TBD
size	208	208	348	214	1008	377	0	0	-1
normalized size	1	1.00	1.67	1.03	4.85	1.81	0.00	0.00	-0.00
time (sec)	N/A	0.395	2.100	0.188	0.388	0.713	0.000	0.000	0.000

Problem 132	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	B	A	C	B	F(-1)	F	F
verified	N/A	Yes	NO	TBD	TBD	TBD	TBD	TBD	TBD
size	268	268	1118	263	1487	468	0	0	-1
normalized size	1	1.00	4.17	0.98	5.55	1.75	0.00	0.00	-0.00
time (sec)	N/A	0.461	6.739	0.330	0.415	0.679	0.000	0.000	0.000
Problem 133	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	B	A	B	B	F(-1)	F	F
verified	N/A	Yes	NO	TBD	TBD	TBD	TBD	TBD	TBD
size	422	422	3829	426	4351	857	0	0	-1
normalized size	1	1.00	9.07	1.01	10.31	2.03	0.00	0.00	-0.00
time (sec)	N/A	0.665	7.284	0.814	0.496	0.926	0.000	0.000	0.000
Problem 134	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	B	F	F	F
verified	N/A	Yes	NO	TBD	TBD	TBD	TBD	TBD	TBD
size	209	209	325	215	1018	381	0	0	-1
normalized size	1	1.00	1.56	1.03	4.87	1.82	0.00	0.00	-0.00
time (sec)	N/A	0.482	1.813	0.201	0.393	2.131	0.000	0.000	0.000
Problem 135	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	A	A	C	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	245	245	180	368	581	256	1760	1774	248
normalized size	1	1.00	0.73	1.50	2.37	1.04	7.18	7.24	1.01
time (sec)	N/A	0.358	1.628	0.424	0.391	0.715	58.624	0.379	3.420
Problem 136	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	A	A	C	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	99	99	83	183	218	83	408	941	84
normalized size	1	1.00	0.84	1.85	2.20	0.84	4.12	9.51	0.85
time (sec)	N/A	0.159	0.570	0.046	0.343	0.652	7.369	0.261	2.590
Problem 137	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	80	80	128	0	0	0	0	0	-1
normalized size	1	1.00	1.60	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.066	1.694	0.196	0.000	0.768	0.000	0.000	0.000

Problem 138	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F(-1)	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	184	184	240	0	0	0	0	0	-1
normalized size	1	1.00	1.30	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.100	3.198	0.954	0.000	0.600	0.000	0.000	0.000

Problem 139	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	A	A	C	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	245	245	228	371	578	242	1760	1772	247
normalized size	1	1.00	0.93	1.51	2.36	0.99	7.18	7.23	1.01
time (sec)	N/A	0.326	0.637	0.314	0.445	1.387	58.625	0.373	3.311

Problem 140	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	A	A	C	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	98	98	82	186	216	80	408	938	83
normalized size	1	1.00	0.84	1.90	2.20	0.82	4.16	9.57	0.85
time (sec)	N/A	0.148	0.240	0.073	0.351	0.699	7.316	0.249	2.557

Problem 141	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F(-1)	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	79	79	80	0	0	0	0	0	-1
normalized size	1	1.00	1.01	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.060	0.049	0.154	0.000	0.565	0.000	0.000	0.000

Problem 142	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F(-1)	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	169	169	145	0	0	0	0	0	-1
normalized size	1	1.00	0.86	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.097	0.394	0.376	0.000	0.599	0.000	0.000	0.000

2.3 Detailed conclusion table specific for Rubi results

The following table is specific to Rubi. It gives additional statistics for each integral. the column **steps** is the number of steps used by Rubi to obtain the antiderivative. The **rules** column is the number of unique rules used. The **integrand size** column is the leaf size of the integrand. Finally the ratio $\frac{\text{number of rules}}{\text{integrand size}}$ is given. The larger this ratio is, the harder the integral was to solve. In this test, problem number [48] had the largest ratio of [.5556]

Table 2.1: Rubi specific breakdown of results for each integral

#	grade	number of steps used	number of unique rules	normalized antiderivative leaf size	integrand leaf size	$\frac{\text{number of rules}}{\text{integrand leaf size}}$
1	A	2	2	1.00	18	0.111
2	A	2	2	1.00	18	0.111
3	A	2	2	1.00	18	0.111
4	A	1	1	1.00	16	0.062
5	A	1	1	1.00	16	0.062
6	A	1	1	1.00	18	0.056
7	A	2	2	1.00	18	0.111
8	A	2	2	1.00	18	0.111
9	A	3	2	1.00	8	0.250
10	A	2	2	1.00	18	0.111
11	A	2	2	1.00	18	0.111
12	A	2	2	1.00	18	0.111
13	A	1	1	1.00	16	0.062
14	A	1	1	1.00	16	0.062
15	A	1	1	1.00	18	0.056
16	A	2	2	1.00	18	0.111
17	A	2	2	1.00	18	0.111
18	A	3	2	1.00	8	0.250
19	A	6	3	1.00	18	0.167
20	A	5	3	1.00	18	0.167
21	A	4	3	1.00	16	0.188
22	A	4	3	1.00	16	0.188
23	A	5	3	1.00	18	0.167
24	A	6	3	1.00	18	0.167
25	A	5	4	1.00	27	0.148
26	A	2	2	1.00	18	0.111
27	A	2	2	1.00	18	0.111
28	F	0	0	N/A	0	N/A
29	A	0	0	0.00	0	0.000
30	A	0	0	0.00	0	0.000
31	A	11	5	1.00	44	0.114
32	F	0	0	N/A	0	N/A
33	A	7	4	1.00	43	0.093
34	B	14	6	19.24	35	0.171
35	A	1	1	1.00	30	0.033

Continued on next page

Table 2.1 – continued from previous page

#	grade	number of steps used	number of unique rules	normalized antiderivative leaf size	integrand leaf size	$\frac{\text{number of rules}}{\text{integrand leaf size}}$
36	A	6	3	1.00	38	0.079
37	A	10	4	1.00	38	0.105
38	A	3	3	1.00	20	0.150
39	A	4	2	1.00	22	0.091
40	A	4	2	1.00	22	0.091
41	A	4	2	1.00	22	0.091
42	A	4	3	1.00	24	0.125
43	A	5	2	1.00	24	0.083
44	A	4	2	1.00	22	0.091
45	A	5	2	1.00	24	0.083
46	A	4	2	1.00	24	0.083
47	A	4	3	1.00	7	0.429
48	A	11	5	1.00	9	0.556
49	A	4	3	1.00	7	0.429
50	A	11	5	1.00	9	0.556
51	A	4	3	1.00	19	0.158
52	A	3	1	1.00	15	0.067
53	A	5	4	1.00	26	0.154
54	A	5	4	1.00	27	0.148
55	A	5	4	1.00	26	0.154
56	A	5	4	1.00	27	0.148
57	A	6	3	1.00	10	0.300
58	A	6	3	1.00	10	0.300
59	A	6	3	1.00	12	0.250
60	A	6	3	1.00	12	0.250
61	A	2	2	1.00	15	0.133
62	A	2	2	1.00	8	0.250
63	A	3	3	1.00	12	0.250
64	A	2	2	1.00	8	0.250
65	A	2	2	1.00	12	0.167
66	A	2	2	1.00	12	0.167
67	A	3	3	1.00	10	0.300
68	A	4	3	1.00	26	0.115
69	A	2	2	1.00	8	0.250
70	A	2	2	1.00	8	0.250
71	A	3	3	1.00	12	0.250

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Table 2.1 – continued from previous page

#	grade	number of steps used	number of unique rules	normalized antiderivative leaf size	integrand leaf size	$\frac{\text{number of rules}}{\text{integrand leaf size}}$
72	A	3	3	1.00	10	0.300
73	A	1	1	1.00	10	0.100
74	A	6	4	1.00	12	0.333
75	A	6	4	1.00	15	0.267
76	A	6	3	1.00	12	0.250
77	A	4	2	1.00	14	0.143
78	A	6	3	1.00	17	0.176
79	A	8	5	1.00	16	0.312
80	A	9	6	1.00	18	0.333
81	A	14	5	1.00	18	0.278
82	A	8	5	1.00	19	0.263
83	A	9	6	1.00	21	0.286
84	A	14	5	1.00	21	0.238
85	A	8	4	1.00	16	0.250
86	A	9	4	1.00	18	0.222
87	A	14	4	1.00	18	0.222
88	A	6	4	1.00	18	0.222
89	A	7	4	1.00	20	0.200
90	A	10	4	1.00	20	0.200
91	A	8	5	1.00	21	0.238
92	A	9	5	1.00	23	0.217
93	A	14	5	1.00	23	0.217
94	A	8	4	1.00	19	0.210
95	A	10	4	1.00	21	0.190
96	A	14	4	1.00	21	0.190
97	A	8	5	1.00	21	0.238
98	A	10	5	1.00	23	0.217
99	A	14	5	1.00	23	0.217
100	A	8	5	1.00	24	0.208
101	A	10	5	1.00	26	0.192
102	A	14	5	1.00	26	0.192
103	A	8	5	1.00	24	0.208
104	A	1	1	1.00	10	0.100
105	A	6	4	1.00	12	0.333
106	A	6	4	1.00	15	0.267
107	A	6	3	1.00	12	0.250

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Table 2.1 – continued from previous page

#	grade	number of steps used	number of unique rules	normalized antiderivative leaf size	integrand leaf size	$\frac{\text{number of rules}}{\text{integrand leaf size}}$
108	A	4	2	1.00	14	0.143
109	A	6	3	1.00	17	0.176
110	A	8	5	1.00	16	0.312
111	A	9	6	1.00	18	0.333
112	A	14	5	1.00	18	0.278
113	A	8	5	1.00	19	0.263
114	A	9	6	1.00	21	0.286
115	A	14	5	1.00	21	0.238
116	A	8	4	1.00	16	0.250
117	A	9	4	1.00	18	0.222
118	A	14	4	1.00	18	0.222
119	A	6	4	1.00	18	0.222
120	A	7	4	1.00	20	0.200
121	A	10	4	1.00	20	0.200
122	A	8	5	1.00	21	0.238
123	A	9	5	1.00	23	0.217
124	A	14	5	1.00	23	0.217
125	A	8	4	1.00	19	0.210
126	A	10	4	1.00	21	0.190
127	A	14	4	1.00	21	0.190
128	A	8	5	1.00	21	0.238
129	A	10	5	1.00	23	0.217
130	A	14	5	1.00	23	0.217
131	A	8	5	1.00	24	0.208
132	A	10	5	1.00	26	0.192
133	A	14	5	1.00	26	0.192
134	A	8	5	1.00	24	0.208
135	A	8	6	1.00	22	0.273
136	A	6	5	1.00	20	0.250
137	A	2	2	1.00	22	0.091
138	A	3	3	1.00	22	0.136
139	A	8	6	1.00	22	0.273
140	A	6	5	1.00	20	0.250
141	A	2	2	1.00	22	0.091
142	A	3	3	1.00	22	0.136

Chapter 3

Listing of integrals

3.1 $\int F^{c(a+bx)} \sin^n(d+ex) dx$

Optimal. Leaf size=107

$$\frac{(1 - e^{2i(d+ex)})^{-n} F^{c(a+bx)} \sin^n(d+ex) {}_2F_1\left(-n, -\frac{en+ibc \log(F)}{2e}; \frac{1}{2}\left(-n - \frac{ibc \log(F)}{e} + 2\right); e^{2i(d+ex)}\right)}{-bc \log(F) + ien}$$

[Out] $-F^{c(bx+a)} \text{hypergeom}([-n, 1/2*(-e*n - I*b*c*\ln(F))/e], [1 - 1/2*n - 1/2*I*b*c*\ln(F)/e], \exp(2*I*(e*x+d))) * \sin(e*x+d)^n / ((1 - \exp(2*I*(e*x+d)))^n) / (I*e^n - b*c*\ln(F))$

Rubi [A] time = 0.14, antiderivative size = 107, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {4440, 2259}

$$\frac{(1 - e^{2i(d+ex)})^{-n} F^{c(a+bx)} \sin^n(d+ex) {}_2F_1\left(-n, -\frac{en+ibc \log(F)}{2e}; \frac{1}{2}\left(-n - \frac{ibc \log(F)}{e} + 2\right); e^{2i(d+ex)}\right)}{-bc \log(F) + ien}$$

Antiderivative was successfully verified.

[In] $\text{Int}[F^{c(a+bx)} \sin^n(d+ex), x]$

[Out] $-\left(F^{c(a+bx)} \text{Hypergeometric2F1}\left[-n, -\frac{e*n + I*b*c*\text{Log}[F]}{2e}, \frac{2-n - (I*b*c*\text{Log}[F])/e}{2}, E^{(2*I)*(d+e*x)}\right] * \sin^n(d+ex) / \left((1 - E^{(2*I)*(d+e*x)})^n * (I*e^n - b*c*\text{Log}[F])\right)\right)$

Rule 2259

$\text{Int}[(a_+ + (b_+)(F_+)^{(e_+)((c_+) + (d_+)(x_+))})^{(p_+)}(G_+)^{(h_+)}((f_+ + (g_+)(x_+)))(H_+)^{(t_+)((r_+) + (s_+)(x_+))}, x_Symbol] \rightarrow \text{Simp}[(G_+^{(h_+)}(f_+ + g_+x_+)^{p_+} H_+^{(t_+)(r_+ + s_+x_+)} (a_+ + b_+F_+^{(e_+(c_+ + d_+x_+))})^{p_+} \text{Hypergeometric2F1}[-p_+, (g_+h_+\text{Log}[G_+] + s_+t_+\text{Log}[H_+])/(d_+e_+\text{Log}[F_+]), (g_+h_+\text{Log}[G_+] + s_+t_+\text{Log}[H_+])/(d_+e_+\text{Log}[F_+] + 1), \text{Simplify}[-(b_+F_+^{(e_+(c_+ + d_+x_+))})/a_+]]) / ((g_+h_+\text{Log}[G_+] + s_+t_+\text{Log}[H_+]) * (a_+ + b_+F_+^{(e_+(c_+ + d_+x_+))})/a_+)^{p_+}], x] /; \text{FreeQ}\{F, G, H, a, b, c, d, e, f, g, h, r, s, t, p\}, x] \&\amp; \text{!IntegerQ}[p]$

Rule 4440

$\text{Int}[F_+^{(c_+)((a_+) + (b_+)(x_+))} \sin^n(d_+ + (e_+)(x_+))^{(n_+)}, x_Symbol] \rightarrow \text{Dist}[(E^{(I*n_+(d_+ + e_+x_+))} \sin^n(d_+ + e_+x_+)) / (-1 + E^{(2*I*(d_+ + e_+x_+))})^{n_+}, \text{Int}[F_+^{c_+(a_+ + b_+x_+)} (-1 + E^{(2*I*(d_+ + e_+x_+))})^{n_+} / E^{(I*n_+(d_+ + e_+x_+))}, x], x] /; \text{FreeQ}\{F, a, b, c, d, e, n\}, x] \&\amp; \text{!IntegerQ}[n]$

Rubi steps

$$\int F^{c(a+bx)} \sin^n(d+ex) dx = \left(e^{in(d+ex)} (-1 + e^{2i(d+ex)})^{-n} \sin^n(d+ex) \right) \int e^{-in(d+ex)} (-1 + e^{2i(d+ex)})^n F^{c(a+bx)} dx$$

$$= \frac{(1 - e^{2i(d+ex)})^{-n} F^{c(a+bx)} {}_2F_1\left(-n, -\frac{en+ibc \log(F)}{2e}; \frac{1}{2} \left(2 - n - \frac{ibc \log(F)}{e}\right); e^{2i(d+ex)}\right) \sin^n(d)}{ien - bc \log(F)}$$

Mathematica [A] time = 0.06, size = 110, normalized size = 1.03

$$\frac{(1 - e^{2i(d+ex)})^{-n} F^{c(a+bx)} \sin^n(d+ex) {}_2F_1\left(-n, -\frac{i(bc \log(F)-ien)}{2e}; 1 - \frac{i(bc \log(F)-ien)}{2e}; e^{2i(d+ex)}\right)}{bc \log(F) - ien}$$

Antiderivative was successfully verified.

[In] Integrate[F^(c*(a + b*x))*Sin[d + e*x]^n,x]

[Out] (F^(c*(a + b*x))*Hypergeometric2F1[-n, ((-1/2*I)*((-I)*e*n + b*c*Log[F]))/e, 1 - ((I/2)*((-I)*e*n + b*c*Log[F]))/e, E^((2*I)*(d + e*x))]*Sin[d + e*x]^n)/((1 - E^((2*I)*(d + e*x)))^n*(-I)*e*n + b*c*Log[F])

fricas [F] time = 0.57, size = 0, normalized size = 0.00

$$\text{integral}\left(F^{bcx+ac} \sin(ex+d)^n, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(F^(c*(b*x+a))*sin(e*x+d)^n,x, algorithm="fricas")

[Out] integral(F^(b*c*x + a*c)*sin(e*x + d)^n, x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int F^{(bx+a)c} \sin(ex+d)^n dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(F^(c*(b*x+a))*sin(e*x+d)^n,x, algorithm="giac")

[Out] integrate(F^((b*x + a)*c)*sin(e*x + d)^n, x)

maple [F] time = 1.02, size = 0, normalized size = 0.00

$$\int F^{c(bx+a)} (\sin^n(ex+d)) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(F^(c*(b*x+a))*sin(e*x+d)^n,x)

[Out] int(F^(c*(b*x+a))*sin(e*x+d)^n,x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int F^{(bx+a)c} \sin(ex+d)^n dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(F^(c*(b*x+a))*sin(e*x+d)^n,x, algorithm="maxima")

[Out] integrate(F^((b*x + a)*c)*sin(e*x + d)^n, x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int F^{c(a+bx)} \sin(d+ex)^n dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(F^(c*(a + b*x))*sin(d + e*x)^n, x)

[Out] int(F^(c*(a + b*x))*sin(d + e*x)^n, x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int F^{c(a+bx)} \sin^n(d+ex) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(F**(c*(b*x+a))*sin(e*x+d)**n, x)

[Out] Integral(F**(c*(a + b*x))*sin(d + e*x)**n, x)

Antiderivative was successfully verified.

[In] Integrate[F^(c*(a + b*x))*Sin[d + e*x]^3,x]

[Out] (F^(c*(a + b*x))*(-3*e*cos[d + e*x]*(9*e^2 + b^2*c^2*Log[F]^2) + 3*Cos[3*(d + e*x)]*(e^3 + b^2*c^2*e*Log[F]^2) - 2*b*c*Log[F]*(-13*e^2 - b^2*c^2*Log[F]^2 + Cos[2*(d + e*x)]*(e^2 + b^2*c^2*Log[F]^2))*Sin[d + e*x]))/(4*(9*e^4 + 10*b^2*c^2*e^2*Log[F]^2 + b^4*c^4*Log[F]^4))

fricas [A] time = 0.62, size = 171, normalized size = 0.86

$$\frac{(3e^3 \cos(ex + d)^3 - 9e^3 \cos(ex + d) + 3(b^2c^2e \cos(ex + d)^3 - b^2c^2e \cos(ex + d)) \log(F)^2 - ((b^3c^3 \cos(ex + d) - b^3c^3) \log(F)^2 - (b^3c^3 \cos(ex + d) - b^3c^3) \log(F)^2))}{b^4c^4 \log(F)^4 + 10b^2c^2e^2 \log(F)^2 + 9e^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(F^(c*(b*x+a))*sin(e*x+d)^3,x, algorithm="fricas")

[Out] (3*e^3*cos(e*x + d)^3 - 9*e^3*cos(e*x + d) + 3*(b^2*c^2*e*cos(e*x + d)^3 - b^2*c^2*e*cos(e*x + d))*log(F)^2 - ((b^3*c^3*cos(e*x + d)^2 - b^3*c^3)*log(F)^3 + (b*c*e^2*cos(e*x + d)^2 - 7*b*c*e^2)*log(F))*sin(e*x + d))*F^(b*c*x + a*c)/(b^4*c^4*log(F)^4 + 10*b^2*c^2*e^2*log(F)^2 + 9*e^4)

giac [C] time = 0.28, size = 1311, normalized size = 6.59

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(F^(c*(b*x+a))*sin(e*x+d)^3,x, algorithm="giac")

[Out] -1/4*(2*b*c*log(abs(F))*sin(1/2*pi*b*c*x*sgn(F) - 1/2*pi*b*c*x + 1/2*pi*a*c*sgn(F) - 1/2*pi*a*c + 3*x*e + 3*d)/(4*b^2*c^2*log(abs(F))^2 + (pi*b*c*sgn(F) - pi*b*c + 6*e)^2) - (pi*b*c*sgn(F) - pi*b*c + 6*e)*cos(1/2*pi*b*c*x*sgn(F) - 1/2*pi*b*c*x + 1/2*pi*a*c*sgn(F) - 1/2*pi*a*c + 3*x*e + 3*d)/(4*b^2*c^2*log(abs(F))^2 + (pi*b*c*sgn(F) - pi*b*c + 6*e)^2))*e^(b*c*x*log(abs(F)) + a*c*log(abs(F))) + 3/4*(2*b*c*log(abs(F))*sin(1/2*pi*b*c*x*sgn(F) - 1/2*pi*b*c*x + 1/2*pi*a*c*sgn(F) - 1/2*pi*a*c + x*e + d)/(4*b^2*c^2*log(abs(F))^2 + (pi*b*c*sgn(F) - pi*b*c + 2*e)^2) - (pi*b*c*sgn(F) - pi*b*c + 2*e)*cos(1/2*pi*b*c*x*sgn(F) - 1/2*pi*b*c*x + 1/2*pi*a*c*sgn(F) - 1/2*pi*a*c + x*e + d)/(4*b^2*c^2*log(abs(F))^2 + (pi*b*c*sgn(F) - pi*b*c + 2*e)^2))*e^(b*c*x*log(abs(F)) + a*c*log(abs(F))) - 3/4*(2*b*c*log(abs(F))*sin(1/2*pi*b*c*x*sgn(F) - 1/2*pi*b*c*x + 1/2*pi*a*c*sgn(F) - 1/2*pi*a*c - x*e - d)/(4*b^2*c^2*log(abs(F))^2 + (pi*b*c*sgn(F) - pi*b*c - 2*e)^2) - (pi*b*c*sgn(F) - pi*b*c - 2*e)*cos(1/2*pi*b*c*x*sgn(F) - 1/2*pi*b*c*x + 1/2*pi*a*c*sgn(F) - 1/2*pi*a*c - x*e - d)/(4*b^2*c^2*log(abs(F))^2 + (pi*b*c*sgn(F) - pi*b*c - 2*e)^2))*e^(b*c*x*log(abs(F)) + a*c*log(abs(F))) + 1/4*(2*b*c*log(abs(F))*sin(1/2*pi*b*c*x*sgn(F) - 1/2*pi*b*c*x + 1/2*pi*a*c*sgn(F) - 1/2*pi*a*c - 3*x*e - 3*d)/(4*b^2*c^2*log(abs(F))^2 + (pi*b*c*sgn(F) - pi*b*c - 6*e)^2) - (pi*b*c*sgn(F) - pi*b*c - 6*e)*cos(1/2*pi*b*c*x*sgn(F) - 1/2*pi*b*c*x + 1/2*pi*a*c*sgn(F) - 1/2*pi*a*c - 3*x*e - 3*d)/(4*b^2*c^2*log(abs(F))^2 + (pi*b*c*sgn(F) - pi*b*c - 6*e)^2))*e^(b*c*x*log(abs(F)) + a*c*log(abs(F))) + 1/2*(-2*I*e^(1/2*I*pi*b*c*x*sgn(F) - 1/2*I*pi*b*c*x + 1/2*I*pi*a*c*sgn(F) - 1/2*I*pi*a*c + 3*I*x*e + 3*I*d)/(8*I*pi*b*c*sgn(F) - 8*I*pi*b*c + 16*b*c*log(abs(F)) + 48*I*e) - 2*I*e^(-1/2*I*pi*b*c*x*sgn(F) + 1/2*I*pi*b*c*x - 1/2*I*pi*a*c*sgn(F) + 1/2*I*pi*a*c - 3*I*x*e - 3*I*d)/(-8*I*pi*b*c*sgn(F) + 8*I*pi*b*c + 16*b*c*log(abs(F)) - 48*I*e))*e^(b*c*x*log(abs(F)) + a*c*log(abs(F))) + 1/2*(6*I*e^(1/2*I*pi*b*c*x*sgn(F) - 1/2*I*pi*b*c*x + 1/2*I*pi*a*c*sgn(F) - 1/2*I*pi*a*c + I*x*e + I*d)/(8*I*pi*b*c*sgn(F) - 8*I*pi*b*c + 16*b*c*log(abs(F)) + 16*I*e) + 6*I*e^(-1/2*I*pi*b*c*x*sgn(F) + 1/2*I*pi*b*c*x - 1/2*I*pi*a*c*sgn(F) + 1/2*I*pi*a*c - I*x*e - I*d)/(-8*I*pi*b*c*sgn(F) + 8*I*pi*b*c + 16*b*c*log(abs(F)) - 16*I*e))*e^(b*c*x*log(abs(F)) + a*c*log(abs(F))) + 1/2

$$\begin{aligned} & *(-6*I*e^{(1/2*I*pi*b*c*x*sgn(F) - 1/2*I*pi*b*c*x + 1/2*I*pi*a*c*sgn(F) - 1/} \\ & 2*I*pi*a*c - I*x*e - I*d)/(8*I*pi*b*c*sgn(F) - 8*I*pi*b*c + 16*b*c*log(abs(\\ & F)) - 16*I*e) - 6*I*e^{(-1/2*I*pi*b*c*x*sgn(F) + 1/2*I*pi*b*c*x - 1/2*I*pi*a \\ & *c*sgn(F) + 1/2*I*pi*a*c + I*x*e + I*d)/(-8*I*pi*b*c*sgn(F) + 8*I*pi*b*c + \\ & 16*b*c*log(abs(F)) + 16*I*e))*e^{(b*c*x*log(abs(F)) + a*c*log(abs(F)))} + 1/2 \\ & *(2*I*e^{(1/2*I*pi*b*c*x*sgn(F) - 1/2*I*pi*b*c*x + 1/2*I*pi*a*c*sgn(F) - 1/2 \\ & *I*pi*a*c - 3*I*x*e - 3*I*d)/(8*I*pi*b*c*sgn(F) - 8*I*pi*b*c + 16*b*c*log(a \\ & bs(F)) - 48*I*e) + 2*I*e^{(-1/2*I*pi*b*c*x*sgn(F) + 1/2*I*pi*b*c*x - 1/2*I*pi \\ & i*a*c*sgn(F) + 1/2*I*pi*a*c + 3*I*x*e + 3*I*d)/(-8*I*pi*b*c*sgn(F) + 8*I*pi \\ & *b*c + 16*b*c*log(abs(F)) + 48*I*e))*e^{(b*c*x*log(abs(F)) + a*c*log(abs(F)) \\ &)} \end{aligned}$$

maple [A] time = 0.44, size = 336, normalized size = 1.69

$$\frac{3F^{ac}e^{bcx \ln(F)}}{4\left(1 + \tan^2\left(\frac{d}{2} + \frac{ex}{2}\right)\right)(e^2 + b^2c^2 \ln(F)^2)} + \frac{3F^{ac}e^{bcx \ln(F)}\left(\tan^2\left(\frac{d}{2} + \frac{ex}{2}\right)\right)}{4\left(1 + \tan^2\left(\frac{d}{2} + \frac{ex}{2}\right)\right)(e^2 + b^2c^2 \ln(F)^2)} + \frac{3F^{ac}bc \ln(F)e^{bcx \ln(F)} \tan\left(\frac{d}{2} + \frac{ex}{2}\right)}{2\left(1 + \tan^2\left(\frac{d}{2} + \frac{ex}{2}\right)\right)(e^2 + b^2c^2 \ln(F)^2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(F^(c*(b*x+a))*sin(e*x+d)^3,x)

[Out]
$$\begin{aligned} & -3/4*F^{(a*c)}/(1+\tan(1/2*d+1/2*e*x)^2)/(e^2+b^2*c^2*\ln(F)^2)*e*\exp(b*c*x*\ln(F))+3/4*F^{(a*c)}/(1+\tan(1/2*d+1/2*e*x)^2)/(e^2+b^2*c^2*\ln(F)^2)*e*\exp(b*c*x* \\ & \ln(F))*\tan(1/2*d+1/2*e*x)^2+3/2*F^{(a*c)}/(1+\tan(1/2*d+1/2*e*x)^2)*b*c*\ln(F)/ \\ & (e^2+b^2*c^2*\ln(F)^2)*\exp(b*c*x*\ln(F))*\tan(1/2*d+1/2*e*x)+3/4*F^{(a*c)}/(1+\tan \\ & (3/2*e*x+3/2*d)^2)/(9*e^2+b^2*c^2*\ln(F)^2)*e*\exp(b*c*x*\ln(F))-3/4*F^{(a*c)}/ \\ & (1+\tan(3/2*e*x+3/2*d)^2)/(9*e^2+b^2*c^2*\ln(F)^2)*e*\exp(b*c*x*\ln(F))*\tan(3/2 \\ & *e*x+3/2*d)^2-1/2*F^{(a*c)}/(1+\tan(3/2*e*x+3/2*d)^2)*\ln(F)*b*c/(9*e^2+b^2*c^2 \\ & *\ln(F)^2)*\exp(b*c*x*\ln(F))*\tan(3/2*e*x+3/2*d) \end{aligned}$$

maxima [B] time = 0.49, size = 813, normalized size = 4.09

$$\frac{(F^{ac}b^3c^3 \log(F)^3 \sin(3d) - 3F^{ac}b^2c^2e \cos(3d) \log(F)^2 + F^{ac}bce^2 \log(F) \sin(3d) - 3F^{ac}e^3 \cos(3d))F^{bcx} \cos(3e)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(F^(c*(b*x+a))*sin(e*x+d)^3,x, algorithm="maxima")

[Out]
$$\begin{aligned} & -1/8*((F^{(a*c)}*b^3*c^3*\log(F)^3*\sin(3*d) - 3*F^{(a*c)}*b^2*c^2*e*\cos(3*d))*\log \\ & (F)^2 + F^{(a*c)}*b*c*e^2*\log(F)*\sin(3*d) - 3*F^{(a*c)}*e^3*\cos(3*d))*F^{(b*c*x)} \\ & *\cos(3*e*x) - (F^{(a*c)}*b^3*c^3*\log(F)^3*\sin(3*d) + 3*F^{(a*c)}*b^2*c^2*e*\cos(\\ & 3*d))*\log(F)^2 + F^{(a*c)}*b*c*e^2*\log(F)*\sin(3*d) + 3*F^{(a*c)}*e^3*\cos(3*d))*F \\ & ^{(b*c*x)}*\cos(3*e*x + 6*d) + 3*(F^{(a*c)}*b^3*c^3*\log(F)^3*\sin(3*d) + F^{(a*c)}* \\ & b^2*c^2*e*\cos(3*d))*\log(F)^2 + 9*F^{(a*c)}*b*c*e^2*\log(F)*\sin(3*d) + 9*F^{(a*c)} \\ & *e^3*\cos(3*d))*F^{(b*c*x)}*\cos(e*x + 4*d) - 3*(F^{(a*c)}*b^3*c^3*\log(F)^3*\sin(3 \\ & *d) - F^{(a*c)}*b^2*c^2*e*\cos(3*d))*\log(F)^2 + 9*F^{(a*c)}*b*c*e^2*\log(F)*\sin(3 \\ & *d) - 9*F^{(a*c)}*e^3*\cos(3*d))*F^{(b*c*x)}*\cos(e*x - 2*d) + (F^{(a*c)}*b^3*c^3*co \\ & s(3*d))*\log(F)^3 + 3*F^{(a*c)}*b^2*c^2*e*\log(F)^2*\sin(3*d) + F^{(a*c)}*b*c*e^2*c \\ & os(3*d))*\log(F) + 3*F^{(a*c)}*e^3*\sin(3*d))*F^{(b*c*x)}*\sin(3*e*x) + (F^{(a*c)}*b^ \\ & 3*c^3*\cos(3*d))*\log(F)^3 - 3*F^{(a*c)}*b^2*c^2*e*\log(F)^2*\sin(3*d) + F^{(a*c)}*b \\ & *c*e^2*\cos(3*d))*\log(F) - 3*F^{(a*c)}*e^3*\sin(3*d))*F^{(b*c*x)}*\sin(3*e*x + 6*d) \\ & - 3*(F^{(a*c)}*b^3*c^3*\cos(3*d))*\log(F)^3 - F^{(a*c)}*b^2*c^2*e*\log(F)^2*\sin(3 \\ & *d) + 9*F^{(a*c)}*b*c*e^2*\cos(3*d))*\log(F) - 9*F^{(a*c)}*e^3*\sin(3*d))*F^{(b*c*x)}* \\ & \sin(e*x + 4*d) - 3*(F^{(a*c)}*b^3*c^3*\cos(3*d))*\log(F)^3 + F^{(a*c)}*b^2*c^2*e* \\ & \log(F)^2*\sin(3*d) + 9*F^{(a*c)}*b*c*e^2*\cos(3*d))*\log(F) + 9*F^{(a*c)}*e^3*\sin(3 \\ & *d))*F^{(b*c*x)}*\sin(e*x - 2*d))/(b^4*c^4*\cos(3*d)^2*\log(F)^4 + b^4*c^4*\log(F) \\ & ^4*\sin(3*d)^2 + 9*(\cos(3*d)^2 + \sin(3*d)^2)*e^4 + 10*(b^2*c^2*\cos(3*d)^2*lo \\ & g(F)^2 + b^2*c^2*\log(F)^2*\sin(3*d)^2)*e^2) \end{aligned}$$

mupad [B] time = 3.22, size = 190, normalized size = 0.95

$$\frac{3F^{c(a+bx)} (\cos(ex) - \sin(ex)1i) (\cos(d) - \sin(d)1i)}{8(e + bc \ln(F)1i)} + \frac{F^{c(a+bx)} (\cos(3ex) + \sin(3ex)1i) (\cos(3d) + \sin(3d)1i)}{8(bc \ln(F) + e3i)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(F^(c*(a + b*x))*sin(d + e*x)^3,x)

[Out] (F^(c*(a + b*x))*(cos(3*e*x) + sin(3*e*x)*1i)*(cos(3*d) + sin(3*d)*1i)*1i)/(8*(e*3i + b*c*log(F))) - (3*F^(c*(a + b*x))*(cos(e*x) - sin(e*x)*1i)*(cos(d) - sin(d)*1i))/(8*(e + b*c*log(F)*1i)) + (F^(c*(a + b*x))*(cos(3*e*x) - sin(3*e*x)*1i)*(cos(3*d) - sin(3*d)*1i))/(8*(3*e + b*c*log(F)*1i)) - (F^(c*(a + b*x))*(cos(e*x) + sin(e*x)*1i)*(cos(d) + sin(d)*1i)*3i)/(8*(e*1i + b*c*log(F)))

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(F**(c*(b*x+a))*sin(e*x+d)**3,x)

[Out] Timed out

3.3 $\int F^{c(a+bx)} \sin^2(d+ex) dx$

Optimal. Leaf size=128

$$\frac{bc \log(F) \sin^2(d+ex) F^{c(a+bx)}}{b^2 c^2 \log^2(F) + 4e^2} - \frac{2e \sin(d+ex) \cos(d+ex) F^{c(a+bx)}}{b^2 c^2 \log^2(F) + 4e^2} + \frac{2e^2 F^{c(a+bx)}}{bc \log(F) (b^2 c^2 \log^2(F) + 4e^2)}$$

[Out] $2e^2 F^{c(a+bx)} / (bc \log(F) (b^2 c^2 \log^2(F) + 4e^2)) - 2e \sin(d+ex) \cos(d+ex) F^{c(a+bx)} / (b^2 c^2 \log^2(F) + 4e^2) + (2e^2 F^{c(a+bx)}) / (bc \log(F) (b^2 c^2 \log^2(F) + 4e^2))$

Rubi [A] time = 0.05, antiderivative size = 128, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {4434, 2194}

$$\frac{bc \log(F) \sin^2(d+ex) F^{c(a+bx)}}{b^2 c^2 \log^2(F) + 4e^2} - \frac{2e \sin(d+ex) \cos(d+ex) F^{c(a+bx)}}{b^2 c^2 \log^2(F) + 4e^2} + \frac{2e^2 F^{c(a+bx)}}{bc \log(F) (b^2 c^2 \log^2(F) + 4e^2)}$$

Antiderivative was successfully verified.

[In] Int[F^(c*(a + b*x))*Sin[d + e*x]^2,x]

[Out] $(2e^2 F^{c(a+bx)}) / (bc \log(F) (4e^2 + b^2 c^2 \log^2(F))) - (2e F^{c(a+bx)} \cos(d+ex) \sin(d+ex)) / (4e^2 + b^2 c^2 \log^2(F)) + (bc F^{c(a+bx)} \log(F) \sin^2(d+ex)) / (4e^2 + b^2 c^2 \log^2(F))$

Rule 2194

Int[((F_)^((c_.)*((a_.) + (b_.)*(x_))))^(n_.), x_Symbol] :> Simp[(F^(c*(a + b*x)))^n/(b*c*n*Log[F]), x] /; FreeQ[{F, a, b, c, n}, x]

Rule 4434

Int[(F_)^((c_.)*((a_.) + (b_.)*(x_)))*Sin[(d_.) + (e_.)*(x_)]^(n_), x_Symbol] :> Simp[(b*c*Log[F]*F^(c*(a + b*x))*Sin[d + e*x]^n]/(e^2*n^2 + b^2*c^2*Log[F]^2), x] + (Dist[(n*(n - 1)*e^2)/(e^2*n^2 + b^2*c^2*Log[F]^2), Int[F^(c*(a + b*x))*Sin[d + e*x]^(n - 2), x], x] - Simp[(e*n*F^(c*(a + b*x))*Cos[d + e*x]*Sin[d + e*x]^(n - 1)]/(e^2*n^2 + b^2*c^2*Log[F]^2), x]) /; FreeQ[{F, a, b, c, d, e}, x] && NeQ[e^2*n^2 + b^2*c^2*Log[F]^2, 0] && GtQ[n, 1]

Rubi steps

$$\begin{aligned} \int F^{c(a+bx)} \sin^2(d+ex) dx &= -\frac{2e F^{c(a+bx)} \cos(d+ex) \sin(d+ex)}{4e^2 + b^2 c^2 \log^2(F)} + \frac{bc F^{c(a+bx)} \log(F) \sin^2(d+ex)}{4e^2 + b^2 c^2 \log^2(F)} + \frac{(2e^2) \int F^{c(a+bx)} dx}{4e^2 + b^2 c^2 \log^2(F)} \\ &= \frac{2e^2 F^{c(a+bx)}}{bc \log(F) (4e^2 + b^2 c^2 \log^2(F))} - \frac{2e F^{c(a+bx)} \cos(d+ex) \sin(d+ex)}{4e^2 + b^2 c^2 \log^2(F)} + \frac{bc F^{c(a+bx)} \log(F) \sin^2(d+ex)}{4e^2 + b^2 c^2 \log^2(F)} \end{aligned}$$

Mathematica [A] time = 0.22, size = 86, normalized size = 0.67

$$\frac{F^{c(a+bx)} (-b^2 c^2 \log^2(F) \cos(2(d+ex)) + b^2 c^2 \log^2(F) - 2bce \log(F) \sin(2(d+ex)) + 4e^2)}{2b^3 c^3 \log^3(F) + 8bce^2 \log(F)}$$

Antiderivative was successfully verified.

[In] Integrate[F^(c*(a + b*x))*Sin[d + e*x]^2,x]

[Out] $(F^{(c(a+bx))} * (4e^2 + b^2c^2 \log(F)^2 - b^2c^2 \cos(2(d+ex))) * \log(F)^2 - 2bce \log(F) \sin(2(d+ex))) / (8b^3c^3 \log(F)^3 + 2b^3c^3 \log(F)^3)$

fricas [A] time = 1.86, size = 89, normalized size = 0.70

$$\frac{(2bce \cos(ex+d) \log(F) \sin(ex+d) + (b^2c^2 \cos(ex+d)^2 - b^2c^2) \log(F)^2 - 2e^2) F^{bcx+ac}}{b^3c^3 \log(F)^3 + 4bce^2 \log(F)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(F^(c*(b*x+a))*sin(e*x+d)^2,x, algorithm="fricas")

[Out] $-(2b^2c^2e \cos(ex+d) \log(F) \sin(ex+d) + (b^2c^2 \cos(ex+d)^2 - b^2c^2) \log(F)^2 - 2e^2) F^{(b^2c^2x + a^2c)} / (b^3c^3 \log(F)^3 + 4b^2c^2e \log(F))$

giac [C] time = 0.24, size = 933, normalized size = 7.29

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(F^(c*(b*x+a))*sin(e*x+d)^2,x, algorithm="giac")

[Out] $-1/2 * (2b^2c^2 \cos(1/2 \pi b^2c^2 x \operatorname{sgn}(F) - 1/2 \pi b^2c^2 x + 1/2 \pi a^2c^2 \operatorname{sgn}(F) - 1/2 \pi a^2c^2 + 2x^2e + 2d) \log(\operatorname{abs}(F)) / (4b^2c^2 \log(\operatorname{abs}(F))^2 + (\pi b^2c^2 \operatorname{sgn}(F) - \pi b^2c^2 + 4e)^2) + (\pi b^2c^2 \operatorname{sgn}(F) - \pi b^2c^2 + 4e) \sin(1/2 \pi b^2c^2 x \operatorname{sgn}(F) - 1/2 \pi b^2c^2 x + 1/2 \pi a^2c^2 \operatorname{sgn}(F) - 1/2 \pi a^2c^2 + 2x^2e + 2d) / (4b^2c^2 \log(\operatorname{abs}(F))^2 + (\pi b^2c^2 \operatorname{sgn}(F) - \pi b^2c^2 + 4e)^2) * e^{(b^2c^2 x \log(\operatorname{abs}(F)) + a^2c^2 \log(\operatorname{abs}(F)))} - 1/2 * (2b^2c^2 \cos(1/2 \pi b^2c^2 x \operatorname{sgn}(F) - 1/2 \pi b^2c^2 x + 1/2 \pi a^2c^2 \operatorname{sgn}(F) - 1/2 \pi a^2c^2 - 2x^2e - 2d) \log(\operatorname{abs}(F)) / (4b^2c^2 \log(\operatorname{abs}(F))^2 + (\pi b^2c^2 \operatorname{sgn}(F) - \pi b^2c^2 - 4e)^2) + (\pi b^2c^2 \operatorname{sgn}(F) - \pi b^2c^2 - 4e) \sin(1/2 \pi b^2c^2 x \operatorname{sgn}(F) - 1/2 \pi b^2c^2 x + 1/2 \pi a^2c^2 \operatorname{sgn}(F) - 1/2 \pi a^2c^2 - 2x^2e - 2d) / (4b^2c^2 \log(\operatorname{abs}(F))^2 + (\pi b^2c^2 \operatorname{sgn}(F) - \pi b^2c^2 - 4e)^2) * e^{(b^2c^2 x \log(\operatorname{abs}(F)) + a^2c^2 \log(\operatorname{abs}(F)))} + (2b^2c^2 \cos(-1/2 \pi b^2c^2 x \operatorname{sgn}(F) + 1/2 \pi b^2c^2 x - 1/2 \pi a^2c^2 \operatorname{sgn}(F) + 1/2 \pi a^2c^2) \log(\operatorname{abs}(F)) / (4b^2c^2 \log(\operatorname{abs}(F))^2 + (\pi b^2c^2 \operatorname{sgn}(F) - \pi b^2c^2)^2) - (\pi b^2c^2 \operatorname{sgn}(F) - \pi b^2c^2) \sin(-1/2 \pi b^2c^2 x \operatorname{sgn}(F) + 1/2 \pi b^2c^2 x - 1/2 \pi a^2c^2 \operatorname{sgn}(F) + 1/2 \pi a^2c^2) / (4b^2c^2 \log(\operatorname{abs}(F))^2 + (\pi b^2c^2 \operatorname{sgn}(F) - \pi b^2c^2)^2) * e^{(b^2c^2 x \log(\operatorname{abs}(F)) + a^2c^2 \log(\operatorname{abs}(F)))} - 1/2 * I * (2I * e^{(1/2 I \pi b^2c^2 x \operatorname{sgn}(F) - 1/2 I \pi b^2c^2 x + 1/2 I \pi a^2c^2 \operatorname{sgn}(F) - 1/2 I \pi a^2c^2 + 2I x^2e + 2I d)} / (4I \pi b^2c^2 \operatorname{sgn}(F) - 4I \pi b^2c^2 + 8b^2c^2 \log(\operatorname{abs}(F)) + 16I e) - 2I * e^{(-1/2 I \pi b^2c^2 x \operatorname{sgn}(F) + 1/2 I \pi b^2c^2 x - 1/2 I \pi a^2c^2 \operatorname{sgn}(F) + 1/2 I \pi a^2c^2 - 2I x^2e - 2I d)} / (-4I \pi b^2c^2 \operatorname{sgn}(F) + 4I \pi b^2c^2 + 8b^2c^2 \log(\operatorname{abs}(F)) - 16I e) * e^{(b^2c^2 x \log(\operatorname{abs}(F)) + a^2c^2 \log(\operatorname{abs}(F)))} - 1/2 * I * (2I * e^{(1/2 I \pi b^2c^2 x \operatorname{sgn}(F) - 1/2 I \pi b^2c^2 x + 1/2 I \pi a^2c^2 \operatorname{sgn}(F) - 1/2 I \pi a^2c^2 - 2I x^2e - 2I d)} / (4I \pi b^2c^2 \operatorname{sgn}(F) - 4I \pi b^2c^2 + 8b^2c^2 \log(\operatorname{abs}(F)) - 16I e) - 2I * e^{(-1/2 I \pi b^2c^2 x \operatorname{sgn}(F) + 1/2 I \pi b^2c^2 x - 1/2 I \pi a^2c^2 \operatorname{sgn}(F) + 1/2 I \pi a^2c^2 + 2I x^2e + 2I d)} / (-4I \pi b^2c^2 \operatorname{sgn}(F) + 4I \pi b^2c^2 + 8b^2c^2 \log(\operatorname{abs}(F)) + 16I e) * e^{(b^2c^2 x \log(\operatorname{abs}(F)) + a^2c^2 \log(\operatorname{abs}(F)))} - 1/2 * I * (-2I * e^{(1/2 I \pi b^2c^2 x \operatorname{sgn}(F) - 1/2 I \pi b^2c^2 x + 1/2 I \pi a^2c^2 \operatorname{sgn}(F) - 1/2 I \pi a^2c^2) / (2I \pi b^2c^2 \operatorname{sgn}(F) - 2I \pi b^2c^2 + 4b^2c^2 \log(\operatorname{abs}(F)))} + 2I * e^{(-1/2 I \pi b^2c^2 x \operatorname{sgn}(F) + 1/2 I \pi b^2c^2 x - 1/2 I \pi a^2c^2 \operatorname{sgn}(F) + 1/2 I \pi a^2c^2) / (-2I \pi b^2c^2 \operatorname{sgn}(F) + 2I \pi b^2c^2 + 4b^2c^2 \log(\operatorname{abs}(F))) * e^{(b^2c^2 x \log(\operatorname{abs}(F)) + a^2c^2 \log(\operatorname{abs}(F)))}$

maple [A] time = 0.17, size = 153, normalized size = 1.20

$$\frac{F^{c(bx+a)}}{2bc \ln(F)} - \frac{bc \ln(F) e^{c(bx+a) \ln(F)}}{4e^2 + b^2c^2 \ln(F)^2} + \frac{4e^{c(bx+a) \ln(F)} \tan(ex+d)}{4e^2 + b^2c^2 \ln(F)^2} - \frac{bc \ln(F) e^{c(bx+a) \ln(F)} (\tan^2(ex+d))}{4e^2 + b^2c^2 \ln(F)^2}$$

$$2(1 + \tan^2(ex+d))$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}(F^{(c*(b*x+a))*\sin(e*x+d)^2}, x)$

[Out] $\frac{1}{2} \frac{b}{c} \frac{1}{\ln(F)} F^{(c*(b*x+a))} - \frac{1}{2} \frac{1}{(4*e^2+b^2*c^2*\ln(F)^2)*b*c*\ln(F)*\exp(c*(b*x+a)*\ln(F))+4/(4*e^2+b^2*c^2*\ln(F)^2)*e*\exp(c*(b*x+a)*\ln(F))*\tan(e*x+d)-1/(4*e^2+b^2*c^2*\ln(F)^2)*b*c*\ln(F)*\exp(c*(b*x+a)*\ln(F))*\tan(e*x+d)^2)/(1+\tan(e*x+d)^2)}$

maxima [B] time = 0.41, size = 356, normalized size = 2.78

$$\frac{(F^{ac}b^2c^2 \cos(2d) \log(F)^2 + 2F^{ac}bce \log(F) \sin(2d))F^{bcx} \cos(2ex) + (F^{ac}b^2c^2 \cos(2d) \log(F)^2 - 2F^{ac}bce \log(F) \sin(2d))F^{bcx} \sin(2ex)}{b^2c^2 \log(F)^2 + 4e^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{integrate}(F^{(c*(b*x+a))*\sin(e*x+d)^2}, x, \text{algorithm}="maxima")$

[Out] $-1/4*((F^{(a*c)}*b^2*c^2*\cos(2*d)*\log(F)^2 + 2*F^{(a*c)}*b*c*e*\log(F)*\sin(2*d))*F^{(b*c*x)}*\cos(2*e*x) + (F^{(a*c)}*b^2*c^2*\cos(2*d)*\log(F)^2 - 2*F^{(a*c)}*b*c*e*\log(F)*\sin(2*d))*F^{(b*c*x)}*\cos(2*e*x + 4*d) - (F^{(a*c)}*b^2*c^2*\log(F)^2*\sin(2*d) - 2*F^{(a*c)}*b*c*e*\cos(2*d)*\log(F))*F^{(b*c*x)}*\sin(2*e*x) + (F^{(a*c)}*b^2*c^2*\log(F)^2*\sin(2*d) + 2*F^{(a*c)}*b*c*e*\cos(2*d)*\log(F))*F^{(b*c*x)}*\sin(2*e*x + 4*d) - 2*(F^{(a*c)}*b^2*c^2*\cos(2*d)^2*\log(F)^2 + F^{(a*c)}*b^2*c^2*\log(F)^2*\sin(2*d)^2 + 4*(F^{(a*c)}*\cos(2*d)^2 + F^{(a*c)}*\sin(2*d)^2)*e^2)*F^{(b*c*x)})/(b^3*c^3*\cos(2*d)^2*\log(F)^3 + b^3*c^3*\log(F)^3*\sin(2*d)^2 + 4*(b*c*\cos(2*d)^2*\log(F) + b*c*\log(F)*\sin(2*d)^2)*e^2)$

mupad [B] time = 3.02, size = 95, normalized size = 0.74

$$\frac{F^{ac+bcx} \left(2e^2 + \frac{b^2c^2 \ln(F)^2}{2} - \frac{b^2c^2 \ln(F)^2 \cos(2d+2ex)}{2} - bce \ln(F) \sin(2d+2ex) \right)}{bc \ln(F) (b^2c^2 \ln(F)^2 + 4e^2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}(F^{(c*(a + b*x))*\sin(d + e*x)^2}, x)$

[Out] $(F^{(a*c + b*c*x)}*(2*e^2 + (b^2*c^2*\log(F)^2)/2 - (b^2*c^2*\log(F)^2*\cos(2*d + 2*e*x))/2 - b*c*e*\log(F)*\sin(2*d + 2*e*x)))/(b*c*\log(F)*(4*e^2 + b^2*c^2*\log(F)^2))$

sympy [A] time = 34.89, size = 627, normalized size = 4.90

$$\left\{ \begin{array}{l} \frac{x \sin^2(d+ex)}{2} + \frac{x \cos^2(d+ex)}{2} - \frac{\sin(d+ex) \cos(d+ex)}{2e} \\ \tilde{\omega} e^2 \left(e^{-\frac{2ie}{bc}} \right)^{ac} \left(e^{-\frac{2ie}{bc}} \right)^{bcx} \sin^2(d+ex) + \tilde{\omega} e^2 \left(e^{-\frac{2ie}{bc}} \right)^{ac} \left(e^{-\frac{2ie}{bc}} \right)^{bcx} \sin(d+ex) \cos(d+ex) + \tilde{\omega} e^2 \left(e^{-\frac{2ie}{bc}} \right)^{ac} \left(e^{-\frac{2ie}{bc}} \right)^{bcx} \cos^2(d+ex) \\ \tilde{\omega} e^2 \left(e^{\frac{2ie}{bc}} \right)^{ac} \left(e^{\frac{2ie}{bc}} \right)^{bcx} \sin^2(d+ex) + \tilde{\omega} e^2 \left(e^{\frac{2ie}{bc}} \right)^{ac} \left(e^{\frac{2ie}{bc}} \right)^{bcx} \sin(d+ex) \cos(d+ex) + \tilde{\omega} e^2 \left(e^{\frac{2ie}{bc}} \right)^{ac} \left(e^{\frac{2ie}{bc}} \right)^{bcx} \cos^2(d+ex) \\ F^{ac} \left(\frac{x \sin^2(d+ex)}{2} + \frac{x \cos^2(d+ex)}{2} - \frac{\sin(d+ex) \cos(d+ex)}{2e} \right) \\ \frac{x \sin^2(d+ex)}{2} + \frac{x \cos^2(d+ex)}{2} - \frac{\sin(d+ex) \cos(d+ex)}{2e} \\ \frac{F^{ac} F^{bcx} b^2 c^2 \log(F)^2 \sin^2(d+ex)}{b^3 c^3 \log(F)^3 + 4 b c e^2 \log(F)} - \frac{2 F^{ac} F^{bcx} b c e \log(F) \sin(d+ex) \cos(d+ex)}{b^3 c^3 \log(F)^3 + 4 b c e^2 \log(F)} + \frac{2 F^{ac} F^{bcx} e^2 \sin^2(d+ex)}{b^3 c^3 \log(F)^3 + 4 b c e^2 \log(F)} + \frac{2 F^{ac} F^{bcx} e^2 \cos^2(d+ex)}{b^3 c^3 \log(F)^3 + 4 b c e^2 \log(F)} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.


```
[In] integrate(F**(c*(b*x+a))*sin(e*x+d)**2,x)
```

```
[Out] Piecewise((x*sin(d + e*x)**2/2 + x*cos(d + e*x)**2/2 - sin(d + e*x)*cos(d +
e*x)/(2*e), Eq(F, 1)), (zoo*e**2*exp(-2*I*e/(b*c))**(a*c)*exp(-2*I*e/(b*c)
)**(b*c*x)*sin(d + e*x)**2 + zoo*e**2*exp(-2*I*e/(b*c))**(a*c)*exp(-2*I*e/(
b*c))**(b*c*x)*sin(d + e*x)*cos(d + e*x) + zoo*e**2*exp(-2*I*e/(b*c))**(a*c
)*exp(-2*I*e/(b*c))**(b*c*x)*cos(d + e*x)**2, Eq(F, exp(-2*I*e/(b*c)))), (z
oo*e**2*exp(2*I*e/(b*c))**(a*c)*exp(2*I*e/(b*c))**(b*c*x)*sin(d + e*x)**2 +
zoo*e**2*exp(2*I*e/(b*c))**(a*c)*exp(2*I*e/(b*c))**(b*c*x)*sin(d + e*x)*co
s(d + e*x) + zoo*e**2*exp(2*I*e/(b*c))**(a*c)*exp(2*I*e/(b*c))**(b*c*x)*cos
(d + e*x)**2, Eq(F, exp(2*I*e/(b*c)))), (F**(a*c)*(x*sin(d + e*x)**2/2 + x*
cos(d + e*x)**2/2 - sin(d + e*x)*cos(d + e*x)/(2*e)), Eq(b, 0)), (x*sin(d +
e*x)**2/2 + x*cos(d + e*x)**2/2 - sin(d + e*x)*cos(d + e*x)/(2*e), Eq(c, 0
)), (F**(a*c)*F**(b*c*x)*b**2*c**2*log(F)**2*sin(d + e*x)**2/(b**3*c**3*log
(F)**3 + 4*b*c*e**2*log(F)) - 2*F**(a*c)*F**(b*c*x)*b*c*e*log(F)*sin(d + e*
x)*cos(d + e*x)/(b**3*c**3*log(F)**3 + 4*b*c*e**2*log(F)) + 2*F**(a*c)*F**(
b*c*x)*e**2*sin(d + e*x)**2/(b**3*c**3*log(F)**3 + 4*b*c*e**2*log(F)) + 2*F
**(a*c)*F**(b*c*x)*e**2*cos(d + e*x)**2/(b**3*c**3*log(F)**3 + 4*b*c*e**2*l
og(F)), True))
```

3.4 $\int F^{c(a+bx)} \sin(d+ex) dx$

Optimal. Leaf size=73

$$\frac{bc \log(F) \sin(d+ex) F^{c(a+bx)}}{b^2 c^2 \log^2(F) + e^2} - \frac{e \cos(d+ex) F^{c(a+bx)}}{b^2 c^2 \log^2(F) + e^2}$$

[Out] $-e F^{c(bx+a)} \cos(ex+d) / (e^2 + b^2 c^2 \ln(F)^2) + b c F^{c(bx+a)} \ln(F) \sin(ex+d) / (e^2 + b^2 c^2 \ln(F)^2)$

Rubi [A] time = 0.02, antiderivative size = 73, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} = 0.062$, Rules used = {4432}

$$\frac{bc \log(F) \sin(d+ex) F^{c(a+bx)}}{b^2 c^2 \log^2(F) + e^2} - \frac{e \cos(d+ex) F^{c(a+bx)}}{b^2 c^2 \log^2(F) + e^2}$$

Antiderivative was successfully verified.

[In] Int[F^(c*(a + b*x))*Sin[d + e*x], x]

[Out] $-((e F^{c(a+bx)}) \cos[d+ex]) / (e^2 + b^2 c^2 \log[F]^2) + (b c F^{c(a+bx)}) \log[F] \sin[d+ex] / (e^2 + b^2 c^2 \log[F]^2)$

Rule 4432

Int[(F_)^((c_.)*((a_.) + (b_.)*(x_)))*Sin[(d_.) + (e_.)*(x_)], x_Symbol] :>
Simp[(b*c*Log[F]*F^(c*(a + b*x))*Sin[d + e*x]) / (e^2 + b^2*c^2*Log[F]^2), x] - Simp[(e*F^(c*(a + b*x))*Cos[d + e*x]) / (e^2 + b^2*c^2*Log[F]^2), x] /; FreeQ[{F, a, b, c, d, e}, x] && NeQ[e^2 + b^2*c^2*Log[F]^2, 0]

Rubi steps

$$\int F^{c(a+bx)} \sin(d+ex) dx = -\frac{e F^{c(a+bx)} \cos(d+ex)}{e^2 + b^2 c^2 \log^2(F)} + \frac{bc F^{c(a+bx)} \log(F) \sin(d+ex)}{e^2 + b^2 c^2 \log^2(F)}$$

Mathematica [A] time = 0.12, size = 48, normalized size = 0.66

$$\frac{F^{c(a+bx)}(bc \log(F) \sin(d+ex) - e \cos(d+ex))}{b^2 c^2 \log^2(F) + e^2}$$

Antiderivative was successfully verified.

[In] Integrate[F^(c*(a + b*x))*Sin[d + e*x], x]

[Out] $(F^{c(a+bx)} * (-e \cos[d+ex]) + b c \log[F] \sin[d+ex]) / (e^2 + b^2 c^2 \log[F]^2)$

fricas [A] time = 0.92, size = 49, normalized size = 0.67

$$\frac{(bc \log(F) \sin(ex+d) - e \cos(ex+d)) F^{bcx+ac}}{b^2 c^2 \log(F)^2 + e^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(F^(c*(b*x+a))*sin(e*x+d), x, algorithm="fricas")

[Out] $(b*c*\log(F)*\sin(e*x + d) - e*\cos(e*x + d))*F^{(b*c*x + a*c)}/(b^2*c^2*\log(F)^2 + e^2)$

giac [C] time = 0.21, size = 652, normalized size = 8.93

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(F^(c*(b*x+a))*sin(e*x+d),x, algorithm="giac")`

[Out] $(2*b*c*\log(\text{abs}(F))*\sin(1/2*\pi*b*c*x*\text{sgn}(F) - 1/2*\pi*b*c*x + 1/2*\pi*a*c*\text{sgn}(F) - 1/2*\pi*a*c + x*e + d)/(4*b^2*c^2*\log(\text{abs}(F))^2 + (\pi*b*c*\text{sgn}(F) - \pi*b*c + 2*e)^2) - (\pi*b*c*\text{sgn}(F) - \pi*b*c + 2*e)*\cos(1/2*\pi*b*c*x*\text{sgn}(F) - 1/2*\pi*b*c*x + 1/2*\pi*a*c*\text{sgn}(F) - 1/2*\pi*a*c + x*e + d)/(4*b^2*c^2*\log(\text{abs}(F))^2 + (\pi*b*c*\text{sgn}(F) - \pi*b*c + 2*e)^2)*e^{(b*c*x*\log(\text{abs}(F)) + a*c*\log(\text{abs}(F)))} - (2*b*c*\log(\text{abs}(F))*\sin(1/2*\pi*b*c*x*\text{sgn}(F) - 1/2*\pi*b*c*x + 1/2*\pi*a*c*\text{sgn}(F) - 1/2*\pi*a*c - x*e - d)/(4*b^2*c^2*\log(\text{abs}(F))^2 + (\pi*b*c*\text{sgn}(F) - \pi*b*c - 2*e)^2) - (\pi*b*c*\text{sgn}(F) - \pi*b*c - 2*e)*\cos(1/2*\pi*b*c*x*\text{sgn}(F) - 1/2*\pi*b*c*x + 1/2*\pi*a*c*\text{sgn}(F) - 1/2*\pi*a*c - x*e - d)/(4*b^2*c^2*\log(\text{abs}(F))^2 + (\pi*b*c*\text{sgn}(F) - \pi*b*c - 2*e)^2)*e^{(b*c*x*\log(\text{abs}(F)) + a*c*\log(\text{abs}(F)))} + 1/2*(2*I*e^{(1/2*I*\pi*b*c*x*\text{sgn}(F) - 1/2*I*\pi*b*c*x + 1/2*I*\pi*a*c*\text{sgn}(F) - 1/2*I*\pi*a*c + I*x*e + I*d)/(2*I*\pi*b*c*\text{sgn}(F) - 2*I*\pi*b*c + 4*b*c*\log(\text{abs}(F)) + 4*I*e)} + 2*I*e^{(-1/2*I*\pi*b*c*x*\text{sgn}(F) + 1/2*I*\pi*b*c*x - 1/2*I*\pi*a*c*\text{sgn}(F) + 1/2*I*\pi*a*c - I*x*e - I*d)/(-2*I*\pi*b*c*\text{sgn}(F) + 2*I*\pi*b*c + 4*b*c*\log(\text{abs}(F)) - 4*I*e)})*e^{(b*c*x*\log(\text{abs}(F)) + a*c*\log(\text{abs}(F)))} + 1/2*(-2*I*e^{(1/2*I*\pi*b*c*x*\text{sgn}(F) - 1/2*I*\pi*b*c*x + 1/2*I*\pi*a*c*\text{sgn}(F) - 1/2*I*\pi*a*c - I*x*e - I*d)/(2*I*\pi*b*c*\text{sgn}(F) - 2*I*\pi*b*c + 4*b*c*\log(\text{abs}(F)) - 4*I*e)} - 2*I*e^{(-1/2*I*\pi*b*c*x*\text{sgn}(F) + 1/2*I*\pi*b*c*x - 1/2*I*\pi*a*c*\text{sgn}(F) + 1/2*I*\pi*a*c + I*x*e + I*d)/(-2*I*\pi*b*c*\text{sgn}(F) + 2*I*\pi*b*c + 4*b*c*\log(\text{abs}(F)) + 4*I*e)})*e^{(b*c*x*\log(\text{abs}(F)) + a*c*\log(\text{abs}(F)))}$

maple [A] time = 0.04, size = 130, normalized size = 1.78

$$\frac{e^{c(bx+a)\ln(F)}\left(\tan^2\left(\frac{d}{2} + \frac{ex}{2}\right)\right)}{e^2 + b^2c^2\ln(F)^2} - \frac{e^{c(bx+a)\ln(F)}}{e^2 + b^2c^2\ln(F)^2} + \frac{2bc\ln(F)e^{c(bx+a)\ln(F)}\tan\left(\frac{d}{2} + \frac{ex}{2}\right)}{e^2 + b^2c^2\ln(F)^2}$$

$$1 + \tan^2\left(\frac{d}{2} + \frac{ex}{2}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(F^(c*(b*x+a))*sin(e*x+d),x)`

[Out] $(1/(e^2 + b^2*c^2*\ln(F)^2))*e*\exp(c*(b*x+a)*\ln(F))*\tan(1/2*d + 1/2*e*x)^2 - 1/(e^2 + b^2*c^2*\ln(F)^2)*e*\exp(c*(b*x+a)*\ln(F)) + 2*b*c*\ln(F)/(e^2 + b^2*c^2*\ln(F)^2)*\exp(c*(b*x+a)*\ln(F))*\tan(1/2*d + 1/2*e*x)/(1 + \tan(1/2*d + 1/2*e*x)^2)$

maxima [B] time = 1.13, size = 194, normalized size = 2.66

$$\frac{(F^{ac}bc\log(F)\sin(d) + F^{ac}e\cos(d))F^{bcx}\cos(ex + 2d) - (F^{ac}bc\log(F)\sin(d) - F^{ac}e\cos(d))F^{bcx}\cos(ex) - (F^{ac}bc\log(F)\sin(d) + F^{ac}e\cos(d))F^{bcx}\cos(ex) - (F^{ac}bc\log(F)\sin(d) - F^{ac}e\cos(d))F^{bcx}\cos(ex)}{2(b^2c^2\cos(d)^2\log(F)^2 + b^2c^2\log(F)^2\sin(d)^2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(F^(c*(b*x+a))*sin(e*x+d),x, algorithm="maxima")`

[Out] $-1/2*((F^{(a*c)}*b*c*\log(F)*\sin(d) + F^{(a*c)}*e*\cos(d))*F^{(b*c*x)}*\cos(e*x + 2*d) - (F^{(a*c)}*b*c*\log(F)*\sin(d) - F^{(a*c)}*e*\cos(d))*F^{(b*c*x)}*\cos(e*x) - (F^{(a*c)}*b*c*\cos(d)*\log(F) - F^{(a*c)}*e*\sin(d))*F^{(b*c*x)}*\sin(e*x + 2*d) - (F^{(a*c)}*b*c*\cos(d)*\log(F) + F^{(a*c)}*e*\sin(d))*F^{(b*c*x)}*\sin(e*x))/(b^2*c^2*\cos(d)^2*\log(F)^2 + b^2*c^2*\log(F)^2*\sin(d)^2 + (\cos(d)^2 + \sin(d)^2)*e^2)$

mupad [B] time = 2.40, size = 50, normalized size = 0.68

$$\frac{F^{ac+bcx} (e \cos(d+ex) - bc \sin(d+ex) \ln(F))}{b^2 c^2 \ln(F)^2 + e^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(F^(c*(a + b*x))*sin(d + e*x),x)`

[Out] `-(F^(a*c + b*c*x)*(e*cos(d + e*x) - b*c*sin(d + e*x)*log(F)))/(e^2 + b^2*c^2*log(F)^2)`

sympy [A] time = 7.84, size = 326, normalized size = 4.47

$$\left\{ \begin{array}{ll} \frac{(-1)^{ac}(-1)^{\frac{ex}{\pi}} x \sin(d+ex)}{2} + \frac{(-1)^{ac}(-1)^{\frac{ex}{\pi}} ix \cos(d+ex)}{2} - \frac{(-1)^{ac}(-1)^{\frac{ex}{\pi}} \cos(d+ex)}{2e} & \text{for } F = -1 \wedge b = \frac{e}{\pi c} \\ x \sin(d) & \text{for } F = 1 \wedge e = 0 \\ \tilde{\omega} e \left(e^{-\frac{ie}{bc}} \right)^{ac} \left(e^{-\frac{ie}{bc}} \right)^{bcx} \sin(d+ex) + \tilde{\omega} e \left(e^{-\frac{ie}{bc}} \right)^{ac} \left(e^{-\frac{ie}{bc}} \right)^{bcx} \cos(d+ex) & \text{for } F = e^{-\frac{ie}{bc}} \\ \tilde{\omega} e \left(e^{\frac{ie}{bc}} \right)^{ac} \left(e^{\frac{ie}{bc}} \right)^{bcx} \sin(d+ex) + \tilde{\omega} e \left(e^{\frac{ie}{bc}} \right)^{ac} \left(e^{\frac{ie}{bc}} \right)^{bcx} \cos(d+ex) & \text{for } F = e^{\frac{ie}{bc}} \\ \frac{F^{ac} F^{bcx} bc \log(F) \sin(d+ex)}{b^2 c^2 \log(F)^2 + e^2} - \frac{F^{ac} F^{bcx} e \cos(d+ex)}{b^2 c^2 \log(F)^2 + e^2} & \text{otherwise} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(F**(c*(b*x+a))*sin(e*x+d),x)`

[Out] `Piecewise((((-1)**(a*c))*(-1)**(e*x/pi)*x*sin(d + e*x)/2 + (-1)**(a*c))*(-1)**(e*x/pi)*I*x*cos(d + e*x)/2 - (-1)**(a*c))*(-1)**(e*x/pi)*cos(d + e*x)/(2*e), Eq(F, -1) & Eq(b, e/(pi*c))), (x*sin(d), Eq(F, 1) & Eq(e, 0)), (zoo*e*exp(-I*e/(b*c))** (a*c)*exp(-I*e/(b*c))** (b*c*x)*sin(d + e*x) + zoo*e*exp(-I*e/(b*c))** (a*c)*exp(-I*e/(b*c))** (b*c*x)*cos(d + e*x), Eq(F, exp(-I*e/(b*c)))), (zoo*e*exp(I*e/(b*c))** (a*c)*exp(I*e/(b*c))** (b*c*x)*sin(d + e*x) + zoo*e*exp(I*e/(b*c))** (a*c)*exp(I*e/(b*c))** (b*c*x)*cos(d + e*x), Eq(F, exp(I*e/(b*c))))), (F**(a*c)*F**(b*c*x)*b*c*log(F)*sin(d + e*x)/(b**2*c**2*log(F)**2 + e**2) - F**(a*c)*F**(b*c*x)*e*cos(d + e*x)/(b**2*c**2*log(F)**2 + e**2), True))`

3.5 $\int F^{c(a+bx)} \csc(d+ex) dx$

Optimal. Leaf size=81

$$\frac{2e^{i(d+ex)} F^{c(a+bx)} {}_2F_1\left(1, \frac{e-ibc \log(F)}{2e}; \frac{1}{2} \left(3 - \frac{ibc \log(F)}{e}\right); e^{2i(d+ex)}\right)}{e - ibc \log(F)}$$

[Out] $-2*\exp(I*(e*x+d))*F^{(c*(b*x+a))*\text{hypergeom}([1, 1/2*(e-I*b*c*\ln(F))/e], [3/2-1/2*I*b*c*\ln(F)/e], \exp(2*I*(e*x+d)))/(e-I*b*c*\ln(F))$

Rubi [A] time = 0.02, antiderivative size = 81, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} = 0.062$, Rules used = {4453}

$$\frac{2e^{i(d+ex)} F^{c(a+bx)} {}_2F_1\left(1, \frac{e-ibc \log(F)}{2e}; \frac{1}{2} \left(3 - \frac{ibc \log(F)}{e}\right); e^{2i(d+ex)}\right)}{e - ibc \log(F)}$$

Antiderivative was successfully verified.

[In] Int[F^(c*(a + b*x))*Csc[d + e*x], x]

[Out] $(-2*E^{(I*(d + e*x))*F^{(c*(a + b*x))*\text{Hypergeometric2F1}[1, (e - I*b*c*\text{Log}[F])/(2*e), (3 - (I*b*c*\text{Log}[F])/e)/2, E^{((2*I)*(d + e*x))}]/(e - I*b*c*\text{Log}[F])$

Rule 4453

Int[Csc[(d_.) + (e_.)*(x_.)]^(n_.)*F_((c_.)*((a_.) + (b_.)*(x_.))), x_Symbol] :> Simp[(-2*I)^n*E^(I*n*(d + e*x))*F^(c*(a + b*x))/(I*e*n + b*c*Log[F])*Hypergeometric2F1[n, n/2 - (I*b*c*Log[F])/(2*e), 1 + n/2 - (I*b*c*Log[F])/(2*e), E^(2*I*(d + e*x))], x] /; FreeQ[{F, a, b, c, d, e}, x] && IntegerQ[n]

Rubi steps

$$\int F^{c(a+bx)} \csc(d+ex) dx = -\frac{2e^{i(d+ex)} F^{c(a+bx)} {}_2F_1\left(1, \frac{e-ibc \log(F)}{2e}; \frac{1}{2} \left(3 - \frac{ibc \log(F)}{e}\right); e^{2i(d+ex)}\right)}{e - ibc \log(F)}$$

Mathematica [A] time = 1.75, size = 114, normalized size = 1.41

$$\frac{iF^{c(a+bx)} \left({}_2F_1\left(1, -\frac{ibc \log(F)}{e}; 1 - \frac{ibc \log(F)}{e}; -\cos(d+ex) - i \sin(d+ex)\right) - {}_2F_1\left(1, -\frac{ibc \log(F)}{e}; 1 - \frac{ibc \log(F)}{e}; \cos(d+ex)\right) \right)}{bc \log(F)}$$

Antiderivative was successfully verified.

[In] Integrate[F^(c*(a + b*x))*Csc[d + e*x], x]

[Out] $(I*F^{(c*(a + b*x))*(\text{Hypergeometric2F1}[1, ((-I)*b*c*\text{Log}[F])/e, 1 - (I*b*c*\text{Log}[F])/e, -\text{Cos}[d + e*x] - I*\text{Sin}[d + e*x]] - \text{Hypergeometric2F1}[1, ((-I)*b*c*\text{Log}[F])/e, 1 - (I*b*c*\text{Log}[F])/e, \text{Cos}[d + e*x] + I*\text{Sin}[d + e*x]])/(b*c*\text{Log}[F])$

fricas [F] time = 0.85, size = 0, normalized size = 0.00

$$\text{integral}\left(F^{bcx+ac} \csc(ex+d), x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(F^(c*(b*x+a))*csc(e*x+d),x, algorithm="fricas")

[Out] integral(F^(b*c*x + a*c)*csc(e*x + d), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int F^{(bx+a)c} \csc(ex + d) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(F^(c*(b*x+a))*csc(e*x+d),x, algorithm="giac")

[Out] integrate(F^((b*x + a)*c)*csc(e*x + d), x)

maple [F] time = 0.09, size = 0, normalized size = 0.00

$$\int F^{c(bx+a)} \csc(ex + d) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(F^(c*(b*x+a))*csc(e*x+d),x)

[Out] int(F^(c*(b*x+a))*csc(e*x+d),x)

maxima [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(F^(c*(b*x+a))*csc(e*x+d),x, algorithm="maxima")

[Out] Timed out

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{F^{c(a+bx)}}{\sin(d + ex)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(F^(c*(a + b*x))/sin(d + e*x),x)

[Out] int(F^(c*(a + b*x))/sin(d + e*x), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int F^{c(a+bx)} \csc(d + ex) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(F**(c*(b*x+a))*csc(e*x+d),x)

[Out] Integral(F**(c*(a + b*x))*csc(d + e*x), x)

3.6 $\int F^{c(a+bx)} \csc^2(d+ex) dx$

Optimal. Leaf size=78

$$-\frac{4e^{2i(d+ex)}F^{c(a+bx)}{}_2F_1\left(2, 1 - \frac{ibc \log(F)}{2e}; 2 - \frac{ibc \log(F)}{2e}; e^{2i(d+ex)}\right)}{bc \log(F) + 2ie}$$

[Out] $-4*\exp(2*I*(e*x+d))*F^{(c*(b*x+a))*\text{hypergeom}([2, 1-1/2*I*b*c*\ln(F)/e], [2-1/2*I*b*c*\ln(F)/e], \exp(2*I*(e*x+d)))/(2*I*e+b*c*\ln(F))$

Rubi [A] time = 0.03, antiderivative size = 78, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.056$, Rules used = {4453}

$$-\frac{4e^{2i(d+ex)}F^{c(a+bx)}{}_2F_1\left(2, 1 - \frac{ibc \log(F)}{2e}; 2 - \frac{ibc \log(F)}{2e}; e^{2i(d+ex)}\right)}{bc \log(F) + 2ie}$$

Antiderivative was successfully verified.

[In] Int[F^(c*(a + b*x))*Csc[d + e*x]^2,x]

[Out] $(-4*E^{((2*I)*(d + e*x))*F^{(c*(a + b*x))*\text{Hypergeometric2F1}[2, 1 - ((I/2)*b*c*\text{Log}[F])/e, 2 - ((I/2)*b*c*\text{Log}[F])/e, E^{((2*I)*(d + e*x))}]/((2*I)*e + b*c*\text{Log}[F])$

Rule 4453

Int[Csc[(d_.) + (e_.)*(x_)]^(n_.)*(F_)^(c_.*(a_.) + (b_.)*(x_)), x_Symbol] :> Simp[(-2*I)^n*E^(I*n*(d + e*x))*F^(c*(a + b*x))/(I*e*n + b*c*Log[F])*Hypergeometric2F1[n, n/2 - (I*b*c*Log[F])/(2*e), 1 + n/2 - (I*b*c*Log[F])/(2*e), E^(2*I*(d + e*x))], x] /; FreeQ[{F, a, b, c, d, e}, x] && IntegerQ[n]

Rubi steps

$$\int F^{c(a+bx)} \csc^2(d+ex) dx = -\frac{4e^{2i(d+ex)}F^{c(a+bx)}{}_2F_1\left(2, 1 - \frac{ibc \log(F)}{2e}; 2 - \frac{ibc \log(F)}{2e}; e^{2i(d+ex)}\right)}{2ie + bc \log(F)}$$

Mathematica [A] time = 1.48, size = 101, normalized size = 1.29

$$\frac{2iF^{c(a+bx)}\left((-1 + e^{2id}){}_2F_1\left(1, -\frac{ibc \log(F)}{2e}; 1 - \frac{ibc \log(F)}{2e}; e^{2i(d+ex)}\right) + \sin(d) \csc(d+ex)(\cos(ex) - i \sin(ex))\right)}{(-1 + e^{2id})e}$$

Antiderivative was successfully verified.

[In] Integrate[F^(c*(a + b*x))*Csc[d + e*x]^2,x]

[Out] $((-2*I)*F^{(c*(a + b*x))*((-1 + E^{((2*I)*d))*\text{Hypergeometric2F1}[1, ((-1/2*I)*b*c*\text{Log}[F])/e, 1 - ((I/2)*b*c*\text{Log}[F])/e, E^{((2*I)*(d + e*x))}] + \text{Csc}[d + e*x]*\text{Sin}[d]*(\text{Cos}[e*x] - I*\text{Sin}[e*x]))/(e*(-1 + E^{((2*I)*d))}$

fricas [F] time = 0.95, size = 0, normalized size = 0.00

$$\text{integral}\left(F^{bcx+ac} \csc(ex+d)^2, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(F^(c*(b*x+a))*csc(e*x+d)^2,x, algorithm="fricas")

[Out] integral(F^(b*c*x + a*c)*csc(e*x + d)^2, x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int F^{(bx+a)c} \csc(ex+d)^2 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(F^(c*(b*x+a))*csc(e*x+d)^2,x, algorithm="giac")

[Out] integrate(F^((b*x + a)*c)*csc(e*x + d)^2, x)

maple [F] time = 0.16, size = 0, normalized size = 0.00

$$\int F^{c(bx+a)} (\csc^2(ex+d)) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(F^(c*(b*x+a))*csc(e*x+d)^2,x)

[Out] int(F^(c*(b*x+a))*csc(e*x+d)^2,x)

maxima [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(F^(c*(b*x+a))*csc(e*x+d)^2,x, algorithm="maxima")

[Out] Timed out

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{F^{c(a+bx)}}{\sin(d+ex)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(F^(c*(a + b*x))/sin(d + e*x)^2,x)

[Out] int(F^(c*(a + b*x))/sin(d + e*x)^2, x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int F^{c(a+bx)} \csc^2(d+ex) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(F**(c*(b*x+a))*csc(e*x+d)**2,x)

[Out] Integral(F**(c*(a + b*x))*csc(d + e*x)**2, x)

3.7 $\int F^{c(a+bx)} \csc^3(d+ex) dx$

Optimal. Leaf size=137

$$\frac{e^{i(d+ex)} F^{c(a+bx)} (e + ibc \log(F)) {}_2F_1\left(1, \frac{e-ibc \log(F)}{2e}; \frac{1}{2} \left(3 - \frac{ibc \log(F)}{e}\right); e^{2i(d+ex)}\right)}{e^2} - \frac{bc \log(F) \csc(d+ex) F^{c(a+bx)} \cot(d+ex)}{2e^2}$$

[Out] $-1/2 * F^{(c*(b*x+a))} * \cot(e*x+d) * \csc(e*x+d) / e - 1/2 * b*c * F^{(c*(b*x+a))} * \csc(e*x+d) * \ln(F) / e^2 - \exp(I*(e*x+d)) * F^{(c*(b*x+a))} * \text{hypergeom}([1, 1/2*(e-I*b*c*\ln(F)) / e], [3/2-1/2*I*b*c*\ln(F) / e], \exp(2*I*(e*x+d))) * (e+I*b*c*\ln(F)) / e^2$

Rubi [A] time = 0.05, antiderivative size = 137, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {4449, 4453}

$$\frac{e^{i(d+ex)} F^{c(a+bx)} (e + ibc \log(F)) {}_2F_1\left(1, \frac{e-ibc \log(F)}{2e}; \frac{1}{2} \left(3 - \frac{ibc \log(F)}{e}\right); e^{2i(d+ex)}\right)}{e^2} - \frac{bc \log(F) \csc(d+ex) F^{c(a+bx)} \cot(d+ex)}{2e^2}$$

Antiderivative was successfully verified.

[In] Int[F^(c*(a + b*x))*Csc[d + e*x]^3,x]

[Out] $-(F^{(c*(a + b*x))} * \cot[d + e*x] * \csc[d + e*x]) / (2*e) - (b*c * F^{(c*(a + b*x))} * \csc[d + e*x] * \log[F]) / (2*e^2) - (E^{(I*(d + e*x))} * F^{(c*(a + b*x))} * \text{Hypergeometric2F1}[1, (e - I*b*c*\log[F]) / (2*e), (3 - (I*b*c*\log[F]) / e) / 2, E^{((2*I)*(d + e*x))}] * (e + I*b*c*\log[F])) / e^2$

Rule 4449

Int[Csc[(d_) + (e_)*(x_)]^(n_)*(F_)^(((c_)*((a_) + (b_)*(x_))), x_Symbol] :> -Simp[(b*c*Log[F]*F^(c*(a + b*x))*Csc[d + e*x]^(n - 2))/(e^2*(n - 1)*(n - 2)), x] + (Dist[(e^2*(n - 2)^2 + b^2*c^2*Log[F]^2)/(e^2*(n - 1)*(n - 2)), Int[F^(c*(a + b*x))*Csc[d + e*x]^(n - 2), x], x] - Simp[(F^(c*(a + b*x))*Csc[d + e*x]^(n - 1)*Cos[d + e*x])/(e*(n - 1)), x]) /; FreeQ[{F, a, b, c, d, e}, x] && NeQ[b^2*c^2*Log[F]^2 + e^2*(n - 2)^2, 0] && GtQ[n, 1] && NeQ[n, 2]

Rule 4453

Int[Csc[(d_) + (e_)*(x_)]^(n_)*(F_)^(((c_)*((a_) + (b_)*(x_))), x_Symbol] :> Simp[(-2*I)^n * E^(I*n*(d + e*x)) * (F^(c*(a + b*x)) / (I*e*n + b*c*Log[F])) * Hypergeometric2F1[n, n/2 - (I*b*c*Log[F]) / (2*e), 1 + n/2 - (I*b*c*Log[F]) / (2*e), E^(2*I*(d + e*x))], x] /; FreeQ[{F, a, b, c, d, e}, x] && IntegerQ[n]

Rubi steps

$$\begin{aligned} \int F^{c(a+bx)} \csc^3(d+ex) dx &= -\frac{F^{c(a+bx)} \cot(d+ex) \csc(d+ex)}{2e} - \frac{bc F^{c(a+bx)} \csc(d+ex) \log(F)}{2e^2} + \frac{1}{2} \left(1 + \frac{b^2 c^2 \log^2(F)}{e^2}\right) e^{i(d+ex)} F^{c(a+bx)} \\ &= -\frac{F^{c(a+bx)} \cot(d+ex) \csc(d+ex)}{2e} - \frac{bc F^{c(a+bx)} \csc(d+ex) \log(F)}{2e^2} - \frac{e^{i(d+ex)} F^{c(a+bx)}}{2e^2} \end{aligned}$$

Mathematica [B] time = 7.67, size = 334, normalized size = 2.44

$$F^{c(a+bx)} \left(-\frac{4i(b^2 c^2 \log^2(F) + e^2) \left(1 + (i \sin(d) + \cos(d) - 1) {}_2F_1\left(1, -\frac{ibc \log(F)}{e}; 1 - \frac{ibc \log(F)}{e}; \cos(d+ex) + i \sin(d+ex)\right)\right)}{bc \log(F) (i \sin(d) + \cos(d) - 1)} - \frac{4i(b^2 c^2 \log^2(F) + e^2) (1 - i \sin(d))}{2e^2} \right)$$

Antiderivative was successfully verified.

[In] Integrate[F^(c*(a + b*x))*Csc[d + e*x]^3,x]

[Out] (F^(c*(a + b*x))*(-(e*Csc[(d + e*x)/2]^2) - 4*b*c*Csc[d]*Log[F] + Csc[d]*((4*e^2)/(b*c*Log[F]) + 4*b*c*Log[F]) + e*Sec[(d + e*x)/2]^2 - ((4*I)*(e^2 + b^2*c^2*Log[F]^2)*(1 + Hypergeometric2F1[1, ((-I)*b*c*Log[F])/e, 1 - (I*b*c*Log[F])/e, Cos[d + e*x] + I*Sin[d + e*x]]*(-1 + Cos[d] + I*Sin[d])))/(b*c*Log[F]*(-1 + Cos[d] + I*Sin[d])) - ((4*I)*(e^2 + b^2*c^2*Log[F]^2)*(1 - Hypergeometric2F1[1, ((-I)*b*c*Log[F])/e, 1 - (I*b*c*Log[F])/e, -Cos[d + e*x] - I*Sin[d + e*x]]*(1 + Cos[d] + I*Sin[d])))/(b*c*Log[F]*(1 + Cos[d] + I*Sin[d])) + 2*b*c*Csc[d/2]*Csc[(d + e*x)/2]*Log[F]*Sin[(e*x)/2] - 2*b*c*Log[F]*Sec[d/2]*Sec[(d + e*x)/2]*Sin[(e*x)/2))/(8*e^2)

fricas [F] time = 0.64, size = 0, normalized size = 0.00

$$\text{integral}\left(F^{bcx+ac} \csc(ex+d)^3, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(F^(c*(b*x+a))*csc(e*x+d)^3,x, algorithm="fricas")

[Out] integral(F^(b*c*x + a*c)*csc(e*x + d)^3, x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int F^{(bx+a)c} \csc(ex+d)^3 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(F^(c*(b*x+a))*csc(e*x+d)^3,x, algorithm="giac")

[Out] integrate(F^((b*x + a)*c)*csc(e*x + d)^3, x)

maple [F] time = 0.22, size = 0, normalized size = 0.00

$$\int F^{c(bx+a)} (\csc^3(ex+d)) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(F^(c*(b*x+a))*csc(e*x+d)^3,x)

[Out] int(F^(c*(b*x+a))*csc(e*x+d)^3,x)

maxima [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(F^(c*(b*x+a))*csc(e*x+d)^3,x, algorithm="maxima")

[Out] Timed out

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{F^{c(a+bx)}}{\sin(d+ex)^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(F^(c*(a + b*x))/sin(d + e*x)^3,x)

[Out] `int(F^(c*(a + b*x))/sin(d + e*x)^3, x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int F^{c(a+bx)} \csc^3(d+ex) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(F**(c*(b*x+a))*csc(e*x+d)**3,x)`

[Out] `Integral(F**(c*(a + b*x))*csc(d + e*x)**3, x)`

3.8 $\int F^{c(a+bx)} \csc^4(d+ex) dx$

Optimal. Leaf size=141

$$\frac{2e^{2i(d+ex)} F^{c(a+bx)} (-bc \log(F) + 2ie) {}_2F_1\left(2, 1 - \frac{ibc \log(F)}{2e}; 2 - \frac{ibc \log(F)}{2e}; e^{2i(d+ex)}\right)}{3e^2} - \frac{bc \log(F) \csc^2(d+ex) F^{c(a+bx)}}{6e^2} - \cot(d+ex) F^{c(a+bx)}$$

[Out] $-1/3 * F^{(c*(b*x+a))} * \cot(e*x+d) * \csc(e*x+d)^2 / e - 1/6 * b*c * F^{(c*(b*x+a))} * \csc(e*x+d)^2 * \ln(F) / e^2 + 2/3 * \exp(2*I*(e*x+d)) * F^{(c*(b*x+a))} * \text{hypergeom}([2, 1-1/2*I*b*c*\ln(F)/e], [2-1/2*I*b*c*\ln(F)/e], \exp(2*I*(e*x+d))) * (2*I*e-b*c*\ln(F)) / e^2$

Rubi [A] time = 0.05, antiderivative size = 141, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {4449, 4453}

$$\frac{2e^{2i(d+ex)} F^{c(a+bx)} (-bc \log(F) + 2ie) {}_2F_1\left(2, 1 - \frac{ibc \log(F)}{2e}; 2 - \frac{ibc \log(F)}{2e}; e^{2i(d+ex)}\right)}{3e^2} - \frac{bc \log(F) \csc^2(d+ex) F^{c(a+bx)}}{6e^2} - \cot(d+ex) F^{c(a+bx)}$$

Antiderivative was successfully verified.

[In] Int[F^(c*(a + b*x))*Csc[d + e*x]^4, x]

[Out] $-(F^{(c*(a + b*x))} * \cot[d + e*x] * \csc[d + e*x]^2) / (3*e) - (b*c * F^{(c*(a + b*x))} * \csc[d + e*x]^2 * \log[F]) / (6*e^2) + (2 * E^{((2*I)*(d + e*x))} * F^{(c*(a + b*x))} * \text{Hypergeometric2F1}[2, 1 - ((I/2)*b*c*\log[F])/e, 2 - ((I/2)*b*c*\log[F])/e, E^{((2*I)*(d + e*x))} * ((2*I)*e - b*c*\log[F])]) / (3*e^2)$

Rule 4449

Int[Csc[(d_.) + (e_.)*(x_.)]^(n_.)*(F_)^(((c_.)*((a_.) + (b_.)*(x_.))), x_Symbol] :> -Simp[(b*c*Log[F]*F^(c*(a + b*x))*Csc[d + e*x]^(n - 2))/(e^2*(n - 1)*(n - 2)), x] + (Dist[(e^2*(n - 2)^2 + b^2*c^2*Log[F]^2)/(e^2*(n - 1)*(n - 2)), Int[F^(c*(a + b*x))*Csc[d + e*x]^(n - 2), x], x] - Simp[(F^(c*(a + b*x))*Csc[d + e*x]^(n - 1)*Cos[d + e*x])/(e*(n - 1)), x]) /; FreeQ[{F, a, b, c, d, e}, x] && NeQ[b^2*c^2*Log[F]^2 + e^2*(n - 2)^2, 0] && GtQ[n, 1] && NeQ[n, 2]

Rule 4453

Int[Csc[(d_.) + (e_.)*(x_.)]^(n_.)*(F_)^(((c_.)*((a_.) + (b_.)*(x_.))), x_Symbol] :> Simp[(-2*I)^n * E^(I*n*(d + e*x)) * (F^(c*(a + b*x)) / (I*e*n + b*c*Log[F])) * Hypergeometric2F1[n, n/2 - (I*b*c*Log[F])/(2*e), 1 + n/2 - (I*b*c*Log[F])/(2*e), E^(2*I*(d + e*x))], x] /; FreeQ[{F, a, b, c, d, e}, x] && IntegerQ[n]

Rubi steps

$$\begin{aligned} \int F^{c(a+bx)} \csc^4(d+ex) dx &= -\frac{F^{c(a+bx)} \cot(d+ex) \csc^2(d+ex)}{3e} - \frac{bc F^{c(a+bx)} \csc^2(d+ex) \log(F)}{6e^2} + \frac{1}{6} \left(4 + \frac{b^2 c^2 \log^2(F)}{e^2} \right) \\ &= -\frac{F^{c(a+bx)} \cot(d+ex) \csc^2(d+ex)}{3e} - \frac{bc F^{c(a+bx)} \csc^2(d+ex) \log(F)}{6e^2} + \frac{2e^{2i(d+ex)} F^{c(a+bx)}}{6e^2} \end{aligned}$$

Mathematica [A] time = 2.96, size = 173, normalized size = 1.23

$$F^{c(a+bx)} \left(-\frac{2i(b^2 c^2 \log^2(F) + 4e^2) \left(1 + (-1 + e^{2id}) {}_2F_1\left(1, -\frac{ibc \log(F)}{2e}; 1 - \frac{ibc \log(F)}{2e}; e^{2i(d+ex)}\right)\right)}{-1 + e^{2id}} + \csc(d) \sin(ex) \csc(d+ex) (b^2 c^2 \log^2(F) + 4e^2) \right) / 6e^3$$

Antiderivative was successfully verified.

[In] Integrate[F^(c*(a + b*x))*Csc[d + e*x]^4,x]

[Out] (F^(c*(a + b*x))*(-(e*Csc[d + e*x]^2*(2*e*Cot[d] + b*c*Log[F])) - ((2*I)*(1 + (-1 + E^((2*I)*d))*Hypergeometric2F1[1, ((-1/2*I)*b*c*Log[F])/e, 1 - ((I/2)*b*c*Log[F])/e, E^((2*I)*(d + e*x))]))*(4*e^2 + b^2*c^2*Log[F]^2))/(-1 + E^((2*I)*d)) + 2*e^2*Csc[d]*Csc[d + e*x]^3*Sin[e*x] + Csc[d]*Csc[d + e*x]*(4*e^2 + b^2*c^2*Log[F]^2)*Sin[e*x]))/(6*e^3)

fricas [F] time = 3.50, size = 0, normalized size = 0.00

$$\text{integral}\left(F^{bcx+ac} \csc(ex+d)^4, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(F^(c*(b*x+a))*csc(e*x+d)^4,x, algorithm="fricas")

[Out] integral(F^(b*c*x + a*c)*csc(e*x + d)^4, x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int F^{(bx+a)c} \csc(ex+d)^4 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(F^(c*(b*x+a))*csc(e*x+d)^4,x, algorithm="giac")

[Out] integrate(F^((b*x + a)*c)*csc(e*x + d)^4, x)

maple [F] time = 0.24, size = 0, normalized size = 0.00

$$\int F^{c(bx+a)} (\csc^4(ex+d)) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(F^(c*(b*x+a))*csc(e*x+d)^4,x)

[Out] int(F^(c*(b*x+a))*csc(e*x+d)^4,x)

maxima [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(F^(c*(b*x+a))*csc(e*x+d)^4,x, algorithm="maxima")

[Out] Timed out

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{F^{c(a+bx)}}{\sin(d+ex)^4} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(F^(c*(a + b*x))/sin(d + e*x)^4,x)

[Out] int(F^(c*(a + b*x))/sin(d + e*x)^4, x)

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(F**(c*(b*x+a))*csc(e*x+d)**4,x)
```

```
[Out] Timed out
```

3.9 $\int e^x \sin^4(x) dx$

Optimal. Leaf size=54

$$\frac{24e^x}{85} + \frac{1}{17}e^x \sin^4(x) + \frac{12}{85}e^x \sin^2(x) - \frac{4}{17}e^x \sin^3(x) \cos(x) - \frac{24}{85}e^x \sin(x) \cos(x)$$

[Out] 24/85*exp(x)-24/85*exp(x)*cos(x)*sin(x)+12/85*exp(x)*sin(x)^2-4/17*exp(x)*cos(x)*sin(x)^3+1/17*exp(x)*sin(x)^4

Rubi [A] time = 0.03, antiderivative size = 54, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 8, $\frac{\text{number of rules}}{\text{integrand size}} = 0.250$, Rules used = {4434, 2194}

$$\frac{24e^x}{85} + \frac{1}{17}e^x \sin^4(x) + \frac{12}{85}e^x \sin^2(x) - \frac{4}{17}e^x \sin^3(x) \cos(x) - \frac{24}{85}e^x \sin(x) \cos(x)$$

Antiderivative was successfully verified.

[In] Int[E^x*Sin[x]^4,x]

[Out] (24*E^x)/85 - (24*E^x*Cos[x]*Sin[x])/85 + (12*E^x*Sin[x]^2)/85 - (4*E^x*Cos[x]*Sin[x]^3)/17 + (E^x*Sin[x]^4)/17

Rule 2194

Int[((F_)^((c_.)*((a_.) + (b_.)*(x_))))^(n_.), x_Symbol] :> Simp[(F^(c*(a + b*x)))^n/(b*c*n*Log[F]), x] /; FreeQ[{F, a, b, c, n}, x]

Rule 4434

Int[(F_)^((c_.)*((a_.) + (b_.)*(x_)))*Sin[(d_.) + (e_.)*(x_)]^(n_), x_Symbol] :> Simp[(b*c*Log[F]*F^(c*(a + b*x))*Sin[d + e*x]^n)/(e^2*n^2 + b^2*c^2*Log[F]^2), x] + (Dist[(n*(n - 1)*e^2)/(e^2*n^2 + b^2*c^2*Log[F]^2), Int[F^(c*(a + b*x))*Sin[d + e*x]^(n - 2), x], x] - Simp[(e*n*F^(c*(a + b*x))*Cos[d + e*x]*Sin[d + e*x]^(n - 1))/(e^2*n^2 + b^2*c^2*Log[F]^2), x]) /; FreeQ[{F, a, b, c, d, e}, x] && NeQ[e^2*n^2 + b^2*c^2*Log[F]^2, 0] && GtQ[n, 1]

Rubi steps

$$\begin{aligned} \int e^x \sin^4(x) dx &= -\frac{4}{17}e^x \cos(x) \sin^3(x) + \frac{1}{17}e^x \sin^4(x) + \frac{12}{17} \int e^x \sin^2(x) dx \\ &= -\frac{24}{85}e^x \cos(x) \sin(x) + \frac{12}{85}e^x \sin^2(x) - \frac{4}{17}e^x \cos(x) \sin^3(x) + \frac{1}{17}e^x \sin^4(x) + \frac{24}{85} \int e^x dx \\ &= \frac{24e^x}{85} - \frac{24}{85}e^x \cos(x) \sin(x) + \frac{12}{85}e^x \sin^2(x) - \frac{4}{17}e^x \cos(x) \sin^3(x) + \frac{1}{17}e^x \sin^4(x) \end{aligned}$$

Mathematica [A] time = 0.04, size = 33, normalized size = 0.61

$$\frac{1}{680}e^x(-136 \sin(2x) + 20 \sin(4x) - 68 \cos(2x) + 5 \cos(4x) + 255)$$

Antiderivative was successfully verified.

[In] Integrate[E^x*Sin[x]^4,x]

[Out] (E^x*(255 - 68*Cos[2*x] + 5*Cos[4*x] - 136*Sin[2*x] + 20*Sin[4*x]))/680

fricas [A] time = 0.64, size = 36, normalized size = 0.67

$$\frac{4}{85} (5 \cos(x)^3 - 11 \cos(x)) e^x \sin(x) + \frac{1}{85} (5 \cos(x)^4 - 22 \cos(x)^2 + 41) e^x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(x)*sin(x)^4,x, algorithm="fricas")

[Out] 4/85*(5*cos(x)^3 - 11*cos(x))*e^x*sin(x) + 1/85*(5*cos(x)^4 - 22*cos(x)^2 + 41)*e^x

giac [A] time = 0.14, size = 35, normalized size = 0.65

$$\frac{1}{136} (\cos(4x) + 4 \sin(4x)) e^x - \frac{1}{10} (\cos(2x) + 2 \sin(2x)) e^x + \frac{3}{8} e^x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(x)*sin(x)^4,x, algorithm="giac")

[Out] 1/136*(cos(4*x) + 4*sin(4*x))*e^x - 1/10*(cos(2*x) + 2*sin(2*x))*e^x + 3/8*e^x

maple [A] time = 0.03, size = 34, normalized size = 0.63

$$\frac{(\sin(x) - 4 \cos(x)) e^x (\sin^3(x))}{17} + \frac{12 (\sin(x) - 2 \cos(x)) e^x \sin(x)}{85} + \frac{24 e^x}{85}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(exp(x)*sin(x)^4,x)

[Out] 1/17*(sin(x)-4*cos(x))*exp(x)*sin(x)^3+12/85*(sin(x)-2*cos(x))*exp(x)*sin(x)+24/85*exp(x)

maxima [A] time = 0.32, size = 37, normalized size = 0.69

$$\frac{1}{136} \cos(4x) e^x - \frac{1}{10} \cos(2x) e^x + \frac{1}{34} e^x \sin(4x) - \frac{1}{5} e^x \sin(2x) + \frac{3}{8} e^x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(x)*sin(x)^4,x, algorithm="maxima")

[Out] 1/136*cos(4*x)*e^x - 1/10*cos(2*x)*e^x + 1/34*e^x*sin(4*x) - 1/5*e^x*sin(2*x) + 3/8*e^x

mupad [B] time = 0.05, size = 41, normalized size = 0.76

$$\frac{3 e^x}{8} - \frac{e^x \left(\frac{4 \cos(2x)}{5} + \frac{8 \sin(2x)}{5} - \frac{2 \cos(2x)^2}{17} - \frac{8 \cos(2x) \sin(2x)}{17} + \frac{1}{17} \right)}{8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(exp(x)*sin(x)^4,x)

[Out] (3*exp(x))/8 - (exp(x)*((4*cos(2*x))/5 + (8*sin(2*x))/5 - (2*cos(2*x)^2)/17 - (8*cos(2*x)*sin(2*x))/17 + 1/17))/8

sympy [A] time = 3.74, size = 70, normalized size = 1.30

$$\frac{41 e^x \sin^4(x)}{85} - \frac{44 e^x \sin^3(x) \cos(x)}{85} + \frac{12 e^x \sin^2(x) \cos^2(x)}{17} - \frac{24 e^x \sin(x) \cos^3(x)}{85} + \frac{24 e^x \cos^4(x)}{85}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(x)*sin(x)**4,x)
```

```
[Out] 41*exp(x)*sin(x)**4/85 - 44*exp(x)*sin(x)**3*cos(x)/85 + 12*exp(x)*sin(x)**  
2*cos(x)**2/17 - 24*exp(x)*sin(x)*cos(x)**3/85 + 24*exp(x)*cos(x)**4/85
```

3.10 $\int F^{c(a+bx)} \cos^n(d+ex) dx$

Optimal. Leaf size=107

$$\frac{(1 + e^{2i(d+ex)})^{-n} F^{c(a+bx)} \cos^n(d+ex) {}_2F_1\left(-n, -\frac{en+ibc \log(F)}{2e}; \frac{1}{2}\left(-n - \frac{ibc \log(F)}{e} + 2\right); -e^{2i(d+ex)}\right)}{-bc \log(F) + ien}$$

[Out] $-F^{(c*(b*x+a))*\cos(e*x+d)^n*\text{hypergeom}([-n, 1/2*(-e*n-I*b*c*\ln(F))/e], [1-1/2*n-1/2*I*b*c*\ln(F)/e], -\exp(2*I*(e*x+d)))/((1+\exp(2*I*(e*x+d)))^n)/(I*e*n-b*c*\ln(F))$

Rubi [A] time = 0.11, antiderivative size = 107, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {4441, 2259}

$$\frac{(1 + e^{2i(d+ex)})^{-n} F^{c(a+bx)} \cos^n(d+ex) {}_2F_1\left(-n, -\frac{en+ibc \log(F)}{2e}; \frac{1}{2}\left(-n - \frac{ibc \log(F)}{e} + 2\right); -e^{2i(d+ex)}\right)}{-bc \log(F) + ien}$$

Antiderivative was successfully verified.

[In] $\text{Int}[F^{(c*(a + b*x))*\text{Cos}[d + e*x]^n, x]$

[Out] $-((F^{(c*(a + b*x))*\text{Cos}[d + e*x]^n*\text{Hypergeometric2F1}[-n, -(e*n + I*b*c*\text{Log}[F])]/(2*e), (2 - n - (I*b*c*\text{Log}[F])/e)/2, -E^{((2*I)*(d + e*x))})/((1 + E^{((2*I)*(d + e*x))})^n*(I*e*n - b*c*\text{Log}[F])))$

Rule 2259

$\text{Int}[(a_ + (b_)*(F_)^{(e_)*((c_) + (d_)*(x_))})^{(p_)}*(G_)^{(h_)*((f_) + (g_)*(x_))})*(H_)^{(t_)*((r_) + (s_)*(x_))}, x_Symbol] \rightarrow \text{Simp}[(G^{(h*(f + g*x))*H^{(t*(r + s*x))*}(a + b*F^{(e*(c + d*x)))})^p*\text{Hypergeometric2F1}[-p, (g*h*\text{Log}[G] + s*t*\text{Log}[H])/(d*e*\text{Log}[F]), (g*h*\text{Log}[G] + s*t*\text{Log}[H])/(d*e*\text{Log}[F]) + 1, \text{Simplify}[-((b*F^{(e*(c + d*x))})/a)])/((g*h*\text{Log}[G] + s*t*\text{Log}[H])*(a + b*F^{(e*(c + d*x))})/a)^p, x] /; \text{FreeQ}\{F, G, H, a, b, c, d, e, f, g, h, r, s, t, p\}, x] \&\& !\text{IntegerQ}[p]$

Rule 4441

$\text{Int}[\text{Cos}[(d_) + (e_)*(x_)]^{(n_)}*(F_)^{(c_)*((a_) + (b_)*(x_))}, x_Symbol] \rightarrow \text{Dist}[(E^{(I*n*(d + e*x))*\text{Cos}[d + e*x]^n)/(1 + E^{(2*I*(d + e*x))})^n, \text{Int}[(F^{(c*(a + b*x))*}(1 + E^{(2*I*(d + e*x))})^n)/E^{(I*n*(d + e*x))}, x], x] /; \text{FreeQ}\{F, a, b, c, d, e, n\}, x] \&\& !\text{IntegerQ}[n]$

Rubi steps

$$\begin{aligned} \int F^{c(a+bx)} \cos^n(d+ex) dx &= \left(e^{in(d+ex)} (1 + e^{2i(d+ex)})^{-n} \cos^n(d+ex) \right) \int e^{-in(d+ex)} (1 + e^{2i(d+ex)})^n F^{c(a+bx)} dx \\ &= -\frac{(1 + e^{2i(d+ex)})^{-n} F^{c(a+bx)} \cos^n(d+ex) {}_2F_1\left(-n, -\frac{en+ibc \log(F)}{2e}; \frac{1}{2}\left(2 - n - \frac{ibc \log(F)}{e}\right); -e^{2i(d+ex)}\right)}{ien - bc \log(F)} \end{aligned}$$

Mathematica [A] time = 0.06, size = 110, normalized size = 1.03

$$\frac{(1 + e^{2i(d+ex)})^{-n} F^{c(a+bx)} \cos^n(d+ex) {}_2F_1\left(-n, -\frac{i(bc \log(F)-ien)}{2e}; 1 - \frac{i(bc \log(F)-ien)}{2e}; -e^{2i(d+ex)}\right)}{bc \log(F) - ien}$$

Antiderivative was successfully verified.

[In] Integrate[F^(c*(a + b*x))*Cos[d + e*x]^n,x]

[Out] (F^(c*(a + b*x))*Cos[d + e*x]^n*Hypergeometric2F1[-n, ((-1/2*I)*((-I)*e*n + b*c*Log[F]))/e, 1 - ((I/2)*((-I)*e*n + b*c*Log[F]))/e, -E^((2*I)*(d + e*x)))/((1 + E^((2*I)*(d + e*x)))^n*((-I)*e*n + b*c*Log[F]))

fricas [F] time = 0.67, size = 0, normalized size = 0.00

$$\text{integral}\left(F^{bcx+ac} \cos(ex + d)^n, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(F^(c*(b*x+a))*cos(e*x+d)^n,x, algorithm="fricas")

[Out] integral(F^(b*c*x + a*c)*cos(e*x + d)^n, x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int F^{(bx+a)c} \cos(ex + d)^n dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(F^(c*(b*x+a))*cos(e*x+d)^n,x, algorithm="giac")

[Out] integrate(F^((b*x + a)*c)*cos(e*x + d)^n, x)

maple [F] time = 0.80, size = 0, normalized size = 0.00

$$\int F^{c(bx+a)} (\cos^n(ex + d)) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(F^(c*(b*x+a))*cos(e*x+d)^n,x)

[Out] int(F^(c*(b*x+a))*cos(e*x+d)^n,x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int F^{(bx+a)c} \cos(ex + d)^n dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(F^(c*(b*x+a))*cos(e*x+d)^n,x, algorithm="maxima")

[Out] integrate(F^((b*x + a)*c)*cos(e*x + d)^n, x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int F^{c(a+bx)} \cos(d + ex)^n dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(F^(c*(a + b*x))*cos(d + e*x)^n,x)

[Out] int(F^(c*(a + b*x))*cos(d + e*x)^n, x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int F^{c(a+bx)} \cos^n(d + ex) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(F**(c*(b*x+a))*cos(e*x+d)**n,x)

[Out] Integral(F**(c*(a + b*x))*cos(d + e*x)**n, x)

3.11 $\int F^{c(a+bx)} \cos^3(d+ex) dx$

Optimal. Leaf size=199

$$\frac{bc \log(F) \cos^3(d+ex) F^{c(a+bx)}}{b^2 c^2 \log^2(F) + 9e^2} + \frac{3e \sin(d+ex) \cos^2(d+ex) F^{c(a+bx)}}{b^2 c^2 \log^2(F) + 9e^2} + \frac{6bce^2 \log(F) \cos(d+ex) F^{c(a+bx)}}{b^4 c^4 \log^4(F) + 10b^2 c^2 e^2 \log^2(F) + 9e^4} + \frac{3e^3 \sin(d+ex) F^{c(a+bx)}}{b^4 c^4 \log^4(F) + 10b^2 c^2 e^2 \log^2(F) + 9e^4}$$

[Out] $b*c*F^{(c*(b*x+a))*\cos(e*x+d)^3*\ln(F)/(9*e^2+b^2*c^2*\ln(F)^2)+6*b*c*e^2*F^{(c*(b*x+a))*\cos(e*x+d)*\ln(F)/(9*e^4+10*b^2*c^2*e^2*\ln(F)^2+b^4*c^4*\ln(F)^4)+3*e*F^{(c*(b*x+a))*\cos(e*x+d)^2*\sin(e*x+d)/(9*e^2+b^2*c^2*\ln(F)^2)+6*e^3*F^{(c*(b*x+a))*\sin(e*x+d)/(9*e^4+10*b^2*c^2*e^2*\ln(F)^2+b^4*c^4*\ln(F)^4)}$

Rubi [A] time = 0.05, antiderivative size = 199, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {4435, 4433}

$$\frac{6e^3 \sin(d+ex) F^{c(a+bx)}}{10b^2 c^2 e^2 \log^2(F) + b^4 c^4 \log^4(F) + 9e^4} + \frac{bc \log(F) \cos^3(d+ex) F^{c(a+bx)}}{b^2 c^2 \log^2(F) + 9e^2} + \frac{6bce^2 \log(F) \cos(d+ex) F^{c(a+bx)}}{10b^2 c^2 e^2 \log^2(F) + b^4 c^4 \log^4(F) + 9e^4} + \frac{3e^3 \sin(d+ex) F^{c(a+bx)}}{10b^2 c^2 e^2 \log^2(F) + b^4 c^4 \log^4(F) + 9e^4}$$

Antiderivative was successfully verified.

[In] Int[F^(c*(a+b*x))*Cos[d+e*x]^3,x]

[Out] $(b*c*F^{(c*(a+b*x))*\text{Cos}[d+e*x]^3*\text{Log}[F]}/(9*e^2+b^2*c^2*\text{Log}[F]^2)+(6*b*c*e^2*F^{(c*(a+b*x))*\text{Cos}[d+e*x]*\text{Log}[F]}/(9*e^4+10*b^2*c^2*e^2*\text{Log}[F]^2+b^4*c^4*\text{Log}[F]^4)+(3*e*F^{(c*(a+b*x))*\text{Cos}[d+e*x]^2*\text{Sin}[d+e*x]}/(9*e^2+b^2*c^2*\text{Log}[F]^2)+(6*e^3*F^{(c*(a+b*x))*\text{Sin}[d+e*x]}/(9*e^4+10*b^2*c^2*e^2*\text{Log}[F]^2+b^4*c^4*\text{Log}[F]^4)$

Rule 4433

Int[Cos[(d_.)+(e_.)*(x_.)]*(F_)^(c_.*((a_.)+(b_.)*(x_.))), x_Symbol] :> Simp[(b*c*Log[F]*F^(c*(a+b*x))*Cos[d+e*x]/(e^2+b^2*c^2*Log[F]^2), x] + Simp[(e*F^(c*(a+b*x))*Sin[d+e*x]/(e^2+b^2*c^2*Log[F]^2), x] /; FreeQ[{F, a, b, c, d, e}, x] && NeQ[e^2+b^2*c^2*Log[F]^2, 0]

Rule 4435

Int[Cos[(d_.)+(e_.)*(x_.)]^(m_)*(F_)^(c_.*((a_.)+(b_.)*(x_.))), x_Symbol] :> Simp[(b*c*Log[F]*F^(c*(a+b*x))*Cos[d+e*x]^m/(e^2*m^2+b^2*c^2*Log[F]^2), x] + (Dist[(m*(m-1)*e^2)/(e^2*m^2+b^2*c^2*Log[F]^2), Int[F^(c*(a+b*x))*Cos[d+e*x]^(m-2), x], x] + Simp[(e*m*F^(c*(a+b*x))*Sin[d+e*x]*Cos[d+e*x]^(m-1)/(e^2*m^2+b^2*c^2*Log[F]^2), x]) /; FreeQ[{F, a, b, c, d, e}, x] && NeQ[e^2*m^2+b^2*c^2*Log[F]^2, 0] && GtQ[m, 1]

Rubi steps

$$\begin{aligned} \int F^{c(a+bx)} \cos^3(d+ex) dx &= \frac{bc F^{c(a+bx)} \cos^3(d+ex) \log(F)}{9e^2 + b^2 c^2 \log^2(F)} + \frac{3e F^{c(a+bx)} \cos^2(d+ex) \sin(d+ex)}{9e^2 + b^2 c^2 \log^2(F)} + \frac{(6e^2) \int F^{c(a+bx)} \cos(d+ex) \log(F) dx}{9e^2 + b^2 c^2 \log^2(F)} \\ &= \frac{bc F^{c(a+bx)} \cos^3(d+ex) \log(F)}{9e^2 + b^2 c^2 \log^2(F)} + \frac{6bce^2 F^{c(a+bx)} \cos(d+ex) \log(F)}{9e^4 + 10b^2 c^2 e^2 \log^2(F) + b^4 c^4 \log^4(F)} + \frac{3e F^{c(a+bx)} \sin(d+ex)}{9e^4 + 10b^2 c^2 e^2 \log^2(F) + b^4 c^4 \log^4(F)} \end{aligned}$$

Mathematica [A] time = 0.67, size = 155, normalized size = 0.78

$$\frac{F^{c(a+bx)} (bc \log(F) \cos(3(d+ex)) (b^2 c^2 \log^2(F) + e^2) + 3bc \log(F) \cos(d+ex) (b^2 c^2 \log^2(F) + 9e^2) + 6e \sin(d+ex))}{4 (b^4 c^4 \log^4(F) + 10b^2 c^2 e^2 \log^2(F) + 9e^4)}$$

Antiderivative was successfully verified.

[In] Integrate[F^(c*(a + b*x))*Cos[d + e*x]^3,x]

[Out] $(F^{c(a+bx)})(b^3c^3\cos^3(d+ex)\log(F)^3 + (b^3c^3\cos^3(d+ex)\log(F)^3 + (bce^2\cos(d+ex))^3 + 6bce^2\cos(d+ex))\log(F) + 3(b^2c^2e\cos(d+ex))^2\log(F)^2 - b^4c^4\log(F)^4 + 10b^2c^2e^2\log(F)^2 + 9e^4)$

fricas [A] time = 2.09, size = 142, normalized size = 0.71

$$\frac{(b^3c^3\cos^3(ex+d)^3\log(F)^3 + (bce^2\cos(ex+d))^3 + 6bce^2\cos(ex+d))\log(F) + 3(b^2c^2e\cos(ex+d))^2\log(F)^2 - b^4c^4\log(F)^4 + 10b^2c^2e^2\log(F)^2 + 9e^4}{b^4c^4\log(F)^4 + 10b^2c^2e^2\log(F)^2 + 9e^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(F^(c*(b*x+a))*cos(e*x+d)^3,x, algorithm="fricas")

[Out] $(b^3c^3\cos^3(ex+d)\log(F)^3 + (b^3c^3\cos^3(ex+d)\log(F)^3 + 6b^2c^2e\cos^2(ex+d)\log(F)^2 + e^3\cos^3(ex+d)\log(F)^2 + 2e^3)\sin(ex+d)F^{(b^2c^2e\cos^2(ex+d)\log(F)^2 + 10b^2c^2e^2\log(F)^2 + 9e^4)}$

giac [C] time = 0.29, size = 1307, normalized size = 6.57

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(F^(c*(b*x+a))*cos(e*x+d)^3,x, algorithm="giac")

[Out] $\frac{1}{4}(2b^2c^2\cos(1/2\pi b^2c^2x\operatorname{sgn}(F) - 1/2\pi b^2c^2x + 1/2\pi a^2c^2\operatorname{sgn}(F) - 1/2\pi a^2c^2x + 3xe + 3d)\log(\operatorname{abs}(F)) / (4b^2c^2\log(\operatorname{abs}(F))^2 + (\pi b^2c^2\operatorname{sgn}(F) - \pi b^2c^2x + 6e)^2) + (\pi b^2c^2\operatorname{sgn}(F) - \pi b^2c^2x + 6e)\sin(1/2\pi b^2c^2x\operatorname{sgn}(F) - 1/2\pi b^2c^2x + 1/2\pi a^2c^2\operatorname{sgn}(F) - 1/2\pi a^2c^2x + 3xe + 3d) / (4b^2c^2\log(\operatorname{abs}(F))^2 + (\pi b^2c^2\operatorname{sgn}(F) - \pi b^2c^2x + 6e)^2))e^{(b^2c^2x\log(\operatorname{abs}(F)) + a^2c^2\log(\operatorname{abs}(F)))} + 3/4(2b^2c^2\cos(1/2\pi b^2c^2x\operatorname{sgn}(F) - 1/2\pi b^2c^2x + 1/2\pi a^2c^2\operatorname{sgn}(F) - 1/2\pi a^2c^2x + xe + d)\log(\operatorname{abs}(F)) / (4b^2c^2\log(\operatorname{abs}(F))^2 + (\pi b^2c^2\operatorname{sgn}(F) - \pi b^2c^2x + 2e)^2) + (\pi b^2c^2\operatorname{sgn}(F) - \pi b^2c^2x + 2e)\sin(1/2\pi b^2c^2x\operatorname{sgn}(F) - 1/2\pi b^2c^2x + 1/2\pi a^2c^2\operatorname{sgn}(F) - 1/2\pi a^2c^2x + xe + d) / (4b^2c^2\log(\operatorname{abs}(F))^2 + (\pi b^2c^2\operatorname{sgn}(F) - \pi b^2c^2x + 2e)^2))e^{(b^2c^2x\log(\operatorname{abs}(F)) + a^2c^2\log(\operatorname{abs}(F)))} + 3/4(2b^2c^2\cos(1/2\pi b^2c^2x\operatorname{sgn}(F) - 1/2\pi b^2c^2x + 1/2\pi a^2c^2\operatorname{sgn}(F) - 1/2\pi a^2c^2x - xe - d)\log(\operatorname{abs}(F)) / (4b^2c^2\log(\operatorname{abs}(F))^2 + (\pi b^2c^2\operatorname{sgn}(F) - \pi b^2c^2x - 2e)^2) + (\pi b^2c^2\operatorname{sgn}(F) - \pi b^2c^2x - 2e)\sin(1/2\pi b^2c^2x\operatorname{sgn}(F) - 1/2\pi b^2c^2x + 1/2\pi a^2c^2\operatorname{sgn}(F) - 1/2\pi a^2c^2x - xe - d) / (4b^2c^2\log(\operatorname{abs}(F))^2 + (\pi b^2c^2\operatorname{sgn}(F) - \pi b^2c^2x - 2e)^2))e^{(b^2c^2x\log(\operatorname{abs}(F)) + a^2c^2\log(\operatorname{abs}(F)))} + 1/4(2b^2c^2\cos(1/2\pi b^2c^2x\operatorname{sgn}(F) - 1/2\pi b^2c^2x + 1/2\pi a^2c^2\operatorname{sgn}(F) - 1/2\pi a^2c^2x - 3xe - 3d)\log(\operatorname{abs}(F)) / (4b^2c^2\log(\operatorname{abs}(F))^2 + (\pi b^2c^2\operatorname{sgn}(F) - \pi b^2c^2x - 6e)^2) + (\pi b^2c^2\operatorname{sgn}(F) - \pi b^2c^2x - 6e)\sin(1/2\pi b^2c^2x\operatorname{sgn}(F) - 1/2\pi b^2c^2x + 1/2\pi a^2c^2\operatorname{sgn}(F) - 1/2\pi a^2c^2x - 3xe - 3d) / (4b^2c^2\log(\operatorname{abs}(F))^2 + (\pi b^2c^2\operatorname{sgn}(F) - \pi b^2c^2x - 6e)^2))e^{(b^2c^2x\log(\operatorname{abs}(F)) + a^2c^2\log(\operatorname{abs}(F)))} - 1/2I(-2Ie^{(1/2I\pi b^2c^2x\operatorname{sgn}(F) - 1/2I\pi b^2c^2x + 1/2I\pi a^2c^2\operatorname{sgn}(F) - 1/2I\pi a^2c^2x + 3Ixe + 3Id)} / (8I\pi b^2c^2\operatorname{sgn}(F) - 8I\pi b^2c^2x + 16b^2c^2\log(\operatorname{abs}(F)) + 48Ie) + 2Ie^{(-1/2I\pi b^2c^2x\operatorname{sgn}(F) + 1/2I\pi b^2c^2x - 1/2I\pi a^2c^2\operatorname{sgn}(F) + 1/2I\pi a^2c^2x - 3Ixe - 3Id)} / (-8I\pi b^2c^2\operatorname{sgn}(F) + 8I\pi b^2c^2x + 16b^2c^2\log(\operatorname{abs}(F)) - 48Ie))e^{(b^2c^2x\log(\operatorname{abs}(F)) + a^2c^2\log(\operatorname{abs}(F)))} - 1/2I(-6Ie^{(1/2I\pi b^2c^2x\operatorname{sgn}(F) - 1/2I\pi b^2c^2x + 1/2I\pi a^2c^2\operatorname{sgn}(F) - 1/2I\pi a^2c^2x + Ixe + Id)} / (8I\pi b^2c^2\operatorname{sgn}(F) - 8I\pi b^2c^2x + 16b^2c^2\log(\operatorname{abs}(F)) + 16Ie) + 6Ie^{(-1/2I\pi b^2c^2x\operatorname{sgn}(F) + 1/2I\pi b^2c^2x - 1/2I\pi a^2c^2\operatorname{sgn}(F) + 1/2I\pi a^2c^2x - Ixe - Id)} / (-8I\pi b^2c^2\operatorname{sgn}(F) + 8I\pi b^2c^2x + 16b^2c^2\log(\operatorname{abs}(F)) - 16Ie))e^{(b^2c^2x\log(\operatorname{abs}(F)) + a^2c^2\log(\operatorname{abs}(F)))} -$

$$\begin{aligned} & \frac{1}{2}I*(-6*I*e^{(1/2*I*pi*b*c*x*sgn(F)} - 1/2*I*pi*b*c*x + 1/2*I*pi*a*c*sgn(F) \\ &) - 1/2*I*pi*a*c - I*x*e - I*d)/(8*I*pi*b*c*sgn(F) - 8*I*pi*b*c + 16*b*c*log \\ & (abs(F)) - 16*I*e) + 6*I*e^{(-1/2*I*pi*b*c*x*sgn(F) + 1/2*I*pi*b*c*x - 1/2* \\ & I*pi*a*c*sgn(F) + 1/2*I*pi*a*c + I*x*e + I*d)/(-8*I*pi*b*c*sgn(F) + 8*I*pi* \\ & b*c + 16*b*c*log(abs(F)) + 16*I*e))*e^{(b*c*x*log(abs(F)) + a*c*log(abs(F)))} \\ & - 1/2*I*(-2*I*e^{(1/2*I*pi*b*c*x*sgn(F)} - 1/2*I*pi*b*c*x + 1/2*I*pi*a*c*sgn \\ & (F) - 1/2*I*pi*a*c - 3*I*x*e - 3*I*d)/(8*I*pi*b*c*sgn(F) - 8*I*pi*b*c + 16* \\ & b*c*log(abs(F)) - 48*I*e) + 2*I*e^{(-1/2*I*pi*b*c*x*sgn(F) + 1/2*I*pi*b*c*x \\ & - 1/2*I*pi*a*c*sgn(F) + 1/2*I*pi*a*c + 3*I*x*e + 3*I*d)/(-8*I*pi*b*c*sgn(F) \\ & + 8*I*pi*b*c + 16*b*c*log(abs(F)) + 48*I*e))*e^{(b*c*x*log(abs(F)) + a*c*log \\ & (abs(F)))} \end{aligned}$$

maple [A] time = 0.43, size = 274, normalized size = 1.38

$$\frac{\frac{\ln(F)bc e^{c(bx+a)\ln(F)}}{9e^2+b^2c^2\ln(F)^2} + \frac{6e e^{c(bx+a)\ln(F)} \tan\left(\frac{3ex}{2} + \frac{3d}{2}\right)}{9e^2+b^2c^2\ln(F)^2} - \frac{\ln(F)bc e^{c(bx+a)\ln(F)} \left(\tan^2\left(\frac{3ex}{2} + \frac{3d}{2}\right)\right)}{9e^2+b^2c^2\ln(F)^2} + \frac{3bc \ln(F) e^{c(bx+a)\ln(F)}}{4(e^2+b^2c^2\ln(F)^2)} + \frac{3e e^{c(bx+a)\ln(F)} \tan\left(\frac{d}{2} + \frac{ex}{2}\right)}{2(e^2+b^2c^2\ln(F)^2)}}{4 + 4 \left(\tan^2\left(\frac{3ex}{2} + \frac{3d}{2}\right)\right)} + \frac{1 + \tan^2\left(\frac{d}{2} + \frac{ex}{2}\right)}{2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(F^(c*(b*x+a))*cos(e*x+d)^3,x)

[Out] 1/4*(ln(F)*b*c/(9*e^2+b^2*c^2*ln(F)^2)*exp(c*(b*x+a)*ln(F))+6/(9*e^2+b^2*c^2*ln(F)^2)*e*exp(c*(b*x+a)*ln(F))*tan(3/2*e*x+3/2*d)-ln(F)*b*c/(9*e^2+b^2*c^2*ln(F)^2)*exp(c*(b*x+a)*ln(F))*tan(3/2*e*x+3/2*d)^2/(1+tan(3/2*e*x+3/2*d))^2)+3/4*(b*c*ln(F)/(e^2+b^2*c^2*ln(F)^2)*exp(c*(b*x+a)*ln(F))+2/(e^2+b^2*c^2*ln(F)^2)*e*exp(c*(b*x+a)*ln(F))*tan(1/2*d+1/2*e*x)-b*c*ln(F)/(e^2+b^2*c^2*ln(F)^2)*exp(c*(b*x+a)*ln(F))*tan(1/2*d+1/2*e*x)^2/(1+tan(1/2*d+1/2*e*x))^2)

maxima [B] time = 0.39, size = 813, normalized size = 4.09

$$\frac{(F^{ac}b^3c^3 \cos(3d) \log(F)^3 + 3F^{ac}b^2c^2e \log(F)^2 \sin(3d) + F^{ac}bce^2 \cos(3d) \log(F) + 3F^{ac}e^3 \sin(3d))F^{bcx} \cos(3ex)}{1}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(F^(c*(b*x+a))*cos(e*x+d)^3,x, algorithm="maxima")

[Out] 1/8*((F^(a*c)*b^3*c^3*cos(3*d)*log(F)^3 + 3F^(a*c)*b^2*c^2*e*log(F)^2*sin(3*d) + F^(a*c)*b*c*e^2*cos(3*d)*log(F) + 3F^(a*c)*e^3*sin(3*d))*F^(b*c*x)*cos(3*e*x) + (F^(a*c)*b^3*c^3*cos(3*d)*log(F)^3 - 3F^(a*c)*b^2*c^2*e*log(F)^2*sin(3*d) + F^(a*c)*b*c*e^2*cos(3*d)*log(F) - 3F^(a*c)*e^3*sin(3*d))*F^(b*c*x)*cos(3*e*x + 6*d) + 3*(F^(a*c)*b^3*c^3*cos(3*d)*log(F)^3 - F^(a*c)*b^2*c^2*e*log(F)^2*sin(3*d) + 9F^(a*c)*b*c*e^2*cos(3*d)*log(F) - 9F^(a*c)*e^3*sin(3*d))*F^(b*c*x)*cos(e*x + 4*d) + 3*(F^(a*c)*b^3*c^3*cos(3*d)*log(F)^3 + F^(a*c)*b^2*c^2*e*log(F)^2*sin(3*d) + 9F^(a*c)*b*c*e^2*cos(3*d)*log(F) + 9F^(a*c)*e^3*sin(3*d))*F^(b*c*x)*cos(e*x - 2*d) - (F^(a*c)*b^3*c^3*log(F)^3*sin(3*d) - 3F^(a*c)*b^2*c^2*e*cos(3*d)*log(F)^2 + F^(a*c)*b*c*e^2*log(F)*sin(3*d) - 3F^(a*c)*e^3*cos(3*d))*F^(b*c*x)*sin(3*e*x) + (F^(a*c)*b^3*c^3*log(F)^3*sin(3*d) + 3F^(a*c)*b^2*c^2*e*cos(3*d)*log(F)^2 + F^(a*c)*b*c*e^2*log(F)*sin(3*d) + 3F^(a*c)*e^3*cos(3*d))*F^(b*c*x)*sin(3*e*x + 6*d) + 3*(F^(a*c)*b^3*c^3*log(F)^3*sin(3*d) + F^(a*c)*b^2*c^2*e*cos(3*d)*log(F)^2 + 9F^(a*c)*b*c*e^2*log(F)*sin(3*d) + 9F^(a*c)*e^3*cos(3*d))*F^(b*c*x)*sin(e*x + 4*d) - 3*(F^(a*c)*b^3*c^3*log(F)^3*sin(3*d) - F^(a*c)*b^2*c^2*e*cos(3*d)*log(F)^2 + 9F^(a*c)*b*c*e^2*log(F)*sin(3*d) - 9F^(a*c)*e^3*cos(3*d))*F^(b*c*x)*sin(e*x - 2*d)/(b^4*c^4*cos(3*d)^2*log(F)^4 + b^4*c^4*log(F)^4*sin(3*d)^2 + 9*(cos(3*d)^2 + sin(3*d)^2)*e^4 + 10*(b^2*c^2*cos(3*d)^2*log(F)^2 + b^2*c^2*log(F)^2*sin(3*d)^2)*e^2)

mupad [B] time = 3.14, size = 191, normalized size = 0.96

$$\frac{F^{c(a+bx)} (\cos(ex) + \sin(ex)1i) (\cos(d) + \sin(d)1i) 3i}{8(e - bc \ln(F)1i)} - \frac{F^{c(a+bx)} (\cos(3ex) - \sin(3ex)1i) (\cos(3d) - \sin(3d)1i)}{8(-bc \ln(F) + e3i)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(F^(c*(a + b*x))*cos(d + e*x)^3,x)

[Out] - (F^(c*(a + b*x))*(cos(e*x) + sin(e*x)*1i)*(cos(d) + sin(d)*1i)*3i)/(8*(e - b*c*log(F)*1i)) - (F^(c*(a + b*x))*(cos(3*e*x) - sin(3*e*x)*1i)*(cos(3*d) - sin(3*d)*1i))/(8*(e*3i - b*c*log(F))) - (F^(c*(a + b*x))*(cos(3*e*x) + sin(3*e*x)*1i)*(cos(3*d) + sin(3*d)*1i)*1i)/(8*(3*e - b*c*log(F)*1i)) - (3*F^(c*(a + b*x))*(cos(e*x) - sin(e*x)*1i)*(cos(d) - sin(d)*1i))/(8*(e*1i - b*c*log(F)))

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(F**(c*(b*x+a))*cos(e*x+d)**3,x)

[Out] Timed out

3.12 $\int F^{c(a+bx)} \cos^2(d+ex) dx$

Optimal. Leaf size=128

$$\frac{bc \log(F) \cos^2(d+ex) F^{c(a+bx)}}{b^2 c^2 \log^2(F) + 4e^2} + \frac{2e \sin(d+ex) \cos(d+ex) F^{c(a+bx)}}{b^2 c^2 \log^2(F) + 4e^2} + \frac{2e^2 F^{c(a+bx)}}{bc \log(F) (b^2 c^2 \log^2(F) + 4e^2)}$$

[Out] $2e^2 F^{c(a+bx)} / (bc \log(F) (4e^2 + b^2 c^2 \log^2(F) + b^2 c^2 \log^2(F) + 4e^2)) + (2e \sin(d+ex) \cos(d+ex) F^{c(a+bx)}) / (b^2 c^2 \log^2(F) + 4e^2) + (2e^2 F^{c(a+bx)}) / (bc \log(F) (b^2 c^2 \log^2(F) + 4e^2))$

Rubi [A] time = 0.04, antiderivative size = 128, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {4435, 2194}

$$\frac{bc \log(F) \cos^2(d+ex) F^{c(a+bx)}}{b^2 c^2 \log^2(F) + 4e^2} + \frac{2e \sin(d+ex) \cos(d+ex) F^{c(a+bx)}}{b^2 c^2 \log^2(F) + 4e^2} + \frac{2e^2 F^{c(a+bx)}}{bc \log(F) (b^2 c^2 \log^2(F) + 4e^2)}$$

Antiderivative was successfully verified.

[In] Int[F^(c*(a + b*x))*Cos[d + e*x]^2, x]

[Out] $(2e^2 F^{c(a+bx)}) / (b^2 c^2 \log^2(F) + 4e^2) + (2e \sin(d+ex) \cos(d+ex) F^{c(a+bx)}) / (b^2 c^2 \log^2(F) + 4e^2) + (2e^2 F^{c(a+bx)}) / (bc \log(F) (b^2 c^2 \log^2(F) + 4e^2))$

Rule 2194

Int[((F_)^((c_.)*((a_.) + (b_.)*(x_))))^(n_.), x_Symbol] :> Simp[(F^(c*(a + b*x)))^n/(b*c*n*Log[F]), x] /; FreeQ[{F, a, b, c, n}, x]

Rule 4435

Int[Cos[(d_.) + (e_.)*(x_)]^(m_)*(F_)^((c_.)*((a_.) + (b_.)*(x_))), x_Symbol] :> Simp[(b*c*Log[F]*F^(c*(a + b*x))*Cos[d + e*x]^m)/(e^2*m^2 + b^2*c^2*Log[F]^2), x] + (Dist[(m*(m - 1)*e^2)/(e^2*m^2 + b^2*c^2*Log[F]^2), Int[F^(c*(a + b*x))*Cos[d + e*x]^(m - 2), x], x] + Simp[(e*m*F^(c*(a + b*x))*Sin[d + e*x]*Cos[d + e*x]^(m - 1)]/(e^2*m^2 + b^2*c^2*Log[F]^2), x]) /; FreeQ[{F, a, b, c, d, e}, x] && NeQ[e^2*m^2 + b^2*c^2*Log[F]^2, 0] && GtQ[m, 1]

Rubi steps

$$\begin{aligned} \int F^{c(a+bx)} \cos^2(d+ex) dx &= \frac{bc F^{c(a+bx)} \cos^2(d+ex) \log(F)}{4e^2 + b^2 c^2 \log^2(F)} + \frac{2e F^{c(a+bx)} \cos(d+ex) \sin(d+ex)}{4e^2 + b^2 c^2 \log^2(F)} + \frac{(2e^2) \int F^{c(a+bx)}}{4e^2 + b^2 c^2 \log^2(F)} \\ &= \frac{2e^2 F^{c(a+bx)}}{bc \log(F) (4e^2 + b^2 c^2 \log^2(F))} + \frac{bc F^{c(a+bx)} \cos^2(d+ex) \log(F)}{4e^2 + b^2 c^2 \log^2(F)} + \frac{2e F^{c(a+bx)} \cos(d+ex) \sin(d+ex)}{4e^2 + b^2 c^2 \log^2(F)} \end{aligned}$$

Mathematica [A] time = 0.21, size = 85, normalized size = 0.66

$$\frac{F^{c(a+bx)} (b^2 c^2 \log^2(F) \cos(2(d+ex)) + b^2 c^2 \log^2(F) + 2bce \log(F) \sin(2(d+ex)) + 4e^2)}{2b^3 c^3 \log^3(F) + 8bce^2 \log(F)}$$

Antiderivative was successfully verified.

[In] Integrate[F^(c*(a + b*x))*Cos[d + e*x]^2, x]

[In] int(F^(c*(b*x+a))*cos(e*x+d)^2,x)

[Out] 1/2/b/c/ln(F)*F^(c*(b*x+a))+1/2*(1/(4*e^2+b^2*c^2*ln(F)^2)*b*c*ln(F)*exp(c*(b*x+a)*ln(F))+4/(4*e^2+b^2*c^2*ln(F)^2)*e*exp(c*(b*x+a)*ln(F))*tan(e*x+d)-1/(4*e^2+b^2*c^2*ln(F)^2)*b*c*ln(F)*exp(c*(b*x+a)*ln(F))*tan(e*x+d)^2)/(1+tan(e*x+d)^2)

maxima [B] time = 0.35, size = 356, normalized size = 2.78

$$\frac{(F^{ac}b^2c^2 \cos(2d) \log(F)^2 + 2F^{ac}bce \log(F) \sin(2d))F^{bcx} \cos(2ex) + (F^{ac}b^2c^2 \cos(2d) \log(F)^2 - 2F^{ac}bce \log(F))F^{bcx} \sin(2ex)}{b^3c^3 \ln(F)^3 + 4bce^2 \ln(F)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(F^(c*(b*x+a))*cos(e*x+d)^2,x, algorithm="maxima")

[Out] 1/4*((F^(a*c)*b^2*c^2*cos(2*d)*log(F)^2 + 2*F^(a*c)*b*c*e*log(F)*sin(2*d))*F^(b*c*x)*cos(2*e*x) + (F^(a*c)*b^2*c^2*cos(2*d)*log(F)^2 - 2*F^(a*c)*b*c*e*log(F)*sin(2*d))*F^(b*c*x)*cos(2*e*x + 4*d) - (F^(a*c)*b^2*c^2*log(F)^2*sin(2*d) - 2*F^(a*c)*b*c*e*cos(2*d)*log(F))*F^(b*c*x)*sin(2*e*x) + (F^(a*c)*b^2*c^2*log(F)^2*sin(2*d) + 2*F^(a*c)*b*c*e*cos(2*d)*log(F))*F^(b*c*x)*sin(2*e*x + 4*d) + 2*(F^(a*c)*b^2*c^2*cos(2*d)^2*log(F)^2 + F^(a*c)*b^2*c^2*log(F)^2*sin(2*d)^2 + 4*(F^(a*c)*cos(2*d)^2 + F^(a*c)*sin(2*d)^2)*e^2)*F^(b*c*x))/(b^3*c^3*cos(2*d)^2*log(F)^3 + b^3*c^3*log(F)^3*sin(2*d)^2 + 4*(b*c*cos(2*d)^2*log(F) + b*c*log(F)*sin(2*d)^2)*e^2)

mupad [B] time = 2.98, size = 98, normalized size = 0.77

$$\frac{2F^{ac+bcx}e^2 + F^{ac+bcx}b^2c^2 \cos(d+ex)^2 \ln(F)^2 + 2F^{ac+bcx}bce \cos(d+ex) \sin(d+ex) \ln(F)}{b^3c^3 \ln(F)^3 + 4bce^2 \ln(F)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(F^(c*(a + b*x))*cos(d + e*x)^2,x)

[Out] (2*F^(a*c + b*c*x)*e^2 + F^(a*c + b*c*x)*b^2*c^2*cos(d + e*x)^2*log(F)^2 + 2*F^(a*c + b*c*x)*b*c*e*cos(d + e*x)*sin(d + e*x)*log(F))/(b^3*c^3*log(F)^3 + 4*b*c*e^2*log(F))

sympy [A] time = 34.78, size = 627, normalized size = 4.90

$$\left\{ \begin{array}{l} \frac{x \sin^2(d+ex)}{2} + \frac{x \cos^2(d+ex)}{2} + \frac{\sin(d+ex) \cos(d+ex)}{2e} \\ \tilde{\omega} e^2 \left(e^{-\frac{2ie}{bc}} \right)^{ac} \left(e^{-\frac{2ie}{bc}} \right)^{bcx} \sin^2(d+ex) + \tilde{\omega} e^2 \left(e^{-\frac{2ie}{bc}} \right)^{ac} \left(e^{-\frac{2ie}{bc}} \right)^{bcx} \sin(d+ex) \cos(d+ex) + \tilde{\omega} e^2 \left(e^{-\frac{2ie}{bc}} \right)^{ac} \left(e^{-\frac{2ie}{bc}} \right)^{bcx} \cos^2(d+ex) \\ \tilde{\omega} e^2 \left(e^{\frac{2ie}{bc}} \right)^{ac} \left(e^{\frac{2ie}{bc}} \right)^{bcx} \sin^2(d+ex) + \tilde{\omega} e^2 \left(e^{\frac{2ie}{bc}} \right)^{ac} \left(e^{\frac{2ie}{bc}} \right)^{bcx} \sin(d+ex) \cos(d+ex) + \tilde{\omega} e^2 \left(e^{\frac{2ie}{bc}} \right)^{ac} \left(e^{\frac{2ie}{bc}} \right)^{bcx} \cos^2(d+ex) \\ F^{ac} \left(\frac{x \sin^2(d+ex)}{2} + \frac{x \cos^2(d+ex)}{2} + \frac{\sin(d+ex) \cos(d+ex)}{2e} \right) \\ \frac{x \sin^2(d+ex)}{2} + \frac{x \cos^2(d+ex)}{2} + \frac{\sin(d+ex) \cos(d+ex)}{2e} \\ \frac{F^{ac}F^{bcx}b^2c^2 \log(F)^2 \cos^2(d+ex)}{b^3c^3 \log(F)^3 + 4bce^2 \log(F)} + \frac{2F^{ac}F^{bcx}bce \log(F) \sin(d+ex) \cos(d+ex)}{b^3c^3 \log(F)^3 + 4bce^2 \log(F)} + \frac{2F^{ac}F^{bcx}e^2 \sin^2(d+ex)}{b^3c^3 \log(F)^3 + 4bce^2 \log(F)} + \frac{2F^{ac}F^{bcx}e^2 \cos^2(d+ex)}{b^3c^3 \log(F)^3 + 4bce^2 \log(F)} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(F**(c*(b*x+a))*cos(e*x+d)**2,x)

```
[Out] Piecewise((x*sin(d + e*x)**2/2 + x*cos(d + e*x)**2/2 + sin(d + e*x)*cos(d +
e*x)/(2*e), Eq(F, 1)), (zoo*e**2*exp(-2*I*e/(b*c))**(a*c)*exp(-2*I*e/(b*c)
)**(b*c*x)*sin(d + e*x)**2 + zoo*e**2*exp(-2*I*e/(b*c))**(a*c)*exp(-2*I*e/(
b*c))**(b*c*x)*sin(d + e*x)*cos(d + e*x) + zoo*e**2*exp(-2*I*e/(b*c))**(a*c
)*exp(-2*I*e/(b*c))**(b*c*x)*cos(d + e*x)**2, Eq(F, exp(-2*I*e/(b*c)))), (z
oo*e**2*exp(2*I*e/(b*c))**(a*c)*exp(2*I*e/(b*c))**(b*c*x)*sin(d + e*x)**2 +
zoo*e**2*exp(2*I*e/(b*c))**(a*c)*exp(2*I*e/(b*c))**(b*c*x)*sin(d + e*x)*co
s(d + e*x) + zoo*e**2*exp(2*I*e/(b*c))**(a*c)*exp(2*I*e/(b*c))**(b*c*x)*cos
(d + e*x)**2, Eq(F, exp(2*I*e/(b*c)))), (F**(a*c)*(x*sin(d + e*x)**2/2 + x*
cos(d + e*x)**2/2 + sin(d + e*x)*cos(d + e*x)/(2*e)), Eq(b, 0)), (x*sin(d +
e*x)**2/2 + x*cos(d + e*x)**2/2 + sin(d + e*x)*cos(d + e*x)/(2*e), Eq(c, 0
)), (F**(a*c)*F**(b*c*x)*b**2*c**2*log(F)**2*cos(d + e*x)**2/(b**3*c**3*log
(F)**3 + 4*b*c*e**2*log(F)) + 2*F**(a*c)*F**(b*c*x)*b*c*e*log(F)*sin(d + e*
x)*cos(d + e*x)/(b**3*c**3*log(F)**3 + 4*b*c*e**2*log(F)) + 2*F**(a*c)*F**(
b*c*x)*e**2*sin(d + e*x)**2/(b**3*c**3*log(F)**3 + 4*b*c*e**2*log(F)) + 2*F
**(a*c)*F**(b*c*x)*e**2*cos(d + e*x)**2/(b**3*c**3*log(F)**3 + 4*b*c*e**2*log(F)), True))
```

3.13 $\int F^{c(a+bx)} \cos(d+ex) dx$

Optimal. Leaf size=72

$$\frac{e \sin(d+ex) F^{c(a+bx)}}{b^2 c^2 \log^2(F) + e^2} + \frac{bc \log(F) \cos(d+ex) F^{c(a+bx)}}{b^2 c^2 \log^2(F) + e^2}$$

[Out] $b*c*F^{(c*(b*x+a))*\cos(e*x+d)*\ln(F)/(e^2+b^2*c^2*\ln(F)^2)+e*F^{(c*(b*x+a))*\sin(e*x+d)/(e^2+b^2*c^2*\ln(F)^2)}$

Rubi [A] time = 0.02, antiderivative size = 72, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} = 0.062$, Rules used = {4433}

$$\frac{e \sin(d+ex) F^{c(a+bx)}}{b^2 c^2 \log^2(F) + e^2} + \frac{bc \log(F) \cos(d+ex) F^{c(a+bx)}}{b^2 c^2 \log^2(F) + e^2}$$

Antiderivative was successfully verified.

[In] Int[F^(c*(a+b*x))*Cos[d+e*x],x]

[Out] $(b*c*F^{(c*(a+b*x))*\cos[d+e*x]*\log[F]}/(e^2+b^2*c^2*\log[F]^2)+(e*F^{(c*(a+b*x))*\sin[d+e*x]}/(e^2+b^2*c^2*\log[F]^2))$

Rule 4433

Int[Cos[(d_.)+(e_.)*(x_)]*(F_)^(c_.*((a_.)+(b_.)*(x_))), x_Symbol] :>
Simp[(b*c*Log[F]*F^(c*(a+b*x))*Cos[d+e*x]/(e^2+b^2*c^2*Log[F]^2), x]
+ Simp[(e*F^(c*(a+b*x))*Sin[d+e*x]/(e^2+b^2*c^2*Log[F]^2), x] /; FreeQ[{F, a, b, c, d, e}, x] && NeQ[e^2+b^2*c^2*Log[F]^2, 0]

Rubi steps

$$\int F^{c(a+bx)} \cos(d+ex) dx = \frac{bc F^{c(a+bx)} \cos(d+ex) \log(F)}{e^2 + b^2 c^2 \log^2(F)} + \frac{e F^{c(a+bx)} \sin(d+ex)}{e^2 + b^2 c^2 \log^2(F)}$$

Mathematica [A] time = 0.11, size = 47, normalized size = 0.65

$$\frac{F^{c(a+bx)}(bc \log(F) \cos(d+ex) + e \sin(d+ex))}{b^2 c^2 \log^2(F) + e^2}$$

Antiderivative was successfully verified.

[In] Integrate[F^(c*(a+b*x))*Cos[d+e*x],x]

[Out] $(F^{(c*(a+b*x))*(b*c*\cos[d+e*x]*\log[F]+e*\sin[d+e*x])}/(e^2+b^2*c^2*\log[F]^2))$

fricas [A] time = 0.73, size = 48, normalized size = 0.67

$$\frac{(bc \cos(ex+d) \log(F) + e \sin(ex+d)) F^{bcx+ac}}{b^2 c^2 \log(F)^2 + e^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(F^(c*(b*x+a))*cos(e*x+d),x, algorithm="fricas")

[Out] $(b*c*\cos(e*x + d)*\log(F) + e*\sin(e*x + d))*F^{(b*c*x + a*c)}/(b^2*c^2*\log(F)^2 + e^2)$

giac [C] time = 0.26, size = 649, normalized size = 9.01

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(F^(c*(b*x+a))*cos(e*x+d),x, algorithm="giac")`

[Out] $(2*b*c*\cos(1/2*\pi*b*c*x*\text{sgn}(F) - 1/2*\pi*b*c*x + 1/2*\pi*a*c*\text{sgn}(F) - 1/2*\pi*a*c + x*e + d)*\log(\text{abs}(F))/(4*b^2*c^2*\log(\text{abs}(F))^2 + (\pi*b*c*\text{sgn}(F) - \pi*b*c + 2*e)^2) + (\pi*b*c*\text{sgn}(F) - \pi*b*c + 2*e)*\sin(1/2*\pi*b*c*x*\text{sgn}(F) - 1/2*\pi*b*c*x + 1/2*\pi*a*c*\text{sgn}(F) - 1/2*\pi*a*c + x*e + d)/(4*b^2*c^2*\log(\text{abs}(F))^2 + (\pi*b*c*\text{sgn}(F) - \pi*b*c + 2*e)^2)*e^{(b*c*x*\log(\text{abs}(F)) + a*c*\log(\text{abs}(F)))} + (2*b*c*\cos(1/2*\pi*b*c*x*\text{sgn}(F) - 1/2*\pi*b*c*x + 1/2*\pi*a*c*\text{sgn}(F) - 1/2*\pi*a*c - x*e - d)*\log(\text{abs}(F))/(4*b^2*c^2*\log(\text{abs}(F))^2 + (\pi*b*c*\text{sgn}(F) - \pi*b*c - 2*e)^2) + (\pi*b*c*\text{sgn}(F) - \pi*b*c - 2*e)*\sin(1/2*\pi*b*c*x*\text{sgn}(F) - 1/2*\pi*b*c*x + 1/2*\pi*a*c*\text{sgn}(F) - 1/2*\pi*a*c - x*e - d)/(4*b^2*c^2*\log(\text{abs}(F))^2 + (\pi*b*c*\text{sgn}(F) - \pi*b*c - 2*e)^2)*e^{(b*c*x*\log(\text{abs}(F)) + a*c*\log(\text{abs}(F)))} - 1/2*I*(-2*I*e^{(1/2*I*\pi*b*c*x*\text{sgn}(F) - 1/2*I*\pi*b*c*x + 1/2*I*\pi*a*c*\text{sgn}(F) - 1/2*I*\pi*a*c + I*x*e + I*d)/(2*I*\pi*b*c*\text{sgn}(F) - 2*I*\pi*b*c + 4*b*c*\log(\text{abs}(F)) + 4*I*e)} + 2*I*e^{(-1/2*I*\pi*b*c*x*\text{sgn}(F) + 1/2*I*\pi*b*c*x - 1/2*I*\pi*a*c*\text{sgn}(F) + 1/2*I*\pi*a*c - I*x*e - I*d)/(-2*I*\pi*b*c*\text{sgn}(F) + 2*I*\pi*b*c + 4*b*c*\log(\text{abs}(F)) - 4*I*e)})*e^{(b*c*x*\log(\text{abs}(F)) + a*c*\log(\text{abs}(F)))} - 1/2*I*(-2*I*e^{(1/2*I*\pi*b*c*x*\text{sgn}(F) - 1/2*I*\pi*b*c*x + 1/2*I*\pi*a*c*\text{sgn}(F) - 1/2*I*\pi*a*c - I*x*e - I*d)/(2*I*\pi*b*c*\text{sgn}(F) - 2*I*\pi*b*c + 4*b*c*\log(\text{abs}(F)) - 4*I*e)} + 2*I*e^{(-1/2*I*\pi*b*c*x*\text{sgn}(F) + 1/2*I*\pi*b*c*x - 1/2*I*\pi*a*c*\text{sgn}(F) + 1/2*I*\pi*a*c + I*x*e + I*d)/(-2*I*\pi*b*c*\text{sgn}(F) + 2*I*\pi*b*c + 4*b*c*\log(\text{abs}(F)) + 4*I*e)})*e^{(b*c*x*\log(\text{abs}(F)) + a*c*\log(\text{abs}(F)))}$

maple [A] time = 0.04, size = 133, normalized size = 1.85

$$\frac{\frac{bc \ln(F) e^{c(bx+a) \ln(F)}}{e^2 + b^2 c^2 \ln(F)^2} + \frac{2e e^{c(bx+a) \ln(F)} \tan\left(\frac{d}{2} + \frac{ex}{2}\right)}{e^2 + b^2 c^2 \ln(F)^2} - \frac{bc \ln(F) e^{c(bx+a) \ln(F)} \left(\tan^2\left(\frac{d}{2} + \frac{ex}{2}\right)\right)}{e^2 + b^2 c^2 \ln(F)^2}}{1 + \tan^2\left(\frac{d}{2} + \frac{ex}{2}\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(F^(c*(b*x+a))*cos(e*x+d),x)`

[Out] $(b*c*\ln(F)/(e^2+b^2*c^2*\ln(F)^2)*\exp(c*(b*x+a)*\ln(F))+2/(e^2+b^2*c^2*\ln(F)^2)*e*\exp(c*(b*x+a)*\ln(F))*\tan(1/2*d+1/2*e*x)-b*c*\ln(F)/(e^2+b^2*c^2*\ln(F)^2)*\exp(c*(b*x+a)*\ln(F))*\tan(1/2*d+1/2*e*x)^2)/(1+\tan(1/2*d+1/2*e*x)^2)$

maxima [B] time = 0.34, size = 192, normalized size = 2.67

$$\frac{(F^{ac}bc \cos(d) \log(F) - F^{ac}e \sin(d))F^{bcx} \cos(ex + 2d) + (F^{ac}bc \cos(d) \log(F) + F^{ac}e \sin(d))F^{bcx} \cos(ex) + (F^{ac}bc \cos(d) \log(F) - F^{ac}e \sin(d))F^{bcx} \cos(ex + 2d)}{2(b^2c^2 \cos(d)^2 \log(F)^2 + b^2c^2 \log(F)^2 \sin(d)^2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(F^(c*(b*x+a))*cos(e*x+d),x, algorithm="maxima")`

[Out] $1/2*((F^{(a*c)}*b*c*\cos(d)*\log(F) - F^{(a*c)}*e*\sin(d))*F^{(b*c*x)}*\cos(e*x + 2*d) + (F^{(a*c)}*b*c*\cos(d)*\log(F) + F^{(a*c)}*e*\sin(d))*F^{(b*c*x)}*\cos(e*x) + (F^{(a*c)}*b*c*\log(F)*\sin(d) + F^{(a*c)}*e*\cos(d))*F^{(b*c*x)}*\sin(e*x + 2*d) - (F^{(a*c)}*b*c*\log(F)*\sin(d) - F^{(a*c)}*e*\cos(d))*F^{(b*c*x)}*\sin(e*x))/(b^2*c^2*\cos(d)^2*\log(F)^2 + b^2*c^2*\log(F)^2*\sin(d)^2 + (\cos(d)^2 + \sin(d)^2)*e^2)$

mupad [B] time = 2.36, size = 48, normalized size = 0.67

$$\frac{F^{ac+bcx} (e \sin(d+ex) + bc \cos(d+ex) \ln(F))}{b^2 c^2 \ln(F)^2 + e^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(F^(c*(a + b*x))*cos(d + e*x), x)`

[Out] `(F^(a*c + b*c*x)*(e*sin(d + e*x) + b*c*cos(d + e*x)*log(F)))/(e^2 + b^2*c^2*log(F)^2)`

sympy [A] time = 7.86, size = 352, normalized size = 4.89

$$\left\{ \begin{array}{ll} -\frac{(-1)^{ac}(-1)^{\frac{ex}{\pi}} ix \sin(d+ex)}{2} + \frac{(-1)^{ac}(-1)^{\frac{ex}{\pi}} x \cos(d+ex)}{2} + \frac{(-1)^{ac}(-1)^{\frac{ex}{\pi}} \sin(d+ex)}{e} + \frac{(-1)^{ac}(-1)^{\frac{ex}{\pi}} i \cos(d+ex)}{2e} & \text{for } F = -1 \wedge b = \frac{e}{\pi c} \\ x \cos(d) & \text{for } F = 1 \wedge e = 0 \\ \tilde{\infty} e \left(e^{-\frac{ie}{bc}} \right)^{ac} \left(e^{-\frac{ie}{bc}} \right)^{bcx} \sin(d+ex) + \tilde{\infty} e \left(e^{-\frac{ie}{bc}} \right)^{ac} \left(e^{-\frac{ie}{bc}} \right)^{bcx} \cos(d+ex) & \text{for } F = e^{-\frac{ie}{bc}} \\ \tilde{\infty} e \left(e^{\frac{ie}{bc}} \right)^{ac} \left(e^{\frac{ie}{bc}} \right)^{bcx} \sin(d+ex) + \tilde{\infty} e \left(e^{\frac{ie}{bc}} \right)^{ac} \left(e^{\frac{ie}{bc}} \right)^{bcx} \cos(d+ex) & \text{for } F = e^{\frac{ie}{bc}} \\ \frac{F^{ac} F^{bcx} bc \log(F) \cos(d+ex)}{b^2 c^2 \log(F)^2 + e^2} + \frac{F^{ac} F^{bcx} e \sin(d+ex)}{b^2 c^2 \log(F)^2 + e^2} & \text{otherwise} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(F**(c*(b*x+a))*cos(e*x+d), x)`

[Out] `Piecewise((-(-1)**(a*c)*(-1)**(e*x/pi)*I*x*sin(d + e*x)/2 + (-1)**(a*c)*(-1)**(e*x/pi)*x*cos(d + e*x)/2 + (-1)**(a*c)*(-1)**(e*x/pi)*sin(d + e*x)/e + (-1)**(a*c)*(-1)**(e*x/pi)*I*cos(d + e*x)/(2*e), Eq(F, -1) & Eq(b, e/(pi*c))), (x*cos(d), Eq(F, 1) & Eq(e, 0)), (zoo*e*exp(-I*e/(b*c))**(a*c)*exp(-I*e/(b*c))**(b*c*x)*sin(d + e*x) + zoo*e*exp(-I*e/(b*c))**(a*c)*exp(-I*e/(b*c))**(b*c*x)*cos(d + e*x), Eq(F, exp(-I*e/(b*c)))), (zoo*e*exp(I*e/(b*c))**(a*c)*exp(I*e/(b*c))**(b*c*x)*sin(d + e*x) + zoo*e*exp(I*e/(b*c))**(a*c)*exp(I*e/(b*c))**(b*c*x)*cos(d + e*x), Eq(F, exp(I*e/(b*c)))), (F**(a*c)*F**(b*c*x)*b*c*log(F)*cos(d + e*x)/(b**2*c**2*log(F)**2 + e**2) + F**(a*c)*F**(b*c*x)*e*sin(d + e*x)/(b**2*c**2*log(F)**2 + e**2), True))`

3.14 $\int F^{c(a+bx)} \sec(d+ex) dx$

Optimal. Leaf size=84

$$\frac{2e^{i(d+ex)} F^{c(a+bx)} {}_2F_1\left(1, \frac{e-ibc \log(F)}{2e}; \frac{1}{2} \left(3 - \frac{ibc \log(F)}{e}\right); -e^{2i(d+ex)}\right)}{bc \log(F) + ie}$$

[Out] $2*\exp(I*(e*x+d))*F^{(c*(b*x+a))*\text{hypergeom}([1, 1/2*(e-I*b*c*\ln(F))/e], [3/2-1/2*I*b*c*\ln(F)/e], -\exp(2*I*(e*x+d)))/(b*c*\ln(F)+I*e)}$

Rubi [A] time = 0.02, antiderivative size = 84, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} = 0.062$, Rules used = {4451}

$$\frac{2e^{i(d+ex)} F^{c(a+bx)} {}_2F_1\left(1, \frac{e-ibc \log(F)}{2e}; \frac{1}{2} \left(3 - \frac{ibc \log(F)}{e}\right); -e^{2i(d+ex)}\right)}{bc \log(F) + ie}$$

Antiderivative was successfully verified.

[In] Int[F^(c*(a + b*x))*Sec[d + e*x], x]

[Out] $(2*E^{(I*(d + e*x))*F^{(c*(a + b*x))*\text{Hypergeometric2F1}[1, (e - I*b*c*\text{Log}[F])/(2*e), (3 - (I*b*c*\text{Log}[F])/e)/2, -E^{((2*I)*(d + e*x))}]/(I*e + b*c*\text{Log}[F])}$

Rule 4451

Int[(F_)^((c_.)*((a_.) + (b_.)*(x_)))*Sec[(d_.) + (e_.)*(x_)]^(n_.), x_Symbol] :> Simp[(2^n*E^(I*n*(d + e*x))*F^(c*(a + b*x))*Hypergeometric2F1[n, n/2 - (I*b*c*Log[F])/(2*e), 1 + n/2 - (I*b*c*Log[F])/(2*e), -E^(2*I*(d + e*x))]/(I*e*n + b*c*Log[F]), x] /; FreeQ[{F, a, b, c, d, e}, x] && IntegerQ[n]

Rubi steps

$$\int F^{c(a+bx)} \sec(d+ex) dx = \frac{2e^{i(d+ex)} F^{c(a+bx)} {}_2F_1\left(1, \frac{e-ibc \log(F)}{2e}; \frac{1}{2} \left(3 - \frac{ibc \log(F)}{e}\right); -e^{2i(d+ex)}\right)}{ie + bc \log(F)}$$

Mathematica [A] time = 0.02, size = 84, normalized size = 1.00

$$\frac{2e^{i(d+ex)} F^{c(a+bx)} {}_2F_1\left(1, \frac{1}{2} - \frac{ibc \log(F)}{2e}; \frac{3}{2} - \frac{ibc \log(F)}{2e}; -e^{2i(d+ex)}\right)}{bc \log(F) + ie}$$

Antiderivative was successfully verified.

[In] Integrate[F^(c*(a + b*x))*Sec[d + e*x], x]

[Out] $(2*E^{(I*(d + e*x))*F^{(c*(a + b*x))*\text{Hypergeometric2F1}[1, 1/2 - ((I/2)*b*c*\text{Log}[F])/e, 3/2 - ((I/2)*b*c*\text{Log}[F])/e, -E^{((2*I)*(d + e*x))}]/(I*e + b*c*\text{Log}[F])}$

fricas [F] time = 0.59, size = 0, normalized size = 0.00

$$\text{integral}\left(F^{bcx+ac} \sec(ex + d), x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(F^(c*(b*x+a))*sec(e*x+d),x, algorithm="fricas")

[Out] integral(F^(b*c*x + a*c)*sec(e*x + d), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int F^{(bx+a)c} \sec(ex + d) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(F^(c*(b*x+a))*sec(e*x+d),x, algorithm="giac")

[Out] integrate(F^((b*x + a)*c)*sec(e*x + d), x)

maple [F] time = 0.10, size = 0, normalized size = 0.00

$$\int F^{c(bx+a)} \sec(ex + d) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(F^(c*(b*x+a))*sec(e*x+d),x)

[Out] int(F^(c*(b*x+a))*sec(e*x+d),x)

maxima [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(F^(c*(b*x+a))*sec(e*x+d),x, algorithm="maxima")

[Out] Timed out

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{F^{c(a+bx)}}{\cos(d + ex)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(F^(c*(a + b*x))/cos(d + e*x),x)

[Out] int(F^(c*(a + b*x))/cos(d + e*x), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int F^{c(a+bx)} \sec(d + ex) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(F**(c*(b*x+a))*sec(e*x+d),x)

[Out] Integral(F**(c*(a + b*x))*sec(d + e*x), x)

3.15 $\int F^{c(a+bx)} \sec^2(d+ex) dx$

Optimal. Leaf size=80

$$\frac{4e^{2i(d+ex)} F^{c(a+bx)} {}_2F_1\left(2, 1 - \frac{ibc \log(F)}{2e}; 2 - \frac{ibc \log(F)}{2e}; -e^{2i(d+ex)}\right)}{bc \log(F) + 2ie}$$

[Out] $4*\exp(2*I*(e*x+d))*F^{(c*(b*x+a))*\text{hypergeom}([2, 1-1/2*I*b*c*\ln(F)/e], [2-1/2*I*b*c*\ln(F)/e], -\exp(2*I*(e*x+d)))/(2*I*e+b*c*\ln(F))$

Rubi [A] time = 0.02, antiderivative size = 80, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.056$, Rules used = {4451}

$$\frac{4e^{2i(d+ex)} F^{c(a+bx)} {}_2F_1\left(2, 1 - \frac{ibc \log(F)}{2e}; 2 - \frac{ibc \log(F)}{2e}; -e^{2i(d+ex)}\right)}{bc \log(F) + 2ie}$$

Antiderivative was successfully verified.

[In] Int[F^(c*(a + b*x))*Sec[d + e*x]^2,x]

[Out] $(4*E^{((2*I)*(d + e*x))*F^{(c*(a + b*x))*\text{Hypergeometric2F1}[2, 1 - ((I/2)*b*c*\text{Log}[F])/e, 2 - ((I/2)*b*c*\text{Log}[F])/e, -E^{((2*I)*(d + e*x))}]/((2*I)*e + b*c*\text{Log}[F])$

Rule 4451

Int[(F_)^(c_.*((a_.) + (b_.)*(x_)))*Sec[(d_.) + (e_.)*(x_)]^(n_.), x_Symbol] :> Simp[(2^n*E^(I*n*(d + e*x))*F^(c*(a + b*x))*Hypergeometric2F1[n, n/2 - (I*b*c*Log[F])/(2*e), 1 + n/2 - (I*b*c*Log[F])/(2*e), -E^(2*I*(d + e*x))]/(I*e*n + b*c*Log[F]), x] /; FreeQ[{F, a, b, c, d, e}, x] && IntegerQ[n]

Rubi steps

$$\int F^{c(a+bx)} \sec^2(d+ex) dx = \frac{4e^{2i(d+ex)} F^{c(a+bx)} {}_2F_1\left(2, 1 - \frac{ibc \log(F)}{2e}; 2 - \frac{ibc \log(F)}{2e}; -e^{2i(d+ex)}\right)}{2ie + bc \log(F)}$$

Mathematica [A] time = 0.01, size = 80, normalized size = 1.00

$$\frac{4e^{2i(d+ex)} F^{c(a+bx)} {}_2F_1\left(2, 1 - \frac{ibc \log(F)}{2e}; 2 - \frac{ibc \log(F)}{2e}; -e^{2i(d+ex)}\right)}{bc \log(F) + 2ie}$$

Antiderivative was successfully verified.

[In] Integrate[F^(c*(a + b*x))*Sec[d + e*x]^2,x]

[Out] $(4*E^{((2*I)*(d + e*x))*F^{(c*(a + b*x))*\text{Hypergeometric2F1}[2, 1 - ((I/2)*b*c*\text{Log}[F])/e, 2 - ((I/2)*b*c*\text{Log}[F])/e, -E^{((2*I)*(d + e*x))}]/((2*I)*e + b*c*\text{Log}[F])$

fricas [F] time = 1.27, size = 0, normalized size = 0.00

$$\text{integral}\left(F^{bcx+ac} \sec(ex+d)^2, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(F^(c*(b*x+a))*sec(e*x+d)^2,x, algorithm="fricas")

[Out] integral(F^(b*c*x + a*c)*sec(e*x + d)^2, x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int F^{(bx+a)c} \sec^2(ex + d) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(F^(c*(b*x+a))*sec(e*x+d)^2,x, algorithm="giac")

[Out] integrate(F^((b*x + a)*c)*sec(e*x + d)^2, x)

maple [F] time = 0.16, size = 0, normalized size = 0.00

$$\int F^{c(bx+a)} (\sec^2(ex + d)) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(F^(c*(b*x+a))*sec(e*x+d)^2,x)

[Out] int(F^(c*(b*x+a))*sec(e*x+d)^2,x)

maxima [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(F^(c*(b*x+a))*sec(e*x+d)^2,x, algorithm="maxima")

[Out] Timed out

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{F^{c(a+bx)}}{\cos(d + ex)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(F^(c*(a + b*x))/cos(d + e*x)^2,x)

[Out] int(F^(c*(a + b*x))/cos(d + e*x)^2, x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int F^{c(a+bx)} \sec^2(d + ex) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(F**(c*(b*x+a))*sec(e*x+d)**2,x)

[Out] Integral(F**(c*(a + b*x))*sec(d + e*x)**2, x)

3.16 $\int F^{c(a+bx)} \sec^3(d+ex) dx$

Optimal. Leaf size=141

$$\frac{e^{i(d+ex)} F^{c(a+bx)} (-bc \log(F) + ie) {}_2F_1\left(1, \frac{e-ibc \log(F)}{2e}; \frac{1}{2} \left(3 - \frac{ibc \log(F)}{e}\right); -e^{2i(d+ex)}\right)}{e^2} - \frac{bc \log(F) \sec(d+ex) F^{c(a+bx)}}{2e^2} + \dots$$

[Out] $-\exp(I*(e*x+d))*F^{c*(b*x+a)}*\text{hypergeom}\left([1, 1/2*(e-I*b*c*\ln(F))/e], [3/2-1/2*I*b*c*\ln(F)/e], -\exp(2*I*(e*x+d))\right)*(I*e-b*c*\ln(F))/e^2-1/2*b*c*F^{c*(b*x+a)}*\ln(F)*\sec(e*x+d)/e^2+1/2*F^{c*(b*x+a)}*\sec(e*x+d)*\tan(e*x+d)/e$

Rubi [A] time = 0.05, antiderivative size = 141, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {4448, 4451}

$$\frac{e^{i(d+ex)} F^{c(a+bx)} (-bc \log(F) + ie) {}_2F_1\left(1, \frac{e-ibc \log(F)}{2e}; \frac{1}{2} \left(3 - \frac{ibc \log(F)}{e}\right); -e^{2i(d+ex)}\right)}{e^2} - \frac{bc \log(F) \sec(d+ex) F^{c(a+bx)}}{2e^2} + \dots$$

Antiderivative was successfully verified.

[In] Int[F^(c*(a + b*x))*Sec[d + e*x]^3,x]

[Out] $-\left(\left(E^{\left(I*(d+e*x)\right)}*F^{c*(a+b*x)}*\text{Hypergeometric2F1}\left[1, \left(\frac{e-I*b*c*\text{Log}[F]}{2e}\right), \left(3-\left(\frac{I*b*c*\text{Log}[F]}{e}\right)/2, -E^{\left((2*I)*(d+e*x)\right)}*\left(I*e-b*c*\text{Log}[F]\right)\right)/e^2\right]-\left(b*c*F^{c*(a+b*x)}*\text{Log}[F]*\text{Sec}[d+e*x]\right)/\left(2*e^2\right)+\left(F^{c*(a+b*x)}*\text{Sec}[d+e*x]*\text{Tan}[d+e*x]\right)/\left(2*e\right)\right)$

Rule 4448

Int[(F_)^((c_.)*((a_.)+(b_.)*(x_)))*Sec[(d_.)+(e_.)*(x_)]^(n_), x_Symbol] :> -Simp[(b*c*Log[F]*F^(c*(a+b*x))*Sec[d+e*x]^(n-2))/(e^2*(n-1)*(n-2)), x] + (Dist[(e^2*(n-2)^2 + b^2*c^2*Log[F]^2)/(e^2*(n-1)*(n-2)), Int[F^(c*(a+b*x))*Sec[d+e*x]^(n-2), x], x] + Simp[(F^(c*(a+b*x))*Sec[d+e*x]^(n-1)*Sin[d+e*x])/(e*(n-1)), x]) /; FreeQ[{F, a, b, c, d, e}, x] && NeQ[b^2*c^2*Log[F]^2 + e^2*(n-2)^2, 0] && GtQ[n, 1] && NeQ[n, 2]

Rule 4451

Int[(F_)^((c_.)*((a_.)+(b_.)*(x_)))*Sec[(d_.)+(e_.)*(x_)]^(n_.), x_Symbol] :> Simp[(2^n*E^(I*n*(d+e*x))*F^(c*(a+b*x))*Hypergeometric2F1[n, n/2 - (I*b*c*Log[F])/(2*e), 1 + n/2 - (I*b*c*Log[F])/(2*e), -E^(2*I*(d+e*x))]/(I*e*n + b*c*Log[F]), x] /; FreeQ[{F, a, b, c, d, e}, x] && IntegerQ[n]

Rubi steps

$$\int F^{c(a+bx)} \sec^3(d+ex) dx = -\frac{bc F^{c(a+bx)} \log(F) \sec(d+ex)}{2e^2} + \frac{F^{c(a+bx)} \sec(d+ex) \tan(d+ex)}{2e} + \frac{1}{2} \left(1 + \frac{b^2 c^2 \log(F)}{e^2}\right) - \frac{e^{i(d+ex)} F^{c(a+bx)} {}_2F_1\left(1, \frac{e-ibc \log(F)}{2e}; \frac{1}{2} \left(3 - \frac{ibc \log(F)}{e}\right); -e^{2i(d+ex)}\right) (ie - bc \log(F))}{e^2} - \dots$$

Mathematica [A] time = 0.29, size = 112, normalized size = 0.79

$$\frac{F^{c(a+bx)} \left(\sec(d+ex) (e \tan(d+ex) - bc \log(F)) + 2e^{i(d+ex)} (bc \log(F) - ie) {}_2F_1\left(1, \frac{e-ibc \log(F)}{2e}; \frac{3}{2} - \frac{ibc \log(F)}{2e}; -e^{2i(d+ex)}\right) \right)}{2e^2}$$

Antiderivative was successfully verified.

[In] Integrate[F^(c*(a + b*x))*Sec[d + e*x]^3,x]

[Out] (F^(c*(a + b*x))*(2*E^(I*(d + e*x))*Hypergeometric2F1[1, (e - I*b*c*Log[F])/(2*e), 3/2 - ((I/2)*b*c*Log[F])/e, -E^((2*I)*(d + e*x))]*((-I)*e + b*c*Log[F]) + Sec[d + e*x]*(-(b*c*Log[F]) + e*Tan[d + e*x])))/(2*e^2)

fricas [F] time = 0.65, size = 0, normalized size = 0.00

$$\text{integral}\left(F^{bcx+ac} \sec(ex+d)^3, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(F^(c*(b*x+a))*sec(e*x+d)^3,x, algorithm="fricas")

[Out] integral(F^(b*c*x + a*c)*sec(e*x + d)^3, x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int F^{(bx+a)c} \sec(ex+d)^3 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(F^(c*(b*x+a))*sec(e*x+d)^3,x, algorithm="giac")

[Out] integrate(F^((b*x + a)*c)*sec(e*x + d)^3, x)

maple [F] time = 0.30, size = 0, normalized size = 0.00

$$\int F^{c(bx+a)} (\sec^3(ex+d)) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(F^(c*(b*x+a))*sec(e*x+d)^3,x)

[Out] int(F^(c*(b*x+a))*sec(e*x+d)^3,x)

maxima [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(F^(c*(b*x+a))*sec(e*x+d)^3,x, algorithm="maxima")

[Out] Timed out

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{F^{c(a+bx)}}{\cos(d+ex)^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(F^(c*(a + b*x))/cos(d + e*x)^3,x)

[Out] int(F^(c*(a + b*x))/cos(d + e*x)^3, x)

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(F**(c*(b*x+a))*sec(e*x+d)**3,x)

[Out] Timed out

3.17 $\int F^{c(a+bx)} \sec^4(d+ex) dx$

Optimal. Leaf size=143

$$\frac{2e^{2i(d+ex)}F^{c(a+bx)}(-bc \log(F) + 2ie) {}_2F_1\left(2, 1 - \frac{ibc \log(F)}{2e}; 2 - \frac{ibc \log(F)}{2e}; -e^{2i(d+ex)}\right)}{3e^2} - \frac{bc \log(F) \sec^2(d+ex)F^{c(a+bx)}}{6e^2}$$

[Out] $-2/3*\exp(2*I*(e*x+d))*F^{c*(b*x+a)}*\text{hypergeom}([2, 1-1/2*I*b*c*\ln(F)/e], [2-1/2*I*b*c*\ln(F)/e], -\exp(2*I*(e*x+d)))*(2*I*e-b*c*\ln(F))/e^2-1/6*b*c*F^{c*(b*x+a)}*\ln(F)*\sec(e*x+d)^2/e^2+1/3*F^{c*(b*x+a)}*\sec(e*x+d)^2*\tan(e*x+d)/e$

Rubi [A] time = 0.05, antiderivative size = 143, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {4448, 4451}

$$\frac{2e^{2i(d+ex)}F^{c(a+bx)}(-bc \log(F) + 2ie) {}_2F_1\left(2, 1 - \frac{ibc \log(F)}{2e}; 2 - \frac{ibc \log(F)}{2e}; -e^{2i(d+ex)}\right)}{3e^2} - \frac{bc \log(F) \sec^2(d+ex)F^{c(a+bx)}}{6e^2}$$

Antiderivative was successfully verified.

[In] Int[F^(c*(a + b*x))*Sec[d + e*x]^4, x]

[Out] $(-2*E^{((2*I)*(d + e*x))*F^{c*(a + b*x)}*Hypergeometric2F1[2, 1 - ((I/2)*b*c*Log[F])/e, 2 - ((I/2)*b*c*Log[F])/e, -E^{((2*I)*(d + e*x))}*((2*I)*e - b*c*Log[F])]/(3*e^2) - (b*c*F^{c*(a + b*x)}*Log[F]*Sec[d + e*x]^2)/(6*e^2) + (F^{c*(a + b*x)}*Sec[d + e*x]^2*Tan[d + e*x])/(3*e)$

Rule 4448

Int[(F_)^((c_.)*((a_.) + (b_.)*(x_)))*Sec[(d_.) + (e_.)*(x_)]^(n_), x_Symbol] :> -Simp[(b*c*Log[F]*F^(c*(a + b*x))*Sec[d + e*x]^(n - 2))/(e^2*(n - 1)*(n - 2)), x] + (Dist[(e^2*(n - 2)^2 + b^2*c^2*Log[F]^2)/(e^2*(n - 1)*(n - 2)), Int[F^(c*(a + b*x))*Sec[d + e*x]^(n - 2), x], x] + Simp[(F^(c*(a + b*x))*Sec[d + e*x]^(n - 1)*Sin[d + e*x])/(e*(n - 1)), x]) /; FreeQ[{F, a, b, c, d, e}, x] && NeQ[b^2*c^2*Log[F]^2 + e^2*(n - 2)^2, 0] && GtQ[n, 1] && NeQ[n, 2]

Rule 4451

Int[(F_)^((c_.)*((a_.) + (b_.)*(x_)))*Sec[(d_.) + (e_.)*(x_)]^(n_.), x_Symbol] :> Simp[(2^n*E^(I*n*(d + e*x))*F^(c*(a + b*x))*Hypergeometric2F1[n, n/2 - (I*b*c*Log[F])/(2*e), 1 + n/2 - (I*b*c*Log[F])/(2*e), -E^(2*I*(d + e*x))]/(I*e*n + b*c*Log[F]), x] /; FreeQ[{F, a, b, c, d, e}, x] && IntegerQ[n]

Rubi steps

$$\int F^{c(a+bx)} \sec^4(d+ex) dx = -\frac{bcF^{c(a+bx)} \log(F) \sec^2(d+ex)}{6e^2} + \frac{F^{c(a+bx)} \sec^2(d+ex) \tan(d+ex)}{3e} + \frac{1}{6} \left(4 + \frac{b^2c^2}{6} \right) \\ = -\frac{2e^{2i(d+ex)}F^{c(a+bx)} {}_2F_1\left(2, 1 - \frac{ibc \log(F)}{2e}; 2 - \frac{ibc \log(F)}{2e}; -e^{2i(d+ex)}\right) (2ie - bc \log(F))}{3e^2} - \frac{bc \log(F) \sec^2(d+ex)F^{c(a+bx)}}{6e^2}$$

Mathematica [A] time = 0.21, size = 111, normalized size = 0.78

$$\frac{F^{c(a+bx)} \left(\sec^2(d+ex)(2e \tan(d+ex) - bc \log(F)) + 4e^{2i(d+ex)}(bc \log(F) - 2ie) {}_2F_1\left(2, 1 - \frac{ibc \log(F)}{2e}; 2 - \frac{ibc \log(F)}{2e}; -e^{2i(d+ex)}\right) (2ie - bc \log(F)) \right)}{6e^2}$$

Antiderivative was successfully verified.

[In] Integrate[F^(c*(a + b*x))*Sec[d + e*x]^4,x]

[Out] (F^(c*(a + b*x))*(4*E^((2*I)*(d + e*x))*Hypergeometric2F1[2, 1 - ((I/2)*b*c*Log[F])/e, 2 - ((I/2)*b*c*Log[F])/e, -E^((2*I)*(d + e*x))]*((-2*I)*e + b*c*Log[F]) + Sec[d + e*x]^2*(-(b*c*Log[F]) + 2*e*Tan[d + e*x])))/(6*e^2)

fricas [F] time = 3.20, size = 0, normalized size = 0.00

$$\text{integral}\left(F^{bcx+ac} \sec(ex+d)^4, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(F^(c*(b*x+a))*sec(e*x+d)^4,x, algorithm="fricas")

[Out] integral(F^(b*c*x + a*c)*sec(e*x + d)^4, x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int F^{(bx+a)c} \sec(ex+d)^4 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(F^(c*(b*x+a))*sec(e*x+d)^4,x, algorithm="giac")

[Out] integrate(F^((b*x + a)*c)*sec(e*x + d)^4, x)

maple [F] time = 0.35, size = 0, normalized size = 0.00

$$\int F^{c(bx+a)} (\sec^4(ex+d)) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(F^(c*(b*x+a))*sec(e*x+d)^4,x)

[Out] int(F^(c*(b*x+a))*sec(e*x+d)^4,x)

maxima [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(F^(c*(b*x+a))*sec(e*x+d)^4,x, algorithm="maxima")

[Out] Timed out

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{F^{c(a+bx)}}{\cos(d+ex)^4} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(F^(c*(a + b*x))/cos(d + e*x)^4,x)

[Out] int(F^(c*(a + b*x))/cos(d + e*x)^4, x)

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(F**(c*(b*x+a))*sec(e*x+d)**4,x)

[Out] Timed out

3.18 $\int e^x \cos^4(x) dx$

Optimal. Leaf size=54

$$\frac{24e^x}{85} + \frac{1}{17}e^x \cos^4(x) + \frac{12}{85}e^x \cos^2(x) + \frac{4}{17}e^x \sin(x) \cos^3(x) + \frac{24}{85}e^x \sin(x) \cos(x)$$

[Out] 24/85*exp(x)+12/85*exp(x)*cos(x)^2+1/17*exp(x)*cos(x)^4+24/85*exp(x)*cos(x)*sin(x)+4/17*exp(x)*cos(x)^3*sin(x)

Rubi [A] time = 0.03, antiderivative size = 54, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 2, integrand size = 8, $\frac{\text{number of rules}}{\text{integrand size}} = 0.250$, Rules used = {4435, 2194}

$$\frac{24e^x}{85} + \frac{1}{17}e^x \cos^4(x) + \frac{12}{85}e^x \cos^2(x) + \frac{4}{17}e^x \sin(x) \cos^3(x) + \frac{24}{85}e^x \sin(x) \cos(x)$$

Antiderivative was successfully verified.

[In] Int[E^x*Cos[x]^4,x]

[Out] (24*E^x)/85 + (12*E^x*Cos[x]^2)/85 + (E^x*Cos[x]^4)/17 + (24*E^x*Cos[x]*Sin[x])/85 + (4*E^x*Cos[x]^3*Sin[x])/17

Rule 2194

Int[((F_)^((c_.)*((a_.) + (b_.)*(x_))))^(n_.), x_Symbol] :> Simp[(F^(c*(a + b*x)))^n/(b*c*n*Log[F]), x] /; FreeQ[{F, a, b, c, n}, x]

Rule 4435

Int[Cos[(d_.) + (e_.)*(x_)]^(m_)*(F_)^((c_.)*((a_.) + (b_.)*(x_))), x_Symbol] :> Simp[(b*c*Log[F]*F^(c*(a + b*x))*Cos[d + e*x]^m)/(e^2*m^2 + b^2*c^2*Log[F]^2), x] + (Dist[(m*(m - 1)*e^2)/(e^2*m^2 + b^2*c^2*Log[F]^2), Int[F^(c*(a + b*x))*Cos[d + e*x]^(m - 2), x], x] + Simp[(e*m*F^(c*(a + b*x))*Sin[d + e*x]*Cos[d + e*x]^(m - 1))/(e^2*m^2 + b^2*c^2*Log[F]^2), x]) /; FreeQ[{F, a, b, c, d, e}, x] && NeQ[e^2*m^2 + b^2*c^2*Log[F]^2, 0] && GtQ[m, 1]

Rubi steps

$$\begin{aligned} \int e^x \cos^4(x) dx &= \frac{1}{17}e^x \cos^4(x) + \frac{4}{17}e^x \cos^3(x) \sin(x) + \frac{12}{17} \int e^x \cos^2(x) dx \\ &= \frac{12}{85}e^x \cos^2(x) + \frac{1}{17}e^x \cos^4(x) + \frac{24}{85}e^x \cos(x) \sin(x) + \frac{4}{17}e^x \cos^3(x) \sin(x) + \frac{24}{85} \int e^x dx \\ &= \frac{24e^x}{85} + \frac{12}{85}e^x \cos^2(x) + \frac{1}{17}e^x \cos^4(x) + \frac{24}{85}e^x \cos(x) \sin(x) + \frac{4}{17}e^x \cos^3(x) \sin(x) \end{aligned}$$

Mathematica [A] time = 0.03, size = 33, normalized size = 0.61

$$\frac{1}{680}e^x(136 \sin(2x) + 20 \sin(4x) + 68 \cos(2x) + 5 \cos(4x) + 255)$$

Antiderivative was successfully verified.

[In] Integrate[E^x*Cos[x]^4,x]

[Out] (E^x*(255 + 68*Cos[2*x] + 5*Cos[4*x] + 136*Sin[2*x] + 20*Sin[4*x]))/680

fricas [A] time = 0.64, size = 36, normalized size = 0.67

$$\frac{4}{85} (5 \cos(x)^3 + 6 \cos(x)) e^x \sin(x) + \frac{1}{85} (5 \cos(x)^4 + 12 \cos(x)^2 + 24) e^x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(x)*cos(x)^4,x, algorithm="fricas")

[Out] 4/85*(5*cos(x)^3 + 6*cos(x))*e^x*sin(x) + 1/85*(5*cos(x)^4 + 12*cos(x)^2 + 24)*e^x

giac [A] time = 0.13, size = 35, normalized size = 0.65

$$\frac{1}{136} (\cos(4x) + 4 \sin(4x)) e^x + \frac{1}{10} (\cos(2x) + 2 \sin(2x)) e^x + \frac{3}{8} e^x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(x)*cos(x)^4,x, algorithm="giac")

[Out] 1/136*(cos(4*x) + 4*sin(4*x))*e^x + 1/10*(cos(2*x) + 2*sin(2*x))*e^x + 3/8*e^x

maple [A] time = 0.03, size = 34, normalized size = 0.63

$$\frac{(\cos(x) + 4 \sin(x)) e^x (\cos^3(x))}{17} + \frac{12 (\cos(x) + 2 \sin(x)) e^x \cos(x)}{85} + \frac{24 e^x}{85}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(exp(x)*cos(x)^4,x)

[Out] 1/17*(cos(x)+4*sin(x))*exp(x)*cos(x)^3+12/85*(cos(x)+2*sin(x))*exp(x)*cos(x)+24/85*exp(x)

maxima [A] time = 0.33, size = 37, normalized size = 0.69

$$\frac{1}{136} \cos(4x) e^x + \frac{1}{10} \cos(2x) e^x + \frac{1}{34} e^x \sin(4x) + \frac{1}{5} e^x \sin(2x) + \frac{3}{8} e^x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(x)*cos(x)^4,x, algorithm="maxima")

[Out] 1/136*cos(4*x)*e^x + 1/10*cos(2*x)*e^x + 1/34*e^x*sin(4*x) + 1/5*e^x*sin(2*x) + 3/8*e^x

mupad [B] time = 0.04, size = 41, normalized size = 0.76

$$\frac{3 e^x}{8} + \frac{e^x \left(\frac{4 \cos(2x)}{5} + \frac{8 \sin(2x)}{5} + \frac{2 \cos(2x)^2}{17} + \frac{8 \cos(2x) \sin(2x)}{17} - \frac{1}{17} \right)}{8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(exp(x)*cos(x)^4,x)

[Out] (3*exp(x))/8 + (exp(x)*((4*cos(2*x))/5 + (8*sin(2*x))/5 + (2*cos(2*x)^2)/17 + (8*cos(2*x)*sin(2*x))/17 - 1/17))/8

sympy [A] time = 3.71, size = 70, normalized size = 1.30

$$\frac{24e^x \sin^4(x)}{85} + \frac{24e^x \sin^3(x) \cos(x)}{85} + \frac{12e^x \sin^2(x) \cos^2(x)}{17} + \frac{44e^x \sin(x) \cos^3(x)}{85} + \frac{41e^x \cos^4(x)}{85}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(x)*cos(x)**4,x)
```

```
[Out] 24*exp(x)*sin(x)**4/85 + 24*exp(x)*sin(x)**3*cos(x)/85 + 12*exp(x)*sin(x)**  
2*cos(x)**2/17 + 44*exp(x)*sin(x)*cos(x)**3/85 + 41*exp(x)*cos(x)**4/85
```

3.19 $\int e^{c(a+bx)} \tan^3(d+ex) dx$

Optimal. Leaf size=194

$$\frac{6ie^{c(a+bx)} {}_2F_1\left(1, -\frac{ibc}{2e}; 1 - \frac{ibc}{2e}; -e^{2i(d+ex)}\right)}{bc} + \frac{12ie^{c(a+bx)} {}_2F_1\left(2, -\frac{ibc}{2e}; 1 - \frac{ibc}{2e}; -e^{2i(d+ex)}\right)}{bc} - \frac{8ie^{c(a+bx)} {}_2F_1\left(3, -\frac{ibc}{2e}; 1 - \frac{ibc}{2e}\right)}{bc}$$

[Out] $I*\exp(c*(b*x+a))/b/c-6*I*\exp(c*(b*x+a))*\text{hypergeom}([1, -1/2*I*b*c/e], [1-1/2*I*b*c/e], -\exp(2*I*(e*x+d)))/b/c+12*I*\exp(c*(b*x+a))*\text{hypergeom}([2, -1/2*I*b*c/e], [1-1/2*I*b*c/e], -\exp(2*I*(e*x+d)))/b/c-8*I*\exp(c*(b*x+a))*\text{hypergeom}([3, -1/2*I*b*c/e], [1-1/2*I*b*c/e], -\exp(2*I*(e*x+d)))/b/c$

Rubi [A] time = 0.20, antiderivative size = 194, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 3, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.167$, Rules used = {4442, 2194, 2251}

$$\frac{6ie^{c(a+bx)} {}_2F_1\left(1, -\frac{ibc}{2e}; 1 - \frac{ibc}{2e}; -e^{2i(d+ex)}\right)}{bc} + \frac{12ie^{c(a+bx)} {}_2F_1\left(2, -\frac{ibc}{2e}; 1 - \frac{ibc}{2e}; -e^{2i(d+ex)}\right)}{bc} - \frac{8ie^{c(a+bx)} {}_2F_1\left(3, -\frac{ibc}{2e}; 1 - \frac{ibc}{2e}\right)}{bc}$$

Antiderivative was successfully verified.

[In] Int[E^(c*(a + b*x))*Tan[d + e*x]^3,x]

[Out] $(I*E^{(c*(a + b*x))})/(b*c) - ((6*I)*E^{(c*(a + b*x))}*\text{Hypergeometric2F1}[1, ((-I/2)*b*c)/e, 1 - ((I/2)*b*c)/e, -E^{((2*I)*(d + e*x))})/(b*c) + ((12*I)*E^{(c*(a + b*x))}*\text{Hypergeometric2F1}[2, ((-I/2)*b*c)/e, 1 - ((I/2)*b*c)/e, -E^{((2*I)*(d + e*x))})/(b*c) - ((8*I)*E^{(c*(a + b*x))}*\text{Hypergeometric2F1}[3, ((-I/2)*b*c)/e, 1 - ((I/2)*b*c)/e, -E^{((2*I)*(d + e*x))})/(b*c)$

Rule 2194

Int[((F_)^((c_.)*((a_.) + (b_.)*(x_))))^(n_.), x_Symbol] := Simp[(F^(c*(a + b*x)))^n/(b*c*n*Log[F]), x] /; FreeQ[{F, a, b, c, n}, x]

Rule 2251

Int[((a_) + (b_.)*(F_)^((e_.)*((c_.) + (d_.)*(x_))))^(p_)*(G_)^((h_.)*(f_.) + (g_.)*(x_)), x_Symbol] := Simp[(a^p*G^(h*(f + g*x))*Hypergeometric2F1[-p, (g*h*Log[G])/(d*e*Log[F]), (g*h*Log[G])/(d*e*Log[F]) + 1, Simplify[-((b*F^(e*(c + d*x)))/a])])/(g*h*Log[G]), x] /; FreeQ[{F, G, a, b, c, d, e, f, g, h, p}, x] && (ILtQ[p, 0] || GtQ[a, 0])

Rule 4442

Int[(F_)^((c_.)*((a_.) + (b_.)*(x_)))*Tan[(d_.) + (e_.)*(x_)]^(n_.), x_Symbol] := Dist[I^n, Int[ExpandIntegrand[(F^(c*(a + b*x)))*(1 - E^(2*I*(d + e*x)))^n]/(1 + E^(2*I*(d + e*x)))^n, x], x] /; FreeQ[{F, a, b, c, d, e}, x] && IntegerQ[n]

Rubi steps

$$\begin{aligned} \int e^{c(a+bx)} \tan^3(d+ex) dx &= - \left(i \int \left(-e^{c(a+bx)} + \frac{8e^{c(a+bx)}}{(1+e^{2i(d+ex)})^3} - \frac{12e^{c(a+bx)}}{(1+e^{2i(d+ex)})^2} + \frac{6e^{c(a+bx)}}{1+e^{2i(d+ex)}} \right) dx \right) \\ &= i \int e^{c(a+bx)} dx - 6i \int \frac{e^{c(a+bx)}}{1+e^{2i(d+ex)}} dx - 8i \int \frac{e^{c(a+bx)}}{(1+e^{2i(d+ex)})^3} dx + 12i \int \frac{e^{c(a+bx)}}{(1+e^{2i(d+ex)})^2} dx \\ &= \frac{ie^{c(a+bx)}}{bc} - \frac{6ie^{c(a+bx)} {}_2F_1\left(1, -\frac{ibc}{2e}; 1 - \frac{ibc}{2e}; -e^{2i(d+ex)}\right)}{bc} + \frac{12ie^{c(a+bx)} {}_2F_1\left(2, -\frac{ibc}{2e}; 1 - \frac{ibc}{2e}; -e^{2i(d+ex)}\right)}{bc} \end{aligned}$$

Mathematica [A] time = 2.14, size = 212, normalized size = 1.09

$$\frac{1}{2} e^{c(a+bx)} \left(\frac{2e^{2id} (b^2c^2 - 2e^2) \left(bce^{2iex} {}_2F_1\left(1, 1 - \frac{ibc}{2e}; 2 - \frac{ibc}{2e}; -e^{2i(d+ex)}\right) - (bc + 2ie) {}_2F_1\left(1, -\frac{ibc}{2e}; 1 - \frac{ibc}{2e}; -e^{2i(d+ex)}\right) \right)}{bc (1 + e^{2id}) e^2 (-2e + ibc)} \right)$$

Antiderivative was successfully verified.

[In] Integrate[E^(c*(a + b*x))*Tan[d + e*x]^3,x]

[Out] (E^(c*(a + b*x))*((2*(b^2*c^2 - 2*e^2)*E^((2*I)*d)*(b*c*E^((2*I)*e*x))*Hypergeometric2F1[1, 1 - ((I/2)*b*c)/e, 2 - ((I/2)*b*c)/e, -E^((2*I)*(d + e*x))] - (b*c + (2*I)*e)*Hypergeometric2F1[1, ((-1/2*I)*b*c)/e, 1 - ((I/2)*b*c)/e, -E^((2*I)*(d + e*x))]))/(b*c*(I*b*c - 2*e)*e^2*(1 + E^((2*I)*d))) + Sec[d + e*x]^2/e - (b*c*Sec[d]*Sec[d + e*x]*Sin[e*x])/e^2 - (2*Tan[d])/(b*c))/2

fricas [F] time = 0.72, size = 0, normalized size = 0.00

$$\text{integral}\left(e^{(bcx+ac)} \tan(ex+d)^3, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(c*(b*x+a))*tan(e*x+d)^3,x, algorithm="fricas")

[Out] integral(e^(b*c*x + a*c)*tan(e*x + d)^3, x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int e^{(bx+a)c} \tan(ex+d)^3 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(c*(b*x+a))*tan(e*x+d)^3,x, algorithm="giac")

[Out] integrate(e^((b*x + a)*c)*tan(e*x + d)^3, x)

maple [F] time = 0.25, size = 0, normalized size = 0.00

$$\int e^{c(bx+a)} (\tan^3(ex+d)) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(exp(c*(b*x+a))*tan(e*x+d)^3,x)

[Out] int(exp(c*(b*x+a))*tan(e*x+d)^3,x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\frac{4e \cos(2ex + 2d)^2 e^{(bcx+ac)} - bce^{(bcx+ac)} \sin(2ex + 2d) + 4ee^{(bcx+ac)} \sin(2ex + 2d)^2 + 2e \cos(2ex + 2d) e^{(bcx+ac)}}{1}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(c*(b*x+a))*tan(e*x+d)^3,x, algorithm="maxima")

[Out] (4*e*cos(2*e*x + 2*d)^2*e^(b*c*x + a*c) - b*c*e^(b*c*x + a*c)*sin(2*e*x + 2*d) + 4*e*e^(b*c*x + a*c)*sin(2*e*x + 2*d)^2 + 2*e*cos(2*e*x + 2*d)*e^(b*c*x + a*c) + (b*c*e^(b*c*x + a*c)*sin(2*e*x + 2*d) + 2*e*cos(2*e*x + 2*d)*e^(b*c*x + a*c))*cos(4*e*x + 4*d) + (b^2*c^2*e^4*e^(a*c) - 2*e^6*e^(a*c) + (b^2*c^2*e^4*e^(a*c) - 2*e^6*e^(a*c))*cos(4*e*x + 4*d)^2 + 4*(b^2*c^2*e^4*e^(a*c) - 2*e^6*e^(a*c))*cos(2*e*x + 2*d)^2 + (b^2*c^2*e^4*e^(a*c) - 2*e^6*e^(a*c))*sin(4*e*x + 4*d)^2 + 4*(b^2*c^2*e^4*e^(a*c) - 2*e^6*e^(a*c))*sin(4*e*x + 4*d)*sin(2*e*x + 2*d) + 4*(b^2*c^2*e^4*e^(a*c) - 2*e^6*e^(a*c))*sin(2*e*x + 2*d)^2 + 2*(b^2*c^2*e^4*e^(a*c) - 2*e^6*e^(a*c) + 2*(b^2*c^2*e^4*e^(a*c) - 2*e^6*e^(a*c))*cos(2*e*x + 2*d))*cos(4*e*x + 4*d) + 4*(b^2*c^2*e^4*e^(a*c) - 2*e^6*e^(a*c))*cos(2*e*x + 2*d))*integrate(e^(b*c*x)*sin(2*e*x + 2*d)/(e^4*cos(2*e*x + 2*d)^2 + e^4*sin(2*e*x + 2*d)^2 + 2*e^4*cos(2*e*x + 2*d) + e^4), x) - (b*c*cos(2*e*x + 2*d)*e^(b*c*x + a*c) + b*c*e^(b*c*x + a*c) - 2*e*e^(b*c*x + a*c)*sin(2*e*x + 2*d))*sin(4*e*x + 4*d))/(e^2*cos(4*e*x + 4*d)^2 + 4*e^2*cos(2*e*x + 2*d)^2 + e^2*sin(4*e*x + 4*d)^2 + 4*e^2*sin(4*e*x + 4*d)*sin(2*e*x + 2*d) + 4*e^2*sin(2*e*x + 2*d)^2 + 4*e^2*cos(2*e*x + 2*d) + e^2 + 2*(2*e^2*cos(2*e*x + 2*d) + e^2)*cos(4*e*x + 4*d))

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int e^{c(a+bx)} \tan(d+ex)^3 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(exp(c*(a + b*x))*tan(d + e*x)^3,x)

[Out] int(exp(c*(a + b*x))*tan(d + e*x)^3, x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$e^{ac} \int e^{bcx} \tan^3(d+ex) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(c*(b*x+a))*tan(e*x+d)**3,x)

[Out] exp(a*c)*Integral(exp(b*c*x)*tan(d + e*x)**3, x)

3.20 $\int e^{c(a+bx)} \tan^2(d+ex) dx$

Optimal. Leaf size=130

$$\frac{4e^{c(a+bx)} {}_2F_1\left(1, -\frac{ibc}{2e}; 1 - \frac{ibc}{2e}; -e^{2i(d+ex)}\right)}{bc} - \frac{4e^{c(a+bx)} {}_2F_1\left(2, -\frac{ibc}{2e}; 1 - \frac{ibc}{2e}; -e^{2i(d+ex)}\right)}{bc} - \frac{e^{c(a+bx)}}{bc}$$

[Out] $-\exp(c*(b*x+a))/b/c+4*\exp(c*(b*x+a))*\text{hypergeom}([1, -1/2*I*b*c/e], [1-1/2*I*b*c/e], -\exp(2*I*(e*x+d)))/b/c-4*\exp(c*(b*x+a))*\text{hypergeom}([2, -1/2*I*b*c/e], [1-1/2*I*b*c/e], -\exp(2*I*(e*x+d)))/b/c$

Rubi [A] time = 0.13, antiderivative size = 130, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 3, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.167$, Rules used = {4442, 2194, 2251}

$$\frac{4e^{c(a+bx)} {}_2F_1\left(1, -\frac{ibc}{2e}; 1 - \frac{ibc}{2e}; -e^{2i(d+ex)}\right)}{bc} - \frac{4e^{c(a+bx)} {}_2F_1\left(2, -\frac{ibc}{2e}; 1 - \frac{ibc}{2e}; -e^{2i(d+ex)}\right)}{bc} - \frac{e^{c(a+bx)}}{bc}$$

Antiderivative was successfully verified.

[In] Int[E^(c*(a + b*x))*Tan[d + e*x]^2, x]

[Out] $-(E^{c*(a + b*x)})/(b*c) + (4*E^{c*(a + b*x)}*\text{Hypergeometric2F1}[1, ((-I/2)*b*c)/e, 1 - ((I/2)*b*c)/e, -E^{((2*I)*(d + e*x))}]/(b*c) - (4*E^{c*(a + b*x)})*\text{Hypergeometric2F1}[2, ((-I/2)*b*c)/e, 1 - ((I/2)*b*c)/e, -E^{((2*I)*(d + e*x))}]/(b*c)$

Rule 2194

Int[((F_)^((c_.)*((a_.) + (b_.)*(x_))))^(n_.), x_Symbol] := Simp[(F^(c*(a + b*x)))^n/(b*c*n*Log[F]), x] /; FreeQ[{F, a, b, c, n}, x]

Rule 2251

Int[((a_) + (b_.)*(F_)^((e_.)*((c_.) + (d_.)*(x_))))^(p_)*(G_)^((h_.)*((f_.) + (g_.)*(x_))), x_Symbol] := Simp[(a^p*G^(h*(f + g*x))*Hypergeometric2F1[-p, (g*h*Log[G])/(d*e*Log[F]), (g*h*Log[G])/(d*e*Log[F]) + 1, Simplify[-((b*F^(e*(c + d*x)))/a])]/(g*h*Log[G]), x] /; FreeQ[{F, G, a, b, c, d, e, f, g, h, p}, x] && (ILtQ[p, 0] || GtQ[a, 0])

Rule 4442

Int[(F_)^((c_.)*((a_.) + (b_.)*(x_)))*Tan[(d_.) + (e_.)*(x_)]^(n_.), x_Symbol] := Dist[I^n, Int[ExpandIntegrand[(F^(c*(a + b*x)))*(1 - E^(2*I*(d + e*x)))^n]/(1 + E^(2*I*(d + e*x)))^n, x], x] /; FreeQ[{F, a, b, c, d, e}, x] && IntegerQ[n]

Rubi steps

$$\begin{aligned} \int e^{c(a+bx)} \tan^2(d+ex) dx &= - \int \left(e^{c(a+bx)} + \frac{4e^{c(a+bx)}}{(1 + e^{2i(d+ex)})^2} - \frac{4e^{c(a+bx)}}{1 + e^{2i(d+ex)}} \right) dx \\ &= - \left(4 \int \frac{e^{c(a+bx)}}{(1 + e^{2i(d+ex)})^2} dx \right) + 4 \int \frac{e^{c(a+bx)}}{1 + e^{2i(d+ex)}} dx - \int e^{c(a+bx)} dx \\ &= -\frac{e^{c(a+bx)}}{bc} + \frac{4e^{c(a+bx)} {}_2F_1\left(1, -\frac{ibc}{2e}; 1 - \frac{ibc}{2e}; -e^{2i(d+ex)}\right)}{bc} - \frac{4e^{c(a+bx)} {}_2F_1\left(2, -\frac{ibc}{2e}; 1 - \frac{ibc}{2e}; -e^{2i(d+ex)}\right)}{bc} \end{aligned}$$

Mathematica [A] time = 1.67, size = 174, normalized size = 1.34

$$e^{c(a+bx)} \left(\frac{2ie^{2id} \left(bce^{2iex} {}_2F_1 \left(1, 1 - \frac{ibc}{2e}; 2 - \frac{ibc}{2e}; -e^{2i(d+ex)} \right) - (bc + 2ie) {}_2F_1 \left(1, -\frac{ibc}{2e}; 1 - \frac{ibc}{2e}; -e^{2i(d+ex)} \right) \right)}{(1 + e^{2id}) e(bc + 2ie)} - \frac{1}{bc} + \frac{\sec(d)}{e} \right)$$

Antiderivative was successfully verified.

[In] Integrate[E^(c*(a + b*x))*Tan[d + e*x]^2,x]

[Out] E^(c*(a + b*x))*(-1/(b*c)) + ((2*I)*E^((2*I)*d)*(b*c*E^((2*I)*e*x)*Hypergeometric2F1[1, 1 - ((I/2)*b*c)/e, 2 - ((I/2)*b*c)/e, -E^((2*I)*(d + e*x))] - (b*c + (2*I)*e)*Hypergeometric2F1[1, ((-1/2*I)*b*c)/e, 1 - ((I/2)*b*c)/e, -E^((2*I)*(d + e*x))])/(b*c + (2*I)*e)*e*(1 + E^((2*I)*d)) + (Sec[d]*Sec[d + e*x]*Sin[e*x])/e

fricas [F] time = 0.74, size = 0, normalized size = 0.00

$$\text{integral}(e^{(bcx+ac)} \tan(ex + d)^2, x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(c*(b*x+a))*tan(e*x+d)^2,x, algorithm="fricas")

[Out] integral(e^(b*c*x + a*c)*tan(e*x + d)^2, x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int e^{(bx+a)c} \tan(ex + d)^2 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(c*(b*x+a))*tan(e*x+d)^2,x, algorithm="giac")

[Out] integrate(e^((b*x + a)*c)*tan(e*x + d)^2, x)

maple [F] time = 0.14, size = 0, normalized size = 0.00

$$\int e^{c(bx+a)} (\tan^2(ex + d)) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(exp(c*(b*x+a))*tan(e*x+d)^2,x)

[Out] int(exp(c*(b*x+a))*tan(e*x+d)^2,x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\frac{e \cos(2ex + 2d)^2 e^{(bcx+ac)} - 2bce^{(bcx+ac)} \sin(2ex + 2d) + ee^{(bcx+ac)} \sin(2ex + 2d)^2 + 2e \cos(2ex + 2d) e^{(bcx+ac)}}{bce \cos(2ex + 2d)^2 + bce \sin(2ex + 2d)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(c*(b*x+a))*tan(e*x+d)^2,x, algorithm="maxima")

[Out] -(e*cos(2*e*x + 2*d)^2*e^(b*c*x + a*c) - 2*b*c*e^(b*c*x + a*c)*sin(2*e*x + 2*d) + e*e^(b*c*x + a*c)*sin(2*e*x + 2*d)^2 + 2*e*cos(2*e*x + 2*d)*e^(b*c*x + a*c) + e*e^(b*c*x + a*c) + 2*(b^2*c^2*e^2*cos(2*e*x + 2*d)^2 + b^2*c^2*e^2*sin(2*e*x + 2*d)^2 + 2*b^2*c^2*e^2*cos(2*e*x + 2*d) + b^2*c^2*e^2)*integrate(e^(b*c*x + a*c)*sin(2*e*x + 2*d)/(e^2*cos(2*e*x + 2*d)^2 + e^2*sin(2*e*x + 2*d)^2), x)

$(x + 2d)^2 + 2e^2 \cos(2ex + 2d) + e^2, x) / (bce \cos(2ex + 2d)^2 + bce \sin(2ex + 2d)^2 + 2bce \cos(2ex + 2d) + bce)$

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int e^{c(a+bx)} \tan(d+ex)^2 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(exp(c*(a + b*x))*tan(d + e*x)^2,x)

[Out] int(exp(c*(a + b*x))*tan(d + e*x)^2, x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$e^{ac} \int e^{bcx} \tan^2(d+ex) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(c*(b*x+a))*tan(e*x+d)**2,x)

[Out] exp(a*c)*Integral(exp(b*c*x)*tan(d + e*x)**2, x)

3.21 $\int e^{c(a+bx)} \tan(d+ex) dx$

Optimal. Leaf size=78

$$\frac{2ie^{c(a+bx)} {}_2F_1\left(1, -\frac{ibc}{2e}; 1 - \frac{ibc}{2e}; -e^{2i(d+ex)}\right)}{bc} - \frac{ie^{c(a+bx)}}{bc}$$

[Out] $-I*\exp(c*(b*x+a))/b/c+2*I*\exp(c*(b*x+a))*\text{hypergeom}([1, -1/2*I*b*c/e], [1-1/2*I*b*c/e], -\exp(2*I*(e*x+d)))/b/c$

Rubi [A] time = 0.08, antiderivative size = 78, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 3, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} = 0.188$, Rules used = {4442, 2194, 2251}

$$\frac{2ie^{c(a+bx)} {}_2F_1\left(1, -\frac{ibc}{2e}; 1 - \frac{ibc}{2e}; -e^{2i(d+ex)}\right)}{bc} - \frac{ie^{c(a+bx)}}{bc}$$

Antiderivative was successfully verified.

[In] Int[E^(c*(a + b*x))*Tan[d + e*x], x]

[Out] $((-I)*E^{c*(a + b*x)})/(b*c) + ((2*I)*E^{c*(a + b*x)})*\text{Hypergeometric2F1}[1, ((-I/2)*b*c)/e, 1 - ((I/2)*b*c)/e, -E^{((2*I)*(d + e*x))}]/(b*c)$

Rule 2194

Int[((F_)^((c_)*(a_) + (b_)*(x_)))^(n_), x_Symbol] :> Simp[(F^(c*(a + b*x)))^n/(b*c*n*Log[F]), x] /; FreeQ[{F, a, b, c, n}, x]

Rule 2251

Int[((a_) + (b_)*(F_)^(e_)*((c_) + (d_)*(x_)))^(p_)*(G_)^(h_)*((f_) + (g_)*(x_)), x_Symbol] :> Simp[(a^p*G^(h*(f + g*x))*Hypergeometric2F1[-p, (g*h*Log[G])/(d*e*Log[F]), (g*h*Log[G])/(d*e*Log[F]) + 1, Simplify[-((b*F^(e*(c + d*x)))/a])]/(g*h*Log[G]), x] /; FreeQ[{F, G, a, b, c, d, e, f, g, h, p}, x] && (ILtQ[p, 0] || GtQ[a, 0])

Rule 4442

Int[(F_)^(c_)*((a_) + (b_)*(x_))*Tan[(d_) + (e_)*(x_)]^(n_), x_Symbol] :> Dist[I^n, Int[ExpandIntegrand[(F^(c*(a + b*x)))*(1 - E^(2*I*(d + e*x)))^n]/(1 + E^(2*I*(d + e*x)))^n, x], x] /; FreeQ[{F, a, b, c, d, e}, x] && IntegerQ[n]

Rubi steps

$$\begin{aligned} \int e^{c(a+bx)} \tan(d+ex) dx &= i \int \left(-e^{c(a+bx)} + \frac{2e^{c(a+bx)}}{1 + e^{2i(d+ex)}} \right) dx \\ &= -\left(i \int e^{c(a+bx)} dx \right) + 2i \int \frac{e^{c(a+bx)}}{1 + e^{2i(d+ex)}} dx \\ &= -\frac{ie^{c(a+bx)}}{bc} + \frac{2ie^{c(a+bx)} {}_2F_1\left(1, -\frac{ibc}{2e}; 1 - \frac{ibc}{2e}; -e^{2i(d+ex)}\right)}{bc} \end{aligned}$$

Mathematica [B] time = 0.47, size = 166, normalized size = 2.13

$$\frac{e^{c(a+bx)} \left(2bce^{2i(d+ex)} {}_2F_1\left(1, 1 - \frac{ibc}{2e}; 2 - \frac{ibc}{2e}; -e^{2i(d+ex)}\right) - (bc + 2ie) \left(2e^{2id} {}_2F_1\left(1, -\frac{ibc}{2e}; 1 - \frac{ibc}{2e}; -e^{2i(d+ex)}\right) - e^{2id} + 1 \right) \right)}{bc(1 + e^{2id})(-2e + ibc)}$$

Antiderivative was successfully verified.

[In] Integrate[E^(c*(a + b*x))*Tan[d + e*x], x]

[Out] (E^(c*(a + b*x))*(2*b*c*E^((2*I)*(d + e*x))*Hypergeometric2F1[1, 1 - ((I/2)*b*c)/e, 2 - ((I/2)*b*c)/e, -E^((2*I)*(d + e*x))] - (b*c + (2*I)*e)*(1 - E^((2*I)*d) + 2*E^((2*I)*d))*Hypergeometric2F1[1, ((-1/2*I)*b*c)/e, 1 - ((I/2)*b*c)/e, -E^((2*I)*(d + e*x))]))/(b*c*(I*b*c - 2*e)*(1 + E^((2*I)*d)))

fricas [F] time = 1.02, size = 0, normalized size = 0.00

$$\text{integral}\left(e^{(bcx+ac)} \tan(ex + d), x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(c*(b*x+a))*tan(e*x+d), x, algorithm="fricas")

[Out] integral(e^(b*c*x + a*c)*tan(e*x + d), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int e^{(bx+a)c} \tan(ex + d) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(c*(b*x+a))*tan(e*x+d), x, algorithm="giac")

[Out] integrate(e^((b*x + a)*c)*tan(e*x + d), x)

maple [F] time = 0.13, size = 0, normalized size = 0.00

$$\int e^{c(bx+a)} \tan(ex + d) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(exp(c*(b*x+a))*tan(e*x+d), x)

[Out] int(exp(c*(b*x+a))*tan(e*x+d), x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int e^{(bx+a)c} \tan(ex + d) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(c*(b*x+a))*tan(e*x+d), x, algorithm="maxima")

[Out] integrate(e^((b*x + a)*c)*tan(e*x + d), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int e^{c(a+bx)} \tan(d + ex) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(exp(c*(a + b*x))*tan(d + e*x), x)

[Out] int(exp(c*(a + b*x))*tan(d + e*x), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$e^{ac} \int e^{bcx} \tan(d + ex) dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(c*(b*x+a))*tan(e*x+d),x)
```

```
[Out] exp(a*c)*Integral(exp(b*c*x)*tan(d + e*x), x)
```

3.22 $\int e^{c(a+bx)} \cot(d+ex) dx$

Optimal. Leaf size=76

$$\frac{ie^{c(a+bx)}}{bc} - \frac{2ie^{c(a+bx)} {}_2F_1\left(1, -\frac{ibc}{2e}; 1 - \frac{ibc}{2e}; e^{2i(d+ex)}\right)}{bc}$$

[Out] $I*\exp(c*(b*x+a))/b/c-2*I*\exp(c*(b*x+a))*\text{hypergeom}([1, -1/2*I*b*c/e], [1-1/2*I*b*c/e], \exp(2*I*(e*x+d)))/b/c$

Rubi [A] time = 0.08, antiderivative size = 76, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 3, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} = 0.188$, Rules used = {4443, 2194, 2251}

$$\frac{ie^{c(a+bx)}}{bc} - \frac{2ie^{c(a+bx)} {}_2F_1\left(1, -\frac{ibc}{2e}; 1 - \frac{ibc}{2e}; e^{2i(d+ex)}\right)}{bc}$$

Antiderivative was successfully verified.

[In] Int[E^(c*(a + b*x))*Cot[d + e*x], x]

[Out] $(I*E^{(c*(a + b*x))})/(b*c) - ((2*I)*E^{(c*(a + b*x))}*\text{Hypergeometric2F1}[1, ((-I/2)*b*c)/e, 1 - ((I/2)*b*c)/e, E^{((2*I)*(d + e*x))}])/b*c$

Rule 2194

Int[((F_)^((c_.)*((a_.) + (b_.)*(x_))))^(n_.), x_Symbol] := Simp[(F^(c*(a + b*x)))^n/(b*c*n*Log[F]), x] /; FreeQ[{F, a, b, c, n}, x]

Rule 2251

Int[((a_) + (b_.)*(F_)^(e_.)*((c_.) + (d_.)*(x_)))^(p_)*(G_)^(h_.)*((f_.) + (g_.)*(x_)), x_Symbol] := Simp[(a^p*G^(h*(f + g*x))*Hypergeometric2F1[-p, (g*h*Log[G])/(d*e*Log[F]), (g*h*Log[G])/(d*e*Log[F]) + 1, Simplify[-((b*F^(e*(c + d*x)))/a])])/(g*h*Log[G]), x] /; FreeQ[{F, G, a, b, c, d, e, f, g, h, p}, x] && (ILtQ[p, 0] || GtQ[a, 0])

Rule 4443

Int[Cot[(d_.) + (e_.)*(x_)]^(n_.)*(F_)^(c_.)*((a_.) + (b_.)*(x_)), x_Symbol] := Dist[(-I)^n, Int[ExpandIntegrand[(F^(c*(a + b*x)))*(1 + E^(2*I*(d + e*x)))^n]/(1 - E^(2*I*(d + e*x)))^n, x], x] /; FreeQ[{F, a, b, c, d, e}, x] && IntegerQ[n]

Rubi steps

$$\begin{aligned} \int e^{c(a+bx)} \cot(d+ex) dx &= -\left(i \int \left(-e^{c(a+bx)} - \frac{2e^{c(a+bx)}}{-1 + e^{2i(d+ex)}}\right) dx\right) \\ &= i \int e^{c(a+bx)} dx + 2i \int \frac{e^{c(a+bx)}}{-1 + e^{2i(d+ex)}} dx \\ &= \frac{ie^{c(a+bx)}}{bc} - \frac{2ie^{c(a+bx)} {}_2F_1\left(1, -\frac{ibc}{2e}; 1 - \frac{ibc}{2e}; e^{2i(d+ex)}\right)}{bc} \end{aligned}$$

Mathematica [B] time = 1.23, size = 163, normalized size = 2.14

$$\frac{e^{c(a+bx)} \left(2ibce^{2i(d+ex)} {}_2F_1\left(1, 1 - \frac{ibc}{2e}; 2 - \frac{ibc}{2e}; e^{2i(d+ex)}\right) + i(bc + 2ie) \left(-2e^{2id} {}_2F_1\left(1, -\frac{ibc}{2e}; 1 - \frac{ibc}{2e}; e^{2i(d+ex)}\right) + e^{2id} + 1\right)\right)}{bc(-1 + e^{2id})(bc + 2ie)}$$

Antiderivative was successfully verified.

[In] Integrate[E^(c*(a + b*x))*Cot[d + e*x],x]

[Out] (E^(c*(a + b*x))*((2*I)*b*c*E^((2*I)*(d + e*x))*Hypergeometric2F1[1, 1 - ((I/2)*b*c)/e, 2 - ((I/2)*b*c)/e, E^((2*I)*(d + e*x))] + I*(b*c + (2*I)*e)*(1 + E^((2*I)*d) - 2*E^((2*I)*d)*Hypergeometric2F1[1, ((-1/2*I)*b*c)/e, 1 - ((I/2)*b*c)/e, E^((2*I)*(d + e*x))]))/(b*c*(b*c + (2*I)*e)*(-1 + E^((2*I)*d)))

fricas [F] time = 0.58, size = 0, normalized size = 0.00

$$\text{integral}(\cot(ex + d)e^{(bcx+ac)}, x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(c*(b*x+a))*cot(e*x+d),x, algorithm="fricas")

[Out] integral(cot(e*x + d)*e^(b*c*x + a*c), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \cot(ex + d)e^{(bx+a)c} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(c*(b*x+a))*cot(e*x+d),x, algorithm="giac")

[Out] integrate(cot(e*x + d)*e^((b*x + a)*c), x)

maple [F] time = 0.18, size = 0, normalized size = 0.00

$$\int e^{c(bx+a)} \cot(ex + d) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(exp(c*(b*x+a))*cot(e*x+d),x)

[Out] int(exp(c*(b*x+a))*cot(e*x+d),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \cot(ex + d)e^{(bx+a)c} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(c*(b*x+a))*cot(e*x+d),x, algorithm="maxima")

[Out] integrate(cot(e*x + d)*e^((b*x + a)*c), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \cot(d + ex) e^{c(a+bx)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(cot(d + e*x)*exp(c*(a + b*x)),x)

[Out] int(cot(d + e*x)*exp(c*(a + b*x)), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$e^{ac} \int e^{bcx} \cot(d + ex) dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(c*(b*x+a))*cot(e*x+d), x)
```

```
[Out] exp(a*c)*Integral(exp(b*c*x)*cot(d + e*x), x)
```

3.23 $\int e^{c(a+bx)} \cot^2(d+ex) dx$

Optimal. Leaf size=126

$$\frac{4e^{c(a+bx)} {}_2F_1\left(1, -\frac{ibc}{2e}; 1 - \frac{ibc}{2e}; e^{2i(d+ex)}\right)}{bc} - \frac{4e^{c(a+bx)} {}_2F_1\left(2, -\frac{ibc}{2e}; 1 - \frac{ibc}{2e}; e^{2i(d+ex)}\right)}{bc} - \frac{e^{c(a+bx)}}{bc}$$

[Out] $-\exp(c*(b*x+a))/b/c+4*\exp(c*(b*x+a))*\text{hypergeom}([1, -1/2*I*b*c/e], [1-1/2*I*b*c/e], \exp(2*I*(e*x+d)))/b/c-4*\exp(c*(b*x+a))*\text{hypergeom}([2, -1/2*I*b*c/e], [1-1/2*I*b*c/e], \exp(2*I*(e*x+d)))/b/c$

Rubi [A] time = 0.12, antiderivative size = 126, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 3, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.167$, Rules used = {4443, 2194, 2251}

$$\frac{4e^{c(a+bx)} {}_2F_1\left(1, -\frac{ibc}{2e}; 1 - \frac{ibc}{2e}; e^{2i(d+ex)}\right)}{bc} - \frac{4e^{c(a+bx)} {}_2F_1\left(2, -\frac{ibc}{2e}; 1 - \frac{ibc}{2e}; e^{2i(d+ex)}\right)}{bc} - \frac{e^{c(a+bx)}}{bc}$$

Antiderivative was successfully verified.

[In] $\text{Int}[E^{(c*(a + b*x))*Cot[d + e*x]^2, x}$

[Out] $-(E^{(c*(a + b*x))}/(b*c)) + (4*E^{(c*(a + b*x))*Hypergeometric2F1[1, ((-I/2)*b*c)/e, 1 - ((I/2)*b*c)/e, E^{((2*I)*(d + e*x))}]/(b*c) - (4*E^{(c*(a + b*x))*Hypergeometric2F1[2, ((-I/2)*b*c)/e, 1 - ((I/2)*b*c)/e, E^{((2*I)*(d + e*x))}]/(b*c)$

Rule 2194

$\text{Int}[(F_)^{((c_.)*((a_.) + (b_.)*(x_)))}^{(n_.)}, x_Symbol] \rightarrow \text{Simp}[(F^{(c*(a + b*x)))^n/(b*c*n*\text{Log}[F]), x] /; \text{FreeQ}\{F, a, b, c, n\}, x]$

Rule 2251

$\text{Int}[(a_.) + (b_.)*(F_)^{((e_.)*((c_.) + (d_.)*(x_)))}^{(p_.)}*(G_)^{((h_.)*((f_.) + (g_.)*(x_)))}, x_Symbol] \rightarrow \text{Simp}[(a^p*G^{(h*(f + g*x))*Hypergeometric2F1[-p, (g*h*\text{Log}[G])/d*e*\text{Log}[F], (g*h*\text{Log}[G])/d*e*\text{Log}[F] + 1, \text{Simplify}[-((b*F^{(e*(c + d*x))})/a])]/(g*h*\text{Log}[G]), x] /; \text{FreeQ}\{F, G, a, b, c, d, e, f, g, h, p\}, x] \&\& (\text{ILtQ}[p, 0] \parallel \text{GtQ}[a, 0])$

Rule 4443

$\text{Int}[\text{Cot}[(d_.) + (e_.)*(x_)]^{(n_.)}*(F_)^{((c_.)*((a_.) + (b_.)*(x_)))}, x_Symbol] \rightarrow \text{Dist}[(-I)^n, \text{Int}[\text{ExpandIntegrand}[(F^{(c*(a + b*x))*}(1 + E^{(2*I*(d + e*x)))^n)/(1 - E^{(2*I*(d + e*x)))^n}, x], x] /; \text{FreeQ}\{F, a, b, c, d, e\}, x] \&\& \text{IntegerQ}[n]$

Rubi steps

$$\begin{aligned} \int e^{c(a+bx)} \cot^2(d+ex) dx &= - \int \left(e^{c(a+bx)} + \frac{4e^{c(a+bx)}}{(-1 + e^{2i(d+ex)})^2} + \frac{4e^{c(a+bx)}}{-1 + e^{2i(d+ex)}} \right) dx \\ &= - \left(4 \int \frac{e^{c(a+bx)}}{(-1 + e^{2i(d+ex)})^2} dx \right) - 4 \int \frac{e^{c(a+bx)}}{-1 + e^{2i(d+ex)}} dx - \int e^{c(a+bx)} dx \\ &= -\frac{e^{c(a+bx)}}{bc} + \frac{4e^{c(a+bx)} {}_2F_1\left(1, -\frac{ibc}{2e}; 1 - \frac{ibc}{2e}; e^{2i(d+ex)}\right)}{bc} - \frac{4e^{c(a+bx)} {}_2F_1\left(2, -\frac{ibc}{2e}; 1 - \frac{ibc}{2e}; e^{2i(d+ex)}\right)}{bc} \end{aligned}$$

Mathematica [A] time = 1.65, size = 170, normalized size = 1.35

$$e^{c(a+bx)} \left(\frac{2ie^{2id} \left((bc + 2ie) {}_2F_1 \left(1, -\frac{ibc}{2e}; 1 - \frac{ibc}{2e}; e^{2i(d+ex)} \right) - bce^{2iex} {}_2F_1 \left(1, 1 - \frac{ibc}{2e}; 2 - \frac{ibc}{2e}; e^{2i(d+ex)} \right) \right)}{(-1 + e^{2id}) e^{(bc + 2ie)}} - \frac{1}{bc} + \frac{\csc(d)}{e} \right)$$

Antiderivative was successfully verified.

[In] Integrate[E^(c*(a + b*x))*Cot[d + e*x]^2,x]

[Out] E^(c*(a + b*x))*(-1/(b*c)) - ((2*I)*E^((2*I)*d))*(-b*c*E^((2*I)*e*x)*Hypergeometric2F1[1, 1 - ((I/2)*b*c)/e, 2 - ((I/2)*b*c)/e, E^((2*I)*(d + e*x))]) + (b*c + (2*I)*e)*Hypergeometric2F1[1, ((-1/2*I)*b*c)/e, 1 - ((I/2)*b*c)/e, E^((2*I)*(d + e*x))])/(b*c + (2*I)*e)*e*(-1 + E^((2*I)*d)) + (Csc[d]*Csc[d + e*x]*Sin[e*x])/e

fricas [F] time = 0.40, size = 0, normalized size = 0.00

$$\text{integral}(\cot(ex + d)^2 e^{(bcx+ac)}, x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(c*(b*x+a))*cot(e*x+d)^2,x, algorithm="fricas")

[Out] integral(cot(e*x + d)^2*e^(b*c*x + a*c), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \cot(ex + d)^2 e^{(bx+a)c} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(c*(b*x+a))*cot(e*x+d)^2,x, algorithm="giac")

[Out] integrate(cot(e*x + d)^2*e^((b*x + a)*c), x)

maple [F] time = 0.19, size = 0, normalized size = 0.00

$$\int e^{c(bx+a)} (\cot^2(ex + d)) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(exp(c*(b*x+a))*cot(e*x+d)^2,x)

[Out] int(exp(c*(b*x+a))*cot(e*x+d)^2,x)

maxima [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(c*(b*x+a))*cot(e*x+d)^2,x, algorithm="maxima")

[Out] Timed out

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \cot(d + ex)^2 e^{c(a+bx)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(cot(d + e*x)^2*exp(c*(a + b*x)),x)
```

```
[Out] int(cot(d + e*x)^2*exp(c*(a + b*x)), x)
```

```
sympy [F] time = 0.00, size = 0, normalized size = 0.00
```

$$e^{ac} \int e^{bcx} \cot^2(d + ex) dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(c*(b*x+a))*cot(e*x+d)**2,x)
```

```
[Out] exp(a*c)*Integral(exp(b*c*x)*cot(d + e*x)**2, x)
```


3.24 $\int e^{c(a+bx)} \cot^3(d+ex) dx$

Optimal. Leaf size=188

$$\frac{6ie^{c(a+bx)} {}_2F_1\left(1, -\frac{ibc}{2e}; 1 - \frac{ibc}{2e}; e^{2i(d+ex)}\right)}{bc} - \frac{12ie^{c(a+bx)} {}_2F_1\left(2, -\frac{ibc}{2e}; 1 - \frac{ibc}{2e}; e^{2i(d+ex)}\right)}{bc} + \frac{8ie^{c(a+bx)} {}_2F_1\left(3, -\frac{ibc}{2e}; 1 - \frac{ibc}{2e}; e^{2i(d+ex)}\right)}{bc}$$

[Out] $-I*\exp(c*(b*x+a))/b/c+6*I*\exp(c*(b*x+a))*\text{hypergeom}([1, -1/2*I*b*c/e], [1-1/2*I*b*c/e], \exp(2*I*(e*x+d)))/b/c-12*I*\exp(c*(b*x+a))*\text{hypergeom}([2, -1/2*I*b*c/e], [1-1/2*I*b*c/e], \exp(2*I*(e*x+d)))/b/c+8*I*\exp(c*(b*x+a))*\text{hypergeom}([3, -1/2*I*b*c/e], [1-1/2*I*b*c/e], \exp(2*I*(e*x+d)))/b/c$

Rubi [A] time = 0.19, antiderivative size = 188, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 3, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.167$, Rules used = {4443, 2194, 2251}

$$\frac{6ie^{c(a+bx)} {}_2F_1\left(1, -\frac{ibc}{2e}; 1 - \frac{ibc}{2e}; e^{2i(d+ex)}\right)}{bc} - \frac{12ie^{c(a+bx)} {}_2F_1\left(2, -\frac{ibc}{2e}; 1 - \frac{ibc}{2e}; e^{2i(d+ex)}\right)}{bc} + \frac{8ie^{c(a+bx)} {}_2F_1\left(3, -\frac{ibc}{2e}; 1 - \frac{ibc}{2e}; e^{2i(d+ex)}\right)}{bc}$$

Antiderivative was successfully verified.

[In] Int[E^(c*(a + b*x))*Cot[d + e*x]^3, x]

[Out] $((-I)*E^{(c*(a + b*x))}/(b*c) + ((6*I)*E^{(c*(a + b*x))*\text{Hypergeometric2F1}[1, ((-I/2)*b*c)/e, 1 - ((I/2)*b*c)/e, E^{((2*I)*(d + e*x))}]} / (b*c) - ((12*I)*E^{(c*(a + b*x))*\text{Hypergeometric2F1}[2, ((-I/2)*b*c)/e, 1 - ((I/2)*b*c)/e, E^{((2*I)*(d + e*x))}]} / (b*c) + ((8*I)*E^{(c*(a + b*x))*\text{Hypergeometric2F1}[3, ((-I/2)*b*c)/e, 1 - ((I/2)*b*c)/e, E^{((2*I)*(d + e*x))}]} / (b*c)$

Rule 2194

Int[((F_)^((c_.)*((a_.) + (b_.)*(x_))))^(n_.), x_Symbol] :> Simp[(F^(c*(a + b*x)))^n/(b*c*n*Log[F]), x] /; FreeQ[{F, a, b, c, n}, x]

Rule 2251

Int[((a_) + (b_.)*(F_)^(e_.)*((c_.) + (d_.)*(x_)))^(p_)*(G_)^(h_.)*((f_.) + (g_.)*(x_)), x_Symbol] :> Simp[(a^p*G^(h*(f + g*x))*Hypergeometric2F1[-p, (g*h*Log[G])/(d*e*Log[F]), (g*h*Log[G])/(d*e*Log[F]) + 1, Simplify[-((b*F^(e*(c + d*x)))/a])]]/(g*h*Log[G]), x] /; FreeQ[{F, G, a, b, c, d, e, f, g, h, p}, x] && (ILtQ[p, 0] || GtQ[a, 0])

Rule 4443

Int[Cot[(d_.) + (e_.)*(x_)]^(n_.)*(F_)^(c_.)*((a_.) + (b_.)*(x_)), x_Symbol] :> Dist[(-I)^n, Int[ExpandIntegrand[(F^(c*(a + b*x))*(1 + E^(2*I*(d + e*x)))^n)/(1 - E^(2*I*(d + e*x)))^n, x], x] /; FreeQ[{F, a, b, c, d, e}, x] && IntegerQ[n]

Rubi steps

$$\begin{aligned} \int e^{c(a+bx)} \cot^3(d+ex) dx &= i \int \left(-e^{c(a+bx)} - \frac{8e^{c(a+bx)}}{(-1+e^{2i(d+ex)})^3} - \frac{12e^{c(a+bx)}}{(-1+e^{2i(d+ex)})^2} - \frac{6e^{c(a+bx)}}{-1+e^{2i(d+ex)}} \right) dx \\ &= -\left(i \int e^{c(a+bx)} dx \right) - 6i \int \frac{e^{c(a+bx)}}{-1+e^{2i(d+ex)}} dx - 8i \int \frac{e^{c(a+bx)}}{(-1+e^{2i(d+ex)})^3} dx - 12i \int \frac{e^{c(a+bx)}}{(-1+e^{2i(d+ex)})^2} dx \\ &= -\frac{ie^{c(a+bx)}}{bc} + \frac{6ie^{c(a+bx)} {}_2F_1\left(1, -\frac{ibc}{2e}; 1 - \frac{ibc}{2e}; e^{2i(d+ex)}\right)}{bc} - \frac{12ie^{c(a+bx)} {}_2F_1\left(2, -\frac{ibc}{2e}; 1 - \frac{ibc}{2e}; e^{2i(d+ex)}\right)}{bc} \end{aligned}$$

Mathematica [A] time = 2.18, size = 210, normalized size = 1.12

$$\frac{1}{2}e^{c(a+bx)} \left(\frac{2e^{2id}(b^2c^2 - 2e^2) \left(ibce^{2iex} {}_2F_1\left(1, 1 - \frac{ibc}{2e}; 2 - \frac{ibc}{2e}; e^{2i(d+ex)}\right) + (2e - ibc) {}_2F_1\left(1, -\frac{ibc}{2e}; 1 - \frac{ibc}{2e}; e^{2i(d+ex)}\right) \right)}{bc(-1+e^{2id})e^2(bc+2ie)} + \dots \right)$$

Antiderivative was successfully verified.

[In] Integrate[E^(c*(a + b*x))*Cot[d + e*x]^3,x]

[Out] (E^(c*(a + b*x))*((-2*Cot[d])/(b*c) - Csc[d + e*x]^2/e + (2*(b^2*c^2 - 2*e^2)*E^((2*I)*d)*(I*b*c*E^((2*I)*e*x)*Hypergeometric2F1[1, 1 - ((I/2)*b*c)/e, 2 - ((I/2)*b*c)/e, E^((2*I)*(d + e*x))]) + ((-I)*b*c + 2*e)*Hypergeometric2F1[1, ((-1/2*I)*b*c)/e, 1 - ((I/2)*b*c)/e, E^((2*I)*(d + e*x))]))/(b*c*(b*c + (2*I)*e)*e^2*(-1 + E^((2*I)*d))) + (b*c*Csc[d]*Csc[d + e*x]*Sin[e*x])/e^2)/2

fricas [F] time = 0.42, size = 0, normalized size = 0.00

$$\text{integral}(\cot(ex + d)^3 e^{(bcx+ac)}, x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(c*(b*x+a))*cot(e*x+d)^3,x, algorithm="fricas")

[Out] integral(cot(e*x + d)^3*e^(b*c*x + a*c), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \cot(ex + d)^3 e^{(bx+a)c} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(c*(b*x+a))*cot(e*x+d)^3,x, algorithm="giac")

[Out] integrate(cot(e*x + d)^3*e^((b*x + a)*c), x)

maple [F] time = 0.28, size = 0, normalized size = 0.00

$$\int e^{c(bx+a)} (\cot^3(ex + d)) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(exp(c*(b*x+a))*cot(e*x+d)^3,x)

[Out] int(exp(c*(b*x+a))*cot(e*x+d)^3,x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(c*(b*x+a))*cot(e*x+d)^3,x, algorithm="maxima")

[Out] $-(4*e*\cos(2*e*x + 2*d)^2*e^{(b*c*x + a*c)} + b*c*e^{(b*c*x + a*c)}*\sin(2*e*x + 2*d) + 4*e*e^{(b*c*x + a*c)}*\sin(2*e*x + 2*d)^2 - 2*e*\cos(2*e*x + 2*d)*e^{(b*c*x + a*c)} - (b*c*e^{(b*c*x + a*c)}*\sin(2*e*x + 2*d) + 2*e*\cos(2*e*x + 2*d)*e^{(b*c*x + a*c)})*\cos(4*e*x + 4*d) + 2*(b^2*c^2*e^4*e^{(a*c)} - 2*e^6*e^{(a*c)} + (b^2*c^2*e^4*e^{(a*c)} - 2*e^6*e^{(a*c)}))*\cos(4*e*x + 4*d)^2 + 4*(b^2*c^2*e^4*e^{(a*c)} - 2*e^6*e^{(a*c)})*\cos(2*e*x + 2*d)^2 + (b^2*c^2*e^4*e^{(a*c)} - 2*e^6*e^{(a*c)})*\sin(4*e*x + 4*d)^2 - 4*(b^2*c^2*e^4*e^{(a*c)} - 2*e^6*e^{(a*c)})*\sin(4*e*x + 4*d)*\sin(2*e*x + 2*d) + 4*(b^2*c^2*e^4*e^{(a*c)} - 2*e^6*e^{(a*c)})*\sin(2*e*x + 2*d)^2 + 2*(b^2*c^2*e^4*e^{(a*c)} - 2*e^6*e^{(a*c)} - 2*(b^2*c^2*e^4*e^{(a*c)} - 2*e^6*e^{(a*c)}))*\cos(2*e*x + 2*d))*\cos(4*e*x + 4*d) - 4*(b^2*c^2*e^4*e^{(a*c)} - 2*e^6*e^{(a*c)})*\cos(2*e*x + 2*d))*\integrate(1/4*e^{(b*c*x)}*\sin(e*x + d)/(e^4*\cos(e*x + d)^2 + e^4*\sin(e*x + d)^2 + 2*e^4*\cos(e*x + d) + e^4), x) - 2*(b^2*c^2*e^4*e^{(a*c)} - 2*e^6*e^{(a*c)} + (b^2*c^2*e^4*e^{(a*c)} - 2*e^6*e^{(a*c)}))*\cos(4*e*x + 4*d)^2 + 4*(b^2*c^2*e^4*e^{(a*c)} - 2*e^6*e^{(a*c)})*\cos(2*e*x + 2*d)^2 + (b^2*c^2*e^4*e^{(a*c)} - 2*e^6*e^{(a*c)})*\sin(4*e*x + 4*d)^2 - 4*(b^2*c^2*e^4*e^{(a*c)} - 2*e^6*e^{(a*c)})*\sin(4*e*x + 4*d)*\sin(2*e*x + 2*d) + 4*(b^2*c^2*e^4*e^{(a*c)} - 2*e^6*e^{(a*c)})*\sin(2*e*x + 2*d)^2 + 2*(b^2*c^2*e^4*e^{(a*c)} - 2*e^6*e^{(a*c)} - 2*(b^2*c^2*e^4*e^{(a*c)} - 2*e^6*e^{(a*c)}))*\cos(2*e*x + 2*d))*\cos(4*e*x + 4*d) - 4*(b^2*c^2*e^4*e^{(a*c)} - 2*e^6*e^{(a*c)})*\cos(2*e*x + 2*d))*\integrate(1/4*e^{(b*c*x)}*\sin(e*x + d)/(e^4*\cos(e*x + d)^2 + e^4*\sin(e*x + d)^2 - 2*e^4*\cos(e*x + d) + e^4), x) + (b*c*\cos(2*e*x + 2*d)*e^{(b*c*x + a*c)} - b*c*e^{(b*c*x + a*c)} - 2*e*e^{(b*c*x + a*c)}*\sin(2*e*x + 2*d))*\sin(4*e*x + 4*d)/(e^2*\cos(4*e*x + 4*d)^2 + 4*e^2*\cos(2*e*x + 2*d)^2 + e^2*\sin(4*e*x + 4*d)^2 - 4*e^2*\sin(4*e*x + 4*d)*\sin(2*e*x + 2*d) + 4*e^2*\sin(2*e*x + 2*d)^2 - 4*e^2*\cos(2*e*x + 2*d) + e^2 - 2*(2*e^2*\cos(2*e*x + 2*d) - e^2)*\cos(4*e*x + 4*d))$

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \cot(d + ex)^3 e^{c(a+bx)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(cot(d + e*x)^3*exp(c*(a + b*x)),x)

[Out] int(cot(d + e*x)^3*exp(c*(a + b*x)), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$e^{ac} \int e^{bcx} \cot^3(d + ex) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(c*(b*x+a))*cot(e*x+d)**3,x)

[Out] exp(a*c)*Integral(exp(b*c*x)*cot(d + e*x)**3, x)

$$3.25 \quad \int F^{a+bx} \tan\left(\frac{\pi}{4} + \frac{1}{2}(-c - dx)\right) dx$$

Optimal. Leaf size=76

$$\frac{iF^{a+bx}}{b \log(F)} - \frac{2iF^{a+bx} {}_2F_1\left(1, -\frac{ib \log(F)}{d}; 1 - \frac{ib \log(F)}{d}; ie^{i(c+dx)}\right)}{b \log(F)}$$

[Out] $I * F^{(b*x+a)}/b/\ln(F) - 2 * I * F^{(b*x+a)} * \text{hypergeom}([1, -I*b*\ln(F)/d], [1 - I*b*\ln(F)/d], I * \exp(I*(d*x+c)))/b/\ln(F)$

Rubi [A] time = 0.09, antiderivative size = 76, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 4, integrand size = 27, $\frac{\text{number of rules}}{\text{integrand size}} = 0.148$, Rules used = {4464, 4442, 2194, 2251}

$$\frac{iF^{a+bx}}{b \log(F)} - \frac{2iF^{a+bx} {}_2F_1\left(1, -\frac{ib \log(F)}{d}; 1 - \frac{ib \log(F)}{d}; ie^{i(c+dx)}\right)}{b \log(F)}$$

Antiderivative was successfully verified.

[In] Int[F^(a + b*x)*Tan[Pi/4 + (-c - d*x)/2], x]

[Out] $(I * F^{(a + b*x)}) / (b * \text{Log}[F]) - ((2 * I) * F^{(a + b*x)} * \text{Hypergeometric2F1}[1, ((-I) * b * \text{Log}[F]) / d, 1 - (I * b * \text{Log}[F]) / d, I * E^{(I * (c + d*x))}] / (b * \text{Log}[F])$

Rule 2194

Int[((F_)^((c_)*(a_) + (b_)*(x_)))^(n_), x_Symbol] := Simp[(F^(c*(a + b*x)))^n/(b*c*n*Log[F]), x] /; FreeQ[{F, a, b, c, n}, x]

Rule 2251

Int[((a_) + (b_)*(F_)^((e_)*((c_) + (d_)*(x_))))^(p_)*(G_)^((h_)*((f_) + (g_)*(x_))), x_Symbol] := Simp[(a^p * G^(h*(f + g*x)) * Hypergeometric2F1[-p, (g*h*Log[G])/(d*e*Log[F]), (g*h*Log[G])/(d*e*Log[F]) + 1, Simplify[-(b * F^(e*(c + d*x)))/a]]) / (g*h*Log[G]), x] /; FreeQ[{F, G, a, b, c, d, e, f, g, h, p}, x] && (ILtQ[p, 0] || GtQ[a, 0])

Rule 4442

Int[(F_)^((c_)*((a_) + (b_)*(x_)))*Tan[(d_) + (e_)*(x_)]^(n_), x_Symbol] := Dist[I^n, Int[ExpandIntegrand[(F^(c*(a + b*x)) * (1 - E^(2*I*(d + e*x)))^n) / (1 + E^(2*I*(d + e*x)))^n, x], x] /; FreeQ[{F, a, b, c, d, e}, x] && IntegerQ[n]

Rule 4464

Int[(F_)^((c_)*(u_))*(G_)[v_]^(n_), x_Symbol] := Int[F^(c*ExpandToSum[u, x]) * G[ExpandToSum[v, x]]^n, x] /; FreeQ[{F, c, n}, x] && TrigQ[G] && LinearQ[{u, v}, x] && !LinearMatchQ[{u, v}, x]

Rubi steps

$$\begin{aligned}
\int F^{a+bx} \tan\left(\frac{\pi}{4} + \frac{1}{2}(-c - dx)\right) dx &= - \int F^{a+bx} \tan\left(\frac{c}{2} - \frac{\pi}{4} + \frac{dx}{2}\right) dx \\
&= - \left(i \int \left(-F^{a+bx} + \frac{2F^{a+bx}}{1 + e^{2i\left(\frac{c}{2} - \frac{\pi}{4} + \frac{dx}{2}\right)}} \right) dx \right) \\
&= i \int F^{a+bx} dx - 2i \int \frac{F^{a+bx}}{1 + e^{2i\left(\frac{c}{2} - \frac{\pi}{4} + \frac{dx}{2}\right)}} dx \\
&= \frac{iF^{a+bx}}{b \log(F)} - \frac{2iF^{a+bx} {}_2F_1\left(1, -\frac{ib \log(F)}{d}; 1 - \frac{ib \log(F)}{d}; ie^{i(c+dx)}\right)}{b \log(F)}
\end{aligned}$$

Mathematica [A] time = 0.31, size = 133, normalized size = 1.75

$$\frac{F^{a+bx} \left(b \log(F) e^{i(c+dx)} {}_2F_1\left(1, 1 - \frac{ib \log(F)}{d}; 2 - \frac{ib \log(F)}{d}; ie^{i(c+dx)}\right) + (d - ib \log(F)) {}_2F_1\left(1, -\frac{ib \log(F)}{d}; 1 - \frac{ib \log(F)}{d}; ie^{i(c+dx)}\right) \right)}{b \log(F)(b \log(F) + id)}$$

Antiderivative was successfully verified.

[In] Integrate[F^(a + b*x)*Tan[Pi/4 + (-c - d*x)/2], x]

[Out] (F^(a + b*x)*(b*E^(I*(c + d*x))*Hypergeometric2F1[1, 1 - (I*b*Log[F])/d, 2 - (I*b*Log[F])/d, I*E^(I*(c + d*x))]*Log[F] + Hypergeometric2F1[1, ((-I)*b*Log[F])/d, 1 - (I*b*Log[F])/d, I*E^(I*(c + d*x))]*(d - I*b*Log[F])))/(b*Log[F]*(I*d + b*Log[F]))

fricas [F] time = 0.76, size = 0, normalized size = 0.00

$$\text{integral}\left(F^{bx+a} \cot\left(\frac{1}{4}\pi + \frac{1}{2}dx + \frac{1}{2}c\right), x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(F^(b*x+a)*cot(1/2*c+1/4*pi+1/2*d*x), x, algorithm="fricas")

[Out] integral(F^(b*x + a)*cot(1/4*pi + 1/2*d*x + 1/2*c), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int F^{bx+a} \cot\left(\frac{1}{4}\pi + \frac{1}{2}dx + \frac{1}{2}c\right) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(F^(b*x+a)*cot(1/2*c+1/4*pi+1/2*d*x), x, algorithm="giac")

[Out] integrate(F^(b*x + a)*cot(1/4*pi + 1/2*d*x + 1/2*c), x)

maple [F] time = 0.22, size = 0, normalized size = 0.00

$$\int F^{bx+a} \cot\left(\frac{\pi}{4} + \frac{dx}{2} + \frac{c}{2}\right) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(F^(b*x+a)*cot(1/4*Pi+1/2*d*x+1/2*c), x)

[Out] int(F^(b*x+a)*cot(1/4*Pi+1/2*d*x+1/2*c), x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int F^{bx+a} \cot\left(\frac{1}{4}\pi + \frac{1}{2}dx + \frac{1}{2}c\right) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(F^(b*x+a)*cot(1/2*c+1/4*pi+1/2*d*x),x, algorithm="maxima")

[Out] integrate(F^(b*x + a)*cot(1/4*pi + 1/2*d*x + 1/2*c), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int F^{a+bx} \cot\left(\frac{\Pi}{4} + \frac{c}{2} + \frac{dx}{2}\right) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(F^(a + b*x)*cot(Pi/4 + c/2 + (d*x)/2),x)

[Out] int(F^(a + b*x)*cot(Pi/4 + c/2 + (d*x)/2), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int F^{a+bx} \cot\left(\frac{c}{2} + \frac{dx}{2} + \frac{\pi}{4}\right) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(F**(b*x+a)*cot(1/2*c+1/4*pi+1/2*d*x),x)

[Out] Integral(F**(a + b*x)*cot(c/2 + d*x/2 + pi/4), x)

3.26 $\int F^{c(a+bx)} \sec^n(d+ex) dx$

Optimal. Leaf size=100

$$\frac{(1 + e^{2i(d+ex)})^n F^{ac+bcx} \sec^n(d+ex) {}_2F_1\left(n, \frac{en-ibc \log(F)}{2e}; \frac{1}{2}\left(n - \frac{ibc \log(F)}{e} + 2\right); -e^{2i(d+ex)}\right)}{bc \log(F) + ien}$$

[Out] (1+exp(2*I*(e*x+d)))^n*F^(b*c*x+a*c)*hypergeom([n, 1/2*(e*n-I*b*c*ln(F))/e], [1+1/2*n-1/2*I*b*c*ln(F)/e], -exp(2*I*(e*x+d)))*sec(e*x+d)^n/(b*c*ln(F)+I*e*n)

Rubi [A] time = 0.14, antiderivative size = 100, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {4454, 2259}

$$\frac{(1 + e^{2i(d+ex)})^n F^{ac+bcx} \sec^n(d+ex) {}_2F_1\left(n, \frac{en-ibc \log(F)}{2e}; \frac{1}{2}\left(n - \frac{ibc \log(F)}{e} + 2\right); -e^{2i(d+ex)}\right)}{bc \log(F) + ien}$$

Antiderivative was successfully verified.

[In] Int[F^(c*(a + b*x))*Sec[d + e*x]^n,x]

[Out] ((1 + E^((2*I)*(d + e*x)))^n*F^(a*c + b*c*x)*Hypergeometric2F1[n, (e*n - I*b*c*Log[F])/(2*e), (2 + n - (I*b*c*Log[F])/e)/2, -E^((2*I)*(d + e*x))]*Sec[d + e*x]^n)/(I*e*n + b*c*Log[F])

Rule 2259

Int[((a_) + (b_)*(F_)^((e_)*((c_) + (d_)*(x_))))^(p_)*(G_)^((h_)*((f_) + (g_)*(x_)))*(H_)^((t_)*((r_) + (s_)*(x_))), x_Symbol] := Simp[(G^(h*(f + g*x))*H^(t*(r + s*x))*(a + b*F^(e*(c + d*x)))^p*Hypergeometric2F1[-p, (g*h*Log[G] + s*t*Log[H])/(d*e*Log[F]), (g*h*Log[G] + s*t*Log[H])/(d*e*Log[F]) + 1, Simplify[-((b*F^(e*(c + d*x)))/a)]]]/((g*h*Log[G] + s*t*Log[H])*(a + b*F^(e*(c + d*x)))/a)^p, x] /; FreeQ[{F, G, H, a, b, c, d, e, f, g, h, r, s, t, p}, x] && !IntegerQ[p]

Rule 4454

Int[(F_)^((c_)*((a_) + (b_)*(x_)))*Sec[(d_) + (e_)*(x_)]^(n_), x_Symbol] := Dist[((1 + E^(2*I*(d + e*x)))^n*Sec[d + e*x]^n)/E^(I*n*(d + e*x)), Int[SimplifyIntegrand[(F^(c*(a + b*x))*E^(I*n*(d + e*x))]/(1 + E^(2*I*(d + e*x)))^n, x], x] /; FreeQ[{F, a, b, c, d, e}, x] && !IntegerQ[n]

Rubi steps

$$\begin{aligned} \int F^{c(a+bx)} \sec^n(d+ex) dx &= \left(e^{-in(d+ex)} (1 + e^{2i(d+ex)})^n \sec^n(d+ex) \right) \int e^{idn+ienx} (1 + e^{2i(d+ex)})^{-n} F^{ac+bcx} dx \\ &= \frac{(1 + e^{2i(d+ex)})^n F^{ac+bcx} {}_2F_1\left(n, \frac{en-ibc \log(F)}{2e}; \frac{1}{2}\left(2 + n - \frac{ibc \log(F)}{e}\right); -e^{2i(d+ex)}\right) \sec^n(d+ex)}{ien + bc \log(F)} \end{aligned}$$

Mathematica [A] time = 0.09, size = 102, normalized size = 1.02

$$\frac{i(1 + e^{2i(d+ex)})^n F^{c(a+bx)} \sec^n(d+ex) {}_2F_1\left(n, \frac{en-ibc \log(F)}{2e}; \frac{1}{2}\left(n - \frac{ibc \log(F)}{e} + 2\right); -e^{2i(d+ex)}\right)}{en - ibc \log(F)}$$

Antiderivative was successfully verified.

```
[In] Integrate[F^(c*(a + b*x))*Sec[d + e*x]^n,x]
[Out] ((-I)*(1 + E^((2*I)*(d + e*x)))^n)*F^(c*(a + b*x))*Hypergeometric2F1[n, (e*n - I*b*c*Log[F])/(2*e), (2 + n - (I*b*c*Log[F])/e)/2, -E^((2*I)*(d + e*x))]
*Sec[d + e*x]^n)/(e*n - I*b*c*Log[F])
fricas [F] time = 1.55, size = 0, normalized size = 0.00
```

$$\text{integral}\left(F^{bcx+ac} \sec(ex + d)^n, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(F^(c*(b*x+a))*sec(e*x+d)^n,x, algorithm="fricas")
[Out] integral(F^(b*c*x + a*c)*sec(e*x + d)^n, x)
giac [F] time = 0.00, size = 0, normalized size = 0.00
```

$$\int F^{(bx+a)c} \sec(ex + d)^n dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(F^(c*(b*x+a))*sec(e*x+d)^n,x, algorithm="giac")
[Out] integrate(F^((b*x + a)*c)*sec(e*x + d)^n, x)
maple [F] time = 0.88, size = 0, normalized size = 0.00
```

$$\int F^{c(bx+a)} (\sec^n(ex + d)) dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(F^(c*(b*x+a))*sec(e*x+d)^n,x)
[Out] int(F^(c*(b*x+a))*sec(e*x+d)^n,x)
maxima [F] time = 0.00, size = 0, normalized size = 0.00
```

$$\int F^{(bx+a)c} \sec(ex + d)^n dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(F^(c*(b*x+a))*sec(e*x+d)^n,x, algorithm="maxima")
[Out] integrate(F^((b*x + a)*c)*sec(e*x + d)^n, x)
mupad [F] time = 0.00, size = -1, normalized size = -0.01
```

$$\int F^{c(a+bx)} \left(\frac{1}{\cos(d + ex)}\right)^n dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(F^(c*(a + b*x))*(1/cos(d + e*x))^n,x)
[Out] int(F^(c*(a + b*x))*(1/cos(d + e*x))^n, x)
sympy [F] time = 0.00, size = 0, normalized size = 0.00
```

$$\int F^{c(a+bx)} \sec^n(d + ex) dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(F**(c*(b*x+a))*sec(e*x+d)**n,x)
```

```
[Out] Integral(F**(c*(a + b*x))*sec(d + e*x)**n, x)
```

3.27 $\int F^{c(a+bx)} \csc^n(d+ex) dx$

Optimal. Leaf size=102

$$\frac{(1 - e^{-2i(d+ex)})^n F^{ac+bcx} \csc^n(d+ex) {}_2F_1\left(n, \frac{en+ibc \log(F)}{2e}; \frac{1}{2}\left(n + \frac{ibc \log(F)}{e} + 2\right); e^{-2i(d+ex)}\right)}{-bc \log(F) + ien}$$

[Out] $-(1-1/\exp(2*I*(e*x+d)))^n * F^{(b*c*x+a*c)} * \csc(e*x+d)^n * \text{hypergeom}([n, 1/2*(I*b*c*\ln(F)+e*n)/e], [1+1/2*n+1/2*I*b*c*\ln(F)/e], \exp(-2*I*(e*x+d)))/(I*e*n-b*c*\ln(F))$

Rubi [A] time = 0.16, antiderivative size = 102, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {4455, 2259}

$$\frac{(1 - e^{-2i(d+ex)})^n F^{ac+bcx} \csc^n(d+ex) {}_2F_1\left(n, \frac{en+ibc \log(F)}{2e}; \frac{1}{2}\left(n + \frac{ibc \log(F)}{e} + 2\right); e^{-2i(d+ex)}\right)}{-bc \log(F) + ien}$$

Antiderivative was successfully verified.

[In] Int[F^(c*(a + b*x))*Csc[d + e*x]^n,x]

[Out] $-\left(\left(1 - E^{(-2*I)*(d + e*x)}\right)^n * F^{(a*c + b*c*x)} * \text{Csc}[d + e*x]^n * \text{Hypergeometric2F1}\left[n, \frac{(e*n + I*b*c*\text{Log}[F])}{(2*e)}, \frac{(2 + n + (I*b*c*\text{Log}[F])/e)}{2}, E^{(-2*I)*(d + e*x)}\right]\right) / (I*e*n - b*c*\text{Log}[F])$

Rule 2259

Int[((a_) + (b_)*(F_)^((e_)*((c_) + (d_)*(x_))))^(p_)*(G_)^((h_)*((f_) + (g_)*(x_)))*(H_)^((t_)*((r_) + (s_)*(x_))), x_Symbol] :> Simp[(G^(h*(f + g*x))*H^(t*(r + s*x))*(a + b*F^(e*(c + d*x)))^p*Hypergeometric2F1[-p, (g*h*Log[G] + s*t*Log[H])/(d*e*Log[F]), (g*h*Log[G] + s*t*Log[H])/(d*e*Log[F]) + 1, Simplify[-((b*F^(e*(c + d*x)))/a)]]]/((g*h*Log[G] + s*t*Log[H])*(a + b*F^(e*(c + d*x)))/a^p), x] /; FreeQ[{F, G, H, a, b, c, d, e, f, g, h, r, s, t, p}, x] && !IntegerQ[p]

Rule 4455

Int[Csc[(d_) + (e_)*(x_)]^(n_)*(F_)^((c_)*((a_) + (b_)*(x_))), x_Symbol] :> Dist[(((1 - E^(-2*I*(d + e*x)))^n * Csc[d + e*x]^n) / E^(-I*n*(d + e*x))), Int[SimplifyIntegrand[F^(c*(a + b*x)) / (E^(I*n*(d + e*x)) * (1 - E^(-2*I*(d + e*x)))^n), x], x] /; FreeQ[{F, a, b, c, d, e}, x] && !IntegerQ[n]

Rubi steps

$$\begin{aligned} \int F^{c(a+bx)} \csc^n(d+ex) dx &= \left(e^{in(d+ex)} (1 - e^{-2i(d+ex)})^n \csc^n(d+ex) \right) \int e^{-idn-ienx} (1 - e^{-2i(d+ex)})^{-n} F^{ac+bcx} dx \\ &= \frac{(1 - e^{-2i(d+ex)})^n F^{ac+bcx} \csc^n(d+ex) {}_2F_1\left(n, \frac{en+ibc \log(F)}{2e}; \frac{1}{2}\left(2 + n + \frac{ibc \log(F)}{e}\right); e^{-2i(d+ex)}\right)}{ien - bc \log(F)} \end{aligned}$$

Mathematica [A] time = 0.10, size = 102, normalized size = 1.00

$$\frac{i(1 - e^{-2i(d+ex)})^n F^{c(a+bx)} \csc^n(d+ex) {}_2F_1\left(n, \frac{en+ibc \log(F)}{2e}; \frac{1}{2}\left(n + \frac{ibc \log(F)}{e} + 2\right); e^{-2i(d+ex)}\right)}{en + ibc \log(F)}$$

Antiderivative was successfully verified.

[In] Integrate[F^(c*(a + b*x))*Csc[d + e*x]^n,x]

[Out] (I*(1 - E^((-2*I)*(d + e*x)))^n * F^(c*(a + b*x)) * Csc[d + e*x]^n * Hypergeometric2F1[n, (e*n + I*b*c*Log[F])/(2*e), (2 + n + (I*b*c*Log[F])/e)/2, E^((-2*I)*(d + e*x))]) / (e*n + I*b*c*Log[F])

fricas [F] time = 0.58, size = 0, normalized size = 0.00

$$\text{integral}\left(F^{bcx+ac} \csc(ex + d)^n, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(F^(c*(b*x+a))*csc(e*x+d)^n,x, algorithm="fricas")

[Out] integral(F^(b*c*x + a*c)*csc(e*x + d)^n, x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int F^{(bx+a)c} \csc(ex + d)^n dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(F^(c*(b*x+a))*csc(e*x+d)^n,x, algorithm="giac")

[Out] integrate(F^((b*x + a)*c)*csc(e*x + d)^n, x)

maple [F] time = 0.98, size = 0, normalized size = 0.00

$$\int F^{c(bx+a)} (\csc^n(ex + d)) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(F^(c*(b*x+a))*csc(e*x+d)^n,x)

[Out] int(F^(c*(b*x+a))*csc(e*x+d)^n,x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int F^{(bx+a)c} \csc(ex + d)^n dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(F^(c*(b*x+a))*csc(e*x+d)^n,x, algorithm="maxima")

[Out] integrate(F^((b*x + a)*c)*csc(e*x + d)^n, x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int F^{c(a+bx)} \left(\frac{1}{\sin(d + ex)}\right)^n dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(F^(c*(a + b*x))*(1/sin(d + e*x))^n,x)

[Out] int(F^(c*(a + b*x))*(1/sin(d + e*x))^n, x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int F^{c(a+bx)} \csc^n(d + ex) dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(F**(c*(b*x+a))*csc(e*x+d)**n,x)
```

```
[Out] Integral(F**(c*(a + b*x))*csc(d + e*x)**n, x)
```

3.28 $\int F^{c(a+bx)}(fx)^m \sin(d+ex) dx$

Optimal. Leaf size=139

$$\frac{e^{id}F^{ac}(fx)^m(-x(bc \log(F) + ie))^{-m}\Gamma(m+1, -x(ie + bc \log(F)))}{2(e - ibc \log(F))} - \frac{e^{-id}F^{ac}(fx)^m(x(-bc \log(F) + ie))^{-m}\Gamma(m+1, x(-bc \log(F) + ie))}{2(e + ibc \log(F))}$$

[Out] $-1/2 * F^{(a*c)} * (f*x)^m * \text{GAMMA}(1+m, x*(I*e-b*c*\ln(F))) / \exp(I*d) / ((x*(I*e-b*c*\ln(F)))^m) / (e+I*b*c*\ln(F)) - 1/2 * \exp(I*d) * F^{(a*c)} * (f*x)^m * \text{GAMMA}(1+m, -x*(b*c*\ln(F)+I*e)) / (e-I*b*c*\ln(F)) / ((-x*(b*c*\ln(F)+I*e))^m)$

Rubi [F] time = 0.49, antiderivative size = 0, normalized size of antiderivative = 0.00, number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int F^{c(a+bx)}(fx)^m \sin(d+ex) dx$$

Verification is Not applicable to the result.

[In] Int[F^(c*(a + b*x))*(f*x)^m*Sin[d + e*x], x]

[Out] Defer[Int][F^(a*c + b*c*x)*(f*x)^m*Sin[d + e*x], x]

Rubi steps

$$\int F^{c(a+bx)}(fx)^m \sin(d+ex) dx = \int F^{ac+bcx}(fx)^m \sin(d+ex) dx$$

Mathematica [A] time = 0.62, size = 143, normalized size = 1.03

$$\frac{1}{2} F^{ac}(fx)^m (x(-bc \log(F) - ie))^{-m} \left(-ix(\cos(d) - i \sin(d))(-bcx \log(F) - iex)^m (ix(e + ibc \log(F)))^{-m-1} \Gamma(m+1, iex) \right)$$

Antiderivative was successfully verified.

[In] Integrate[F^(c*(a + b*x))*(f*x)^m*Sin[d + e*x], x]

[Out] $(F^{(a*c)} * (f*x)^m * ((-I)*x*\text{Gamma}[1 + m, I*e*x - b*c*x*\text{Log}[F]]) * (I*x*(e + I*b*c*\text{Log}[F]))^{(-1 - m)} * ((-I)*e*x - b*c*x*\text{Log}[F])^m * (\text{Cos}[d] - I*\text{Sin}[d]) - (\text{Gamma}[1 + m, (-I)*e*x - b*c*x*\text{Log}[F]] * (\text{Cos}[d] + I*\text{Sin}[d])) / (e - I*b*c*\text{Log}[F])) / (2*(x*((-I)*e - b*c*\text{Log}[F]))^m)$

fricas [A] time = 0.90, size = 130, normalized size = 0.94

$$\frac{(ibc \log(F) - e)e^{(ac \log(F) - m \log(-\frac{bc \log(F) - ie}{f}) - id)} \Gamma(m+1, -bcx \log(F) + iex) + (-ibc \log(F) - e)e^{(ac \log(F) - m \log(-\frac{bc \log(F) - ie}{f}) - id)}}{2(b^2c^2 \log(F)^2 + e^2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(F^(c*(b*x+a))*(f*x)^m*sin(e*x+d), x, algorithm="fricas")

[Out] $1/2 * ((I*b*c*\log(F) - e)*e^{(a*c*\log(F) - m*\log(-(b*c*\log(F) - I*e)/f) - I*d)} * \text{gamma}(m+1, -b*c*x*\log(F) + I*e*x) + (-I*b*c*\log(F) - e)*e^{(a*c*\log(F) - m*\log(-(b*c*\log(F) + I*e)/f) + I*d)} * \text{gamma}(m+1, -b*c*x*\log(F) - I*e*x)) / (b^2*c^2*\log(F)^2 + e^2)$

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (fx)^m F^{(bx+a)c} \sin(ex+d) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(F^(c*(b*x+a))*(f*x)^m*sin(e*x+d),x, algorithm="giac")

[Out] integrate((f*x)^m*F^((b*x + a)*c)*sin(e*x + d), x)

maple [F] time = 0.43, size = 0, normalized size = 0.00

$$\int F^{c(bx+a)} (fx)^m \sin(ex + d) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(F^(c*(b*x+a))*(f*x)^m*sin(e*x+d),x)

[Out] int(F^(c*(b*x+a))*(f*x)^m*sin(e*x+d),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (fx)^m F^{(bx+a)c} \sin(ex + d) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(F^(c*(b*x+a))*(f*x)^m*sin(e*x+d),x, algorithm="maxima")

[Out] integrate((f*x)^m*F^((b*x + a)*c)*sin(e*x + d), x)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int F^{c(a+bx)} \sin(d + ex) (fx)^m dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(F^(c*(a + b*x))*sin(d + e*x)*(f*x)^m,x)

[Out] int(F^(c*(a + b*x))*sin(d + e*x)*(f*x)^m, x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int F^{c(a+bx)} (fx)^m \sin(d + ex) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(F**(c*(b*x+a))*(f*x)**m*sin(e*x+d),x)

[Out] Integral(F**(c*(a + b*x))*(f*x)**m*sin(d + e*x), x)

3.29 $\int F^{c(a+bx)}(fx)^m \csc(d+ex) dx$

Optimal. Leaf size=25

$$\text{Int}\left((fx)^m \csc(d+ex)F^{ac+bcx}, x\right)$$

[Out] CannotIntegrate(F^(b*c*x+a*c)*(f*x)^m*csc(e*x+d), x)

Rubi [A] time = 0.62, antiderivative size = 0, normalized size of antiderivative = 0.00, number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int F^{c(a+bx)}(fx)^m \csc(d+ex) dx$$

Verification is Not applicable to the result.

[In] Int[F^(c*(a + b*x))*(f*x)^m*Csc[d + e*x], x]

[Out] Defer[Int][F^(a*c + b*c*x)*(f*x)^m*Csc[d + e*x], x]

Rubi steps

$$\int F^{c(a+bx)}(fx)^m \csc(d+ex) dx = \int F^{ac+bcx}(fx)^m \csc(d+ex) dx$$

Mathematica [A] time = 9.20, size = 0, normalized size = 0.00

$$\int F^{c(a+bx)}(fx)^m \csc(d+ex) dx$$

Verification is Not applicable to the result.

[In] Integrate[F^(c*(a + b*x))*(f*x)^m*Csc[d + e*x], x]

[Out] Integrate[F^(c*(a + b*x))*(f*x)^m*Csc[d + e*x], x]

fricas [A] time = 1.48, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{(fx)^m F^{bcx+ac}}{\sin(ex+d)}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(F^(c*(b*x+a))*(f*x)^m/sin(e*x+d), x, algorithm="fricas")

[Out] integral((f*x)^m*F^(b*c*x + a*c)/sin(e*x + d), x)

giac [A] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(fx)^m F^{(bx+a)c}}{\sin(ex+d)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(F^(c*(b*x+a))*(f*x)^m/sin(e*x+d), x, algorithm="giac")

[Out] integrate((f*x)^m*F^((b*x + a)*c)/sin(e*x + d), x)

maple [A] time = 0.15, size = 0, normalized size = 0.00

$$\int \frac{F^{c(bx+a)}(fx)^m}{\sin(ex+d)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(F^(c*(b*x+a))*(f*x)^m/sin(e*x+d),x)`

[Out] `int(F^(c*(b*x+a))*(f*x)^m/sin(e*x+d),x)`

maxima [A] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(fx)^m F^{(bx+a)c}}{\sin(ex+d)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(F^(c*(b*x+a))*(f*x)^m/sin(e*x+d),x, algorithm="maxima")`

[Out] `integrate((f*x)^m*F^((b*x+a)*c)/sin(e*x+d), x)`

mupad [A] time = 0.00, size = -1, normalized size = -0.04

$$\int \frac{F^{c(a+bx)} (fx)^m}{\sin(d+ex)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((F^(c*(a+b*x))*(f*x)^m)/sin(d+e*x),x)`

[Out] `int((F^(c*(a+b*x))*(f*x)^m)/sin(d+e*x), x)`

sympy [A] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{F^{c(a+bx)} (fx)^m}{\sin(d+ex)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(F**(c*(b*x+a))*(f*x)**m/sin(e*x+d),x)`

[Out] `Integral(F**(c*(a+b*x))*(f*x)**m/sin(d+e*x), x)`

3.30 $\int F^{c(a+bx)}(fx)^m \csc^2(d+ex) dx$

Optimal. Leaf size=27

$$\text{Int}\left((fx)^m \csc^2(d+ex)F^{ac+bcx}, x\right)$$

[Out] CannotIntegrate(F^(b*c*x+a*c)*(f*x)^m*csc(e*x+d)^2, x)

Rubi [A] time = 0.95, antiderivative size = 0, normalized size of antiderivative = 0.00, number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int F^{c(a+bx)}(fx)^m \csc^2(d+ex) dx$$

Verification is Not applicable to the result.

[In] Int[F^(c*(a + b*x))*(f*x)^m*Csc[d + e*x]^2, x]

[Out] Defer[Int][F^(a*c + b*c*x)*(f*x)^m*Csc[d + e*x]^2, x]

Rubi steps

$$\int F^{c(a+bx)}(fx)^m \csc^2(d+ex) dx = \int F^{ac+bcx}(fx)^m \csc^2(d+ex) dx$$

Mathematica [A] time = 10.72, size = 0, normalized size = 0.00

$$\int F^{c(a+bx)}(fx)^m \csc^2(d+ex) dx$$

Verification is Not applicable to the result.

[In] Integrate[F^(c*(a + b*x))*(f*x)^m*Csc[d + e*x]^2, x]

[Out] Integrate[F^(c*(a + b*x))*(f*x)^m*Csc[d + e*x]^2, x]

fricas [A] time = 0.60, size = 0, normalized size = 0.00

$$\text{integral}\left(-\frac{(fx)^m F^{bcx+ac}}{\cos(ex+d)^2-1}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(F^(c*(b*x+a))*(f*x)^m/sin(e*x+d)^2, x, algorithm="fricas")

[Out] integral(-(f*x)^m*F^(b*c*x + a*c)/(cos(e*x + d)^2 - 1), x)

giac [A] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(fx)^m F^{(bx+a)c}}{\sin(ex+d)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(F^(c*(b*x+a))*(f*x)^m/sin(e*x+d)^2, x, algorithm="giac")

[Out] integrate((f*x)^m*F^((b*x + a)*c)/sin(e*x + d)^2, x)

maple [A] time = 0.18, size = 0, normalized size = 0.00

$$\int \frac{F^{c(bx+a)}(fx)^m}{\sin(ex+d)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(F^(c*(b*x+a))*(f*x)^m/sin(e*x+d)^2,x)`

[Out] `int(F^(c*(b*x+a))*(f*x)^m/sin(e*x+d)^2,x)`

maxima [A] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(fx)^m F^{(bx+a)c}}{\sin(ex+d)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(F^(c*(b*x+a))*(f*x)^m/sin(e*x+d)^2,x, algorithm="maxima")`

[Out] `integrate((f*x)^m*F^((b*x + a)*c)/sin(e*x + d)^2, x)`

mupad [A] time = 0.00, size = -1, normalized size = -0.04

$$\int \frac{F^{c(a+bx)} (fx)^m}{\sin(d+ex)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((F^(c*(a + b*x))*(f*x)^m)/sin(d + e*x)^2,x)`

[Out] `int((F^(c*(a + b*x))*(f*x)^m)/sin(d + e*x)^2, x)`

sympy [A] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{F^{c(a+bx)} (fx)^m}{\sin^2(d+ex)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(F**(c*(b*x+a))*(f*x)**m/sin(e*x+d)**2,x)`

[Out] `Integral(F**(c*(a + b*x))*(f*x)**m/sin(d + e*x)**2, x)`

$$3.31 \quad \int f F^{c(a+bx)} (fx)^{-2+m} (ex \cos(d+ex) + (-1+m+bcx \log(F)) \sin(d+ex)) dx$$

Optimal. Leaf size=24

$$(fx)^{m-1} \sin(d+ex) F^{ac+bcx}$$

[Out] $F^{(b*c*x+a*c)*(f*x)^{-1+m}*\sin(e*x+d)}$

Rubi [A] time = 3.98, antiderivative size = 24, normalized size of antiderivative = 1.00, number of steps used = 11, number of rules used = 5, integrand size = 44, $\frac{\text{number of rules}}{\text{integrand size}} = 0.114$, Rules used = {12, 6741, 6742, 4468, 4467}

$$(fx)^{m-1} \sin(d+ex) F^{ac+bcx}$$

Antiderivative was successfully verified.

[In] $\text{Int}[f*F^{(c*(a+b*x))*(f*x)^{-2+m}*(e*x*\text{Cos}[d+e*x]+(-1+m+b*c*x*\text{Log}[F])*\text{Sin}[d+e*x]),x]$

[Out] $F^{(a*c+b*c*x)*(f*x)^{-1+m}*\text{Sin}[d+e*x]$

Rule 12

$\text{Int}[(a_*)*(u_), x_Symbol] \rightarrow \text{Dist}[a, \text{Int}[u, x], x] /; \text{FreeQ}[a, x] \&\& \text{!MatchQ}[u, (b_*)*(v_) /; \text{FreeQ}[b, x]]$

Rule 4467

$\text{Int}[(F_)^{((c_*)*((a_*)+(b_*)*(x_)))}*((f_*)*(x_))^{(m_*)}*\text{Sin}[(d_*)+(e_*)*(x_)], x_Symbol] \rightarrow \text{Simp}[(f*x)^{(m+1)}*F^{(c*(a+b*x))*\text{Sin}[d+e*x]}/(f*(m+1)), x] + (-\text{Dist}[e/(f*(m+1)), \text{Int}[(f*x)^{(m+1)}*F^{(c*(a+b*x))*\text{Cos}[d+e*x]}, x], x] - \text{Dist}[(b*c*\text{Log}[F])/(f*(m+1)), \text{Int}[(f*x)^{(m+1)}*F^{(c*(a+b*x))*\text{Sin}[d+e*x]}, x], x]) /; \text{FreeQ}\{F, a, b, c, d, e, f, m\}, x] \&\& (\text{LtQ}[m, -1] || \text{SumSimplerQ}[m, 1])$

Rule 4468

$\text{Int}[\text{Cos}[(d_*)+(e_*)*(x_)]*(F_)^{((c_*)*((a_*)+(b_*)*(x_)))}*((f_*)*(x_))^{(m_*)}, x_Symbol] \rightarrow \text{Simp}[(f*x)^{(m+1)}*F^{(c*(a+b*x))*\text{Cos}[d+e*x]}/(f*(m+1)), x] + (\text{Dist}[e/(f*(m+1)), \text{Int}[(f*x)^{(m+1)}*F^{(c*(a+b*x))*\text{Sin}[d+e*x]}, x], x] - \text{Dist}[(b*c*\text{Log}[F])/(f*(m+1)), \text{Int}[(f*x)^{(m+1)}*F^{(c*(a+b*x))*\text{Cos}[d+e*x]}, x], x]) /; \text{FreeQ}\{F, a, b, c, d, e, f, m\}, x] \&\& (\text{LtQ}[m, -1] || \text{SumSimplerQ}[m, 1])$

Rule 6741

$\text{Int}[u_, x_Symbol] \rightarrow \text{With}\{v = \text{NormalizeIntegrand}[u, x]\}, \text{Int}[v, x] /; v \neq u]$

Rule 6742

$\text{Int}[u_, x_Symbol] \rightarrow \text{With}\{v = \text{ExpandIntegrand}[u, x]\}, \text{Int}[v, x] /; \text{SumQ}[v]$

Rubi steps

$$\begin{aligned}
\int f F^{c(a+bx)} (fx)^{-2+m} (ex \cos(d+ex) + (-1+m+bcx \log(F)) \sin(d+ex)) dx &= f \int F^{c(a+bx)} (fx)^{-2+m} (ex \cos(d+ex) + (-1+m+bcx \log(F)) \sin(d+ex)) dx \\
&= f \int F^{ac+bcx} (fx)^{-2+m} (ex \cos(d+ex) + (-1+m+bcx \log(F)) \sin(d+ex)) dx \\
&= f \int \left(\frac{e F^{ac+bcx} (fx)^{-1+m} \cos(d+ex)}{f} + \frac{(-1+m+bcx \log(F)) F^{ac+bcx} (fx)^{-1+m} \sin(d+ex)}{f} \right) dx \\
&= e \int F^{ac+bcx} (fx)^{-1+m} \cos(d+ex) dx + (-1+m) \int F^{ac+bcx} (fx)^{-1+m} \sin(d+ex) dx + bcx \int F^{ac+bcx} (fx)^{-1+m} \sin(d+ex) dx \\
&= \frac{e F^{ac+bcx} (fx)^m \cos(d+ex)}{fm} + f \int \left(\frac{(-1+m) F^{ac+bcx} (fx)^{-1+m} \sin(d+ex)}{f} + bcx F^{ac+bcx} (fx)^{-1+m} \sin(d+ex) \right) dx \\
&= \frac{e F^{ac+bcx} (fx)^m \cos(d+ex)}{fm} - (f(1-m)) \int F^{ac+bcx} (fx)^{-1+m} \sin(d+ex) dx + bcx \int F^{ac+bcx} (fx)^{-1+m} \sin(d+ex) dx \\
&= \frac{e F^{ac+bcx} (fx)^m \cos(d+ex)}{fm} + F^{ac+bcx} (fx)^{-1+m} \sin(d+ex)
\end{aligned}$$

Mathematica [A] time = 1.35, size = 26, normalized size = 1.08

$$fx (fx)^{m-2} \sin(d+ex) F^{ac+bcx}$$

Antiderivative was successfully verified.

[In] Integrate[f*F^(c*(a+b*x))*(f*x)^(-2+m)*(e*x*Cos[d+e*x]+(-1+m+b*c*x*Log[F])*Sin[d+e*x]),x]

[Out] f*F^(a*c+b*c*x)*x*(f*x)^(-2+m)*Sin[d+e*x]

fricas [A] time = 0.56, size = 26, normalized size = 1.08

$$(fx)^{m-2} F^{bcx+ac} fx \sin(ex+d)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f*F^(c*(b*x+a))*(f*x)^(-2+m)*(e*x*cos(e*x+d)+(-1+m+b*c*x*log(F))*sin(e*x+d)),x, algorithm="fricas")

[Out] (f*x)^(m-2)*F^(b*c*x+a*c)*f*x*sin(e*x+d)

giac [B] time = 0.92, size = 6402, normalized size = 266.75

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f*F^(c*(b*x+a))*(f*x)^(-2+m)*(e*x*cos(e*x+d)+(-1+m+b*c*x*log(F))*sin(e*x+d)),x, algorithm="giac")

[Out] (x*abs(F)^(a*c)*e^(b*c*x*log(abs(F))+m*log(abs(f)*abs(x))-2*log(abs(f)*abs(x))) * tan(1/4*pi*b*c*x*sgn(F)-1/4*pi*b*c*x+pi*m*floor(-1/4*sgn(f)-1/4*sgn(x)+1)+1/4*pi*m*sgn(f)+1/4*pi*m*sgn(x)-1/2*pi*m+1/2*x*e-2*pi*floor(-1/4*sgn(f)-1/4*sgn(x)+1)-1/2*pi*sgn(f)-1/2*pi*sgn(x))^2 * tan(1/4*pi*b*c*x*sgn(F)-1/4*pi*b*c*x+pi*m*floor(-1/4*sgn(f)-1/4*sgn(x)+1)+1/4*pi*m*sgn(f)+1/4*pi*m*sgn(x)-1/2*pi*m-1/2*x*e-2*pi*floor(-1/4*sgn(f)-1/4*sgn(x)+1)-1/2*pi*sgn(f)-1/2*pi*sgn(x))^2 * tan(1/4*pi*a*c*sgn(F)-1/4*pi*a*c+1/2*d)^2 * tan(1/4*pi*a*c*sgn(F)-1/4*pi*a*c-1/2*d) - x*abs(F)^(a*c)*e^(b*c*x*log(abs(F))+m*log(abs(f)*abs(x))-2*log(abs(f)*abs(x)))

$$\begin{aligned}
& 1/4*\pi*a*c + 1/2*d) + x*abs(F)^(a*c)*e^(b*c*x*log(abs(F)) + m*log(abs(f)*abs(x)) - 2*log(abs(f)*abs(x))) * \tan(1/4*\pi*b*c*x*sgn(F) - 1/4*\pi*b*c*x + \pi*m \\
& *floor(-1/4*sgn(f) - 1/4*sgn(x) + 1) + 1/4*\pi*m*sgn(f) + 1/4*\pi*m*sgn(x) - \\
& 1/2*\pi*m - 1/2*x*e - 2*\pi*floor(-1/4*sgn(f) - 1/4*sgn(x) + 1) - 1/2*\pi*sgn(f) - 1/2*\pi*sgn(x))^2 * \tan(1/4*\pi*a*c*sgn(F) - 1/4*\pi*a*c + 1/2*d) - x*abs(F) \\
&)^(a*c)*e^(b*c*x*log(abs(F)) + m*log(abs(f)*abs(x)) - 2*log(abs(f)*abs(x))) \\
& * \tan(1/4*\pi*b*c*x*sgn(F) - 1/4*\pi*b*c*x + \pi*m*floor(-1/4*sgn(f) - 1/4*sgn(x) \\
& + 1) + 1/4*\pi*m*sgn(f) + 1/4*\pi*m*sgn(x) - 1/2*\pi*m + 1/2*x*e - 2*\pi*floor(-1/4*sgn(f) - 1/4*sgn(x) + 1) - 1/2*\pi*sgn(f) - 1/2*\pi*sgn(x)) * \tan(1/4*\pi \\
& *a*c*sgn(F) - 1/4*\pi*a*c + 1/2*d)^2 - x*abs(F)^(a*c)*e^(b*c*x*log(abs(F)) \\
& + m*log(abs(f)*abs(x)) - 2*log(abs(f)*abs(x))) * \tan(1/4*\pi*b*c*x*sgn(F) - 1/4*\pi*b*c*x + \pi*m*floor(-1/4*sgn(f) - 1/4*sgn(x) + 1) + 1/4*\pi \\
& *m*sgn(f) + 1/4*\pi*m*sgn(x) - 1/2*\pi*m - 1/2*x*e - 2*\pi*floor(-1/4*sgn(f) - 1/4*sgn(x) + 1) - 1/2*\pi*sgn(f) - 1/2*\pi*sgn(x)) * \tan(1/4*\pi*a*c*sgn(F) - 1/4*\pi*a*c + 1 \\
& /2*d)^2 - x*abs(F)^(a*c)*e^(b*c*x*log(abs(F)) + m*log(abs(f)*abs(x)) - 2*log(abs(f)*abs(x))) * \tan(1/4*\pi*b*c*x*sgn(F) - 1/4*\pi*b*c*x + \pi*m*floor(-1/4* \\
& sgn(f) - 1/4*sgn(x) + 1) + 1/4*\pi*m*sgn(f) + 1/4*\pi*m*sgn(x) - 1/2*\pi*m + 1 \\
& /2*x*e - 2*\pi*floor(-1/4*sgn(f) - 1/4*sgn(x) + 1) - 1/2*\pi*sgn(f) - 1/2*\pi* \\
& sgn(x))^2 * \tan(1/4*\pi*a*c*sgn(F) - 1/4*\pi*a*c - 1/2*d) + x*abs(F)^(a*c)*e^(b \\
& *c*x*log(abs(F)) + m*log(abs(f)*abs(x)) - 2*log(abs(f)*abs(x))) * \tan(1/4*\pi* \\
& b*c*x*sgn(F) - 1/4*\pi*b*c*x + \pi*m*floor(-1/4*sgn(f) - 1/4*sgn(x) + 1) + 1/4*\pi \\
& *m*sgn(f) + 1/4*\pi*m*sgn(x) - 1/2*\pi*m - 1/2*x*e - 2*\pi*floor(-1/4*sgn(f) - \\
& 1/4*sgn(x) + 1) - 1/2*\pi*sgn(f) - 1/2*\pi*sgn(x))^2 * \tan(1/4*\pi*a*c*sgn(F) \\
& - 1/4*\pi*a*c - 1/2*d) - x*abs(F)^(a*c)*e^(b*c*x*log(abs(F)) + m*log(abs(f) \\
& *abs(x)) - 2*log(abs(f)*abs(x))) * \tan(1/4*\pi*a*c*sgn(F) - 1/4*\pi*a*c + 1/2 \\
& *d)^2 * \tan(1/4*\pi*a*c*sgn(F) - 1/4*\pi*a*c - 1/2*d) + x*abs(F)^(a*c)*e^(b*c*x \\
& *log(abs(F)) + m*log(abs(f)*abs(x)) - 2*log(abs(f)*abs(x))) * \tan(1/4*\pi*b*c* \\
& x*sgn(F) - 1/4*\pi*b*c*x + \pi*m*floor(-1/4*sgn(f) - 1/4*sgn(x) + 1) + 1/4*\pi \\
& *m*sgn(f) + 1/4*\pi*m*sgn(x) - 1/2*\pi*m + 1/2*x*e - 2*\pi*floor(-1/4*sgn(f) - \\
& 1/4*sgn(x) + 1) - 1/2*\pi*sgn(f) - 1/2*\pi*sgn(x)) * \tan(1/4*\pi*a*c*sgn(F) - 1 \\
& /4*\pi*a*c - 1/2*d)^2 + x*abs(F)^(a*c)*e^(b*c*x*log(abs(F)) + m*log(abs(f)*a \\
& bs(x)) - 2*log(abs(f)*abs(x))) * \tan(1/4*\pi*b*c*x*sgn(F) - 1/4*\pi*b*c*x + \pi* \\
& m*floor(-1/4*sgn(f) - 1/4*sgn(x) + 1) + 1/4*\pi*m*sgn(f) + 1/4*\pi*m*sgn(x) - \\
& 1/2*\pi*m - 1/2*x*e - 2*\pi*floor(-1/4*sgn(f) - 1/4*sgn(x) + 1) - 1/2*\pi*sgn \\
& (f) - 1/2*\pi*sgn(x)) * \tan(1/4*\pi*a*c*sgn(F) - 1/4*\pi*a*c - 1/2*d)^2 + x*abs(F) \\
&)^(a*c)*e^(b*c*x*log(abs(F)) + m*log(abs(f)*abs(x)) - 2*log(abs(f)*abs(x))) \\
&) * \tan(1/4*\pi*a*c*sgn(F) - 1/4*\pi*a*c + 1/2*d) * \tan(1/4*\pi*a*c*sgn(F) - 1/4*\pi \\
& *a*c - 1/2*d)^2 + x*abs(F)^(a*c)*e^(b*c*x*log(abs(F)) + m*log(abs(f)*abs(x) \\
&)) - 2*log(abs(f)*abs(x))) * \tan(1/4*\pi*b*c*x*sgn(F) - 1/4*\pi*b*c*x + \pi*m*fl \\
& oor(-1/4*sgn(f) - 1/4*sgn(x) + 1) + 1/4*\pi*m*sgn(f) + 1/4*\pi*m*sgn(x) - 1/2 \\
& *\pi*m + 1/2*x*e - 2*\pi*floor(-1/4*sgn(f) - 1/4*sgn(x) + 1) - 1/2*\pi*sgn(f) \\
& - 1/2*\pi*sgn(x)) - x*abs(F)^(a*c)*e^(b*c*x*log(abs(F)) + m*log(abs(f)*abs(x) \\
&)) - 2*log(abs(f)*abs(x))) * \tan(1/4*\pi*b*c*x*sgn(F) - 1/4*\pi*b*c*x + \pi*m*fl \\
& oor(-1/4*sgn(f) - 1/4*sgn(x) + 1) + 1/4*\pi*m*sgn(f) + 1/4*\pi*m*sgn(x) - 1/2 \\
& *\pi*m - 1/2*x*e - 2*\pi*floor(-1/4*sgn(f) - 1/4*sgn(x) + 1) - 1/2*\pi*sgn(f) \\
& - 1/2*\pi*sgn(x)) + x*abs(F)^(a*c)*e^(b*c*x*log(abs(F)) + m*log(abs(f)*abs(x) \\
&)) - 2*log(abs(f)*abs(x))) * \tan(1/4*\pi*a*c*sgn(F) - 1/4*\pi*a*c + 1/2*d) - x* \\
& abs(F)^(a*c)*e^(b*c*x*log(abs(F)) + m*log(abs(f)*abs(x)) - 2*log(abs(f)*abs \\
& (x))) * \tan(1/4*\pi*a*c*sgn(F) - 1/4*\pi*a*c - 1/2*d)) * f / (\tan(1/4*\pi*b*c*x*sgn(F) \\
& - 1/4*\pi*b*c*x + \pi*m*floor(-1/4*sgn(f) - 1/4*sgn(x) + 1) + 1/4*\pi*m*sgn \\
& (f) + 1/4*\pi*m*sgn(x) - 1/2*\pi*m + 1/2*x*e - 2*\pi*floor(-1/4*sgn(f) - 1/4*sg \\
& n(x) + 1) - 1/2*\pi*sgn(f) - 1/2*\pi*sgn(x))^2 * \tan(1/4*\pi*b*c*x*sgn(F) - 1/4 \\
& *\pi*b*c*x + \pi*m*floor(-1/4*sgn(f) - 1/4*sgn(x) + 1) + 1/4*\pi*m*sgn(f) + 1/ \\
& 4*\pi*m*sgn(x) - 1/2*\pi*m - 1/2*x*e - 2*\pi*floor(-1/4*sgn(f) - 1/4*sgn(x) + \\
& 1) - 1/2*\pi*sgn(f) - 1/2*\pi*sgn(x))^2 * \tan(1/4*\pi*a*c*sgn(F) - 1/4*\pi*a*c + \\
& 1/2*d)^2 * \tan(1/4*\pi*a*c*sgn(F) - 1/4*\pi*a*c - 1/2*d)^2 + \tan(1/4*\pi*b*c*x*sg \\
& n(F) - 1/4*\pi*b*c*x + \pi*m*floor(-1/4*sgn(f) - 1/4*sgn(x) + 1) + 1/4*\pi*m* \\
& sgn(f) + 1/4*\pi*m*sgn(x) - 1/2*\pi*m + 1/2*x*e - 2*\pi*floor(-1/4*sgn(f) - 1/ \\
& 4*sgn(x) + 1) - 1/2*\pi*sgn(f) - 1/2*\pi*sgn(x))^2 * \tan(1/4*\pi*b*c*x*sgn(F) -
\end{aligned}$$

$$\begin{aligned}
 & 1/4*\pi*b*c*x + \pi*m*\text{floor}(-1/4*\text{sgn}(f) - 1/4*\text{sgn}(x) + 1) + 1/4*\pi*m*\text{sgn}(f) + \\
 & 1/4*\pi*m*\text{sgn}(x) - 1/2*\pi*m - 1/2*x*e - 2*\pi*\text{floor}(-1/4*\text{sgn}(f) - 1/4*\text{sgn}(x) \\
 & + 1) - 1/2*\pi*\text{sgn}(f) - 1/2*\pi*\text{sgn}(x))^2*\tan(1/4*\pi*a*c*\text{sgn}(F) - 1/4*\pi*a*c \\
 & + 1/2*d)^2 + \tan(1/4*\pi*b*c*x*\text{sgn}(F) - 1/4*\pi*b*c*x + \pi*m*\text{floor}(-1/4*\text{sgn}(f) \\
 & - 1/4*\text{sgn}(x) + 1) + 1/4*\pi*m*\text{sgn}(f) + 1/4*\pi*m*\text{sgn}(x) - 1/2*\pi*m + 1/2*x \\
 & *e - 2*\pi*\text{floor}(-1/4*\text{sgn}(f) - 1/4*\text{sgn}(x) + 1) - 1/2*\pi*\text{sgn}(f) - 1/2*\pi*\text{sgn}(\\
 & x))^2*\tan(1/4*\pi*b*c*x*\text{sgn}(F) - 1/4*\pi*b*c*x + \pi*m*\text{floor}(-1/4*\text{sgn}(f) - 1/4 \\
 & *\text{sgn}(x) + 1) + 1/4*\pi*m*\text{sgn}(f) + 1/4*\pi*m*\text{sgn}(x) - 1/2*\pi*m - 1/2*x*e - 2*\pi \\
 & *\text{floor}(-1/4*\text{sgn}(f) - 1/4*\text{sgn}(x) + 1) - 1/2*\pi*\text{sgn}(f) - 1/2*\pi*\text{sgn}(x))^2*\tan \\
 & (1/4*\pi*a*c*\text{sgn}(F) - 1/4*\pi*a*c - 1/2*d)^2 + \tan(1/4*\pi*b*c*x*\text{sgn}(F) - 1/4 \\
 & *\pi*b*c*x + \pi*m*\text{floor}(-1/4*\text{sgn}(f) - 1/4*\text{sgn}(x) + 1) + 1/4*\pi*m*\text{sgn}(f) + 1/ \\
 & 4*\pi*m*\text{sgn}(x) - 1/2*\pi*m + 1/2*x*e - 2*\pi*\text{floor}(-1/4*\text{sgn}(f) - 1/4*\text{sgn}(x) + \\
 & 1) - 1/2*\pi*\text{sgn}(f) - 1/2*\pi*\text{sgn}(x))^2*\tan(1/4*\pi*a*c*\text{sgn}(F) - 1/4*\pi*a*c + \\
 & 1/2*d)^2*\tan(1/4*\pi*a*c*\text{sgn}(F) - 1/4*\pi*a*c - 1/2*d)^2 + \tan(1/4*\pi*b*c*x*s \\
 & \text{gn}(F) - 1/4*\pi*b*c*x + \pi*m*\text{floor}(-1/4*\text{sgn}(f) - 1/4*\text{sgn}(x) + 1) + 1/4*\pi*m* \\
 & \text{sgn}(f) + 1/4*\pi*m*\text{sgn}(x) - 1/2*\pi*m - 1/2*x*e - 2*\pi*\text{floor}(-1/4*\text{sgn}(f) - 1/ \\
 & 4*\text{sgn}(x) + 1) - 1/2*\pi*\text{sgn}(f) - 1/2*\pi*\text{sgn}(x))^2*\tan(1/4*\pi*a*c*\text{sgn}(F) - 1/ \\
 & 4*\pi*a*c + 1/2*d)^2*\tan(1/4*\pi*a*c*\text{sgn}(F) - 1/4*\pi*a*c - 1/2*d)^2 + \tan(1/4 \\
 & *\pi*b*c*x*\text{sgn}(F) - 1/4*\pi*b*c*x + \pi*m*\text{floor}(-1/4*\text{sgn}(f) - 1/4*\text{sgn}(x) + 1) \\
 & + 1/4*\pi*m*\text{sgn}(f) + 1/4*\pi*m*\text{sgn}(x) - 1/2*\pi*m + 1/2*x*e - 2*\pi*\text{floor}(-1/4* \\
 & \text{sgn}(f) - 1/4*\text{sgn}(x) + 1) - 1/2*\pi*\text{sgn}(f) - 1/2*\pi*\text{sgn}(x))^2*\tan(1/4*\pi*b*c* \\
 & x*\text{sgn}(F) - 1/4*\pi*b*c*x + \pi*m*\text{floor}(-1/4*\text{sgn}(f) - 1/4*\text{sgn}(x) + 1) + 1/4*\pi \\
 & *m*\text{sgn}(f) + 1/4*\pi*m*\text{sgn}(x) - 1/2*\pi*m - 1/2*x*e - 2*\pi*\text{floor}(-1/4*\text{sgn}(f) - \\
 & 1/4*\text{sgn}(x) + 1) - 1/2*\pi*\text{sgn}(f) - 1/2*\pi*\text{sgn}(x))^2 + \tan(1/4*\pi*b*c*x*\text{sgn}(\\
 & F) - 1/4*\pi*b*c*x + \pi*m*\text{floor}(-1/4*\text{sgn}(f) - 1/4*\text{sgn}(x) + 1) + 1/4*\pi*m*\text{sgn} \\
 & (f) + 1/4*\pi*m*\text{sgn}(x) - 1/2*\pi*m + 1/2*x*e - 2*\pi*\text{floor}(-1/4*\text{sgn}(f) - 1/4*s \\
 & \text{gn}(x) + 1) - 1/2*\pi*\text{sgn}(f) - 1/2*\pi*\text{sgn}(x))^2*\tan(1/4*\pi*a*c*\text{sgn}(F) - 1/4*\pi \\
 & *a*c + 1/2*d)^2 + \tan(1/4*\pi*b*c*x*\text{sgn}(F) - 1/4*\pi*b*c*x + \pi*m*\text{floor}(-1/4 \\
 & *\text{sgn}(f) - 1/4*\text{sgn}(x) + 1) + 1/4*\pi*m*\text{sgn}(f) + 1/4*\pi*m*\text{sgn}(x) - 1/2*\pi*m - \\
 & 1/2*x*e - 2*\pi*\text{floor}(-1/4*\text{sgn}(f) - 1/4*\text{sgn}(x) + 1) - 1/2*\pi*\text{sgn}(f) - 1/2*\pi \\
 & *\text{sgn}(x))^2*\tan(1/4*\pi*a*c*\text{sgn}(F) - 1/4*\pi*a*c + 1/2*d)^2 + \tan(1/4*\pi*b*c*x \\
 & *\text{sgn}(F) - 1/4*\pi*b*c*x + \pi*m*\text{floor}(-1/4*\text{sgn}(f) - 1/4*\text{sgn}(x) + 1) + 1/4*\pi \\
 & *m*\text{sgn}(f) + 1/4*\pi*m*\text{sgn}(x) - 1/2*\pi*m + 1/2*x*e - 2*\pi*\text{floor}(-1/4*\text{sgn}(f) - \\
 & 1/4*\text{sgn}(x) + 1) - 1/2*\pi*\text{sgn}(f) - 1/2*\pi*\text{sgn}(x))^2*\tan(1/4*\pi*a*c*\text{sgn}(F) - \\
 & 1/4*\pi*a*c - 1/2*d)^2 + \tan(1/4*\pi*b*c*x*\text{sgn}(F) - 1/4*\pi*b*c*x + \pi*m*\text{floor} \\
 & (-1/4*\text{sgn}(f) - 1/4*\text{sgn}(x) + 1) + 1/4*\pi*m*\text{sgn}(f) + 1/4*\pi*m*\text{sgn}(x) - 1/2*\pi \\
 & *m - 1/2*x*e - 2*\pi*\text{floor}(-1/4*\text{sgn}(f) - 1/4*\text{sgn}(x) + 1) - 1/2*\pi*\text{sgn}(f) - 1 \\
 & /2*\pi*\text{sgn}(x))^2*\tan(1/4*\pi*a*c*\text{sgn}(F) - 1/4*\pi*a*c - 1/2*d)^2 + \tan(1/4*\pi* \\
 & a*c*\text{sgn}(F) - 1/4*\pi*a*c + 1/2*d)^2*\tan(1/4*\pi*a*c*\text{sgn}(F) - 1/4*\pi*a*c - 1/2 \\
 & *d)^2 + \tan(1/4*\pi*b*c*x*\text{sgn}(F) - 1/4*\pi*b*c*x + \pi*m*\text{floor}(-1/4*\text{sgn}(f) - 1 \\
 & /4*\text{sgn}(x) + 1) + 1/4*\pi*m*\text{sgn}(f) + 1/4*\pi*m*\text{sgn}(x) - 1/2*\pi*m + 1/2*x*e - 2 \\
 & *\pi*\text{floor}(-1/4*\text{sgn}(f) - 1/4*\text{sgn}(x) + 1) - 1/2*\pi*\text{sgn}(f) - 1/2*\pi*\text{sgn}(x))^2 \\
 & + \tan(1/4*\pi*b*c*x*\text{sgn}(F) - 1/4*\pi*b*c*x + \pi*m*\text{floor}(-1/4*\text{sgn}(f) - 1/4*\text{sgn} \\
 & (x) + 1) + 1/4*\pi*m*\text{sgn}(f) + 1/4*\pi*m*\text{sgn}(x) - 1/2*\pi*m - 1/2*x*e - 2*\pi*\text{fl \\
 & oor}(-1/4*\text{sgn}(f) - 1/4*\text{sgn}(x) + 1) - 1/2*\pi*\text{sgn}(f) - 1/2*\pi*\text{sgn}(x))^2 + \tan(\\
 & 1/4*\pi*a*c*\text{sgn}(F) - 1/4*\pi*a*c + 1/2*d)^2 + \tan(1/4*\pi*a*c*\text{sgn}(F) - 1/4*\pi* \\
 & a*c - 1/2*d)^2 + 1)
 \end{aligned}$$

maple [C] time = 0.37, size = 213, normalized size = 8.88

$$\frac{iF^{c(bx+a)}xf \left(\frac{f^m x^m e^{iex} e^{id} e^{-\frac{i\text{ncsgn}(ifx)^3 m}{2}} e^{\frac{i\text{ncsgn}(ifx)^2 \text{csgn}(if)m}{2}} e^{\frac{i\text{ncsgn}(ifx)^2 \text{csgn}(ix)m}{2}} e^{-\frac{i\pi \text{csgn}(ifx) \text{csgn}(if) \text{csgn}(ix)m}{2}}}{f^2 x^2} - \frac{f^m x^m e^{-iex} e^{-id} e^{-\frac{i\text{ncsgn}(ifx)^3 m}{2}}}{2} \right)}{2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(f*F^(c*(b*x+a))*(f*x)^(-2+m)*(e*x*cos(e*x+d)+(-1+m+b*c*x*ln(F))*sin(e*x+d)), x)

[Out] $-1/2*I*F^{(c*(b*x+a))*x*f*(f^m*x^m/f^2/x^2*\exp(I*e*x)*\exp(I*d)*\exp(-1/2*I*Pi*csgn(I*f*x)^3*m)*\exp(1/2*I*Pi*csgn(I*f*x)^2*csgn(I*f)*m)*\exp(1/2*I*Pi*csgn(I*f*x)^2*csgn(I*x)*m)*\exp(-1/2*I*Pi*csgn(I*f*x)*csgn(I*f)*csgn(I*x)*m)-f^m*x^m/f^2/x^2*\exp(-I*e*x)*\exp(-I*d)*\exp(-1/2*I*Pi*csgn(I*f*x)^3*m)*\exp(1/2*I*Pi*csgn(I*f*x)^2*csgn(I*f)*m)*\exp(1/2*I*Pi*csgn(I*f*x)^2*csgn(I*x)*m)*\exp(-1/2*I*Pi*csgn(I*f*x)*csgn(I*f)*csgn(I*x)*m)}$

maxima [A] time = 0.73, size = 32, normalized size = 1.33

$$\frac{F^{ac} f^{m-1} e^{(bcx \log(F) + m \log(x))} \sin(ex + d)}{x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(f*F^(c*(b*x+a))*(f*x)^(-2+m)*(e*x*cos(e*x+d)+(-1+m+b*c*x*log(F))*sin(e*x+d)),x, algorithm="maxima")`

[Out] $F^{(a*c)}*f^{(m-1)}*e^{(b*c*x*\log(F) + m*\log(x))*\sin(e*x + d)/x}$

mupad [B] time = 2.90, size = 27, normalized size = 1.12

$$\frac{F^{c(a+bx)} \sin(d + ex) (fx)^m}{fx}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(F^(c*(a + b*x))*f*(f*x)^(m - 2)*(sin(d + e*x)*(m + b*c*x*log(F) - 1) + e*x*cos(d + e*x)),x)`

[Out] $(F^{c*(a + b*x)}*\sin(d + e*x)*(f*x)^m)/(f*x)$

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(f*F**(c*(b*x+a))*(f*x)**(-2+m)*(e*x*cos(e*x+d)+(-1+m+b*c*x*ln(F))*sin(e*x+d)),x)`

[Out] Timed out

$$3.32 \quad \int f F^{c(a+bx)} (fx)^m (ex \cos(d+ex) + (1+m+bcx \log(F)) \sin(d+ex)) dx$$

Optimal. Leaf size=23

$$fx(fx)^m \sin(d+ex)F^{c(a+bx)}$$

[Out] $f * F^{(c * (b * x + a)) * x * (f * x)^m * \sin(e * x + d)}$

Rubi [F] time = 2.34, antiderivative size = 0, normalized size of antiderivative = 0.00, number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int f F^{c(a+bx)} (fx)^m (ex \cos(d+ex) + (1+m+bcx \log(F)) \sin(d+ex)) dx$$

Verification is Not applicable to the result.

[In] $\text{Int}[f * F^{(c * (a + b * x)) * (f * x)^m * (e * x * \text{Cos}[d + e * x] + (1 + m + b * c * x * \text{Log}[F])) * \text{Sin}[d + e * x]}, x]$

[Out] $e * \text{Defer}[\text{Int}[F^{(a * c + b * c * x)} * (f * x)^{(1 + m)} * \text{Cos}[d + e * x], x] + f * (1 + m) * \text{Defer}[\text{Int}[F^{(a * c + b * c * x)} * (f * x)^m * \text{Sin}[d + e * x], x] + b * c * \text{Log}[F] * \text{Defer}[\text{Int}[F^{(a * c + b * c * x)} * (f * x)^{(1 + m)} * \text{Sin}[d + e * x], x]$

Rubi steps

$$\begin{aligned} \int f F^{c(a+bx)} (fx)^m (ex \cos(d+ex) + (1+m+bcx \log(F)) \sin(d+ex)) dx &= f \int F^{c(a+bx)} (fx)^m (ex \cos(d+ex) + (1+m+bcx \log(F)) \sin(d+ex)) dx \\ &= f \int F^{ac+bcx} (fx)^m (ex \cos(d+ex) + (1+m+bcx \log(F)) \sin(d+ex)) dx \\ &= f \int \left(\frac{e F^{ac+bcx} (fx)^{1+m} \cos(d+ex)}{f} + F^{ac+bcx} (fx)^m \sin(d+ex) \right) dx \\ &= e \int F^{ac+bcx} (fx)^{1+m} \cos(d+ex) dx + f \int F^{ac+bcx} (fx)^m \sin(d+ex) dx \\ &= e \int F^{ac+bcx} (fx)^{1+m} \cos(d+ex) dx + f \int F^{ac+bcx} (fx)^m \sin(d+ex) dx \\ &= e \int F^{ac+bcx} (fx)^{1+m} \cos(d+ex) dx + f \int F^{ac+bcx} (fx)^m \sin(d+ex) dx \end{aligned}$$

Mathematica [A] time = 0.93, size = 23, normalized size = 1.00

$$fx(fx)^m \sin(d+ex)F^{c(a+bx)}$$

Antiderivative was successfully verified.

[In] $\text{Integrate}[f * F^{(c * (a + b * x)) * (f * x)^m * (e * x * \text{Cos}[d + e * x] + (1 + m + b * c * x * \text{Log}[F])) * \text{Sin}[d + e * x]}, x]$

[Out] $f * F^{(c * (a + b * x)) * x * (f * x)^m * \text{Sin}[d + e * x]}$

fricas [A] time = 0.80, size = 24, normalized size = 1.04

$$(fx)^m F^{bcx+ac} fx \sin(ex+d)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{integrate}(f * F^{(c * (b * x + a)) * (f * x)^m * (e * x * \cos(e * x + d) + (1 + m + b * c * x * \log(F)) * \sin(e * x + d)), x, \text{algorithm} = \text{"fricas"})$

maple [C] time = 0.26, size = 201, normalized size = 8.74

$$iF^{c(bx+a)} x f \left(f^m x^m e^{iex} e^{id} e^{-\frac{i\text{csgn}(ifx)^3 m}{2}} e^{\frac{i\text{csgn}(ifx)^2 \text{csgn}(if)m}{2}} e^{\frac{i\text{csgn}(ifx)^2 \text{csgn}(ix)m}{2}} e^{-\frac{i\text{csgn}(ifx)\text{csgn}(if)\text{csgn}(ix)m}{2}} - f^m x^m e^{-iex} e^{-id} e^{-\frac{i\text{csgn}(ifx)^3 m}{2}} e^{\frac{i\text{csgn}(ifx)^2 \text{csgn}(if)m}{2}} e^{\frac{i\text{csgn}(ifx)^2 \text{csgn}(ix)m}{2}} e^{-\frac{i\text{csgn}(ifx)\text{csgn}(if)\text{csgn}(ix)m}{2}} \right)$$

2

Verification of antiderivative is not currently implemented for this CAS.

[In] int(f*F^(c*(b*x+a))*(f*x)^m*(e*x*cos(e*x+d)+(1+m+b*c*x*ln(F))*sin(e*x+d)),x)

[Out] $-1/2*I*F^{c*(b*x+a)}*x*f*(f^m*x^m*\exp(I*e*x)*\exp(I*d)*\exp(-1/2*I*Pi*\text{csgn}(I*f*x)^3*m)*\exp(1/2*I*Pi*\text{csgn}(I*f*x)^2*\text{csgn}(I*f)*m)*\exp(1/2*I*Pi*\text{csgn}(I*f*x)^2*\text{csgn}(I*x)*m)*\exp(-1/2*I*Pi*\text{csgn}(I*f*x)*\text{csgn}(I*f)*\text{csgn}(I*x)*m)-f^m*x^m*\exp(-I*e*x)*\exp(-I*d)*\exp(-1/2*I*Pi*\text{csgn}(I*f*x)^3*m)*\exp(1/2*I*Pi*\text{csgn}(I*f*x)^2*\text{csgn}(I*f)*m)*\exp(1/2*I*Pi*\text{csgn}(I*f*x)^2*\text{csgn}(I*x)*m)*\exp(-1/2*I*Pi*\text{csgn}(I*f*x)*\text{csgn}(I*f)*\text{csgn}(I*x)*m)$

maxima [A] time = 0.70, size = 30, normalized size = 1.30

$$F^{ac} f^{m+1} x e^{(bcx \log(F) + m \log(x))} \sin(ex + d)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f*F^(c*(b*x+a))*(f*x)^m*(e*x*cos(e*x+d)+(1+m+b*c*x*log(F))*sin(e*x+d)),x, algorithm="maxima")

[Out] $F^{(a*c)}*f^{(m+1)}*x*e^{(b*c*x*\log(F)+m*\log(x))*\sin(e*x+d)}$

mupad [B] time = 2.86, size = 23, normalized size = 1.00

$$F^{c(a+bx)} f x \sin(d + ex) (f x)^m$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(F^(c*(a+b*x))*f*(f*x)^m*(sin(d+e*x)*(m+b*c*x*log(F)+1)+e*x*cos(d+e*x)),x)

[Out] $F^{c*(a+b*x)}*f*x*\sin(d+e*x)*(f*x)^m$

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f*F**(c*(b*x+a))*(f*x)**m*(e*x*cos(e*x+d)+(1+m+b*c*x*ln(F))*sin(e*x+d)),x)

[Out] Timed out

$$3.33 \quad \int \frac{F^{c(a+bx)}(fx)^m(ex \cos(d+ex) + (m+bcx \log(F)) \sin(d+ex))}{x} dx$$

Optimal. Leaf size=22

$$(fx)^m \sin(d+ex) F^{ac+bcx}$$

[Out] $F^{(b*c*x+a*c)}*(f*x)^m*\sin(e*x+d)$

Rubi [A] time = 2.56, antiderivative size = 22, normalized size of antiderivative = 1.00, number of steps used = 7, number of rules used = 4, integrand size = 43, $\frac{\text{number of rules}}{\text{integrand size}} = 0.093$, Rules used = {16, 6741, 6742, 4467}

$$(fx)^m \sin(d+ex) F^{ac+bcx}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(F^{(c*(a+b*x))}*(f*x)^m*(e*x*\text{Cos}[d+e*x] + (m+b*c*x*\text{Log}[F])* \text{Sin}[d+e*x]))/x, x]$

[Out] $F^{(a*c+b*c*x)}*(f*x)^m*\text{Sin}[d+e*x]$

Rule 16

$\text{Int}[(u_)*(v_)^{(m_)}*((b_)*(v_))^{(n_)}, x_Symbol] \rightarrow \text{Dist}[1/b^m, \text{Int}[u*(b*v)^{(m+n)}, x], x] /;$ FreeQ[{b, n}, x] && IntegerQ[m]

Rule 4467

$\text{Int}[(F_)^{((c_)*((a_)+(b_)*(x_)))*((f_)*(x_))^{(m_)}*\text{Sin}[(d_)+(e_)*(x_)]}, x_Symbol] \rightarrow \text{Simp}[(f*x)^{(m+1)}*F^{(c*(a+b*x))*\text{Sin}[d+e*x]}/(f*(m+1)), x] + (-\text{Dist}[e/(f*(m+1)), \text{Int}[(f*x)^{(m+1)}*F^{(c*(a+b*x))*\text{Cos}[d+e*x]}, x], x] - \text{Dist}[(b*c*\text{Log}[F])/(f*(m+1)), \text{Int}[(f*x)^{(m+1)}*F^{(c*(a+b*x))*\text{Sin}[d+e*x]}, x], x]) /;$ FreeQ[{F, a, b, c, d, e, f, m}, x] && (LtQ[m, -1] || SumSimplerQ[m, 1])

Rule 6741

$\text{Int}[u_, x_Symbol] \rightarrow \text{With}[\{v = \text{NormalizeIntegrand}[u, x]\}, \text{Int}[v, x] /;$ v != u]

Rule 6742

$\text{Int}[u_, x_Symbol] \rightarrow \text{With}[\{v = \text{ExpandIntegrand}[u, x]\}, \text{Int}[v, x] /;$ SumQ[v]

Rubi steps

$$\begin{aligned}
 \int \frac{F^{c(a+bx)}(fx)^m(ex \cos(d+ex) + (m+bcx \log(F)) \sin(d+ex))}{x} dx &= f \int F^{c(a+bx)}(fx)^{-1+m}(ex \cos(d+ex) + (m+bcx \log(F)) \sin(d+ex)) dx \\
 &= f \int F^{ac+bcx}(fx)^{-1+m}(ex \cos(d+ex) + (m+bcx \log(F)) \sin(d+ex)) dx \\
 &= f \int \left(\frac{eF^{ac+bcx}(fx)^m \cos(d+ex)}{f} + F^{ac+bcx}(fx)^m \sin(d+ex) \right) dx \\
 &= e \int F^{ac+bcx}(fx)^m \cos(d+ex) dx + f \int F^{ac+bcx}(fx)^m \sin(d+ex) dx \\
 &= e \int F^{ac+bcx}(fx)^m \cos(d+ex) dx + f \int \left(F^{ac+bcx}(fx)^m \sin(d+ex) \right) dx \\
 &= e \int F^{ac+bcx}(fx)^m \cos(d+ex) dx + (fm) \int F^{ac+bcx}(fx)^m \sin(d+ex) dx \\
 &= F^{ac+bcx}(fx)^m \sin(d+ex)
 \end{aligned}$$

Mathematica [A] time = 0.87, size = 22, normalized size = 1.00

$$(fx)^m \sin(d+ex) F^{ac+bcx}$$

Antiderivative was successfully verified.

```
[In] Integrate[(F^(c*(a + b*x))*(f*x)^m*(e*x*Cos[d + e*x] + (m + b*c*x*Log[F]))*Sin[d + e*x])/x,x]
```

```
[Out] F^(a*c + b*c*x)*(f*x)^m*Sin[d + e*x]
```

fricas [A] time = 0.65, size = 22, normalized size = 1.00

$$(fx)^m F^{bcx+ac} \sin(ex+d)$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(F^(c*(b*x+a))*(f*x)^m*(e*x*cos(e*x+d)+(m+b*c*x*log(F))*sin(e*x+d))/x,x, algorithm="fricas")
```

```
[Out] (f*x)^m*F^(b*c*x + a*c)*sin(e*x + d)
```

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(ex \cos(ex+d) + (bcx \log(F) + m) \sin(ex+d)) (fx)^m F^{(bx+a)c}}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(F^(c*(b*x+a))*(f*x)^m*(e*x*cos(e*x+d)+(m+b*c*x*log(F))*sin(e*x+d))/x,x, algorithm="giac")
```

```
[Out] integrate((e*x*cos(e*x + d) + (b*c*x*log(F) + m)*sin(e*x + d))*(f*x)^m*F^((b*x + a)*c)/x, x)
```

maple [C] time = 0.23, size = 199, normalized size = 9.05

$$iF^{c(bx+a)} \left(f^m x^m e^{ix} e^{id} e^{-\frac{i\pi \operatorname{csgn}(ifx)^3}{2}} e^{\frac{i\pi \operatorname{csgn}(ifx)^2 \operatorname{csgn}(if)m}{2}} e^{\frac{i\pi \operatorname{csgn}(ifx)^2 \operatorname{csgn}(ix)m}{2}} e^{-\frac{i\pi \operatorname{csgn}(ifx) \operatorname{csgn}(if) \operatorname{csgn}(ix)m}{2}} - f^m x^m e^{-ix} e^{-id} e^{-\frac{i\pi \operatorname{csgn}(ifx)^3}{2}} e^{\frac{i\pi \operatorname{csgn}(ifx)^2 \operatorname{csgn}(if)m}{2}} e^{\frac{i\pi \operatorname{csgn}(ifx)^2 \operatorname{csgn}(ix)m}{2}} e^{-\frac{i\pi \operatorname{csgn}(ifx) \operatorname{csgn}(if) \operatorname{csgn}(ix)m}{2}} \right)$$

Verification of antiderivative is not currently implemented for this CAS.


```
[In] int(F^(c*(b*x+a))*(f*x)^m*(e*x*cos(e*x+d)+(m+b*c*x*ln(F))*sin(e*x+d))/x,x)
[Out] -1/2*I*F^(c*(b*x+a))*(f^m*x^m*exp(I*e*x)*exp(I*d)*exp(-1/2*I*Pi*csgn(I*f*x)
^3*m)*exp(1/2*I*Pi*csgn(I*f*x)^2*csgn(I*f)*m)*exp(1/2*I*Pi*csgn(I*f*x)^2*cs
gn(I*x)*m)*exp(-1/2*I*Pi*csgn(I*f*x)*csgn(I*f)*csgn(I*x)*m)-f^m*x^m*exp(-I*
e*x)*exp(-I*d)*exp(-1/2*I*Pi*csgn(I*f*x)^3*m)*exp(1/2*I*Pi*csgn(I*f*x)^2*cs
gn(I*f)*m)*exp(1/2*I*Pi*csgn(I*f*x)^2*csgn(I*x)*m)*exp(-1/2*I*Pi*csgn(I*f*x
)*csgn(I*f)*csgn(I*x)*m))
```

maxima [A] time = 0.71, size = 27, normalized size = 1.23

$$F^{ac} f^m e^{(bcx \log(F) + m \log(x))} \sin(ex + d)$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(F^(c*(b*x+a))*(f*x)^m*(e*x*cos(e*x+d)+(m+b*c*x*log(F))*sin(e*x+d)
)/x,x, algorithm="maxima")
```

```
[Out] F^(a*c)*f^m*e^(b*c*x*log(F) + m*log(x))*sin(e*x + d)
```

mupad [B] time = 2.80, size = 21, normalized size = 0.95

$$F^{c(a+bx)} \sin(d + ex) (fx)^m$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((F^(c*(a + b*x))*(f*x)^m*(sin(d + e*x)*(m + b*c*x*log(F)) + e*x*cos(d +
e*x)))/x,x)
```

```
[Out] F^(c*(a + b*x))*sin(d + e*x)*(f*x)^m
```

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(F**(c*(b*x+a))*(f*x)**m*(e*x*cos(e*x+d)+(m+b*c*x*ln(F))*sin(e*x+d)
))/x,x)
```

```
[Out] Timed out
```

$$3.34 \quad \int F^{c(a+bx)}(ex \cos(d+ex)+(1+bcx \log(F)) \sin(d+ex)) dx$$

Optimal. Leaf size=17

$$x \sin(d + ex) F^{c(a+bx)}$$

[Out] $F^{c*(b*x+a)}*x*\sin(e*x+d)$

Rubi [B] time = 0.77, antiderivative size = 327, normalized size of antiderivative = 19.24, number of steps used = 14, number of rules used = 6, integrand size = 35, $\frac{\text{number of rules}}{\text{integrand size}} = 0.171$, Rules used = {6741, 6742, 4433, 4466, 4432, 4465}

$$\frac{b^2 c^2 x \log^2(F) \sin(d + ex) F^{ac+bcx}}{b^2 c^2 \log^2(F) + e^2} + \frac{e^2 x \sin(d + ex) F^{ac+bcx}}{b^2 c^2 \log^2(F) + e^2} + \frac{bc \log(F) \sin(d + ex) F^{ac+bcx}}{b^2 c^2 \log^2(F) + e^2} - \frac{b^3 c^3 \log^3(F) \sin(d + ex) F^{ac+bcx}}{(b^2 c^2 \log^2(F) + e^2)^2}$$

Antiderivative was successfully verified.

[In] Int[F^(c*(a + b*x))*(e*x*Cos[d + e*x] + (1 + b*c*x*Log[F])*Sin[d + e*x]),x]

[Out] $(e^3 F^{a*c + b*c*x} * \text{Cos}[d + e*x]) / (e^2 + b^2 * c^2 * \text{Log}[F]^2)^2 + (b^2 * c^2 * e * F^{a*c + b*c*x} * \text{Cos}[d + e*x] * \text{Log}[F]^2) / (e^2 + b^2 * c^2 * \text{Log}[F]^2)^2 - (e * F^{a*c + b*c*x} * \text{Cos}[d + e*x]) / (e^2 + b^2 * c^2 * \text{Log}[F]^2) - (b * c * e^2 * F^{a*c + b*c*x} * \text{Log}[F] * \text{Sin}[d + e*x]) / (e^2 + b^2 * c^2 * \text{Log}[F]^2)^2 - (b^3 * c^3 * F^{a*c + b*c*x} * \text{Log}[F]^3 * \text{Sin}[d + e*x]) / (e^2 + b^2 * c^2 * \text{Log}[F]^2)^2 + (e^2 * F^{a*c + b*c*x} * x * \text{Sin}[d + e*x]) / (e^2 + b^2 * c^2 * \text{Log}[F]^2) + (b * c * F^{a*c + b*c*x} * \text{Log}[F] * \text{Sin}[d + e*x]) / (e^2 + b^2 * c^2 * \text{Log}[F]^2) + (b^2 * c^2 * F^{a*c + b*c*x} * x * \text{Log}[F]^2 * \text{Sin}[d + e*x]) / (e^2 + b^2 * c^2 * \text{Log}[F]^2)$

Rule 4432

Int[(F_)^((c_.)*((a_.) + (b_.)*(x_)))*Sin[(d_.) + (e_.)*(x_)], x_Symbol] :> Simp[(b*c*Log[F]*F^(c*(a + b*x))*Sin[d + e*x])/(e^2 + b^2*c^2*Log[F]^2), x] - Simp[(e*F^(c*(a + b*x))*Cos[d + e*x])/(e^2 + b^2*c^2*Log[F]^2), x] /; FreeQ[{F, a, b, c, d, e}, x] && NeQ[e^2 + b^2*c^2*Log[F]^2, 0]

Rule 4433

Int[Cos[(d_.) + (e_.)*(x_)]*(F_)^((c_.)*((a_.) + (b_.)*(x_))), x_Symbol] :> Simp[(b*c*Log[F]*F^(c*(a + b*x))*Cos[d + e*x])/(e^2 + b^2*c^2*Log[F]^2), x] + Simp[(e*F^(c*(a + b*x))*Sin[d + e*x])/(e^2 + b^2*c^2*Log[F]^2), x] /; FreeQ[{F, a, b, c, d, e}, x] && NeQ[e^2 + b^2*c^2*Log[F]^2, 0]

Rule 4465

Int[(F_)^((c_.)*((a_.) + (b_.)*(x_)))*((f_.)*(x_)^(m_.)*Sin[(d_.) + (e_.)*(x_)^(n_.)], x_Symbol] :> Module[{u = IntHide[F^(c*(a + b*x))*Sin[d + e*x]^n, x]}, Dist[(f*x)^m, u, x] - Dist[f*m, Int[(f*x)^(m - 1)*u, x], x] /; FreeQ[{F, a, b, c, d, e, f}, x] && IGtQ[n, 0] && GtQ[m, 0]

Rule 4466

Int[Cos[(d_.) + (e_.)*(x_)]^(n_.)*(F_)^((c_.)*((a_.) + (b_.)*(x_)))*((f_.)*(x_)^(m_.)], x_Symbol] :> Module[{u = IntHide[F^(c*(a + b*x))*Cos[d + e*x]^n, x]}, Dist[(f*x)^m, u, x] - Dist[f*m, Int[(f*x)^(m - 1)*u, x], x] /; FreeQ[{F, a, b, c, d, e, f}, x] && IGtQ[n, 0] && GtQ[m, 0]

Rule 6741

Int[u_, x_Symbol] :=> With[{v = NormalizeIntegrand[u, x]}, Int[v, x] /; v != u]

Rule 6742

Int[u_, x_Symbol] :=> With[{v = ExpandIntegrand[u, x]}, Int[v, x] /; SumQ[v]

Rubi steps

$$\begin{aligned}
 \int F^{c(a+bx)}(ex \cos(d+ex) + (1+bcx \log(F)) \sin(d+ex)) dx &= \int F^{ac+bcx}(ex \cos(d+ex) + (1+bcx \log(F)) \sin(d+ex)) dx \\
 &= \int (eF^{ac+bcx}x \cos(d+ex) + F^{ac+bcx}(1+bcx \log(F)) \sin(d+ex)) dx \\
 &= e \int F^{ac+bcx}x \cos(d+ex) dx + \int F^{ac+bcx}(1+bcx \log(F)) \sin(d+ex) dx \\
 &= \frac{bceF^{ac+bcx}x \cos(d+ex) \log(F)}{e^2 + b^2c^2 \log^2(F)} + \frac{e^2F^{ac+bcx}x \sin(d+ex)}{e^2 + b^2c^2 \log^2(F)} \\
 &= \frac{bceF^{ac+bcx}x \cos(d+ex) \log(F)}{e^2 + b^2c^2 \log^2(F)} + \frac{e^2F^{ac+bcx}x \sin(d+ex)}{e^2 + b^2c^2 \log^2(F)} \\
 &= \frac{e^3F^{ac+bcx} \cos(d+ex)}{(e^2 + b^2c^2 \log^2(F))^2} - \frac{b^2c^2eF^{ac+bcx} \cos(d+ex)}{(e^2 + b^2c^2 \log^2(F))} \\
 &= \frac{e^3F^{ac+bcx} \cos(d+ex)}{(e^2 + b^2c^2 \log^2(F))^2} - \frac{b^2c^2eF^{ac+bcx} \cos(d+ex)}{(e^2 + b^2c^2 \log^2(F))} \\
 &= \frac{e^3F^{ac+bcx} \cos(d+ex)}{(e^2 + b^2c^2 \log^2(F))^2} + \frac{b^2c^2eF^{ac+bcx} \cos(d+ex)}{(e^2 + b^2c^2 \log^2(F))}
 \end{aligned}$$

Mathematica [A] time = 0.41, size = 17, normalized size = 1.00

$$x \sin(d+ex)F^{c(a+bx)}$$

Antiderivative was successfully verified.

[In] Integrate[F^(c*(a + b*x))*(e*x*Cos[d + e*x] + (1 + b*c*x*Log[F]))*Sin[d + e*x], x]

[Out] F^(c*(a + b*x))*x*Sin[d + e*x]

fricas [A] time = 4.00, size = 18, normalized size = 1.06

$$F^{bcx+ac}x \sin(ex+d)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(F^(c*(b*x+a))*(e*x*cos(e*x+d)+(1+b*c*x*log(F))*sin(e*x+d)), x, algorithm="fricas")

[Out] F^(b*c*x + a*c)*x*sin(e*x + d)

giac [C] time = 0.38, size = 3933, normalized size = 231.35

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

maple [B] time = 0.16, size = 682, normalized size = 40.12

$$\frac{e^{e^{c(bx+a)\ln(F)}\left(\tan^2\left(\frac{d}{2}+\frac{ex}{2}\right)\right)} - \frac{e^{e^{c(bx+a)\ln(F)}}}{e^{2+b^2c^2\ln(F)^2}} + \frac{2bc\ln(F)e^{e^{c(bx+a)\ln(F)}\tan\left(\frac{d}{2}+\frac{ex}{2}\right)}}{e^{2+b^2c^2\ln(F)^2}}}{1 + \tan^2\left(\frac{d}{2} + \frac{ex}{2}\right)} + \frac{e^{\left(\frac{(b^2c^2\ln(F)^2 - e^2)e^{c(bx+a)\ln(F)}\left(\tan^2\left(\frac{d}{2}+\frac{ex}{2}\right)\right)}\right)} + \frac{bc\ln(F)x e^{e^{c(bx+a)\ln(F)}}}{e^{2+b^2c^2\ln(F)^2}}}{(e^{2+b^2c^2\ln(F)^2})^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(F^(c*(b*x+a))*(e*x*cos(e*x+d)+(1+b*c*x*ln(F))*sin(e*x+d)), x)

[Out] (1/(e^2+b^2*c^2*ln(F)^2)*e*exp(c*(b*x+a)*ln(F))*tan(1/2*d+1/2*e*x)^2-1/(e^2+b^2*c^2*ln(F)^2)*e*exp(c*(b*x+a)*ln(F))+2*b*c*ln(F)/(e^2+b^2*c^2*ln(F)^2)*exp(c*(b*x+a)*ln(F))*tan(1/2*d+1/2*e*x))/(1+tan(1/2*d+1/2*e*x)^2)+e*((b^2*c^2*ln(F)^2-e^2)/(e^2+b^2*c^2*ln(F)^2)^2*exp(c*(b*x+a)*ln(F))*tan(1/2*d+1/2*e*x)^2+b*c*ln(F)/(e^2+b^2*c^2*ln(F)^2)*x*exp(c*(b*x+a)*ln(F))-(b^2*c^2*ln(F)^2-e^2)/(e^2+b^2*c^2*ln(F)^2)^2*exp(c*(b*x+a)*ln(F))+2/(e^2+b^2*c^2*ln(F)^2)*e*x*exp(c*(b*x+a)*ln(F))*tan(1/2*d+1/2*e*x)-4*b*c*ln(F)*e/(e^2+b^2*c^2*ln(F)^2)^2*exp(c*(b*x+a)*ln(F))*tan(1/2*d+1/2*e*x)-b*c*ln(F)/(e^2+b^2*c^2*ln(F)^2)*x*exp(c*(b*x+a)*ln(F))*tan(1/2*d+1/2*e*x)^2)/(1+tan(1/2*d+1/2*e*x)^2)+b*c*ln(F)*(1/(e^2+b^2*c^2*ln(F)^2)*e*x*exp(c*(b*x+a)*ln(F))*tan(1/2*d+1/2*e*x)^2-1/(e^2+b^2*c^2*ln(F)^2)*e*x*exp(c*(b*x+a)*ln(F))-2*(b^2*c^2*ln(F)^2-e^2)/(e^2+b^2*c^2*ln(F)^2)^2*exp(c*(b*x+a)*ln(F))*tan(1/2*d+1/2*e*x)+2*b*c*ln(F)*e/(e^2+b^2*c^2*ln(F)^2)^2*exp(c*(b*x+a)*ln(F))-2*b*c*ln(F)*e/(e^2+b^2*c^2*ln(F)^2)^2*exp(c*(b*x+a)*ln(F))*tan(1/2*d+1/2*e*x)^2+2*b*c*ln(F)/(e^2+b^2*c^2*ln(F)^2)*x*exp(c*(b*x+a)*ln(F))*tan(1/2*d+1/2*e*x))/(1+tan(1/2*d+1/2*e*x)^2)

maxima [B] time = 0.46, size = 1382, normalized size = 81.29

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(F^(c*(b*x+a))*(e*x*cos(e*x+d)+(1+b*c*x*log(F))*sin(e*x+d)), x, algorithm="maxima")

[Out] 1/2*((F^(a*c)*b^2*c^2*log(F)^2*sin(d) + 2*F^(a*c)*b*c*e*cos(d)*log(F) - F^(a*c)*e^2*sin(d) - (F^(a*c)*b^3*c^3*log(F)^3*sin(d) + F^(a*c)*b^2*c^2*e*cos(d)*log(F)^2 + F^(a*c)*b*c*e^2*log(F)*sin(d) + F^(a*c)*e^3*cos(d))*x)*F^(b*c*x)*cos(e*x + 2*d) - (F^(a*c)*b^2*c^2*log(F)^2*sin(d) - 2*F^(a*c)*b*c*e*cos(d)*log(F) - F^(a*c)*e^2*sin(d) - (F^(a*c)*b^3*c^3*log(F)^3*sin(d) - F^(a*c)*b^2*c^2*e*cos(d)*log(F)^2 + F^(a*c)*b*c*e^2*log(F)*sin(d) - F^(a*c)*e^3*cos(d))*x)*F^(b*c*x)*cos(e*x) - (F^(a*c)*b^2*c^2*cos(d)*log(F)^2 - 2*F^(a*c)*b*c*e*log(F)*sin(d) - F^(a*c)*e^2*cos(d) - (F^(a*c)*b^3*c^3*cos(d)*log(F)^3 - F^(a*c)*b^2*c^2*e*log(F)^2*sin(d) + F^(a*c)*b*c*e^2*cos(d)*log(F) - F^(a*c)*e^3*sin(d))*x)*F^(b*c*x)*sin(e*x + 2*d) - (F^(a*c)*b^2*c^2*cos(d)*log(F)^2 + 2*F^(a*c)*b*c*e*log(F)*sin(d) - F^(a*c)*e^2*cos(d) - (F^(a*c)*b^3*c^3*cos(d)*log(F)^3 + F^(a*c)*b^2*c^2*e*log(F)^2*sin(d) + F^(a*c)*b*c*e^2*cos(d)*log(F) + F^(a*c)*e^3*sin(d))*x)*F^(b*c*x)*sin(e*x))*b*c*log(F)/(b^4*c^4*cos(d)^2*log(F)^4 + b^4*c^4*log(F)^4*sin(d)^2 + (cos(d)^2 + sin(d)^2)*e^4 + 2*(b^2*c^2*cos(d)^2*log(F)^2 + b^2*c^2*log(F)^2*sin(d)^2)*e^2) - 1/2*((F^(a*c)*b^2*c^2*cos(d)*log(F)^2 - 2*F^(a*c)*b*c*e*log(F)*sin(d) - F^(a*c)*e^2*cos(d) - (F^(a*c)*b^3*c^3*cos(d)*log(F)^3 - F^(a*c)*b^2*c^2*e*log(F)^2*sin(d) + F^(a*c)*b*c*e^2*cos(d)*log(F) - F^(a*c)*e^3*sin(d))*x)*F^(b*c*x)*cos(e*x + 2*d) + (F^(a*c)*b^2*c^2*cos(d)*log(F)^2 + 2*F^(a*c)*b*c*e*log(F)*sin(d) - F^(a*c)*e^2*cos(d) - (F^(a*c)*b^3*c^3*cos(d)*log(F)^3 + F^(a*c)*b^2*c^2*e*log(F)^2*sin(d) + F^(a*c)*b*c*e^2*cos(d)*log(F) + F^(a*c)*e^3*sin(d))*x)*F^(b*c*x)*cos(e*x) + (F^(a*c)*b^2*c^2*log(F)^2*sin(d) + 2*F^(a*c)*b*c*e*cos(d)*log(F) - F^(a*c)*e^2*sin(d) - (F^(a*c)*b^3*c^3*log(F)^3*sin(d) + F^(a

```
*c)*b^2*c^2*e*cos(d)*log(F)^2 + F^(a*c)*b*c*e^2*log(F)*sin(d) + F^(a*c)*e^3
*cos(d))*x)*F^(b*c*x)*sin(e*x + 2*d) - (F^(a*c)*b^2*c^2*log(F)^2*sin(d) - 2
*F^(a*c)*b*c*e*cos(d)*log(F) - F^(a*c)*e^2*sin(d) - (F^(a*c)*b^3*c^3*log(F)
^3*sin(d) - F^(a*c)*b^2*c^2*e*cos(d)*log(F)^2 + F^(a*c)*b*c*e^2*log(F)*sin(
d) - F^(a*c)*e^3*cos(d))*x)*F^(b*c*x)*sin(e*x))*e/(b^4*c^4*cos(d)^2*log(F)^
4 + b^4*c^4*log(F)^4*sin(d)^2 + (cos(d)^2 + sin(d)^2)*e^4 + 2*(b^2*c^2*cos(
d)^2*log(F)^2 + b^2*c^2*log(F)^2*sin(d)^2)*e^2) - 1/2*((F^(a*c)*b*c*log(F)*
sin(d) + F^(a*c)*e*cos(d))*F^(b*c*x)*cos(e*x + 2*d) - (F^(a*c)*b*c*log(F)*s
in(d) - F^(a*c)*e*cos(d))*F^(b*c*x)*cos(e*x) - (F^(a*c)*b*c*cos(d)*log(F) -
F^(a*c)*e*sin(d))*F^(b*c*x)*sin(e*x + 2*d) - (F^(a*c)*b*c*cos(d)*log(F) +
F^(a*c)*e*sin(d))*F^(b*c*x)*sin(e*x))/(b^2*c^2*cos(d)^2*log(F)^2 + b^2*c^2*
log(F)^2*sin(d)^2 + (cos(d)^2 + sin(d)^2)*e^2)
```

mupad [B] time = 2.87, size = 17, normalized size = 1.00

$$F^{c(a+bx)} x \sin(d + ex)$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(F^(c*(a + b*x))*(sin(d + e*x)*(b*c*x*log(F) + 1) + e*x*cos(d + e*x)),x)
[Out] F^(c*(a + b*x))*x*sin(d + e*x)
```

sympy [A] time = 7.56, size = 19, normalized size = 1.12

$$F^{ac} F^{bcx} x \sin(d + ex)$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(F**(c*(b*x+a))*(e*x*cos(e*x+d)+(1+b*c*x*ln(F))*sin(e*x+d)),x)
[Out] F**(a*c)*F**(b*c*x))*x*sin(d + e*x)
```

3.35 $\int F^{c(a+bx)}(e \cos(d+ex) + bc \log(F) \sin(d+ex)) dx$

Optimal. Leaf size=16

$$\sin(d+ex)F^{c(a+bx)}$$

[Out] $F^{c(bx+a)} \sin(ex+d)$

Rubi [A] time = 0.03, antiderivative size = 16, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 30, $\frac{\text{number of rules}}{\text{integrand size}} = 0.033$, Rules used = {2288}

$$\sin(d+ex)F^{c(a+bx)}$$

Antiderivative was successfully verified.

[In] $\text{Int}[F^{c(a+bx)}(e \cos(d+ex) + bc \log[F] \sin(d+ex)), x]$

[Out] $F^{c(a+bx)} \sin(d+ex)$

Rule 2288

$\text{Int}[(y_.) \cdot (F_.)^{(u_)} \cdot ((v_)+ (w_)), x_Symbol] \rightarrow \text{With}[\{z = (v \cdot y) / (\log[F] \cdot D[u, x])\}, \text{Simp}[F^u \cdot z, x] /; \text{EqQ}[D[z, x], w \cdot y]] /; \text{FreeQ}[F, x]$

Rubi steps

$$\int F^{c(a+bx)}(e \cos(d+ex) + bc \log(F) \sin(d+ex)) dx = F^{c(a+bx)} \sin(d+ex)$$

Mathematica [A] time = 0.03, size = 16, normalized size = 1.00

$$\sin(d+ex)F^{c(a+bx)}$$

Antiderivative was successfully verified.

[In] $\text{Integrate}[F^{c(a+bx)}(e \cos(d+ex) + bc \log[F] \sin(d+ex)), x]$

[Out] $F^{c(a+bx)} \sin(d+ex)$

fricas [A] time = 0.79, size = 17, normalized size = 1.06

$$F^{bcx+ac} \sin(ex+d)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{integrate}(F^{c(bx+a)}(e \cos(ex+d) + b \cdot c \cdot \log(F) \sin(ex+d)), x, \text{algorithm} = \text{"fricas"})$

[Out] $F^{(b \cdot c \cdot x + a \cdot c)} \sin(ex+d)$

giac [C] time = 0.34, size = 1267, normalized size = 79.19

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{integrate}(F^{c(bx+a)}(e \cos(ex+d) + b \cdot c \cdot \log(F) \sin(ex+d)), x, \text{algorithm} = \text{"giac"})$

[Out] $(2 \cdot b \cdot c \cdot \cos(1/2 \cdot \pi \cdot b \cdot c \cdot x \cdot \text{sgn}(F)) - 1/2 \cdot \pi \cdot b \cdot c \cdot x + 1/2 \cdot \pi \cdot a \cdot c \cdot \text{sgn}(F) - 1/2 \cdot \pi \cdot a \cdot c + x \cdot e + d) \cdot \log(\text{abs}(F)) / (4 \cdot b^2 \cdot c^2 \cdot \log(\text{abs}(F))^2 + (\pi \cdot b \cdot c \cdot \text{sgn}(F) - \pi \cdot b$


```

*c + 2*e)^2) + (pi*b*c*sgn(F) - pi*b*c + 2*e)*sin(1/2*pi*b*c*x*sgn(F) - 1/2
*pi*b*c*x + 1/2*pi*a*c*sgn(F) - 1/2*pi*a*c + x*e + d)/(4*b^2*c^2*log(abs(F)
)^2 + (pi*b*c*sgn(F) - pi*b*c + 2*e)^2))*e^(b*c*x*log(abs(F)) + a*c*log(abs
(F)) + 1) + (2*b*c*cos(1/2*pi*b*c*x*sgn(F) - 1/2*pi*b*c*x + 1/2*pi*a*c*sgn(
F) - 1/2*pi*a*c - x*e - d)*log(abs(F))/(4*b^2*c^2*log(abs(F))^2 + (pi*b*c*s
gn(F) - pi*b*c - 2*e)^2) + (pi*b*c*sgn(F) - pi*b*c - 2*e)*sin(1/2*pi*b*c*x*
sgn(F) - 1/2*pi*b*c*x + 1/2*pi*a*c*sgn(F) - 1/2*pi*a*c - x*e - d)/(4*b^2*c^
2*log(abs(F))^2 + (pi*b*c*sgn(F) - pi*b*c - 2*e)^2))*e^(b*c*x*log(abs(F)) +
a*c*log(abs(F)) + 1) - 1/2*I*(-2*I*e^(1/2*I*pi*b*c*x*sgn(F) - 1/2*I*pi*b*c
*x + 1/2*I*pi*a*c*sgn(F) - 1/2*I*pi*a*c + I*x*e + I*d)/(2*I*pi*b*c*sgn(F) -
2*I*pi*b*c + 4*b*c*log(abs(F)) + 4*I*e) + 2*I*e^(-1/2*I*pi*b*c*x*sgn(F) +
1/2*I*pi*b*c*x - 1/2*I*pi*a*c*sgn(F) + 1/2*I*pi*a*c - I*x*e - I*d)/(-2*I*pi
*b*c*sgn(F) + 2*I*pi*b*c + 4*b*c*log(abs(F)) - 4*I*e))*e^(b*c*x*log(abs(F))
+ a*c*log(abs(F)) + 1) - 1/2*I*(-2*I*e^(1/2*I*pi*b*c*x*sgn(F) - 1/2*I*pi*b
*c*x + 1/2*I*pi*a*c*sgn(F) - 1/2*I*pi*a*c - I*x*e - I*d)/(2*I*pi*b*c*sgn(F)
- 2*I*pi*b*c + 4*b*c*log(abs(F)) - 4*I*e) + 2*I*e^(-1/2*I*pi*b*c*x*sgn(F)
+ 1/2*I*pi*b*c*x - 1/2*I*pi*a*c*sgn(F) + 1/2*I*pi*a*c + I*x*e + I*d)/(-2*I*
pi*b*c*sgn(F) + 2*I*pi*b*c + 4*b*c*log(abs(F)) + 4*I*e))*e^(b*c*x*log(abs(F)
)) + a*c*log(abs(F)) + 1) - I*(b*c*e^(1/2*I*pi*b*c*x*sgn(F) - 1/2*I*pi*b*c*
x + 1/2*I*pi*a*c*sgn(F) - 1/2*I*pi*a*c + I*x*e + I*d)*log(F)/(2*I*pi*b*c*sg
n(F) - 2*I*pi*b*c + 4*b*c*log(abs(F)) + 4*I*e) - b*c*e^(-1/2*I*pi*b*c*x*sgn
(F) + 1/2*I*pi*b*c*x - 1/2*I*pi*a*c*sgn(F) + 1/2*I*pi*a*c - I*x*e - I*d)*lo
g(F)/(-2*I*pi*b*c*sgn(F) + 2*I*pi*b*c + 4*b*c*log(abs(F)) - 4*I*e))*e^(b*c*
x*log(abs(F)) + a*c*log(abs(F))) + 1/2*(2*I*b*c*e^(1/2*I*pi*b*c*x*sgn(F) -
1/2*I*pi*b*c*x + 1/2*I*pi*a*c*sgn(F) - 1/2*I*pi*a*c + I*x*e + I*d)*log(F)/(
2*I*pi*b*c*sgn(F) - 2*I*pi*b*c + 4*b*c*log(abs(F)) + 4*I*e) + 2*I*b*c*e^(-1
/2*I*pi*b*c*x*sgn(F) + 1/2*I*pi*b*c*x - 1/2*I*pi*a*c*sgn(F) + 1/2*I*pi*a*c
- I*x*e - I*d)*log(F)/(-2*I*pi*b*c*sgn(F) + 2*I*pi*b*c + 4*b*c*log(abs(F))
- 4*I*e))*e^(b*c*x*log(abs(F)) + a*c*log(abs(F))) + I*(b*c*e^(1/2*I*pi*b*c*
x*sgn(F) - 1/2*I*pi*b*c*x + 1/2*I*pi*a*c*sgn(F) - 1/2*I*pi*a*c - I*x*e - I*
d)*log(F)/(2*I*pi*b*c*sgn(F) - 2*I*pi*b*c + 4*b*c*log(abs(F)) - 4*I*e) - b*
c*e^(-1/2*I*pi*b*c*x*sgn(F) + 1/2*I*pi*b*c*x - 1/2*I*pi*a*c*sgn(F) + 1/2*I*
pi*a*c + I*x*e + I*d)*log(F)/(-2*I*pi*b*c*sgn(F) + 2*I*pi*b*c + 4*b*c*log(a
bs(F)) + 4*I*e))*e^(b*c*x*log(abs(F)) + a*c*log(abs(F))) + 1/2*(-2*I*b*c*e^
(1/2*I*pi*b*c*x*sgn(F) - 1/2*I*pi*b*c*x + 1/2*I*pi*a*c*sgn(F) - 1/2*I*pi*a*
c - I*x*e - I*d)*log(F)/(2*I*pi*b*c*sgn(F) - 2*I*pi*b*c + 4*b*c*log(abs(F))
- 4*I*e) - 2*I*b*c*e^(-1/2*I*pi*b*c*x*sgn(F) + 1/2*I*pi*b*c*x - 1/2*I*pi*a
*c*sgn(F) + 1/2*I*pi*a*c + I*x*e + I*d)*log(F)/(-2*I*pi*b*c*sgn(F) + 2*I*pi
*b*c + 4*b*c*log(abs(F)) + 4*I*e))*e^(b*c*x*log(abs(F)) + a*c*log(abs(F)))

```

maple [B] time = 0.04, size = 268, normalized size = 16.75

$$e^{\left(\frac{bc \ln(F) e^{c(bx+a) \ln(F)}}{e^2 + b^2 c^2 \ln(F)^2} + \frac{2e e^{c(bx+a) \ln(F)} \tan\left(\frac{d}{2} + \frac{ex}{2}\right)}{e^2 + b^2 c^2 \ln(F)^2} - \frac{bc \ln(F) e^{c(bx+a) \ln(F)} \left(\tan^2\left(\frac{d}{2} + \frac{ex}{2}\right)\right)}{e^2 + b^2 c^2 \ln(F)^2} \right)} + \frac{bc \ln(F) \left(\frac{e e^{c(bx+a) \ln(F)} \left(\tan^2\left(\frac{d}{2} + \frac{ex}{2}\right)\right)}{e^2 + b^2 c^2 \ln(F)^2} - \frac{e e^{c(bx+a) \ln(F)}}{e^2 + b^2 c^2 \ln(F)^2} \right)}{1 + \tan^2\left(\frac{d}{2} + \frac{ex}{2}\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(F^(c*(b*x+a))*(e*cos(e*x+d)+b*c*ln(F)*sin(e*x+d)),x)

[Out] e*(b*c*ln(F)/(e^2+b^2*c^2*ln(F)^2)*exp(c*(b*x+a)*ln(F))+2/(e^2+b^2*c^2*ln(F)^2)*e*exp(c*(b*x+a)*ln(F))*tan(1/2*d+1/2*e*x)-b*c*ln(F)/(e^2+b^2*c^2*ln(F)^2)*exp(c*(b*x+a)*ln(F))*tan(1/2*d+1/2*e*x)^2/(1+tan(1/2*d+1/2*e*x)^2)+b*c*ln(F)*(1/(e^2+b^2*c^2*ln(F)^2)*e*exp(c*(b*x+a)*ln(F))*tan(1/2*d+1/2*e*x)^2-1/(e^2+b^2*c^2*ln(F)^2)*e*exp(c*(b*x+a)*ln(F))+2*b*c*ln(F)/(e^2+b^2*c^2*ln(F)^2)*exp(c*(b*x+a)*ln(F))*tan(1/2*d+1/2*e*x))/(1+tan(1/2*d+1/2*e*x)^2)

$$3.36 \quad \int \frac{F^{c(a+bx)}(ex \cos(d+ex) + (-1+bcx \log(F)) \sin(d+ex))}{x^2} dx$$

Optimal. Leaf size=20

$$\frac{\sin(d+ex)F^{ac+bcx}}{x}$$

[Out] $F^{(b*c*x+a*c)*\sin(e*x+d)}/x$

Rubi [A] time = 1.73, antiderivative size = 20, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 3, integrand size = 38, $\frac{\text{number of rules}}{\text{integrand size}} = 0.079$, Rules used = {6741, 6742, 4467}

$$\frac{\sin(d+ex)F^{ac+bcx}}{x}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(F^{(c*(a+b*x))}*(e*x*\text{Cos}[d+e*x] + (-1+b*c*x*\text{Log}[F]))*\text{Sin}[d+e*x])]/x^2, x]$

[Out] $(F^{(a*c+b*c*x)*\text{Sin}[d+e*x]})/x$

Rule 4467

$\text{Int}[(F_)^{((c_.)*((a_.)+(b_.)*(x_)))}*((f_.)*(x_))^{(m_)}*\text{Sin}[(d_.)+(e_.)*(x_)]], x_Symbol] := \text{Simp}[(f*x)^{(m+1)}*F^{(c*(a+b*x))*\text{Sin}[d+e*x]}/(f*(m+1)), x] + (-\text{Dist}[e/(f*(m+1)), \text{Int}[(f*x)^{(m+1)}*F^{(c*(a+b*x))*\text{Cos}[d+e*x]}, x], x] - \text{Dist}[(b*c*\text{Log}[F])/(f*(m+1)), \text{Int}[(f*x)^{(m+1)}*F^{(c*(a+b*x))*\text{Sin}[d+e*x]}, x], x]) /; \text{FreeQ}\{F, a, b, c, d, e, f, m\}, x] \&\& (\text{LtQ}[m, -1] || \text{SumSimplerQ}[m, 1])$

Rule 6741

$\text{Int}[u_, x_Symbol] := \text{With}\{v = \text{NormalizeIntegrand}[u, x]\}, \text{Int}[v, x] /; v \neq u]$

Rule 6742

$\text{Int}[u_, x_Symbol] := \text{With}\{v = \text{ExpandIntegrand}[u, x]\}, \text{Int}[v, x] /; \text{SumQ}[v]$

Rubi steps

$$\begin{aligned} \int \frac{F^{c(a+bx)}(ex \cos(d+ex) + (-1+bcx \log(F)) \sin(d+ex))}{x^2} dx &= \int \frac{F^{ac+bcx}(ex \cos(d+ex) + (-1+bcx \log(F)))}{x^2} dx \\ &= \int \left(\frac{eF^{ac+bcx} \cos(d+ex)}{x} + \frac{F^{ac+bcx}(-1+bcx \log(F))}{x^2} \right) dx \\ &= e \int \frac{F^{ac+bcx} \cos(d+ex)}{x} dx + \int \frac{F^{ac+bcx}(-1+bcx \log(F))}{x^2} dx \\ &= e \int \frac{F^{ac+bcx} \cos(d+ex)}{x} dx + \int \left(-\frac{F^{ac+bcx} \sin(d+ex)}{x^2} \right) dx \\ &= e \int \frac{F^{ac+bcx} \cos(d+ex)}{x} dx + (bc \log(F)) \int \frac{F^{ac+bcx}}{x} dx \\ &= \frac{F^{ac+bcx} \sin(d+ex)}{x} \end{aligned}$$

Mathematica [A] time = 0.61, size = 19, normalized size = 0.95

$$\frac{\sin(d + ex)F^{c(a+bx)}}{x}$$

Antiderivative was successfully verified.

[In] Integrate[(F^(c*(a + b*x))*(e*x*Cos[d + e*x] + (-1 + b*c*x*Log[F])*Sin[d + e*x]))/x^2,x]

[Out] (F^(c*(a + b*x))*Sin[d + e*x])/x

fricas [A] time = 0.94, size = 20, normalized size = 1.00

$$\frac{F^{bcx+ac} \sin(ex + d)}{x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(F^(c*(b*x+a))*(e*x*cos(e*x+d)+(-1+b*c*x*log(F))*sin(e*x+d))/x^2,x, algorithm="fricas")

[Out] F^(b*c*x + a*c)*sin(e*x + d)/x

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(ex \cos(ex + d) + (bcx \log(F) - 1) \sin(ex + d))F^{(bx+a)c}}{x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(F^(c*(b*x+a))*(e*x*cos(e*x+d)+(-1+b*c*x*log(F))*sin(e*x+d))/x^2,x, algorithm="giac")

[Out] integrate((e*x*cos(e*x + d) + (b*c*x*log(F) - 1)*sin(e*x + d))*F^((b*x + a)*c)/x^2, x)

maple [A] time = 0.13, size = 40, normalized size = 2.00

$$\frac{2 e^{c(bx+a) \ln(F)} \tan\left(\frac{d}{2} + \frac{ex}{2}\right)}{\left(1 + \tan^2\left(\frac{d}{2} + \frac{ex}{2}\right)\right) x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(F^(c*(b*x+a))*(e*x*cos(e*x+d)+(-1+b*c*x*ln(F))*sin(e*x+d))/x^2,x)

[Out] 2*exp(c*(b*x+a)*ln(F))*tan(1/2*d+1/2*e*x)/(1+tan(1/2*d+1/2*e*x)^2)/x

maxima [C] time = 1.03, size = 564, normalized size = 28.20

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(F^(c*(b*x+a))*(e*x*cos(e*x+d)+(-1+b*c*x*log(F))*sin(e*x+d))/x^2,x, algorithm="maxima")

[Out] -1/4*F^(a*c)*b*c*(I*conjugate(gamma(-1, -(b*c*log(F) + I*e)*x)) - I*conjugate(gamma(-1, -(b*c*log(F) - I*e)*x)) - I*gamma(-1, -(b*c*log(F) + I*e)*x) + I*gamma(-1, -(b*c*log(F) - I*e)*x))*cos(d)*log(F) - 1/4*F^(a*c)*b*c*(conjugate(gamma(-1, -(b*c*log(F) + I*e)*x)) + conjugate(gamma(-1, -(b*c*log(F) - I*e)*x)) + gamma(-1, -(b*c*log(F) + I*e)*x) + gamma(-1, -(b*c*log(F) - I*e)*x))

```

)*x))*log(F)*sin(d) - 1/4*(F^(a*c)*(I*Ei((b*c*log(F) + I*e)*x) - I*Ei((b*c*
log(F) - I*e)*x) - I*conjugate(Ei((b*c*log(F) + I*e)*x)) + I*conjugate(Ei((
b*c*log(F) - I*e)*x)))*cos(d) - F^(a*c)*(Ei((b*c*log(F) + I*e)*x) + Ei((b*c
*log(F) - I*e)*x) + conjugate(Ei((b*c*log(F) + I*e)*x)) + conjugate(Ei((b*c
*log(F) - I*e)*x)))*sin(d))*b*c*log(F) + 1/4*(F^(a*c)*(Ei((b*c*log(F) + I*e
)*x) + Ei((b*c*log(F) - I*e)*x) + conjugate(Ei((b*c*log(F) + I*e)*x)) + con
jugate(Ei((b*c*log(F) - I*e)*x)))*cos(d) - F^(a*c)*(-I*Ei((b*c*log(F) + I*e
)*x) + I*Ei((b*c*log(F) - I*e)*x) + I*conjugate(Ei((b*c*log(F) + I*e)*x)) -
I*conjugate(Ei((b*c*log(F) - I*e)*x)))*sin(d))*e - 1/4*(F^(a*c)*(conjugate
(gamma(-1, -(b*c*log(F) + I*e)*x)) + conjugate(gamma(-1, -(b*c*log(F) - I*e
)*x)) + gamma(-1, -(b*c*log(F) + I*e)*x) + gamma(-1, -(b*c*log(F) - I*e)*x)
)*cos(d) + F^(a*c)*(-I*conjugate(gamma(-1, -(b*c*log(F) + I*e)*x)) + I*conj
ugate(gamma(-1, -(b*c*log(F) - I*e)*x)) + I*gamma(-1, -(b*c*log(F) + I*e)*x
) - I*gamma(-1, -(b*c*log(F) - I*e)*x))*sin(d))*e

```

mupad [B] time = 2.74, size = 19, normalized size = 0.95

$$\frac{F^{c(a+bx)} \sin(d+ex)}{x}$$

Verification of antiderivative is not currently implemented for this CAS.

```

[In] int((F^(c*(a + b*x))*(sin(d + e*x)*(b*c*x*log(F) - 1) + e*x*cos(d + e*x)))/
x^2,x)

```

```

[Out] (F^(c*(a + b*x))*sin(d + e*x))/x

```

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{F^{c(a+bx)} (bcx \log(F) \sin(d+ex) + ex \cos(d+ex) - \sin(d+ex))}{x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```

[In] integrate(F**(c*(b*x+a))*(e*x*cos(e*x+d)+(-1+b*c*x*ln(F))*sin(e*x+d))/x**2,
x)

```

```

[Out] Integral(F**(c*(a + b*x))*(b*c*x*log(F)*sin(d + e*x) + e*x*cos(d + e*x) - s
in(d + e*x))/x**2, x)

```

$$3.37 \quad \int \frac{F^{c(a+bx)}(ex \cos(d+ex) + (-2+bcx \log(F)) \sin(d+ex))}{x^3} dx$$

Optimal. Leaf size=20

$$\frac{\sin(d+ex)F^{ac+bcx}}{x^2}$$

[Out] $F^{(b*c*x+a*c)*\sin(e*x+d)/x^2$

Rubi [A] time = 1.95, antiderivative size = 20, normalized size of antiderivative = 1.00, number of steps used = 10, number of rules used = 4, integrand size = 38, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {6741, 6742, 4468, 4467}

$$\frac{\sin(d+ex)F^{ac+bcx}}{x^2}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(F^{(c*(a+b*x))}*(e*x*\text{Cos}[d+e*x] + (-2+b*c*x*\text{Log}[F])* \text{Sin}[d+e*x]))/x^3, x]$

[Out] $(F^{(a*c+b*c*x)*\text{Sin}[d+e*x]})/x^2$

Rule 4467

$\text{Int}[(F_)^{((c_.)*((a_.)+(b_.)*(x_)))*((f_.)*(x_))^{(m_)*\text{Sin}[d_.+(e_.)*(x_)]}, x_Symbol] \rightarrow \text{Simp}[(f*x)^{(m+1)}*F^{(c*(a+b*x))*\text{Sin}[d+e*x]}/(f*(m+1)), x] + (-\text{Dist}[e/(f*(m+1)), \text{Int}[(f*x)^{(m+1)}*F^{(c*(a+b*x))*\text{Cos}[d+e*x]}, x], x] - \text{Dist}[(b*c*\text{Log}[F])/(f*(m+1)), \text{Int}[(f*x)^{(m+1)}*F^{(c*(a+b*x))*\text{Sin}[d+e*x]}, x], x]) /; \text{FreeQ}\{F, a, b, c, d, e, f, m\}, x\} \&\& (\text{LtQ}[m, -1] \|\ \text{SumSimplerQ}[m, 1])$

Rule 4468

$\text{Int}[\text{Cos}[(d_.)+(e_.)*(x_)]*(F_)^{((c_.)*((a_.)+(b_.)*(x_)))*((f_.)*(x_))^{(m_)}], x_Symbol] \rightarrow \text{Simp}[(f*x)^{(m+1)}*F^{(c*(a+b*x))*\text{Cos}[d+e*x]}/(f*(m+1)), x] + (\text{Dist}[e/(f*(m+1)), \text{Int}[(f*x)^{(m+1)}*F^{(c*(a+b*x))*\text{Sin}[d+e*x]}, x], x] - \text{Dist}[(b*c*\text{Log}[F])/(f*(m+1)), \text{Int}[(f*x)^{(m+1)}*F^{(c*(a+b*x))*\text{Cos}[d+e*x]}, x], x]) /; \text{FreeQ}\{F, a, b, c, d, e, f, m\}, x\} \&\& (\text{LtQ}[m, -1] \|\ \text{SumSimplerQ}[m, 1])$

Rule 6741

$\text{Int}[u_, x_Symbol] \rightarrow \text{With}\{v = \text{NormalizeIntegrand}[u, x]\}, \text{Int}[v, x] /; v \neq u]$

Rule 6742

$\text{Int}[u_, x_Symbol] \rightarrow \text{With}\{v = \text{ExpandIntegrand}[u, x]\}, \text{Int}[v, x] /; \text{SumQ}[v]$

Rubi steps

$$\begin{aligned}
\int \frac{F^{c(a+bx)}(ex \cos(d+ex) + (-2 + bcx \log(F)) \sin(d+ex))}{x^3} dx &= \int \frac{F^{ac+bcx}(ex \cos(d+ex) + (-2 + bcx \log(F)))}{x^3} \\
&= \int \left(\frac{eF^{ac+bcx} \cos(d+ex)}{x^2} + \frac{F^{ac+bcx}(-2 + bcx \log(F))}{x^3} \right) dx \\
&= e \int \frac{F^{ac+bcx} \cos(d+ex)}{x^2} dx + \int \frac{F^{ac+bcx}(-2 + bcx \log(F))}{x^3} dx \\
&= -\frac{eF^{ac+bcx} \cos(d+ex)}{x} - e^2 \int \frac{F^{ac+bcx} \sin(d+ex)}{x} dx \\
&= -\frac{eF^{ac+bcx} \cos(d+ex)}{x} - 2 \int \frac{F^{ac+bcx} \sin(d+ex)}{x^3} dx \\
&= -\frac{eF^{ac+bcx} \cos(d+ex)}{x} + \frac{F^{ac+bcx} \sin(d+ex)}{x^2} \\
&= \frac{F^{ac+bcx} \sin(d+ex)}{x^2}
\end{aligned}$$

Mathematica [A] time = 0.65, size = 19, normalized size = 0.95

$$\frac{\sin(d+ex)F^{c(a+bx)}}{x^2}$$

Antiderivative was successfully verified.

[In] Integrate[(F^(c*(a + b*x))*(e*x*Cos[d + e*x] + (-2 + b*c*x*Log[F]))*Sin[d + e*x])/x^3, x]

[Out] (F^(c*(a + b*x))*Sin[d + e*x])/x^2

fricas [A] time = 0.58, size = 20, normalized size = 1.00

$$\frac{F^{bcx+ac} \sin(ex+d)}{x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(F^(c*(b*x+a))*(e*x*cos(e*x+d)+(-2+b*c*x*log(F))*sin(e*x+d))/x^3, x, algorithm="fricas")

[Out] F^(b*c*x + a*c)*sin(e*x + d)/x^2

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(ex \cos(ex+d) + (bcx \log(F) - 2) \sin(ex+d))F^{(bx+a)c}}{x^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(F^(c*(b*x+a))*(e*x*cos(e*x+d)+(-2+b*c*x*log(F))*sin(e*x+d))/x^3, x, algorithm="giac")

[Out] integrate((e*x*cos(e*x + d) + (b*c*x*log(F) - 2)*sin(e*x + d))*F^((b*x + a)*c)/x^3, x)

maple [A] time = 0.16, size = 40, normalized size = 2.00

$$\frac{2e^{c(bx+a)\ln(F)} \tan\left(\frac{d}{2} + \frac{ex}{2}\right)}{\left(1 + \tan^2\left(\frac{d}{2} + \frac{ex}{2}\right)\right)x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(F^(c*(b*x+a))*(e*x*cos(e*x+d)+(-2+b*c*x*ln(F))*sin(e*x+d))/x^3,x)
[Out] 2*exp(c*(b*x+a)*ln(F))*tan(1/2*d+1/2*e*x)/(1+tan(1/2*d+1/2*e*x)^2)/x^2
maxima [C] time = 1.44, size = 1072, normalized size = 53.60
```

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(F^(c*(b*x+a))*(e*x*cos(e*x+d)+(-2+b*c*x*log(F))*sin(e*x+d))/x^3,x
, algorithm="maxima")
```

```
[Out] -1/2*F^(a*c)*b^2*c^2*(-I*conjugate(gamma(-2, -(b*c*log(F) + I*e)*x)) + I*co
njugate(gamma(-2, -(b*c*log(F) - I*e)*x)) + I*gamma(-2, -(b*c*log(F) + I*e)
*x) - I*gamma(-2, -(b*c*log(F) - I*e)*x))*cos(d)*log(F)^2 + 1/2*F^(a*c)*b^2
*c^2*(conjugate(gamma(-2, -(b*c*log(F) + I*e)*x)) + conjugate(gamma(-2, -(b
*c*log(F) - I*e)*x)) + gamma(-2, -(b*c*log(F) + I*e)*x) + gamma(-2, -(b*c*1
og(F) - I*e)*x))*log(F)^2*sin(d) + 1/4*(F^(a*c)*b*c*(I*conjugate(gamma(-1,
-(b*c*log(F) + I*e)*x)) - I*conjugate(gamma(-1, -(b*c*log(F) - I*e)*x)) - I
*gamma(-1, -(b*c*log(F) + I*e)*x) + I*gamma(-1, -(b*c*log(F) - I*e)*x))*cos
(d)*log(F) + F^(a*c)*b*c*(conjugate(gamma(-1, -(b*c*log(F) + I*e)*x)) + con
jugate(gamma(-1, -(b*c*log(F) - I*e)*x)) + gamma(-1, -(b*c*log(F) + I*e)*x)
+ gamma(-1, -(b*c*log(F) - I*e)*x))*log(F)*sin(d) + (F^(a*c)*(conjugate(ga
mma(-1, -(b*c*log(F) + I*e)*x)) + conjugate(gamma(-1, -(b*c*log(F) - I*e)*x
)) + gamma(-1, -(b*c*log(F) + I*e)*x) + gamma(-1, -(b*c*log(F) - I*e)*x))*c
os(d) + F^(a*c)*(-I*conjugate(gamma(-1, -(b*c*log(F) + I*e)*x)) + I*conjugat
e(gamma(-1, -(b*c*log(F) - I*e)*x)) + I*gamma(-1, -(b*c*log(F) + I*e)*x) -
I*gamma(-1, -(b*c*log(F) - I*e)*x))*sin(d))*e)*b*c*log(F) - 1/2*(F^(a*c)*(
I*conjugate(gamma(-2, -(b*c*log(F) + I*e)*x)) - I*conjugate(gamma(-2, -(b*c
*log(F) - I*e)*x)) - I*gamma(-2, -(b*c*log(F) + I*e)*x) + I*gamma(-2, -(b*c
*log(F) - I*e)*x))*cos(d) + F^(a*c)*(conjugate(gamma(-2, -(b*c*log(F) + I*
e)*x)) + conjugate(gamma(-2, -(b*c*log(F) - I*e)*x)) + gamma(-2, -(b*c*log(F
) + I*e)*x) + gamma(-2, -(b*c*log(F) - I*e)*x))*sin(d))*e^2 + 1/4*(F^(a*c)*
b*c*(conjugate(gamma(-1, -(b*c*log(F) + I*e)*x)) + conjugate(gamma(-1, -(b*
c*log(F) - I*e)*x)) + gamma(-1, -(b*c*log(F) + I*e)*x) + gamma(-1, -(b*c*lo
g(F) - I*e)*x))*cos(d)*log(F) - F^(a*c)*b*c*(I*conjugate(gamma(-1, -(b*c*lo
g(F) + I*e)*x)) - I*conjugate(gamma(-1, -(b*c*log(F) - I*e)*x)) - I*gamma(-
1, -(b*c*log(F) + I*e)*x) + I*gamma(-1, -(b*c*log(F) - I*e)*x))*log(F)*sin(
d) - (F^(a*c)*(I*conjugate(gamma(-1, -(b*c*log(F) + I*e)*x)) - I*conjugate(
gamma(-1, -(b*c*log(F) - I*e)*x)) - I*gamma(-1, -(b*c*log(F) + I*e)*x) + I*
gamma(-1, -(b*c*log(F) - I*e)*x))*cos(d) + F^(a*c)*(conjugate(gamma(-1, -(b
*c*log(F) + I*e)*x)) + conjugate(gamma(-1, -(b*c*log(F) - I*e)*x)) + gamma(
-1, -(b*c*log(F) + I*e)*x) + gamma(-1, -(b*c*log(F) - I*e)*x))*sin(d))*e)*e
+ 1/2*(2*F^(a*c)*b*c*(conjugate(gamma(-2, -(b*c*log(F) + I*e)*x)) + conjug
ate(gamma(-2, -(b*c*log(F) - I*e)*x)) + gamma(-2, -(b*c*log(F) + I*e)*x) +
gamma(-2, -(b*c*log(F) - I*e)*x))*cos(d)*log(F) - F^(a*c)*b*c*(2*I*conjugat
e(gamma(-2, -(b*c*log(F) + I*e)*x)) - 2*I*conjugate(gamma(-2, -(b*c*log(F)
- I*e)*x)) - 2*I*gamma(-2, -(b*c*log(F) + I*e)*x) + 2*I*gamma(-2, -(b*c*log
(F) - I*e)*x))*log(F)*sin(d))*e
```

```
mupad [B] time = 2.75, size = 19, normalized size = 0.95
```

$$\frac{F^{c(a+bx)} \sin(d+ex)}{x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((F^(c*(a + b*x))*(sin(d + e*x)*(b*c*x*log(F) - 2) + e*x*cos(d + e*x)))/
x^3,x)
```


[Out] $(F^{c(a+bx)} \sin(d+ex))/x^2$

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{F^{c(a+bx)} (bcx \log(F) \sin(d+ex) + ex \cos(d+ex) - 2 \sin(d+ex))}{x^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(F**(c*(b*x+a))*(e*x*cos(e*x+d)+(-2+b*c*x*ln(F))*sin(e*x+d))/x**3, x)

[Out] Integral(F**(c*(a + b*x))*(b*c*x*log(F)*sin(d + e*x) + e*x*cos(d + e*x) - 2 *sin(d + e*x))/x**3, x)

3.38 $\int e^{a+bx} \cos(c + dx) \sin(c + dx) dx$

Optimal. Leaf size=63

$$\frac{be^{a+bx} \sin(2c + 2dx)}{2(b^2 + 4d^2)} - \frac{de^{a+bx} \cos(2c + 2dx)}{b^2 + 4d^2}$$

[Out] $-d*\exp(b*x+a)*\cos(2*d*x+2*c)/(b^2+4*d^2)+1/2*b*\exp(b*x+a)*\sin(2*d*x+2*c)/(b^2+4*d^2)$

Rubi [A] time = 0.05, antiderivative size = 63, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 3, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.150$, Rules used = {4469, 12, 4432}

$$\frac{be^{a+bx} \sin(2c + 2dx)}{2(b^2 + 4d^2)} - \frac{de^{a+bx} \cos(2c + 2dx)}{b^2 + 4d^2}$$

Antiderivative was successfully verified.

[In] Int[E^(a + b*x)*Cos[c + d*x]*Sin[c + d*x], x]

[Out] $-((d*E^{(a + b*x)*\cos[2*c + 2*d*x]})/(b^2 + 4*d^2)) + (b*E^{(a + b*x)*\sin[2*c + 2*d*x]})/(2*(b^2 + 4*d^2))$

Rule 12

Int[(a_)*(u_), x_Symbol] := Dist[a, Int[u, x], x] /; FreeQ[a, x] && !MatchQ[u, (b_)*(v_)] /; FreeQ[b, x]

Rule 4432

Int[(F_)^((c_.)*((a_.) + (b_.)*(x_)))*Sin[(d_.) + (e_.)*(x_)], x_Symbol] := Simp[(b*c*Log[F]*F^(c*(a + b*x))*Sin[d + e*x])/(e^2 + b^2*c^2*Log[F]^2), x] - Simp[(e*F^(c*(a + b*x))*Cos[d + e*x])/(e^2 + b^2*c^2*Log[F]^2), x] /; FreeQ[{F, a, b, c, d, e}, x] && NeQ[e^2 + b^2*c^2*Log[F]^2, 0]

Rule 4469

Int[Cos[(f_.) + (g_.)*(x_)]^(n_.)*(F_)^((c_.)*((a_.) + (b_.)*(x_)))*Sin[(d_.) + (e_.)*(x_)]^(m_.), x_Symbol] := Int[ExpandTrigReduce[F^(c*(a + b*x)), Sin[d + e*x]^m*Cos[f + g*x]^n, x], x] /; FreeQ[{F, a, b, c, d, e, f, g}, x] && IGtQ[m, 0] && IGtQ[n, 0]

Rubi steps

$$\begin{aligned} \int e^{a+bx} \cos(c + dx) \sin(c + dx) dx &= \int \frac{1}{2} e^{a+bx} \sin(2c + 2dx) dx \\ &= \frac{1}{2} \int e^{a+bx} \sin(2c + 2dx) dx \\ &= -\frac{de^{a+bx} \cos(2c + 2dx)}{b^2 + 4d^2} + \frac{be^{a+bx} \sin(2c + 2dx)}{2(b^2 + 4d^2)} \end{aligned}$$

Mathematica [A] time = 0.15, size = 44, normalized size = 0.70

$$\frac{e^{a+bx}(b \sin(2(c + dx)) - 2d \cos(2(c + dx)))}{2(b^2 + 4d^2)}$$

Antiderivative was successfully verified.

[In] Integrate[E^(a + b*x)*Cos[c + d*x]*Sin[c + d*x],x]

[Out] (E^(a + b*x)*(-2*d*Cos[2*(c + d*x)] + b*Ssin[2*(c + d*x)]))/(2*(b^2 + 4*d^2))

fricas [A] time = 0.61, size = 56, normalized size = 0.89

$$\frac{b \cos(dx + c) e^{(bx+a)} \sin(dx + c) - (2d \cos(dx + c)^2 - d) e^{(bx+a)}}{b^2 + 4d^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(b*x+a)*cos(d*x+c)*sin(d*x+c),x, algorithm="fricas")

[Out] (b*cos(d*x + c)*e^(b*x + a)*sin(d*x + c) - (2*d*cos(d*x + c)^2 - d)*e^(b*x + a))/(b^2 + 4*d^2)

giac [A] time = 0.13, size = 55, normalized size = 0.87

$$-\frac{1}{2} \left(\frac{2d \cos(2dx + 2c)}{b^2 + 4d^2} - \frac{b \sin(2dx + 2c)}{b^2 + 4d^2} \right) e^{(bx+a)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(b*x+a)*cos(d*x+c)*sin(d*x+c),x, algorithm="giac")

[Out] -1/2*(2*d*cos(2*d*x + 2*c)/(b^2 + 4*d^2) - b*sin(2*d*x + 2*c)/(b^2 + 4*d^2))*e^(b*x + a)

maple [A] time = 0.06, size = 60, normalized size = 0.95

$$-\frac{d e^{bx+a} \cos(2dx + 2c)}{b^2 + 4d^2} + \frac{b e^{bx+a} \sin(2dx + 2c)}{2b^2 + 8d^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(exp(b*x+a)*cos(d*x+c)*sin(d*x+c),x)

[Out] -d*exp(b*x+a)*cos(2*d*x+2*c)/(b^2+4*d^2)+1/2*b*exp(b*x+a)*sin(2*d*x+2*c)/(b^2+4*d^2)

maxima [A] time = 0.32, size = 44, normalized size = 0.70

$$\frac{(2d \cos(2dx + 2c) - b \sin(2dx + 2c)) e^{(bx+a)}}{2(b^2 + 4d^2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(b*x+a)*cos(d*x+c)*sin(d*x+c),x, algorithm="maxima")

[Out] -1/2*(2*d*cos(2*d*x + 2*c) - b*sin(2*d*x + 2*c))*e^(b*x + a)/(b^2 + 4*d^2)

mupad [B] time = 0.50, size = 46, normalized size = 0.73

$$-\frac{e^{a+bx} (2d \cos(2c + 2dx) - b \sin(2c + 2dx))}{2(b^2 + 4d^2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(cos(c + d*x)*exp(a + b*x)*sin(c + d*x),x)

[Out] $-(\exp(a + b*x)*(2*d*\cos(2*c + 2*d*x) - b*\sin(2*c + 2*d*x)))/(2*(b^2 + 4*d^2))$

sympy [A] time = 8.52, size = 325, normalized size = 5.16

$$\left\{ \begin{array}{ll} x e^a \sin(c) \cos(c) & \text{for } b = 0 \wedge d = 0 \\ \frac{i x e^a e^{-2idx} \sin^2(c+dx)}{4} + \frac{x e^a e^{-2idx} \sin(c+dx) \cos(c+dx)}{2} - \frac{i x e^a e^{-2idx} \cos^2(c+dx)}{4} + \frac{i e^a e^{-2idx} \sin(c+dx) \cos(c+dx)}{4d} & \text{for } b = -2id \\ -\frac{i x e^a e^{2idx} \sin^2(c+dx)}{4} + \frac{x e^a e^{2idx} \sin(c+dx) \cos(c+dx)}{2} + \frac{i x e^a e^{2idx} \cos^2(c+dx)}{4} - \frac{i e^a e^{2idx} \sin(c+dx) \cos(c+dx)}{4d} & \text{for } b = 2id \\ \frac{b e^a e^{bx} \sin(c+dx) \cos(c+dx)}{b^2+4d^2} + \frac{d e^a e^{bx} \sin^2(c+dx)}{b^2+4d^2} - \frac{d e^a e^{bx} \cos^2(c+dx)}{b^2+4d^2} & \text{otherwise} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(exp(b*x+a)*cos(d*x+c)*sin(d*x+c),x)`

[Out] `Piecewise((x*exp(a)*sin(c)*cos(c), Eq(b, 0) & Eq(d, 0)), (I*x*exp(a)*exp(-2*I*d*x)*sin(c + d*x)**2/4 + x*exp(a)*exp(-2*I*d*x)*sin(c + d*x)*cos(c + d*x)/2 - I*x*exp(a)*exp(-2*I*d*x)*cos(c + d*x)**2/4 + I*exp(a)*exp(-2*I*d*x)*sin(c + d*x)*cos(c + d*x)/(4*d), Eq(b, -2*I*d)), (-I*x*exp(a)*exp(2*I*d*x)*sin(c + d*x)**2/4 + x*exp(a)*exp(2*I*d*x)*sin(c + d*x)*cos(c + d*x)/2 + I*x*exp(a)*exp(2*I*d*x)*cos(c + d*x)**2/4 - I*exp(a)*exp(2*I*d*x)*sin(c + d*x)*cos(c + d*x)/(4*d), Eq(b, 2*I*d)), (b*exp(a)*exp(b*x)*sin(c + d*x)*cos(c + d*x)/(b**2 + 4*d**2) + d*exp(a)*exp(b*x)*sin(c + d*x)**2/(b**2 + 4*d**2) - d*exp(a)*exp(b*x)*cos(c + d*x)**2/(b**2 + 4*d**2), True))`

3.39 $\int e^{a+bx} \cos(c+dx) \sin^2(c+dx) dx$

Optimal. Leaf size=119

$$\frac{de^{a+bx} \sin(c+dx)}{4(b^2+d^2)} - \frac{3de^{a+bx} \sin(3c+3dx)}{4(b^2+9d^2)} + \frac{be^{a+bx} \cos(c+dx)}{4(b^2+d^2)} - \frac{be^{a+bx} \cos(3c+3dx)}{4(b^2+9d^2)}$$

[Out] $1/4*b*\exp(b*x+a)*\cos(d*x+c)/(b^2+d^2)-1/4*b*\exp(b*x+a)*\cos(3*d*x+3*c)/(b^2+9*d^2)+1/4*d*\exp(b*x+a)*\sin(d*x+c)/(b^2+d^2)-3/4*d*\exp(b*x+a)*\sin(3*d*x+3*c)/(b^2+9*d^2)$

Rubi [A] time = 0.09, antiderivative size = 119, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 2, integrand size = 22, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {4469, 4433}

$$\frac{de^{a+bx} \sin(c+dx)}{4(b^2+d^2)} - \frac{3de^{a+bx} \sin(3c+3dx)}{4(b^2+9d^2)} + \frac{be^{a+bx} \cos(c+dx)}{4(b^2+d^2)} - \frac{be^{a+bx} \cos(3c+3dx)}{4(b^2+9d^2)}$$

Antiderivative was successfully verified.

[In] Int[E^(a + b*x)*Cos[c + d*x]*Sin[c + d*x]^2, x]

[Out] $(b*E^{(a + b*x)*\cos[c + d*x]})/(4*(b^2 + d^2)) - (b*E^{(a + b*x)*\cos[3*c + 3*d*x]})/(4*(b^2 + 9*d^2)) + (d*E^{(a + b*x)*\sin[c + d*x]})/(4*(b^2 + d^2)) - (3*d*E^{(a + b*x)*\sin[3*c + 3*d*x]})/(4*(b^2 + 9*d^2))$

Rule 4433

Int[Cos[(d_.) + (e_.)*(x_.)]*(F_)^((c_.)*((a_.) + (b_.)*(x_.))), x_Symbol] :=
Simp[(b*c*Log[F]*F^(c*(a + b*x))*Cos[d + e*x]/(e^2 + b^2*c^2*Log[F]^2), x]
+ Simp[(e*F^(c*(a + b*x))*Sin[d + e*x]/(e^2 + b^2*c^2*Log[F]^2), x] /; FreeQ[{F, a, b, c, d, e}, x] && NeQ[e^2 + b^2*c^2*Log[F]^2, 0]

Rule 4469

Int[Cos[(f_.) + (g_.)*(x_.)]^(n_.)*(F_)^((c_.)*((a_.) + (b_.)*(x_.)))*Sin[(d_.) + (e_.)*(x_.)]^(m_.), x_Symbol] := Int[ExpandTrigReduce[F^(c*(a + b*x)), Sin[d + e*x]^m*Cos[f + g*x]^n, x], x] /; FreeQ[{F, a, b, c, d, e, f, g}, x] && IGtQ[m, 0] && IGtQ[n, 0]

Rubi steps

$$\begin{aligned} \int e^{a+bx} \cos(c+dx) \sin^2(c+dx) dx &= \int \left(\frac{1}{4} e^{a+bx} \cos(c+dx) - \frac{1}{4} e^{a+bx} \cos(3c+3dx) \right) dx \\ &= \frac{1}{4} \int e^{a+bx} \cos(c+dx) dx - \frac{1}{4} \int e^{a+bx} \cos(3c+3dx) dx \\ &= \frac{be^{a+bx} \cos(c+dx)}{4(b^2+d^2)} - \frac{be^{a+bx} \cos(3c+3dx)}{4(b^2+9d^2)} + \frac{de^{a+bx} \sin(c+dx)}{4(b^2+d^2)} - \frac{3de^{a+bx} \sin(3c+3dx)}{4(b^2+9d^2)} \end{aligned}$$

Mathematica [A] time = 0.66, size = 74, normalized size = 0.62

$$\frac{1}{4} e^{a+bx} \left(\frac{b \cos(c+dx) + d \sin(c+dx)}{b^2+d^2} - \frac{b \cos(3(c+dx)) + 3d \sin(3(c+dx))}{b^2+9d^2} \right)$$

Antiderivative was successfully verified.

[In] Integrate[E^(a + b*x)*Cos[c + d*x]*Sin[c + d*x]^2,x]

[Out] (E^(a + b*x)*((b*Cos[c + d*x] + d*SIN[c + d*x])/(b^2 + d^2) - (b*Cos[3*(c + d*x)] + 3*d*SIN[3*(c + d*x)])/(b^2 + 9*d^2)))/4

fricas [A] time = 0.57, size = 109, normalized size = 0.92

$$\frac{(b^2d + 3d^3 - 3(b^2d + d^3)\cos(dx + c)^2)e^{(bx+a)}\sin(dx + c) - ((b^3 + bd^2)\cos(dx + c)^3 - (b^3 + 3bd^2)\cos(dx + c))}{b^4 + 10b^2d^2 + 9d^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(b*x+a)*cos(d*x+c)*sin(d*x+c)^2,x, algorithm="fricas")

[Out] ((b^2*d + 3*d^3 - 3*(b^2*d + d^3)*cos(d*x + c)^2)*e^(b*x + a)*sin(d*x + c) - ((b^3 + b*d^2)*cos(d*x + c)^3 - (b^3 + 3*b*d^2)*cos(d*x + c))*e^(b*x + a))/(b^4 + 10*b^2*d^2 + 9*d^4)

giac [A] time = 0.12, size = 98, normalized size = 0.82

$$-\frac{1}{4}\left(\frac{b\cos(3dx + 3c)}{b^2 + 9d^2} + \frac{3d\sin(3dx + 3c)}{b^2 + 9d^2}\right)e^{(bx+a)} + \frac{1}{4}\left(\frac{b\cos(dx + c)}{b^2 + d^2} + \frac{d\sin(dx + c)}{b^2 + d^2}\right)e^{(bx+a)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(b*x+a)*cos(d*x+c)*sin(d*x+c)^2,x, algorithm="giac")

[Out] -1/4*(b*cos(3*d*x + 3*c)/(b^2 + 9*d^2) + 3*d*sin(3*d*x + 3*c)/(b^2 + 9*d^2))*e^(b*x + a) + 1/4*(b*cos(d*x + c)/(b^2 + d^2) + d*sin(d*x + c)/(b^2 + d^2))*e^(b*x + a)

maple [A] time = 0.16, size = 108, normalized size = 0.91

$$\frac{be^{bx+a}\cos(dx + c)}{4b^2 + 4d^2} - \frac{be^{bx+a}\cos(3dx + 3c)}{4(b^2 + 9d^2)} + \frac{de^{bx+a}\sin(dx + c)}{4b^2 + 4d^2} - \frac{3de^{bx+a}\sin(3dx + 3c)}{4(b^2 + 9d^2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(exp(b*x+a)*cos(d*x+c)*sin(d*x+c)^2,x)

[Out] 1/4*b*exp(b*x+a)*cos(d*x+c)/(b^2+d^2)-1/4*b*exp(b*x+a)*cos(3*d*x+3*c)/(b^2+9*d^2)+1/4*d*exp(b*x+a)*sin(d*x+c)/(b^2+d^2)-3/4*d*exp(b*x+a)*sin(3*d*x+3*c)/(b^2+9*d^2)

maxima [B] time = 0.35, size = 538, normalized size = 4.52

$$\frac{(b^3\cos(3c)e^a + bd^2\cos(3c)e^a + 3b^2de^a\sin(3c) + 3d^3e^a\sin(3c))\cos(3dx)e^{(bx)} + (b^3\cos(3c)e^a + bd^2\cos(3c)e^a)}{b^4 + 10b^2d^2 + 9d^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(b*x+a)*cos(d*x+c)*sin(d*x+c)^2,x, algorithm="maxima")

[Out] -1/8*((b^3*cos(3*c)*e^a + b*d^2*cos(3*c)*e^a + 3*b^2*d*e^a*sin(3*c) + 3*d^3*e^a*sin(3*c))*cos(3*d*x)*e^(b*x) + (b^3*cos(3*c)*e^a + b*d^2*cos(3*c)*e^a - 3*b^2*d*e^a*sin(3*c) - 3*d^3*e^a*sin(3*c))*cos(3*d*x + 6*c)*e^(b*x) - (b^3*cos(3*c)*e^a + 9*b*d^2*cos(3*c)*e^a - b^2*d*e^a*sin(3*c) - 9*d^3*e^a*sin(3*c))*cos(d*x + 4*c)*e^(b*x) - (b^3*cos(3*c)*e^a + 9*b*d^2*cos(3*c)*e^a + b^2*d*e^a*sin(3*c) + 9*d^3*e^a*sin(3*c))*cos(d*x - 2*c)*e^(b*x) + (3*b^2*d*cos(3*c)*e^a + 3*d^3*cos(3*c)*e^a - b^3*e^a*sin(3*c) - b*d^2*e^a*sin(3*c))*e^(b*x)*sin(3*d*x) + (3*b^2*d*cos(3*c)*e^a + 3*d^3*cos(3*c)*e^a + b^3*e^a*sin(3*c) + b*d^2*e^a*sin(3*c))*e^(b*x)*sin(3*d*x + 6*c) - (b^2*d*cos(3*c)*e^a

$$+ 9*d^3*\cos(3*c)*e^a + b^3*e^a*\sin(3*c) + 9*b*d^2*e^a*\sin(3*c))*e^{(b*x)*\sin(d*x + 4*c) - (b^2*d*\cos(3*c)*e^a + 9*d^3*\cos(3*c)*e^a - b^3*e^a*\sin(3*c) - 9*b*d^2*e^a*\sin(3*c))*e^{(b*x)*\sin(d*x - 2*c)}/(b^4*\cos(3*c)^2 + b^4*\sin(3*c)^2 + 9*(\cos(3*c)^2 + \sin(3*c)^2)*d^4 + 10*(b^2*\cos(3*c)^2 + b^2*\sin(3*c)^2)*d^2)$$

mupad [B] time = 3.01, size = 166, normalized size = 1.39

$$\frac{e^{a+bx} (\cos(dx) - \sin(dx) 1i) (\cos(c) - \sin(c) 1i)}{8 (b - d 1i)} - \frac{e^{a+bx} (\cos(3dx) + \sin(3dx) 1i) (\cos(3c) + \sin(3c) 1i)}{8 (-3d + b 1i)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(cos(c + d*x)*exp(a + b*x)*sin(c + d*x)^2,x)

[Out] (exp(a + b*x)*(cos(d*x) - sin(d*x)*1i)*(cos(c) - sin(c)*1i))/(8*(b - d*1i)) - (exp(a + b*x)*(cos(3*d*x) + sin(3*d*x)*1i)*(cos(3*c) + sin(3*c)*1i)*1i)/(8*(b*1i - 3*d)) + (exp(a + b*x)*(cos(d*x) + sin(d*x)*1i)*(cos(c) + sin(c)*1i)*1i)/(8*(b*1i - d)) - (exp(a + b*x)*(cos(3*d*x) - sin(3*d*x)*1i)*(cos(3*c) - sin(3*c)*1i))/(8*(b - d*3i))

sympy [A] time = 44.43, size = 1030, normalized size = 8.66

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(b*x+a)*cos(d*x+c)*sin(d*x+c)**2,x)

[Out] Piecewise((x*exp(a)*sin(c)**2*cos(c), Eq(b, 0) & Eq(d, 0)), (I*x*exp(a)*exp(-3*I*d*x)*sin(c + d*x)**3/8 + 3*x*exp(a)*exp(-3*I*d*x)*sin(c + d*x)**2*cos(c + d*x)/8 - 3*I*x*exp(a)*exp(-3*I*d*x)*sin(c + d*x)*cos(c + d*x)**2/8 - x*exp(a)*exp(-3*I*d*x)*cos(c + d*x)**3/8 + exp(a)*exp(-3*I*d*x)*sin(c + d*x)**3/(24*d) - exp(a)*exp(-3*I*d*x)*sin(c + d*x)*cos(c + d*x)**2/(4*d) + I*exp(a)*exp(-3*I*d*x)*cos(c + d*x)**3/(8*d), Eq(b, -3*I*d)), (I*x*exp(a)*exp(-I*d*x)*sin(c + d*x)**3/8 + x*exp(a)*exp(-I*d*x)*sin(c + d*x)**2*cos(c + d*x)/8 + I*x*exp(a)*exp(-I*d*x)*sin(c + d*x)*cos(c + d*x)**2/8 + x*exp(a)*exp(-I*d*x)*cos(c + d*x)**3/8 + exp(a)*exp(-I*d*x)*sin(c + d*x)**3/(8*d) - exp(a)*exp(-I*d*x)*sin(c + d*x)*cos(c + d*x)**2/(4*d) + I*exp(a)*exp(-I*d*x)*cos(c + d*x)**3/(8*d), Eq(b, -I*d)), (-I*x*exp(a)*exp(I*d*x)*sin(c + d*x)**3/8 + x*exp(a)*exp(I*d*x)*sin(c + d*x)**2*cos(c + d*x)/8 - I*x*exp(a)*exp(I*d*x)*sin(c + d*x)*cos(c + d*x)**2/8 + x*exp(a)*exp(I*d*x)*cos(c + d*x)**3/8 + exp(a)*exp(I*d*x)*sin(c + d*x)**3/(8*d) - exp(a)*exp(I*d*x)*sin(c + d*x)*cos(c + d*x)**2/(4*d) - I*exp(a)*exp(I*d*x)*cos(c + d*x)**3/(8*d), Eq(b, I*d)), (-I*x*exp(a)*exp(3*I*d*x)*sin(c + d*x)**3/8 + 3*x*exp(a)*exp(3*I*d*x)*sin(c + d*x)**2*cos(c + d*x)/8 + 3*I*x*exp(a)*exp(3*I*d*x)*sin(c + d*x)*cos(c + d*x)**2/8 - x*exp(a)*exp(3*I*d*x)*cos(c + d*x)**3/8 + exp(a)*exp(3*I*d*x)*sin(c + d*x)**3/(24*d) - exp(a)*exp(3*I*d*x)*sin(c + d*x)*cos(c + d*x)**2/(4*d) - I*exp(a)*exp(3*I*d*x)*cos(c + d*x)**3/(8*d), Eq(b, 3*I*d)), (b**3*exp(a)*exp(b*x)*sin(c + d*x)**2*cos(c + d*x)/(b**4 + 10*b**2*d**2 + 9*d**4) + b**2*d*exp(a)*exp(b*x)*sin(c + d*x)**3/(b**4 + 10*b**2*d**2 + 9*d**4) - 2*b**2*d*exp(a)*exp(b*x)*sin(c + d*x)*cos(c + d*x)**2/(b**4 + 10*b**2*d**2 + 9*d**4) + 3*b*d**2*exp(a)*exp(b*x)*sin(c + d*x)**2*cos(c + d*x)/(b**4 + 10*b**2*d**2 + 9*d**4) + 2*b*d**2*exp(a)*exp(b*x)*cos(c + d*x)**3/(b**4 + 10*b**2*d**2 + 9*d**4) + 3*d**3*exp(a)*exp(b*x)*sin(c + d*x)**3/(b**4 + 10*b**2*d**2 + 9*d**4), True))

3.40 $\int e^{a+bx} \cos(c + dx) \sin^3(c + dx) dx$

Optimal. Leaf size=129

$$\frac{be^{a+bx} \sin(2c + 2dx)}{4(b^2 + 4d^2)} - \frac{be^{a+bx} \sin(4c + 4dx)}{8(b^2 + 16d^2)} - \frac{de^{a+bx} \cos(2c + 2dx)}{2(b^2 + 4d^2)} + \frac{de^{a+bx} \cos(4c + 4dx)}{2(b^2 + 16d^2)}$$

[Out] $-1/2*d*\exp(b*x+a)*\cos(2*d*x+2*c)/(b^2+4*d^2)+1/2*d*\exp(b*x+a)*\cos(4*d*x+4*c)/(b^2+16*d^2)+1/4*b*\exp(b*x+a)*\sin(2*d*x+2*c)/(b^2+4*d^2)-1/8*b*\exp(b*x+a)*\sin(4*d*x+4*c)/(b^2+16*d^2)$

Rubi [A] time = 0.09, antiderivative size = 129, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 2, integrand size = 22, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {4469, 4432}

$$\frac{be^{a+bx} \sin(2c + 2dx)}{4(b^2 + 4d^2)} - \frac{be^{a+bx} \sin(4c + 4dx)}{8(b^2 + 16d^2)} - \frac{de^{a+bx} \cos(2c + 2dx)}{2(b^2 + 4d^2)} + \frac{de^{a+bx} \cos(4c + 4dx)}{2(b^2 + 16d^2)}$$

Antiderivative was successfully verified.

[In] $\text{Int}[E^{(a + b*x)}*\text{Cos}[c + d*x]*\text{Sin}[c + d*x]^3, x]$

[Out] $-(d*E^{(a + b*x)}*\text{Cos}[2*c + 2*d*x])/(2*(b^2 + 4*d^2)) + (d*E^{(a + b*x)}*\text{Cos}[4*c + 4*d*x])/(2*(b^2 + 16*d^2)) + (b*E^{(a + b*x)}*\text{Sin}[2*c + 2*d*x])/(4*(b^2 + 4*d^2)) - (b*E^{(a + b*x)}*\text{Sin}[4*c + 4*d*x])/(8*(b^2 + 16*d^2))$

Rule 4432

$\text{Int}[(F_)^{((c_.)*((a_.) + (b_.)*(x_)))}*\text{Sin}[(d_.) + (e_.)*(x_)], x_Symbol] \rightarrow \text{Simp}[(b*c*\text{Log}[F]*F^{(c*(a + b*x))*\text{Sin}[d + e*x]})/(e^2 + b^2*c^2*\text{Log}[F]^2), x] - \text{Simp}[(e*F^{(c*(a + b*x))*\text{Cos}[d + e*x]})/(e^2 + b^2*c^2*\text{Log}[F]^2), x] /; \text{FreeQ}\{F, a, b, c, d, e, x\} \&\& \text{NeQ}[e^2 + b^2*c^2*\text{Log}[F]^2, 0]$

Rule 4469

$\text{Int}[\text{Cos}[(f_.) + (g_.)*(x_)]^{(n_.)}*(F_)^{((c_.)*((a_.) + (b_.)*(x_)))}*\text{Sin}[(d_.) + (e_.)*(x_)]^{(m_.)}, x_Symbol] \rightarrow \text{Int}[\text{ExpandTrigReduce}[F^{(c*(a + b*x))}, \text{Sin}[d + e*x]^{m*\text{Cos}[f + g*x]^n}, x], x] /; \text{FreeQ}\{F, a, b, c, d, e, f, g, x\} \&\& \text{IGtQ}[m, 0] \&\& \text{IGtQ}[n, 0]$

Rubi steps

$$\begin{aligned} \int e^{a+bx} \cos(c + dx) \sin^3(c + dx) dx &= \int \left(\frac{1}{4} e^{a+bx} \sin(2c + 2dx) - \frac{1}{8} e^{a+bx} \sin(4c + 4dx) \right) dx \\ &= -\left(\frac{1}{8} \int e^{a+bx} \sin(4c + 4dx) dx \right) + \frac{1}{4} \int e^{a+bx} \sin(2c + 2dx) dx \\ &= -\frac{de^{a+bx} \cos(2c + 2dx)}{2(b^2 + 4d^2)} + \frac{de^{a+bx} \cos(4c + 4dx)}{2(b^2 + 16d^2)} + \frac{be^{a+bx} \sin(2c + 2dx)}{4(b^2 + 4d^2)} - \frac{be^{a+bx} \sin(4c + 4dx)}{8(b^2 + 16d^2)} \end{aligned}$$

Mathematica [A] time = 0.90, size = 82, normalized size = 0.64

$$\frac{1}{8} e^{a+bx} \left(\frac{2(b \sin(2(c + dx)) - 2d \cos(2(c + dx)))}{b^2 + 4d^2} + \frac{4d \cos(4(c + dx)) - b \sin(4(c + dx))}{b^2 + 16d^2} \right)$$

Antiderivative was successfully verified.

[In] Integrate[E^(a + b*x)*Cos[c + d*x]*Sin[c + d*x]^3,x]

[Out] (E^(a + b*x)*((2*(-2*d*Cos[2*(c + d*x)] + b*Ssin[2*(c + d*x)])))/(b^2 + 4*d^2) + (4*d*Cos[4*(c + d*x)] - b*Ssin[4*(c + d*x)])/(b^2 + 16*d^2))/8

fricas [A] time = 0.65, size = 135, normalized size = 1.05

$$\frac{\left(\left(b^3 + 4bd^2\right)\cos(dx + c)^3 - \left(b^3 + 10bd^2\right)\cos(dx + c)\right)e^{(bx+a)}\sin(dx + c) - \left(4\left(b^2d + 4d^3\right)\cos(dx + c)^4 + b^4 + 20b^2d^2 + 64d^4\right)}{b^4 + 20b^2d^2 + 64d^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(b*x+a)*cos(d*x+c)*sin(d*x+c)^3,x, algorithm="fricas")

[Out] -(((b^3 + 4*b*d^2)*cos(d*x + c)^3 - (b^3 + 10*b*d^2)*cos(d*x + c))*e^(b*x + a)*sin(d*x + c) - (4*(b^2*d + 4*d^3)*cos(d*x + c)^4 + b^2*d + 10*d^3 - (5*b^2*d + 32*d^3)*cos(d*x + c)^2)*e^(b*x + a))/(b^4 + 20*b^2*d^2 + 64*d^4)

giac [A] time = 0.14, size = 111, normalized size = 0.86

$$\frac{1}{8}\left(\frac{4d\cos(4dx + 4c)}{b^2 + 16d^2} - \frac{b\sin(4dx + 4c)}{b^2 + 16d^2}\right)e^{(bx+a)} - \frac{1}{4}\left(\frac{2d\cos(2dx + 2c)}{b^2 + 4d^2} - \frac{b\sin(2dx + 2c)}{b^2 + 4d^2}\right)e^{(bx+a)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(b*x+a)*cos(d*x+c)*sin(d*x+c)^3,x, algorithm="giac")

[Out] 1/8*(4*d*cos(4*d*x + 4*c)/(b^2 + 16*d^2) - b*sin(4*d*x + 4*c)/(b^2 + 16*d^2))*e^(b*x + a) - 1/4*(2*d*cos(2*d*x + 2*c)/(b^2 + 4*d^2) - b*sin(2*d*x + 2*c)/(b^2 + 4*d^2))*e^(b*x + a)

maple [A] time = 0.10, size = 118, normalized size = 0.91

$$\frac{de^{bx+a}\cos(2dx + 2c)}{2(b^2 + 4d^2)} + \frac{de^{bx+a}\cos(4dx + 4c)}{2b^2 + 32d^2} + \frac{be^{bx+a}\sin(2dx + 2c)}{4b^2 + 16d^2} - \frac{be^{bx+a}\sin(4dx + 4c)}{8(b^2 + 16d^2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(exp(b*x+a)*cos(d*x+c)*sin(d*x+c)^3,x)

[Out] -1/2*d*exp(b*x+a)*cos(2*d*x+2*c)/(b^2+4*d^2)+1/2*d*exp(b*x+a)*cos(4*d*x+4*c)/(b^2+16*d^2)+1/4*b*exp(b*x+a)*sin(2*d*x+2*c)/(b^2+4*d^2)-1/8*b*exp(b*x+a)*sin(4*d*x+4*c)/(b^2+16*d^2)

maxima [B] time = 0.35, size = 550, normalized size = 4.26

$$\frac{\left(4b^2d\cos(4c)e^a + 16d^3\cos(4c)e^a - b^3e^a\sin(4c) - 4bd^2e^a\sin(4c)\right)\cos(4dx)e^{(bx)} + \left(4b^2d\cos(4c)e^a + 16d^3\cos(4c)e^a - b^3e^a\sin(4c) - 4bd^2e^a\sin(4c)\right)\sin(4dx)e^{(bx)}}{b^4 + 20b^2d^2 + 64d^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(b*x+a)*cos(d*x+c)*sin(d*x+c)^3,x, algorithm="maxima")

[Out] 1/16*((4*b^2*d*cos(4*c))*e^a + 16*d^3*cos(4*c))*e^a - b^3*e^a*sin(4*c) - 4*b*d^2*e^a*sin(4*c))*cos(4*d*x)*e^(b*x) + (4*b^2*d*cos(4*c))*e^a + 16*d^3*cos(4*c))*e^a + b^3*e^a*sin(4*c) + 4*b*d^2*e^a*sin(4*c))*cos(4*d*x + 8*c)*e^(b*x) - 2*(2*b^2*d*cos(4*c))*e^a + 32*d^3*cos(4*c))*e^a + b^3*e^a*sin(4*c) + 16*b*d^2*e^a*sin(4*c))*cos(2*d*x + 6*c)*e^(b*x) - 2*(2*b^2*d*cos(4*c))*e^a + 32*d^3*cos(4*c))*e^a - b^3*e^a*sin(4*c) - 16*b*d^2*e^a*sin(4*c))*cos(2*d*x - 2*c)*e^(b*x) - (b^3*cos(4*c))*e^a + 4*b*d^2*cos(4*c))*e^a + 4*b^2*d*e^a*sin(4*c) + 16*d^3*e^a*sin(4*c))*e^(b*x)*sin(4*d*x) - (b^3*cos(4*c))*e^a + 4*b*d^2*cos(4*c))*e^a - 4*b^2*d*e^a*sin(4*c) - 16*d^3*e^a*sin(4*c))*e^(b*x)*sin(4*d*x

$$+ 8*c) + 2*(b^3*\cos(4*c)*e^a + 16*b*d^2*\cos(4*c)*e^a - 2*b^2*d*e^a*\sin(4*c) - 32*d^3*e^a*\sin(4*c))*e^{(b*x)*\sin(2*d*x + 6*c)} + 2*(b^3*\cos(4*c)*e^a + 16*b*d^2*\cos(4*c)*e^a + 2*b^2*d*e^a*\sin(4*c) + 32*d^3*e^a*\sin(4*c))*e^{(b*x)*\sin(2*d*x - 2*c)}/(b^4*\cos(4*c)^2 + b^4*\sin(4*c)^2 + 64*(\cos(4*c)^2 + \sin(4*c)^2)*d^4 + 20*(b^2*\cos(4*c)^2 + b^2*\sin(4*c)^2)*d^2)$$

mupad [B] time = 3.03, size = 178, normalized size = 1.38

$$\frac{e^{a+bx} (\cos(2dx) - \sin(2dx) 1i) (\cos(2c) - \sin(2c) 1i)}{8(2d + b1i)} + \frac{e^{a+bx} (\cos(4dx) - \sin(4dx) 1i) (\cos(4c) - \sin(4c) 1i)}{16(4d + b1i)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(cos(c + d*x)*exp(a + b*x)*sin(c + d*x)^3,x)

[Out] (exp(a + b*x)*(cos(4*d*x) - sin(4*d*x)*1i)*(cos(4*c) - sin(4*c)*1i))/(16*(b*1i + 4*d)) - (exp(a + b*x)*(cos(2*d*x) - sin(2*d*x)*1i)*(cos(2*c) - sin(2*c)*1i))/(8*(b*1i + 2*d)) - (exp(a + b*x)*(cos(2*d*x) + sin(2*d*x)*1i)*(cos(2*c) + sin(2*c)*1i)*1i)/(8*(b + d*2i)) + (exp(a + b*x)*(cos(4*d*x) + sin(4*d*x)*1i)*(cos(4*c) + sin(4*c)*1i)*1i)/(16*(b + d*4i))

sympy [A] time = 148.00, size = 1353, normalized size = 10.49

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(b*x+a)*cos(d*x+c)*sin(d*x+c)**3,x)

[Out] Piecewise((x*exp(a)*sin(c)**3*cos(c), Eq(b, 0) & Eq(d, 0)), (I*x*exp(a)*exp(-4*I*d*x)*sin(c + d*x)**4/16 + x*exp(a)*exp(-4*I*d*x)*sin(c + d*x)**3*cos(c + d*x)/4 - 3*I*x*exp(a)*exp(-4*I*d*x)*sin(c + d*x)**2*cos(c + d*x)**2/8 - x*exp(a)*exp(-4*I*d*x)*sin(c + d*x)*cos(c + d*x)**3/4 + I*x*exp(a)*exp(-4*I*d*x)*cos(c + d*x)**4/16 - exp(a)*exp(-4*I*d*x)*sin(c + d*x)**4/(24*d) + 11*I*exp(a)*exp(-4*I*d*x)*sin(c + d*x)**3*cos(c + d*x)/(48*d) + 5*I*exp(a)*exp(-4*I*d*x)*sin(c + d*x)*cos(c + d*x)**3/(48*d) + exp(a)*exp(-4*I*d*x)*cos(c + d*x)**4/(24*d), Eq(b, -4*I*d)), (I*x*exp(a)*exp(-2*I*d*x)*sin(c + d*x)**4/8 + x*exp(a)*exp(-2*I*d*x)*sin(c + d*x)**3*cos(c + d*x)/4 + x*exp(a)*exp(-2*I*d*x)*sin(c + d*x)*cos(c + d*x)**3/4 - I*x*exp(a)*exp(-2*I*d*x)*cos(c + d*x)**4/8 + exp(a)*exp(-2*I*d*x)*sin(c + d*x)**4/(16*d) - exp(a)*exp(-2*I*d*x)*sin(c + d*x)**2*cos(c + d*x)**2/(4*d) + I*exp(a)*exp(-2*I*d*x)*sin(c + d*x)*cos(c + d*x)**3/(6*d) + exp(a)*exp(-2*I*d*x)*cos(c + d*x)**4/(48*d), Eq(b, -2*I*d)), (-I*x*exp(a)*exp(2*I*d*x)*sin(c + d*x)**4/8 + x*exp(a)*exp(2*I*d*x)*sin(c + d*x)**3*cos(c + d*x)/4 + x*exp(a)*exp(2*I*d*x)*sin(c + d*x)*cos(c + d*x)**3/4 + I*x*exp(a)*exp(2*I*d*x)*cos(c + d*x)**4/8 + exp(a)*exp(2*I*d*x)*sin(c + d*x)**4/(16*d) - exp(a)*exp(2*I*d*x)*sin(c + d*x)**2*cos(c + d*x)**2/(4*d) - I*exp(a)*exp(2*I*d*x)*sin(c + d*x)*cos(c + d*x)**3/(6*d) + exp(a)*exp(2*I*d*x)*cos(c + d*x)**4/(48*d), Eq(b, 2*I*d)), (-I*x*exp(a)*exp(4*I*d*x)*sin(c + d*x)**4/16 + x*exp(a)*exp(4*I*d*x)*sin(c + d*x)**3*cos(c + d*x)/4 + 3*I*x*exp(a)*exp(4*I*d*x)*sin(c + d*x)**2*cos(c + d*x)**2/8 - x*exp(a)*exp(4*I*d*x)*sin(c + d*x)*cos(c + d*x)**3/4 - I*x*exp(a)*exp(4*I*d*x)*cos(c + d*x)**4/16 - exp(a)*exp(4*I*d*x)*sin(c + d*x)**4/(24*d) - 11*I*exp(a)*exp(4*I*d*x)*sin(c + d*x)**3*cos(c + d*x)/(48*d) - 5*I*exp(a)*exp(4*I*d*x)*sin(c + d*x)*cos(c + d*x)**3/(48*d) + exp(a)*exp(4*I*d*x)*cos(c + d*x)**4/(24*d), Eq(b, 4*I*d)), (b**3*exp(a)*exp(b*x)*sin(c + d*x)**3*cos(c + d*x)/(b**4 + 20*b**2*d**2 + 64*d**4) + b**2*d*exp(a)*exp(b*x)*sin(c + d*x)**4/(b**4 + 20*b**2*d**2 + 64*d**4) - 3*b**2*d*exp(a)*exp(b*x)*sin(c + d*x)**2*cos(c + d*x)**2/(b**4 + 20*b**2*d**2 + 64*d**4) + 10*b*d**2*exp(a)*exp(b*x)*sin(c + d*x)**3*cos(c + d*x)/(b**4 + 20*b**2*d**2 + 64*d**4) + 6*b*d**2*exp(a)*exp(b*x)*sin(c + d*x)*cos(c + d*x)**3/(b**4 + 20*b**2*d**2 + 64*d**4) + 10*d**3*exp(a)*exp(b*x)*sin(c + d*x)**4/(b**4 + 20*b**2*d**2 + 64

```
*d**4) - 12*d**3*exp(a)*exp(b*x)*sin(c + d*x)**2*cos(c + d*x)**2/(b**4 + 20
*b**2*d**2 + 64*d**4) - 6*d**3*exp(a)*exp(b*x)*cos(c + d*x)**4/(b**4 + 20*b
**2*d**2 + 64*d**4), True))
```

3.41 $\int e^{a+bx} \cos^2(c+dx) \sin(c+dx) dx$

Optimal. Leaf size=119

$$\frac{be^{a+bx} \sin(c+dx)}{4(b^2+d^2)} + \frac{be^{a+bx} \sin(3c+3dx)}{4(b^2+9d^2)} - \frac{de^{a+bx} \cos(c+dx)}{4(b^2+d^2)} - \frac{3de^{a+bx} \cos(3c+3dx)}{4(b^2+9d^2)}$$

[Out] $-1/4*d*\exp(b*x+a)*\cos(d*x+c)/(b^2+d^2)-3/4*d*\exp(b*x+a)*\cos(3*d*x+3*c)/(b^2+9*d^2)+1/4*b*\exp(b*x+a)*\sin(d*x+c)/(b^2+d^2)+1/4*b*\exp(b*x+a)*\sin(3*d*x+3*c)/(b^2+9*d^2)$

Rubi [A] time = 0.08, antiderivative size = 119, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 2, integrand size = 22, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {4469, 4432}

$$\frac{be^{a+bx} \sin(c+dx)}{4(b^2+d^2)} + \frac{be^{a+bx} \sin(3c+3dx)}{4(b^2+9d^2)} - \frac{de^{a+bx} \cos(c+dx)}{4(b^2+d^2)} - \frac{3de^{a+bx} \cos(3c+3dx)}{4(b^2+9d^2)}$$

Antiderivative was successfully verified.

[In] Int[E^(a + b*x)*Cos[c + d*x]^2*Sin[c + d*x], x]

[Out] $-(d*E^{(a + b*x)*Cos[c + d*x]})/(4*(b^2 + d^2)) - (3*d*E^{(a + b*x)*Cos[3*c + 3*d*x]})/(4*(b^2 + 9*d^2)) + (b*E^{(a + b*x)*Sin[c + d*x]})/(4*(b^2 + d^2)) + (b*E^{(a + b*x)*Sin[3*c + 3*d*x]})/(4*(b^2 + 9*d^2))$

Rule 4432

Int[(F_)^((c_.)*((a_.) + (b_.)*(x_)))*Sin[(d_.) + (e_.)*(x_)], x_Symbol] :=
Simp[(b*c*Log[F]*F^(c*(a + b*x))*Sin[d + e*x])/(e^2 + b^2*c^2*Log[F]^2), x]
- Simp[(e*F^(c*(a + b*x))*Cos[d + e*x])/(e^2 + b^2*c^2*Log[F]^2), x] /; FreeQ[{F, a, b, c, d, e}, x] && NeQ[e^2 + b^2*c^2*Log[F]^2, 0]

Rule 4469

Int[Cos[(f_.) + (g_.)*(x_)]^(n_.)*(F_)^((c_.)*((a_.) + (b_.)*(x_)))*Sin[(d_.) + (e_.)*(x_)]^(m_.), x_Symbol] := Int[ExpandTrigReduce[F^(c*(a + b*x)), Sin[d + e*x]^m*Cos[f + g*x]^n, x], x] /; FreeQ[{F, a, b, c, d, e, f, g}, x] && IGtQ[m, 0] && IGtQ[n, 0]

Rubi steps

$$\begin{aligned} \int e^{a+bx} \cos^2(c+dx) \sin(c+dx) dx &= \int \left(\frac{1}{4} e^{a+bx} \sin(c+dx) + \frac{1}{4} e^{a+bx} \sin(3c+3dx) \right) dx \\ &= \frac{1}{4} \int e^{a+bx} \sin(c+dx) dx + \frac{1}{4} \int e^{a+bx} \sin(3c+3dx) dx \\ &= -\frac{de^{a+bx} \cos(c+dx)}{4(b^2+d^2)} - \frac{3de^{a+bx} \cos(3c+3dx)}{4(b^2+9d^2)} + \frac{be^{a+bx} \sin(c+dx)}{4(b^2+d^2)} + \frac{be^{a+bx} \sin(3c+3dx)}{4(b^2+9d^2)} \end{aligned}$$

Mathematica [A] time = 0.67, size = 74, normalized size = 0.62

$$\frac{1}{4} e^{a+bx} \left(\frac{b \sin(c+dx) - d \cos(c+dx)}{b^2+d^2} + \frac{b \sin(3(c+dx)) - 3d \cos(3(c+dx))}{b^2+9d^2} \right)$$

Antiderivative was successfully verified.

[In] Integrate[E^(a + b*x)*Cos[c + d*x]^2*Sin[c + d*x],x]

[Out] (E^(a + b*x)*((-d*cos[c + d*x]) + b*Sin[c + d*x])/(b^2 + d^2) + (-3*d*cos[3*(c + d*x)] + b*Sin[3*(c + d*x)])/(b^2 + 9*d^2))/4

fricas [A] time = 0.89, size = 98, normalized size = 0.82

$$\frac{(2bd^2 + (b^3 + bd^2)\cos(dx + c)^2)e^{(bx+a)}\sin(dx + c) + (2b^2d\cos(dx + c) - 3(b^2d + d^3)\cos(dx + c)^3)e^{(bx+a)}}{b^4 + 10b^2d^2 + 9d^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(b*x+a)*cos(d*x+c)^2*sin(d*x+c),x, algorithm="fricas")

[Out] ((2*b*d^2 + (b^3 + b*d^2)*cos(d*x + c)^2)*e^(b*x + a)*sin(d*x + c) + (2*b^2*d*cos(d*x + c) - 3*(b^2*d + d^3)*cos(d*x + c)^3)*e^(b*x + a))/(b^4 + 10*b^2*d^2 + 9*d^4)

giac [A] time = 0.14, size = 100, normalized size = 0.84

$$-\frac{1}{4}\left(\frac{3d\cos(3dx + 3c)}{b^2 + 9d^2} - \frac{b\sin(3dx + 3c)}{b^2 + 9d^2}\right)e^{(bx+a)} - \frac{1}{4}\left(\frac{d\cos(dx + c)}{b^2 + d^2} - \frac{b\sin(dx + c)}{b^2 + d^2}\right)e^{(bx+a)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(b*x+a)*cos(d*x+c)^2*sin(d*x+c),x, algorithm="giac")

[Out] -1/4*(3*d*cos(3*d*x + 3*c)/(b^2 + 9*d^2) - b*sin(3*d*x + 3*c)/(b^2 + 9*d^2))*e^(b*x + a) - 1/4*(d*cos(d*x + c)/(b^2 + d^2) - b*sin(d*x + c)/(b^2 + d^2))*e^(b*x + a)

maple [A] time = 0.10, size = 108, normalized size = 0.91

$$-\frac{de^{bx+a}\cos(dx + c)}{4(b^2 + d^2)} - \frac{3de^{bx+a}\cos(3dx + 3c)}{4(b^2 + 9d^2)} + \frac{be^{bx+a}\sin(dx + c)}{4b^2 + 4d^2} + \frac{be^{bx+a}\sin(3dx + 3c)}{4b^2 + 36d^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(exp(b*x+a)*cos(d*x+c)^2*sin(d*x+c),x)

[Out] -1/4*d*exp(b*x+a)*cos(d*x+c)/(b^2+d^2)-3/4*d*exp(b*x+a)*cos(3*d*x+3*c)/(b^2+9*d^2)+1/4*b*exp(b*x+a)*sin(d*x+c)/(b^2+d^2)+1/4*b*exp(b*x+a)*sin(3*d*x+3*c)/(b^2+9*d^2)

maxima [B] time = 0.36, size = 538, normalized size = 4.52

$$\frac{(3b^2d\cos(3c)e^a + 3d^3\cos(3c)e^a - b^3e^a\sin(3c) - bd^2e^a\sin(3c))\cos(3dx)e^{(bx)} + (3b^2d\cos(3c)e^a + 3d^3\cos(3c)e^a - b^3e^a\sin(3c) - bd^2e^a\sin(3c))\sin(3dx)e^{(bx)}}{b^4 + 10b^2d^2 + 9d^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(b*x+a)*cos(d*x+c)^2*sin(d*x+c),x, algorithm="maxima")

[Out] -1/8*((3*b^2*d*cos(3*c)*e^a + 3*d^3*cos(3*c)*e^a - b^3*e^a*sin(3*c) - b*d^2*e^a*sin(3*c))*cos(3*d*x)*e^(b*x) + (3*b^2*d*cos(3*c)*e^a + 3*d^3*cos(3*c)*e^a + b^3*e^a*sin(3*c) + b*d^2*e^a*sin(3*c))*cos(3*d*x + 6*c)*e^(b*x) + (b^2*d*cos(3*c)*e^a + 9*d^3*cos(3*c)*e^a + b^3*e^a*sin(3*c) + 9*b*d^2*e^a*sin(3*c))*cos(d*x + 4*c)*e^(b*x) + (b^2*d*cos(3*c)*e^a + 9*d^3*cos(3*c)*e^a - b^3*e^a*sin(3*c) - 9*b*d^2*e^a*sin(3*c))*cos(d*x - 2*c)*e^(b*x) - (b^3*cos(3*c)*e^a + b*d^2*cos(3*c)*e^a + 3*b^2*d*e^a*sin(3*c) + 3*d^3*e^a*sin(3*c))*e^(b*x)*sin(3*d*x) - (b^3*cos(3*c)*e^a + b*d^2*cos(3*c)*e^a - 3*b^2*d*e^a*sin(3*c) - 3*d^3*e^a*sin(3*c))*e^(b*x)*sin(3*d*x + 6*c) - (b^3*cos(3*c)*e^a + b*d^2*cos(3*c)*e^a + 3*b^2*d*e^a*sin(3*c) + 3*d^3*e^a*sin(3*c))*e^(b*x)*sin(3*d*x + 6*c)

$$\frac{9*b*d^2*\cos(3*c)*e^a - b^2*d*e^a*\sin(3*c) - 9*d^3*e^a*\sin(3*c))*e^{(b*x)*\sin(d*x + 4*c)} - (b^3*\cos(3*c)*e^a + 9*b*d^2*\cos(3*c)*e^a + b^2*d*e^a*\sin(3*c) + 9*d^3*e^a*\sin(3*c))*e^{(b*x)*\sin(d*x - 2*c)}}{(b^4*\cos(3*c)^2 + b^4*\sin(3*c)^2 + 9*(\cos(3*c)^2 + \sin(3*c)^2)*d^4 + 10*(b^2*\cos(3*c)^2 + b^2*\sin(3*c)^2)*d^2)}$$

mupad [B] time = 0.86, size = 167, normalized size = 1.40

$$\frac{e^{a+bx} (\cos(dx) - \sin(dx) 1i) (\cos(c) - \sin(c) 1i)}{8 (d + b 1i)} - \frac{e^{a+bx} (\cos(dx) + \sin(dx) 1i) (\cos(c) + \sin(c) 1i) 1i}{8 (b + d 1i)} - \frac{e^{a+bx}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(cos(c + d*x)^2*exp(a + b*x)*sin(c + d*x),x)

[Out] - (exp(a + b*x)*(cos(d*x) - sin(d*x)*1i)*(cos(c) - sin(c)*1i))/(8*(b*1i + d)) - (exp(a + b*x)*(cos(d*x) + sin(d*x)*1i)*(cos(c) + sin(c)*1i)*1i)/(8*(b + d*1i)) - (exp(a + b*x)*(cos(3*d*x) - sin(3*d*x)*1i)*(cos(3*c) - sin(3*c)*1i))/(8*(b*1i + 3*d)) - (exp(a + b*x)*(cos(3*d*x) + sin(3*d*x)*1i)*(cos(3*c) + sin(3*c)*1i)*1i)/(8*(b + d*3i))

sympy [A] time = 44.75, size = 1040, normalized size = 8.74

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(b*x+a)*cos(d*x+c)**2*sin(d*x+c),x)

[Out] Piecewise((x*exp(a)*sin(c)*cos(c)**2, Eq(b, 0) & Eq(d, 0)), (-x*exp(a)*exp(-3*I*d*x)*sin(c + d*x)**3/8 + 3*I*x*exp(a)*exp(-3*I*d*x)*sin(c + d*x)**2*cos(c + d*x)/8 + 3*x*exp(a)*exp(-3*I*d*x)*sin(c + d*x)*cos(c + d*x)**2/8 - I*x*exp(a)*exp(-3*I*d*x)*cos(c + d*x)**3/8 + I*exp(a)*exp(-3*I*d*x)*sin(c + d*x)**3/(24*d) + I*exp(a)*exp(-3*I*d*x)*sin(c + d*x)*cos(c + d*x)**2/(4*d) + exp(a)*exp(-3*I*d*x)*cos(c + d*x)**3/(24*d), Eq(b, -3*I*d)), (x*exp(a)*exp(-I*d*x)*sin(c + d*x)**3/8 - I*x*exp(a)*exp(-I*d*x)*sin(c + d*x)**2*cos(c + d*x)/8 + x*exp(a)*exp(-I*d*x)*sin(c + d*x)*cos(c + d*x)**2/8 - I*x*exp(a)*exp(-I*d*x)*cos(c + d*x)**3/8 - I*exp(a)*exp(-I*d*x)*sin(c + d*x)**3/(8*d) - I*exp(a)*exp(-I*d*x)*sin(c + d*x)*cos(c + d*x)**2/(4*d) - 3*exp(a)*exp(-I*d*x)*cos(c + d*x)**3/(8*d), Eq(b, -I*d)), (x*exp(a)*exp(I*d*x)*sin(c + d*x)**3/8 + I*x*exp(a)*exp(I*d*x)*sin(c + d*x)**2*cos(c + d*x)/8 + x*exp(a)*exp(I*d*x)*sin(c + d*x)*cos(c + d*x)**2/8 + I*x*exp(a)*exp(I*d*x)*cos(c + d*x)**3/8 + I*exp(a)*exp(I*d*x)*sin(c + d*x)**3/(8*d) + I*exp(a)*exp(I*d*x)*sin(c + d*x)*cos(c + d*x)**2/(4*d) - 3*exp(a)*exp(I*d*x)*cos(c + d*x)**3/(8*d), Eq(b, I*d)), (-x*exp(a)*exp(3*I*d*x)*sin(c + d*x)**3/8 - 3*I*x*exp(a)*exp(3*I*d*x)*sin(c + d*x)**2*cos(c + d*x)/8 + 3*x*exp(a)*exp(3*I*d*x)*sin(c + d*x)*cos(c + d*x)**2/8 + I*x*exp(a)*exp(3*I*d*x)*cos(c + d*x)**3/8 - I*exp(a)*exp(3*I*d*x)*sin(c + d*x)**3/(24*d) - I*exp(a)*exp(3*I*d*x)*sin(c + d*x)*cos(c + d*x)**2/(4*d) + exp(a)*exp(3*I*d*x)*cos(c + d*x)**3/(24*d), Eq(b, 3*I*d)), (b**3*exp(a)*exp(b*x)*sin(c + d*x)*cos(c + d*x)**2/(b**4 + 10*b**2*d**2 + 9*d**4) + 2*b**2*d*exp(a)*exp(b*x)*sin(c + d*x)**2*cos(c + d*x)/(b**4 + 10*b**2*d**2 + 9*d**4) - b**2*d*exp(a)*exp(b*x)*cos(c + d*x)**3/(b**4 + 10*b**2*d**2 + 9*d**4) + 2*b*d**2*exp(a)*exp(b*x)*sin(c + d*x)**3/(b**4 + 10*b**2*d**2 + 9*d**4) + 3*b*d**2*exp(a)*exp(b*x)*sin(c + d*x)*cos(c + d*x)**2/(b**4 + 10*b**2*d**2 + 9*d**4) - 3*d**3*exp(a)*exp(b*x)*cos(c + d*x)**3/(b**4 + 10*b**2*d**2 + 9*d**4), True))

3.42 $\int e^{a+bx} \cos^2(c + dx) \sin^2(c + dx) dx$

Optimal. Leaf size=79

$$-\frac{de^{a+bx} \sin(4c + 4dx)}{2(b^2 + 16d^2)} - \frac{be^{a+bx} \cos(4c + 4dx)}{8(b^2 + 16d^2)} + \frac{e^{a+bx}}{8b}$$

[Out] $1/8*\exp(b*x+a)/b-1/8*b*\exp(b*x+a)*\cos(4*d*x+4*c)/(b^2+16*d^2)-1/2*d*\exp(b*x+a)*\sin(4*d*x+4*c)/(b^2+16*d^2)$

Rubi [A] time = 0.08, antiderivative size = 79, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 3, integrand size = 24, $\frac{\text{number of rules}}{\text{integrand size}} = 0.125$, Rules used = {4469, 2194, 4433}

$$-\frac{de^{a+bx} \sin(4c + 4dx)}{2(b^2 + 16d^2)} - \frac{be^{a+bx} \cos(4c + 4dx)}{8(b^2 + 16d^2)} + \frac{e^{a+bx}}{8b}$$

Antiderivative was successfully verified.

[In] Int[E^(a + b*x)*Cos[c + d*x]^2*Sin[c + d*x]^2,x]

[Out] $E^{(a + b*x)}/(8*b) - (b*E^{(a + b*x)*Cos[4*c + 4*d*x]})/(8*(b^2 + 16*d^2)) - (d*E^{(a + b*x)*Sin[4*c + 4*d*x]})/(2*(b^2 + 16*d^2))$

Rule 2194

Int[((F_)^((c_)*(a_) + (b_)*(x_)))^(n_), x_Symbol] := Simp[(F^(c*(a + b*x)))^n/(b*c*n*Log[F]), x] /; FreeQ[{F, a, b, c, n}, x]

Rule 4433

Int[Cos[(d_) + (e_)*(x_)]*(F_)^((c_)*(a_) + (b_)*(x_)), x_Symbol] := Simp[(b*c*Log[F]*F^(c*(a + b*x))*Cos[d + e*x]/(e^2 + b^2*c^2*Log[F]^2), x] + Simp[(e*F^(c*(a + b*x))*Sin[d + e*x]/(e^2 + b^2*c^2*Log[F]^2), x] /; FreeQ[{F, a, b, c, d, e}, x] && NeQ[e^2 + b^2*c^2*Log[F]^2, 0]

Rule 4469

Int[Cos[(f_) + (g_)*(x_)]^(n_)*(F_)^((c_)*(a_) + (b_)*(x_))*Sin[(d_) + (e_)*(x_)]^(m_), x_Symbol] := Int[ExpandTrigReduce[F^(c*(a + b*x)), Sin[d + e*x]^m*Cos[f + g*x]^n, x], x] /; FreeQ[{F, a, b, c, d, e, f, g}, x] && IGtQ[m, 0] && IGtQ[n, 0]

Rubi steps

$$\begin{aligned} \int e^{a+bx} \cos^2(c + dx) \sin^2(c + dx) dx &= \int \left(\frac{1}{8}e^{a+bx} - \frac{1}{8}e^{a+bx} \cos(4c + 4dx) \right) dx \\ &= \frac{1}{8} \int e^{a+bx} dx - \frac{1}{8} \int e^{a+bx} \cos(4c + 4dx) dx \\ &= \frac{e^{a+bx}}{8b} - \frac{be^{a+bx} \cos(4c + 4dx)}{8(b^2 + 16d^2)} - \frac{de^{a+bx} \sin(4c + 4dx)}{2(b^2 + 16d^2)} \end{aligned}$$

Mathematica [A] time = 0.38, size = 57, normalized size = 0.72

$$\frac{e^{a+bx} (b^2(-\cos(4(c + dx))) + b^2 - 4bd \sin(4(c + dx)) + 16d^2)}{8(b^3 + 16bd^2)}$$

Antiderivative was successfully verified.

[In] Integrate[E^(a + b*x)*Cos[c + d*x]^2*Sin[c + d*x]^2,x]

[Out] (E^(a + b*x)*(b^2 + 16*d^2 - b^2*cos[4*(c + d*x)] - 4*b*d*Sin[4*(c + d*x)])/(8*(b^3 + 16*b*d^2))

fricas [A] time = 0.47, size = 90, normalized size = 1.14

$$\frac{2 \left(2 b d \cos(dx + c)^3 - b d \cos(dx + c) \right) e^{(bx+a)} \sin(dx + c) + \left(b^2 \cos(dx + c)^4 - b^2 \cos(dx + c)^2 - 2 d^2 \right) e^{(bx+a)}}{b^3 + 16 b d^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(b*x+a)*cos(d*x+c)^2*sin(d*x+c)^2,x, algorithm="fricas")

[Out] -(2*(2*b*d*cos(d*x + c)^3 - b*d*cos(d*x + c))*e^(b*x + a)*sin(d*x + c) + (b^2*cos(d*x + c)^4 - b^2*cos(d*x + c)^2 - 2*d^2)*e^(b*x + a))/(b^3 + 16*b*d^2)

giac [A] time = 0.15, size = 66, normalized size = 0.84

$$-\frac{1}{8} \left(\frac{b \cos(4 dx + 4 c)}{b^2 + 16 d^2} + \frac{4 d \sin(4 dx + 4 c)}{b^2 + 16 d^2} \right) e^{(bx+a)} + \frac{e^{(bx+a)}}{8 b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(b*x+a)*cos(d*x+c)^2*sin(d*x+c)^2,x, algorithm="giac")

[Out] -1/8*(b*cos(4*d*x + 4*c)/(b^2 + 16*d^2) + 4*d*sin(4*d*x + 4*c)/(b^2 + 16*d^2))*e^(b*x + a) + 1/8*e^(b*x + a)/b

maple [A] time = 0.12, size = 71, normalized size = 0.90

$$\frac{e^{bx+a}}{8b} - \frac{b e^{bx+a} \cos(4dx + 4c)}{8(b^2 + 16d^2)} - \frac{d e^{bx+a} \sin(4dx + 4c)}{2(b^2 + 16d^2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(exp(b*x+a)*cos(d*x+c)^2*sin(d*x+c)^2,x)

[Out] 1/8*exp(b*x+a)/b-1/8*b*exp(b*x+a)*cos(4*d*x+4*c)/(b^2+16*d^2)-1/2*d*exp(b*x+a)*sin(4*d*x+4*c)/(b^2+16*d^2)

maxima [B] time = 0.35, size = 236, normalized size = 2.99

$$\frac{\left(b^2 \cos(4c) e^a + 4 b d e^a \sin(4c) \right) \cos(4 dx) e^{(bx)} + \left(b^2 \cos(4c) e^a - 4 b d e^a \sin(4c) \right) \cos(4 dx + 8c) e^{(bx)} + \left(4 b d \cos(4c) e^a + 4 b^2 \sin(4c) e^a \right) \sin(4 dx) e^{(bx)} + \left(4 b d \cos(4c) e^a - 4 b^2 \sin(4c) e^a \right) \sin(4 dx + 8c) e^{(bx)}}{8 b (b^2 + 16 d^2)}$$

16

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(b*x+a)*cos(d*x+c)^2*sin(d*x+c)^2,x, algorithm="maxima")

[Out] -1/16*((b^2*cos(4*c)*e^a + 4*b*d*e^a*sin(4*c))*cos(4*d*x)*e^(b*x) + (b^2*cos(4*c)*e^a - 4*b*d*e^a*sin(4*c))*cos(4*d*x + 8*c)*e^(b*x) + (4*b*d*cos(4*c)*e^a - b^2*e^a*sin(4*c))*e^(b*x)*sin(4*d*x) + (4*b*d*cos(4*c)*e^a + b^2*e^a*sin(4*c))*e^(b*x)*sin(4*d*x + 8*c) - 2*(b^2*cos(4*c)^2*e^a + b^2*e^a*sin(4*c)^2 + 16*(cos(4*c)^2*e^a + e^a*sin(4*c)^2)*d^2)*e^(b*x))/(b^3*cos(4*c)^2 + b^3*sin(4*c)^2 + 16*(b*cos(4*c)^2 + b*sin(4*c)^2)*d^2)

mupad [B] time = 0.37, size = 58, normalized size = 0.73

$$\frac{e^{a+bx} \left(b^2 + 16 d^2 - b^2 \cos(4c + 4 dx) - 4 b d \sin(4c + 4 dx) \right)}{8 b (b^2 + 16 d^2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(cos(c + d*x)^2*exp(a + b*x)*sin(c + d*x)^2,x)`

[Out] `(exp(a + b*x)*(b^2 + 16*d^2 - b^2*cos(4*c + 4*d*x) - 4*b*d*sin(4*c + 4*d*x)))/(8*b*(b^2 + 16*d^2))`

sympy [A] time = 94.60, size = 850, normalized size = 10.76

$$\left(\begin{aligned} & x e^a \sin^2(c) \cos^2(c) \\ & \left(\frac{x \sin^4(c+dx)}{8} + \frac{x \sin^2(c+dx) \cos^2(c+dx)}{4} + \frac{x \cos^4(c+dx)}{8} + \frac{\sin^3(c+dx) \cos(c+dx)}{8d} - \frac{\sin(c+dx) \cos^3(c+dx)}{8d} \right) e^a \\ & - \frac{x e^a e^{-4idx} \sin^4(c+dx)}{16} + \frac{i x e^a e^{-4idx} \sin^3(c+dx) \cos(c+dx)}{4} + \frac{3 x e^a e^{-4idx} \sin^2(c+dx) \cos^2(c+dx)}{8} - \frac{i x e^a e^{-4idx} \sin(c+dx) \cos^3(c+dx)}{4} - \frac{x e^a e^{-4idx} \cos^4(c+dx)}{8} \\ & - \frac{x e^a e^{4idx} \sin^4(c+dx)}{16} - \frac{i x e^a e^{4idx} \sin^3(c+dx) \cos(c+dx)}{4} + \frac{3 x e^a e^{4idx} \sin^2(c+dx) \cos^2(c+dx)}{8} + \frac{i x e^a e^{4idx} \sin(c+dx) \cos^3(c+dx)}{4} - \frac{x e^a e^{4idx} \cos^4(c+dx)}{8} \\ & \frac{b^2 e^a e^{bx} \sin^2(c+dx) \cos^2(c+dx)}{b^3+16bd^2} + \frac{2 b d e^a e^{bx} \sin^3(c+dx) \cos(c+dx)}{b^3+16bd^2} - \frac{2 b d e^a e^{bx} \sin(c+dx) \cos^3(c+dx)}{b^3+16bd^2} + \frac{2 d^2 e^a e^{bx} \sin^4(c+dx)}{b^3+16bd^2} + \frac{4 d^2 e^a e^{bx} \sin^2(c+dx) \cos^2(c+dx)}{b^3+16bd^2} \end{aligned} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(exp(b*x+a)*cos(d*x+c)**2*sin(d*x+c)**2,x)`

[Out] `Piecewise((x*exp(a)*sin(c)**2*cos(c)**2, Eq(b, 0) & Eq(d, 0)), ((x*sin(c + d*x)**4/8 + x*sin(c + d*x)**2*cos(c + d*x)**2/4 + x*cos(c + d*x)**4/8 + sin(c + d*x)**3*cos(c + d*x)/(8*d) - sin(c + d*x)*cos(c + d*x)**3/(8*d))*exp(a), Eq(b, 0)), (-x*exp(a)*exp(-4*I*d*x)*sin(c + d*x)**4/16 + I*x*exp(a)*exp(-4*I*d*x)*sin(c + d*x)**3*cos(c + d*x)/4 + 3*x*exp(a)*exp(-4*I*d*x)*sin(c + d*x)**2*cos(c + d*x)**2/8 - I*x*exp(a)*exp(-4*I*d*x)*sin(c + d*x)*cos(c + d*x)**3/4 - x*exp(a)*exp(-4*I*d*x)*cos(c + d*x)**4/16 + I*exp(a)*exp(-4*I*d*x)*sin(c + d*x)**4/(24*d) + 5*exp(a)*exp(-4*I*d*x)*sin(c + d*x)**3*cos(c + d*x)/(48*d) - 5*exp(a)*exp(-4*I*d*x)*sin(c + d*x)*cos(c + d*x)**3/(48*d) + I*exp(a)*exp(-4*I*d*x)*cos(c + d*x)**4/(24*d), Eq(b, -4*I*d)), (-x*exp(a)*exp(4*I*d*x)*sin(c + d*x)**4/16 - I*x*exp(a)*exp(4*I*d*x)*sin(c + d*x)**3*cos(c + d*x)/4 + 3*x*exp(a)*exp(4*I*d*x)*sin(c + d*x)**2*cos(c + d*x)**2/8 + I*x*exp(a)*exp(4*I*d*x)*sin(c + d*x)*cos(c + d*x)**3/4 - x*exp(a)*exp(4*I*d*x)*cos(c + d*x)**4/16 - I*exp(a)*exp(4*I*d*x)*sin(c + d*x)**4/(24*d) + 5*exp(a)*exp(4*I*d*x)*sin(c + d*x)**3*cos(c + d*x)/(48*d) - 5*exp(a)*exp(4*I*d*x)*sin(c + d*x)*cos(c + d*x)**3/(48*d) - I*exp(a)*exp(4*I*d*x)*cos(c + d*x)**4/(24*d), Eq(b, 4*I*d)), (b**2*exp(a)*exp(b*x)*sin(c + d*x)**2*cos(c + d*x)**2/(b**3 + 16*b*d**2) + 2*b*d*exp(a)*exp(b*x)*sin(c + d*x)**3*cos(c + d*x)/(b**3 + 16*b*d**2) - 2*b*d*exp(a)*exp(b*x)*sin(c + d*x)*cos(c + d*x)**3/(b**3 + 16*b*d**2) + 2*d**2*exp(a)*exp(b*x)*sin(c + d*x)**4/(b**3 + 16*b*d**2) + 4*d**2*exp(a)*exp(b*x)*sin(c + d*x)**2*cos(c + d*x)**2/(b**3 + 16*b*d**2) + 2*d**2*exp(a)*exp(b*x)*cos(c + d*x)**4/(b**3 + 16*b*d**2), True))`

3.43 $\int e^{a+bx} \cos^2(c+dx) \sin^3(c+dx) dx$

Optimal. Leaf size=183

$$\frac{be^{a+bx} \sin(c+dx)}{8(b^2+d^2)} + \frac{be^{a+bx} \sin(3c+3dx)}{16(b^2+9d^2)} - \frac{be^{a+bx} \sin(5c+5dx)}{16(b^2+25d^2)} - \frac{de^{a+bx} \cos(c+dx)}{8(b^2+d^2)} - \frac{3de^{a+bx} \cos(3c+3dx)}{16(b^2+9d^2)} + \frac{5de^{a+bx} \cos(5c+5dx)}{16(b^2+25d^2)}$$

[Out] $-1/8*d*\exp(b*x+a)*\cos(d*x+c)/(b^2+d^2)-3/16*d*\exp(b*x+a)*\cos(3*d*x+3*c)/(b^2+9*d^2)+5/16*d*\exp(b*x+a)*\cos(5*d*x+5*c)/(b^2+25*d^2)+1/8*b*\exp(b*x+a)*\sin(d*x+c)/(b^2+d^2)+1/16*b*\exp(b*x+a)*\sin(3*d*x+3*c)/(b^2+9*d^2)-1/16*b*\exp(b*x+a)*\sin(5*d*x+5*c)/(b^2+25*d^2)$

Rubi [A] time = 0.13, antiderivative size = 183, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 2, integrand size = 24, $\frac{\text{number of rules}}{\text{integrand size}} = 0.083$, Rules used = {4469, 4432}

$$\frac{be^{a+bx} \sin(c+dx)}{8(b^2+d^2)} + \frac{be^{a+bx} \sin(3c+3dx)}{16(b^2+9d^2)} - \frac{be^{a+bx} \sin(5c+5dx)}{16(b^2+25d^2)} - \frac{de^{a+bx} \cos(c+dx)}{8(b^2+d^2)} - \frac{3de^{a+bx} \cos(3c+3dx)}{16(b^2+9d^2)} + \frac{5de^{a+bx} \cos(5c+5dx)}{16(b^2+25d^2)}$$

Antiderivative was successfully verified.

[In] Int[E^(a + b*x)*Cos[c + d*x]^2*Sin[c + d*x]^3,x]

[Out] $-(d*E^{(a + b*x)*Cos[c + d*x]})/(8*(b^2 + d^2)) - (3*d*E^{(a + b*x)*Cos[3*c + 3*d*x]})/(16*(b^2 + 9*d^2)) + (5*d*E^{(a + b*x)*Cos[5*c + 5*d*x]})/(16*(b^2 + 25*d^2)) + (b*E^{(a + b*x)*Sin[c + d*x]})/(8*(b^2 + d^2)) + (b*E^{(a + b*x)*Sin[3*c + 3*d*x]})/(16*(b^2 + 9*d^2)) - (b*E^{(a + b*x)*Sin[5*c + 5*d*x]})/(16*(b^2 + 25*d^2))$

Rule 4432

Int[(F_)^((c_.)*((a_.) + (b_.)*(x_)))*Sin[(d_.) + (e_.)*(x_)], x_Symbol] :> Simp[(b*c*Log[F]*F^(c*(a + b*x))*Sin[d + e*x])/(e^2 + b^2*c^2*Log[F]^2), x] - Simp[(e*F^(c*(a + b*x))*Cos[d + e*x])/(e^2 + b^2*c^2*Log[F]^2), x] /; FreeQ[{F, a, b, c, d, e}, x] && NeQ[e^2 + b^2*c^2*Log[F]^2, 0]

Rule 4469

Int[Cos[(f_.) + (g_.)*(x_)]^(n_.)*(F_)^((c_.)*((a_.) + (b_.)*(x_)))*Sin[(d_.) + (e_.)*(x_)]^(m_.), x_Symbol] :> Int[ExpandTrigReduce[F^(c*(a + b*x)), Sin[d + e*x]^m*Cos[f + g*x]^n, x], x] /; FreeQ[{F, a, b, c, d, e, f, g}, x] && IGtQ[m, 0] && IGtQ[n, 0]

Rubi steps

$$\begin{aligned} \int e^{a+bx} \cos^2(c+dx) \sin^3(c+dx) dx &= \int \left(\frac{1}{8} e^{a+bx} \sin(c+dx) + \frac{1}{16} e^{a+bx} \sin(3c+3dx) - \frac{1}{16} e^{a+bx} \sin(5c+5dx) \right) dx \\ &= \frac{1}{16} \int e^{a+bx} \sin(3c+3dx) dx - \frac{1}{16} \int e^{a+bx} \sin(5c+5dx) dx + \frac{1}{8} \int e^{a+bx} \sin(c+dx) dx \\ &= -\frac{de^{a+bx} \cos(c+dx)}{8(b^2+d^2)} - \frac{3de^{a+bx} \cos(3c+3dx)}{16(b^2+9d^2)} + \frac{5de^{a+bx} \cos(5c+5dx)}{16(b^2+25d^2)} + \frac{be^{a+bx} \sin(c+dx)}{8(b^2+d^2)} \end{aligned}$$

Mathematica [A] time = 0.92, size = 110, normalized size = 0.60

$$\frac{1}{16} e^{a+bx} \left(\frac{2(b \sin(c+dx) - d \cos(c+dx))}{b^2+d^2} + \frac{b \sin(3(c+dx)) - 3d \cos(3(c+dx))}{b^2+9d^2} + \frac{5d \cos(5(c+dx)) - b \sin(5(c+dx))}{b^2+25d^2} \right)$$

Antiderivative was successfully verified.

[In] Integrate[E^(a + b*x)*Cos[c + d*x]^2*Sin[c + d*x]^3,x]

[Out] (E^(a + b*x)*((2*(-(d*Cos[c + d*x]) + b*Sin[c + d*x]))/(b^2 + d^2) + (-3*d*Cos[3*(c + d*x)] + b*Sin[3*(c + d*x)])/(b^2 + 9*d^2) + (5*d*Cos[5*(c + d*x)] - b*Sin[5*(c + d*x)])/(b^2 + 25*d^2)))/16

fricas [A] time = 0.57, size = 201, normalized size = 1.10

$$\frac{(2b^3d^2 + 26bd^4 - (b^5 + 10b^3d^2 + 9bd^4)\cos(dx + c)^4 + (b^5 + 14b^3d^2 + 13bd^4)\cos(dx + c)^2)e^{(bx+a)}\sin(dx + c)}{b^6 + 35bd^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(b*x+a)*cos(d*x+c)^2*sin(d*x+c)^3,x, algorithm="fricas")

[Out] ((2*b^3*d^2 + 26*b*d^4 - (b^5 + 10*b^3*d^2 + 9*b*d^4)*cos(d*x + c)^4 + (b^5 + 14*b^3*d^2 + 13*b*d^4)*cos(d*x + c)^2)*e^(b*x + a)*sin(d*x + c) + (5*(b^4*d + 10*b^2*d^3 + 9*d^5)*cos(d*x + c)^5 - (7*b^4*d + 82*b^2*d^3 + 75*d^5)*cos(d*x + c)^3 + 2*(b^4*d + 13*b^2*d^3)*cos(d*x + c))*e^(b*x + a))/(b^6 + 35*b^4*d^2 + 259*b^2*d^4 + 225*d^6)

giac [A] time = 0.15, size = 155, normalized size = 0.85

$$\frac{1}{16} \left(\frac{5d \cos(5dx + 5c)}{b^2 + 25d^2} - \frac{b \sin(5dx + 5c)}{b^2 + 25d^2} \right) e^{(bx+a)} - \frac{1}{16} \left(\frac{3d \cos(3dx + 3c)}{b^2 + 9d^2} - \frac{b \sin(3dx + 3c)}{b^2 + 9d^2} \right) e^{(bx+a)} - \frac{1}{8} \left(\frac{d \cos(dx + c)}{b^2 + d^2} - \frac{b \sin(dx + c)}{b^2 + d^2} \right) e^{(bx+a)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(b*x+a)*cos(d*x+c)^2*sin(d*x+c)^3,x, algorithm="giac")

[Out] 1/16*(5*d*cos(5*d*x + 5*c)/(b^2 + 25*d^2) - b*sin(5*d*x + 5*c)/(b^2 + 25*d^2))*e^(b*x + a) - 1/16*(3*d*cos(3*d*x + 3*c)/(b^2 + 9*d^2) - b*sin(3*d*x + 3*c)/(b^2 + 9*d^2))*e^(b*x + a) - 1/8*(d*cos(d*x + c)/(b^2 + d^2) - b*sin(d*x + c)/(b^2 + d^2))*e^(b*x + a)

maple [A] time = 0.08, size = 166, normalized size = 0.91

$$\frac{d e^{bx+a} \cos(dx + c)}{8(b^2 + d^2)} - \frac{3d e^{bx+a} \cos(3dx + 3c)}{16(b^2 + 9d^2)} + \frac{5d e^{bx+a} \cos(5dx + 5c)}{16(b^2 + 25d^2)} + \frac{b e^{bx+a} \sin(dx + c)}{8b^2 + 8d^2} + \frac{b e^{bx+a} \sin(3dx + 3c)}{16b^2 + 144d^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(exp(b*x+a)*cos(d*x+c)^2*sin(d*x+c)^3,x)

[Out] -1/8*d*exp(b*x+a)*cos(d*x+c)/(b^2+d^2)-3/16*d*exp(b*x+a)*cos(3*d*x+3*c)/(b^2+9*d^2)+5/16*d*exp(b*x+a)*cos(5*d*x+5*c)/(b^2+25*d^2)+1/8*b*exp(b*x+a)*sin(d*x+c)/(b^2+d^2)+1/16*b*exp(b*x+a)*sin(3*d*x+3*c)/(b^2+9*d^2)-1/16*b*exp(b*x+a)*sin(5*d*x+5*c)/(b^2+25*d^2)

maxima [B] time = 0.41, size = 1148, normalized size = 6.27

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(b*x+a)*cos(d*x+c)^2*sin(d*x+c)^3,x, algorithm="maxima")

[Out] 1/32*((5*b^4*d*cos(5*c)*e^a + 50*b^2*d^3*cos(5*c)*e^a + 45*d^5*cos(5*c)*e^a - b^5*e^a*sin(5*c) - 10*b^3*d^2*e^a*sin(5*c) - 9*b*d^4*e^a*sin(5*c))*cos(5*d*x)*e^(b*x) + (5*b^4*d*cos(5*c)*e^a + 50*b^2*d^3*cos(5*c)*e^a + 45*d^5*cos(5*c)*e^a + b^5*e^a*sin(5*c) + 10*b^3*d^2*e^a*sin(5*c) + 9*b*d^4*e^a*sin(5*c))*sin(5*d*x)*e^(b*x)

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*c))*cos(5*d*x + 10*c)*e^(b*x) - (3*b^4*d*cos(5*c)*e^a + 78*b^2*d^3*cos(5*c)
)*e^a + 75*d^5*cos(5*c)*e^a + b^5*e^a*sin(5*c) + 26*b^3*d^2*e^a*sin(5*c) +
25*b*d^4*e^a*sin(5*c))*cos(3*d*x + 8*c)*e^(b*x) - (3*b^4*d*cos(5*c)*e^a + 7
8*b^2*d^3*cos(5*c)*e^a + 75*d^5*cos(5*c)*e^a - b^5*e^a*sin(5*c) - 26*b^3*d^
2*e^a*sin(5*c) - 25*b*d^4*e^a*sin(5*c))*cos(3*d*x - 2*c)*e^(b*x) - 2*(b^4*d
*cos(5*c)*e^a + 34*b^2*d^3*cos(5*c)*e^a + 225*d^5*cos(5*c)*e^a + b^5*e^a*si
n(5*c) + 34*b^3*d^2*e^a*sin(5*c) + 225*b*d^4*e^a*sin(5*c))*cos(d*x + 6*c)*e
^(b*x) - 2*(b^4*d*cos(5*c)*e^a + 34*b^2*d^3*cos(5*c)*e^a + 225*d^5*cos(5*c)
*e^a - b^5*e^a*sin(5*c) - 34*b^3*d^2*e^a*sin(5*c) - 225*b*d^4*e^a*sin(5*c))
*cos(d*x - 4*c)*e^(b*x) - (b^5*cos(5*c)*e^a + 10*b^3*d^2*cos(5*c)*e^a + 9*b
*d^4*cos(5*c)*e^a + 5*b^4*d*e^a*sin(5*c) + 50*b^2*d^3*e^a*sin(5*c) + 45*d^5
*e^a*sin(5*c))*e^(b*x)*sin(5*d*x) - (b^5*cos(5*c)*e^a + 10*b^3*d^2*cos(5*c)
*e^a + 9*b*d^4*cos(5*c)*e^a - 5*b^4*d*e^a*sin(5*c) - 50*b^2*d^3*e^a*sin(5*c)
) - 45*d^5*e^a*sin(5*c))*e^(b*x)*sin(5*d*x + 10*c) + (b^5*cos(5*c)*e^a + 26
*b^3*d^2*cos(5*c)*e^a + 25*b*d^4*cos(5*c)*e^a - 3*b^4*d*e^a*sin(5*c) - 78*b
^2*d^3*e^a*sin(5*c) - 75*d^5*e^a*sin(5*c))*e^(b*x)*sin(3*d*x + 8*c) + (b^5*
cos(5*c)*e^a + 26*b^3*d^2*cos(5*c)*e^a + 25*b*d^4*cos(5*c)*e^a + 3*b^4*d*e^
a*sin(5*c) + 78*b^2*d^3*e^a*sin(5*c) + 75*d^5*e^a*sin(5*c))*e^(b*x)*sin(3*d
*x - 2*c) + 2*(b^5*cos(5*c)*e^a + 34*b^3*d^2*cos(5*c)*e^a + 225*b*d^4*cos(5
*c)*e^a - b^4*d*e^a*sin(5*c) - 34*b^2*d^3*e^a*sin(5*c) - 225*d^5*e^a*sin(5*
c))*e^(b*x)*sin(d*x + 6*c) + 2*(b^5*cos(5*c)*e^a + 34*b^3*d^2*cos(5*c)*e^a
+ 225*b*d^4*cos(5*c)*e^a + b^4*d*e^a*sin(5*c) + 34*b^2*d^3*e^a*sin(5*c) + 2
25*d^5*e^a*sin(5*c))*e^(b*x)*sin(d*x - 4*c))/(b^6*cos(5*c)^2 + b^6*sin(5*c)
^2 + 225*(cos(5*c)^2 + sin(5*c)^2)*d^6 + 259*(b^2*cos(5*c)^2 + b^2*sin(5*c)
^2)*d^4 + 35*(b^4*cos(5*c)^2 + b^4*sin(5*c)^2)*d^2)

```

mupad [B] time = 3.74, size = 255, normalized size = 1.39

$$\frac{e^{a+bx} (\cos(dx) - \sin(dx) 1i) (\cos(c) - \sin(c) 1i)}{16 (d + b 1i)} - \frac{e^{a+bx} (\cos(dx) + \sin(dx) 1i) (\cos(c) + \sin(c) 1i) 1i}{16 (b + d 1i)} - \frac{e^{a+bx}}{16 (b + d 1i)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(cos(c + d*x)^2*exp(a + b*x)*sin(c + d*x)^3,x)

[Out] (exp(a + b*x)*(cos(5*d*x) - sin(5*d*x)*1i)*(cos(5*c) - sin(5*c)*1i))/(32*(b*1i + 5*d)) - (exp(a + b*x)*(cos(d*x) + sin(d*x)*1i)*(cos(c) + sin(c)*1i)*1i)/(16*(b + d*1i)) - (exp(a + b*x)*(cos(3*d*x) - sin(3*d*x)*1i)*(cos(3*c) - sin(3*c)*1i))/(32*(b*1i + 3*d)) - (exp(a + b*x)*(cos(d*x) - sin(d*x)*1i)*(cos(c) - sin(c)*1i))/(16*(b*1i + d)) - (exp(a + b*x)*(cos(3*d*x) + sin(3*d*x)*1i)*(cos(3*c) + sin(3*c)*1i)*1i)/(32*(b + d*3i)) + (exp(a + b*x)*(cos(5*d*x) + sin(5*d*x)*1i)*(cos(5*c) + sin(5*c)*1i)*1i)/(32*(b + d*5i))

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(b*x+a)*cos(d*x+c)**2*sin(d*x+c)**3,x)

[Out] Timed out

3.44 $\int e^{a+bx} \cos^3(c+dx) \sin(c+dx) dx$

Optimal. Leaf size=129

$$\frac{be^{a+bx} \sin(2c+2dx)}{4(b^2+4d^2)} + \frac{be^{a+bx} \sin(4c+4dx)}{8(b^2+16d^2)} - \frac{de^{a+bx} \cos(2c+2dx)}{2(b^2+4d^2)} - \frac{de^{a+bx} \cos(4c+4dx)}{2(b^2+16d^2)}$$

[Out] $-1/2*d*\exp(b*x+a)*\cos(2*d*x+2*c)/(b^2+4*d^2)-1/2*d*\exp(b*x+a)*\cos(4*d*x+4*c)/(b^2+16*d^2)+1/4*b*\exp(b*x+a)*\sin(2*d*x+2*c)/(b^2+4*d^2)+1/8*b*\exp(b*x+a)*\sin(4*d*x+4*c)/(b^2+16*d^2)$

Rubi [A] time = 0.09, antiderivative size = 129, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 2, integrand size = 22, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {4469, 4432}

$$\frac{be^{a+bx} \sin(2c+2dx)}{4(b^2+4d^2)} + \frac{be^{a+bx} \sin(4c+4dx)}{8(b^2+16d^2)} - \frac{de^{a+bx} \cos(2c+2dx)}{2(b^2+4d^2)} - \frac{de^{a+bx} \cos(4c+4dx)}{2(b^2+16d^2)}$$

Antiderivative was successfully verified.

[In] $\text{Int}[E^{(a+bx)}*\text{Cos}[c+dx]^3*\text{Sin}[c+dx], x]$

[Out] $-(d*E^{(a+bx)}*\text{Cos}[2*c+2*d*x])/(2*(b^2+4*d^2)) - (d*E^{(a+bx)}*\text{Cos}[4*c+4*d*x])/(2*(b^2+16*d^2)) + (b*E^{(a+bx)}*\text{Sin}[2*c+2*d*x])/(4*(b^2+4*d^2)) + (b*E^{(a+bx)}*\text{Sin}[4*c+4*d*x])/(8*(b^2+16*d^2))$

Rule 4432

$\text{Int}[(F_)^{((c_.)*((a_.)+(b_.)*(x_)))}*\text{Sin}[(d_.)+(e_.)*(x_)], x_Symbol] := \text{Simp}[(b*c*\text{Log}[F]*F^{(c*(a+bx))}*\text{Sin}[d+e*x])/(e^2+b^2*c^2*\text{Log}[F]^2), x] - \text{Simp}[(e*F^{(c*(a+bx))}*\text{Cos}[d+e*x])/(e^2+b^2*c^2*\text{Log}[F]^2), x] /;$ FreeQ[{F, a, b, c, d, e}, x] && NeQ[e^2+b^2*c^2*Log[F]^2, 0]

Rule 4469

$\text{Int}[\text{Cos}[(f_.)+(g_.)*(x_)]^{(n_.)}*(F_)^{((c_.)*((a_.)+(b_.)*(x_)))}*\text{Sin}[(d_.)+(e_.)*(x_)]^{(m_.)}, x_Symbol] := \text{Int}[\text{ExpandTrigReduce}[F^{(c*(a+bx))}, \text{Sin}[d+e*x]^m*\text{Cos}[f+g*x]^n, x], x] /;$ FreeQ[{F, a, b, c, d, e, f, g}, x] && IGtQ[m, 0] && IGtQ[n, 0]

Rubi steps

$$\begin{aligned} \int e^{a+bx} \cos^3(c+dx) \sin(c+dx) dx &= \int \left(\frac{1}{4} e^{a+bx} \sin(2c+2dx) + \frac{1}{8} e^{a+bx} \sin(4c+4dx) \right) dx \\ &= \frac{1}{8} \int e^{a+bx} \sin(4c+4dx) dx + \frac{1}{4} \int e^{a+bx} \sin(2c+2dx) dx \\ &= -\frac{de^{a+bx} \cos(2c+2dx)}{2(b^2+4d^2)} - \frac{de^{a+bx} \cos(4c+4dx)}{2(b^2+16d^2)} + \frac{be^{a+bx} \sin(2c+2dx)}{4(b^2+4d^2)} + \end{aligned}$$

Mathematica [A] time = 0.68, size = 81, normalized size = 0.63

$$\frac{1}{8} e^{a+bx} \left(\frac{2(b \sin(2(c+dx)) - 2d \cos(2(c+dx)))}{b^2+4d^2} + \frac{b \sin(4(c+dx)) - 4d \cos(4(c+dx))}{b^2+16d^2} \right)$$

Antiderivative was successfully verified.

[In] Integrate[E^(a + b*x)*Cos[c + d*x]^3*Sin[c + d*x],x]

[Out] (E^(a + b*x)*((2*(-2*d*Cos[2*(c + d*x)] + b*Sin[2*(c + d*x)]))/(b^2 + 4*d^2) + (-4*d*Cos[4*(c + d*x)] + b*Sin[4*(c + d*x)]/(b^2 + 16*d^2)))/8

fricas [A] time = 0.58, size = 114, normalized size = 0.88

$$\frac{(6bd^2 \cos(dx + c) + (b^3 + 4bd^2) \cos(dx + c)^3) e^{(bx+a)} \sin(dx + c) + (3b^2d \cos(dx + c)^2 - 4(b^2d + 4d^3) \cos(dx + c)) e^{(bx+a)}}{b^4 + 20b^2d^2 + 64d^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(b*x+a)*cos(d*x+c)^3*sin(d*x+c),x, algorithm="fricas")

[Out] ((6*b*d^2*cos(d*x + c) + (b^3 + 4*b*d^2)*cos(d*x + c)^3)*e^(b*x + a)*sin(d*x + c) + (3*b^2*d*cos(d*x + c)^2 - 4*(b^2*d + 4*d^3)*cos(d*x + c)^4 + 6*d^3)*e^(b*x + a))/(b^4 + 20*b^2*d^2 + 64*d^4)

giac [A] time = 0.13, size = 111, normalized size = 0.86

$$\frac{1}{8} \left(\frac{4d \cos(4dx + 4c)}{b^2 + 16d^2} - \frac{b \sin(4dx + 4c)}{b^2 + 16d^2} \right) e^{(bx+a)} - \frac{1}{4} \left(\frac{2d \cos(2dx + 2c)}{b^2 + 4d^2} - \frac{b \sin(2dx + 2c)}{b^2 + 4d^2} \right) e^{(bx+a)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(b*x+a)*cos(d*x+c)^3*sin(d*x+c),x, algorithm="giac")

[Out] -1/8*(4*d*cos(4*d*x + 4*c)/(b^2 + 16*d^2) - b*sin(4*d*x + 4*c)/(b^2 + 16*d^2))*e^(b*x + a) - 1/4*(2*d*cos(2*d*x + 2*c)/(b^2 + 4*d^2) - b*sin(2*d*x + 2*c)/(b^2 + 4*d^2))*e^(b*x + a)

maple [A] time = 0.09, size = 118, normalized size = 0.91

$$\frac{d e^{bx+a} \cos(2dx + 2c)}{2(b^2 + 4d^2)} - \frac{d e^{bx+a} \cos(4dx + 4c)}{2(b^2 + 16d^2)} + \frac{b e^{bx+a} \sin(2dx + 2c)}{4b^2 + 16d^2} + \frac{b e^{bx+a} \sin(4dx + 4c)}{8b^2 + 128d^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(exp(b*x+a)*cos(d*x+c)^3*sin(d*x+c),x)

[Out] -1/2*d*exp(b*x+a)*cos(2*d*x+2*c)/(b^2+4*d^2)-1/2*d*exp(b*x+a)*cos(4*d*x+4*c)/(b^2+16*d^2)+1/4*b*exp(b*x+a)*sin(2*d*x+2*c)/(b^2+4*d^2)+1/8*b*exp(b*x+a)*sin(4*d*x+4*c)/(b^2+16*d^2)

maxima [B] time = 0.35, size = 550, normalized size = 4.26

$$\frac{(4b^2d \cos(4c) e^a + 16d^3 \cos(4c) e^a - b^3 e^a \sin(4c) - 4bd^2 e^a \sin(4c)) \cos(4dx) e^{(bx)} + (4b^2d \cos(4c) e^a + 16d^3 \cos(4c) e^a - b^3 e^a \sin(4c) - 4bd^2 e^a \sin(4c)) \sin(4dx) e^{(bx)}}{b^4 + 20b^2d^2 + 64d^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(b*x+a)*cos(d*x+c)^3*sin(d*x+c),x, algorithm="maxima")

[Out] -1/16*((4*b^2*d*cos(4*c)*e^a + 16*d^3*cos(4*c)*e^a - b^3*e^a*sin(4*c) - 4*b*d^2*e^a*sin(4*c))*cos(4*d*x)*e^(b*x) + (4*b^2*d*cos(4*c)*e^a + 16*d^3*cos(4*c)*e^a + b^3*e^a*sin(4*c) + 4*b*d^2*e^a*sin(4*c))*cos(4*d*x + 8*c)*e^(b*x) + 2*(2*b^2*d*cos(4*c)*e^a + 32*d^3*cos(4*c)*e^a + b^3*e^a*sin(4*c) + 16*b*d^2*e^a*sin(4*c))*cos(2*d*x + 6*c)*e^(b*x) + 2*(2*b^2*d*cos(4*c)*e^a + 32*d^3*cos(4*c)*e^a - b^3*e^a*sin(4*c) - 16*b*d^2*e^a*sin(4*c))*cos(2*d*x - 2*c)*e^(b*x) - (b^3*cos(4*c)*e^a + 4*b*d^2*cos(4*c)*e^a + 4*b^2*d*e^a*sin(4*c) + 16*d^3*e^a*sin(4*c))*e^(b*x)*sin(4*d*x) - (b^3*cos(4*c)*e^a + 4*b*d^2*cos(4*c)*e^a - 4*b^2*d*e^a*sin(4*c) - 16*d^3*e^a*sin(4*c))*e^(b*x)*sin(4*d*x)

$$+ 8*c) - 2*(b^3*\cos(4*c)*e^a + 16*b*d^2*\cos(4*c)*e^a - 2*b^2*d*e^a*\sin(4*c) - 32*d^3*e^a*\sin(4*c))*e^{(b*x)*\sin(2*d*x + 6*c)} - 2*(b^3*\cos(4*c)*e^a + 16*b*d^2*\cos(4*c)*e^a + 2*b^2*d*e^a*\sin(4*c) + 32*d^3*e^a*\sin(4*c))*e^{(b*x)*\sin(2*d*x - 2*c)}/(b^4*\cos(4*c)^2 + b^4*\sin(4*c)^2 + 64*(\cos(4*c)^2 + \sin(4*c)^2)*d^4 + 20*(b^2*\cos(4*c)^2 + b^2*\sin(4*c)^2)*d^2)$$

mupad [B] time = 0.82, size = 179, normalized size = 1.39

$$\frac{e^{a+bx} (\cos(2dx) - \sin(2dx) 1i) (\cos(2c) - \sin(2c) 1i)}{8(2d + b1i)} - \frac{e^{a+bx} (\cos(4dx) - \sin(4dx) 1i) (\cos(4c) - \sin(4c) 1i)}{16(4d + b1i)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(cos(c + d*x)^3*exp(a + b*x)*sin(c + d*x),x)

[Out] - (exp(a + b*x)*(cos(2*d*x) - sin(2*d*x)*1i)*(cos(2*c) - sin(2*c)*1i))/(8*(b*1i + 2*d)) - (exp(a + b*x)*(cos(4*d*x) - sin(4*d*x)*1i)*(cos(4*c) - sin(4*c)*1i))/(16*(b*1i + 4*d)) - (exp(a + b*x)*(cos(2*d*x) + sin(2*d*x)*1i)*(cos(2*c) + sin(2*c)*1i)*1i)/(8*(b + d*2i)) - (exp(a + b*x)*(cos(4*d*x) + sin(4*d*x)*1i)*(cos(4*c) + sin(4*c)*1i)*1i)/(16*(b + d*4i))

sympy [A] time = 146.90, size = 1357, normalized size = 10.52

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(b*x+a)*cos(d*x+c)**3*sin(d*x+c),x)

[Out] Piecewise((x*exp(a)*sin(c)*cos(c)**3, Eq(b, 0) & Eq(d, 0)), (-I*x*exp(a)*exp(-4*I*d*x)*sin(c + d*x)**4/16 - x*exp(a)*exp(-4*I*d*x)*sin(c + d*x)**3*cos(c + d*x)/4 + 3*I*x*exp(a)*exp(-4*I*d*x)*sin(c + d*x)**2*cos(c + d*x)**2/8 + x*exp(a)*exp(-4*I*d*x)*sin(c + d*x)*cos(c + d*x)**3/4 - I*x*exp(a)*exp(-4*I*d*x)*cos(c + d*x)**4/16 - exp(a)*exp(-4*I*d*x)*sin(c + d*x)**4/(24*d) + 5*I*exp(a)*exp(-4*I*d*x)*sin(c + d*x)**3*cos(c + d*x)/(48*d) + 11*I*exp(a)*exp(-4*I*d*x)*sin(c + d*x)*cos(c + d*x)**3/(48*d) + exp(a)*exp(-4*I*d*x)*cos(c + d*x)**4/(24*d), Eq(b, -4*I*d)), (I*x*exp(a)*exp(-2*I*d*x)*sin(c + d*x)**4/8 + x*exp(a)*exp(-2*I*d*x)*sin(c + d*x)**3*cos(c + d*x)/4 + x*exp(a)*exp(-2*I*d*x)*sin(c + d*x)*cos(c + d*x)**3/4 - I*x*exp(a)*exp(-2*I*d*x)*cos(c + d*x)**4/8 + exp(a)*exp(-2*I*d*x)*sin(c + d*x)**4/(16*d) + exp(a)*exp(-2*I*d*x)*sin(c + d*x)**2*cos(c + d*x)**2/(4*d) - I*exp(a)*exp(-2*I*d*x)*sin(c + d*x)*cos(c + d*x)**3/(6*d) - 7*exp(a)*exp(-2*I*d*x)*cos(c + d*x)**4/(48*d), Eq(b, -2*I*d)), (-I*x*exp(a)*exp(2*I*d*x)*sin(c + d*x)**4/8 + x*exp(a)*exp(2*I*d*x)*sin(c + d*x)**3*cos(c + d*x)/4 + x*exp(a)*exp(2*I*d*x)*sin(c + d*x)*cos(c + d*x)**3/4 + I*x*exp(a)*exp(2*I*d*x)*cos(c + d*x)**4/8 + exp(a)*exp(2*I*d*x)*sin(c + d*x)**4/(16*d) + exp(a)*exp(2*I*d*x)*sin(c + d*x)**2*cos(c + d*x)**2/(4*d) + I*exp(a)*exp(2*I*d*x)*sin(c + d*x)*cos(c + d*x)**3/(6*d) - 7*exp(a)*exp(2*I*d*x)*cos(c + d*x)**4/(48*d), Eq(b, 2*I*d)), (I*x*exp(a)*exp(4*I*d*x)*sin(c + d*x)**4/16 - x*exp(a)*exp(4*I*d*x)*sin(c + d*x)**3*cos(c + d*x)/4 - 3*I*x*exp(a)*exp(4*I*d*x)*sin(c + d*x)**2*cos(c + d*x)**2/8 + x*exp(a)*exp(4*I*d*x)*sin(c + d*x)*cos(c + d*x)**3/4 + I*x*exp(a)*exp(4*I*d*x)*cos(c + d*x)**4/16 - exp(a)*exp(4*I*d*x)*sin(c + d*x)**4/(24*d) - 5*I*exp(a)*exp(4*I*d*x)*sin(c + d*x)**3*cos(c + d*x)/(48*d) - 11*I*exp(a)*exp(4*I*d*x)*sin(c + d*x)*cos(c + d*x)**3/(48*d) + exp(a)*exp(4*I*d*x)*cos(c + d*x)**4/(24*d), Eq(b, 4*I*d)), (b**3*exp(a)*exp(b*x)*sin(c + d*x)*cos(c + d*x)**3/(b**4 + 20*b**2*d**2 + 64*d**4) + 3*b**2*d*exp(a)*exp(b*x)*sin(c + d*x)**2*cos(c + d*x)**2/(b**4 + 20*b**2*d**2 + 64*d**4) - b**2*d*exp(a)*exp(b*x)*cos(c + d*x)**4/(b**4 + 20*b**2*d**2 + 64*d**4) + 6*b*d**2*exp(a)*exp(b*x)*sin(c + d*x)**3*cos(c + d*x)/(b**4 + 20*b**2*d**2 + 64*d**4) + 10*b*d**2*exp(a)*exp(b*x)*sin(c + d*x)*cos(c + d*x)**3/(b**4 + 20*b**2*d**2 + 64*d**4) + 6*d**3*exp(a)*exp(b*x)*sin(c + d*x)**4/(b**4 + 20*b**2*d**2 +

```
64*d**4) + 12*d**3*exp(a)*exp(b*x)*sin(c + d*x)**2*cos(c + d*x)**2/(b**4 +
20*b**2*d**2 + 64*d**4) - 10*d**3*exp(a)*exp(b*x)*cos(c + d*x)**4/(b**4 +
20*b**2*d**2 + 64*d**4), True))
```


3.45 $\int e^{a+bx} \cos^3(c+dx) \sin^2(c+dx) dx$

Optimal. Leaf size=183

$$\frac{de^{a+bx} \sin(c+dx)}{8(b^2+d^2)} - \frac{3de^{a+bx} \sin(3c+3dx)}{16(b^2+9d^2)} - \frac{5de^{a+bx} \sin(5c+5dx)}{16(b^2+25d^2)} + \frac{be^{a+bx} \cos(c+dx)}{8(b^2+d^2)} - \frac{be^{a+bx} \cos(3c+3dx)}{16(b^2+9d^2)}$$

[Out] $1/8*b*\exp(b*x+a)*\cos(d*x+c)/(b^2+d^2)-1/16*b*\exp(b*x+a)*\cos(3*d*x+3*c)/(b^2+9*d^2)-1/16*b*\exp(b*x+a)*\cos(5*d*x+5*c)/(b^2+25*d^2)+1/8*d*\exp(b*x+a)*\sin(d*x+c)/(b^2+d^2)-3/16*d*\exp(b*x+a)*\sin(3*d*x+3*c)/(b^2+9*d^2)-5/16*d*\exp(b*x+a)*\sin(5*d*x+5*c)/(b^2+25*d^2)$

Rubi [A] time = 0.13, antiderivative size = 183, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 2, integrand size = 24, $\frac{\text{number of rules}}{\text{integrand size}} = 0.083$, Rules used = {4469, 4433}

$$\frac{de^{a+bx} \sin(c+dx)}{8(b^2+d^2)} - \frac{3de^{a+bx} \sin(3c+3dx)}{16(b^2+9d^2)} - \frac{5de^{a+bx} \sin(5c+5dx)}{16(b^2+25d^2)} + \frac{be^{a+bx} \cos(c+dx)}{8(b^2+d^2)} - \frac{be^{a+bx} \cos(3c+3dx)}{16(b^2+9d^2)}$$

Antiderivative was successfully verified.

[In] Int[E^(a + b*x)*Cos[c + d*x]^3*Sin[c + d*x]^2, x]

[Out] $(b*E^{(a + b*x)*Cos[c + d*x]})/(8*(b^2 + d^2)) - (b*E^{(a + b*x)*Cos[3*c + 3*d*x]})/(16*(b^2 + 9*d^2)) - (b*E^{(a + b*x)*Cos[5*c + 5*d*x]})/(16*(b^2 + 25*d^2)) + (d*E^{(a + b*x)*Sin[c + d*x]})/(8*(b^2 + d^2)) - (3*d*E^{(a + b*x)*Sin[3*c + 3*d*x]})/(16*(b^2 + 9*d^2)) - (5*d*E^{(a + b*x)*Sin[5*c + 5*d*x]})/(16*(b^2 + 25*d^2))$

Rule 4433

Int[Cos[(d_.) + (e_.)*(x_.)]*(F_)^((c_.)*((a_.) + (b_.)*(x_.))), x_Symbol] :=
Simp[(b*c*Log[F]*F^(c*(a + b*x))*Cos[d + e*x]/(e^2 + b^2*c^2*Log[F]^2), x]
+ Simp[(e*F^(c*(a + b*x))*Sin[d + e*x]/(e^2 + b^2*c^2*Log[F]^2), x] /; FreeQ[{F, a, b, c, d, e}, x] && NeQ[e^2 + b^2*c^2*Log[F]^2, 0]

Rule 4469

Int[Cos[(f_.) + (g_.)*(x_.)]^(n_.)*(F_)^((c_.)*((a_.) + (b_.)*(x_.)))*Sin[(d_.) + (e_.)*(x_.)]^(m_.), x_Symbol] := Int[ExpandTrigReduce[F^(c*(a + b*x)), Sin[d + e*x]^m*Cos[f + g*x]^n, x] /; FreeQ[{F, a, b, c, d, e, f, g}, x] && IGtQ[m, 0] && IGtQ[n, 0]

Rubi steps

$$\begin{aligned} \int e^{a+bx} \cos^3(c+dx) \sin^2(c+dx) dx &= \int \left(\frac{1}{8} e^{a+bx} \cos(c+dx) - \frac{1}{16} e^{a+bx} \cos(3c+3dx) - \frac{1}{16} e^{a+bx} \cos(5c+5dx) \right) dx \\ &= - \left(\frac{1}{16} \int e^{a+bx} \cos(3c+3dx) dx \right) - \frac{1}{16} \int e^{a+bx} \cos(5c+5dx) dx + \frac{1}{8} \int e^{a+bx} \cos(c+dx) dx \\ &= \frac{be^{a+bx} \cos(c+dx)}{8(b^2+d^2)} - \frac{be^{a+bx} \cos(3c+3dx)}{16(b^2+9d^2)} - \frac{be^{a+bx} \cos(5c+5dx)}{16(b^2+25d^2)} + \frac{de^{a+bx} \sin(c+dx)}{8(b^2+d^2)} \end{aligned}$$

Mathematica [A] time = 0.78, size = 110, normalized size = 0.60

$$\frac{1}{16} e^{a+bx} \left(\frac{2(b \cos(c+dx) + d \sin(c+dx))}{b^2+d^2} - \frac{b \cos(3(c+dx)) + 3d \sin(3(c+dx))}{b^2+9d^2} - \frac{b \cos(5(c+dx)) + 5d \sin(5(c+dx))}{b^2+25d^2} \right) + \frac{1}{8} e^{a+bx} \sin(c+dx)$$

Antiderivative was successfully verified.

[In] Integrate[E^(a + b*x)*Cos[c + d*x]^3*Sin[c + d*x]^2,x]

[Out] (E^(a + b*x)*((2*(b*Cos[c + d*x] + d*Sin[c + d*x]))/(b^2 + d^2) - (b*Cos[3*(c + d*x)] + 3*d*Sin[3*(c + d*x)])/(b^2 + 9*d^2) - (b*Cos[5*(c + d*x)] + 5*d*Sin[5*(c + d*x)])/(b^2 + 25*d^2)))/16

fricas [A] time = 0.66, size = 200, normalized size = 1.09

$$\frac{(6b^2d^3 + 30d^5 - 5(b^4d + 10b^2d^3 + 9d^5))\cos(dx + c)^4 + 3(b^4d + 6b^2d^3 + 5d^5)\cos(dx + c)^2}{b^6 + 35b^4d^2 + 25b^2d^4 + d^6} e^{(bx+a)} \sin(dx + c)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(b*x+a)*cos(d*x+c)^3*sin(d*x+c)^2,x, algorithm="fricas")

[Out] ((6*b^2*d^3 + 30*d^5 - 5*(b^4*d + 10*b^2*d^3 + 9*d^5)*cos(d*x + c)^4 + 3*(b^4*d + 6*b^2*d^3 + 5*d^5)*cos(d*x + c)^2)*e^(b*x + a)*sin(d*x + c) - ((b^5 + 10*b^3*d^2 + 9*b*d^4)*cos(d*x + c)^5 - (b^5 + 6*b^3*d^2 + 5*b*d^4)*cos(d*x + c)^3 - 6*(b^3*d^2 + 5*b*d^4)*cos(d*x + c))*e^(b*x + a))/(b^6 + 35*b^4*d^2 + 25*b^2*d^4 + 225*d^6)

giac [A] time = 0.16, size = 152, normalized size = 0.83

$$-\frac{1}{16} \left(\frac{b \cos(5dx + 5c)}{b^2 + 25d^2} + \frac{5d \sin(5dx + 5c)}{b^2 + 25d^2} \right) e^{(bx+a)} - \frac{1}{16} \left(\frac{b \cos(3dx + 3c)}{b^2 + 9d^2} + \frac{3d \sin(3dx + 3c)}{b^2 + 9d^2} \right) e^{(bx+a)} + \frac{1}{8} \left(\frac{b \cos(dx + c)}{b^2 + d^2} + \frac{d \sin(dx + c)}{b^2 + d^2} \right) e^{(bx+a)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(b*x+a)*cos(d*x+c)^3*sin(d*x+c)^2,x, algorithm="giac")

[Out] -1/16*(b*cos(5*d*x + 5*c)/(b^2 + 25*d^2) + 5*d*sin(5*d*x + 5*c)/(b^2 + 25*d^2))*e^(b*x + a) - 1/16*(b*cos(3*d*x + 3*c)/(b^2 + 9*d^2) + 3*d*sin(3*d*x + 3*c)/(b^2 + 9*d^2))*e^(b*x + a) + 1/8*(b*cos(d*x + c)/(b^2 + d^2) + d*sin(d*x + c)/(b^2 + d^2))*e^(b*x + a)

maple [A] time = 0.14, size = 166, normalized size = 0.91

$$\frac{b e^{bx+a} \cos(dx + c)}{8b^2 + 8d^2} - \frac{b e^{bx+a} \cos(3dx + 3c)}{16(b^2 + 9d^2)} - \frac{b e^{bx+a} \cos(5dx + 5c)}{16(b^2 + 25d^2)} + \frac{d e^{bx+a} \sin(dx + c)}{8b^2 + 8d^2} - \frac{3d e^{bx+a} \sin(3dx + 3c)}{16(b^2 + 9d^2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(exp(b*x+a)*cos(d*x+c)^3*sin(d*x+c)^2,x)

[Out] 1/8*b*exp(b*x+a)*cos(d*x+c)/(b^2+d^2)-1/16*b*exp(b*x+a)*cos(3*d*x+3*c)/(b^2+9*d^2)-1/16*b*exp(b*x+a)*cos(5*d*x+5*c)/(b^2+25*d^2)+1/8*d*exp(b*x+a)*sin(d*x+c)/(b^2+d^2)-3/16*d*exp(b*x+a)*sin(3*d*x+3*c)/(b^2+9*d^2)-5/16*d*exp(b*x+a)*sin(5*d*x+5*c)/(b^2+25*d^2)

maxima [B] time = 0.39, size = 1144, normalized size = 6.25

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(b*x+a)*cos(d*x+c)^3*sin(d*x+c)^2,x, algorithm="maxima")

[Out] -1/32*((b^5*cos(5*c)*e^a + 10*b^3*d^2*cos(5*c)*e^a + 9*b*d^4*cos(5*c)*e^a + 5*b^4*d*e^a*sin(5*c) + 50*b^2*d^3*e^a*sin(5*c) + 45*d^5*e^a*sin(5*c))*cos(5*d*x)*e^(b*x) + (b^5*cos(5*c)*e^a + 10*b^3*d^2*cos(5*c)*e^a + 9*b*d^4*cos(5*c)*e^a - 5*b^4*d*e^a*sin(5*c) - 50*b^2*d^3*e^a*sin(5*c) - 45*d^5*e^a*sin(5*c))*sin(5*d*x)*e^(b*x) - (b^5*cos(5*c)*e^a + 10*b^3*d^2*cos(5*c)*e^a + 9*b*d^4*cos(5*c)*e^a + 5*b^4*d*e^a*sin(5*c) + 50*b^2*d^3*e^a*sin(5*c) + 45*d^5*e^a*sin(5*c))*cos(dx + c)*e^(bx+a) - (b^5*cos(3*d*x + 3*c)*e^(bx+a) + 3*d*sin(3*d*x + 3*c)*e^(bx+a) - (b^5*cos(dx + c)*e^(bx+a) + d*sin(dx + c)*e^(bx+a)))/(b^6 + 35*b^4*d^2 + 25*b^2*d^4 + 225*d^6)

$$\begin{aligned}
& 5*c)) * \cos(5*d*x + 10*c) * e^{(b*x)} + (b^5 * \cos(5*c) * e^a + 26*b^3*d^2 * \cos(5*c) * e^a \\
& + 25*b*d^4 * \cos(5*c) * e^a - 3*b^4*d * e^a * \sin(5*c) - 78*b^2*d^3 * e^a * \sin(5*c) \\
& - 75*d^5 * e^a * \sin(5*c)) * \cos(3*d*x + 8*c) * e^{(b*x)} + (b^5 * \cos(5*c) * e^a + 26*b^3*d^2 * \cos(5*c) * e^a \\
& + 25*b*d^4 * \cos(5*c) * e^a + 3*b^4*d * e^a * \sin(5*c) + 78*b^2*d^3 * e^a * \sin(5*c) + 75*d^5 * e^a * \sin(5*c)) * \cos(3*d*x - 2*c) * e^{(b*x)} \\
& - 2*(b^5 * \cos(5*c) * e^a + 34*b^3*d^2 * \cos(5*c) * e^a + 225*b*d^4 * \cos(5*c) * e^a - b^4*d * e^a * \sin(5*c) \\
& - 34*b^2*d^3 * e^a * \sin(5*c) - 225*d^5 * e^a * \sin(5*c)) * \cos(d*x + 6*c) * e^{(b*x)} - 2*(b^5 * \cos(5*c) * e^a + 34*b^3*d^2 * \cos(5*c) * e^a \\
& + 225*b*d^4 * \cos(5*c) * e^a + b^4*d * e^a * \sin(5*c) + 34*b^2*d^3 * e^a * \sin(5*c) + 225*d^5 * e^a * \sin(5*c)) * \cos(d*x - 4*c) * e^{(b*x)} \\
& + (5*b^4*d * \cos(5*c) * e^a + 50*b^2*d^3 * \cos(5*c) * e^a + 45*d^5 * \cos(5*c) * e^a - b^5 * e^a * \sin(5*c) - 10*b^3*d^2 * e^a * \sin(5*c) - 9*b*d^4 * e^a * \sin(5*c)) * e^{(b*x)} * \sin(5*d*x) \\
& + (5*b^4*d * \cos(5*c) * e^a + 50*b^2*d^3 * \cos(5*c) * e^a + 45*d^5 * \cos(5*c) * e^a + b^5 * e^a * \sin(5*c) + 10*b^3*d^2 * e^a * \sin(5*c) + 9*b*d^4 * e^a * \sin(5*c)) * e^{(b*x)} * \sin(5*d*x + 10*c) \\
& + (3*b^4*d * \cos(5*c) * e^a + 78*b^2*d^3 * \cos(5*c) * e^a + 75*d^5 * \cos(5*c) * e^a + b^5 * e^a * \sin(5*c) + 26*b^3*d^2 * e^a * \sin(5*c) + 25*b*d^4 * e^a * \sin(5*c)) * e^{(b*x)} * \sin(3*d*x + 8*c) \\
& + (3*b^4*d * \cos(5*c) * e^a + 78*b^2*d^3 * \cos(5*c) * e^a + 75*d^5 * \cos(5*c) * e^a - b^5 * e^a * \sin(5*c) - 26*b^3*d^2 * e^a * \sin(5*c) - 25*b*d^4 * e^a * \sin(5*c)) * e^{(b*x)} * \sin(3*d*x - 2*c) \\
& - 2*(b^4*d * \cos(5*c) * e^a + 34*b^2*d^3 * \cos(5*c) * e^a + 225*d^5 * \cos(5*c) * e^a + b^5 * e^a * \sin(5*c) + 34*b^3*d^2 * e^a * \sin(5*c) + 225*b*d^4 * e^a * \sin(5*c)) * e^{(b*x)} * \sin(d*x + 6*c) \\
& - 2*(b^4*d * \cos(5*c) * e^a + 34*b^2*d^3 * \cos(5*c) * e^a + 225*d^5 * \cos(5*c) * e^a + b^5 * e^a * \sin(5*c) - 34*b^3*d^2 * e^a * \sin(5*c) - 225*b*d^4 * e^a * \sin(5*c)) * e^{(b*x)} * \sin(d*x - 4*c)) / (b^6 * \cos(5*c)^2 + b^6 * \sin(5*c)^2 + 225 * (\cos(5*c)^2 + \sin(5*c)^2) * d^6 + 259 * (b^2 * \cos(5*c)^2 + b^2 * \sin(5*c)^2) * d^4 + 35 * (b^4 * \cos(5*c)^2 + b^4 * \sin(5*c)^2) * d^2)
\end{aligned}$$

mupad [B] time = 3.71, size = 255, normalized size = 1.39

$$\frac{e^{a+bx} (\cos(dx) - \sin(dx) 1i) (\cos(c) - \sin(c) 1i)}{16 (b - d 1i)} \frac{e^{a+bx} (\cos(3dx) + \sin(3dx) 1i) (\cos(3c) + \sin(3c) 1i)}{32 (-3d + b 1i)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(cos(c + d*x)^3*exp(a + b*x)*sin(c + d*x)^2,x)

[Out] (exp(a + b*x)*(cos(d*x) - sin(d*x)*1i)*(cos(c) - sin(c)*1i))/(16*(b - d*1i)) - (exp(a + b*x)*(cos(3*d*x) + sin(3*d*x)*1i)*(cos(3*c) + sin(3*c)*1i)*1i)/(32*(b*1i - 3*d)) - (exp(a + b*x)*(cos(5*d*x) + sin(5*d*x)*1i)*(cos(5*c) + sin(5*c)*1i)*1i)/(32*(b*1i - 5*d)) + (exp(a + b*x)*(cos(d*x) + sin(d*x)*1i)*(cos(c) + sin(c)*1i)*1i)/(16*(b*1i - d)) - (exp(a + b*x)*(cos(3*d*x) - sin(3*d*x)*1i)*(cos(3*c) - sin(3*c)*1i))/(32*(b - d*3i)) - (exp(a + b*x)*(cos(5*d*x) - sin(5*d*x)*1i)*(cos(5*c) - sin(5*c)*1i))/(32*(b - d*5i))

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(b*x+a)*cos(d*x+c)**3*sin(d*x+c)**2,x)

[Out] Timed out

3.46 $\int e^{a+bx} \cos^3(c+dx) \sin^3(c+dx) dx$

Optimal. Leaf size=129

$$\frac{3be^{a+bx} \sin(2c+2dx)}{32(b^2+4d^2)} - \frac{be^{a+bx} \sin(6c+6dx)}{32(b^2+36d^2)} - \frac{3de^{a+bx} \cos(2c+2dx)}{16(b^2+4d^2)} + \frac{3de^{a+bx} \cos(6c+6dx)}{16(b^2+36d^2)}$$

[Out] $-3/16*d*\exp(b*x+a)*\cos(2*d*x+2*c)/(b^2+4*d^2)+3/16*d*\exp(b*x+a)*\cos(6*d*x+6*c)/(b^2+36*d^2)+3/32*b*\exp(b*x+a)*\sin(2*d*x+2*c)/(b^2+4*d^2)-1/32*b*\exp(b*x+a)*\sin(6*d*x+6*c)/(b^2+36*d^2)$

Rubi [A] time = 0.10, antiderivative size = 129, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 2, integrand size = 24, $\frac{\text{number of rules}}{\text{integrand size}} = 0.083$, Rules used = {4469, 4432}

$$\frac{3be^{a+bx} \sin(2c+2dx)}{32(b^2+4d^2)} - \frac{be^{a+bx} \sin(6c+6dx)}{32(b^2+36d^2)} - \frac{3de^{a+bx} \cos(2c+2dx)}{16(b^2+4d^2)} + \frac{3de^{a+bx} \cos(6c+6dx)}{16(b^2+36d^2)}$$

Antiderivative was successfully verified.

[In] `Int[E^(a + b*x)*Cos[c + d*x]^3*Sin[c + d*x]^3,x]`

[Out] $(-3*d*E^{(a + b*x)*\cos[2*c + 2*d*x]})/(16*(b^2 + 4*d^2)) + (3*d*E^{(a + b*x)*\cos[6*c + 6*d*x]})/(16*(b^2 + 36*d^2)) + (3*b*E^{(a + b*x)*\sin[2*c + 2*d*x]})/(32*(b^2 + 4*d^2)) - (b*E^{(a + b*x)*\sin[6*c + 6*d*x]})/(32*(b^2 + 36*d^2))$

Rule 4432

`Int[(F_)^((c_.)*((a_.) + (b_.)*(x_)))*Sin[(d_.) + (e_.)*(x_)], x_Symbol] :> Simp[(b*c*Log[F]*F^(c*(a + b*x))*Sin[d + e*x])/(e^2 + b^2*c^2*Log[F]^2), x] - Simp[(e*F^(c*(a + b*x))*Cos[d + e*x])/(e^2 + b^2*c^2*Log[F]^2), x] /; FreeQ[{F, a, b, c, d, e}, x] && NeQ[e^2 + b^2*c^2*Log[F]^2, 0]`

Rule 4469

`Int[Cos[(f_.) + (g_.)*(x_)]^(n_.)*(F_)^((c_.)*((a_.) + (b_.)*(x_)))*Sin[(d_.) + (e_.)*(x_)]^(m_.), x_Symbol] :> Int[ExpandTrigReduce[F^(c*(a + b*x)), Sin[d + e*x]^m*Cos[f + g*x]^n, x], x] /; FreeQ[{F, a, b, c, d, e, f, g}, x] && IGtQ[m, 0] && IGtQ[n, 0]`

Rubi steps

$$\begin{aligned} \int e^{a+bx} \cos^3(c+dx) \sin^3(c+dx) dx &= \int \left(\frac{3}{32} e^{a+bx} \sin(2c+2dx) - \frac{1}{32} e^{a+bx} \sin(6c+6dx) \right) dx \\ &= - \left(\frac{1}{32} \int e^{a+bx} \sin(6c+6dx) dx \right) + \frac{3}{32} \int e^{a+bx} \sin(2c+2dx) dx \\ &= - \frac{3de^{a+bx} \cos(2c+2dx)}{16(b^2+4d^2)} + \frac{3de^{a+bx} \cos(6c+6dx)}{16(b^2+36d^2)} + \frac{3be^{a+bx} \sin(2c+2dx)}{32(b^2+4d^2)} \end{aligned}$$

Mathematica [A] time = 0.94, size = 111, normalized size = 0.86

$$\frac{e^{a+bx} \left(-6d(b^2+36d^2) \cos(2(c+dx)) + 6d(b^2+4d^2) \cos(6(c+dx)) - 2b \sin(2(c+dx)) \right) \left((b^2+4d^2) \cos(4(c+dx)) \right)}{32(b^4+40b^2d^2+144d^4)}$$

Antiderivative was successfully verified.

[In] Integrate[E^(a + b*x)*Cos[c + d*x]^3*Sin[c + d*x]^3,x]

[Out] (E^(a + b*x)*(-6*d*(b^2 + 36*d^2)*Cos[2*(c + d*x)] + 6*d*(b^2 + 4*d^2)*Cos[6*(c + d*x)] - 2*b*(-b^2 - 52*d^2 + (b^2 + 4*d^2)*Cos[4*(c + d*x)])*Sin[2*(c + d*x)])/(32*(b^4 + 40*b^2*d^2 + 144*d^4))

fricas [A] time = 1.46, size = 156, normalized size = 1.21

$$\frac{\left(\left(b^3 + 4bd^2\right)\cos(dx + c)^5 - 6bd^2\cos(dx + c) - \left(b^3 + 4bd^2\right)\cos(dx + c)^3\right)e^{(bx+a)}\sin(dx + c) - 3\left(2\left(b^2d + 4d^3\right)\cos(dx + c)^6 + b^2d\cos(dx + c)^2 - 3\left(b^2d + 4d^3\right)\cos(dx + c)^4 + 2d^3\right)e^{(bx+a)}}{b^4 + 40b^2d^2 + 144d^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(b*x+a)*cos(d*x+c)^3*sin(d*x+c)^3,x, algorithm="fricas")

[Out] -(((b^3 + 4*b*d^2)*cos(d*x + c)^5 - 6*b*d^2*cos(d*x + c) - (b^3 + 4*b*d^2)*cos(d*x + c)^3)*e^(b*x + a)*sin(d*x + c) - 3*(2*(b^2*d + 4*d^3)*cos(d*x + c)^6 + b^2*d*cos(d*x + c)^2 - 3*(b^2*d + 4*d^3)*cos(d*x + c)^4 + 2*d^3)*e^(b*x + a))/(b^4 + 40*b^2*d^2 + 144*d^4)

giac [A] time = 0.16, size = 111, normalized size = 0.86

$$\frac{1}{32}\left(\frac{6d\cos(6dx + 6c)}{b^2 + 36d^2} - \frac{b\sin(6dx + 6c)}{b^2 + 36d^2}\right)e^{(bx+a)} - \frac{3}{32}\left(\frac{2d\cos(2dx + 2c)}{b^2 + 4d^2} - \frac{b\sin(2dx + 2c)}{b^2 + 4d^2}\right)e^{(bx+a)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(b*x+a)*cos(d*x+c)^3*sin(d*x+c)^3,x, algorithm="giac")

[Out] 1/32*(6*d*cos(6*d*x + 6*c)/(b^2 + 36*d^2) - b*sin(6*d*x + 6*c)/(b^2 + 36*d^2))*e^(b*x + a) - 3/32*(2*d*cos(2*d*x + 2*c)/(b^2 + 4*d^2) - b*sin(2*d*x + 2*c)/(b^2 + 4*d^2))*e^(b*x + a)

maple [A] time = 0.10, size = 118, normalized size = 0.91

$$\frac{3de^{bx+a}\cos(2dx + 2c)}{16(b^2 + 4d^2)} + \frac{3de^{bx+a}\cos(6dx + 6c)}{16(b^2 + 36d^2)} + \frac{3be^{bx+a}\sin(2dx + 2c)}{32(b^2 + 4d^2)} - \frac{be^{bx+a}\sin(6dx + 6c)}{32(b^2 + 36d^2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(exp(b*x+a)*cos(d*x+c)^3*sin(d*x+c)^3,x)

[Out] -3/16*d*exp(b*x+a)*cos(2*d*x+2*c)/(b^2+4*d^2)+3/16*d*exp(b*x+a)*cos(6*d*x+6*c)/(b^2+36*d^2)+3/32*b*exp(b*x+a)*sin(2*d*x+2*c)/(b^2+4*d^2)-1/32*b*exp(b*x+a)*sin(6*d*x+6*c)/(b^2+36*d^2)

maxima [B] time = 0.36, size = 550, normalized size = 4.26

$$\frac{\left(6b^2d\cos(6c)e^a + 24d^3\cos(6c)e^a - b^3e^a\sin(6c) - 4bd^2e^a\sin(6c)\right)\cos(6dx)e^{(bx)} + \left(6b^2d\cos(6c)e^a + 24d^3\cos(6c)e^a - b^3e^a\sin(6c) - 4bd^2e^a\sin(6c)\right)\sin(6dx)e^{(bx)}}{b^4 + 40b^2d^2 + 144d^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(b*x+a)*cos(d*x+c)^3*sin(d*x+c)^3,x, algorithm="maxima")

[Out] 1/64*((6*b^2*d*cos(6*c))*e^a + 24*d^3*cos(6*c)*e^a - b^3*e^a*sin(6*c) - 4*b*d^2*e^a*sin(6*c))*cos(6*d*x)*e^(b*x) + (6*b^2*d*cos(6*c))*e^a + 24*d^3*cos(6*c)*e^a + b^3*e^a*sin(6*c) + 4*b*d^2*e^a*sin(6*c))*cos(6*d*x + 12*c)*e^(b*x) - 3*(2*b^2*d*cos(6*c))*e^a + 72*d^3*cos(6*c)*e^a + b^3*e^a*sin(6*c) + 36*b*d^2*e^a*sin(6*c))*cos(2*d*x + 8*c)*e^(b*x) - 3*(2*b^2*d*cos(6*c))*e^a + 72*d^3*cos(6*c)*e^a - b^3*e^a*sin(6*c) - 36*b*d^2*e^a*sin(6*c))*cos(2*d*x - 4*c)*e^(b*x) - (b^3*cos(6*c))*e^a + 4*b*d^2*cos(6*c)*e^a + 6*b^2*d*e^a*sin(6*c)

) + 24*d^3*e^a*sin(6*c))*e^(b*x)*sin(6*d*x) - (b^3*cos(6*c)*e^a + 4*b*d^2*cos(6*c)*e^a - 6*b^2*d*e^a*sin(6*c) - 24*d^3*e^a*sin(6*c))*e^(b*x)*sin(6*d*x + 12*c) + 3*(b^3*cos(6*c)*e^a + 36*b*d^2*cos(6*c)*e^a - 2*b^2*d*e^a*sin(6*c) - 72*d^3*e^a*sin(6*c))*e^(b*x)*sin(2*d*x + 8*c) + 3*(b^3*cos(6*c)*e^a + 36*b*d^2*cos(6*c)*e^a + 2*b^2*d*e^a*sin(6*c) + 72*d^3*e^a*sin(6*c))*e^(b*x)*sin(2*d*x - 4*c))/(b^4*cos(6*c)^2 + b^4*sin(6*c)^2 + 144*(cos(6*c)^2 + sin(6*c)^2)*d^4 + 40*(b^2*cos(6*c)^2 + b^2*sin(6*c)^2)*d^2)

mupad [B] time = 1.01, size = 178, normalized size = 1.38

$$\frac{3 e^{a+bx} (\cos(2dx) - \sin(2dx) 1i) (\cos(2c) - \sin(2c) 1i)}{64 (2d + b1i)} + \frac{e^{a+bx} (\cos(6dx) - \sin(6dx) 1i) (\cos(6c) - \sin(6c) 1i)}{64 (6d + b1i)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(cos(c + d*x)^3*exp(a + b*x)*sin(c + d*x)^3,x)

[Out] (exp(a + b*x)*(cos(6*d*x) - sin(6*d*x)*1i)*(cos(6*c) - sin(6*c)*1i))/(64*(b*1i + 6*d)) - (3*exp(a + b*x)*(cos(2*d*x) - sin(2*d*x)*1i)*(cos(2*c) - sin(2*c)*1i))/(64*(b*1i + 2*d)) - (exp(a + b*x)*(cos(2*d*x) + sin(2*d*x)*1i)*(cos(2*c) + sin(2*c)*1i)*3i)/(64*(b + d*2i)) + (exp(a + b*x)*(cos(6*d*x) + sin(6*d*x)*1i)*(cos(6*c) + sin(6*c)*1i)*1i)/(64*(b + d*6i))

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(b*x+a)*cos(d*x+c)**3*sin(d*x+c)**3,x)

[Out] Timed out

3.47 $\int e^x x \sin(x) dx$

Optimal. Leaf size=30

$$\frac{1}{2}e^x x \sin(x) + \frac{1}{2}e^x \cos(x) - \frac{1}{2}e^x x \cos(x)$$

[Out] 1/2*exp(x)*cos(x)-1/2*exp(x)*x*cos(x)+1/2*exp(x)*x*sin(x)

Rubi [A] time = 0.04, antiderivative size = 30, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 3, integrand size = 7, $\frac{\text{number of rules}}{\text{integrand size}} = 0.429$, Rules used = {4432, 4465, 4433}

$$\frac{1}{2}e^x x \sin(x) + \frac{1}{2}e^x \cos(x) - \frac{1}{2}e^x x \cos(x)$$

Antiderivative was successfully verified.

[In] Int[E^x*x*Sin[x],x]

[Out] (E^x*Cos[x])/2 - (E^x*x*Cos[x])/2 + (E^x*x*Sin[x])/2

Rule 4432

Int[(F_)^((c_.)*((a_.) + (b_.)*(x_)))*Sin[(d_.) + (e_.)*(x_)], x_Symbol] :=
Simp[(b*c*Log[F]*F^(c*(a + b*x))*Sin[d + e*x]/(e^2 + b^2*c^2*Log[F]^2), x
] - Simp[(e*F^(c*(a + b*x))*Cos[d + e*x]/(e^2 + b^2*c^2*Log[F]^2), x] /; FreeQ[{F, a, b, c, d, e}, x] && NeQ[e^2 + b^2*c^2*Log[F]^2, 0]

Rule 4433

Int[Cos[(d_.) + (e_.)*(x_)]*(F_)^((c_.)*((a_.) + (b_.)*(x_))), x_Symbol] :=
Simp[(b*c*Log[F]*F^(c*(a + b*x))*Cos[d + e*x]/(e^2 + b^2*c^2*Log[F]^2), x
] + Simp[(e*F^(c*(a + b*x))*Sin[d + e*x]/(e^2 + b^2*c^2*Log[F]^2), x] /; FreeQ[{F, a, b, c, d, e}, x] && NeQ[e^2 + b^2*c^2*Log[F]^2, 0]

Rule 4465

Int[(F_)^((c_.)*((a_.) + (b_.)*(x_)))*((f_.)*(x_))^(m_.)*Sin[(d_.) + (e_.)*(x_)]^(n_.), x_Symbol] := Module[{u = IntHide[F^(c*(a + b*x))*Sin[d + e*x]^n, x]}, Dist[(f*x)^m, u, x] - Dist[f*m, Int[(f*x)^(m - 1)*u, x], x] /; FreeQ[{F, a, b, c, d, e, f}, x] && IGtQ[n, 0] && GtQ[m, 0]

Rubi steps

$$\begin{aligned} \int e^x x \sin(x) dx &= -\frac{1}{2}e^x x \cos(x) + \frac{1}{2}e^x x \sin(x) - \int \left(-\frac{1}{2}e^x \cos(x) + \frac{1}{2}e^x \sin(x) \right) dx \\ &= -\frac{1}{2}e^x x \cos(x) + \frac{1}{2}e^x x \sin(x) + \frac{1}{2} \int e^x \cos(x) dx - \frac{1}{2} \int e^x \sin(x) dx \\ &= \frac{1}{2}e^x \cos(x) - \frac{1}{2}e^x x \cos(x) + \frac{1}{2}e^x x \sin(x) \end{aligned}$$

Mathematica [A] time = 0.04, size = 19, normalized size = 0.63

$$\frac{1}{2}e^x(x \sin(x) - x \cos(x) + \cos(x))$$

Antiderivative was successfully verified.

[In] Integrate[E^x*x*Sin[x],x]

[Out] (E^x*(Cos[x] - x*Cos[x] + x*Sin[x]))/2

fricas [A] time = 0.84, size = 17, normalized size = 0.57

$$-\frac{1}{2}(x-1)\cos(x)e^x + \frac{1}{2}xe^x\sin(x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(x)*x*sin(x),x, algorithm="fricas")

[Out] -1/2*(x - 1)*cos(x)*e^x + 1/2*x*e^x*sin(x)

giac [A] time = 0.13, size = 16, normalized size = 0.53

$$-\frac{1}{2}((x-1)\cos(x) - x\sin(x))e^x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(x)*x*sin(x),x, algorithm="giac")

[Out] -1/2*((x - 1)*cos(x) - x*sin(x))*e^x

maple [A] time = 0.03, size = 19, normalized size = 0.63

$$\left(-\frac{x}{2} + \frac{1}{2}\right)e^x\cos(x) + \frac{e^xx\sin(x)}{2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(exp(x)*x*sin(x),x)

[Out] (-1/2*x+1/2)*exp(x)*cos(x)+1/2*exp(x)*x*sin(x)

maxima [A] time = 0.32, size = 17, normalized size = 0.57

$$-\frac{1}{2}(x-1)\cos(x)e^x + \frac{1}{2}xe^x\sin(x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(x)*x*sin(x),x, algorithm="maxima")

[Out] -1/2*(x - 1)*cos(x)*e^x + 1/2*x*e^x*sin(x)

mupad [B] time = 0.08, size = 16, normalized size = 0.53

$$\frac{e^x(\cos(x) - x\cos(x) + x\sin(x))}{2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x*exp(x)*sin(x),x)

[Out] (exp(x)*(cos(x) - x*cos(x) + x*sin(x)))/2

sympy [A] time = 0.64, size = 27, normalized size = 0.90

$$\frac{xe^x\sin(x)}{2} - \frac{xe^x\cos(x)}{2} + \frac{e^x\cos(x)}{2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(x)*x*sin(x),x)

[Out] x*exp(x)*sin(x)/2 - x*exp(x)*cos(x)/2 + exp(x)*cos(x)/2

3.48 $\int e^x x^2 \sin(x) dx$

Optimal. Leaf size=50

$$\frac{1}{2}e^x x^2 \sin(x) - \frac{1}{2}e^x x^2 \cos(x) - \frac{1}{2}e^x \sin(x) + e^x x \cos(x) - \frac{1}{2}e^x \cos(x)$$

[Out] $-1/2*\exp(x)*\cos(x)+\exp(x)*x*\cos(x)-1/2*\exp(x)*x^2*\cos(x)-1/2*\exp(x)*\sin(x)+1/2*\exp(x)*x^2*\sin(x)$

Rubi [A] time = 0.12, antiderivative size = 50, normalized size of antiderivative = 1.00, number of steps used = 11, number of rules used = 5, integrand size = 9, $\frac{\text{number of rules}}{\text{integrand size}} = 0.556$, Rules used = {4432, 4465, 14, 4433, 4466}

$$\frac{1}{2}e^x x^2 \sin(x) - \frac{1}{2}e^x x^2 \cos(x) - \frac{1}{2}e^x \sin(x) + e^x x \cos(x) - \frac{1}{2}e^x \cos(x)$$

Antiderivative was successfully verified.

[In] Int[E^x*x^2*Sin[x],x]

[Out] $-(E^x*\cos[x])/2 + E^x*x*\cos[x] - (E^x*x^2*\cos[x])/2 - (E^x*\sin[x])/2 + (E^x*x^2*\sin[x])/2$

Rule 14

Int[(u_)*((c_)*(x_))^(m_), x_Symbol] :> Int[ExpandIntegrand[(c*x)^m*u, x], x] /; FreeQ[{c, m}, x] && SumQ[u] && !LinearQ[u, x] && !MatchQ[u, (a_ + (b_)*(v_)) /; FreeQ[{a, b}, x] && InverseFunctionQ[v]]

Rule 4432

Int[(F_)^((c_)*((a_) + (b_)*(x_)))*Sin[(d_) + (e_)*(x_)], x_Symbol] :> Simp[(b*c*Log[F]*F^(c*(a + b*x))*Sin[d + e*x]/(e^2 + b^2*c^2*Log[F]^2), x] - Simp[(e*F^(c*(a + b*x))*Cos[d + e*x]/(e^2 + b^2*c^2*Log[F]^2), x] /; FreeQ[{F, a, b, c, d, e}, x] && NeQ[e^2 + b^2*c^2*Log[F]^2, 0]

Rule 4433

Int[Cos[(d_) + (e_)*(x_)]*(F_)^((c_)*((a_) + (b_)*(x_))), x_Symbol] :> Simp[(b*c*Log[F]*F^(c*(a + b*x))*Cos[d + e*x]/(e^2 + b^2*c^2*Log[F]^2), x] + Simp[(e*F^(c*(a + b*x))*Sin[d + e*x]/(e^2 + b^2*c^2*Log[F]^2), x] /; FreeQ[{F, a, b, c, d, e}, x] && NeQ[e^2 + b^2*c^2*Log[F]^2, 0]

Rule 4465

Int[(F_)^((c_)*((a_) + (b_)*(x_)))*((f_)*(x_))^(m_)*Sin[(d_) + (e_)*(x_)]^(n_), x_Symbol] :> Module[{u = IntHide[F^(c*(a + b*x))*Sin[d + e*x]^n, x]}, Dist[(f*x)^m, u, x] - Dist[f*m, Int[(f*x)^(m - 1)*u, x], x] /; FreeQ[{F, a, b, c, d, e, f}, x] && IGtQ[n, 0] && GtQ[m, 0]

Rule 4466

Int[Cos[(d_) + (e_)*(x_)]^(n_)*(F_)^((c_)*((a_) + (b_)*(x_)))*((f_)*(x_))^(m_), x_Symbol] :> Module[{u = IntHide[F^(c*(a + b*x))*Cos[d + e*x]^n, x]}, Dist[(f*x)^m, u, x] - Dist[f*m, Int[(f*x)^(m - 1)*u, x], x] /; FreeQ[{F, a, b, c, d, e, f}, x] && IGtQ[n, 0] && GtQ[m, 0]

Rubi steps

$$\begin{aligned}
\int e^x x^2 \sin(x) dx &= -\frac{1}{2} e^x x^2 \cos(x) + \frac{1}{2} e^x x^2 \sin(x) - 2 \int x \left(-\frac{1}{2} e^x \cos(x) + \frac{1}{2} e^x \sin(x) \right) dx \\
&= -\frac{1}{2} e^x x^2 \cos(x) + \frac{1}{2} e^x x^2 \sin(x) - 2 \int \left(-\frac{1}{2} e^x x \cos(x) + \frac{1}{2} e^x x \sin(x) \right) dx \\
&= -\frac{1}{2} e^x x^2 \cos(x) + \frac{1}{2} e^x x^2 \sin(x) + \int e^x x \cos(x) dx - \int e^x x \sin(x) dx \\
&= e^x x \cos(x) - \frac{1}{2} e^x x^2 \cos(x) + \frac{1}{2} e^x x^2 \sin(x) + \int \left(-\frac{1}{2} e^x \cos(x) + \frac{1}{2} e^x \sin(x) \right) dx - \int \left(\frac{1}{2} e^x \cos(x) \right) dx \\
&= e^x x \cos(x) - \frac{1}{2} e^x x^2 \cos(x) + \frac{1}{2} e^x x^2 \sin(x) - 2 \left(\frac{1}{2} \int e^x \cos(x) dx \right) \\
&= e^x x \cos(x) - \frac{1}{2} e^x x^2 \cos(x) + \frac{1}{2} e^x x^2 \sin(x) - 2 \left(\frac{1}{4} e^x \cos(x) + \frac{1}{4} e^x \sin(x) \right)
\end{aligned}$$

Mathematica [A] time = 0.04, size = 25, normalized size = 0.50

$$\frac{1}{2} e^x \left((x^2 - 1) \sin(x) - (x - 1)^2 \cos(x) \right)$$

Antiderivative was successfully verified.

[In] Integrate[E^x*x^2*Sin[x],x]

[Out] (E^x*(-((-1 + x)^2*Cos[x]) + (-1 + x^2)*Sin[x]))/2

fricas [A] time = 1.58, size = 26, normalized size = 0.52

$$-\frac{1}{2} (x^2 - 2x + 1) \cos(x) e^x + \frac{1}{2} (x^2 - 1) e^x \sin(x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(x)*x^2*sin(x),x, algorithm="fricas")

[Out] -1/2*(x^2 - 2*x + 1)*cos(x)*e^x + 1/2*(x^2 - 1)*e^x*sin(x)

giac [A] time = 0.12, size = 25, normalized size = 0.50

$$-\frac{1}{2} \left((x^2 - 2x + 1) \cos(x) - (x^2 - 1) \sin(x) \right) e^x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(x)*x^2*sin(x),x, algorithm="giac")

[Out] -1/2*((x^2 - 2*x + 1)*cos(x) - (x^2 - 1)*sin(x))*e^x

maple [A] time = 0.02, size = 27, normalized size = 0.54

$$\left(-\frac{1}{2} x^2 + x - \frac{1}{2} \right) e^x \cos(x) + \left(\frac{x^2}{2} - \frac{1}{2} \right) e^x \sin(x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(exp(x)*x^2*sin(x),x)

[Out] (-1/2*x^2+x-1/2)*exp(x)*cos(x)+(1/2*x^2-1/2)*exp(x)*sin(x)

maxima [A] time = 0.33, size = 26, normalized size = 0.52

$$-\frac{1}{2} (x^2 - 2x + 1) \cos(x) e^x + \frac{1}{2} (x^2 - 1) e^x \sin(x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(x)*x^2*sin(x),x, algorithm="maxima")

[Out] -1/2*(x^2 - 2*x + 1)*cos(x)*e^x + 1/2*(x^2 - 1)*e^x*sin(x)

mupad [B] time = 2.38, size = 21, normalized size = 0.42

$$\frac{e^x (x - 1) (\cos(x) + \sin(x) - x \cos(x) + x \sin(x))}{2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^2*exp(x)*sin(x),x)

[Out] (exp(x)*(x - 1)*(cos(x) + sin(x) - x*cos(x) + x*sin(x)))/2

sympy [A] time = 1.56, size = 48, normalized size = 0.96

$$\frac{x^2 e^x \sin(x)}{2} - \frac{x^2 e^x \cos(x)}{2} + x e^x \cos(x) - \frac{e^x \sin(x)}{2} - \frac{e^x \cos(x)}{2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(x)*x**2*sin(x),x)

[Out] x**2*exp(x)*sin(x)/2 - x**2*exp(x)*cos(x)/2 + x*exp(x)*cos(x) - exp(x)*sin(x)/2 - exp(x)*cos(x)/2

3.49 $\int e^x x \cos(x) dx$

Optimal. Leaf size=30

$$-\frac{1}{2}e^x \sin(x) + \frac{1}{2}e^x x \sin(x) + \frac{1}{2}e^x x \cos(x)$$

[Out] 1/2*exp(x)*x*cos(x)-1/2*exp(x)*sin(x)+1/2*exp(x)*x*sin(x)

Rubi [A] time = 0.04, antiderivative size = 30, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 3, integrand size = 7, $\frac{\text{number of rules}}{\text{integrand size}} = 0.429$, Rules used = {4433, 4466, 4432}

$$-\frac{1}{2}e^x \sin(x) + \frac{1}{2}e^x x \sin(x) + \frac{1}{2}e^x x \cos(x)$$

Antiderivative was successfully verified.

[In] Int[E^x*x*Cos[x],x]

[Out] (E^x*x*Cos[x])/2 - (E^x*Sin[x])/2 + (E^x*x*Sin[x])/2

Rule 4432

```
Int[(F_)^((c_.)*((a_.) + (b_.)*(x_)))*Sin[(d_.) + (e_.)*(x_)], x_Symbol] :>
  Simp[(b*c*Log[F]*F^(c*(a + b*x))*Sin[d + e*x])/(e^2 + b^2*c^2*Log[F]^2), x
] - Simp[(e*F^(c*(a + b*x))*Cos[d + e*x])/(e^2 + b^2*c^2*Log[F]^2), x] /; F
reeQ[{F, a, b, c, d, e}, x] && NeQ[e^2 + b^2*c^2*Log[F]^2, 0]
```

Rule 4433

```
Int[Cos[(d_.) + (e_.)*(x_)]*(F_)^((c_.)*((a_.) + (b_.)*(x_))), x_Symbol] :>
  Simp[(b*c*Log[F]*F^(c*(a + b*x))*Cos[d + e*x])/(e^2 + b^2*c^2*Log[F]^2), x
] + Simp[(e*F^(c*(a + b*x))*Sin[d + e*x])/(e^2 + b^2*c^2*Log[F]^2), x] /; F
reeQ[{F, a, b, c, d, e}, x] && NeQ[e^2 + b^2*c^2*Log[F]^2, 0]
```

Rule 4466

```
Int[Cos[(d_.) + (e_.)*(x_)]^(n_.)*(F_)^((c_.)*((a_.) + (b_.)*(x_)))*((f_.)*
(x_))^(m_.), x_Symbol] :> Module[{u = IntHide[F^(c*(a + b*x))*Cos[d + e*x]^
n, x]}, Dist[(f*x)^m, u, x] - Dist[f*m, Int[(f*x)^(m - 1)*u, x], x] /; Fre
eQ[{F, a, b, c, d, e, f}, x] && IGtQ[n, 0] && GtQ[m, 0]
```

Rubi steps

$$\begin{aligned} \int e^x x \cos(x) dx &= \frac{1}{2}e^x x \cos(x) + \frac{1}{2}e^x x \sin(x) - \int \left(\frac{1}{2}e^x \cos(x) + \frac{1}{2}e^x \sin(x) \right) dx \\ &= \frac{1}{2}e^x x \cos(x) + \frac{1}{2}e^x x \sin(x) - \frac{1}{2} \int e^x \cos(x) dx - \frac{1}{2} \int e^x \sin(x) dx \\ &= \frac{1}{2}e^x x \cos(x) - \frac{1}{2}e^x \sin(x) + \frac{1}{2}e^x x \sin(x) \end{aligned}$$

Mathematica [A] time = 0.03, size = 18, normalized size = 0.60

$$\frac{1}{2}e^x((x-1)\sin(x) + x\cos(x))$$

Antiderivative was successfully verified.

[In] Integrate[E^x*x*Cos[x],x]

[Out] (E^x*(x*Cos[x] + (-1 + x)*Sin[x]))/2

fricas [A] time = 0.63, size = 17, normalized size = 0.57

$$\frac{1}{2} x \cos(x) e^x + \frac{1}{2} (x - 1) e^x \sin(x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(x)*x*cos(x),x, algorithm="fricas")

[Out] 1/2*x*cos(x)*e^x + 1/2*(x - 1)*e^x*sin(x)

giac [A] time = 0.13, size = 15, normalized size = 0.50

$$\frac{1}{2} (x \cos(x) + (x - 1) \sin(x)) e^x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(x)*x*cos(x),x, algorithm="giac")

[Out] 1/2*(x*cos(x) + (x - 1)*sin(x))*e^x

maple [A] time = 0.03, size = 20, normalized size = 0.67

$$\frac{e^x x \cos(x)}{2} - \left(-\frac{x}{2} + \frac{1}{2} \right) e^x \sin(x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(exp(x)*x*cos(x),x)

[Out] 1/2*exp(x)*x*cos(x) - (-1/2*x+1/2)*exp(x)*sin(x)

maxima [A] time = 0.32, size = 17, normalized size = 0.57

$$\frac{1}{2} x \cos(x) e^x + \frac{1}{2} (x - 1) e^x \sin(x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(x)*x*cos(x),x, algorithm="maxima")

[Out] 1/2*x*cos(x)*e^x + 1/2*(x - 1)*e^x*sin(x)

mupad [B] time = 2.35, size = 17, normalized size = 0.57

$$\frac{e^x (x \cos(x) - \sin(x) + x \sin(x))}{2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x*exp(x)*cos(x),x)

[Out] (exp(x)*(x*cos(x) - sin(x) + x*sin(x)))/2

sympy [A] time = 0.63, size = 27, normalized size = 0.90

$$\frac{x e^x \sin(x)}{2} + \frac{x e^x \cos(x)}{2} - \frac{e^x \sin(x)}{2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(x)*x*cos(x),x)

[Out] x*exp(x)*sin(x)/2 + x*exp(x)*cos(x)/2 - exp(x)*sin(x)/2

3.50 $\int e^x x^2 \cos(x) dx$

Optimal. Leaf size=51

$$\frac{1}{2}e^x x^2 \sin(x) + \frac{1}{2}e^x x^2 \cos(x) - e^x x \sin(x) + \frac{1}{2}e^x \sin(x) - \frac{1}{2}e^x \cos(x)$$

[Out] $-1/2*\exp(x)*\cos(x)+1/2*\exp(x)*x^2*\cos(x)+1/2*\exp(x)*\sin(x)-\exp(x)*x*\sin(x)+1/2*\exp(x)*x^2*\sin(x)$

Rubi [A] time = 0.12, antiderivative size = 51, normalized size of antiderivative = 1.00, number of steps used = 11, number of rules used = 5, integrand size = 9, $\frac{\text{number of rules}}{\text{integrand size}} = 0.556$, Rules used = {4433, 4466, 14, 4432, 4465}

$$\frac{1}{2}e^x x^2 \sin(x) + \frac{1}{2}e^x x^2 \cos(x) - e^x x \sin(x) + \frac{1}{2}e^x \sin(x) - \frac{1}{2}e^x \cos(x)$$

Antiderivative was successfully verified.

[In] Int[E^x*x^2*Cos[x],x]

[Out] $-(E^x*\cos[x])/2 + (E^x*x^2*\cos[x])/2 + (E^x*\sin[x])/2 - E^x*x*\sin[x] + (E^x*x^2*\sin[x])/2$

Rule 14

Int[(u_)*((c_)*(x_))^(m_), x_Symbol] := Int[ExpandIntegrand[(c*x)^m*u, x], x] /; FreeQ[{c, m}, x] && SumQ[u] && !LinearQ[u, x] && !MatchQ[u, (a_ + (b_)*(v_)) /; FreeQ[{a, b}, x] && InverseFunctionQ[v]]

Rule 4432

Int[(F_)^((c_)*(a_) + (b_)*(x_))*Sin[(d_) + (e_)*(x_)], x_Symbol] := Simp[(b*c*Log[F]*F^(c*(a + b*x))*Sin[d + e*x])/(e^2 + b^2*c^2*Log[F]^2), x] - Simp[(e*F^(c*(a + b*x))*Cos[d + e*x])/(e^2 + b^2*c^2*Log[F]^2), x] /; FreeQ[{F, a, b, c, d, e}, x] && NeQ[e^2 + b^2*c^2*Log[F]^2, 0]

Rule 4433

Int[Cos[(d_) + (e_)*(x_)]*(F_)^((c_)*(a_) + (b_)*(x_)), x_Symbol] := Simp[(b*c*Log[F]*F^(c*(a + b*x))*Cos[d + e*x])/(e^2 + b^2*c^2*Log[F]^2), x] + Simp[(e*F^(c*(a + b*x))*Sin[d + e*x])/(e^2 + b^2*c^2*Log[F]^2), x] /; FreeQ[{F, a, b, c, d, e}, x] && NeQ[e^2 + b^2*c^2*Log[F]^2, 0]

Rule 4465

Int[(F_)^((c_)*(a_) + (b_)*(x_))*((f_)*(x_))^(m_)*Sin[(d_) + (e_)*(x_)]^(n_), x_Symbol] := Module[{u = IntHide[F^(c*(a + b*x))*Sin[d + e*x]^n, x]}, Dist[(f*x)^m, u, x] - Dist[f*m, Int[(f*x)^(m - 1)*u, x], x] /; FreeQ[{F, a, b, c, d, e, f}, x] && IGtQ[n, 0] && GtQ[m, 0]

Rule 4466

Int[Cos[(d_) + (e_)*(x_)]^(n_)*(F_)^((c_)*(a_) + (b_)*(x_))*((f_)*(x_))^(m_), x_Symbol] := Module[{u = IntHide[F^(c*(a + b*x))*Cos[d + e*x]^n, x]}, Dist[(f*x)^m, u, x] - Dist[f*m, Int[(f*x)^(m - 1)*u, x], x] /; FreeQ[{F, a, b, c, d, e, f}, x] && IGtQ[n, 0] && GtQ[m, 0]

Rubi steps

$$\begin{aligned}
\int e^x x^2 \cos(x) dx &= \frac{1}{2} e^x x^2 \cos(x) + \frac{1}{2} e^x x^2 \sin(x) - 2 \int x \left(\frac{1}{2} e^x \cos(x) + \frac{1}{2} e^x \sin(x) \right) dx \\
&= \frac{1}{2} e^x x^2 \cos(x) + \frac{1}{2} e^x x^2 \sin(x) - 2 \int \left(\frac{1}{2} e^x x \cos(x) + \frac{1}{2} e^x x \sin(x) \right) dx \\
&= \frac{1}{2} e^x x^2 \cos(x) + \frac{1}{2} e^x x^2 \sin(x) - \int e^x x \cos(x) dx - \int e^x x \sin(x) dx \\
&= \frac{1}{2} e^x x^2 \cos(x) - e^x x \sin(x) + \frac{1}{2} e^x x^2 \sin(x) + \int \left(-\frac{1}{2} e^x \cos(x) + \frac{1}{2} e^x \sin(x) \right) dx + \int \left(\frac{1}{2} e^x \cos(x) - e^x x \sin(x) \right) dx \\
&= \frac{1}{2} e^x x^2 \cos(x) - e^x x \sin(x) + \frac{1}{2} e^x x^2 \sin(x) + 2 \left(\frac{1}{2} \int e^x \sin(x) dx \right) \\
&= \frac{1}{2} e^x x^2 \cos(x) - e^x x \sin(x) + \frac{1}{2} e^x x^2 \sin(x) + 2 \left(-\frac{1}{4} e^x \cos(x) + \frac{1}{4} e^x \sin(x) \right)
\end{aligned}$$

Mathematica [A] time = 0.03, size = 23, normalized size = 0.45

$$\frac{1}{2} e^x (x-1) ((x-1) \sin(x) + (x+1) \cos(x))$$

Antiderivative was successfully verified.

[In] Integrate[E^x*x^2*Cos[x],x]

[Out] (E^x*(-1+x)*((1+x)*Cos[x]+(-1+x)*Sin[x]))/2

fricas [A] time = 0.66, size = 26, normalized size = 0.51

$$\frac{1}{2} (x^2 - 1) \cos(x) e^x + \frac{1}{2} (x^2 - 2x + 1) e^x \sin(x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(x)*x^2*cos(x),x, algorithm="fricas")

[Out] 1/2*(x^2 - 1)*cos(x)*e^x + 1/2*(x^2 - 2*x + 1)*e^x*sin(x)

giac [A] time = 0.13, size = 24, normalized size = 0.47

$$\frac{1}{2} ((x^2 - 1) \cos(x) + (x^2 - 2x + 1) \sin(x)) e^x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(x)*x^2*cos(x),x, algorithm="giac")

[Out] 1/2*((x^2 - 1)*cos(x) + (x^2 - 2*x + 1)*sin(x))*e^x

maple [A] time = 0.03, size = 28, normalized size = 0.55

$$\left(\frac{x^2}{2} - \frac{1}{2} \right) e^x \cos(x) - \left(-\frac{1}{2} x^2 + x - \frac{1}{2} \right) e^x \sin(x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(exp(x)*x^2*cos(x),x)

[Out] (1/2*x^2-1/2)*exp(x)*cos(x)-(-1/2*x^2+x-1/2)*exp(x)*sin(x)

maxima [A] time = 0.32, size = 26, normalized size = 0.51

$$\frac{1}{2} (x^2 - 1) \cos(x) e^x + \frac{1}{2} (x^2 - 2x + 1) e^x \sin(x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(x)*x^2*cos(x),x, algorithm="maxima")

[Out] 1/2*(x^2 - 1)*cos(x)*e^x + 1/2*(x^2 - 2*x + 1)*e^x*sin(x)

mupad [B] time = 2.36, size = 22, normalized size = 0.43

$$\frac{e^x (x - 1) (\cos(x) - \sin(x) + x \cos(x) + x \sin(x))}{2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^2*exp(x)*cos(x),x)

[Out] (exp(x)*(x - 1)*(cos(x) - sin(x) + x*cos(x) + x*sin(x)))/2

sympy [A] time = 1.56, size = 48, normalized size = 0.94

$$\frac{x^2 e^x \sin(x)}{2} + \frac{x^2 e^x \cos(x)}{2} - x e^x \sin(x) + \frac{e^x \sin(x)}{2} - \frac{e^x \cos(x)}{2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(x)*x**2*cos(x),x)

[Out] x**2*exp(x)*sin(x)/2 + x**2*exp(x)*cos(x)/2 - x*exp(x)*sin(x) + exp(x)*sin(x)/2 - exp(x)*cos(x)/2

3.51 $\int e^{3x}(-5 \cos(4x) + 2 \sin(4x)) dx$

Optimal. Leaf size=27

$$-\frac{14}{25}e^{3x} \sin(4x) - \frac{23}{25}e^{3x} \cos(4x)$$

[Out] $-23/25*\exp(3*x)*\cos(4*x)-14/25*\exp(3*x)*\sin(4*x)$

Rubi [A] time = 0.08, antiderivative size = 27, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 3, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.158$, Rules used = {6742, 4433, 4432}

$$-\frac{14}{25}e^{3x} \sin(4x) - \frac{23}{25}e^{3x} \cos(4x)$$

Antiderivative was successfully verified.

[In] $\text{Int}[E^{(3*x)}*(-5*\text{Cos}[4*x] + 2*\text{Sin}[4*x]),x]$

[Out] $(-23*E^{(3*x)}*\text{Cos}[4*x])/25 - (14*E^{(3*x)}*\text{Sin}[4*x])/25$

Rule 4432

$\text{Int}[(F_)^{((c_.)*(a_.) + (b_.)*(x_))}*\text{Sin}[(d_.) + (e_.)*(x_)], x_Symbol] \rightarrow$
 $\text{Simp}[(b*c*\text{Log}[F]*F^{(c*(a + b*x))}*\text{Sin}[d + e*x])/(e^2 + b^2*c^2*\text{Log}[F]^2), x]$
 $- \text{Simp}[(e*F^{(c*(a + b*x))}*\text{Cos}[d + e*x])/(e^2 + b^2*c^2*\text{Log}[F]^2), x] /;$
 $\text{FreeQ}\{F, a, b, c, d, e\}, x \ \&\& \ \text{NeQ}[e^2 + b^2*c^2*\text{Log}[F]^2, 0]$

Rule 4433

$\text{Int}[\text{Cos}[(d_.) + (e_.)*(x_)]*(F_)^{((c_.)*(a_.) + (b_.)*(x_))}, x_Symbol] \rightarrow$
 $\text{Simp}[(b*c*\text{Log}[F]*F^{(c*(a + b*x))}*\text{Cos}[d + e*x])/(e^2 + b^2*c^2*\text{Log}[F]^2), x]$
 $+ \text{Simp}[(e*F^{(c*(a + b*x))}*\text{Sin}[d + e*x])/(e^2 + b^2*c^2*\text{Log}[F]^2), x] /;$
 $\text{FreeQ}\{F, a, b, c, d, e\}, x \ \&\& \ \text{NeQ}[e^2 + b^2*c^2*\text{Log}[F]^2, 0]$

Rule 6742

$\text{Int}[u_, x_Symbol] \rightarrow \text{With}\{v = \text{ExpandIntegrand}[u, x]\}, \text{Int}[v, x] /;$
 $\text{SumQ}[v]$

Rubi steps

$$\begin{aligned} \int e^{3x}(-5 \cos(4x) + 2 \sin(4x)) dx &= \int (-5e^{3x} \cos(4x) + 2e^{3x} \sin(4x)) dx \\ &= 2 \int e^{3x} \sin(4x) dx - 5 \int e^{3x} \cos(4x) dx \\ &= -\frac{23}{25}e^{3x} \cos(4x) - \frac{14}{25}e^{3x} \sin(4x) \end{aligned}$$

Mathematica [A] time = 0.09, size = 22, normalized size = 0.81

$$-\frac{1}{25}e^{3x}(14 \sin(4x) + 23 \cos(4x))$$

Antiderivative was successfully verified.

[In] $\text{Integrate}[E^{(3*x)}*(-5*\text{Cos}[4*x] + 2*\text{Sin}[4*x]),x]$

[Out] $-1/25*(E^{(3*x)}*(23*\text{Cos}[4*x] + 14*\text{Sin}[4*x]))$

fricas [A] time = 1.97, size = 21, normalized size = 0.78

$$-\frac{23}{25} \cos(4x) e^{(3x)} - \frac{14}{25} e^{(3x)} \sin(4x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(3*x)*(-5*cos(4*x)+2*sin(4*x)),x, algorithm="fricas")

[Out] -23/25*cos(4*x)*e^(3*x) - 14/25*e^(3*x)*sin(4*x)

giac [A] time = 0.14, size = 39, normalized size = 1.44

$$-\frac{2}{25} (4 \cos(4x) - 3 \sin(4x)) e^{(3x)} - \frac{1}{5} (3 \cos(4x) + 4 \sin(4x)) e^{(3x)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(3*x)*(-5*cos(4*x)+2*sin(4*x)),x, algorithm="giac")

[Out] -2/25*(4*cos(4*x) - 3*sin(4*x))*e^(3*x) - 1/5*(3*cos(4*x) + 4*sin(4*x))*e^(3*x)

maple [B] time = 0.05, size = 103, normalized size = 3.81

$$-\frac{8(3\cos(x)+4\sin(x))e^{3x}(\cos^3(x))}{5} + \frac{8(3\cos(x)+2\sin(x))e^{3x}\cos(x)}{5} - \frac{3e^{3x}}{5} - \frac{8e^{3x}\cos(4x)}{25} + \frac{6e^{3x}\sin(4x)}{25} - \frac{8e^{3x}\sin^3(4x)}{25}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(exp(3*x)*(-5*cos(4*x)+2*sin(4*x)),x)

[Out] -8/5*(3*cos(x)+4*sin(x))*exp(3*x)*cos(x)^3+8/5*(3*cos(x)+2*sin(x))*exp(3*x)*cos(x)-3/5*exp(x)^3-8/25*exp(3*x)*cos(4*x)+6/25*exp(3*x)*sin(4*x)-8/13*exp(3*x)*cos(2*x)+12/13*exp(3*x)*sin(2*x)-4/13*exp(3*x)*(3*sin(2*x)-2*cos(2*x))

maxima [A] time = 0.31, size = 39, normalized size = 1.44

$$-\frac{2}{25} (4 \cos(4x) - 3 \sin(4x)) e^{(3x)} - \frac{1}{5} (3 \cos(4x) + 4 \sin(4x)) e^{(3x)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(3*x)*(-5*cos(4*x)+2*sin(4*x)),x, algorithm="maxima")

[Out] -2/25*(4*cos(4*x) - 3*sin(4*x))*e^(3*x) - 1/5*(3*cos(4*x) + 4*sin(4*x))*e^(3*x)

mupad [B] time = 0.06, size = 19, normalized size = 0.70

$$\frac{e^{3x} (23 \cos(4x) + 14 \sin(4x))}{25}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(-exp(3*x)*(5*cos(4*x) - 2*sin(4*x)),x)

[Out] -(exp(3*x)*(23*cos(4*x) + 14*sin(4*x)))/25

sympy [A] time = 0.25, size = 27, normalized size = 1.00

$$-\frac{14e^{3x}\sin(4x)}{25} - \frac{23e^{3x}\cos(4x)}{25}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(3*x)*(-5*cos(4*x)+2*sin(4*x)),x)

[Out] -14*exp(3*x)*sin(4*x)/25 - 23*exp(3*x)*cos(4*x)/25

3.52 $\int (e^{-x} \sin(x) + e^x \sin(x)) dx$

Optimal. Leaf size=41

$$-\frac{1}{2}e^{-x} \sin(x) + \frac{1}{2}e^x \sin(x) - \frac{1}{2}e^{-x} \cos(x) - \frac{1}{2}e^x \cos(x)$$

[Out] $-1/2*\cos(x)/\exp(x)-1/2*\exp(x)*\cos(x)-1/2*\sin(x)/\exp(x)+1/2*\exp(x)*\sin(x)$

Rubi [A] time = 0.03, antiderivative size = 41, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {4432}

$$-\frac{1}{2}e^{-x} \sin(x) + \frac{1}{2}e^x \sin(x) - \frac{1}{2}e^{-x} \cos(x) - \frac{1}{2}e^x \cos(x)$$

Antiderivative was successfully verified.

[In] Int[Sin[x]/E^x + E^x*Sin[x], x]

[Out] $-\text{Cos}[x]/(2*\text{E}^x) - (\text{E}^x*\text{Cos}[x])/2 - \text{Sin}[x]/(2*\text{E}^x) + (\text{E}^x*\text{Sin}[x])/2$

Rule 4432

Int[(F_)^((c_.)*((a_.) + (b_.)*(x_)))*Sin[(d_.) + (e_.)*(x_)], x_Symbol] :>
Simp[(b*c*Log[F]*F^(c*(a + b*x))*Sin[d + e*x])/(e^2 + b^2*c^2*Log[F]^2), x]
- Simp[(e*F^(c*(a + b*x))*Cos[d + e*x])/(e^2 + b^2*c^2*Log[F]^2), x] /; FreeQ[{F, a, b, c, d, e}, x] && NeQ[e^2 + b^2*c^2*Log[F]^2, 0]

Rubi steps

$$\begin{aligned} \int (e^{-x} \sin(x) + e^x \sin(x)) dx &= \int e^{-x} \sin(x) dx + \int e^x \sin(x) dx \\ &= -\frac{1}{2}e^{-x} \cos(x) - \frac{1}{2}e^x \cos(x) - \frac{1}{2}e^{-x} \sin(x) + \frac{1}{2}e^x \sin(x) \end{aligned}$$

Mathematica [A] time = 0.07, size = 33, normalized size = 0.80

$$-\frac{1}{2}e^x (e^{-2x} - 1) \sin(x) - \frac{1}{2}e^x (e^{-2x} + 1) \cos(x)$$

Antiderivative was successfully verified.

[In] Integrate[Sin[x]/E^x + E^x*Sin[x], x]

[Out] $-1/2*(\text{E}^x*(1 + \text{E}^{-2*x}))*\text{Cos}[x] - (\text{E}^x*(-1 + \text{E}^{-2*x}))*\text{Sin}[x])/2$

fricas [A] time = 0.58, size = 26, normalized size = 0.63

$$-\frac{1}{2} (\cos(x)e^{(2x)} - (e^{(2x)} - 1) \sin(x) + \cos(x))e^{(-x)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(sin(x)/exp(x)+exp(x)*sin(x), x, algorithm="fricas")

[Out] $-1/2*(\cos(x)*e^{(2*x)} - (e^{(2*x)} - 1)*\sin(x) + \cos(x))*e^{(-x)}$

giac [A] time = 0.12, size = 23, normalized size = 0.56

$$-\frac{1}{2} (\cos(x) + \sin(x))e^{(-x)} - \frac{1}{2} (\cos(x) - \sin(x))e^x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(sin(x)/exp(x)+exp(x)*sin(x),x, algorithm="giac")

[Out] -1/2*(cos(x) + sin(x))*e^(-x) - 1/2*(cos(x) - sin(x))*e^x

maple [A] time = 0.03, size = 30, normalized size = 0.73

$$-\frac{e^x \cos(x)}{2} + \frac{e^x \sin(x)}{2} - \frac{e^{-x} \cos(x)}{2} - \frac{e^{-x} \sin(x)}{2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(sin(x)/exp(x)+exp(x)*sin(x),x)

[Out] -1/2*exp(x)*cos(x)+1/2*exp(x)*sin(x)-1/2*exp(-x)*cos(x)-1/2*exp(-x)*sin(x)

maxima [A] time = 0.32, size = 23, normalized size = 0.56

$$-\frac{1}{2}(\cos(x) + \sin(x))e^{(-x)} - \frac{1}{2}(\cos(x) - \sin(x))e^x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(sin(x)/exp(x)+exp(x)*sin(x),x, algorithm="maxima")

[Out] -1/2*(cos(x) + sin(x))*e^(-x) - 1/2*(cos(x) - sin(x))*e^x

mupad [B] time = 2.41, size = 31, normalized size = 0.76

$$-e^{-x} \left(\frac{\cos(x)}{2} + \frac{\sin(x)}{2} + \frac{e^{2x} \cos(x)}{2} - \frac{e^{2x} \sin(x)}{2} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(exp(x)*sin(x) + exp(-x)*sin(x),x)

[Out] -exp(-x)*(cos(x)/2 + sin(x)/2 + (exp(2*x)*cos(x))/2 - (exp(2*x)*sin(x))/2)

sympy [A] time = 0.47, size = 32, normalized size = 0.78

$$\frac{e^x \sin(x)}{2} - \frac{e^x \cos(x)}{2} - \frac{e^{-x} \sin(x)}{2} - \frac{e^{-x} \cos(x)}{2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(sin(x)/exp(x)+exp(x)*sin(x),x)

[Out] exp(x)*sin(x)/2 - exp(x)*cos(x)/2 - exp(-x)*sin(x)/2 - exp(-x)*cos(x)/2

$$3.53 \quad \int \frac{F^{a+bx} \cos(c+dx)}{e+e \sin(c+dx)} dx$$

Optimal. Leaf size=82

$$\frac{iF^{a+bx}}{be \log(F)} - \frac{2iF^{a+bx} {}_2F_1\left(1, -\frac{ib \log(F)}{d}; 1 - \frac{ib \log(F)}{d}; ie^{i(c+dx)}\right)}{be \log(F)}$$

[Out] $I * F^{(b*x+a)}/b/e/\ln(F) - 2 * I * F^{(b*x+a)} * \text{hypergeom}([1, -I*b*\ln(F)/d], [1 - I*b*\ln(F)/d], I * \exp(I*(d*x+c)))/b/e/\ln(F)$

Rubi [A] time = 0.14, antiderivative size = 82, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 4, integrand size = 26, $\frac{\text{number of rules}}{\text{integrand size}} = 0.154$, Rules used = {4459, 4442, 2194, 2251}

$$\frac{iF^{a+bx}}{be \log(F)} - \frac{2iF^{a+bx} {}_2F_1\left(1, -\frac{ib \log(F)}{d}; 1 - \frac{ib \log(F)}{d}; ie^{i(c+dx)}\right)}{be \log(F)}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(F^{(a + b*x)} * \text{Cos}[c + d*x]) / (e + e * \text{Sin}[c + d*x]), x]$

[Out] $(I * F^{(a + b*x)}) / (b * e * \text{Log}[F]) - ((2 * I) * F^{(a + b*x)} * \text{Hypergeometric2F1}[1, ((-I) * b * \text{Log}[F]) / d, 1 - (I * b * \text{Log}[F]) / d, I * E^{(I * (c + d*x))}]) / (b * e * \text{Log}[F])$

Rule 2194

$\text{Int}[(F_{-})^{((c_{-}) * (a_{-}) + (b_{-}) * (x_{-}))}^{(n_{-})}, x_Symbol] \rightarrow \text{Simp}[(F^{(c*(a + b*x))})^n / (b*c*n*\text{Log}[F]), x] /;$ FreeQ[{F, a, b, c, n}, x]

Rule 2251

$\text{Int}[(a_{-}) + (b_{-}) * (F_{-})^{(e_{-}) * ((c_{-}) + (d_{-}) * (x_{-}))}^{(p_{-})} * (G_{-})^{(h_{-}) * ((f_{-}) + (g_{-}) * (x_{-}))}, x_Symbol] \rightarrow \text{Simp}[(a^p * G^{h*(f + g*x)} * \text{Hypergeometric2F1}[-p, (g*h*\text{Log}[G]) / (d*e*\text{Log}[F]), (g*h*\text{Log}[G]) / (d*e*\text{Log}[F]) + 1, \text{Simplify}[-((b * F^{(e*(c + d*x))})/a)])] / (g*h*\text{Log}[G]), x] /;$ FreeQ[{F, G, a, b, c, d, e, f, g, h, p}, x] && (ILtQ[p, 0] || GtQ[a, 0])

Rule 4442

$\text{Int}[(F_{-})^{((c_{-}) * (a_{-}) + (b_{-}) * (x_{-}))} * \text{Tan}[(d_{-}) + (e_{-}) * (x_{-})]^{(n_{-})}, x_Symbol] \rightarrow \text{Dist}[I^n, \text{Int}[\text{ExpandIntegrand}[(F^{(c*(a + b*x))}) * (1 - E^{(2*I*(d + e*x))})^n] / (1 + E^{(2*I*(d + e*x))})^n, x], x] /;$ FreeQ[{F, a, b, c, d, e}, x] && IntegerQ[n]

Rule 4459

$\text{Int}[\text{Cos}[(d_{-}) + (e_{-}) * (x_{-})]^{(m_{-})} * (F_{-})^{((c_{-}) * (a_{-}) + (b_{-}) * (x_{-}))} * ((f_{-}) + (g_{-}) * \text{Sin}[(d_{-}) + (e_{-}) * (x_{-})])^{(n_{-})}, x_Symbol] \rightarrow \text{Dist}[g^n, \text{Int}[F^{(c*(a + b*x))} * \text{Tan}[(f*Pi)/(4*g) - d/2 - (e*x)/2]^m, x], x] /;$ FreeQ[{F, a, b, c, d, e, f, g}, x] && EqQ[f^2 - g^2, 0] && IntegersQ[m, n] && EqQ[m + n, 0]

Rubi steps

$$\begin{aligned}
\int \frac{F^{a+bx} \cos(c+dx)}{e+e \sin(c+dx)} dx &= -\frac{\int F^{a+bx} \tan\left(\frac{c}{2} - \frac{\pi}{4} + \frac{dx}{2}\right) dx}{e} \\
&= -\frac{i \int \left(-F^{a+bx} + \frac{2F^{a+bx}}{1+e^{2i\left(\frac{c}{2} - \frac{\pi}{4} + \frac{dx}{2}\right)}}\right) dx}{e} \\
&= \frac{i \int F^{a+bx} dx}{e} - \frac{(2i) \int \frac{F^{a+bx}}{1+e^{2i\left(\frac{c}{2} - \frac{\pi}{4} + \frac{dx}{2}\right)}} dx}{e} \\
&= \frac{iF^{a+bx}}{be \log(F)} - \frac{2iF^{a+bx} {}_2F_1\left(1, -\frac{ib \log(F)}{d}; 1 - \frac{ib \log(F)}{d}; ie^{i(c+dx)}\right)}{be \log(F)}
\end{aligned}$$

Mathematica [A] time = 2.55, size = 64, normalized size = 0.78

$$\frac{iF^{a+bx} \left(-1 + 2 {}_2F_1\left(1, -\frac{ib \log(F)}{d}; 1 - \frac{ib \log(F)}{d}; ie^{i(c+dx)}\right)\right)}{be \log(F)}$$

Antiderivative was successfully verified.

[In] Integrate[(F^(a + b*x)*Cos[c + d*x])/(e + e*Sin[c + d*x]),x]

[Out] ((-I)*F^(a + b*x)*(-1 + 2*Hypergeometric2F1[1, ((-I)*b*Log[F])/d, 1 - (I*b*Log[F])/d, I*E^(I*(c + d*x))]))/(b*e*Log[F])

fricas [F] time = 0.77, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{F^{bx+a} \cos(dx+c)}{e \sin(dx+c) + e}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(F^(b*x+a)*cos(d*x+c)/(e+e*sin(d*x+c)),x, algorithm="fricas")

[Out] integral(F^(b*x + a)*cos(d*x + c)/(e*sin(d*x + c) + e), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{F^{bx+a} \cos(dx+c)}{e \sin(dx+c) + e} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(F^(b*x+a)*cos(d*x+c)/(e+e*sin(d*x+c)),x, algorithm="giac")

[Out] integrate(F^(b*x + a)*cos(d*x + c)/(e*sin(d*x + c) + e), x)

maple [F] time = 0.37, size = 0, normalized size = 0.00

$$\int \frac{F^{bx+a} \cos(dx+c)}{e + e \sin(dx+c)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(F^(b*x+a)*cos(d*x+c)/(e+e*sin(d*x+c)),x)

[Out] int(F^(b*x+a)*cos(d*x+c)/(e+e*sin(d*x+c)),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$2F^{bx}F^a b d \cos(dx + c) \log(F) + 2F^{bx}F^a d^2 \sin(dx + c) + (F^a b^2 \log(F)^2 + F^a d^2)F^{bx} \cos(dx + c)^2 + (F^a b^2 \log(F)$$

$(b^3 \log(F)$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(F^(b*x+a)*cos(d*x+c)/(e+e*sin(d*x+c)),x, algorithm="maxima")

[Out] $-(2F^{(b*x)}F^{a*b*d}\cos(d*x + c)\log(F) + 2F^{(b*x)}F^{a*d^2}\sin(d*x + c) + (F^{a*b^2}\log(F)^2 + F^{a*d^2})F^{(b*x)}\cos(d*x + c)^2 + (F^{a*b^2}\log(F)^2 + F^{a*d^2})F^{(b*x)}\sin(d*x + c)^2 - (F^{a*b^2}\log(F)^2 - F^{a*d^2})F^{(b*x)} - 2((F^{a*b^3*d}\log(F)^3 + F^{a*b*d^3}\log(F))e\cos(d*x + c)^2 + (F^{a*b^3*d}\log(F)^3 + F^{a*b*d^3}\log(F))e\sin(d*x + c)^2 + 2*(F^{a*b^3*d}\log(F)^3 + F^{a*b*d^3}\log(F))e*\int \text{rate}((2F^{(b*x)}*b*\cos(2*d*x + 2*c)\log(F) + F^{(b*x)}*b*\log(F)*\sin(2*d*x + 2*c) - F^{(b*x)}*d*\cos(2*d*x + 2*c) + 2F^{(b*x)}*d*\sin(d*x + c) + F^{(b*x)}*d)/(b^2*\log(F)^2 + d^2)*e*\cos(2*d*x + 2*c)^2 + 4*(b^2*\log(F)^2 + d^2)*e*\cos(d*x + c)^2 + 4*(b^2*\log(F)^2 + d^2)*e*\cos(d*x + c)*\sin(2*d*x + 2*c) + (b^2*\log(F)^2 + d^2)*e*\sin(2*d*x + 2*c)^2 + 4*(b^2*\log(F)^2 + d^2)*e*\sin(d*x + c)^2 + 4*(b^2*\log(F)^2 + d^2)*e*\sin(d*x + c) + (b^2*\log(F)^2 + d^2)*e - 2*(2*(b^2*\log(F)^2 + d^2)*e*\sin(d*x + c) + (b^2*\log(F)^2 + d^2)*e)*\cos(2*d*x + 2*c)), x))/((b^3*\log(F)^3 + b*d^2*\log(F))e*\cos(d*x + c)^2 + (b^3*\log(F)^3 + b*d^2*\log(F))e*\sin(d*x + c)^2 + 2*(b^3*\log(F)^3 + b*d^2*\log(F))e*\sin(d*x + c) + (b^3*\log(F)^3 + b*d^2*\log(F))e)$

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{F^{a+bx} \cos(c + dx)}{e + e \sin(c + dx)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((F^(a + b*x)*cos(c + d*x))/(e + e*sin(c + d*x)),x)

[Out] int((F^(a + b*x)*cos(c + d*x))/(e + e*sin(c + d*x)), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\frac{\int \frac{F^a F^{bx} \cos(c+dx)}{\sin(c+dx)+1} dx}{e}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(F**(b*x+a)*cos(d*x+c)/(e+e*sin(d*x+c)),x)

[Out] Integral(F**a*F**(b*x)*cos(c + d*x)/(sin(c + d*x) + 1), x)/e

$$3.54 \quad \int \frac{F^{a+bx} \cos(c+dx)}{e-e \sin(c+dx)} dx$$

Optimal. Leaf size=82

$$\frac{2iF^{a+bx} {}_2F_1\left(1, -\frac{ib \log(F)}{d}; 1 - \frac{ib \log(F)}{d}; -ie^{i(c+dx)}\right)}{be \log(F)} - \frac{iF^{a+bx}}{be \log(F)}$$

[Out] $-I * F^{(b * x + a)} / b / e / \ln(F) + 2 * I * F^{(b * x + a)} * \text{hypergeom}([1, -I * b * \ln(F) / d], [1 - I * b * \ln(F) / d], -I * \exp(I * (d * x + c))) / b / e / \ln(F)$

Rubi [A] time = 0.13, antiderivative size = 82, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 4, integrand size = 27, $\frac{\text{number of rules}}{\text{integrand size}} = 0.148$, Rules used = {4459, 4442, 2194, 2251}

$$\frac{2iF^{a+bx} {}_2F_1\left(1, -\frac{ib \log(F)}{d}; 1 - \frac{ib \log(F)}{d}; -ie^{i(c+dx)}\right)}{be \log(F)} - \frac{iF^{a+bx}}{be \log(F)}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(F^{(a + b * x)} * \text{Cos}[c + d * x]) / (e - e * \text{Sin}[c + d * x]), x]$

[Out] $((-I) * F^{(a + b * x)}) / (b * e * \text{Log}[F]) + ((2 * I) * F^{(a + b * x)} * \text{Hypergeometric2F1}[1, (-I) * b * \text{Log}[F] / d, 1 - (I * b * \text{Log}[F]) / d, (-I) * E^{(I * (c + d * x))}] / (b * e * \text{Log}[F])$

Rule 2194

$\text{Int}[(F^{((c_.) * ((a_.) + (b_.) * (x_))))^{(n_.)}, x_Symbol] :> \text{Simp}[F^{(c * (a + b * x))} / (b * c * n * \text{Log}[F]), x] /;$ $\text{FreeQ}\{F, a, b, c, n\}, x]$

Rule 2251

$\text{Int}[(a_.) + (b_.) * (F^{(e_.) * ((c_.) + (d_.) * (x_))))^{(p_.)} * (G_.)^{(h_.)} * ((f_.) + (g_.) * (x_)), x_Symbol] :> \text{Simp}[(a^{p_} * G^{(h * (f + g * x))} * \text{Hypergeometric2F1}[-p, (g * h * \text{Log}[G]) / (d * e * \text{Log}[F]), (g * h * \text{Log}[G]) / (d * e * \text{Log}[F]) + 1, \text{Simplify}[-(b * F^{(e * (c + d * x))}) / a]]) / (g * h * \text{Log}[G]), x] /;$ $\text{FreeQ}\{F, G, a, b, c, d, e, f, g, h, p\}, x] \&\& (\text{ILtQ}[p, 0] \mid \mid \text{GtQ}[a, 0])$

Rule 4442

$\text{Int}[(F^{((c_.) * ((a_.) + (b_.) * (x_)))) * \text{Tan}[(d_.) + (e_.) * (x_)]^{(n_.)}, x_Symbol] :> \text{Dist}[I^{n_}, \text{Int}[\text{ExpandIntegrand}[F^{(c * (a + b * x))} * (1 - E^{(2 * I * (d + e * x))})^{(n_)} / (1 + E^{(2 * I * (d + e * x))})^{(n_)}, x], x] /;$ $\text{FreeQ}\{F, a, b, c, d, e\}, x] \&\& \text{IntegerQ}[n]$

Rule 4459

$\text{Int}[\text{Cos}[(d_.) + (e_.) * (x_)]^{(m_.)} * (F^{((c_.) * ((a_.) + (b_.) * (x_)))) * ((f_.) + (g_.) * \text{Sin}[(d_.) + (e_.) * (x_)]^{(n_.)}, x_Symbol] :> \text{Dist}[g^{n_}, \text{Int}[F^{(c * (a + b * x))} * \text{Tan}[(f * \text{Pi}) / (4 * g) - d / 2 - (e * x) / 2]^{(m_)}, x] /;$ $\text{FreeQ}\{F, a, b, c, d, e, f, g\}, x] \&\& \text{EqQ}[f^2 - g^2, 0] \&\& \text{IntegersQ}[m, n] \&\& \text{EqQ}[m + n, 0]$

Rubi steps

$$\begin{aligned}
\int \frac{F^{a+bx} \cos(c+dx)}{e - e \sin(c+dx)} dx &= \frac{\int F^{a+bx} \tan\left(\frac{c}{2} + \frac{\pi}{4} + \frac{dx}{2}\right) dx}{e} \\
&= \frac{i \int \left(-F^{a+bx} + \frac{2F^{a+bx}}{1+e^{2i\left(\frac{c}{2} + \frac{\pi}{4} + \frac{dx}{2}\right)}} \right) dx}{e} \\
&= -\frac{i \int F^{a+bx} dx}{e} + \frac{(2i) \int \frac{F^{a+bx}}{1+e^{2i\left(\frac{c}{2} + \frac{\pi}{4} + \frac{dx}{2}\right)}} dx}{e} \\
&= -\frac{iF^{a+bx}}{be \log(F)} + \frac{2iF^{a+bx} {}_2F_1\left(1, -\frac{ib \log(F)}{d}; 1 - \frac{ib \log(F)}{d}; -ie^{i(c+dx)}\right)}{be \log(F)}
\end{aligned}$$

Mathematica [A] time = 2.64, size = 64, normalized size = 0.78

$$\frac{iF^{a+bx} \left(-1 + 2 {}_2F_1\left(1, -\frac{ib \log(F)}{d}; 1 - \frac{ib \log(F)}{d}; -ie^{i(c+dx)}\right) \right)}{be \log(F)}$$

Antiderivative was successfully verified.

[In] Integrate[(F^(a + b*x)*Cos[c + d*x])/(e - e*Sin[c + d*x]),x]

[Out] (I*F^(a + b*x)*(-1 + 2*Hypergeometric2F1[1, ((-I)*b*Log[F])/d, 1 - (I*b*Log[F])/d, (-I)*E^(I*(c + d*x))]))/(b*e*Log[F])

fricas [F] time = 0.75, size = 0, normalized size = 0.00

$$\text{integral}\left(-\frac{F^{bx+a} \cos(dx+c)}{e \sin(dx+c) - e}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(F^(b*x+a)*cos(d*x+c)/(e-e*sin(d*x+c)),x, algorithm="fricas")

[Out] integral(-F^(b*x + a)*cos(d*x + c)/(e*sin(d*x + c) - e), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int -\frac{F^{bx+a} \cos(dx+c)}{e \sin(dx+c) - e} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(F^(b*x+a)*cos(d*x+c)/(e-e*sin(d*x+c)),x, algorithm="giac")

[Out] integrate(-F^(b*x + a)*cos(d*x + c)/(e*sin(d*x + c) - e), x)

maple [F] time = 0.37, size = 0, normalized size = 0.00

$$\int \frac{F^{bx+a} \cos(dx+c)}{e - e \sin(dx+c)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(F^(b*x+a)*cos(d*x+c)/(e-e*sin(d*x+c)),x)

[Out] int(F^(b*x+a)*cos(d*x+c)/(e-e*sin(d*x+c)),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\frac{2 F^{bx} F^a b d \cos(dx + c) \log(F) + 2 F^{bx} F^a d^2 \sin(dx + c) - (F^a b^2 \log(F)^2 + F^a d^2) F^{bx} \cos(dx + c)^2 - (F^a b^2 \log(F)^2 + F^a d^2) F^{bx} \sin(dx + c)^2}{(b^3 \log(F))^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(F^(b*x+a)*cos(d*x+c)/(e-e*sin(d*x+c)),x, algorithm="maxima")

[Out] $-(2 F^{(b x)} F^{a b d} \cos(d x + c) \log(F) + 2 F^{(b x)} F^{a d^2} \sin(d x + c) - (F^{a b^2} \log(F)^2 + F^{a d^2}) F^{(b x)} \cos(d x + c)^2 - (F^{a b^2} \log(F)^2 + F^{a d^2}) F^{(b x)} \sin(d x + c)^2 + (F^{a b^2} \log(F)^2 - F^{a d^2}) F^{(b x)} + 2 * ((F^{a b^3} d \log(F)^3 + F^{a b d^3} \log(F)) * e * \cos(d x + c)^2 + (F^{a b^3} d \log(F)^3 + F^{a b d^3} \log(F)) * e * \sin(d x + c)^2 - 2 * (F^{a b^3} d \log(F)^3 + F^{a b d^3} \log(F)) * e) * \int (-2 F^{(b x)} * b * \cos(d x + c) * \log(F) - F^{(b x)} * b * \log(F) * \sin(2 d x + 2 c) + F^{(b x)} * d * \cos(2 d x + 2 c) + 2 F^{(b x)} * d * \sin(d x + c) - F^{(b x)} * d) / ((b^2 * \log(F)^2 + d^2) * e * \cos(2 d x + 2 c)^2 + 4 * (b^2 * \log(F)^2 + d^2) * e * \cos(d x + c)^2 - 4 * (b^2 * \log(F)^2 + d^2) * e * \cos(d x + c) * \sin(2 d x + 2 c) + (b^2 * \log(F)^2 + d^2) * e * \sin(2 d x + 2 c)^2 + 4 * (b^2 * \log(F)^2 + d^2) * e * \sin(d x + c)^2 - 4 * (b^2 * \log(F)^2 + d^2) * e * \sin(d x + c) + (b^2 * \log(F)^2 + d^2) * e + 2 * (2 * (b^2 * \log(F)^2 + d^2) * e * \sin(d x + c) - (b^2 * \log(F)^2 + d^2) * e) * \cos(2 d x + 2 c)), x) / ((b^3 * \log(F)^3 + b * d^2 * \log(F)) * e * \cos(d x + c)^2 + (b^3 * \log(F)^3 + b * d^2 * \log(F)) * e * \sin(d x + c)^2 - 2 * (b^3 * \log(F)^3 + b * d^2 * \log(F)) * e * \sin(d x + c) + (b^3 * \log(F)^3 + b * d^2 * \log(F)) * e)$

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{F^{a+bx} \cos(c+dx)}{e - e \sin(c+dx)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((F^(a + b*x)*cos(c + d*x))/(e - e*sin(c + d*x)),x)

[Out] int((F^(a + b*x)*cos(c + d*x))/(e - e*sin(c + d*x)), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\frac{\int \frac{F^a F^{bx} \cos(c+dx)}{\sin(c+dx)-1} dx}{e}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(F**(b*x+a)*cos(d*x+c)/(e-e*sin(d*x+c)),x)

[Out] -Integral(F**a*F**(b*x)*cos(c + d*x)/(sin(c + d*x) - 1), x)/e

$$3.55 \quad \int \frac{F^{a+bx} \sin(c+dx)}{e+e \cos(c+dx)} dx$$

Optimal. Leaf size=80

$$\frac{2iF^{a+bx} {}_2F_1\left(1, -\frac{ib \log(F)}{d}; 1 - \frac{ib \log(F)}{d}; -e^{i(c+dx)}\right)}{be \log(F)} - \frac{iF^{a+bx}}{be \log(F)}$$

[Out] $-I * F^{(b*x+a)}/b/e/\ln(F) + 2 * I * F^{(b*x+a)} * \text{hypergeom}([1, -I * b * \ln(F)/d], [1 - I * b * \ln(F)/d], -\exp(I * (d*x+c)))/b/e/\ln(F)$

Rubi [A] time = 0.12, antiderivative size = 80, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 4, integrand size = 26, $\frac{\text{number of rules}}{\text{integrand size}} = 0.154$, Rules used = {4460, 4442, 2194, 2251}

$$\frac{2iF^{a+bx} {}_2F_1\left(1, -\frac{ib \log(F)}{d}; 1 - \frac{ib \log(F)}{d}; -e^{i(c+dx)}\right)}{be \log(F)} - \frac{iF^{a+bx}}{be \log(F)}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(F^{(a + b*x)} * \text{Sin}[c + d*x]) / (e + e * \text{Cos}[c + d*x]), x]$

[Out] $((-I) * F^{(a + b*x)}) / (b * e * \text{Log}[F]) + ((2 * I) * F^{(a + b*x)} * \text{Hypergeometric2F1}[1, (-I) * b * \text{Log}[F]/d, 1 - (I * b * \text{Log}[F])/d, -E^{(I * (c + d*x))}]) / (b * e * \text{Log}[F])$

Rule 2194

$\text{Int}[(F^{((c_.) * (a_.) + (b_.) * (x_)))})^{(n_.)}, x_Symbol] \rightarrow \text{Simp}[(F^{(c * (a + b * x))})^{(n)} / (b * c * n * \text{Log}[F]), x] /;$ FreeQ[{F, a, b, c, n}, x]

Rule 2251

$\text{Int}[(a_.) + (b_.) * (F^{(e_.) * (c_.) + (d_.) * (x_)))})^{(p_.)} * (G_.)^{(h_.) * (f_.) + (g_.) * (x_))}, x_Symbol] \rightarrow \text{Simp}[(a^{p * G^{(h * (f + g * x))}} * \text{Hypergeometric2F1}[-p, (g * h * \text{Log}[G]) / (d * e * \text{Log}[F]), (g * h * \text{Log}[G]) / (d * e * \text{Log}[F]) + 1, \text{Simplify}[-(b * F^{(e * (c + d * x))}) / a]]) / (g * h * \text{Log}[G]), x] /;$ FreeQ[{F, G, a, b, c, d, e, f, g, h, p}, x] && (ILtQ[p, 0] || GtQ[a, 0])

Rule 4442

$\text{Int}[(F^{(c_.) * (a_.) + (b_.) * (x_))}) * \text{Tan}[(d_.) + (e_.) * (x_)]^{(n_.)}, x_Symbol] \rightarrow \text{Dist}[I^n, \text{Int}[\text{ExpandIntegrand}[(F^{(c * (a + b * x))}) * (1 - E^{(2 * I * (d + e * x))})^{(n)}] / (1 + E^{(2 * I * (d + e * x))})^{(n)}, x], x] /;$ FreeQ[{F, a, b, c, d, e}, x] && IntegerQ[n]

Rule 4460

$\text{Int}[(\text{Cos}[(d_.) + (e_.) * (x_)] * (g_.) + (f_.))^{(n_.)} * (F^{(c_.) * (a_.) + (b_.) * (x_))}) * \text{Sin}[(d_.) + (e_.) * (x_)]^{(m_.)}, x_Symbol] \rightarrow \text{Dist}[f^n, \text{Int}[F^{(c * (a + b * x))} * \text{Tan}[d/2 + (e * x)/2]^{(m)}, x] /;$ FreeQ[{F, a, b, c, d, e, f, g}, x] && EqQ[f - g, 0] && IntegersQ[m, n] && EqQ[m + n, 0]

Rubi steps

$$\begin{aligned}
\int \frac{F^{a+bx} \sin(c+dx)}{e+e \cos(c+dx)} dx &= \frac{\int F^{a+bx} \tan\left(\frac{c}{2} + \frac{dx}{2}\right) dx}{e} \\
&= \frac{i \int \left(-F^{a+bx} + \frac{2F^{a+bx}}{1+e^{2i\left(\frac{c}{2} + \frac{dx}{2}\right)}} \right) dx}{e} \\
&= -\frac{i \int F^{a+bx} dx}{e} + \frac{(2i) \int \frac{F^{a+bx}}{1+e^{2i\left(\frac{c}{2} + \frac{dx}{2}\right)}} dx}{e} \\
&= -\frac{iF^{a+bx}}{be \log(F)} + \frac{2iF^{a+bx} {}_2F_1\left(1, -\frac{ib \log(F)}{d}; 1 - \frac{ib \log(F)}{d}; -e^{i(c+dx)}\right)}{be \log(F)}
\end{aligned}$$

Mathematica [A] time = 0.67, size = 68, normalized size = 0.85

$$\frac{iF^{a+bx} \left(-1 + 2 {}_2F_1\left(1, -\frac{ib \log(F)}{d}; 1 - \frac{ib \log(F)}{d}; -\cos(c+dx) - i \sin(c+dx)\right) \right)}{be \log(F)}$$

Antiderivative was successfully verified.

[In] Integrate[(F^(a + b*x)*Sin[c + d*x])/(e + e*Cos[c + d*x]),x]

[Out] (I*F^(a + b*x)*(-1 + 2*Hypergeometric2F1[1, ((-I)*b*Log[F])/d, 1 - (I*b*Log[F])/d, -Cos[c + d*x] - I*Sin[c + d*x]]))/(b*e*Log[F])

fricas [F] time = 0.68, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{F^{bx+a} \sin(dx+c)}{e \cos(dx+c) + e}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(F^(b*x+a)*sin(d*x+c)/(e+e*cos(d*x+c)),x, algorithm="fricas")

[Out] integral(F^(b*x + a)*sin(d*x + c)/(e*cos(d*x + c) + e), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{F^{bx+a} \sin(dx+c)}{e \cos(dx+c) + e} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(F^(b*x+a)*sin(d*x+c)/(e+e*cos(d*x+c)),x, algorithm="giac")

[Out] integrate(F^(b*x + a)*sin(d*x + c)/(e*cos(d*x + c) + e), x)

maple [F] time = 0.16, size = 0, normalized size = 0.00

$$\int \frac{F^{bx+a} \sin(dx+c)}{e + e \cos(dx+c)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(F^(b*x+a)*sin(d*x+c)/(e+e*cos(d*x+c)),x)

[Out] int(F^(b*x+a)*sin(d*x+c)/(e+e*cos(d*x+c)),x)

maxima [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(F^(b*x+a)*sin(d*x+c)/(e+e*cos(d*x+c)),x, algorithm="maxima")

[Out] Timed out

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{F^{a+bx} \sin(c+dx)}{e+e \cos(c+dx)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((F^(a + b*x)*sin(c + d*x))/(e + e*cos(c + d*x)),x)

[Out] int((F^(a + b*x)*sin(c + d*x))/(e + e*cos(c + d*x)), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\frac{\int \frac{F^a F^{bx} \sin(c+dx)}{\cos(c+dx)+1} dx}{e}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(F**(b*x+a)*sin(d*x+c)/(e+e*cos(d*x+c)),x)

[Out] Integral(F**a*F**(b*x)*sin(c + d*x)/(cos(c + d*x) + 1), x)/e

$$3.56 \quad \int \frac{F^{a+bx} \sin(c+dx)}{e-e \cos(c+dx)} dx$$

Optimal. Leaf size=78

$$\frac{iF^{a+bx}}{be \log(F)} - \frac{2iF^{a+bx} {}_2F_1\left(1, -\frac{ib \log(F)}{d}; 1 - \frac{ib \log(F)}{d}; e^{i(c+dx)}\right)}{be \log(F)}$$

[Out] $I * F^{(b * x + a) / b / e / \ln(F) - 2 * I * F^{(b * x + a)} * \text{hypergeom}([1, -I * b * \ln(F) / d], [1 - I * b * \ln(F) / d], \exp(I * (d * x + c))) / b / e / \ln(F)$

Rubi [A] time = 0.12, antiderivative size = 78, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 4, integrand size = 27, $\frac{\text{number of rules}}{\text{integrand size}} = 0.148$, Rules used = {4461, 4443, 2194, 2251}

$$\frac{iF^{a+bx}}{be \log(F)} - \frac{2iF^{a+bx} {}_2F_1\left(1, -\frac{ib \log(F)}{d}; 1 - \frac{ib \log(F)}{d}; e^{i(c+dx)}\right)}{be \log(F)}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(F^{(a + b * x)} * \text{Sin}[c + d * x]) / (e - e * \text{Cos}[c + d * x]), x]$

[Out] $(I * F^{(a + b * x)}) / (b * e * \text{Log}[F]) - ((2 * I) * F^{(a + b * x)} * \text{Hypergeometric2F1}[1, ((-I) * b * \text{Log}[F]) / d, 1 - (I * b * \text{Log}[F]) / d, E^{(I * (c + d * x))}]) / (b * e * \text{Log}[F])$

Rule 2194

$\text{Int}[(F^{((c_.) * ((a_.) + (b_.) * (x_.)))})^{(n_.)}, x_Symbol] \rightarrow \text{Simp}[F^{(c * (a + b * x))})^n / (b * c * n * \text{Log}[F]), x] /;$ $\text{FreeQ}\{F, a, b, c, n\}, x]$

Rule 2251

$\text{Int}[(a_. + (b_.) * (F^{(e_.) * ((c_.) + (d_.) * (x_.))})^{(p_.)} * (G^{(h_.) * ((f_.) + (g_.) * (x_.))})^{(q_.)}), x_Symbol] \rightarrow \text{Simp}[(a^p * G^{(h * (f + g * x))} * \text{Hypergeometric2F1}[-p, (g * h * \text{Log}[G]) / (d * e * \text{Log}[F]), (g * h * \text{Log}[G]) / (d * e * \text{Log}[F]) + 1, \text{Simplify}[-((b * F^{(e * (c + d * x))}) / a])]) / (g * h * \text{Log}[G]), x] /;$ $\text{FreeQ}\{F, G, a, b, c, d, e, f, g, h, p\}, x]$ && $(\text{ILtQ}[p, 0] \mid \mid \text{GtQ}[a, 0])$

Rule 4443

$\text{Int}[\text{Cot}[(d_.) + (e_.) * (x_.)]^{(n_.)} * (F^{(c_.) * ((a_.) + (b_.) * (x_.))})^{(m_.)}, x_Symbol] \rightarrow \text{Dist}[(-I)^n, \text{Int}[\text{ExpandIntegrand}[F^{(c * (a + b * x))} * (1 + E^{(2 * I * (d + e * x))})^n] / (1 - E^{(2 * I * (d + e * x))})^n, x], x] /;$ $\text{FreeQ}\{F, a, b, c, d, e\}, x]$ && $\text{IntegerQ}[n]$

Rule 4461

$\text{Int}[(\text{Cos}[(d_.) + (e_.) * (x_.)] * (g_.) + (f_.))^{(n_.)} * (F^{(c_.) * ((a_.) + (b_.) * (x_.))})^{(m_.)} * \text{Sin}[(d_.) + (e_.) * (x_.)]^{(m_.)}, x_Symbol] \rightarrow \text{Dist}[f^n, \text{Int}[F^{(c * (a + b * x))} * \text{Cot}[d / 2 + (e * x) / 2]^m, x], x] /;$ $\text{FreeQ}\{F, a, b, c, d, e, f, g\}, x]$ & $\text{EqQ}[f + g, 0]$ && $\text{IntegersQ}[m, n]$ && $\text{EqQ}[m + n, 0]$

Rubi steps

$$\begin{aligned}
\int \frac{F^{a+bx} \sin(c+dx)}{e - e \cos(c+dx)} dx &= \frac{\int F^{a+bx} \cot\left(\frac{c}{2} + \frac{dx}{2}\right) dx}{e} \\
&= \frac{i \int \left(-F^{a+bx} - \frac{2F^{a+bx}}{-1+e^{2i\left(\frac{c}{2} + \frac{dx}{2}\right)}} \right) dx}{e} \\
&= \frac{i \int F^{a+bx} dx}{e} + \frac{(2i) \int \frac{F^{a+bx}}{-1+e^{2i\left(\frac{c}{2} + \frac{dx}{2}\right)}} dx}{e} \\
&= \frac{iF^{a+bx}}{be \log(F)} - \frac{2iF^{a+bx} {}_2F_1\left(1, -\frac{ib \log(F)}{d}; 1 - \frac{ib \log(F)}{d}; e^{i(c+dx)}\right)}{be \log(F)}
\end{aligned}$$

Mathematica [A] time = 0.63, size = 66, normalized size = 0.85

$$-\frac{iF^{a+bx} \left(-1 + 2 {}_2F_1\left(1, -\frac{ib \log(F)}{d}; 1 - \frac{ib \log(F)}{d}; \cos(c+dx) + i \sin(c+dx)\right) \right)}{be \log(F)}$$

Antiderivative was successfully verified.

[In] Integrate[(F^(a + b*x)*Sin[c + d*x])/(e - e*Cos[c + d*x]),x]

[Out] (((-I)*F^(a + b*x)*(-1 + 2*Hypergeometric2F1[1, ((-I)*b*Log[F])/d, 1 - (I*b*Log[F])/d, Cos[c + d*x] + I*Sin[c + d*x]])))/(b*e*Log[F])

fricas [F] time = 0.71, size = 0, normalized size = 0.00

$$\text{integral}\left(-\frac{F^{bx+a} \sin(dx+c)}{e \cos(dx+c) - e}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(F^(b*x+a)*sin(d*x+c)/(e-e*cos(d*x+c)),x, algorithm="fricas")

[Out] integral(-F^(b*x + a)*sin(d*x + c)/(e*cos(d*x + c) - e), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int -\frac{F^{bx+a} \sin(dx+c)}{e \cos(dx+c) - e} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(F^(b*x+a)*sin(d*x+c)/(e-e*cos(d*x+c)),x, algorithm="giac")

[Out] integrate(-F^(b*x + a)*sin(d*x + c)/(e*cos(d*x + c) - e), x)

maple [F] time = 0.19, size = 0, normalized size = 0.00

$$\int \frac{F^{bx+a} \sin(dx+c)}{e - e \cos(dx+c)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(F^(b*x+a)*sin(d*x+c)/(e-e*cos(d*x+c)),x)

[Out] int(F^(b*x+a)*sin(d*x+c)/(e-e*cos(d*x+c)),x)

maxima [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(F^(b*x+a)*sin(d*x+c)/(e-e*cos(d*x+c)),x, algorithm="maxima")

[Out] Timed out

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{F^{a+bx} \sin(c+dx)}{e - e \cos(c+dx)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((F^(a + b*x)*sin(c + d*x))/(e - e*cos(c + d*x)),x)

[Out] int((F^(a + b*x)*sin(c + d*x))/(e - e*cos(c + d*x)), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$-\frac{\int \frac{F^a F^{bx} \sin(c+dx)}{\cos(c+dx)-1} dx}{e}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(F**(b*x+a)*sin(d*x+c)/(e-e*cos(d*x+c)),x)

[Out] -Integral(F**a*F**(b*x)*sin(c + d*x)/(cos(c + d*x) - 1), x)/e

3.57 $\int e^{x^2} \sin(bx) dx$

Optimal. Leaf size=69

$$\frac{1}{4}i\sqrt{\pi}e^{\frac{b^2}{4}}\operatorname{erfi}\left(\frac{1}{2}(2x-ib)\right) - \frac{1}{4}i\sqrt{\pi}e^{\frac{b^2}{4}}\operatorname{erfi}\left(\frac{1}{2}(2x+ib)\right)$$

[Out] $-1/4*I*\exp(1/4*b^2)*\operatorname{erfi}(1/2*I*b-x)*\operatorname{Pi}^{(1/2)} - 1/4*I*\exp(1/4*b^2)*\operatorname{erfi}(1/2*I*b+x)*\operatorname{Pi}^{(1/2)}$

Rubi [A] time = 0.05, antiderivative size = 69, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 3, integrand size = 10, $\frac{\text{number of rules}}{\text{integrand size}} = 0.300$, Rules used = {4472, 2234, 2204}

$$\frac{1}{4}i\sqrt{\pi}e^{\frac{b^2}{4}}\operatorname{Erfi}\left(\frac{1}{2}(2x-ib)\right) - \frac{1}{4}i\sqrt{\pi}e^{\frac{b^2}{4}}\operatorname{Erfi}\left(\frac{1}{2}(2x+ib)\right)$$

Antiderivative was successfully verified.

[In] Int[E^x^2*Sin[b*x],x]

[Out] $(I/4)*E^{(b^2/4)}*\operatorname{Sqrt}[\operatorname{Pi}]*\operatorname{Erfi}[((-I)*b + 2*x)/2] - (I/4)*E^{(b^2/4)}*\operatorname{Sqrt}[\operatorname{Pi}]*\operatorname{Erfi}[(I*b + 2*x)/2]$

Rule 2204

Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_)) ^2), x_Symbol] := Simp[(F^a*Sqrt[Pi]*Erfi[(c + d*x)*Rt[b*Log[F], 2]])/(2*d*Rt[b*Log[F], 2]), x] /; FreeQ[{F, a, b, c, d}, x] && PosQ[b]

Rule 2234

Int[(F_)^((a_.) + (b_.)*(x_) + (c_.)*(x_) ^2), x_Symbol] := Dist[F^(a - b^2/(4*c)), Int[F^((b + 2*c*x)^2/(4*c)), x], x] /; FreeQ[{F, a, b, c}, x]

Rule 4472

Int[(F_)^(u_)*Sin[v_]^(n_), x_Symbol] := Int[ExpandTrigToExp[F^u, Sin[v]^n, x], x] /; FreeQ[F, x] && (LinearQ[u, x] || PolyQ[u, x, 2]) && (LinearQ[v, x] || PolyQ[v, x, 2]) && IGtQ[n, 0]

Rubi steps

$$\begin{aligned} \int e^{x^2} \sin(bx) dx &= \int \left(\frac{1}{2}ie^{-ibx+x^2} - \frac{1}{2}ie^{ibx+x^2} \right) dx \\ &= \frac{1}{2}i \int e^{-ibx+x^2} dx - \frac{1}{2}i \int e^{ibx+x^2} dx \\ &= \frac{1}{2} \left(ie^{\frac{b^2}{4}} \right) \int e^{\frac{1}{4}(-ib+2x)^2} dx - \frac{1}{2} \left(ie^{\frac{b^2}{4}} \right) \int e^{\frac{1}{4}(ib+2x)^2} dx \\ &= \frac{1}{4}ie^{\frac{b^2}{4}}\sqrt{\pi}\operatorname{erfi}\left(\frac{1}{2}(-ib+2x)\right) - \frac{1}{4}ie^{\frac{b^2}{4}}\sqrt{\pi}\operatorname{erfi}\left(\frac{1}{2}(ib+2x)\right) \end{aligned}$$

Mathematica [A] time = 0.03, size = 43, normalized size = 0.62

$$\frac{1}{4}\sqrt{\pi}e^{\frac{b^2}{4}}\left(\operatorname{erf}\left(\frac{b}{2}-ix\right)+\operatorname{erf}\left(\frac{b}{2}+ix\right)\right)$$

Antiderivative was successfully verified.

[In] Integrate[E^x^2*Sin[b*x],x]

[Out] (E^(b^2/4)*Sqrt[Pi]*(Erf[b/2 - I*x] + Erf[b/2 + I*x]))/4

fricas [A] time = 0.67, size = 30, normalized size = 0.43

$$\frac{1}{4} \sqrt{\pi} \left(\operatorname{erf} \left(\frac{1}{2} b + ix \right) - \operatorname{erf} \left(-\frac{1}{2} b + ix \right) \right) e^{\left(\frac{1}{4} b^2 \right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(x^2)*sin(b*x),x, algorithm="fricas")

[Out] 1/4*sqrt(pi)*(erf(1/2*b + I*x) - erf(-1/2*b + I*x))*e^(1/4*b^2)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int e^{x^2} \sin(bx) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(x^2)*sin(b*x),x, algorithm="giac")

[Out] integrate(e^(x^2)*sin(b*x), x)

maple [A] time = 0.12, size = 42, normalized size = 0.61

$$\frac{\sqrt{\pi} e^{\frac{b^2}{4}} \operatorname{erf} \left(-ix + \frac{b}{2} \right)}{4} + \frac{\sqrt{\pi} e^{\frac{b^2}{4}} \operatorname{erf} \left(ix + \frac{b}{2} \right)}{4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(exp(x^2)*sin(b*x),x)

[Out] 1/4*Pi^(1/2)*exp(1/4*b^2)*erf(-I*x+1/2*b)+1/4*Pi^(1/2)*exp(1/4*b^2)*erf(I*x+1/2*b)

maxima [A] time = 0.35, size = 37, normalized size = 0.54

$$\frac{1}{4} \sqrt{\pi} \left(\operatorname{erf} \left(\frac{1}{2} b + ix \right) e^{\left(\frac{1}{4} b^2 \right)} - \operatorname{erf} \left(-\frac{1}{2} b + ix \right) e^{\left(\frac{1}{4} b^2 \right)} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(x^2)*sin(b*x),x, algorithm="maxima")

[Out] 1/4*sqrt(pi)*(erf(1/2*b + I*x)*e^(1/4*b^2) - erf(-1/2*b + I*x)*e^(1/4*b^2))

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int e^{x^2} \sin(bx) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(exp(x^2)*sin(b*x),x)

[Out] int(exp(x^2)*sin(b*x), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int e^{x^2} \sin(bx) dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(x**2)*sin(b*x), x)
```

```
[Out] Integral(exp(x**2)*sin(b*x), x)
```

3.58 $\int e^{x^2} \cos(bx) dx$

Optimal. Leaf size=65

$$\frac{1}{4}\sqrt{\pi}e^{\frac{b^2}{4}}\operatorname{erfi}\left(\frac{1}{2}(2x-ib)\right)+\frac{1}{4}\sqrt{\pi}e^{\frac{b^2}{4}}\operatorname{erfi}\left(\frac{1}{2}(2x+ib)\right)$$

[Out] $-1/4*\exp(1/4*b^2)*\operatorname{erfi}(1/2*I*b-x)*\operatorname{Pi}^{(1/2)}+1/4*\exp(1/4*b^2)*\operatorname{erfi}(1/2*I*b+x)*\operatorname{Pi}^{(1/2)}$

Rubi [A] time = 0.05, antiderivative size = 65, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 3, integrand size = 10, $\frac{\text{number of rules}}{\text{integrand size}} = 0.300$, Rules used = {4473, 2234, 2204}

$$\frac{1}{4}\sqrt{\pi}e^{\frac{b^2}{4}}\operatorname{Erfi}\left(\frac{1}{2}(2x-ib)\right)+\frac{1}{4}\sqrt{\pi}e^{\frac{b^2}{4}}\operatorname{Erfi}\left(\frac{1}{2}(2x+ib)\right)$$

Antiderivative was successfully verified.

[In] Int[E^x^2*Cos[b*x],x]

[Out] $(E^{(b^2/4)}*\operatorname{Sqrt}[\operatorname{Pi}]*\operatorname{Erfi}[((-I)*b+2*x)/2])/4+(E^{(b^2/4)}*\operatorname{Sqrt}[\operatorname{Pi}]*\operatorname{Erfi}[(I*b+2*x)/2])/4$

Rule 2204

Int[(F_)^((a_.)+(b_.)*((c_.)+(d_.)*(x_)^2), x_Symbol] :> Simp[(F^a*Sqrt[Pi]*Erfi[(c+d*x)*Rt[b*Log[F], 2]])/(2*d*Rt[b*Log[F], 2]), x] /; FreeQ[{F, a, b, c, d}, x] && PosQ[b]

Rule 2234

Int[(F_)^((a_.)+(b_.)*(x_) + (c_.)*(x_)^2), x_Symbol] :> Dist[F^(a-b^2/(4*c)), Int[F^((b+2*c*x)^2/(4*c)), x], x] /; FreeQ[{F, a, b, c}, x]

Rule 4473

Int[Cos[v_]^(n_.)*(F_)^(u_), x_Symbol] :> Int[ExpandTrigToExp[F^u, Cos[v]^n, x], x] /; FreeQ[F, x] && (LinearQ[u, x] || PolyQ[u, x, 2]) && (LinearQ[v, x] || PolyQ[v, x, 2]) && IGtQ[n, 0]

Rubi steps

$$\begin{aligned}\int e^{x^2} \cos(bx) dx &= \int \left(\frac{1}{2}e^{-ibx+x^2} + \frac{1}{2}e^{ibx+x^2} \right) dx \\ &= \frac{1}{2} \int e^{-ibx+x^2} dx + \frac{1}{2} \int e^{ibx+x^2} dx \\ &= \frac{1}{2}e^{\frac{b^2}{4}} \int e^{\frac{1}{4}(-ib+2x)^2} dx + \frac{1}{2}e^{\frac{b^2}{4}} \int e^{\frac{1}{4}(ib+2x)^2} dx \\ &= \frac{1}{4}e^{\frac{b^2}{4}}\sqrt{\pi}\operatorname{erfi}\left(\frac{1}{2}(-ib+2x)\right)+\frac{1}{4}e^{\frac{b^2}{4}}\sqrt{\pi}\operatorname{erfi}\left(\frac{1}{2}(ib+2x)\right)\end{aligned}$$

Mathematica [A] time = 0.02, size = 47, normalized size = 0.72

$$\frac{1}{4}\sqrt{\pi}e^{\frac{b^2}{4}}\left(\operatorname{erfi}\left(\frac{1}{2}(2x-ib)\right)+\operatorname{erfi}\left(\frac{1}{2}(2x+ib)\right)\right)$$

Antiderivative was successfully verified.

[In] Integrate[E^x^2*cos[b*x],x]

[Out] (E^(b^2/4)*Sqrt[Pi]*(Erfi[((-I)*b + 2*x)/2] + Erfi[(I*b + 2*x)/2]))/4

fricas [A] time = 0.77, size = 32, normalized size = 0.49

$$\frac{1}{4} \sqrt{\pi} \left(-i \operatorname{erf} \left(\frac{1}{2} b + ix \right) - i \operatorname{erf} \left(-\frac{1}{2} b + ix \right) \right) e^{\left(\frac{1}{4} b^2 \right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(x^2)*cos(b*x),x, algorithm="fricas")

[Out] 1/4*sqrt(pi)*(-I*erf(1/2*b + I*x) - I*erf(-1/2*b + I*x))*e^(1/4*b^2)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \cos(bx) e^{x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(x^2)*cos(b*x),x, algorithm="giac")

[Out] integrate(cos(b*x)*e^(x^2), x)

maple [A] time = 0.08, size = 44, normalized size = 0.68

$$-\frac{i\sqrt{\pi} e^{\frac{b^2}{4}} \operatorname{erf} \left(ix + \frac{b}{2} \right)}{4} + \frac{i\sqrt{\pi} e^{\frac{b^2}{4}} \operatorname{erf} \left(-ix + \frac{b}{2} \right)}{4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(exp(x^2)*cos(b*x),x)

[Out] -1/4*I*Pi^(1/2)*exp(1/4*b^2)*erf(I*x+1/2*b)+1/4*I*Pi^(1/2)*exp(1/4*b^2)*erf(-I*x+1/2*b)

maxima [A] time = 0.36, size = 38, normalized size = 0.58

$$-\frac{1}{4} \sqrt{\pi} \left(i \operatorname{erf} \left(\frac{1}{2} b + ix \right) e^{\left(\frac{1}{4} b^2 \right)} + i \operatorname{erf} \left(-\frac{1}{2} b + ix \right) e^{\left(\frac{1}{4} b^2 \right)} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(x^2)*cos(b*x),x, algorithm="maxima")

[Out] -1/4*sqrt(pi)*(I*erf(1/2*b + I*x)*e^(1/4*b^2) + I*erf(-1/2*b + I*x)*e^(1/4*b^2))

mupad [F] time = 0.00, size = -1, normalized size = -0.02

$$\int e^{x^2} \cos(bx) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(exp(x^2)*cos(b*x),x)

[Out] int(exp(x^2)*cos(b*x), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int e^{x^2} \cos(bx) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(x**2)*cos(b*x), x)

[Out] Integral(exp(x**2)*cos(b*x), x)

3.59 $\int e^{x^2} \sin(a + bx) dx$

Optimal. Leaf size=81

$$\frac{1}{4}i\sqrt{\pi}e^{\frac{b^2}{4}-ia}\operatorname{erfi}\left(\frac{1}{2}(2x-ib)\right) - \frac{1}{4}i\sqrt{\pi}e^{\frac{b^2}{4}+ia}\operatorname{erfi}\left(\frac{1}{2}(2x+ib)\right)$$

[Out] $-1/4*I*\exp(-I*a+1/4*b^2)*\operatorname{erfi}(1/2*I*b-x)*\operatorname{Pi}^{(1/2)} - 1/4*I*\exp(I*a+1/4*b^2)*\operatorname{erfi}(1/2*I*b+x)*\operatorname{Pi}^{(1/2)}$

Rubi [A] time = 0.07, antiderivative size = 81, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 3, integrand size = 12, $\frac{\text{number of rules}}{\text{integrand size}} = 0.250$, Rules used = {4472, 2234, 2204}

$$\frac{1}{4}i\sqrt{\pi}e^{\frac{b^2}{4}-ia}\operatorname{Erfi}\left(\frac{1}{2}(2x-ib)\right) - \frac{1}{4}i\sqrt{\pi}e^{\frac{b^2}{4}+ia}\operatorname{Erfi}\left(\frac{1}{2}(2x+ib)\right)$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[E^{x^2}*\operatorname{Sin}[a + b*x], x]$

[Out] $(I/4)*E^{((-I)*a + b^2/4)*\operatorname{Sqrt}[\operatorname{Pi}]}*\operatorname{Erfi}[((-I)*b + 2*x)/2] - (I/4)*E^{(I*a + b^2/4)*\operatorname{Sqrt}[\operatorname{Pi}]}*\operatorname{Erfi}[(I*b + 2*x)/2]$

Rule 2204

$\operatorname{Int}[(F_)^{((a_.) + (b_.)*((c_.) + (d_.)*(x_))^2)}, x_Symbol] \rightarrow \operatorname{Simp}[(F^a*\operatorname{Sqrt}[\operatorname{Pi}]*\operatorname{Erfi}[(c + d*x)*\operatorname{Rt}[b*\operatorname{Log}[F], 2]])/(2*d*\operatorname{Rt}[b*\operatorname{Log}[F], 2]), x] /; \operatorname{FreeQ}\{F, a, b, c, d\}, x] \&\& \operatorname{PosQ}[b]$

Rule 2234

$\operatorname{Int}[(F_)^{((a_.) + (b_.)*(x_.) + (c_.)*(x_.)^2)}, x_Symbol] \rightarrow \operatorname{Dist}[F^{(a - b^2/(4*c))}, \operatorname{Int}[F^{((b + 2*c*x)^2/(4*c))}, x], x] /; \operatorname{FreeQ}\{F, a, b, c\}, x]$

Rule 4472

$\operatorname{Int}[(F_)^{(u_)}*\operatorname{Sin}[v_]^{(n_.)}, x_Symbol] \rightarrow \operatorname{Int}[\operatorname{ExpandTrigToExp}[F^u, \operatorname{Sin}[v]^{n}], x] /; \operatorname{FreeQ}[F, x] \&\& (\operatorname{LinearQ}[u, x] \parallel \operatorname{PolyQ}[u, x, 2]) \&\& (\operatorname{LinearQ}[v, x] \parallel \operatorname{PolyQ}[v, x, 2]) \&\& \operatorname{IGtQ}[n, 0]$

Rubi steps

$$\begin{aligned} \int e^{x^2} \sin(a + bx) dx &= \int \left(\frac{1}{2}ie^{-ia-ibx+x^2} - \frac{1}{2}ie^{ia+ibx+x^2} \right) dx \\ &= \frac{1}{2}i \int e^{-ia-ibx+x^2} dx - \frac{1}{2}i \int e^{ia+ibx+x^2} dx \\ &= \frac{1}{2} \left(ie^{-ia+\frac{b^2}{4}} \right) \int e^{\frac{1}{4}(-ib+2x)^2} dx - \frac{1}{2} \left(ie^{ia+\frac{b^2}{4}} \right) \int e^{\frac{1}{4}(ib+2x)^2} dx \\ &= \frac{1}{4}ie^{-ia+\frac{b^2}{4}} \sqrt{\pi} \operatorname{erfi}\left(\frac{1}{2}(-ib+2x)\right) - \frac{1}{4}ie^{ia+\frac{b^2}{4}} \sqrt{\pi} \operatorname{erfi}\left(\frac{1}{2}(ib+2x)\right) \end{aligned}$$

Mathematica [A] time = 0.08, size = 81, normalized size = 1.00

$$\frac{1}{4}\sqrt{\pi}e^{\frac{b^2}{4}} \left(\cos(a)\operatorname{erf}\left(\frac{b}{2} - ix\right) + \cos(a)\operatorname{erf}\left(\frac{b}{2} + ix\right) + \sin(a) \left(\operatorname{erfi}\left(\frac{1}{2}(2x-ib)\right) + \operatorname{erfi}\left(\frac{1}{2}(2x+ib)\right) \right) \right)$$

Antiderivative was successfully verified.

[In] Integrate[E^x^2*Sin[a + b*x],x]

[Out] (E^(b^2/4)*Sqrt[Pi]*(Cos[a]*Erf[b/2 - I*x] + Cos[a]*Erf[b/2 + I*x] + (Erfi[(-I)*b + 2*x]/2] + Erfi[(I*b + 2*x)/2])*Sin[a])/4

fricas [A] time = 0.64, size = 45, normalized size = 0.56

$$-\frac{1}{4}\sqrt{\pi}\left(\operatorname{erf}\left(-\frac{1}{2}b+ix\right)e^{\left(\frac{1}{4}b^2+ia\right)}-\operatorname{erf}\left(\frac{1}{2}b+ix\right)e^{\left(\frac{1}{4}b^2-ia\right)}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(x^2)*sin(b*x+a),x, algorithm="fricas")

[Out] -1/4*sqrt(pi)*(erf(-1/2*b + I*x)*e^(1/4*b^2 + I*a) - erf(1/2*b + I*x)*e^(1/4*b^2 - I*a))

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int e^{(x^2)} \sin(bx + a) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(x^2)*sin(b*x+a),x, algorithm="giac")

[Out] integrate(e^(x^2)*sin(b*x + a), x)

maple [A] time = 0.08, size = 52, normalized size = 0.64

$$\frac{\sqrt{\pi} e^{\frac{b^2}{4}} e^{ia} \operatorname{erf}\left(-ix + \frac{b}{2}\right)}{4} + \frac{\sqrt{\pi} e^{\frac{b^2}{4}} e^{-ia} \operatorname{erf}\left(ix + \frac{b}{2}\right)}{4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(exp(x^2)*sin(b*x+a),x)

[Out] 1/4*Pi^(1/2)*exp(1/4*b^2)*exp(I*a)*erf(-I*x+1/2*b)+1/4*Pi^(1/2)*exp(1/4*b^2)*exp(-I*a)*erf(I*x+1/2*b)

maxima [A] time = 0.33, size = 51, normalized size = 0.63

$$\frac{1}{4}\sqrt{\pi}\left((\cos(a)-i\sin(a))\operatorname{erf}\left(\frac{1}{2}b+ix\right)e^{\left(\frac{1}{4}b^2\right)}-(\cos(a)+i\sin(a))\operatorname{erf}\left(-\frac{1}{2}b+ix\right)e^{\left(\frac{1}{4}b^2\right)}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(x^2)*sin(b*x+a),x, algorithm="maxima")

[Out] 1/4*sqrt(pi)*((cos(a) - I*sin(a))*erf(1/2*b + I*x)*e^(1/4*b^2) - (cos(a) + I*sin(a))*erf(-1/2*b + I*x)*e^(1/4*b^2))

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int e^{x^2} \sin(a + bx) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(exp(x^2)*sin(a + b*x),x)

[Out] int(exp(x^2)*sin(a + b*x), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int e^{x^2} \sin(a + bx) dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(x**2)*sin(b*x+a), x)
```

```
[Out] Integral(exp(x**2)*sin(a + b*x), x)
```

3.60 $\int e^{x^2} \cos(a + bx) dx$

Optimal. Leaf size=77

$$\frac{1}{4}\sqrt{\pi}e^{\frac{b^2}{4}-ia}\operatorname{erfi}\left(\frac{1}{2}(2x-ib)\right)+\frac{1}{4}\sqrt{\pi}e^{\frac{b^2}{4}+ia}\operatorname{erfi}\left(\frac{1}{2}(2x+ib)\right)$$

[Out] $-1/4*\exp(-I*a+1/4*b^2)*\operatorname{erfi}(1/2*I*b-x)*\operatorname{Pi}^{(1/2)}+1/4*\exp(I*a+1/4*b^2)*\operatorname{erfi}(1/2*I*b+x)*\operatorname{Pi}^{(1/2)}$

Rubi [A] time = 0.05, antiderivative size = 77, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 3, integrand size = 12, $\frac{\text{number of rules}}{\text{integrand size}} = 0.250$, Rules used = {4473, 2234, 2204}

$$\frac{1}{4}\sqrt{\pi}e^{\frac{b^2}{4}-ia}\operatorname{Erfi}\left(\frac{1}{2}(2x-ib)\right)+\frac{1}{4}\sqrt{\pi}e^{\frac{b^2}{4}+ia}\operatorname{Erfi}\left(\frac{1}{2}(2x+ib)\right)$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[E^{x^2}*\operatorname{Cos}[a + b*x], x]$

[Out] $(E^{((-I)*a + b^2/4)*\operatorname{Sqrt}[\operatorname{Pi}]*\operatorname{Erfi}[((-I)*b + 2*x)/2]})/4 + (E^{(I*a + b^2/4)*\operatorname{Sqrt}[\operatorname{Pi}]*\operatorname{Erfi}[(I*b + 2*x)/2]})/4$

Rule 2204

$\operatorname{Int}[(F_)^{((a_.) + (b_.)*((c_.) + (d_.)*(x_))^{2})}, x_Symbol] \rightarrow \operatorname{Simp}[(F^a*\operatorname{Sqrt}[\operatorname{Pi}]*\operatorname{Erfi}[(c + d*x)*\operatorname{Rt}[b*\operatorname{Log}[F], 2]])/(2*d*\operatorname{Rt}[b*\operatorname{Log}[F], 2]), x] /; \operatorname{FreeQ}\{F, a, b, c, d\}, x] \&\& \operatorname{PosQ}[b]$

Rule 2234

$\operatorname{Int}[(F_)^{((a_.) + (b_.)*(x_) + (c_.)*(x_)^2)}, x_Symbol] \rightarrow \operatorname{Dist}[F^{(a - b^2/(4*c))}, \operatorname{Int}[F^{((b + 2*c*x)^2/(4*c))}, x], x] /; \operatorname{FreeQ}\{F, a, b, c\}, x]$

Rule 4473

$\operatorname{Int}[\operatorname{Cos}[v_]^{(n_.)}*(F_)^{(u_)}, x_Symbol] \rightarrow \operatorname{Int}[\operatorname{ExpandTrigToExp}[F^u, \operatorname{Cos}[v]^{(n)}, x], x] /; \operatorname{FreeQ}[F, x] \&\& (\operatorname{LinearQ}[u, x] \mid\mid \operatorname{PolyQ}[u, x, 2]) \&\& (\operatorname{LinearQ}[v, x] \mid\mid \operatorname{PolyQ}[v, x, 2]) \&\& \operatorname{IGtQ}[n, 0]$

Rubi steps

$$\begin{aligned} \int e^{x^2} \cos(a + bx) dx &= \int \left(\frac{1}{2}e^{-ia-ibx+x^2} + \frac{1}{2}e^{ia+ibx+x^2} \right) dx \\ &= \frac{1}{2} \int e^{-ia-ibx+x^2} dx + \frac{1}{2} \int e^{ia+ibx+x^2} dx \\ &= \frac{1}{2}e^{-ia+\frac{b^2}{4}} \int e^{\frac{1}{4}(-ib+2x)^2} dx + \frac{1}{2}e^{ia+\frac{b^2}{4}} \int e^{\frac{1}{4}(ib+2x)^2} dx \\ &= \frac{1}{4}e^{-ia+\frac{b^2}{4}}\sqrt{\pi}\operatorname{erfi}\left(\frac{1}{2}(-ib+2x)\right) + \frac{1}{4}e^{ia+\frac{b^2}{4}}\sqrt{\pi}\operatorname{erfi}\left(\frac{1}{2}(ib+2x)\right) \end{aligned}$$

Mathematica [A] time = 0.08, size = 82, normalized size = 1.06

$$\frac{1}{4}\sqrt{\pi}e^{\frac{b^2}{4}}\left(-\sin(a)\left(\operatorname{erf}\left(\frac{b}{2}-ix\right)+\operatorname{erf}\left(\frac{b}{2}+ix\right)\right)+\cos(a)\operatorname{erfi}\left(\frac{1}{2}(2x-ib)\right)+\cos(a)\operatorname{erfi}\left(\frac{1}{2}(2x+ib)\right)\right)$$

Antiderivative was successfully verified.

[In] Integrate[E^x^2*Cos[a + b*x], x]

[Out] (E^(b^2/4)*Sqrt[Pi]*(Cos[a]*Erfi[((-I)*b + 2*x)/2] + Cos[a]*Erfi[(I*b + 2*x)/2] - (Erf[b/2 - I*x] + Erf[b/2 + I*x])*Sin[a])/4

fricas [A] time = 0.61, size = 46, normalized size = 0.60

$$\frac{1}{4} \sqrt{\pi} \left(-i \operatorname{erf} \left(-\frac{1}{2} b + ix \right) e^{\left(\frac{1}{4} b^2 + ia \right)} - i \operatorname{erf} \left(\frac{1}{2} b + ix \right) e^{\left(\frac{1}{4} b^2 - ia \right)} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(x^2)*cos(b*x+a), x, algorithm="fricas")

[Out] 1/4*sqrt(pi)*(-I*erf(-1/2*b + I*x)*e^(1/4*b^2 + I*a) - I*erf(1/2*b + I*x)*e^(1/4*b^2 - I*a))

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \cos(bx + a) e^{x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(x^2)*cos(b*x+a), x, algorithm="giac")

[Out] integrate(cos(b*x + a)*e^(x^2), x)

maple [A] time = 0.08, size = 54, normalized size = 0.70

$$-\frac{i\sqrt{\pi} e^{\frac{b^2}{4}} e^{-ia} \operatorname{erf} \left(ix + \frac{b}{2} \right)}{4} + \frac{i\sqrt{\pi} e^{\frac{b^2}{4}} e^{ia} \operatorname{erf} \left(-ix + \frac{b}{2} \right)}{4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(exp(x^2)*cos(b*x+a), x)

[Out] -1/4*I*Pi^(1/2)*exp(1/4*b^2)*exp(-I*a)*erf(I*x+1/2*b)+1/4*I*Pi^(1/2)*exp(1/4*b^2)*exp(I*a)*erf(-I*x+1/2*b)

maxima [A] time = 0.34, size = 52, normalized size = 0.68

$$-\frac{1}{4} \sqrt{\pi} \left((i \cos(a) + \sin(a)) \operatorname{erf} \left(\frac{1}{2} b + ix \right) e^{\left(\frac{1}{4} b^2 \right)} + (i \cos(a) - \sin(a)) \operatorname{erf} \left(-\frac{1}{2} b + ix \right) e^{\left(\frac{1}{4} b^2 \right)} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(x^2)*cos(b*x+a), x, algorithm="maxima")

[Out] -1/4*sqrt(pi)*((I*cos(a) + sin(a))*erf(1/2*b + I*x)*e^(1/4*b^2) + (I*cos(a) - sin(a))*erf(-1/2*b + I*x)*e^(1/4*b^2))

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \cos(a + bx) e^{x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(cos(a + b*x)*exp(x^2), x)

[Out] int(cos(a + b*x)*exp(x^2), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int e^{x^2} \cos(a + bx) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(x**2)*cos(b*x+a), x)

[Out] Integral(exp(x**2)*cos(a + b*x), x)

3.61 $\int e^{2x^2} x \cos(2x^2) dx$

Optimal. Leaf size=35

$$\frac{1}{8}e^{2x^2} \sin(2x^2) + \frac{1}{8}e^{2x^2} \cos(2x^2)$$

[Out] 1/8*exp(2*x^2)*cos(2*x^2)+1/8*exp(2*x^2)*sin(2*x^2)

Rubi [A] time = 0.08, antiderivative size = 35, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.133$, Rules used = {6715, 4433}

$$\frac{1}{8}e^{2x^2} \sin(2x^2) + \frac{1}{8}e^{2x^2} \cos(2x^2)$$

Antiderivative was successfully verified.

[In] Int[E^(2*x^2)*x*Cos[2*x^2],x]

[Out] (E^(2*x^2)*Cos[2*x^2])/8 + (E^(2*x^2)*Sin[2*x^2])/8

Rule 4433

Int[Cos[(d_.) + (e_.)*(x_.)]*(F_)^((c_.)*((a_.) + (b_.)*(x_.))), x_Symbol] :>
Simp[(b*c*Log[F]*F^(c*(a + b*x))*Cos[d + e*x]]/(e^2 + b^2*c^2*Log[F]^2), x
] + Simp[(e*F^(c*(a + b*x))*Sin[d + e*x]]/(e^2 + b^2*c^2*Log[F]^2), x] /; F
reeQ[{F, a, b, c, d, e}, x] && NeQ[e^2 + b^2*c^2*Log[F]^2, 0]

Rule 6715

Int[(u_)*(x_)^(m_.), x_Symbol] :> Dist[1/(m + 1), Subst[Int[SubstFor[x^(m + 1), u, x], x], x, x^(m + 1)], x] /; FreeQ[m, x] && NeQ[m, -1] && FunctionOfQ[x^(m + 1), u, x]

Rubi steps

$$\begin{aligned} \int e^{2x^2} x \cos(2x^2) dx &= \frac{1}{2} \text{Subst} \left(\int e^{2x} \cos(2x) dx, x, x^2 \right) \\ &= \frac{1}{8} e^{2x^2} \cos(2x^2) + \frac{1}{8} e^{2x^2} \sin(2x^2) \end{aligned}$$

Mathematica [A] time = 0.04, size = 24, normalized size = 0.69

$$\frac{1}{8}e^{2x^2} (\sin(2x^2) + \cos(2x^2))$$

Antiderivative was successfully verified.

[In] Integrate[E^(2*x^2)*x*Cos[2*x^2],x]

[Out] (E^(2*x^2)*(Cos[2*x^2] + Sin[2*x^2]))/8

fricas [A] time = 0.73, size = 29, normalized size = 0.83

$$\frac{1}{8} \cos(2x^2) e^{(2x^2)} + \frac{1}{8} e^{(2x^2)} \sin(2x^2)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(2*x^2)*x*cos(2*x^2),x, algorithm="fricas")

[Out] $1/8*\cos(2*x^2)*e^{(2*x^2)} + 1/8*e^{(2*x^2)}*\sin(2*x^2)$

giac [A] time = 0.14, size = 21, normalized size = 0.60

$$\frac{1}{8} (\cos(2x^2) + \sin(2x^2))e^{(2x^2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(exp(2*x^2)*x*cos(2*x^2),x, algorithm="giac")`

[Out] $1/8*(\cos(2*x^2) + \sin(2*x^2))*e^{(2*x^2)}$

maple [A] time = 0.06, size = 30, normalized size = 0.86

$$\frac{e^{2x^2} \cos(2x^2)}{8} + \frac{e^{2x^2} \sin(2x^2)}{8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(exp(2*x^2)*x*cos(2*x^2),x)`

[Out] $1/8*\exp(2*x^2)*\cos(2*x^2)+1/8*\exp(2*x^2)*\sin(2*x^2)$

maxima [A] time = 0.36, size = 29, normalized size = 0.83

$$\frac{1}{8} \cos(2x^2)e^{(2x^2)} + \frac{1}{8} e^{(2x^2)} \sin(2x^2)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(exp(2*x^2)*x*cos(2*x^2),x, algorithm="maxima")`

[Out] $1/8*\cos(2*x^2)*e^{(2*x^2)} + 1/8*e^{(2*x^2)}*\sin(2*x^2)$

mupad [B] time = 0.08, size = 21, normalized size = 0.60

$$\frac{e^{2x^2} (\cos(2x^2) + \sin(2x^2))}{8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x*exp(2*x^2)*cos(2*x^2),x)`

[Out] $(\exp(2*x^2)*(\cos(2*x^2) + \sin(2*x^2)))/8$

sympy [A] time = 6.23, size = 29, normalized size = 0.83

$$\frac{e^{2x^2} \sin(2x^2)}{8} + \frac{e^{2x^2} \cos(2x^2)}{8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(exp(2*x**2)*x*cos(2*x**2),x)`

[Out] $\exp(2*x**2)*\sin(2*x**2)/8 + \exp(2*x**2)*\cos(2*x**2)/8$

3.62 $\int e^x \sin(e^x) dx$

Optimal. Leaf size=6

$$-\cos(e^x)$$

[Out] -cos(exp(x))

Rubi [A] time = 0.01, antiderivative size = 6, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 8, $\frac{\text{number of rules}}{\text{integrand size}} = 0.250$, Rules used = {2282, 2638}

$$-\cos(e^x)$$

Antiderivative was successfully verified.

[In] Int[E^x*Sin[E^x],x]

[Out] -Cos[E^x]

Rule 2282

```
Int[u_, x_Symbol] := With[{v = FunctionOfExponential[u, x]}, Dist[v/D[v, x], Subst[Int[FunctionOfExponentialFunction[u, x]/x, x], x, v], x]] /; FunctionOfExponentialQ[u, x] && !MatchQ[u, (w_)*((a_.)*(v_)^(n_))^(m_)] /; FreeQ[{a, m, n}, x] && IntegerQ[m*n] && !MatchQ[u, E^((c_.)*((a_.) + (b_.)*x))*(F_)[v_] /; FreeQ[{a, b, c}, x] && InverseFunctionQ[F[x]]]
```

Rule 2638

```
Int[sin[(c_.) + (d_.)*(x_)], x_Symbol] := -Simp[Cos[c + d*x]/d, x] /; FreeQ[{c, d}, x]
```

Rubi steps

$$\begin{aligned} \int e^x \sin(e^x) dx &= \text{Subst}\left(\int \sin(x) dx, x, e^x\right) \\ &= -\cos(e^x) \end{aligned}$$

Mathematica [A] time = 0.01, size = 6, normalized size = 1.00

$$-\cos(e^x)$$

Antiderivative was successfully verified.

[In] Integrate[E^x*Sin[E^x],x]

[Out] -Cos[E^x]

fricas [A] time = 2.29, size = 5, normalized size = 0.83

$$-\cos(e^x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(x)*sin(exp(x)),x, algorithm="fricas")

[Out] -cos(e^x)

giac [A] time = 0.14, size = 5, normalized size = 0.83

$$-\cos(e^x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(exp(x)*sin(exp(x)),x, algorithm="giac")`

[Out] `-cos(e^x)`

maple [A] time = 0.00, size = 6, normalized size = 1.00

$$-\cos(e^x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(exp(x)*sin(exp(x)),x)`

[Out] `-cos(exp(x))`

maxima [A] time = 0.34, size = 5, normalized size = 0.83

$$-\cos(e^x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(exp(x)*sin(exp(x)),x, algorithm="maxima")`

[Out] `-cos(e^x)`

mupad [B] time = 2.21, size = 5, normalized size = 0.83

$$-\cos(e^x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(sin(exp(x))*exp(x),x)`

[Out] `-cos(exp(x))`

sympy [A] time = 0.23, size = 5, normalized size = 0.83

$$-\cos(e^x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(exp(x)*sin(exp(x)),x)`

[Out] `-cos(exp(x))`

3.63 $\int e^x \csc(e^x) \sec(e^x) dx$

Optimal. Leaf size=5

$$\log(\tan(e^x))$$

[Out] ln(tan(exp(x)))

Rubi [A] time = 0.02, antiderivative size = 5, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 3, integrand size = 12, $\frac{\text{number of rules}}{\text{integrand size}} = 0.250$, Rules used = {2282, 2620, 29}

$$\log(\tan(e^x))$$

Antiderivative was successfully verified.

[In] Int[E^x*Csc[E^x]*Sec[E^x], x]

[Out] Log[Tan[E^x]]

Rule 29

Int[(x_)^(-1), x_Symbol] := Simp[Log[x], x]

Rule 2282

Int[u_, x_Symbol] := With[{v = FunctionOfExponential[u, x]}, Dist[v/D[v, x], Subst[Int[FunctionOfExponentialFunction[u, x]/x, x], x, v], x] /; FunctionOfExponentialQ[u, x] && !MatchQ[u, (w_)*((a_.)*(v_)^(n_))^(m_)] /; FreeQ[{a, m, n}, x] && IntegerQ[m*n] && !MatchQ[u, E^((c_.)*((a_.) + (b_.)*x))*(F_)[v_] /; FreeQ[{a, b, c}, x] && InverseFunctionQ[F[x]]]

Rule 2620

Int[csc[(e_.) + (f_.)*(x_)]^(m_.)*sec[(e_.) + (f_.)*(x_)]^(n_.), x_Symbol] := Dist[1/f, Subst[Int[(1 + x^2)^((m + n)/2 - 1)/x^m, x], x, Tan[e + f*x]], x] /; FreeQ[{e, f}, x] && IntegersQ[m, n, (m + n)/2]

Rubi steps

$$\begin{aligned} \int e^x \csc(e^x) \sec(e^x) dx &= \text{Subst} \left(\int \csc(x) \sec(x) dx, x, e^x \right) \\ &= \text{Subst} \left(\int \frac{1}{x} dx, x, \tan(e^x) \right) \\ &= \log(\tan(e^x)) \end{aligned}$$

Mathematica [B] time = 0.02, size = 21, normalized size = 4.20

$$2 \left(\frac{1}{2} \log(\sin(e^x)) - \frac{1}{2} \log(\cos(e^x)) \right)$$

Antiderivative was successfully verified.

[In] Integrate[E^x*Csc[E^x]*Sec[E^x], x]

[Out] 2*(-1/2*Log[Cos[E^x]] + Log[Sin[E^x]]/2)

fricas [B] time = 0.57, size = 21, normalized size = 4.20

$$-\frac{1}{2} \log(\cos(e^x)^2) + \frac{1}{2} \log\left(-\frac{1}{4} \cos(e^x)^2 + \frac{1}{4}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(x)*csc(exp(x))*sec(exp(x)),x, algorithm="fricas")

[Out] -1/2*log(cos(e^x)^2) + 1/2*log(-1/4*cos(e^x)^2 + 1/4)

giac [B] time = 0.14, size = 17, normalized size = 3.40

$$-\frac{1}{2} \log(|\sin(e^x)^2 - 1|) + \log(|\sin(e^x)|)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(x)*csc(exp(x))*sec(exp(x)),x, algorithm="giac")

[Out] -1/2*log(abs(sin(e^x)^2 - 1)) + log(abs(sin(e^x)))

maple [A] time = 0.08, size = 5, normalized size = 1.00

$$\ln(\tan(e^x))$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(exp(x)*csc(exp(x))*sec(exp(x)),x)

[Out] ln(tan(exp(x)))

maxima [B] time = 0.31, size = 19, normalized size = 3.80

$$-\frac{1}{2} \log(\sin(e^x)^2 - 1) + \frac{1}{2} \log(\sin(e^x)^2)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(x)*csc(exp(x))*sec(exp(x)),x, algorithm="maxima")

[Out] -1/2*log(sin(e^x)^2 - 1) + 1/2*log(sin(e^x)^2)

mupad [B] time = 2.51, size = 43, normalized size = 8.60

$$-\ln(-16e^{2x} - 16e^{2x}e^{e^x 2i}) + \ln(16e^{2x} - 16e^{2x}e^{e^x 2i})$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(exp(x)/(cos(exp(x))*sin(exp(x))),x)

[Out] log(16*exp(2*x) - 16*exp(2*x)*exp(exp(x)*2i)) - log(-16*exp(2*x) - 16*exp(2*x)*exp(exp(x)*2i))

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int e^x \csc(e^x) \sec(e^x) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(x)*csc(exp(x))*sec(exp(x)),x)

[Out] Integral(exp(x)*csc(exp(x))*sec(exp(x)), x)

3.64 $\int e^x \cos(e^x) dx$

Optimal. Leaf size=4

$$\sin(e^x)$$

[Out] sin(exp(x))

Rubi [A] time = 0.01, antiderivative size = 4, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 8, $\frac{\text{number of rules}}{\text{integrand size}} = 0.250$, Rules used = {2282, 2637}

$$\sin(e^x)$$

Antiderivative was successfully verified.

[In] Int[E^x*Cos[E^x],x]

[Out] Sin[E^x]

Rule 2282

```
Int[u_, x_Symbol] := With[{v = FunctionOfExponential[u, x]}, Dist[v/D[v, x], Subst[Int[FunctionOfExponentialFunction[u, x]/x, x], x, v], x] /; FunctionOfExponentialQ[u, x] && !MatchQ[u, (w_)*((a_.)*(v_)^(n_))^(m_) /; FreeQ[{a, m, n}, x] && IntegerQ[m*n]] && !MatchQ[u, E^((c_.)*((a_.) + (b_.)*x))*(F_)[v_] /; FreeQ[{a, b, c}, x] && InverseFunctionQ[F[x]]]
```

Rule 2637

```
Int[sin[Pi/2 + (c_.) + (d_.)*(x_)], x_Symbol] := Simp[Sin[c + d*x]/d, x] /; FreeQ[{c, d}, x]
```

Rubi steps

$$\begin{aligned} \int e^x \cos(e^x) dx &= \text{Subst}\left(\int \cos(x) dx, x, e^x\right) \\ &= \sin(e^x) \end{aligned}$$

Mathematica [A] time = 0.01, size = 4, normalized size = 1.00

$$\sin(e^x)$$

Antiderivative was successfully verified.

[In] Integrate[E^x*Cos[E^x],x]

[Out] Sin[E^x]

fricas [A] time = 0.76, size = 3, normalized size = 0.75

$$\sin(e^x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(x)*cos(exp(x)),x, algorithm="fricas")

[Out] sin(e^x)

giac [A] time = 0.12, size = 3, normalized size = 0.75

$$\sin(e^x)$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(x)*cos(exp(x)),x, algorithm="giac")
```

```
[Out] sin(e^x)
```

maple [A] time = 0.04, size = 4, normalized size = 1.00

$$\sin(e^x)$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(x)*cos(exp(x)),x)
```

```
[Out] sin(exp(x))
```

maxima [A] time = 0.31, size = 3, normalized size = 0.75

$$\sin(e^x)$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(x)*cos(exp(x)),x, algorithm="maxima")
```

```
[Out] sin(e^x)
```

mupad [B] time = 0.04, size = 3, normalized size = 0.75

$$\sin(e^x)$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(cos(exp(x))*exp(x),x)
```

```
[Out] sin(exp(x))
```

sympy [A] time = 0.23, size = 3, normalized size = 0.75

$$\sin(e^x)$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(x)*cos(exp(x)),x)
```

```
[Out] sin(exp(x))
```

3.65 $\int e^{2x} \cos(e^{2x}) dx$

Optimal. Leaf size=10

$$\frac{1}{2} \sin(e^{2x})$$

[Out] 1/2*sin(exp(2*x))

Rubi [A] time = 0.01, antiderivative size = 10, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 12, $\frac{\text{number of rules}}{\text{integrand size}} = 0.167$, Rules used = {2282, 2637}

$$\frac{1}{2} \sin(e^{2x})$$

Antiderivative was successfully verified.

[In] Int[E^(2*x)*Cos[E^(2*x)],x]

[Out] Sin[E^(2*x)]/2

Rule 2282

```
Int[u_, x_Symbol] := With[{v = FunctionOfExponential[u, x]}, Dist[v/D[v, x], Subst[Int[FunctionOfExponentialFunction[u, x]/x, x], x, v], x] /; FunctionOfExponentialQ[u, x] && !MatchQ[u, (w_)*((a_.)*(v_)^(n_))^(m_) /; FreeQ[{a, m, n}, x] && IntegerQ[m*n]] && !MatchQ[u, E^((c_.)*((a_.) + (b_.)*x))*(F_)[v_] /; FreeQ[{a, b, c}, x] && InverseFunctionQ[F[x]]]
```

Rule 2637

```
Int[sin[Pi/2 + (c_.) + (d_.)*(x_)], x_Symbol] := Simp[Sin[c + d*x]/d, x] /; FreeQ[{c, d}, x]
```

Rubi steps

$$\begin{aligned} \int e^{2x} \cos(e^{2x}) dx &= \frac{1}{2} \text{Subst} \left(\int \cos(x) dx, x, e^{2x} \right) \\ &= \frac{1}{2} \sin(e^{2x}) \end{aligned}$$

Mathematica [A] time = 0.01, size = 10, normalized size = 1.00

$$\frac{1}{2} \sin(e^{2x})$$

Antiderivative was successfully verified.

[In] Integrate[E^(2*x)*Cos[E^(2*x)],x]

[Out] Sin[E^(2*x)]/2

fricas [A] time = 0.63, size = 7, normalized size = 0.70

$$\frac{1}{2} \sin(e^{2x})$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(2*x)*cos(exp(2*x)),x, algorithm="fricas")

[Out] $1/2*\sin(e^{(2*x)})$

giac [A] time = 0.14, size = 7, normalized size = 0.70

$$\frac{1}{2} \sin(e^{2x})$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(exp(2*x)*cos(exp(2*x)),x, algorithm="giac")`

[Out] $1/2*\sin(e^{(2*x)})$

maple [A] time = 0.04, size = 8, normalized size = 0.80

$$\frac{\sin(e^{2x})}{2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(exp(2*x)*cos(exp(2*x)),x)`

[Out] $1/2*\sin(\exp(2*x))$

maxima [A] time = 0.31, size = 7, normalized size = 0.70

$$\frac{1}{2} \sin(e^{2x})$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(exp(2*x)*cos(exp(2*x)),x, algorithm="maxima")`

[Out] $1/2*\sin(e^{(2*x)})$

mupad [B] time = 0.05, size = 7, normalized size = 0.70

$$\frac{\sin(e^{2x})}{2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(exp(2*x)*cos(exp(2*x)),x)`

[Out] $\sin(\exp(2*x))/2$

sympy [A] time = 0.24, size = 7, normalized size = 0.70

$$\frac{\sin(e^{2x})}{2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(exp(2*x)*cos(exp(2*x)),x)`

[Out] $\sin(\exp(2*x))/2$

3.66 $\int e^{-2x} \cos(e^{-2x}) dx$

Optimal. Leaf size=10

$$-\frac{1}{2} \sin(e^{-2x})$$

[Out] -1/2*sin(exp(-2*x))

Rubi [A] time = 0.01, antiderivative size = 10, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 12, $\frac{\text{number of rules}}{\text{integrand size}} = 0.167$, Rules used = {2282, 2637}

$$-\frac{1}{2} \sin(e^{-2x})$$

Antiderivative was successfully verified.

[In] Int[Cos[E^(-2*x)]/E^(2*x),x]

[Out] -Sin[E^(-2*x)]/2

Rule 2282

```
Int[u_, x_Symbol] := With[{v = FunctionOfExponential[u, x]}, Dist[v/D[v, x], Subst[Int[FunctionOfExponentialFunction[u, x]/x, x, v], x]] /; FunctionOfExponentialQ[u, x] && !MatchQ[u, (w_)*((a_.)*(v_)^(n_))^(m_)] /; FreeQ[{a, m, n}, x] && IntegerQ[m*n] && !MatchQ[u, E^((c_.)*((a_.) + (b_.)*x))*(F_)[v_] /; FreeQ[{a, b, c}, x] && InverseFunctionQ[F[x]]]
```

Rule 2637

```
Int[sin[Pi/2 + (c_.) + (d_.)*(x_)], x_Symbol] := Simp[Sin[c + d*x]/d, x] /; FreeQ[{c, d}, x]
```

Rubi steps

$$\begin{aligned} \int e^{-2x} \cos(e^{-2x}) dx &= -\left(\frac{1}{2} \text{Subst}\left(\int \cos(x) dx, x, e^{-2x}\right)\right) \\ &= -\frac{1}{2} \sin(e^{-2x}) \end{aligned}$$

Mathematica [A] time = 0.01, size = 10, normalized size = 1.00

$$-\frac{1}{2} \sin(e^{-2x})$$

Antiderivative was successfully verified.

[In] Integrate[Cos[E^(-2*x)]/E^(2*x),x]

[Out] -1/2*Sin[E^(-2*x)]

fricas [A] time = 0.68, size = 7, normalized size = 0.70

$$-\frac{1}{2} \sin(e^{(-2x)})$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(cos(exp(-2*x))/exp(2*x),x, algorithm="fricas")

[Out] $-1/2*\sin(e^{(-2*x)})$

giac [A] time = 0.12, size = 7, normalized size = 0.70

$$-\frac{1}{2} \sin(e^{(-2x)})$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(cos(exp(-2*x))/exp(2*x),x, algorithm="giac")`

[Out] $-1/2*\sin(e^{(-2*x)})$

maple [A] time = 0.05, size = 8, normalized size = 0.80

$$-\frac{\sin(e^{-2x})}{2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(cos(exp(-2*x))/exp(2*x),x)`

[Out] $-1/2*\sin(\exp(-2*x))$

maxima [A] time = 0.32, size = 7, normalized size = 0.70

$$-\frac{1}{2} \sin(e^{(-2x)})$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(cos(exp(-2*x))/exp(2*x),x, algorithm="maxima")`

[Out] $-1/2*\sin(e^{(-2*x)})$

mupad [B] time = 2.20, size = 7, normalized size = 0.70

$$-\frac{\sin(e^{-2x})}{2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(exp(-2*x)*cos(exp(-2*x)),x)`

[Out] $-\sin(\exp(-2*x))/2$

sympy [A] time = 0.37, size = 10, normalized size = 1.00

$$-\frac{\sin(e^{-2x})}{2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(cos(exp(-2*x))/exp(2*x),x)`

[Out] $-\sin(\exp(-2*x))/2$

3.67 $\int e^{2x} \cos(e^x) dx$

Optimal. Leaf size=13

$$e^x \sin(e^x) + \cos(e^x)$$

[Out] `cos(exp(x))+exp(x)*sin(exp(x))`

Rubi [A] time = 0.02, antiderivative size = 13, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 3, integrand size = 10, $\frac{\text{number of rules}}{\text{integrand size}} = 0.300$, Rules used = {2282, 3296, 2638}

$$e^x \sin(e^x) + \cos(e^x)$$

Antiderivative was successfully verified.

[In] `Int[E^(2*x)*Cos[E^x],x]`

[Out] `Cos[E^x] + E^x*Sin[E^x]`

Rule 2282

```
Int[u_, x_Symbol] := With[{v = FunctionOfExponential[u, x]}, Dist[v/D[v, x],
Subst[Int[FunctionOfExponentialFunction[u, x]/x, x], x, v], x] /; FunctionOfExponentialQ[u, x] && !MatchQ[u, (w_)*((a_.)*(v_)^(n_))^(m_) /; FreeQ[{a, m, n}, x] && IntegerQ[m*n]] && !MatchQ[u, E^((c_.)*((a_.) + (b_.)*x))*(F_) [v_] /; FreeQ[{a, b, c}, x] && InverseFunctionQ[F[x]]]
```

Rule 2638

```
Int[sin[(c_.) + (d_.)*(x_)], x_Symbol] := -Simp[Cos[c + d*x]/d, x] /; FreeQ[{c, d}, x]
```

Rule 3296

```
Int[((c_.) + (d_.)*(x_))^(m_.)*sin[(e_.) + (f_.)*(x_)], x_Symbol] := -Simp[(c + d*x)^m*Cos[e + f*x]/f, x] + Dist[(d*m)/f, Int[(c + d*x)^(m - 1)*Cos[e + f*x], x], x] /; FreeQ[{c, d, e, f}, x] && GtQ[m, 0]
```

Rubi steps

$$\begin{aligned} \int e^{2x} \cos(e^x) dx &= \text{Subst} \left(\int x \cos(x) dx, x, e^x \right) \\ &= e^x \sin(e^x) - \text{Subst} \left(\int \sin(x) dx, x, e^x \right) \\ &= \cos(e^x) + e^x \sin(e^x) \end{aligned}$$

Mathematica [A] time = 0.02, size = 13, normalized size = 1.00

$$e^x \sin(e^x) + \cos(e^x)$$

Antiderivative was successfully verified.

[In] `Integrate[E^(2*x)*Cos[E^x],x]`

[Out] `Cos[E^x] + E^x*Sin[E^x]`

fricas [A] time = 0.60, size = 10, normalized size = 0.77

$$e^x \sin(e^x) + \cos(e^x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(2*x)*cos(exp(x)),x, algorithm="fricas")

[Out] $e^x \sin(e^x) + \cos(e^x)$

giac [A] time = 0.12, size = 10, normalized size = 0.77

$$e^x \sin(e^x) + \cos(e^x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(2*x)*cos(exp(x)),x, algorithm="giac")

[Out] $e^x \sin(e^x) + \cos(e^x)$

maple [B] time = 0.05, size = 24, normalized size = 1.85

$$\frac{2e^x \tan\left(\frac{e^x}{2}\right) + 2}{1 + \tan^2\left(\frac{e^x}{2}\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(exp(2*x)*cos(exp(x)),x)

[Out] $(2*\exp(x)*\tan(1/2*\exp(x))+2)/(1+\tan(1/2*\exp(x))^2)$

maxima [A] time = 0.32, size = 10, normalized size = 0.77

$$e^x \sin(e^x) + \cos(e^x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(2*x)*cos(exp(x)),x, algorithm="maxima")

[Out] $e^x \sin(e^x) + \cos(e^x)$

mupad [B] time = 2.23, size = 10, normalized size = 0.77

$$\cos(e^x) + \sin(e^x) e^x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(cos(exp(x))*exp(2*x),x)

[Out] $\cos(\exp(x)) + \sin(\exp(x))*\exp(x)$

sympy [A] time = 10.68, size = 12, normalized size = 0.92

$$e^x \sin(e^x) + \cos(e^x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(2*x)*cos(exp(x)),x)

[Out] $\exp(x)*\sin(\exp(x)) + \cos(\exp(x))$

$$3.68 \quad \int e^{-1+3x} \cos(e^{-1+3x}) \sin(1 + e^{-1+3x}) dx$$

Optimal. Leaf size=30

$$\frac{1}{6}e^{3x-1} \sin(1) - \frac{1}{12} \cos(2e^{3x-1} + 1)$$

[Out] -1/12*cos(1+2*exp(-1+3*x))+1/6*exp(-1+3*x)*sin(1)

Rubi [A] time = 0.04, antiderivative size = 30, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 3, integrand size = 26, $\frac{\text{number of rules}}{\text{integrand size}} = 0.115$, Rules used = {2282, 4574, 2638}

$$\frac{1}{6}e^{3x-1} \sin(1) - \frac{1}{12} \cos(2e^{3x-1} + 1)$$

Antiderivative was successfully verified.

[In] Int[E^(-1 + 3*x)*Cos[E^(-1 + 3*x)]*Sin[1 + E^(-1 + 3*x)],x]

[Out] -Cos[1 + 2*E^(-1 + 3*x)]/12 + (E^(-1 + 3*x)*Sin[1])/6

Rule 2282

Int[u_, x_Symbol] :=> With[{v = FunctionOfExponential[u, x]}, Dist[v/D[v, x], Subst[Int[FunctionOfExponentialFunction[u, x]/x, x], x, v], x] /; FunctionOfExponentialQ[u, x] && !MatchQ[u, (w_)*((a_.)*(v_)^(n_))^(m_)] /; FreeQ[{a, m, n}, x] && IntegerQ[m*n] && !MatchQ[u, E^((c_.)*((a_.) + (b_.)*x))*(F_)[v_] /; FreeQ[{a, b, c}, x] && InverseFunctionQ[F[x]]]

Rule 2638

Int[sin[(c_.) + (d_.)*(x_)], x_Symbol] :=> -Simp[Cos[c + d*x]/d, x] /; FreeQ[{c, d}, x]

Rule 4574

Int[Cos[w_]^(q_.)*Sin[v_]^(p_.), x_Symbol] :=> Int[ExpandTrigReduce[Sin[v]^p *Cos[w]^q, x], x] /; IGtQ[p, 0] && IGtQ[q, 0] && ((PolynomialQ[v, x] && PolynomialQ[w, x]) || (BinomialQ[{v, w}, x] && IndependentQ[Cancel[v/w], x]))

Rubi steps

$$\begin{aligned} \int e^{-1+3x} \cos(e^{-1+3x}) \sin(1 + e^{-1+3x}) dx &= \frac{1}{3} \text{Subst} \left(\int \cos(x) \sin(1 + x) dx, x, e^{-1+3x} \right) \\ &= \frac{1}{3} \text{Subst} \left(\int \left(\frac{\sin(1)}{2} + \frac{1}{2} \sin(1 + 2x) \right) dx, x, e^{-1+3x} \right) \\ &= \frac{1}{6} e^{-1+3x} \sin(1) + \frac{1}{6} \text{Subst} \left(\int \sin(1 + 2x) dx, x, e^{-1+3x} \right) \\ &= -\frac{1}{12} \cos(1 + 2e^{-1+3x}) + \frac{1}{6} e^{-1+3x} \sin(1) \end{aligned}$$

Mathematica [A] time = 0.06, size = 30, normalized size = 1.00

$$\frac{1}{6}e^{3x-1} \sin(1) - \frac{1}{12} \cos(2e^{3x-1} + 1)$$

Antiderivative was successfully verified.

[In] Integrate[E^{-1 + 3*x}*Cos[E^{-1 + 3*x}]*Sin[1 + E^{-1 + 3*x}], x]

[Out] -1/12*Cos[1 + 2*E^{-1 + 3*x}] + (E^{-1 + 3*x}*Sin[1])/6

fricas [A] time = 0.99, size = 42, normalized size = 1.40

$$-\frac{1}{6} \cos(1) \cos(e^{(3x-1)})^2 + \frac{1}{6} \cos(e^{(3x-1)}) \sin(1) \sin(e^{(3x-1)}) + \frac{1}{6} e^{(3x-1)} \sin(1)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(-1+3*x)*cos(exp(-1+3*x))*sin(1+exp(-1+3*x)), x, algorithm="fricas")

[Out] -1/6*cos(1)*cos(e^(3*x - 1))² + 1/6*cos(e^(3*x - 1))*sin(1)*sin(e^(3*x - 1)) + 1/6*e^(3*x - 1)*sin(1)

giac [A] time = 0.13, size = 24, normalized size = 0.80

$$\frac{1}{6} e^{(3x-1)} \sin(1) - \frac{1}{12} \cos(2e^{(3x-1)} + 1)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(-1+3*x)*cos(exp(-1+3*x))*sin(1+exp(-1+3*x)), x, algorithm="giac")

[Out] 1/6*e^(3*x - 1)*sin(1) - 1/12*cos(2*e^(3*x - 1) + 1)

maple [A] time = 0.26, size = 25, normalized size = 0.83

$$-\frac{\cos(1 + 2e^{-1+3x})}{12} + \frac{e^{-1+3x} \sin(1)}{6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(exp(-1+3*x)*cos(exp(-1+3*x))*sin(1+exp(-1+3*x)), x)

[Out] -1/12*cos(1+2*exp(-1+3*x))+1/6*exp(-1+3*x)*sin(1)

maxima [A] time = 0.32, size = 24, normalized size = 0.80

$$\frac{1}{6} e^{(3x-1)} \sin(1) - \frac{1}{12} \cos(2e^{(3x-1)} + 1)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(-1+3*x)*cos(exp(-1+3*x))*sin(1+exp(-1+3*x)), x, algorithm="maxima")

[Out] 1/6*e^(3*x - 1)*sin(1) - 1/12*cos(2*e^(3*x - 1) + 1)

mupad [B] time = 0.31, size = 24, normalized size = 0.80

$$\frac{e^{3x-1} \sin(1)}{6} - \frac{\cos(2e^{3x-1} + 1)}{12}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(exp(3*x - 1)*sin(exp(3*x - 1) + 1)*cos(exp(3*x - 1)), x)

[Out] (exp(3*x - 1)*sin(1))/6 - cos(2*exp(3*x - 1) + 1)/12

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(-1+3*x)*cos(exp(-1+3*x))*sin(1+exp(-1+3*x)),x)
```

```
[Out] Timed out
```

3.69 $\int e^x \tan(e^x) dx$

Optimal. Leaf size=7

$$-\log(\cos(e^x))$$

[Out] $-\ln(\cos(\exp(x)))$

Rubi [A] time = 0.01, antiderivative size = 7, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 8, $\frac{\text{number of rules}}{\text{integrand size}} = 0.250$, Rules used = {2282, 3475}

$$-\log(\cos(e^x))$$

Antiderivative was successfully verified.

[In] $\text{Int}[E^x \cdot \text{Tan}[E^x], x]$

[Out] $-\text{Log}[\text{Cos}[E^x]]$

Rule 2282

```
Int[u_, x_Symbol] :=> With[{v = FunctionOfExponential[u, x]}, Dist[v/D[v, x], Subst[Int[FunctionOfExponentialFunction[u, x]/x, x], x, v], x]] /; FunctionOfExponentialQ[u, x] && !MatchQ[u, (w_)*((a_.)*(v_)^(n_))^(m_) /; FreeQ[{a, m, n}, x] && IntegerQ[m*n]] && !MatchQ[u, E^((c_.)*((a_.) + (b_.)*x))*(F_)[v_] /; FreeQ[{a, b, c}, x] && InverseFunctionQ[F[x]]]
```

Rule 3475

```
Int[tan[(c_.) + (d_.)*(x_)], x_Symbol] :=> -Simp[Log[RemoveContent[Cos[c + d*x], x]]/d, x] /; FreeQ[{c, d}, x]
```

Rubi steps

$$\begin{aligned} \int e^x \tan(e^x) dx &= \text{Subst}\left(\int \tan(x) dx, x, e^x\right) \\ &= -\log(\cos(e^x)) \end{aligned}$$

Mathematica [A] time = 0.01, size = 7, normalized size = 1.00

$$-\log(\cos(e^x))$$

Antiderivative was successfully verified.

[In] $\text{Integrate}[E^x \cdot \text{Tan}[E^x], x]$

[Out] $-\text{Log}[\text{Cos}[E^x]]$

fricas [A] time = 1.10, size = 12, normalized size = 1.71

$$-\frac{1}{2} \log\left(\frac{1}{\tan(e^x)^2 + 1}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{integrate}(\exp(x) \cdot \tan(\exp(x)), x, \text{algorithm}="fricas")$

[Out] $-1/2 \cdot \log(1/(\tan(e^x)^2 + 1))$

giac [A] time = 0.12, size = 7, normalized size = 1.00

$$-\log(|\cos(e^x)|)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(x)*tan(exp(x)),x, algorithm="giac")

[Out] -log(abs(cos(e^x)))

maple [A] time = 0.00, size = 7, normalized size = 1.00

$$-\ln(\cos(e^x))$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(exp(x)*tan(exp(x)),x)

[Out] -ln(cos(exp(x)))

maxima [A] time = 0.31, size = 4, normalized size = 0.57

$$\log(\sec(e^x))$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(x)*tan(exp(x)),x, algorithm="maxima")

[Out] log(sec(e^x))

mupad [B] time = 2.65, size = 10, normalized size = 1.43

$$\frac{\ln(\tan(e^x)^2 + 1)}{2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(tan(exp(x))*exp(x),x)

[Out] log(tan(exp(x))^2 + 1)/2

sympy [A] time = 0.16, size = 10, normalized size = 1.43

$$\frac{\log(\tan^2(e^x) + 1)}{2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(x)*tan(exp(x)),x)

[Out] log(tan(exp(x))**2 + 1)/2

3.70 $\int e^x \sec(e^x) dx$

Optimal. Leaf size=5

$$\tanh^{-1}(\sin(e^x))$$

[Out] arctanh(sin(exp(x)))

Rubi [A] time = 0.01, antiderivative size = 5, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 8, $\frac{\text{number of rules}}{\text{integrand size}} = 0.250$, Rules used = {2282, 3770}

$$\tanh^{-1}(\sin(e^x))$$

Antiderivative was successfully verified.

[In] Int[E^x*Sec[E^x],x]

[Out] ArcTanh[Sin[E^x]]

Rule 2282

```
Int[u_, x_Symbol] := With[{v = FunctionOfExponential[u, x]}, Dist[v/D[v, x], Subst[Int[FunctionOfExponentialFunction[u, x]/x, x], x, v], x] /; FunctionOfExponentialQ[u, x] && !MatchQ[u, (w_)*((a_.)*(v_)^(n_))^(m_) /; FreeQ[{a, m, n}, x] && IntegerQ[m*n]] && !MatchQ[u, E^((c_.)*((a_.) + (b_.)*x))*(F_)[v_] /; FreeQ[{a, b, c}, x] && InverseFunctionQ[F[x]]]
```

Rule 3770

```
Int[csc[(c_.) + (d_.)*(x_)], x_Symbol] := -Simp[ArcTanh[Cos[c + d*x]]/d, x] /; FreeQ[{c, d}, x]
```

Rubi steps

$$\begin{aligned} \int e^x \sec(e^x) dx &= \text{Subst}\left(\int \sec(x) dx, x, e^x\right) \\ &= \tanh^{-1}(\sin(e^x)) \end{aligned}$$

Mathematica [A] time = 0.01, size = 5, normalized size = 1.00

$$\tanh^{-1}(\sin(e^x))$$

Antiderivative was successfully verified.

[In] Integrate[E^x*Sec[E^x],x]

[Out] ArcTanh[Sin[E^x]]

fricas [B] time = 0.53, size = 19, normalized size = 3.80

$$\frac{1}{2} \log(\sin(e^x) + 1) - \frac{1}{2} \log(-\sin(e^x) + 1)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(x)*sec(exp(x)),x, algorithm="fricas")

[Out] 1/2*log(sin(e^x) + 1) - 1/2*log(-sin(e^x) + 1)

giac [B] time = 0.12, size = 29, normalized size = 5.80

$$\frac{1}{4} \log \left(\left| \frac{1}{\sin(e^x)} + \sin(e^x) + 2 \right| \right) - \frac{1}{4} \log \left(\left| \frac{1}{\sin(e^x)} + \sin(e^x) - 2 \right| \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(x)*sec(exp(x)),x, algorithm="giac")

[Out] 1/4*log(abs(1/sin(e^x) + sin(e^x) + 2)) - 1/4*log(abs(1/sin(e^x) + sin(e^x) - 2))

maple [A] time = 0.00, size = 9, normalized size = 1.80

$$\ln(\sec(e^x) + \tan(e^x))$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(exp(x)*sec(exp(x)),x)

[Out] ln(sec(exp(x))+tan(exp(x)))

maxima [A] time = 0.31, size = 8, normalized size = 1.60

$$\log(\sec(e^x) + \tan(e^x))$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(x)*sec(exp(x)),x, algorithm="maxima")

[Out] log(sec(e^x) + tan(e^x))

mupad [B] time = 2.79, size = 10, normalized size = 2.00

$$-\operatorname{atan}\left(e^{e^x} 1i\right) 2i$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(exp(x)/cos(exp(x)),x)

[Out] -atan(exp(exp(x)*1i))*2i

sympy [A] time = 1.02, size = 10, normalized size = 2.00

$$\log(\tan(e^x) + \sec(e^x))$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(x)*sec(exp(x)),x)

[Out] log(tan(exp(x)) + sec(exp(x)))

3.71 $\int e^x \sec(e^x) \tan(e^x) dx$

Optimal. Leaf size=4

$$\sec(e^x)$$

[Out] sec(exp(x))

Rubi [A] time = 0.02, antiderivative size = 4, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 3, integrand size = 12, $\frac{\text{number of rules}}{\text{integrand size}} = 0.250$, Rules used = {2282, 2606, 8}

$$\sec(e^x)$$

Antiderivative was successfully verified.

[In] Int[E^x*Sec[E^x]*Tan[E^x],x]

[Out] Sec[E^x]

Rule 8

Int[a_, x_Symbol] :> Simp[a*x, x] /; FreeQ[a, x]

Rule 2282

Int[u_, x_Symbol] :> With[{v = FunctionOfExponential[u, x]}, Dist[v/D[v, x], Subst[Int[FunctionOfExponentialFunction[u, x]/x, x], x, v], x] /; FunctionOfExponentialQ[u, x] && !MatchQ[u, (w_)*((a_.)*(v_)^(n_))^(m_)] /; FreeQ[{a, m, n}, x] && IntegerQ[m*n] && !MatchQ[u, E^((c_.)*((a_.) + (b_.)*x))*(F_)[v_] /; FreeQ[{a, b, c}, x] && InverseFunctionQ[F[x]]]

Rule 2606

Int[((a_.)*sec[(e_.) + (f_.)*(x_)])^(m_.)*((b_.)*tan[(e_.) + (f_.)*(x_)])^(n_.), x_Symbol] :> Dist[a/f, Subst[Int[(a*x)^(m - 1)*(-1 + x^2)^((n - 1)/2), x], x, Sec[e + f*x]], x] /; FreeQ[{a, e, f, m}, x] && IntegerQ[(n - 1)/2] && !(IntegerQ[m/2] && LtQ[0, m, n + 1])

Rubi steps

$$\begin{aligned} \int e^x \sec(e^x) \tan(e^x) dx &= \text{Subst} \left(\int \sec(x) \tan(x) dx, x, e^x \right) \\ &= \text{Subst} \left(\int 1 dx, x, \sec(e^x) \right) \\ &= \sec(e^x) \end{aligned}$$

Mathematica [A] time = 0.01, size = 4, normalized size = 1.00

$$\sec(e^x)$$

Antiderivative was successfully verified.

[In] Integrate[E^x*Sec[E^x]*Tan[E^x],x]

[Out] Sec[E^x]

fricas [A] time = 1.10, size = 5, normalized size = 1.25

$$\frac{1}{\cos(e^x)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(x)*sec(exp(x))*tan(exp(x)),x, algorithm="fricas")

[Out] 1/cos(e^x)

giac [A] time = 0.13, size = 5, normalized size = 1.25

$$\frac{1}{\cos(e^x)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(x)*sec(exp(x))*tan(exp(x)),x, algorithm="giac")

[Out] 1/cos(e^x)

maple [A] time = 0.03, size = 4, normalized size = 1.00

$$\sec(e^x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(exp(x)*sec(exp(x))*tan(exp(x)),x)

[Out] sec(exp(x))

maxima [A] time = 0.31, size = 5, normalized size = 1.25

$$\frac{1}{\cos(e^x)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(x)*sec(exp(x))*tan(exp(x)),x, algorithm="maxima")

[Out] 1/cos(e^x)

mupad [B] time = 0.09, size = 5, normalized size = 1.25

$$\frac{1}{\cos(e^x)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((tan(exp(x))*exp(x))/cos(exp(x)),x)

[Out] 1/cos(exp(x))

sympy [A] time = 0.60, size = 3, normalized size = 0.75

$$\sec(e^x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(x)*sec(exp(x))*tan(exp(x)),x)

[Out] sec(exp(x))

3.72 $\int e^x \csc^2(e^x) dx$

Optimal. Leaf size=6

$$-\cot(e^x)$$

[Out] $-\cot(\exp(x))$

Rubi [A] time = 0.02, antiderivative size = 6, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 3, integrand size = 10, $\frac{\text{number of rules}}{\text{integrand size}} = 0.300$, Rules used = {2282, 3767, 8}

$$-\cot(e^x)$$

Antiderivative was successfully verified.

[In] $\text{Int}[E^x * \text{Csc}[E^x]^2, x]$

[Out] $-\text{Cot}[E^x]$

Rule 8

$\text{Int}[a_, x_Symbol] \rightarrow \text{Simp}[a*x, x] /; \text{FreeQ}[a, x]$

Rule 2282

$\text{Int}[u_, x_Symbol] \rightarrow \text{With}[\{v = \text{FunctionOfExponential}[u, x]\}, \text{Dist}[v/D[v, x], \text{Subst}[\text{Int}[\text{FunctionOfExponentialFunction}[u, x]/x, x], x, v], x]] /; \text{FunctionOfExponentialQ}[u, x] \&\& \text{!MatchQ}[u, (w_)*((a_.)*(v_)^(n_))^(m_)] /; \text{FreeQ}[\{a, m, n\}, x] \&\& \text{IntegerQ}[m*n] \&\& \text{!MatchQ}[u, E^((c_.)*((a_.) + (b_.)*x))*(F_)[v_]] /; \text{FreeQ}[\{a, b, c\}, x] \&\& \text{InverseFunctionQ}[F[x]]]$

Rule 3767

$\text{Int}[\text{csc}[(c_.) + (d_.)*(x_)]^(n_), x_Symbol] \rightarrow -\text{Dist}[d^(-1), \text{Subst}[\text{Int}[\text{ExpandIntegrand}[(1 + x^2)^(n/2 - 1), x], x], x, \text{Cot}[c + d*x]], x] /; \text{FreeQ}[\{c, d\}, x] \&\& \text{IGtQ}[n/2, 0]$

Rubi steps

$$\begin{aligned} \int e^x \csc^2(e^x) dx &= \text{Subst}\left(\int \csc^2(x) dx, x, e^x\right) \\ &= -\text{Subst}\left(\int 1 dx, x, \cot(e^x)\right) \\ &= -\cot(e^x) \end{aligned}$$

Mathematica [A] time = 0.02, size = 6, normalized size = 1.00

$$-\cot(e^x)$$

Antiderivative was successfully verified.

[In] $\text{Integrate}[E^x * \text{Csc}[E^x]^2, x]$

[Out] $-\text{Cot}[E^x]$

fricas [A] time = 0.76, size = 10, normalized size = 1.67

$$-\frac{\cos(e^x)}{\sin(e^x)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(x)*csc(exp(x))^2,x, algorithm="fricas")

[Out] -cos(e^x)/sin(e^x)

giac [A] time = 0.12, size = 7, normalized size = 1.17

$$-\frac{1}{\tan(e^x)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(x)*csc(exp(x))^2,x, algorithm="giac")

[Out] -1/tan(e^x)

maple [A] time = 0.03, size = 6, normalized size = 1.00

$$-\cot(e^x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(exp(x)*csc(exp(x))^2,x)

[Out] -cot(exp(x))

maxima [A] time = 0.31, size = 7, normalized size = 1.17

$$-\frac{1}{\tan(e^x)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(x)*csc(exp(x))^2,x, algorithm="maxima")

[Out] -1/tan(e^x)

mupad [B] time = 2.27, size = 13, normalized size = 2.17

$$-\frac{2i}{e^{e^x 2i} - 1}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(exp(x)/sin(exp(x))^2,x)

[Out] -2i/(exp(exp(x)*2i) - 1)

sympy [A] time = 0.81, size = 5, normalized size = 0.83

$$-\cot(e^x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(x)*csc(exp(x))**2,x)

[Out] -cot(exp(x))

3.73 $\int e^x \sin(a + bx) dx$

Optimal. Leaf size=37

$$\frac{e^x \sin(a + bx)}{b^2 + 1} - \frac{be^x \cos(a + bx)}{b^2 + 1}$$

[Out] $-b \exp(x) \cos(bx+a)/(b^2+1) + \exp(x) \sin(bx+a)/(b^2+1)$

Rubi [A] time = 0.01, antiderivative size = 37, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 10, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {4432}

$$\frac{e^x \sin(a + bx)}{b^2 + 1} - \frac{be^x \cos(a + bx)}{b^2 + 1}$$

Antiderivative was successfully verified.

[In] Int[E^x*Sin[a + b*x],x]

[Out] $-((b \cdot E^x \cdot \cos[a + b \cdot x]) / (1 + b^2)) + (E^x \cdot \sin[a + b \cdot x]) / (1 + b^2)$

Rule 4432

Int[(F_)^((c_.)*((a_.) + (b_.)*(x_)))*Sin[(d_.) + (e_.)*(x_)], x_Symbol] :>
 Simp[(b*c*Log[F]*F^(c*(a + b*x))*Sin[d + e*x])/(e^2 + b^2*c^2*Log[F]^2), x
] - Simp[(e*F^(c*(a + b*x))*Cos[d + e*x])/(e^2 + b^2*c^2*Log[F]^2), x] /; FreeQ[{F, a, b, c, d, e}, x] && NeQ[e^2 + b^2*c^2*Log[F]^2, 0]

Rubi steps

$$\int e^x \sin(a + bx) dx = -\frac{be^x \cos(a + bx)}{1 + b^2} + \frac{e^x \sin(a + bx)}{1 + b^2}$$

Mathematica [A] time = 0.06, size = 27, normalized size = 0.73

$$\frac{e^x(\sin(a + bx) - b \cos(a + bx))}{b^2 + 1}$$

Antiderivative was successfully verified.

[In] Integrate[E^x*Sin[a + b*x],x]

[Out] $(E^x * (-b \cos[a + b \cdot x]) + \sin[a + b \cdot x]) / (1 + b^2)$

fricas [A] time = 1.19, size = 30, normalized size = 0.81

$$-\frac{b \cos(bx + a) e^x - e^x \sin(bx + a)}{b^2 + 1}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(x)*sin(b*x+a),x, algorithm="fricas")

[Out] $-(b \cos(bx + a) \cdot e^x - e^x \sin(bx + a)) / (b^2 + 1)$

giac [A] time = 0.12, size = 35, normalized size = 0.95

$$-\left(\frac{b \cos(bx + a)}{b^2 + 1} - \frac{\sin(bx + a)}{b^2 + 1}\right) e^x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(x)*sin(b*x+a),x, algorithm="giac")

[Out] $-(b \cos(bx + a)/(b^2 + 1) - \sin(bx + a)/(b^2 + 1))e^x$

maple [A] time = 0.01, size = 36, normalized size = 0.97

$$-\frac{b e^x \cos(bx + a)}{b^2 + 1} + \frac{e^x \sin(bx + a)}{b^2 + 1}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(exp(x)*sin(b*x+a),x)

[Out] $-b \exp(x) \cos(bx+a)/(b^2+1) + \exp(x) \sin(bx+a)/(b^2+1)$

maxima [A] time = 0.31, size = 28, normalized size = 0.76

$$\frac{(b \cos(bx + a) - \sin(bx + a))e^x}{b^2 + 1}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(x)*sin(b*x+a),x, algorithm="maxima")

[Out] $-(b \cos(bx + a) - \sin(bx + a))e^x/(b^2 + 1)$

mupad [B] time = 0.10, size = 26, normalized size = 0.70

$$\frac{e^x (\sin(a + bx) - b \cos(a + bx))}{b^2 + 1}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(exp(x)*sin(a + b*x),x)

[Out] $(\exp(x) * (\sin(a + b*x) - b \cos(a + b*x)))/(b^2 + 1)$

sympy [A] time = 0.79, size = 116, normalized size = 3.14

$$\begin{cases} \frac{x e^x \sin(a - ix)}{2} + \frac{i x e^x \cos(a - ix)}{2} - \frac{i e^x \cos(a - ix)}{2} & \text{for } b = -i \\ \frac{x e^x \sin(a + ix)}{2} - \frac{i x e^x \cos(a + ix)}{2} + \frac{i e^x \cos(a + ix)}{2} & \text{for } b = i \\ -\frac{b e^x \cos(a + bx)}{b^2 + 1} + \frac{e^x \sin(a + bx)}{b^2 + 1} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(x)*sin(b*x+a),x)

[Out] Piecewise((x*exp(x)*sin(a - I*x)/2 + I*x*exp(x)*cos(a - I*x)/2 - I*exp(x)*cos(a - I*x)/2, Eq(b, -I)), (x*exp(x)*sin(a + I*x)/2 - I*x*exp(x)*cos(a + I*x)/2 + I*exp(x)*cos(a + I*x)/2, Eq(b, I)), (-b*exp(x)*cos(a + b*x)/(b**2 + 1) + exp(x)*sin(a + b*x)/(b**2 + 1), True))

3.74 $\int e^x \sin(a + cx^2) dx$

Optimal. Leaf size=115

$$\frac{(-1)^{3/4} \sqrt{\pi} e^{\frac{1}{4}i(4a+\frac{1}{c})} \operatorname{erf}\left(\frac{\sqrt[4]{-1}(1+2icx)}{2\sqrt{c}}\right)}{4\sqrt{c}} + \frac{(-1)^{3/4} \sqrt{\pi} e^{-\frac{1}{4}i(4a+\frac{1}{c})} \operatorname{erfi}\left(\frac{\sqrt[4]{-1}(1-2icx)}{2\sqrt{c}}\right)}{4\sqrt{c}}$$

[Out] $1/4*(-1)^{(3/4)}*\exp(1/4*I*(4*a+1/c))*\operatorname{erf}(1/2*(-1)^{(1/4)}*(1+2*I*c*x)/c^{(1/2)})$
 $*\pi^{(1/2)}/c^{(1/2)}+1/4*(-1)^{(3/4)}*\operatorname{erfi}(1/2*(-1)^{(1/4)}*(1-2*I*c*x)/c^{(1/2)})*P$
 $i^{(1/2)}/\exp(1/4*I*(4*a+1/c))/c^{(1/2)}$

Rubi [A] time = 0.12, antiderivative size = 115, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 4, integrand size = 12, $\frac{\text{number of rules}}{\text{integrand size}} = 0.333$, Rules used = {4472, 2234, 2204, 2205}

$$\frac{(-1)^{3/4} \sqrt{\pi} e^{\frac{1}{4}i(4a+\frac{1}{c})} \operatorname{Erf}\left(\frac{\sqrt[4]{-1}(1+2icx)}{2\sqrt{c}}\right)}{4\sqrt{c}} + \frac{(-1)^{3/4} \sqrt{\pi} e^{-\frac{1}{4}i(4a+\frac{1}{c})} \operatorname{Erfi}\left(\frac{\sqrt[4]{-1}(1-2icx)}{2\sqrt{c}}\right)}{4\sqrt{c}}$$

Antiderivative was successfully verified.

[In] Int[E^x*Sin[a + c*x^2], x]

[Out] $((-1)^{(3/4)}*E^{((I/4)*(4*a + c^{(-1))})}*Sqrt[\pi]*\operatorname{Erf}[\frac{((-1)^{(1/4)}*(1 + (2*I)*c*x))/(2*Sqrt[c])}{(4*Sqrt[c])}] + ((-1)^{(3/4)}*Sqrt[\pi]*\operatorname{Erfi}[\frac{((-1)^{(1/4)}*(1 - (2*I)*c*x))/(2*Sqrt[c])}{(4*Sqrt[c]*E^{((I/4)*(4*a + c^{(-1))})})})])$

Rule 2204

Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))²), x_Symbol] := Simp[(F^a*Sqrt[\pi]*Erfi[(c + d*x)*Rt[b*Log[F], 2]])/(2*d*Rt[b*Log[F], 2]), x] /; FreeQ[{F, a, b, c, d}, x] && PosQ[b]

Rule 2205

Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))²), x_Symbol] := Simp[(F^a*Sqrt[\pi]*Erf[(c + d*x)*Rt[-(b*Log[F]), 2]])/(2*d*Rt[-(b*Log[F]), 2]), x] /; FreeQ[{F, a, b, c, d}, x] && NegQ[b]

Rule 2234

Int[(F_)^((a_.) + (b_.)*(x_) + (c_.)*(x_)²), x_Symbol] := Dist[F^(a - b^2/(4*c)), Int[F^((b + 2*c*x)^2/(4*c)), x], x] /; FreeQ[{F, a, b, c}, x]

Rule 4472

Int[(F_)^(u_)*Sin[v_]^(n_), x_Symbol] := Int[ExpandTrigToExp[F^u, Sin[v]^n, x], x] /; FreeQ[F, x] && (LinearQ[u, x] || PolyQ[u, x, 2]) && (LinearQ[v, x] || PolyQ[v, x, 2]) && IGtQ[n, 0]

Rubi steps

$$\begin{aligned}
\int e^x \sin(a + cx^2) dx &= \int \left(\frac{1}{2} i e^{-ia+x-icx^2} - \frac{1}{2} i e^{ia+x+icx^2} \right) dx \\
&= \frac{1}{2} i \int e^{-ia+x-icx^2} dx - \frac{1}{2} i \int e^{ia+x+icx^2} dx \\
&= \frac{1}{2} \left(i e^{-\frac{1}{4}i(4a+\frac{1}{c})} \right) \int e^{\frac{i(1-2icx)^2}{4c}} dx - \frac{1}{2} \left(i e^{\frac{1}{4}i(4a+\frac{1}{c})} \right) \int e^{-\frac{i(1+2icx)^2}{4c}} dx \\
&= \frac{(-1)^{3/4} e^{\frac{1}{4}i(4a+\frac{1}{c})} \sqrt{\pi} \operatorname{erf} \left(\frac{\sqrt[4]{-1}(1+2icx)}{2\sqrt{c}} \right) + (-1)^{3/4} e^{-\frac{1}{4}i(4a+\frac{1}{c})} \sqrt{\pi} \operatorname{erfi} \left(\frac{\sqrt[4]{-1}(1-2icx)}{2\sqrt{c}} \right)}{4\sqrt{c}}
\end{aligned}$$

Mathematica [A] time = 0.16, size = 108, normalized size = 0.94

$$\frac{\sqrt[4]{-1} \sqrt{\pi} e^{-\frac{i}{4}/c} \left(e^{\frac{i}{2}/c} (\cos(a) + i \sin(a)) \operatorname{erfi} \left(\frac{\sqrt[4]{-1}(2cx-i)}{2\sqrt{c}} \right) + (\sin(a) + i \cos(a)) \operatorname{erfi} \left(\frac{(-1)^{3/4}(2cx+i)}{2\sqrt{c}} \right) \right)}{4\sqrt{c}}$$

Antiderivative was successfully verified.

[In] Integrate[E^x*Sin[a + c*x^2],x]

[Out] $-1/4 * ((-1)^{(1/4)} * \operatorname{Sqrt}[\pi] * (E^{((I/2)/c)} * \operatorname{Erfi} [((-1)^{(1/4)} * (-I + 2*c*x)) / (2*\operatorname{Sqrt}[c])]) * (\operatorname{Cos}[a] + I*\operatorname{Sin}[a]) + \operatorname{Erfi} [((-1)^{(3/4)} * (I + 2*c*x)) / (2*\operatorname{Sqrt}[c])]) * (I * \operatorname{Cos}[a] + \operatorname{Sin}[a])) / (\operatorname{Sqrt}[c] * E^{(I/4)/c})$

fricas [B] time = 0.57, size = 193, normalized size = 1.68

$$\frac{i \sqrt{2} \pi \sqrt{\frac{c}{\pi}} e^{\left(\frac{-4iac-i}{4c}\right)} C\left(\frac{\sqrt{2}(2cx+i)\sqrt{\frac{c}{\pi}}}{2c}\right) + i \sqrt{2} \pi \sqrt{\frac{c}{\pi}} e^{\left(\frac{4iac+i}{4c}\right)} C\left(-\frac{\sqrt{2}(2cx-i)\sqrt{\frac{c}{\pi}}}{2c}\right) + \sqrt{2} \pi \sqrt{\frac{c}{\pi}} e^{\left(\frac{-4iac-i}{4c}\right)} S\left(\frac{\sqrt{2}(2cx+i)\sqrt{\frac{c}{\pi}}}{2c}\right) + \sqrt{2} \pi \sqrt{\frac{c}{\pi}} e^{\left(\frac{4iac+i}{4c}\right)} S\left(-\frac{\sqrt{2}(2cx-i)\sqrt{\frac{c}{\pi}}}{2c}\right)}{4c}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(x)*sin(c*x^2+a),x, algorithm="fricas")

[Out] $1/4 * (I*\operatorname{sqrt}(2)*\pi*\operatorname{sqrt}(c/\pi)*e^{(1/4*(-4*I*a*c - I)/c)}*\operatorname{fresnel_cos}(1/2*\operatorname{sqrt}(2)*(2*c*x + I)*\operatorname{sqrt}(c/\pi)/c) + I*\operatorname{sqrt}(2)*\pi*\operatorname{sqrt}(c/\pi)*e^{(1/4*(4*I*a*c + I)/c)}*\operatorname{fresnel_cos}(-1/2*\operatorname{sqrt}(2)*(2*c*x - I)*\operatorname{sqrt}(c/\pi)/c) + \operatorname{sqrt}(2)*\pi*\operatorname{sqrt}(c/\pi)*e^{(1/4*(-4*I*a*c - I)/c)}*\operatorname{fresnel_sin}(1/2*\operatorname{sqrt}(2)*(2*c*x + I)*\operatorname{sqrt}(c/\pi)/c) - \operatorname{sqrt}(2)*\pi*\operatorname{sqrt}(c/\pi)*e^{(1/4*(4*I*a*c + I)/c)}*\operatorname{fresnel_sin}(-1/2*\operatorname{sqrt}(2)*(2*c*x - I)*\operatorname{sqrt}(c/\pi)/c)) / c$

giac [A] time = 0.16, size = 127, normalized size = 1.10

$$\frac{i \sqrt{2} \sqrt{\pi} \operatorname{erf} \left(-\frac{1}{4} \sqrt{2} \left(2x + \frac{i}{c} \right) \left(\frac{ic}{|c|} + 1 \right) \sqrt{|c|} \right) e^{\left(\frac{-4iac+i}{4c} \right)} + i \sqrt{2} \sqrt{\pi} \operatorname{erf} \left(-\frac{1}{4} \sqrt{2} \left(2x - \frac{i}{c} \right) \left(-\frac{ic}{|c|} + 1 \right) \sqrt{|c|} \right) e^{\left(\frac{-4iac-i}{4c} \right)}}{4 \left(\frac{ic}{|c|} + 1 \right) \sqrt{|c|}} + \frac{i \sqrt{2} \sqrt{\pi} \operatorname{erf} \left(-\frac{1}{4} \sqrt{2} \left(2x - \frac{i}{c} \right) \left(-\frac{ic}{|c|} + 1 \right) \sqrt{|c|} \right) e^{\left(\frac{-4iac-i}{4c} \right)} + i \sqrt{2} \sqrt{\pi} \operatorname{erf} \left(-\frac{1}{4} \sqrt{2} \left(2x + \frac{i}{c} \right) \left(\frac{ic}{|c|} + 1 \right) \sqrt{|c|} \right) e^{\left(\frac{-4iac+i}{4c} \right)}}{4 \left(-\frac{ic}{|c|} + 1 \right) \sqrt{|c|}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(x)*sin(c*x^2+a),x, algorithm="giac")

[Out] $-1/4 * I*\operatorname{sqrt}(2)*\operatorname{sqrt}(\pi)*\operatorname{erf}(-1/4*\operatorname{sqrt}(2)*(2*x + I/c)*(I*c/\operatorname{abs}(c) + 1)*\operatorname{sqrt}(\operatorname{abs}(c))) * e^{(-1/4*(4*I*a*c + I)/c)} / ((I*c/\operatorname{abs}(c) + 1)*\operatorname{sqrt}(\operatorname{abs}(c))) + 1/4 * I*\operatorname{sqrt}(2)*\operatorname{sqrt}(\pi)*\operatorname{erf}(-1/4*\operatorname{sqrt}(2)*(2*x - I/c)*(-I*c/\operatorname{abs}(c) + 1)*\operatorname{sqrt}(\operatorname{abs}(c))) * e^{(-1/4*(-4*I*a*c - I)/c)} / ((-I*c/\operatorname{abs}(c) + 1)*\operatorname{sqrt}(\operatorname{abs}(c)))$

maple [A] time = 0.16, size = 88, normalized size = 0.77

$$-\frac{i\sqrt{\pi} e^{\frac{i(4ac+1)}{4c}} \operatorname{erf}\left(\sqrt{-ic} x - \frac{1}{2\sqrt{-ic}}\right)}{4\sqrt{-ic}} + \frac{i\sqrt{\pi} e^{-\frac{i(4ac+1)}{4c}} \operatorname{erf}\left(\sqrt{ic} x - \frac{1}{2\sqrt{ic}}\right)}{4\sqrt{ic}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(exp(x)*sin(c*x^2+a),x)`

[Out] $-1/4*I*Pi^{(1/2)}*exp(1/4*I*(4*a*c+1)/c)/(-I*c)^{(1/2)}*erf((-I*c)^{(1/2)}*x-1/2/(-I*c)^{(1/2)})+1/4*I*Pi^{(1/2)}*exp(-1/4*I*(4*a*c+1)/c)/(I*c)^{(1/2)}*erf((I*c)^{(1/2)}*x-1/2/(I*c)^{(1/2)})$

maxima [A] time = 0.34, size = 100, normalized size = 0.87

$$\frac{\sqrt{2}\sqrt{\pi}\left(\left(-(i+1)\cos\left(\frac{4ac+1}{4c}\right)+(i-1)\sin\left(\frac{4ac+1}{4c}\right)\right)\operatorname{erf}\left(\frac{2icx-1}{2\sqrt{ic}}\right)+\left(-(i-1)\cos\left(\frac{4ac+1}{4c}\right)+(i+1)\sin\left(\frac{4ac+1}{4c}\right)\right)\right)}{8\sqrt{c}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(exp(x)*sin(c*x^2+a),x, algorithm="maxima")`

[Out] $-1/8*\sqrt{2}*\sqrt{\pi}*((-(I+1)*\cos(1/4*(4*a*c+1)/c)+(I-1)*\sin(1/4*(4*a*c+1)/c))*\operatorname{erf}(1/2*(2*I*c*x-1)/\sqrt{I*c})+(-(I-1)*\cos(1/4*(4*a*c+1)/c)+(I+1)*\sin(1/4*(4*a*c+1)/c))*\operatorname{erf}(1/2*(2*I*c*x+1)/\sqrt{-I*c})/\sqrt{c}$

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int e^x \sin(cx^2 + a) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(exp(x)*sin(a+c*x^2),x)`

[Out] `int(exp(x)*sin(a+c*x^2),x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int e^x \sin(a + cx^2) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(exp(x)*sin(c*x**2+a),x)`

[Out] `Integral(exp(x)*sin(a+c*x**2),x)`

3.75 $\int e^x \sin(a + bx + cx^2) dx$

Optimal. Leaf size=144

$$\frac{(-1)^{3/4} \sqrt{\pi} e^{\frac{1}{4}i\left(4a + \frac{(1+ib)^2}{c}\right)} \operatorname{erf}\left(\frac{\sqrt[4]{-1}(ib+2icx+1)}{2\sqrt{c}}\right)}{4\sqrt{c}} + \frac{(-1)^{3/4} \sqrt{\pi} e^{\frac{i(b+i)^2}{4c} - ia} \operatorname{erfi}\left(\frac{\sqrt[4]{-1}(-ib-2icx+1)}{2\sqrt{c}}\right)}{4\sqrt{c}}$$

[Out] $1/4*(-1)^{(3/4)}*\exp(1/4*I*(4*a+(1+I*b)^2/c))*\operatorname{erf}(1/2*(-1)^{(1/4)}*(1+I*b+2*I*c*x)/c^{(1/2)})*\operatorname{Pi}^{(1/2)}/c^{(1/2)}+1/4*(-1)^{(3/4)}*\exp(-I*a+1/4*I*(I+b)^2/c)*\operatorname{erfi}(1/2*(-1)^{(1/4)}*(1-I*b-2*I*c*x)/c^{(1/2)})*\operatorname{Pi}^{(1/2)}/c^{(1/2)}$

Rubi [A] time = 0.22, antiderivative size = 144, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 4, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.267$, Rules used = {4472, 2234, 2204, 2205}

$$\frac{(-1)^{3/4} \sqrt{\pi} e^{\frac{1}{4}i\left(4a + \frac{(1+ib)^2}{c}\right)} \operatorname{Erf}\left(\frac{\sqrt[4]{-1}(ib+2icx+1)}{2\sqrt{c}}\right)}{4\sqrt{c}} + \frac{(-1)^{3/4} \sqrt{\pi} e^{\frac{i(b+i)^2}{4c} - ia} \operatorname{Erfi}\left(\frac{\sqrt[4]{-1}(-ib-2icx+1)}{2\sqrt{c}}\right)}{4\sqrt{c}}$$

Antiderivative was successfully verified.

[In] `Int[E^x*Sin[a + b*x + c*x^2], x]`

[Out] $((-1)^{(3/4)}*E^{((I/4)*(4*a + (1 + I*b)^2/c))*\operatorname{Sqrt}[\operatorname{Pi}]*\operatorname{Erf}(((1 + I*b + (2*I)*c*x)/(2*\operatorname{Sqrt}[c])))/(4*\operatorname{Sqrt}[c])} + ((-1)^{(3/4)}*E^{((-I)*a + ((I/4)*(I + b)^2)/c))*\operatorname{Sqrt}[\operatorname{Pi}]*\operatorname{Erfi}(((1 - I*b - (2*I)*c*x)/(2*\operatorname{Sqrt}[c])))/(4*\operatorname{Sqrt}[c])}$

Rule 2204

`Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_)) ^2), x_Symbol] := Simp[(F^a*Sqrt[Pi]*Erfi[(c + d*x)*Rt[b*Log[F], 2]])/(2*d*Rt[b*Log[F], 2]), x] /; FreeQ[{F, a, b, c, d}, x] && PosQ[b]`

Rule 2205

`Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_)) ^2), x_Symbol] := Simp[(F^a*Sqrt[Pi]*Erf[(c + d*x)*Rt[-(b*Log[F]), 2]])/(2*d*Rt[-(b*Log[F]), 2]), x] /; FreeQ[{F, a, b, c, d}, x] && NegQ[b]`

Rule 2234

`Int[(F_)^((a_.) + (b_.)*(x_) + (c_.)*(x_) ^2), x_Symbol] := Dist[F^(a - b^2/(4*c)), Int[F^((b + 2*c*x)^2/(4*c)), x], x] /; FreeQ[{F, a, b, c}, x]`

Rule 4472

`Int[(F_)^(u_)*Sin[v_]^(n_), x_Symbol] := Int[ExpandTrigToExp[F^u, Sin[v]^n, x], x] /; FreeQ[F, x] && (LinearQ[u, x] || PolyQ[u, x, 2]) && (LinearQ[v, x] || PolyQ[v, x, 2]) && IGtQ[n, 0]`

Rubi steps

$$\begin{aligned}
\int e^x \sin(a + bx + cx^2) dx &= \int \left(\frac{1}{2} i e^{-ia + (1-ib)x - icx^2} - \frac{1}{2} i e^{ia + (1+ib)x + icx^2} \right) dx \\
&= \frac{1}{2} i \int e^{-ia + (1-ib)x - icx^2} dx - \frac{1}{2} i \int e^{ia + (1+ib)x + icx^2} dx \\
&= -\left(\frac{1}{2} \left(i e^{\frac{1}{4} \left(4a + \frac{(1+ib)^2}{c} \right)} \right) \int e^{-\frac{i(1+ib+2icx)^2}{4c}} dx \right) + \frac{1}{2} \left(i e^{-\frac{i(1-2ib-b^2+4ac)}{4c}} \right) \int e^{\frac{i(1-ib-2icx)^2}{4c}} dx \\
&= \frac{(-1)^{3/4} e^{\frac{1}{4} \left(4a + \frac{(1+ib)^2}{c} \right)} \sqrt{\pi} \operatorname{erf} \left(\frac{\sqrt[4]{-1} (1+ib+2icx)}{2\sqrt{c}} \right)}{4\sqrt{c}} + \frac{(-1)^{3/4} e^{-\frac{i(1-2ib-b^2+4ac)}{4c}} \sqrt{\pi} \operatorname{erfi} \left(\frac{\sqrt[4]{-1} (1-ib-2icx)}{2\sqrt{c}} \right)}{4\sqrt{c}}
\end{aligned}$$

Mathematica [A] time = 0.26, size = 134, normalized size = 0.93

$$\frac{\sqrt[4]{-1} \sqrt{\pi} e^{-\frac{i(b^2-2ib+1)}{4c}} \left(e^{\frac{ib^2}{2c}} (\sin(a) + i \cos(a)) \operatorname{erfi} \left(\frac{(-1)^{3/4} (b+2cx+i)}{2\sqrt{c}} \right) + e^{\frac{i}{2c}} (\cos(a) + i \sin(a)) \operatorname{erfi} \left(\frac{\sqrt[4]{-1} (b+2cx-i)}{2\sqrt{c}} \right) \right)}{4\sqrt{c}}$$

Antiderivative was successfully verified.

[In] Integrate[E^x*Sin[a + b*x + c*x^2],x]

[Out] $-1/4 * ((-1)^{(1/4)} * \text{Sqrt}[\text{Pi}] * (E^{((I/2)/c)} * \text{Erfi} [((-1)^{(1/4)} * (-I + b + 2*c*x)) / (2*\text{Sqrt}[c])]) * (\text{Cos}[a] + I*\text{Sin}[a]) + E^{(((I/2)*b^2)/c)} * \text{Erfi} [((-1)^{(3/4)} * (I + b + 2*c*x)) / (2*\text{Sqrt}[c])]) * (I*\text{Cos}[a] + \text{Sin}[a])) / (\text{Sqrt}[c] * E^{(((I/4)*(1 - (2*I)*b + b^2))/c)})$

fricas [B] time = 0.87, size = 229, normalized size = 1.59

$$\frac{i \sqrt{2} \pi \sqrt{\frac{c}{\pi}} e^{\left(\frac{ib^2-4iac-2b-i}{4c} \right)} C \left(\frac{\sqrt{2}(2cx+b+i)\sqrt{\frac{c}{\pi}}}{2c} \right) + i \sqrt{2} \pi \sqrt{\frac{c}{\pi}} e^{\left(\frac{-ib^2+4iac-2b+i}{4c} \right)} C \left(-\frac{\sqrt{2}(2cx+b-i)\sqrt{\frac{c}{\pi}}}{2c} \right) + \sqrt{2} \pi \sqrt{\frac{c}{\pi}} e^{\left(\frac{ib^2-4iac-2b-i}{4c} \right)}}{4c}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(x)*sin(c*x^2+b*x+a),x, algorithm="fricas")

[Out] $1/4 * (I*\text{sqrt}(2)*\text{pi}*\text{sqrt}(c/\text{pi}) * e^{(1/4*(I*b^2 - 4*I*a*c - 2*b - I)/c)} * \text{fresnel_cos}(1/2*\text{sqrt}(2)*(2*c*x + b + I)*\text{sqrt}(c/\text{pi})/c) + I*\text{sqrt}(2)*\text{pi}*\text{sqrt}(c/\text{pi}) * e^{(1/4*(-I*b^2 + 4*I*a*c - 2*b + I)/c)} * \text{fresnel_cos}(-1/2*\text{sqrt}(2)*(2*c*x + b - I)*\text{sqrt}(c/\text{pi})/c) + \text{sqrt}(2)*\text{pi}*\text{sqrt}(c/\text{pi}) * e^{(1/4*(I*b^2 - 4*I*a*c - 2*b - I)/c)} * \text{fresnel_sin}(1/2*\text{sqrt}(2)*(2*c*x + b + I)*\text{sqrt}(c/\text{pi})/c) - \text{sqrt}(2)*\text{pi}*\text{sqrt}(c/\text{pi}) * e^{(1/4*(-I*b^2 + 4*I*a*c - 2*b + I)/c)} * \text{fresnel_sin}(-1/2*\text{sqrt}(2)*(2*c*x + b - I)*\text{sqrt}(c/\text{pi})/c)) / c$

giac [A] time = 0.16, size = 147, normalized size = 1.02

$$\frac{i \sqrt{2} \sqrt{\pi} \operatorname{erf} \left(-\frac{1}{4} \sqrt{2} \left(2x + \frac{b-i}{c} \right) \left(-\frac{ic}{|c|} + 1 \right) \sqrt{|c|} \right) e^{\left(\frac{ib^2-4iac+2b-i}{4c} \right)} + i \sqrt{2} \sqrt{\pi} \operatorname{erf} \left(-\frac{1}{4} \sqrt{2} \left(2x + \frac{b+i}{c} \right) \left(\frac{ic}{|c|} + 1 \right) \sqrt{|c|} \right) e^{\left(\frac{-ib^2+4iac-2b+i}{4c} \right)}}{4 \left(-\frac{ic}{|c|} + 1 \right) \sqrt{|c|}} + \frac{i \sqrt{2} \sqrt{\pi} \operatorname{erf} \left(-\frac{1}{4} \sqrt{2} \left(2x + \frac{b+i}{c} \right) \left(\frac{ic}{|c|} + 1 \right) \sqrt{|c|} \right) e^{\left(\frac{-ib^2+4iac-2b+i}{4c} \right)}}{4 \left(\frac{ic}{|c|} + 1 \right) \sqrt{|c|}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(x)*sin(c*x^2+b*x+a),x, algorithm="giac")

[Out] $1/4 * I*\text{sqrt}(2)*\text{sqrt}(\text{pi}) * \operatorname{erf}(-1/4*\text{sqrt}(2)*(2*x + (b - I)/c)*(-I*c/\text{abs}(c) + 1)*\text{sqrt}(\text{abs}(c))) * e^{(-1/4*(I*b^2 - 4*I*a*c + 2*b - I)/c)} / (((-I*c/\text{abs}(c) + 1)*\text{sq}$

rt(abs(c))) - 1/4*I*sqrt(2)*sqrt(pi)*erf(-1/4*sqrt(2)*(2*x + (b + I)/c)*(I*c/abs(c) + 1)*sqrt(abs(c)))*e^(-1/4*(-I*b^2 + 4*I*a*c + 2*b + I)/c)/((I*c/abs(c) + 1)*sqrt(abs(c)))

maple [A] time = 0.16, size = 119, normalized size = 0.83

$$\frac{i\sqrt{\pi} e^{\frac{i(4ac-b^2+2ib+1)}{4c}} \operatorname{erf}\left(-\sqrt{-ic} x + \frac{ib+1}{2\sqrt{-ic}}\right)}{4\sqrt{-ic}} + \frac{i\sqrt{\pi} e^{-\frac{i(4ac-b^2-2ib+1)}{4c}} \operatorname{erf}\left(\sqrt{ic} x - \frac{-ib+1}{2\sqrt{ic}}\right)}{4\sqrt{ic}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(exp(x)*sin(c*x^2+b*x+a), x)

[Out] 1/4*I*Pi^(1/2)*exp(1/4*I*(-b^2+2*I*b+4*a*c+1)/c)/(-I*c)^(1/2)*erf(-(-I*c)^(1/2)*x+1/2*(1+I*b)/(-I*c)^(1/2))+1/4*I*Pi^(1/2)*exp(-1/4*I*(-b^2-2*I*b+4*a*c+1)/c)/(I*c)^(1/2)*erf((I*c)^(1/2)*x-1/2*(-I*b+1)/(I*c)^(1/2))

maxima [A] time = 0.35, size = 131, normalized size = 0.91

$$\frac{\sqrt{2}\sqrt{\pi}\left(\left((i+1)\cos\left(-\frac{b^2-4ac-1}{4c}\right)-(i-1)\sin\left(-\frac{b^2-4ac-1}{4c}\right)\right)\operatorname{erf}\left(\frac{i(2ic+ib-1)\sqrt{ic}}{2c}\right)+\left(-(i-1)\cos\left(-\frac{b^2-4ac-1}{4c}\right)\right)\right)}{8\sqrt{c}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(x)*sin(c*x^2+b*x+a), x, algorithm="maxima")

[Out] -1/8*sqrt(2)*sqrt(pi)*(((I + 1)*cos(-1/4*(b^2 - 4*a*c - 1)/c) - (I - 1)*sin(-1/4*(b^2 - 4*a*c - 1)/c))*erf(1/2*I*(2*I*c*x + I*b - 1)*sqrt(I*c)/c) + (- (I - 1)*cos(-1/4*(b^2 - 4*a*c - 1)/c) + (I + 1)*sin(-1/4*(b^2 - 4*a*c - 1)/c))*erf(1/2*I*(2*I*c*x + I*b + 1)*sqrt(-I*c)/c)*e^(-1/2*b/c)/sqrt(c)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \sin(cx^2 + bx + a) e^x dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(sin(a + b*x + c*x^2)*exp(x), x)

[Out] int(sin(a + b*x + c*x^2)*exp(x), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int e^x \sin(a + bx + cx^2) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(x)*sin(c*x**2+b*x+a), x)

[Out] Integral(exp(x)*sin(a + b*x + c*x**2), x)

3.76 $\int e^{x^2} \sin(a + bx) dx$

Optimal. Leaf size=81

$$\frac{1}{4}i\sqrt{\pi}e^{\frac{b^2}{4}-ia}\operatorname{erfi}\left(\frac{1}{2}(2x-ib)\right) - \frac{1}{4}i\sqrt{\pi}e^{\frac{b^2}{4}+ia}\operatorname{erfi}\left(\frac{1}{2}(2x+ib)\right)$$

[Out] $-1/4*I*\exp(-I*a+1/4*b^2)*\operatorname{erfi}(1/2*I*b-x)*\operatorname{Pi}^{(1/2)}-1/4*I*\exp(I*a+1/4*b^2)*\operatorname{erfi}(1/2*I*b+x)*\operatorname{Pi}^{(1/2)}$

Rubi [A] time = 0.05, antiderivative size = 81, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 3, integrand size = 12, $\frac{\text{number of rules}}{\text{integrand size}} = 0.250$, Rules used = {4472, 2234, 2204}

$$\frac{1}{4}i\sqrt{\pi}e^{\frac{b^2}{4}-ia}\operatorname{Erfi}\left(\frac{1}{2}(2x-ib)\right) - \frac{1}{4}i\sqrt{\pi}e^{\frac{b^2}{4}+ia}\operatorname{Erfi}\left(\frac{1}{2}(2x+ib)\right)$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[E^{x^2}*\operatorname{Sin}[a + b*x], x]$

[Out] $(I/4)*E^{((-I)*a + b^2/4)*\operatorname{Sqrt}[\operatorname{Pi}]*\operatorname{Erfi}[((-I)*b + 2*x)/2]} - (I/4)*E^{(I*a + b^2/4)*\operatorname{Sqrt}[\operatorname{Pi}]*\operatorname{Erfi}[(I*b + 2*x)/2]}$

Rule 2204

$\operatorname{Int}[(F_)^{((a_.) + (b_.)*((c_.) + (d_.)*(x_))^{2})}, x_Symbol] \rightarrow \operatorname{Simp}[(F^a*\operatorname{Sqrt}[\operatorname{Pi}]*\operatorname{Erfi}[(c + d*x)*\operatorname{Rt}[b*\operatorname{Log}[F], 2]])/(2*d*\operatorname{Rt}[b*\operatorname{Log}[F], 2]), x] /; \operatorname{FreeQ}\{F, a, b, c, d\}, x] \&\& \operatorname{PosQ}[b]$

Rule 2234

$\operatorname{Int}[(F_)^{((a_.) + (b_.)*(x_) + (c_.)*(x_)^2)}, x_Symbol] \rightarrow \operatorname{Dist}[F^{(a - b^2/(4*c))}, \operatorname{Int}[F^{((b + 2*c*x)^2/(4*c))}, x], x] /; \operatorname{FreeQ}\{F, a, b, c\}, x]$

Rule 4472

$\operatorname{Int}[(F_)^{(u_)*\operatorname{Sin}[v_]^{(n_.)}}, x_Symbol] \rightarrow \operatorname{Int}[\operatorname{ExpandTrigToExp}[F^u, \operatorname{Sin}[v]^{(n)}], x] /; \operatorname{FreeQ}[F, x] \&\& (\operatorname{LinearQ}[u, x] \parallel \operatorname{PolyQ}[u, x, 2]) \&\& (\operatorname{LinearQ}[v, x] \parallel \operatorname{PolyQ}[v, x, 2]) \&\& \operatorname{IGtQ}[n, 0]$

Rubi steps

$$\begin{aligned} \int e^{x^2} \sin(a + bx) dx &= \int \left(\frac{1}{2}ie^{-ia-ibx+x^2} - \frac{1}{2}ie^{ia+ibx+x^2} \right) dx \\ &= \frac{1}{2}i \int e^{-ia-ibx+x^2} dx - \frac{1}{2}i \int e^{ia+ibx+x^2} dx \\ &= \frac{1}{2} \left(ie^{-ia+\frac{b^2}{4}} \right) \int e^{\frac{1}{4}(-ib+2x)^2} dx - \frac{1}{2} \left(ie^{ia+\frac{b^2}{4}} \right) \int e^{\frac{1}{4}(ib+2x)^2} dx \\ &= \frac{1}{4}ie^{-ia+\frac{b^2}{4}}\sqrt{\pi}\operatorname{erfi}\left(\frac{1}{2}(-ib+2x)\right) - \frac{1}{4}ie^{ia+\frac{b^2}{4}}\sqrt{\pi}\operatorname{erfi}\left(\frac{1}{2}(ib+2x)\right) \end{aligned}$$

Mathematica [A] time = 0.02, size = 81, normalized size = 1.00

$$\frac{1}{4}\sqrt{\pi}e^{\frac{b^2}{4}}\left(\cos(a)\operatorname{erf}\left(\frac{b}{2}-ix\right)+\cos(a)\operatorname{erf}\left(\frac{b}{2}+ix\right)+\sin(a)\left(\operatorname{erfi}\left(\frac{1}{2}(2x-ib)\right)+\operatorname{erfi}\left(\frac{1}{2}(2x+ib)\right)\right)\right)$$

Antiderivative was successfully verified.

[In] Integrate[E^x^2*Sin[a + b*x],x]

[Out] (E^(b^2/4)*Sqrt[Pi]*(Cos[a]*Erf[b/2 - I*x] + Cos[a]*Erf[b/2 + I*x] + (Erfi[(-I)*b + 2*x]/2] + Erfi[(I*b + 2*x)/2])*Sin[a])/4

fricas [A] time = 0.70, size = 45, normalized size = 0.56

$$-\frac{1}{4}\sqrt{\pi}\left(\operatorname{erf}\left(-\frac{1}{2}b+ix\right)e^{\left(\frac{1}{4}b^2+ia\right)}-\operatorname{erf}\left(\frac{1}{2}b+ix\right)e^{\left(\frac{1}{4}b^2-ia\right)}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(x^2)*sin(b*x+a),x, algorithm="fricas")

[Out] -1/4*sqrt(pi)*(erf(-1/2*b + I*x)*e^(1/4*b^2 + I*a) - erf(1/2*b + I*x)*e^(1/4*b^2 - I*a))

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int e^{x^2} \sin(bx + a) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(x^2)*sin(b*x+a),x, algorithm="giac")

[Out] integrate(e^(x^2)*sin(b*x + a), x)

maple [A] time = 0.00, size = 52, normalized size = 0.64

$$\frac{\sqrt{\pi} e^{\frac{b^2}{4}} e^{ia} \operatorname{erf}\left(-ix + \frac{b}{2}\right)}{4} + \frac{\sqrt{\pi} e^{\frac{b^2}{4}} e^{-ia} \operatorname{erf}\left(ix + \frac{b}{2}\right)}{4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(exp(x^2)*sin(b*x+a),x)

[Out] 1/4*Pi^(1/2)*exp(1/4*b^2)*exp(I*a)*erf(-I*x+1/2*b)+1/4*Pi^(1/2)*exp(1/4*b^2)*exp(-I*a)*erf(I*x+1/2*b)

maxima [A] time = 0.33, size = 51, normalized size = 0.63

$$\frac{1}{4}\sqrt{\pi}\left((\cos(a)-i\sin(a))\operatorname{erf}\left(\frac{1}{2}b+ix\right)e^{\left(\frac{1}{4}b^2\right)}-(\cos(a)+i\sin(a))\operatorname{erf}\left(-\frac{1}{2}b+ix\right)e^{\left(\frac{1}{4}b^2\right)}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(x^2)*sin(b*x+a),x, algorithm="maxima")

[Out] 1/4*sqrt(pi)*((cos(a) - I*sin(a))*erf(1/2*b + I*x)*e^(1/4*b^2) - (cos(a) + I*sin(a))*erf(-1/2*b + I*x)*e^(1/4*b^2))

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int e^{x^2} \sin(a + bx) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(exp(x^2)*sin(a + b*x),x)

[Out] int(exp(x^2)*sin(a + b*x), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int e^{x^2} \sin(a + bx) dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(x**2)*sin(b*x+a),x)
```

```
[Out] Integral(exp(x**2)*sin(a + b*x), x)
```


3.77 $\int e^{x^2} \sin(a + cx^2) dx$

Optimal. Leaf size=87

$$\frac{i\sqrt{\pi} e^{-ia} \operatorname{erfi}(\sqrt{1-ic}x)}{4\sqrt{1-ic}} - \frac{i\sqrt{\pi} e^{ia} \operatorname{erfi}(\sqrt{1+ic}x)}{4\sqrt{1+ic}}$$

[Out] $1/4*I*\operatorname{erfi}(x*(1-I*c)^{(1/2)})*Pi^{(1/2)}/\exp(I*a)/(1-I*c)^{(1/2)}-1/4*I*\exp(I*a)*\operatorname{erfi}(x*(1+I*c)^{(1/2)})*Pi^{(1/2)/(1+I*c)^{(1/2)}$

Rubi [A] time = 0.10, antiderivative size = 87, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 2, integrand size = 14, $\frac{\text{number of rules}}{\text{integrand size}} = 0.143$, Rules used = {4472, 2204}

$$\frac{i\sqrt{\pi} e^{-ia} \operatorname{Erfi}(\sqrt{1-ic}x)}{4\sqrt{1-ic}} - \frac{i\sqrt{\pi} e^{ia} \operatorname{Erfi}(\sqrt{1+ic}x)}{4\sqrt{1+ic}}$$

Antiderivative was successfully verified.

[In] Int[E^x^2*Sin[a + c*x^2],x]

[Out] $((I/4)*\operatorname{Sqrt}[Pi]*\operatorname{Erfi}[\operatorname{Sqrt}[1-I*c]*x])/(\operatorname{Sqrt}[1-I*c]*E^{(I*a)}) - ((I/4)*E^{(I*a)}*\operatorname{Sqrt}[Pi]*\operatorname{Erfi}[\operatorname{Sqrt}[1+I*c]*x])/(\operatorname{Sqrt}[1+I*c])$

Rule 2204

Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_)^2), x_Symbol] :> Simp[(F^a*Sqrt[Pi]*Erfi[(c + d*x)*Rt[b*Log[F], 2]])/(2*d*Rt[b*Log[F], 2]), x] /; FreeQ[{F, a, b, c, d}, x] && PosQ[b]

Rule 4472

Int[(F_)^(u_)*Sin[v_]^(n_), x_Symbol] :> Int[ExpandTrigToExp[F^u, Sin[v]^n, x], x] /; FreeQ[F, x] && (LinearQ[u, x] || PolyQ[u, x, 2]) && (LinearQ[v, x] || PolyQ[v, x, 2]) && IGtQ[n, 0]

Rubi steps

$$\begin{aligned} \int e^{x^2} \sin(a + cx^2) dx &= \int \left(\frac{1}{2} i e^{-ia+(1-ic)x^2} - \frac{1}{2} i e^{ia+(1+ic)x^2} \right) dx \\ &= \frac{1}{2} i \int e^{-ia+(1-ic)x^2} dx - \frac{1}{2} i \int e^{ia+(1+ic)x^2} dx \\ &= \frac{i e^{-ia} \sqrt{\pi} \operatorname{erfi}(\sqrt{1-ic}x)}{4\sqrt{1-ic}} - \frac{i e^{ia} \sqrt{\pi} \operatorname{erfi}(\sqrt{1+ic}x)}{4\sqrt{1+ic}} \end{aligned}$$

Mathematica [A] time = 0.24, size = 129, normalized size = 1.48

$$\frac{\sqrt[4]{-1} \sqrt{\pi} \left(\sqrt{c+i} \left(\sin(a) \operatorname{erf}\left(\frac{(1+i)\sqrt{c+ix}}{\sqrt{2}}\right) + \operatorname{erfi}\left((-1)^{3/4} \sqrt{c+ix}\right) (c \sin(a) + ic \cos(a) + \cos(a)) \right) + \sqrt{c-i} (c + \dots) \right)}{4(c^2 + 1)}$$

Antiderivative was successfully verified.

[In] Integrate[E^x^2*Sin[a + c*x^2],x]

```
[Out] -1/4*((-1)^(1/4)*Sqrt[Pi]*(Sqrt[-I + c]*(I + c)*Erfi[(-1)^(1/4)*Sqrt[-I + c]
]*x)*(Cos[a] + I*Sin[a] + Sqrt[I + c]*(Erf[((1 + I)*Sqrt[I + c]*x)/Sqrt[2]
]*Sin[a] + Erfi[(-1)^(3/4)*Sqrt[I + c]*x]*(Cos[a] + I*c*Cos[a] + c*Sin[a]))
)/(1 + c^2)
```

fricas [A] time = 0.71, size = 66, normalized size = 0.76

$$\frac{\sqrt{\pi}(c+i)\sqrt{-ic-1} \operatorname{erf}(\sqrt{-ic-1}x)e^{ia} + \sqrt{\pi}(c-i)\sqrt{ic-1} \operatorname{erf}(\sqrt{ic-1}x)e^{-ia}}{4(c^2+1)}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(x^2)*sin(c*x^2+a),x, algorithm="fricas")
```

```
[Out] 1/4*(sqrt(pi)*(c + I)*sqrt(-I*c - 1)*erf(sqrt(-I*c - 1)*x)*e^(I*a) + sqrt(pi)
i*(c - I)*sqrt(I*c - 1)*erf(sqrt(I*c - 1)*x)*e^(-I*a))/(c^2 + 1)
```

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int e^{(x^2)} \sin(cx^2 + a) dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(x^2)*sin(c*x^2+a),x, algorithm="giac")
```

```
[Out] integrate(e^(x^2)*sin(c*x^2 + a), x)
```

maple [A] time = 0.09, size = 62, normalized size = 0.71

$$-\frac{i\sqrt{\pi} e^{ia} \operatorname{erf}(\sqrt{-ic-1}x)}{4\sqrt{-ic-1}} + \frac{i\sqrt{\pi} e^{-ia} \operatorname{erf}(\sqrt{ic-1}x)}{4\sqrt{ic-1}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(x^2)*sin(c*x^2+a),x)
```

```
[Out] -1/4*I*Pi^(1/2)*exp(I*a)/(-I*c-1)^(1/2)*erf((-I*c-1)^(1/2)*x)+1/4*I*Pi^(1/2)
)*exp(-I*a)/(-1+I*c)^(1/2)*erf((-1+I*c)^(1/2)*x)
```

maxima [B] time = 0.34, size = 137, normalized size = 1.57

$$\frac{\sqrt{\pi} \sqrt{2c^2+2} ((\cos(a) - i \sin(a)) \operatorname{erf}(\sqrt{ic-1}x) + (\cos(a) + i \sin(a)) \operatorname{erf}(\sqrt{-ic-1}x)) \sqrt{\sqrt{c^2+1}+1} - \sqrt{\pi} \sqrt{2}}{8(c^2+1)}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(x^2)*sin(c*x^2+a),x, algorithm="maxima")
```

```
[Out] 1/8*(sqrt(pi)*sqrt(2*c^2 + 2)*((cos(a) - I*sin(a))*erf(sqrt(I*c - 1)*x) + (
cos(a) + I*sin(a))*erf(sqrt(-I*c - 1)*x))*sqrt(sqrt(c^2 + 1) + 1) - sqrt(pi)
)*sqrt(2*c^2 + 2)*((-I*cos(a) - sin(a))*erf(sqrt(I*c - 1)*x) + (I*cos(a) -
sin(a))*erf(sqrt(-I*c - 1)*x))*sqrt(sqrt(c^2 + 1) - 1))/(c^2 + 1)
```

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int e^{x^2} \sin(cx^2 + a) dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(x^2)*sin(a + c*x^2),x)
```

```
[Out] int(exp(x^2)*sin(a + c*x^2), x)
```

```
sympy [F] time = 0.00, size = 0, normalized size = 0.00
```

$$\int e^{x^2} \sin(a + cx^2) dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(x**2)*sin(c*x**2+a), x)
```

```
[Out] Integral(exp(x**2)*sin(a + c*x**2), x)
```

3.78 $\int e^{x^2} \sin(a + bx + cx^2) dx$

Optimal. Leaf size=155

$$\frac{i\sqrt{\pi} e^{-i\left(a - \frac{b^2}{4c+4i}\right)} \operatorname{erfi}\left(\frac{ib-2(1-ic)x}{2\sqrt{1-ic}}\right)}{4\sqrt{1-ic}} - \frac{i\sqrt{\pi} e^{ia + \frac{b^2}{4(1+ic)}} \operatorname{erfi}\left(\frac{ib+2(1+ic)x}{2\sqrt{1+ic}}\right)}{4\sqrt{1+ic}}$$

[Out] $-1/4*I*\operatorname{erfi}(1/2*(I*b-2*(1-I*c)*x)/(1-I*c)^{(1/2)})*\Pi^{(1/2)}/\exp(I*(a-b^2/(4*I+4*c)))/(1-I*c)^{(1/2)}-1/4*I*\exp(I*a+1/4*b^2/(1+I*c))*\operatorname{erfi}(1/2*(I*b+2*(1+I*c)*x)/(1+I*c)^{(1/2)})*\Pi^{(1/2)}/(1+I*c)^{(1/2)}$

Rubi [A] time = 0.20, antiderivative size = 155, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 3, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.176$, Rules used = {4472, 2234, 2204}

$$\frac{i\sqrt{\pi} e^{-i\left(a - \frac{b^2}{4c+4i}\right)} \operatorname{Erfi}\left(\frac{ib-2(1-ic)x}{2\sqrt{1-ic}}\right)}{4\sqrt{1-ic}} - \frac{i\sqrt{\pi} e^{ia + \frac{b^2}{4(1+ic)}} \operatorname{Erfi}\left(\frac{ib+2(1+ic)x}{2\sqrt{1+ic}}\right)}{4\sqrt{1+ic}}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[E^{x^2} \sin[a + b*x + c*x^2], x]$

[Out] $((-I/4)*\operatorname{Sqrt}[\Pi]*\operatorname{Erfi}[(I*b - 2*(1 - I*c)*x)/(2*\operatorname{Sqrt}[1 - I*c]])/(\operatorname{Sqrt}[1 - I*c]*E^{(I*(a - b^2/(4*I + 4*c)))}) - ((I/4)*E^{(I*a + b^2/(4*(1 + I*c)))})*\operatorname{Sqrt}[\Pi]*\operatorname{Erfi}[(I*b + 2*(1 + I*c)*x)/(2*\operatorname{Sqrt}[1 + I*c]])/\operatorname{Sqrt}[1 + I*c])$

Rule 2204

$\operatorname{Int}[(F_)^{((a_.) + (b_.)*((c_.) + (d_.)*(x_.)^2))}, x_Symbol] \rightarrow \operatorname{Simp}[(F^a*\operatorname{Sqrt}[\Pi]*\operatorname{Erfi}[(c + d*x)*\operatorname{Rt}[b*\operatorname{Log}[F], 2]])/(2*d*\operatorname{Rt}[b*\operatorname{Log}[F], 2]), x] /; \operatorname{FreeQ}[F, a, b, c, d], x] \&\& \operatorname{PosQ}[b]$

Rule 2234

$\operatorname{Int}[(F_)^{((a_.) + (b_.)*(x_.) + (c_.)*(x_.)^2))}, x_Symbol] \rightarrow \operatorname{Dist}[F^{(a - b^2/(4*c))}, \operatorname{Int}[F^{((b + 2*c*x)^2/(4*c))}, x], x] /; \operatorname{FreeQ}[F, a, b, c], x]$

Rule 4472

$\operatorname{Int}[(F_)^{(u_)}*\sin[v_]^{(n_.)}, x_Symbol] \rightarrow \operatorname{Int}[\operatorname{ExpandTrigToExp}[F^u, \sin[v]^n], x] /; \operatorname{FreeQ}[F, x] \&\& (\operatorname{LinearQ}[u, x] \parallel \operatorname{PolyQ}[u, x, 2]) \&\& (\operatorname{LinearQ}[v, x] \parallel \operatorname{PolyQ}[v, x, 2]) \&\& \operatorname{IGtQ}[n, 0]$

Rubi steps

$$\begin{aligned} \int e^{x^2} \sin(a + bx + cx^2) dx &= \int \left(\frac{1}{2} i e^{-ia - ibx + (1-ic)x^2} - \frac{1}{2} i e^{ia + ibx + (1+ic)x^2} \right) dx \\ &= \frac{1}{2} i \int e^{-ia - ibx + (1-ic)x^2} dx - \frac{1}{2} i \int e^{ia + ibx + (1+ic)x^2} dx \\ &= -\left(\frac{1}{2} \left(i e^{ia + \frac{b^2}{4(1+ic)}} \right) \int \exp\left(\frac{(ib + 2(1+ic)x)^2}{4(1+ic)}\right) dx \right) + \frac{1}{2} \left(i e^{-i\left(a - \frac{b^2}{4i+4c}\right)} \right) \int \exp\left(\frac{(-ib + 2(1-ic)x)^2}{4(1-ic)}\right) dx \\ &= -\frac{i e^{-i\left(a - \frac{b^2}{4i+4c}\right)} \sqrt{\pi} \operatorname{erfi}\left(\frac{ib-2(1-ic)x}{2\sqrt{1-ic}}\right)}{4\sqrt{1-ic}} - \frac{i e^{ia + \frac{b^2}{4(1+ic)}} \sqrt{\pi} \operatorname{erfi}\left(\frac{ib+2(1+ic)x}{2\sqrt{1+ic}}\right)}{4\sqrt{1+ic}} \end{aligned}$$

Mathematica [A] time = 0.58, size = 165, normalized size = 1.06

$$\frac{(-1)^{3/4} \sqrt{\pi} e^{-\frac{ib^2}{-4c+4i}} \left((c-i) \sqrt{c+i} e^{\frac{ib^2 c}{2c^2+2}} (\cos(a) - i \sin(a)) \operatorname{erfi} \left(\frac{(-1)^{3/4} (b+2(c+i)x)}{2\sqrt{c+i}} \right) + \sqrt{c-i} (c+i) (\sin(a) - i \cos(a)) \right)}{4(c^2+1)}$$

Antiderivative was successfully verified.

[In] Integrate[E^x^2*Sin[a + b*x + c*x^2], x]

[Out] -1/4*((-1)^(3/4)*E^((I*b^2)/(4*I - 4*c))*Sqrt[Pi]*((-I + c)*Sqrt[I + c]*E^((I*b^2*c)/(2 + 2*c^2))*Erfi[((-1)^(3/4)*(b + 2*(I + c)*x))/(2*Sqrt[I + c]])*(Cos[a] - I*Sin[a]) + Sqrt[-I + c]*(I + c)*Erfi[((-1)^(1/4)*(b + 2*(-I + c)*x))/(2*Sqrt[-I + c]])*((-I)*Cos[a] + Sin[a]))/(1 + c^2)

fricas [A] time = 2.07, size = 161, normalized size = 1.04

$$\frac{\sqrt{\pi} (c-i) \sqrt{ic-1} \operatorname{erf} \left(-\frac{(bc+2(c^2+1)x-ib) \sqrt{ic-1}}{2(c^2+1)} \right) e^{\left(\frac{ib^2c-4iac^2+b^2-4ia}{4(c^2+1)} \right)} - \sqrt{\pi} (c+i) \sqrt{-ic-1} \operatorname{erf} \left(\frac{(bc+2(c^2+1)x+ib) \sqrt{-ic-1}}{2(c^2+1)} \right)}{4(c^2+1)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(x^2)*sin(c*x^2+b*x+a), x, algorithm="fricas")

[Out] -1/4*(sqrt(pi)*(c - I)*sqrt(I*c - 1)*erf(-1/2*(b*c + 2*(c^2 + 1)*x - I*b)*sqrt(I*c - 1)/(c^2 + 1))*e^(1/4*(I*b^2*c - 4*I*a*c^2 + b^2 - 4*I*a)/(c^2 + 1)) - sqrt(pi)*(c + I)*sqrt(-I*c - 1)*erf(1/2*(b*c + 2*(c^2 + 1)*x + I*b)*sqrt(-I*c - 1)/(c^2 + 1))*e^(1/4*(-I*b^2*c + 4*I*a*c^2 + b^2 + 4*I*a)/(c^2 + 1)))/(c^2 + 1)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int e^{(x^2)} \sin(cx^2 + bx + a) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(x^2)*sin(c*x^2+b*x+a), x, algorithm="giac")

[Out] integrate(e^(x^2)*sin(c*x^2 + b*x + a), x)

maple [A] time = 0.19, size = 129, normalized size = 0.83

$$\frac{i\sqrt{\pi} e^{-\frac{4ac-4ia-b^2}{4(ic+1)}} \operatorname{erf} \left(-\sqrt{-ic-1} x + \frac{ib}{2\sqrt{-ic-1}} \right)}{4\sqrt{-ic-1}} + \frac{i\sqrt{\pi} e^{\frac{4ac+4ia-b^2}{4ic-4}} \operatorname{erf} \left(\sqrt{ic-1} x + \frac{ib}{2\sqrt{ic-1}} \right)}{4\sqrt{ic-1}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(exp(x^2)*sin(c*x^2+b*x+a), x)

[Out] 1/4*I*Pi^(1/2)*exp(-1/4*(4*a*c-4*I*a-b^2)/(1+I*c))/(-I*c-1)^(1/2)*erf(-(-I*c-1)^(1/2)*x+1/2*I*b/(-I*c-1)^(1/2))+1/4*I*Pi^(1/2)*exp(1/4*(4*a*c+4*I*a-b^2)/(-1+I*c))/(-1+I*c)^(1/2)*erf((-1+I*c)^(1/2)*x+1/2*I*b/(-1+I*c)^(1/2))

maxima [B] time = 0.40, size = 475, normalized size = 3.06

$$\sqrt{\pi} \sqrt{2c^2+2} \left(\left(\cos \left(-\frac{b^2c-4ac^2-4a}{4(c^2+1)} \right) e^{\left(\frac{b^2}{4(c^2+1)} \right)} - i e^{\left(\frac{b^2}{4(c^2+1)} \right)} \sin \left(-\frac{b^2c-4ac^2-4a}{4(c^2+1)} \right) \right) \operatorname{erf} \left(-\frac{2(-ic+1)x-ib}{2\sqrt{ic-1}} \right) - \left(\cos \left(-\frac{b^2c-4ac^2-4a}{4(c^2+1)} \right) e^{\left(\frac{b^2}{4(c^2+1)} \right)} + i e^{\left(\frac{b^2}{4(c^2+1)} \right)} \sin \left(-\frac{b^2c-4ac^2-4a}{4(c^2+1)} \right) \right) \operatorname{erf} \left(\frac{2(-ic+1)x+ib}{2\sqrt{-ic-1}} \right) \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(x^2)*sin(c*x^2+b*x+a),x, algorithm="maxima")

[Out] $\frac{1}{8}(\sqrt{\pi})\sqrt{2c^2 + 2}((\cos(-\frac{1}{4}(b^2c - 4ac^2 - 4a)/(c^2 + 1))e^{\frac{1}{4}b^2/(c^2 + 1)} - Ie^{\frac{1}{4}b^2/(c^2 + 1)}\sin(-\frac{1}{4}(b^2c - 4ac^2 - 4a)/(c^2 + 1)))\operatorname{erf}(-\frac{1}{2}(2(-Ic + 1)x - Ib)/\sqrt{Ic - 1}) - (\cos(-\frac{1}{4}(b^2c - 4ac^2 - 4a)/(c^2 + 1))e^{\frac{1}{4}b^2/(c^2 + 1)} + Ie^{\frac{1}{4}b^2/(c^2 + 1)}\sin(-\frac{1}{4}(b^2c - 4ac^2 - 4a)/(c^2 + 1)))\operatorname{erf}(-\frac{1}{2}(2(-Ic - 1)x - Ib)/\sqrt{-Ic - 1}))\sqrt{(\sqrt{c^2 + 1} + 1) - \sqrt{\pi})\sqrt{2c^2 + 2}}((-\cos(-\frac{1}{4}(b^2c - 4ac^2 - 4a)/(c^2 + 1))e^{\frac{1}{4}b^2/(c^2 + 1)} - e^{\frac{1}{4}b^2/(c^2 + 1)}\sin(-\frac{1}{4}(b^2c - 4ac^2 - 4a)/(c^2 + 1)))\operatorname{erf}(-\frac{1}{2}(2(-Ic + 1)x - Ib)/\sqrt{Ic - 1}) + (-\cos(-\frac{1}{4}(b^2c - 4ac^2 - 4a)/(c^2 + 1))e^{\frac{1}{4}b^2/(c^2 + 1)} + e^{\frac{1}{4}b^2/(c^2 + 1)}\sin(-\frac{1}{4}(b^2c - 4ac^2 - 4a)/(c^2 + 1)))\operatorname{erf}(-\frac{1}{2}(2(-Ic - 1)x - Ib)/\sqrt{-Ic - 1}))\sqrt{(\sqrt{c^2 + 1} - 1)/(c^2 + 1)}$

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \sin(cx^2 + bx + a) e^{x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(sin(a + b*x + c*x^2)*exp(x^2),x)

[Out] int(sin(a + b*x + c*x^2)*exp(x^2), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int e^{x^2} \sin(a + bx + cx^2) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(x**2)*sin(c*x**2+b*x+a),x)

[Out] Integral(exp(x**2)*sin(a + b*x + c*x**2), x)

3.79 $\int f^{a+bx} \sin(d + fx^2) dx$

Optimal. Leaf size=142

$$\frac{1}{4}(-1)^{3/4}\sqrt{\pi}f^{a-1/2}e^{\frac{1}{4}i\left(\frac{b^2\log^2(f)}{f}+4d\right)}\operatorname{erf}\left(\frac{\sqrt[4]{-1}(b\log(f)+2ifx)}{2\sqrt{f}}\right)-\frac{1}{4}(-1)^{3/4}\sqrt{\pi}f^{a-1/2}e^{-\frac{1}{4}i\left(\frac{b^2\log^2(f)}{f}+4d\right)}\operatorname{erfi}\left(\frac{\sqrt[4]{-1}(-b\log(f)+2ifx)}{2\sqrt{f}}\right)$$

[Out] $\frac{1}{4}(-1)^{3/4}\exp(1/4*I*(4*d+b^2*\ln(f)^2/f))*f^{(-1/2+a)}*\operatorname{erf}(1/2*(-1)^{(1/4)}*(2*I*f*x+b*\ln(f))/f^{(1/2)})*\operatorname{Pi}^{(1/2)}-1/4*(-1)^{3/4}*f^{(-1/2+a)}*\operatorname{erfi}(1/2*(-1)^{(1/4)}*(2*I*f*x-b*\ln(f))/f^{(1/2)})*\operatorname{Pi}^{(1/2)}/\exp(1/4*I*(4*d+b^2*\ln(f)^2/f))$

Rubi [A] time = 0.21, antiderivative size = 142, normalized size of antiderivative = 1.00, number of steps used = 8, number of rules used = 5, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} = 0.312$, Rules used = {4472, 2287, 2234, 2204, 2205}

$$\frac{1}{4}(-1)^{3/4}\sqrt{\pi}f^{a-1/2}e^{\frac{1}{4}i\left(\frac{b^2\log^2(f)}{f}+4d\right)}\operatorname{Erf}\left(\frac{\sqrt[4]{-1}(b\log(f)+2ifx)}{2\sqrt{f}}\right)-\frac{1}{4}(-1)^{3/4}\sqrt{\pi}f^{a-1/2}e^{-\frac{1}{4}i\left(\frac{b^2\log^2(f)}{f}+4d\right)}\operatorname{Erfi}\left(\frac{\sqrt[4]{-1}(-b\log(f)+2ifx)}{2\sqrt{f}}\right)$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[f^{(a + b*x)}*\operatorname{Sin}[d + f*x^2], x]$

[Out] $((-1)^{(3/4)}*E^{((I/4)*(4*d + (b^2*\operatorname{Log}[f]^2)/f))}*f^{(-1/2 + a)}*\operatorname{Sqrt}[\operatorname{Pi}]*\operatorname{Erf}[((-1)^{(1/4)}*((2*I)*f*x + b*\operatorname{Log}[f]))/(2*\operatorname{Sqrt}[f])])/4 - ((-1)^{(3/4)}*f^{(-1/2 + a)}*\operatorname{Sqrt}[\operatorname{Pi}]*\operatorname{Erfi}[((-1)^{(1/4)}*((2*I)*f*x - b*\operatorname{Log}[f]))/(2*\operatorname{Sqrt}[f])])/(4*E^{((I/4)*(4*d + (b^2*\operatorname{Log}[f]^2)/f))})$

Rule 2204

$\operatorname{Int}[(F_)^{((a_.) + (b_.)*((c_.) + (d_.)*(x_))^2)}, x_Symbol] := \operatorname{Simp}[(F^a*\operatorname{Sqrt}[\operatorname{Pi}]*\operatorname{Erfi}[(c + d*x)*\operatorname{Rt}[b*\operatorname{Log}[F], 2]])/(2*d*\operatorname{Rt}[b*\operatorname{Log}[F], 2]), x] /;$ $\operatorname{FreeQ}\{F, a, b, c, d, x\} \ \&\& \ \operatorname{PosQ}[b]$

Rule 2205

$\operatorname{Int}[(F_)^{((a_.) + (b_.)*((c_.) + (d_.)*(x_))^2)}, x_Symbol] := \operatorname{Simp}[(F^a*\operatorname{Sqrt}[\operatorname{Pi}]*\operatorname{Erf}[(c + d*x)*\operatorname{Rt}[-(b*\operatorname{Log}[F]), 2]])/(2*d*\operatorname{Rt}[-(b*\operatorname{Log}[F]), 2]), x] /;$ $\operatorname{FreeQ}\{F, a, b, c, d, x\} \ \&\& \ \operatorname{NegQ}[b]$

Rule 2234

$\operatorname{Int}[(F_)^{((a_.) + (b_.)*(x_) + (c_.)*(x_)^2)}, x_Symbol] := \operatorname{Dist}[F^{(a - b^2/(4*c))}, \operatorname{Int}[F^{((b + 2*c*x)^2/(4*c))}, x], x] /;$ $\operatorname{FreeQ}\{F, a, b, c, x\}$

Rule 2287

$\operatorname{Int}[(u_)*(F_)^{(v_)}*(G_)^{(w_)}, x_Symbol] := \operatorname{With}\{z = v*\operatorname{Log}[F] + w*\operatorname{Log}[G]\}, \operatorname{Int}[u*\operatorname{NormalizeIntegrand}[E^z, x], x] /;$ $\operatorname{BinomialQ}[z, x] \ || \ (\operatorname{PolynomialQ}[z, x] \ \&\& \ \operatorname{LeQ}[\operatorname{Exponent}[z, x], 2]) /;$ $\operatorname{FreeQ}\{F, G, x\}$

Rule 4472

$\operatorname{Int}[(F_)^{(u_)}*\operatorname{Sin}[v_]^{(n_.)}, x_Symbol] := \operatorname{Int}[\operatorname{ExpandTrigToExp}[F^u, \operatorname{Sin}[v]^n], x] /;$ $\operatorname{FreeQ}[F, x] \ \&\& \ (\operatorname{LinearQ}[u, x] \ || \ \operatorname{PolyQ}[u, x, 2]) \ \&\& \ (\operatorname{LinearQ}[v, x] \ || \ \operatorname{PolyQ}[v, x, 2]) \ \&\& \ \operatorname{IGtQ}[n, 0]$

Rubi steps

$$\begin{aligned}
\int f^{a+bx} \sin(d + fx^2) dx &= \int \left(\frac{1}{2} i e^{-id-ifx^2} f^{a+bx} - \frac{1}{2} i e^{id+ifx^2} f^{a+bx} \right) dx \\
&= \frac{1}{2} i \int e^{-id-ifx^2} f^{a+bx} dx - \frac{1}{2} i \int e^{id+ifx^2} f^{a+bx} dx \\
&= \frac{1}{2} i \int e^{-id-ifx^2+a \log(f)+bx \log(f)} dx - \frac{1}{2} i \int e^{id+ifx^2+a \log(f)+bx \log(f)} dx \\
&= \frac{1}{2} \left(i e^{-\frac{1}{4} i \left(4d + \frac{b^2 \log^2(f)}{f} \right)} f^a \right) \int e^{\frac{i(-2ifx+b \log(f))^2}{4f}} dx - \frac{1}{2} \left(i e^{\frac{1}{4} i \left(4d + \frac{b^2 \log^2(f)}{f} \right)} f^a \right) \int e^{-\frac{i(2ifx+b \log(f))^2}{4f}} dx \\
&= \frac{1}{4} (-1)^{3/4} e^{\frac{1}{4} i \left(4d + \frac{b^2 \log^2(f)}{f} \right)} f^{-\frac{1}{2}+a} \sqrt{\pi} \operatorname{erf} \left(\frac{\sqrt[4]{-1} (2ifx + b \log(f))}{2\sqrt{f}} \right) - \frac{1}{4} (-1)^{3/4} e^{-\frac{1}{4} i \left(4d + \frac{b^2 \log^2(f)}{f} \right)} f^{-\frac{1}{2}+a} \sqrt{\pi} \operatorname{erf} \left(\frac{\sqrt[4]{-1} (2ifx + b \log(f))}{2\sqrt{f}} \right)
\end{aligned}$$

Mathematica [A] time = 0.23, size = 132, normalized size = 0.93

$$-\frac{1}{4} \sqrt[4]{-1} \sqrt{\pi} f^{a-\frac{1}{2}} e^{-\frac{ib^2 \log^2(f)}{4f}} \left(e^{\frac{ib^2 \log^2(f)}{2f}} (\cos(d) + i \sin(d)) \operatorname{erfi} \left(\frac{\sqrt[4]{-1} (2fx - ib \log(f))}{2\sqrt{f}} \right) + (\sin(d) + i \cos(d)) \operatorname{erfi} \left(\frac{\sqrt[4]{-1} (2fx + ib \log(f))}{2\sqrt{f}} \right) \right)$$

Antiderivative was successfully verified.

[In] Integrate[f^(a + b*x)*Sin[d + f*x^2],x]

[Out] $-\frac{1}{4}((-1)^{1/4})f^{a-1/2}\sqrt{\pi}\left(e^{\frac{ib^2\log^2(f)}{2f}}(\cos(d)+i\sin(d))\operatorname{erfi}\left(\frac{\sqrt[4]{-1}(2fx-ib\log(f))}{2\sqrt{f}}\right)+(\sin(d)+i\cos(d))\operatorname{erfi}\left(\frac{\sqrt[4]{-1}(2fx+ib\log(f))}{2\sqrt{f}}\right)\right)$

fricas [B] time = 0.73, size = 265, normalized size = 1.87

$$i\sqrt{2}\pi\sqrt{\frac{f}{\pi}}e^{\left(\frac{-ib^2\log(f)^2+4af\log(f)-4idf}{4f}\right)}C\left(\frac{\sqrt{2}(2fx+ib\log(f))\sqrt{\frac{f}{\pi}}}{2f}\right)+i\sqrt{2}\pi\sqrt{\frac{f}{\pi}}e^{\left(\frac{ib^2\log(f)^2+4af\log(f)+4idf}{4f}\right)}C\left(-\frac{\sqrt{2}(2fx-ib\log(f))\sqrt{\frac{f}{\pi}}}{2f}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(b*x+a)*sin(f*x^2+d),x, algorithm="fricas")

[Out] $\frac{1}{4}(i\sqrt{2})\pi\sqrt{\frac{f}{\pi}}e^{\frac{1}{4}(-Ib^2\log(f)^2+4af\log(f)-4Idf)/f}\operatorname{fresnel_cos}\left(\frac{1}{2}\sqrt{2}(2fx+Ib\log(f))\sqrt{\frac{f}{\pi}}/f\right)+i\sqrt{2}\pi\sqrt{\frac{f}{\pi}}e^{\frac{1}{4}(Ib^2\log(f)^2+4af\log(f)+4Idf)/f}\operatorname{fresnel_cos}\left(-\frac{1}{2}\sqrt{2}(2fx-Ib\log(f))\sqrt{\frac{f}{\pi}}/f\right)+\sqrt{2}\pi\sqrt{\frac{f}{\pi}}e^{\frac{1}{4}(-Ib^2\log(f)^2+4af\log(f)-4Idf)/f}\operatorname{fresnel_sin}\left(\frac{1}{2}\sqrt{2}(2fx+Ib\log(f))\sqrt{\frac{f}{\pi}}/f\right)-\sqrt{2}\pi\sqrt{\frac{f}{\pi}}e^{\frac{1}{4}(Ib^2\log(f)^2+4af\log(f)+4Idf)/f}\operatorname{fresnel_sin}\left(-\frac{1}{2}\sqrt{2}(2fx-Ib\log(f))\sqrt{\frac{f}{\pi}}/f\right)$

giac [B] time = 0.27, size = 300, normalized size = 2.11

$$i\sqrt{2}\sqrt{\pi}\operatorname{erf}\left(-\frac{1}{8}\sqrt{2}\left(4x-\frac{\pi b \operatorname{sgn}(f)-\pi b+2ib\log(|f|)}{f}\right)\left(-\frac{if}{|f|}+1\right)\sqrt{|f|}\right)e^{\left(\frac{i\pi^2 b^2 \operatorname{sgn}(f)}{8f}+\frac{\pi b^2 \log(|f|) \operatorname{sgn}(f)}{4f}-\frac{i\pi^2 b^2}{8f}-\frac{\pi b^2 \log(|f|)}{4f}+\frac{ib^2 \log(|f|)}{4f}\right)}4\left(-\frac{if}{|f|}+1\right)\sqrt{|f|}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(b*x+a)*sin(f*x^2+d),x, algorithm="giac")


```
[Out] 1/4*I*sqrt(2)*sqrt(pi)*erf(-1/8*sqrt(2)*(4*x - (pi*b*sgn(f) - pi*b + 2*I*b*log(abs(f))))/f)*(-I*f/abs(f) + 1)*sqrt(abs(f)))*e^(1/8*I*pi^2*b^2*sgn(f)/f + 1/4*pi*b^2*log(abs(f))*sgn(f)/f - 1/8*I*pi^2*b^2/f - 1/4*pi*b^2*log(abs(f)))/f + 1/4*I*b^2*log(abs(f))^2/f - 1/2*I*pi*a*sgn(f) + 1/2*I*pi*a + a*log(abs(f)) + I*d)/((-I*f/abs(f) + 1)*sqrt(abs(f))) - 1/4*I*sqrt(2)*sqrt(pi)*erf(-1/8*sqrt(2)*(4*x + (pi*b*sgn(f) - pi*b + 2*I*b*log(abs(f))))/f)*(I*f/abs(f) + 1)*sqrt(abs(f)))*e^(-1/8*I*pi^2*b^2*sgn(f)/f - 1/4*pi*b^2*log(abs(f))*sgn(f)/f + 1/8*I*pi^2*b^2/f + 1/4*pi*b^2*log(abs(f)))/f - 1/4*I*b^2*log(abs(f))^2/f - 1/2*I*pi*a*sgn(f) + 1/2*I*pi*a + a*log(abs(f)) - I*d)/((I*f/abs(f) + 1)*sqrt(abs(f)))
```

maple [A] time = 0.50, size = 116, normalized size = 0.82

$$\frac{i\sqrt{\pi} f^a e^{\frac{i(\ln(f)^2 b^2 + 4df)}{4f}} \operatorname{erf}\left(-\sqrt{-if} x + \frac{\ln(f)b}{2\sqrt{-if}}\right)}{4\sqrt{-if}} - \frac{i\sqrt{\pi} f^a e^{\frac{i(\ln(f)^2 b^2 + 4df)}{4f}} \operatorname{erf}\left(-\sqrt{if} x + \frac{\ln(f)b}{2\sqrt{if}}\right)}{4\sqrt{if}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(f^(b*x+a)*sin(f*x^2+d), x)
```

```
[Out] 1/4*I*Pi^(1/2)*f^a*exp(1/4*I*(ln(f)^2*b^2+4*d*f)/f)/(-I*f)^(1/2)*erf(-(-I*f)^(1/2)*x+1/2*ln(f)*b/(-I*f)^(1/2))-1/4*I*Pi^(1/2)*f^a*exp(-1/4*I*(ln(f)^2*b^2+4*d*f)/f)/(I*f)^(1/2)*erf(-(-I*f)^(1/2)*x+1/2*ln(f)*b/(I*f)^(1/2))
```

maxima [A] time = 0.34, size = 147, normalized size = 1.04

$$\frac{\sqrt{2}\sqrt{\pi}\left(\left(-i+1\right)f^a\cos\left(\frac{b^2\log(f)^2+4df}{4f}\right)+\left(i-1\right)f^a\sin\left(\frac{b^2\log(f)^2+4df}{4f}\right)\right)\operatorname{erf}\left(\frac{2ifx-b\log(f)}{2\sqrt{if}}\right)+\left(-i-1\right)f^a\cos\left(\frac{b^2\log(f)^2+4df}{4f}\right)}{8\sqrt{f}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(f^(b*x+a)*sin(f*x^2+d), x, algorithm="maxima")
```

```
[Out] -1/8*sqrt(2)*sqrt(pi)*((-I + 1)*f^a*cos(1/4*(b^2*log(f)^2 + 4*d*f)/f) + (I - 1)*f^a*sin(1/4*(b^2*log(f)^2 + 4*d*f)/f))*erf(1/2*(2*I*f*x - b*log(f))/sqrt(I*f)) + (-I - 1)*f^a*cos(1/4*(b^2*log(f)^2 + 4*d*f)/f) + (I + 1)*f^a*sin(1/4*(b^2*log(f)^2 + 4*d*f)/f))*erf(1/2*(2*I*f*x + b*log(f))/sqrt(-I*f))/sqrt(f)
```

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int f^{a+bx} \sin(fx^2 + d) dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(f^(a + b*x)*sin(d + f*x^2), x)
```

```
[Out] int(f^(a + b*x)*sin(d + f*x^2), x)
```

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int f^{a+bx} \sin(d + fx^2) dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(f**(b*x+a)*sin(f*x**2+d), x)
```

```
[Out] Integral(f**(a + b*x)*sin(d + f*x**2), x)
```

3.80 $\int f^{a+bx} \sin^2(d + fx^2) dx$

Optimal. Leaf size=157

$$\left(\frac{1}{16} + \frac{i}{16}\right) \sqrt{\pi} f^{a-\frac{1}{2}} e^{\frac{ib^2 \log^2(f)}{8f} + 2id} \operatorname{erf}\left(\frac{\left(\frac{1}{4} + \frac{i}{4}\right)(b \log(f) + 4ifx)}{\sqrt{f}}\right) + \left(\frac{1}{16} + \frac{i}{16}\right) \sqrt{\pi} f^{a-\frac{1}{2}} e^{-\frac{1}{8}i\left(\frac{b^2 \log^2(f)}{f} + 16d\right)} \operatorname{erfi}\left(\frac{\left(\frac{1}{4} + \frac{i}{4}\right)(b \log(f) + 4ifx)}{\sqrt{f}}\right)$$

[Out] 1/2*f^(b*x+a)/b/ln(f)+(1/16+1/16*I)*exp(2*I*d+1/8*I*b^2*ln(f)^2/f)*f^(-1/2+a)*erf((1/4+1/4*I)*(4*I*f*x+b*ln(f))/f^(1/2))*Pi^(1/2)+(1/16+1/16*I)*f^(-1/2+a)*erfi((1/4+1/4*I)*(4*I*f*x-b*ln(f))/f^(1/2))*Pi^(1/2)/exp(1/8*I*(16*d+b^2*ln(f)^2/f))

Rubi [A] time = 0.20, antiderivative size = 157, normalized size of antiderivative = 1.00, number of steps used = 9, number of rules used = 6, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.333$, Rules used = {4472, 2194, 2287, 2234, 2204, 2205}

$$\left(\frac{1}{16} + \frac{i}{16}\right) \sqrt{\pi} f^{a-\frac{1}{2}} e^{\frac{ib^2 \log^2(f)}{8f} + 2id} \operatorname{Erf}\left(\frac{\left(\frac{1}{4} + \frac{i}{4}\right)(b \log(f) + 4ifx)}{\sqrt{f}}\right) + \left(\frac{1}{16} + \frac{i}{16}\right) \sqrt{\pi} f^{a-\frac{1}{2}} e^{-\frac{1}{8}i\left(\frac{b^2 \log^2(f)}{f} + 16d\right)} \operatorname{Erfi}\left(\frac{\left(\frac{1}{4} + \frac{i}{4}\right)(b \log(f) + 4ifx)}{\sqrt{f}}\right)$$

Antiderivative was successfully verified.

[In] Int[f^(a + b*x)*Sin[d + f*x^2]^2,x]

[Out] (1/16 + I/16)*E^((2*I)*d + ((I/8)*b^2*Log[f]^2)/f)*f^(-1/2 + a)*Sqrt[Pi]*Erf[((1/4 + I/4)*((4*I)*f*x + b*Log[f]))/Sqrt[f]] + ((1/16 + I/16)*f^(-1/2 + a)*Sqrt[Pi]*Erfi[((1/4 + I/4)*((4*I)*f*x - b*Log[f]))/Sqrt[f]])/E^((I/8)*(16*d + (b^2*Log[f]^2)/f)) + f^(a + b*x)/(2*b*Log[f])

Rule 2194

Int[((F_)^((c_.)*((a_.) + (b_.)*(x_))))^(n_.), x_Symbol] := Simp[(F^(c*(a + b*x)))^n/(b*c*n*Log[F]), x] /; FreeQ[{F, a, b, c, n}, x]

Rule 2204

Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^2), x_Symbol] := Simp[(F^a*Sqrt[Pi]*Erfi[(c + d*x)*Rt[b*Log[F], 2]])/(2*d*Rt[b*Log[F], 2]), x] /; FreeQ[{F, a, b, c, d}, x] && PosQ[b]

Rule 2205

Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^2), x_Symbol] := Simp[(F^a*Sqrt[Pi]*Erf[(c + d*x)*Rt[-(b*Log[F]), 2]])/(2*d*Rt[-(b*Log[F]), 2]), x] /; FreeQ[{F, a, b, c, d}, x] && NegQ[b]

Rule 2234

Int[(F_)^((a_.) + (b_.)*(x_) + (c_.)*(x_)^2), x_Symbol] := Dist[F^(a - b^2/(4*c)), Int[F^((b + 2*c*x)^2/(4*c)), x], x] /; FreeQ[{F, a, b, c}, x]

Rule 2287

Int[(u_)*(F_)^(v_)*(G_)^(w_), x_Symbol] := With[{z = v*Log[F] + w*Log[G]}, Int[u*NormalizeIntegrand[E^z, x], x] /; BinomialQ[z, x] || (PolynomialQ[z, x] && LeQ[Exponent[z, x], 2])] /; FreeQ[{F, G}, x]

Rule 4472

`Int[(F_)^(u_)*Sin[v_]^(n_), x_Symbol] := Int[ExpandTrigToExp[F^u, Sin[v]^n, x], x] /; FreeQ[F, x] && (LinearQ[u, x] || PolyQ[u, x, 2]) && (LinearQ[v, x] || PolyQ[v, x, 2]) && IGtQ[n, 0]`

Rubi steps

$$\begin{aligned}
 \int f^{a+bx} \sin^2(d + fx^2) dx &= \int \left(\frac{1}{2} f^{a+bx} - \frac{1}{4} e^{-2id-2ifx^2} f^{a+bx} - \frac{1}{4} e^{2id+2ifx^2} f^{a+bx} \right) dx \\
 &= -\left(\frac{1}{4} \int e^{-2id-2ifx^2} f^{a+bx} dx \right) - \frac{1}{4} \int e^{2id+2ifx^2} f^{a+bx} dx + \frac{1}{2} \int f^{a+bx} dx \\
 &= \frac{f^{a+bx}}{2b \log(f)} - \frac{1}{4} \int e^{-2id-2ifx^2+a \log(f)+bx \log(f)} dx - \frac{1}{4} \int e^{2id+2ifx^2+a \log(f)+bx \log(f)} dx \\
 &= \frac{f^{a+bx}}{2b \log(f)} - \frac{1}{4} \left(e^{2id+\frac{ib^2 \log^2(f)}{8f}} f^a \right) \int e^{-\frac{i(4ifx+b \log(f))^2}{8f}} dx - \frac{1}{4} \left(e^{-\frac{1}{8}i \left(16d+\frac{b^2 \log^2(f)}{f} \right)} f^a \right) \int e^{\frac{i(4ifx+b \log(f))^2}{8f}} dx \\
 &= \left(\frac{1}{16} + \frac{i}{16} \right) e^{2id+\frac{ib^2 \log^2(f)}{8f}} f^{-\frac{1}{2}+a} \sqrt{\pi} \operatorname{erf} \left(\frac{\left(\frac{1}{4} + \frac{i}{4} \right) (4ifx + b \log(f))}{\sqrt{f}} \right) + \left(\frac{1}{16} + \frac{i}{16} \right) e^{-\frac{1}{8}i \left(16d+\frac{b^2 \log^2(f)}{f} \right)} f^a \sqrt{\pi} \operatorname{erfi} \left(\frac{\left(\frac{1}{4} + \frac{i}{4} \right) (4ifx + b \log(f))}{\sqrt{f}} \right)
 \end{aligned}$$

Mathematica [A] time = 1.04, size = 156, normalized size = 0.99

$$\frac{1}{16} f^a \left(\frac{(1-i)\sqrt{\pi} e^{-\frac{ib^2 \log^2(f)}{8f}} (\cos(d) - i \sin(d))^2 \operatorname{erf} \left(\frac{(4+4i)fx - (1-i)b \log(f)}{4\sqrt{f}} \right)}{\sqrt{f}} - \frac{(1-i)\sqrt{\pi} e^{\frac{ib^2 \log^2(f)}{8f}} (\cos(d) + i \sin(d))^2 \operatorname{erfi} \left(\frac{(4+4i)fx - (1-i)b \log(f)}{4\sqrt{f}} \right)}{\sqrt{f}} \right)$$

Antiderivative was successfully verified.

[In] Integrate[f^(a + b*x)*Sin[d + f*x^2]^2,x]

[Out] (f^a*((8*f^(b*x))/(b*Log[f]) - ((1 - I)*Sqrt[Pi]*Erf[((4 + 4*I)*f*x - (1 - I)*b*Log[f])/(4*Sqrt[f])])*(Cos[d] - I*Sin[d])^2)/(E^(((I/8)*b^2*Log[f]^2)/f)*Sqrt[f]) - ((1 - I)*E^(((I/8)*b^2*Log[f]^2)/f)*Sqrt[Pi]*Erfi[((4 + 4*I)*f*x + (1 - I)*b*Log[f])/(4*Sqrt[f])])*(Cos[d] + I*Sin[d])^2/Sqrt[f])/16

fricas [B] time = 1.25, size = 271, normalized size = 1.73

$$\frac{2\pi b \sqrt{\frac{f}{\pi}} e^{\left(\frac{-ib^2 \log(f)^2 + 8af \log(f) - 16idf}{8f} \right)} C \left(\frac{(4fx + ib \log(f)) \sqrt{\frac{f}{\pi}}}{2f} \right) \log(f) - 2\pi b \sqrt{\frac{f}{\pi}} e^{\left(\frac{ib^2 \log(f)^2 + 8af \log(f) + 16idf}{8f} \right)} C \left(-\frac{(4fx - ib \log(f)) \sqrt{\frac{f}{\pi}}}{2f} \right)}{16}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(b*x+a)*sin(f*x^2+d)^2,x, algorithm="fricas")

[Out] -1/16*(2*pi*b*sqrt(f/pi)*e^(1/8*(-I*b^2*log(f)^2 + 8*a*f*log(f) - 16*I*d*f)/f)*fresnel_cos(1/2*(4*f*x + I*b*log(f))*sqrt(f/pi)/f)*log(f) - 2*pi*b*sqrt(f/pi)*e^(1/8*(I*b^2*log(f)^2 + 8*a*f*log(f) + 16*I*d*f)/f)*fresnel_cos(-1/2*(4*f*x - I*b*log(f))*sqrt(f/pi)/f)*log(f) - 2*I*pi*b*sqrt(f/pi)*e^(1/8*(-I*b^2*log(f)^2 + 8*a*f*log(f) - 16*I*d*f)/f)*fresnel_sin(1/2*(4*f*x + I*b*log(f))*sqrt(f/pi)/f)*log(f) - 2*I*pi*b*sqrt(f/pi)*e^(1/8*(I*b^2*log(f)^2 + 8*a*f*log(f) + 16*I*d*f)/f)*fresnel_sin(-1/2*(4*f*x - I*b*log(f))*sqrt(f/pi)/f)*log(f) - 8*f*f^(b*x + a))/(b*f*log(f))

giac [B] time = 0.28, size = 521, normalized size = 3.32

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(b*x+a)*sin(f*x^2+d)^2,x, algorithm="giac")

[Out] (2*b*cos(-1/2*pi*b*x*sgn(f) + 1/2*pi*b*x - 1/2*pi*a*sgn(f) + 1/2*pi*a)*log(abs(f))/(4*b^2*log(abs(f))^2 + (pi*b*sgn(f) - pi*b)^2) - (pi*b*sgn(f) - pi*b)*sin(-1/2*pi*b*x*sgn(f) + 1/2*pi*b*x - 1/2*pi*a*sgn(f) + 1/2*pi*a)/(4*b^2*log(abs(f))^2 + (pi*b*sgn(f) - pi*b)^2))*e^(b*x*log(abs(f)) + a*log(abs(f))) - 1/2*I*(-2*I*e^(1/2*I*pi*b*x*sgn(f) - 1/2*I*pi*b*x + 1/2*I*pi*a*sgn(f) - 1/2*I*pi*a)/(2*I*pi*b*sgn(f) - 2*I*pi*b + 4*b*log(abs(f))) + 2*I*e^(-1/2*I*pi*b*x*sgn(f) + 1/2*I*pi*b*x - 1/2*I*pi*a*sgn(f) + 1/2*I*pi*a)/(-2*I*pi*b*sgn(f) + 2*I*pi*b + 4*b*log(abs(f))))*e^(b*x*log(abs(f)) + a*log(abs(f))) + 1/8*sqrt(pi)*erf(-1/8*sqrt(f)*(8*x - (pi*b*sgn(f) - pi*b + 2*I*b*log(abs(f))))/f)*(-I*f/abs(f) + 1))*e^(1/16*I*pi^2*b^2*sgn(f)/f + 1/8*pi*b^2*log(abs(f))*sgn(f)/f - 1/16*I*pi^2*b^2/f - 1/8*pi*b^2*log(abs(f))/f + 1/8*I*b^2*log(abs(f))^2/f - 1/2*I*pi*a*sgn(f) + 1/2*I*pi*a + a*log(abs(f)) + 2*I*d)/(sqrt(f)*(-I*f/abs(f) + 1)) + 1/8*sqrt(pi)*erf(-1/8*sqrt(f)*(8*x + (pi*b*sgn(f) - pi*b + 2*I*b*log(abs(f))))/f)*(I*f/abs(f) + 1))*e^(-1/16*I*pi^2*b^2*sgn(f)/f - 1/8*pi*b^2*log(abs(f))*sgn(f)/f + 1/16*I*pi^2*b^2/f + 1/8*pi*b^2*log(abs(f))/f - 1/8*I*b^2*log(abs(f))^2/f - 1/2*I*pi*a*sgn(f) + 1/2*I*pi*a + a*log(abs(f)) - 2*I*d)/(sqrt(f)*(I*f/abs(f) + 1))

maple [A] time = 0.67, size = 139, normalized size = 0.89

$$\frac{\sqrt{\pi} f^a e^{-\frac{i(\ln(f)^2 b^2 + 16df)}{8f}} \sqrt{2} \operatorname{erf}\left(-\sqrt{2} \sqrt{if} x + \frac{\ln(f)b\sqrt{2}}{4\sqrt{if}}\right)}{16\sqrt{if}} + \frac{\sqrt{\pi} f^a e^{\frac{i(\ln(f)^2 b^2 + 16df)}{8f}} \operatorname{erf}\left(-\sqrt{-2if} x + \frac{\ln(f)b}{2\sqrt{-2if}}\right)}{8\sqrt{-2if}} + \frac{f^{bx+a}}{2b \ln(f)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(f^(b*x+a)*sin(f*x^2+d)^2,x)

[Out] 1/16*Pi^(1/2)*f^a*exp(-1/8*I*(ln(f)^2*b^2+16*d*f)/f)*2^(1/2)/(I*f)^(1/2)*erf(-2^(1/2)*(I*f)^(1/2)*x+1/4*ln(f)*b*2^(1/2)/(I*f)^(1/2))+1/8*Pi^(1/2)*f^a*exp(1/8*I*(ln(f)^2*b^2+16*d*f)/f)/(-2*I*f)^(1/2)*erf(-(-2*I*f)^(1/2)*x+1/2*ln(f)*b/(-2*I*f)^(1/2))+1/2*f^(b*x+a)/b/ln(f)

maxima [A] time = 0.45, size = 186, normalized size = 1.18

$$\frac{4^{\frac{1}{4}} \sqrt{2} \sqrt{\pi} \left((i-1) b f^a \cos\left(\frac{b^2 \log(f)^2 + 16df}{8f}\right) \log(f) + (i+1) b f^a \log(f) \sin\left(\frac{b^2 \log(f)^2 + 16df}{8f}\right) \right) \operatorname{erf}\left(\frac{4i f x - b \log(f)}{2 \sqrt{2if}}\right) + \left((i-1) b f^a \cos\left(\frac{b^2 \log(f)^2 + 16df}{8f}\right) \log(f) + (i+1) b f^a \log(f) \sin\left(\frac{b^2 \log(f)^2 + 16df}{8f}\right) \right) \operatorname{erf}\left(\frac{4i f x - b \log(f)}{2 \sqrt{2if}}\right)}{32 b f^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(b*x+a)*sin(f*x^2+d)^2,x, algorithm="maxima")

[Out] 1/32*(4^(1/4)*sqrt(2)*sqrt(pi)*(((I - 1)*b*f^a*cos(1/8*(b^2*log(f)^2 + 16*d*f)/f)*log(f) + (I + 1)*b*f^a*cos(1/8*(b^2*log(f)^2 + 16*d*f)/f))*erf(1/2*(4*I*f*x - b*log(f))/sqrt(2*I*f)) + (((I + 1)*b*f^a*cos(1/8*(b^2*log(f)^2 + 16*d*f)/f)*log(f) + (I - 1)*b*f^a*cos(1/8*(b^2*log(f)^2 + 16*d*f)/f))*erf(1/2*(4*I*f*x + b*log(f))/sqrt(-2*I*f)))*f^(3/2) + 16*f^(b*x)*f^(a + 2))/(b*f^2*log(f))

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int f^{a+bx} \sin(fx^2 + d)^2 dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(f^(a + b*x)*sin(d + f*x^2)^2,x)
```

```
[Out] int(f^(a + b*x)*sin(d + f*x^2)^2, x)
```

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int f^{a+bx} \sin^2(d + fx^2) dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(f**(b*x+a)*sin(f*x**2+d)**2,x)
```

```
[Out] Integral(f**(a + b*x)*sin(d + f*x**2)**2, x)
```

3.81 $\int f^{a+bx} \sin^3(d + fx^2) dx$

Optimal. Leaf size=298

$$\frac{3}{16}(-1)^{3/4}\sqrt{\pi}f^{a-\frac{1}{2}}e^{\frac{1}{4}i\left(\frac{b^2\log^2(f)}{f}+4d\right)}\operatorname{erf}\left(\frac{\sqrt[4]{-1}(b\log(f)+2ifx)}{2\sqrt{f}}\right)+\left(\frac{1}{16}-\frac{i}{16}\right)\sqrt{\frac{\pi}{6}}f^{a-\frac{1}{2}}e^{\frac{ib^2\log^2(f)}{12f}+3id}\operatorname{erf}\left(\frac{\left(\frac{1}{2}+\frac{i}{2}\right)(b\log(f)+2ifx)}{\sqrt{6}}\right)$$

[Out] (1/96-1/96*I)*exp(3*I*d+1/12*I*b^2*ln(f)^2/f)*f^(-1/2+a)*erf((1/12+1/12*I)*(6*I*f*x+b*ln(f))*6^(1/2)/f^(1/2))*6^(1/2)*Pi^(1/2)+(-1/96+1/96*I)*f^(-1/2+a)*erfi((1/12+1/12*I)*(6*I*f*x-b*ln(f))*6^(1/2)/f^(1/2))*6^(1/2)*Pi^(1/2)/exp(1/12*I*(36*d+b^2*ln(f)^2/f))+3/16*(-1)^(3/4)*exp(1/4*I*(4*d+b^2*ln(f)^2/f))*f^(-1/2+a)*erf(1/2*(-1)^(1/4)*(2*I*f*x+b*ln(f))/f^(1/2))*Pi^(1/2)-3/16*(-1)^(3/4)*f^(-1/2+a)*erfi(1/2*(-1)^(1/4)*(2*I*f*x-b*ln(f))/f^(1/2))*Pi^(1/2)/exp(1/4*I*(4*d+b^2*ln(f)^2/f))

Rubi [A] time = 0.37, antiderivative size = 298, normalized size of antiderivative = 1.00, number of steps used = 14, number of rules used = 5, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.278$, Rules used = {4472, 2287, 2234, 2204, 2205}

$$\frac{3}{16}(-1)^{3/4}\sqrt{\pi}f^{a-\frac{1}{2}}e^{\frac{1}{4}i\left(\frac{b^2\log^2(f)}{f}+4d\right)}\operatorname{Erf}\left(\frac{\sqrt[4]{-1}(b\log(f)+2ifx)}{2\sqrt{f}}\right)+\left(\frac{1}{16}-\frac{i}{16}\right)\sqrt{\frac{\pi}{6}}f^{a-\frac{1}{2}}e^{\frac{ib^2\log^2(f)}{12f}+3id}\operatorname{Erf}\left(\frac{\left(\frac{1}{2}+\frac{i}{2}\right)(b\log(f)+2ifx)}{\sqrt{6}}\right)$$

Antiderivative was successfully verified.

[In] Int[f^(a + b*x)*Sin[d + f*x^2]^3,x]

[Out] (3*(-1)^(3/4)*E^((I/4)*(4*d + (b^2*Log[f]^2)/f))*f^(-1/2 + a)*Sqrt[Pi]*Erf[(-1)^(1/4)*((2*I)*f*x + b*Log[f])/(2*Sqrt[f])]/16 + (1/16 - I/16)*E^((3*I)*d + ((I/12)*b^2*Log[f]^2)/f)*f^(-1/2 + a)*Sqrt[Pi/6]*Erf[((1/2 + I/2)*((6*I)*f*x + b*Log[f]))/(Sqrt[6]*Sqrt[f])] - (3*(-1)^(3/4)*f^(-1/2 + a)*Sqrt[Pi]*Erfi[(-1)^(1/4)*((2*I)*f*x - b*Log[f])/(2*Sqrt[f])]/(16*E^((I/4)*(4*d + (b^2*Log[f]^2)/f))) - ((1/16 - I/16)*f^(-1/2 + a)*Sqrt[Pi/6]*Erfi[((1/2 + I/2)*((6*I)*f*x - b*Log[f]))/(Sqrt[6]*Sqrt[f])])/E^((I/12)*(36*d + (b^2*Log[f]^2)/f))

Rule 2204

Int[(F_)^((a_) + (b_)*((c_) + (d_)*(x_)^2), x_Symbol] := Simp[(F^a*Sqrt[Pi]*Erfi[(c + d*x)*Rt[b*Log[F], 2]]/(2*d*Rt[b*Log[F], 2]), x] /; FreeQ[{F, a, b, c, d}, x] && PosQ[b]

Rule 2205

Int[(F_)^((a_) + (b_)*((c_) + (d_)*(x_)^2), x_Symbol] := Simp[(F^a*Sqrt[Pi]*Erf[(c + d*x)*Rt[-(b*Log[F]), 2]]/(2*d*Rt[-(b*Log[F]), 2]), x] /; FreeQ[{F, a, b, c, d}, x] && NegQ[b]

Rule 2234

Int[(F_)^((a_) + (b_)*(x_) + (c_)*(x_)^2), x_Symbol] := Dist[F^(a - b^2/(4*c)), Int[F^((b + 2*c*x)^2/(4*c)), x], x] /; FreeQ[{F, a, b, c}, x]

Rule 2287

Int[(u_)*(F_)^(v_)*(G_)^(w_), x_Symbol] := With[{z = v*Log[F] + w*Log[G]}, Int[u*NormalizeIntegrand[E^z, x], x] /; BinomialQ[z, x] || (PolynomialQ[z, x] && LeQ[Exponent[z, x], 2]) /; FreeQ[{F, G}, x]

Rule 4472

$\text{Int}[(F_)^{(u_)} \sin[v_]^{(n_)}, x_Symbol] \rightarrow \text{Int}[\text{ExpandTrigToExp}[F^u, \sin[v]^{n}], x], x] /;$ FreeQ[F, x] && (LinearQ[u, x] || PolyQ[u, x, 2]) && (LinearQ[v, x] || PolyQ[v, x, 2]) && IGtQ[n, 0]

Rubi steps

$$\begin{aligned} \int f^{a+bx} \sin^3(d+fx^2) dx &= \int \left(\frac{3}{8} i e^{-id-ifx^2} f^{a+bx} - \frac{3}{8} i e^{id+ifx^2} f^{a+bx} - \frac{1}{8} i e^{-3id-3ifx^2} f^{a+bx} + \frac{1}{8} i e^{3id+3ifx^2} f^{a+bx} \right) dx \\ &= -\left(\frac{1}{8} i \int e^{-3id-3ifx^2} f^{a+bx} dx \right) + \frac{1}{8} i \int e^{3id+3ifx^2} f^{a+bx} dx + \frac{3}{8} i \int e^{-id-ifx^2} f^{a+bx} dx - \\ &= -\left(\frac{1}{8} i \int e^{-3id-3ifx^2+a \log(f)+bx \log(f)} dx \right) + \frac{1}{8} i \int e^{3id+3ifx^2+a \log(f)+bx \log(f)} dx + \frac{3}{8} i \int e^{-id-ifx^2+a \log(f)+bx \log(f)} dx - \\ &= \frac{1}{8} \left(i e^{3id+\frac{ib^2 \log^2(f)}{12f}} f^a \right) \int e^{-\frac{i(6fx+b \log(f))^2}{12f}} dx + \frac{1}{8} \left(3 i e^{-\frac{1}{4} \left(4d+\frac{b^2 \log^2(f)}{f} \right)} f^a \right) \int e^{\frac{i(-2fx+b \log(f))}{4f}} dx \\ &= \frac{3}{16} (-1)^{3/4} e^{\frac{1}{4} \left(4d+\frac{b^2 \log^2(f)}{f} \right)} f^{-\frac{1}{2}+a} \sqrt{\pi} \operatorname{erf} \left(\frac{\sqrt[4]{-1} (2fx+b \log(f))}{2\sqrt{f}} \right) + \left(\frac{1}{16} - \frac{i}{16} \right) e^{3id+a} \end{aligned}$$

Mathematica [A] time = 0.81, size = 268, normalized size = 0.90

$$\frac{1}{48} (-1)^{3/4} \sqrt{\pi} f^{a-\frac{1}{2}} e^{-\frac{ib^2 \log^2(f)}{4f}} \left(9 i e^{\frac{ib^2 \log^2(f)}{2f}} (\cos(d) + i \sin(d)) \operatorname{erfi} \left(\frac{\sqrt[4]{-1} (2fx - ib \log(f))}{2\sqrt{f}} \right) + \sqrt{3} e^{\frac{ib^2 \log^2(f)}{6f}} \left(e^{\frac{ib^2 \log^2(f)}{6f}} \right) \right)$$

Antiderivative was successfully verified.

[In] Integrate[f^(a + b*x)*Sin[d + f*x^2]^3,x]

[Out] $((-1)^{(3/4)} * f^{(-1/2 + a)} * \text{Sqrt}[\text{Pi}] * (-9 * \text{Erfi}[\frac{((-1)^{(3/4)} * (2 * f * x + I * b * \text{Log}[f]))}{2 * \text{Sqrt}[f]}]) * (\text{Cos}[d] - I * \text{Sin}[d]) + (9 * I) * \text{E}^{\frac{((I/2) * b^2 * \text{Log}[f]^2)/f}} * \text{Erfi}[\frac{((-1)^{(1/4)} * (2 * f * x - I * b * \text{Log}[f]))}{2 * \text{Sqrt}[f]}]) * (\text{Cos}[d] + I * \text{Sin}[d]) + \text{Sqrt}[3] * \text{E}^{\frac{((I/6) * b^2 * \text{Log}[f]^2)/f}} * (\text{Erfi}[\frac{((-1)^{(3/4)} * (6 * f * x + I * b * \text{Log}[f]))}{2 * \text{Sqrt}[3] * \text{Sqrt}[f]}]) * (\text{Cos}[3 * d] - I * \text{Sin}[3 * d]) + \text{E}^{\frac{((I/6) * b^2 * \text{Log}[f]^2)/f}} * \text{Erfi}[\frac{((6 + 6 * I) * f * x + (1 - I) * b * \text{Log}[f])}{2 * \text{Sqrt}[6] * \text{Sqrt}[f]}]) * ((-I) * \text{Cos}[3 * d] + \text{Sin}[3 * d])}))/ (48 * \text{E}^{\frac{((I/4) * b^2 * \text{Log}[f]^2)/f}})$

fricas [B] time = 0.72, size = 525, normalized size = 1.76

$$-i \sqrt{6} \pi \sqrt{\frac{f}{\pi}} e^{\left(\frac{-ib^2 \log(f)^2 + 12af \log(f) - 36idf}{12f} \right)} C \left(\frac{\sqrt{6} (6fx + ib \log(f)) \sqrt{\frac{f}{\pi}}}{6f} \right) - i \sqrt{6} \pi \sqrt{\frac{f}{\pi}} e^{\left(\frac{ib^2 \log(f)^2 + 12af \log(f) + 36idf}{12f} \right)} C \left(-\frac{\sqrt{6} (6fx - ib \log(f)) \sqrt{\frac{f}{\pi}}}{6f} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(b*x+a)*sin(f*x^2+d)^3,x, algorithm="fricas")

[Out] $\frac{1}{48} * (-I * \text{sqrt}(6) * \text{pi} * \text{sqrt}(f/\text{pi}) * e^{\frac{1}{12} * (-I * b^2 * \log(f)^2 + 12 * a * f * \log(f) - 36 * I * d * f)/f}} * \text{fresnel_cos}(1/6 * \text{sqrt}(6) * (6 * f * x + I * b * \log(f)) * \text{sqrt}(f/\text{pi})/f) - I * \text{sqrt}(6) * \text{pi} * \text{sqrt}(f/\text{pi}) * e^{\frac{1}{12} * (I * b^2 * \log(f)^2 + 12 * a * f * \log(f) + 36 * I * d * f)/f}} * \text{fresnel_cos}(-1/6 * \text{sqrt}(6) * (6 * f * x - I * b * \log(f)) * \text{sqrt}(f/\text{pi})/f) + 9 * I * \text{sqrt}(2) * \text{pi} * \text{sqrt}(f/\text{pi}) * e^{\frac{1}{4} * (-I * b^2 * \log(f)^2 + 4 * a * f * \log(f) - 4 * I * d * f)/f}} * \text{fresnel_cos}(1/2 * \text{sqrt}(2) * (2 * f * x + I * b * \log(f)) * \text{sqrt}(f/\text{pi})/f) + 9 * I * \text{sqrt}(2) * \text{pi} * \text{sqrt}(f/\text{pi}) * e^{\frac{1}{4} * (I * b^2 * \log(f)^2 + 4 * a * f * \log(f) + 4 * I * d * f)/f}} * \text{fresnel_cos}(-1/2 * \text{sqrt}(2) * (2 * f * x - I * b * \log(f)) * \text{sqrt}(f/\text{pi})/f)$

```

qrt(2)*(2*f*x - I*b*log(f))*sqrt(f/pi)/f) - sqrt(6)*pi*sqrt(f/pi)*e^(1/12*(
-I*b^2*log(f)^2 + 12*a*f*log(f) - 36*I*d*f)/f)*fresnel_sin(1/6*sqrt(6)*(6*f
*x + I*b*log(f))*sqrt(f/pi)/f) + sqrt(6)*pi*sqrt(f/pi)*e^(1/12*(I*b^2*log(f)
)^2 + 12*a*f*log(f) + 36*I*d*f)/f)*fresnel_sin(-1/6*sqrt(6)*(6*f*x - I*b*lo
g(f))*sqrt(f/pi)/f) + 9*sqrt(2)*pi*sqrt(f/pi)*e^(1/4*(-I*b^2*log(f)^2 + 4*a
*f*log(f) - 4*I*d*f)/f)*fresnel_sin(1/2*sqrt(2)*(2*f*x + I*b*log(f))*sqrt(f
/pi)/f) - 9*sqrt(2)*pi*sqrt(f/pi)*e^(1/4*(I*b^2*log(f)^2 + 4*a*f*log(f) + 4
*I*d*f)/f)*fresnel_sin(-1/2*sqrt(2)*(2*f*x - I*b*log(f))*sqrt(f/pi)/f))/f

```

giac [B] time = 0.40, size = 595, normalized size = 2.00

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(b*x+a)*sin(f*x^2+d)^3,x, algorithm="giac")

```

[Out] 3/16*I*sqrt(2)*sqrt(pi)*erf(-1/8*sqrt(2)*(4*x - (pi*b*sgn(f) - pi*b + 2*I*b
*log(abs(f)))/f)*(-I*f/abs(f) + 1)*sqrt(abs(f)))*e^(1/8*I*pi^2*b^2*sgn(f)/f
+ 1/4*pi*b^2*log(abs(f))*sgn(f)/f - 1/8*I*pi^2*b^2/f - 1/4*pi*b^2*log(abs(
f))/f + 1/4*I*b^2*log(abs(f))^2/f - 1/2*I*pi*a*sgn(f) + 1/2*I*pi*a + a*log(
abs(f)) + I*d)/((-I*f/abs(f) + 1)*sqrt(abs(f))) - 1/48*I*sqrt(6)*sqrt(pi)*e
rf(-1/24*sqrt(6)*sqrt(f)*(12*x - (pi*b*sgn(f) - pi*b + 2*I*b*log(abs(f)))/f
)*(-I*f/abs(f) + 1))*e^(1/24*I*pi^2*b^2*sgn(f)/f + 1/12*pi*b^2*log(abs(f))*
sgn(f)/f - 1/24*I*pi^2*b^2/f - 1/12*pi*b^2*log(abs(f))/f + 1/12*I*b^2*log(a
bs(f))^2/f - 1/2*I*pi*a*sgn(f) + 1/2*I*pi*a + a*log(abs(f)) + 3*I*d)/(sqrt(
f)*(-I*f/abs(f) + 1)) + 1/48*I*sqrt(6)*sqrt(pi)*erf(-1/24*sqrt(6)*sqrt(f)*(
12*x + (pi*b*sgn(f) - pi*b + 2*I*b*log(abs(f)))/f)*(I*f/abs(f) + 1))*e^(-1/
24*I*pi^2*b^2*sgn(f)/f - 1/12*pi*b^2*log(abs(f))*sgn(f)/f + 1/24*I*pi^2*b^2
/f + 1/12*pi*b^2*log(abs(f))/f - 1/12*I*b^2*log(abs(f))^2/f - 1/2*I*pi*a*sg
n(f) + 1/2*I*pi*a + a*log(abs(f)) - 3*I*d)/(sqrt(f)*(I*f/abs(f) + 1)) - 3/1
6*I*sqrt(2)*sqrt(pi)*erf(-1/8*sqrt(2)*(4*x + (pi*b*sgn(f) - pi*b + 2*I*b*lo
g(abs(f)))/f)*(I*f/abs(f) + 1)*sqrt(abs(f)))*e^(-1/8*I*pi^2*b^2*sgn(f)/f -
1/4*pi*b^2*log(abs(f))*sgn(f)/f + 1/8*I*pi^2*b^2/f + 1/4*pi*b^2*log(abs(f)
)/f - 1/4*I*b^2*log(abs(f))^2/f - 1/2*I*pi*a*sgn(f) + 1/2*I*pi*a + a*log(abs
(f)) - I*d)/((I*f/abs(f) + 1)*sqrt(abs(f)))

```

maple [A] time = 1.00, size = 239, normalized size = 0.80

$$\frac{i\sqrt{\pi} f^a e^{\frac{i(\ln(f)^2 b^2 + 36df)}{12f}} \operatorname{erf}\left(-\sqrt{-3if} x + \frac{\ln(f)b}{2\sqrt{-3if}}\right) + i\sqrt{\pi} f^a e^{-\frac{i(\ln(f)^2 b^2 + 36df)}{12f}} \sqrt{3} \operatorname{erf}\left(-\sqrt{3} \sqrt{if} x + \frac{\ln(f)b\sqrt{3}}{6\sqrt{if}}\right) - 3i\sqrt{\pi} f^a}{16\sqrt{-3if}} + \frac{3i\sqrt{\pi} f^a e^{\frac{i(\ln(f)^2 b^2 + 36df)}{12f}} \sqrt{3} \operatorname{erf}\left(-\sqrt{3} \sqrt{if} x + \frac{\ln(f)b\sqrt{3}}{6\sqrt{if}}\right) - 3i\sqrt{\pi} f^a}{48\sqrt{if}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(f^(b*x+a)*sin(f*x^2+d)^3,x)

```

[Out] -1/16*I*Pi^(1/2)*f^a*exp(1/12*I*(ln(f)^2*b^2+36*d*f)/f)/(-3*I*f)^(1/2)*erf(
-(-3*I*f)^(1/2)*x+1/2*ln(f)*b/(-3*I*f)^(1/2))+1/48*I*Pi^(1/2)*f^a*exp(-1/12
*I*(ln(f)^2*b^2+36*d*f)/f)*3^(1/2)/(I*f)^(1/2)*erf(-3^(1/2)*(I*f)^(1/2)*x+1
/6*ln(f)*b*3^(1/2)/(I*f)^(1/2))-3/16*I*Pi^(1/2)*f^a*exp(-1/4*I*(ln(f)^2*b^2
+4*d*f)/f)/(I*f)^(1/2)*erf(-(I*f)^(1/2)*x+1/2*ln(f)*b/(I*f)^(1/2))+3/16*I*P
i^(1/2)*f^a*exp(1/4*I*(ln(f)^2*b^2+4*d*f)/f)/(-I*f)^(1/2)*erf(-(-I*f)^(1/2)
*x+1/2*ln(f)*b/(-I*f)^(1/2))

```

maxima [A] time = 0.46, size = 302, normalized size = 1.01

$$3 \cdot 9^{\frac{1}{4}} \sqrt{2} \sqrt{\pi} \left(\left(-(i+1) f^a \cos\left(\frac{b^2 \log(f)^2 + 36df}{12f}\right) + (i-1) f^a \sin\left(\frac{b^2 \log(f)^2 + 36df}{12f}\right) \right) \operatorname{erf}\left(\frac{6ifx - b \log(f)}{2\sqrt{3if}}\right) + \left(-(i-1) f^a \cos\left(\frac{b^2 \log(f)^2 + 36df}{12f}\right) + (i+1) f^a \sin\left(\frac{b^2 \log(f)^2 + 36df}{12f}\right) \right) \operatorname{erf}\left(\frac{6ifx - b \log(f)}{2\sqrt{3if}}\right) \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(b*x+a)*sin(f*x^2+d)^3,x, algorithm="maxima")

[Out] $\frac{1}{288} \cdot (3 \cdot 9^{1/4}) \cdot \sqrt{2} \cdot \sqrt{\pi} \cdot \left((-I + 1) \cdot f^a \cdot \cos\left(\frac{1}{12} \cdot (b^2 \cdot \log(f)^2 + 36 \cdot d \cdot f) / f\right) + (I - 1) \cdot f^a \cdot \sin\left(\frac{1}{12} \cdot (b^2 \cdot \log(f)^2 + 36 \cdot d \cdot f) / f\right) \right) \cdot \operatorname{erf}\left(\frac{1}{2} \cdot (6 \cdot I \cdot f \cdot x - b \cdot \log(f)) / \sqrt{3 \cdot I \cdot f}\right) + (-I - 1) \cdot f^a \cdot \cos\left(\frac{1}{12} \cdot (b^2 \cdot \log(f)^2 + 36 \cdot d \cdot f) / f\right) + (I + 1) \cdot f^a \cdot \sin\left(\frac{1}{12} \cdot (b^2 \cdot \log(f)^2 + 36 \cdot d \cdot f) / f\right) \right) \cdot \operatorname{erf}\left(\frac{1}{2} \cdot (6 \cdot I \cdot f \cdot x + b \cdot \log(f)) / \sqrt{-3 \cdot I \cdot f}\right) \cdot f^{3/2} + \sqrt{2} \cdot \sqrt{\pi} \cdot \left((27 \cdot I + 27) \cdot f^a \cdot \cos\left(\frac{1}{4} \cdot (b^2 \cdot \log(f)^2 + 4 \cdot d \cdot f) / f\right) - (27 \cdot I - 27) \cdot f^a \cdot \sin\left(\frac{1}{4} \cdot (b^2 \cdot \log(f)^2 + 4 \cdot d \cdot f) / f\right) \right) \cdot \operatorname{erf}\left(\frac{1}{2} \cdot (2 \cdot I \cdot f \cdot x - b \cdot \log(f)) / \sqrt{I \cdot f}\right) + \left((27 \cdot I - 27) \cdot f^a \cdot \cos\left(\frac{1}{4} \cdot (b^2 \cdot \log(f)^2 + 4 \cdot d \cdot f) / f\right) - (27 \cdot I + 27) \cdot f^a \cdot \sin\left(\frac{1}{4} \cdot (b^2 \cdot \log(f)^2 + 4 \cdot d \cdot f) / f\right) \right) \cdot \operatorname{erf}\left(\frac{1}{2} \cdot (2 \cdot I \cdot f \cdot x + b \cdot \log(f)) / \sqrt{-I \cdot f}\right) \cdot f^{3/2} \right) / f^2$

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int f^{a+bx} \sin(fx^2 + d)^3 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(f^(a + b*x)*sin(d + f*x^2)^3,x)

[Out] int(f^(a + b*x)*sin(d + f*x^2)^3, x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int f^{a+bx} \sin^3(d + fx^2) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f**(b*x+a)*sin(f*x**2+d)**3,x)

[Out] Integral(f**(a + b*x)*sin(d + f*x**2)**3, x)

3.82 $\int f^{a+bx} \sin(d + ex + fx^2) dx$

Optimal. Leaf size=162

$$\frac{1}{4}(-1)^{3/4}\sqrt{\pi}f^{a-\frac{1}{2}}e^{\frac{1}{4}i\left(4d+\frac{(b\log(f)+ie)^2}{f}\right)}\operatorname{erf}\left(\frac{\sqrt[4]{-1}(b\log(f)+ie+2ifx)}{2\sqrt{f}}\right)-\frac{1}{4}(-1)^{3/4}\sqrt{\pi}f^{a-\frac{1}{2}}e^{\frac{i(e+ib\log(f))^2}{4f}-id}\operatorname{erfi}\left(\frac{\sqrt[4]{-1}(-b\log(f)+ie+2ifx)}{2\sqrt{f}}\right)$$

[Out] $\frac{1}{4}(-1)^{3/4}\exp\left(\frac{1}{4}i(4d+(Ie+b\ln(f))^2/f)\right)f^{-1/2+a}\operatorname{erf}\left(\frac{1}{2}(-1)^{1/4}(Ie+2Ifx+b\ln(f))/f^{1/2}\right)\pi^{1/2}-\frac{1}{4}(-1)^{3/4}\exp(-Id+1/4I(e+Ib\ln(f))^2/f)f^{-1/2+a}\operatorname{erfi}\left(\frac{1}{2}(-1)^{1/4}(Ie+2Ifx-b\ln(f))/f^{1/2}\right)\pi^{1/2}$

Rubi [A] time = 0.33, antiderivative size = 162, normalized size of antiderivative = 1.00, number of steps used = 8, number of rules used = 5, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.263$, Rules used = {4472, 2287, 2234, 2204, 2205}

$$\frac{1}{4}(-1)^{3/4}\sqrt{\pi}f^{a-\frac{1}{2}}e^{\frac{1}{4}i\left(4d+\frac{(b\log(f)+ie)^2}{f}\right)}\operatorname{Erf}\left(\frac{\sqrt[4]{-1}(b\log(f)+ie+2ifx)}{2\sqrt{f}}\right)-\frac{1}{4}(-1)^{3/4}\sqrt{\pi}f^{a-\frac{1}{2}}e^{\frac{i(e+ib\log(f))^2}{4f}-id}\operatorname{Erfi}\left(\frac{\sqrt[4]{-1}(-b\log(f)+ie+2ifx)}{2\sqrt{f}}\right)$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[f^{(a + b*x)}*\operatorname{Sin}[d + e*x + f*x^2], x]$

[Out] $((-1)^{3/4}*E^{((I/4)*(4*d + (I*e + b*Log[f])^2/f))*f^{-1/2 + a}*Sqrt[\pi]*Erf[((-1)^{1/4}*(I*e + (2*I)*f*x + b*Log[f]))/(2*Sqrt[f])])/4 - ((-1)^{3/4}*E^{((-I)*d + ((I/4)*(e + I*b*Log[f])^2)/f))*f^{-1/2 + a}*Sqrt[\pi]*Erfi[((-1)^{1/4}*(I*e + (2*I)*f*x - b*Log[f]))/(2*Sqrt[f])])/4$

Rule 2204

$\operatorname{Int}[(F_)^{((a_.) + (b_.)*((c_.) + (d_.)*(x_.))^2)}, x_Symbol] \rightarrow \operatorname{Simp}[(F^a*\operatorname{Sqrt}[\pi]*\operatorname{Erfi}[(c + d*x)*\operatorname{Rt}[b*\operatorname{Log}[F], 2]])/(2*d*\operatorname{Rt}[b*\operatorname{Log}[F], 2]), x] /; \operatorname{FreeQ}\{F, a, b, c, d\}, x] \&\& \operatorname{PosQ}[b]$

Rule 2205

$\operatorname{Int}[(F_)^{((a_.) + (b_.)*((c_.) + (d_.)*(x_.))^2)}, x_Symbol] \rightarrow \operatorname{Simp}[(F^a*\operatorname{Sqrt}[\pi]*\operatorname{Erf}[(c + d*x)*\operatorname{Rt}[-(b*\operatorname{Log}[F]), 2]])/(2*d*\operatorname{Rt}[-(b*\operatorname{Log}[F]), 2]), x] /; \operatorname{FreeQ}\{F, a, b, c, d\}, x] \&\& \operatorname{NegQ}[b]$

Rule 2234

$\operatorname{Int}[(F_)^{((a_.) + (b_.)*(x_.) + (c_.)*(x_.)^2)}, x_Symbol] \rightarrow \operatorname{Dist}[F^{(a - b^2/(4*c))}, \operatorname{Int}[F^{((b + 2*c*x)^2/(4*c))}, x], x] /; \operatorname{FreeQ}\{F, a, b, c\}, x]$

Rule 2287

$\operatorname{Int}[(u_)*(F_)^{(v_)}*(G_)^{(w_)}], x_Symbol] \rightarrow \operatorname{With}[\{z = v*\operatorname{Log}[F] + w*\operatorname{Log}[G]\}, \operatorname{Int}[u*\operatorname{NormalizeIntegrand}[E^z, x], x] /; \operatorname{BinomialQ}[z, x] \mid\mid (\operatorname{PolynomialQ}[z, x] \&\& \operatorname{LeQ}[\operatorname{Exponent}[z, x], 2])] /; \operatorname{FreeQ}\{F, G\}, x]$

Rule 4472

$\operatorname{Int}[(F_)^{(u_)}*\operatorname{Sin}[v_]^{(n_)}], x_Symbol] \rightarrow \operatorname{Int}[\operatorname{ExpandTrigToExp}[F^u, \operatorname{Sin}[v]^n], x] /; \operatorname{FreeQ}[F, x] \&\& (\operatorname{LinearQ}[u, x] \mid\mid \operatorname{PolyQ}[u, x, 2]) \&\& (\operatorname{LinearQ}[v, x] \mid\mid \operatorname{PolyQ}[v, x, 2]) \&\& \operatorname{IGtQ}[n, 0]$

Rubi steps

$$\begin{aligned}
\int f^{a+bx} \sin(d+ex+fx^2) dx &= \int \left(\frac{1}{2} i e^{-id-idx-ifx^2} f^{a+bx} - \frac{1}{2} i e^{id+idx+ifx^2} f^{a+bx} \right) dx \\
&= \frac{1}{2} i \int e^{-id-idx-ifx^2} f^{a+bx} dx - \frac{1}{2} i \int e^{id+idx+ifx^2} f^{a+bx} dx \\
&= \frac{1}{2} i \int \exp(-id-idx-ifx^2+a \log(f)-x(ie-b \log(f))) dx - \frac{1}{2} i \int \exp(id+idx+ifx^2+a \log(f)+x(ie-b \log(f))) dx \\
&= \frac{1}{2} \left(i e^{-id+\frac{i(e+ib \log(f))^2}{4f}} f^a \right) \int e^{\frac{i(-ie-2ifx+b \log(f))^2}{4f}} dx - \frac{1}{2} \left(i e^{\frac{1}{4} i \left(4d+\frac{(ie+b \log(f))^2}{f} \right)} f^a \right) \int e^{-\frac{i(-ie-2ifx+b \log(f))^2}{4f}} dx \\
&= \frac{1}{4} (-1)^{3/4} e^{\frac{1}{4} i \left(4d+\frac{(ie+b \log(f))^2}{f} \right)} f^{-\frac{1}{2}+a} \sqrt{\pi} \operatorname{erf} \left(\frac{\sqrt[4]{-1} (ie+2ifx+b \log(f))}{2\sqrt{f}} \right) - \frac{1}{4} (-1)^{1/4} e^{-\frac{1}{4} i \left(4d+\frac{(ie+b \log(f))^2}{f} \right)} f^{-\frac{1}{2}+a} \sqrt{\pi} \operatorname{erf} \left(\frac{\sqrt[4]{-1} (-ie+2ifx+b \log(f))}{2\sqrt{f}} \right)
\end{aligned}$$

Mathematica [A] time = 0.38, size = 162, normalized size = 1.00

$$-\frac{1}{4} \sqrt[4]{-1} \sqrt{\pi} f^{a-\frac{be+f}{2f}} e^{-\frac{i(b^2 \log^2(f)+e^2)}{4f}} \left(e^{\frac{ib^2 \log^2(f)}{2f}} (\cos(d) + i \sin(d)) \operatorname{erfi} \left(\frac{\sqrt[4]{-1} (-ib \log(f) + e + 2fx)}{2\sqrt{f}} \right) + e^{\frac{ie^2}{2f}} (\sin(d) + i \cos(d)) \operatorname{erfi} \left(\frac{\sqrt[4]{-1} (ib \log(f) - e - 2fx)}{2\sqrt{f}} \right) \right)$$

Antiderivative was successfully verified.

[In] Integrate[f^(a + b*x)*Sin[d + e*x + f*x^2], x]

[Out] -1/4*((-1)^(1/4))*f^(a - (b*e + f)/(2*f))*Sqrt[Pi]*(E^(((I/2)*b^2*Log[f]^2)/f)*Erfi[(((-1)^(1/4)*(e + 2*f*x - I*b*Log[f]))/(2*Sqrt[f]))*(Cos[d] + I*Sin[d]) + E^(((I/2)*e^2)/f)*Erfi[(((-1)^(3/4)*(e + 2*f*x + I*b*Log[f]))/(2*Sqrt[f]))*(I*Cos[d] + Sin[d])])/E^(((I/4)*(e^2 + b^2*Log[f]^2))/f)

fricas [B] time = 1.36, size = 313, normalized size = 1.93

$$i \sqrt{2} \pi \sqrt{\frac{f}{\pi}} e^{\left(\frac{-ib^2 \log(f)^2 + ie^2 - 4idf - 2(be - 2af) \log(f)}{4f} \right)} C \left(\frac{\sqrt{2}(2fx + ib \log(f) + e) \sqrt{\frac{f}{\pi}}}{2f} \right) + i \sqrt{2} \pi \sqrt{\frac{f}{\pi}} e^{\left(\frac{ib^2 \log(f)^2 - ie^2 + 4idf - 2(be - 2af) \log(f)}{4f} \right)} S \left(\frac{\sqrt{2}(2fx + ib \log(f) + e) \sqrt{\frac{f}{\pi}}}{2f} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(b*x+a)*sin(f*x^2+e*x+d), x, algorithm="fricas")

[Out] 1/4*(I*sqrt(2)*pi*sqrt(f/pi)*e^(1/4*(-I*b^2*log(f)^2 + I*e^2 - 4*I*d*f - 2*(b*e - 2*a*f)*log(f))/f)*fresnel_cos(1/2*sqrt(2)*(2*f*x + I*b*log(f) + e)*sqrt(f/pi)/f) + I*sqrt(2)*pi*sqrt(f/pi)*e^(1/4*(I*b^2*log(f)^2 - I*e^2 + 4*I*d*f - 2*(b*e - 2*a*f)*log(f))/f)*fresnel_cos(-1/2*sqrt(2)*(2*f*x - I*b*log(f) + e)*sqrt(f/pi)/f) + sqrt(2)*pi*sqrt(f/pi)*e^(1/4*(-I*b^2*log(f)^2 + I*e^2 - 4*I*d*f - 2*(b*e - 2*a*f)*log(f))/f)*fresnel_sin(1/2*sqrt(2)*(2*f*x + I*b*log(f) + e)*sqrt(f/pi)/f) - sqrt(2)*pi*sqrt(f/pi)*e^(1/4*(I*b^2*log(f)^2 - I*e^2 + 4*I*d*f - 2*(b*e - 2*a*f)*log(f))/f)*fresnel_sin(-1/2*sqrt(2)*(2*f*x - I*b*log(f) + e)*sqrt(f/pi)/f)/f

giac [B] time = 0.29, size = 384, normalized size = 2.37

$$i \sqrt{2} \sqrt{\pi} \operatorname{erf} \left(-\frac{1}{8} \sqrt{2} \left(4x - \frac{\pi \operatorname{sgn}(f) - \pi b + 2i b \log(|f|) - 2e}{f} \right) \left(-\frac{if}{|f|} + 1 \right) \sqrt{|f|} \right) e^{\left(\frac{i \pi^2 b^2 \operatorname{sgn}(f)}{8f} + \frac{\pi b^2 \log(|f|) \operatorname{sgn}(f)}{4f} - \frac{i \pi^2 b^2}{8f} - \frac{\pi b^2 \log(|f|)}{4f} + \frac{ie^2}{2f} \right)} \sqrt{|f|}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(b*x+a)*sin(f*x^2+e*x+d),x, algorithm="giac")

[Out] $\frac{1}{4}I\sqrt{2}\sqrt{\pi}\operatorname{erf}\left(-\frac{1}{8}\sqrt{2}\left(4x - (\pi b \operatorname{sgn}(f) - \pi b + 2Ib \log(\operatorname{abs}(f)) - 2e)/f\right)\sqrt{\operatorname{abs}(f)}\right)e^{\left(\frac{1}{8}I\pi^2 b^2 \operatorname{sgn}(f)/f + \frac{1}{4}\pi b^2 \log(\operatorname{abs}(f)) \operatorname{sgn}(f)/f - \frac{1}{8}I\pi^2 b^2/f - \frac{1}{4}\pi b^2 \log(\operatorname{abs}(f))/f + \frac{1}{4}Ib^2 \log(\operatorname{abs}(f))^2/f - \frac{1}{2}I\pi a \operatorname{sgn}(f) + \frac{1}{4}I\pi b e \operatorname{sgn}(f)/f + \frac{1}{2}I\pi a - \frac{1}{4}I\pi b e/f + a \log(\operatorname{abs}(f)) - \frac{1}{2}b e \log(\operatorname{abs}(f))/f + Id - \frac{1}{4}Ie^2/f\right)/\left((-I f/\operatorname{abs}(f) + 1)\sqrt{\operatorname{abs}(f)}\right)} - \frac{1}{4}I\sqrt{2}\sqrt{\pi}\operatorname{erf}\left(-\frac{1}{8}\sqrt{2}\left(4x + (\pi b \operatorname{sgn}(f) - \pi b + 2Ib \log(\operatorname{abs}(f)) + 2e)/f\right)\sqrt{\operatorname{abs}(f)}\right)e^{\left(-\frac{1}{8}I\pi^2 b^2 \operatorname{sgn}(f)/f - \frac{1}{4}\pi b^2 \log(\operatorname{abs}(f)) \operatorname{sgn}(f)/f + \frac{1}{8}I\pi^2 b^2/f + \frac{1}{4}\pi b^2 \log(\operatorname{abs}(f))/f - \frac{1}{4}Ib^2 \log(\operatorname{abs}(f))^2/f - \frac{1}{2}I\pi a \operatorname{sgn}(f) + \frac{1}{4}I\pi b e \operatorname{sgn}(f)/f + \frac{1}{2}I\pi a - \frac{1}{4}I\pi b e/f + a \log(\operatorname{abs}(f)) - \frac{1}{2}b e \log(\operatorname{abs}(f))/f - Id + \frac{1}{4}Ie^2/f\right)/\left((I f/\operatorname{abs}(f) + 1)\sqrt{\operatorname{abs}(f)}\right)}$

maple [A] time = 0.43, size = 152, normalized size = 0.94

$$\frac{i\sqrt{\pi} f^a e^{\frac{i(-e^2+2i\ln(f)be+\ln(f)^2b^2+4df)}{4f}} \operatorname{erf}\left(-\sqrt{-if} x + \frac{ie+b\ln(f)}{2\sqrt{-if}}\right)}{4\sqrt{-if}} - \frac{i\sqrt{\pi} f^a e^{-\frac{i(-e^2-2i\ln(f)be+\ln(f)^2b^2+4df)}{4f}} \operatorname{erf}\left(-\sqrt{if} x + \frac{-ie+b\ln(f)}{2\sqrt{if}}\right)}{4\sqrt{if}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(f^(b*x+a)*sin(f*x^2+e*x+d),x)

[Out] $\frac{1}{4}I\pi^{1/2}f^a \exp\left(\frac{1}{4}I(-e^2+2I\ln(f)b e+\ln(f)^2b^2+4d f)/f\right)/(-I f)^{1/2} \operatorname{erf}\left(-(-I f)^{1/2}x + \frac{1}{2}(I e+b \ln(f))/(-I f)^{1/2}\right) - \frac{1}{4}I\pi^{1/2}f^a \exp\left(-\frac{1}{4}I(-e^2-2I\ln(f)b e+\ln(f)^2b^2+4d f)/f\right)/(I f)^{1/2} \operatorname{erf}\left(-(-I f)^{1/2}x + \frac{1}{2}(-I e+b \ln(f))/(I f)^{1/2}\right)$

maxima [A] time = 0.36, size = 190, normalized size = 1.17

$$\frac{\sqrt{2}\sqrt{\pi}\left(\left((i+1)f^a \cos\left(\frac{b^2 \log(f)^2 - e^2 + 4df}{4f}\right) - (i-1)f^a \sin\left(\frac{b^2 \log(f)^2 - e^2 + 4df}{4f}\right)\right) \operatorname{erf}\left(\frac{i(2ifx - b \log(f) + ie)\sqrt{if}}{2f}\right) + \left(- (i-1)\right) \operatorname{erf}\left(\frac{-i(2ifx - b \log(f) + ie)\sqrt{if}}{2f}\right)\right)}{8\sqrt{f} f^{\frac{be}{2f}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(b*x+a)*sin(f*x^2+e*x+d),x, algorithm="maxima")

[Out] $-\frac{1}{8}\sqrt{2}\sqrt{\pi}\left(\left((I+1)f^a \cos\left(\frac{1}{4}(b^2 \log(f)^2 - e^2 + 4d f)/f\right) - (I-1)f^a \sin\left(\frac{1}{4}(b^2 \log(f)^2 - e^2 + 4d f)/f\right)\right) \operatorname{erf}\left(\frac{1}{2}I(2I f x - b \log(f) + I e)\sqrt{I f}/f\right) + \left(- (I-1)f^a \cos\left(\frac{1}{4}(b^2 \log(f)^2 - e^2 + 4d f)/f\right) + (I+1)f^a \sin\left(\frac{1}{4}(b^2 \log(f)^2 - e^2 + 4d f)/f\right)\right) \operatorname{erf}\left(\frac{1}{2}I(2I f x + b \log(f) + I e)\sqrt{-I f}/f\right)\right)/(\sqrt{f} f^{1/2 b e/f})$

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int f^{a+bx} \sin(fx^2 + ex + d) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(f^(a + b*x)*sin(d + e*x + f*x^2),x)

[Out] int(f^(a + b*x)*sin(d + e*x + f*x^2), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int f^{a+bx} \sin(d + ex + fx^2) dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(f**(b*x+a)*sin(f*x**2+e*x+d),x)
```

```
[Out] Integral(f**(a + b*x)*sin(d + e*x + f*x**2), x)
```

3.83 $\int f^{a+bx} \sin^2(d + ex + fx^2) dx$

Optimal. Leaf size=179

$$\left(\frac{1}{16} + \frac{i}{16}\right) \sqrt{\pi} f^{a-\frac{1}{2}} e^{\frac{i(b \log(f)+2ie)^2}{8f} + 2id} \operatorname{erf}\left(\frac{\left(\frac{1}{4} + \frac{i}{4}\right)(b \log(f) + 2ie + 4ifx)}{\sqrt{f}}\right) + \left(\frac{1}{16} + \frac{i}{16}\right) \sqrt{\pi} f^{a-\frac{1}{2}} e^{\frac{i(2e+ib \log(f))^2}{8f} - 2id} \operatorname{erfi}\left(\frac{\left(\frac{1}{4} + \frac{i}{4}\right)(b \log(f) + 2ie + 4ifx)}{\sqrt{f}}\right)$$

[Out] 1/2*f^(b*x+a)/b/ln(f)+(1/16+1/16*I)*exp(2*I*d+1/8*I*(2*I*e+b*ln(f))^2/f)*f^(-1/2+a)*erf((1/4+1/4*I)*(2*I*e+4*I*f*x+b*ln(f))/f^(1/2))*Pi^(1/2)+(1/16+1/16*I)*exp(-2*I*d+1/8*I*(2*e+I*b*ln(f))^2/f)*f^(-1/2+a)*erfi((1/4+1/4*I)*(2*I*e+4*I*f*x-b*ln(f))/f^(1/2))*Pi^(1/2)

Rubi [A] time = 0.35, antiderivative size = 179, normalized size of antiderivative = 1.00, number of steps used = 9, number of rules used = 6, integrand size = 21, $\frac{\text{number of rules}}{\text{integrand size}} = 0.286$, Rules used = {4472, 2194, 2287, 2234, 2204, 2205}

$$\left(\frac{1}{16} + \frac{i}{16}\right) \sqrt{\pi} f^{a-\frac{1}{2}} e^{\frac{i(b \log(f)+2ie)^2}{8f} + 2id} \operatorname{Erf}\left(\frac{\left(\frac{1}{4} + \frac{i}{4}\right)(b \log(f) + 2ie + 4ifx)}{\sqrt{f}}\right) + \left(\frac{1}{16} + \frac{i}{16}\right) \sqrt{\pi} f^{a-\frac{1}{2}} e^{\frac{i(2e+ib \log(f))^2}{8f} - 2id} \operatorname{Erfi}\left(\frac{\left(\frac{1}{4} + \frac{i}{4}\right)(b \log(f) + 2ie + 4ifx)}{\sqrt{f}}\right)$$

Antiderivative was successfully verified.

[In] Int[f^(a + b*x)*Sin[d + e*x + f*x^2]^2,x]

[Out] (1/16 + I/16)*E^((2*I)*d + ((I/8)*((2*I)*e + b*Log[f])^2)/f)*f^(-1/2 + a)*Sqrt[Pi]*Erf[(((1/4 + I/4)*((2*I)*e + (4*I)*f*x + b*Log[f]))/Sqrt[f]] + (1/16 + I/16)*E^((-2*I)*d + ((I/8)*(2*e + I*b*Log[f])^2)/f)*f^(-1/2 + a)*Sqrt[Pi]*Erfi[(((1/4 + I/4)*((2*I)*e + (4*I)*f*x - b*Log[f]))/Sqrt[f]] + f^(a + b*x)/(2*b*Log[f])]

Rule 2194

Int[((F_)^((c_.)*((a_.) + (b_.)*(x_))))^(n_.), x_Symbol] :> Simp[(F^(c*(a + b*x)))^n/(b*c*n*Log[F]), x] /; FreeQ[{F, a, b, c, n}, x]

Rule 2204

Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^2), x_Symbol] :> Simp[(F^a*Sqrt[Pi]*Erfi[(c + d*x)*Rt[b*Log[F], 2]])/(2*d*Rt[b*Log[F], 2]), x] /; FreeQ[{F, a, b, c, d}, x] && PosQ[b]

Rule 2205

Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^2), x_Symbol] :> Simp[(F^a*Sqrt[Pi]*Erf[(c + d*x)*Rt[-(b*Log[F]), 2]])/(2*d*Rt[-(b*Log[F]), 2]), x] /; FreeQ[{F, a, b, c, d}, x] && NegQ[b]

Rule 2234

Int[(F_)^((a_.) + (b_.)*(x_) + (c_.)*(x_)^2), x_Symbol] :> Dist[F^(a - b^2/(4*c)), Int[F^((b + 2*c*x)^2/(4*c)), x], x] /; FreeQ[{F, a, b, c}, x]

Rule 2287

Int[(u_.)*(F_)^(v_.)*(G_)^(w_.), x_Symbol] :> With[{z = v*Log[F] + w*Log[G]}, Int[u*NormalizeIntegrand[E^z, x], x] /; BinomialQ[z, x] || (PolynomialQ[z, x] && LeQ[Exponent[z, x], 2])] /; FreeQ[{F, G}, x]

Rule 4472

$\text{Int}[(F_)^{(u_)} * \text{Sin}[v_]^{(n_.)}, x_Symbol] \rightarrow \text{Int}[\text{ExpandTrigToExp}[F^u, \text{Sin}[v]^{n}], x], x] /;$ FreeQ[F, x] && (LinearQ[u, x] || PolyQ[u, x, 2]) && (LinearQ[v, x] || PolyQ[v, x, 2]) && IGtQ[n, 0]

Rubi steps

$$\begin{aligned} \int f^{a+bx} \sin^2(d+ex+fx^2) dx &= \int \left(\frac{1}{2} f^{a+bx} - \frac{1}{4} e^{-2id-2iex-2ifx^2} f^{a+bx} - \frac{1}{4} e^{2id+2iex+2ifx^2} f^{a+bx} \right) dx \\ &= -\left(\frac{1}{4} \int e^{-2id-2iex-2ifx^2} f^{a+bx} dx \right) - \frac{1}{4} \int e^{2id+2iex+2ifx^2} f^{a+bx} dx + \frac{1}{2} \int f^{a+bx} dx \\ &= \frac{f^{a+bx}}{2b \log(f)} - \frac{1}{4} \int \exp(-2id - 2ifx^2 + a \log(f) - x(2ie - b \log(f))) dx - \frac{1}{4} \int \exp(2id + 2iex + 2ifx^2 + a \log(f) + x(2ie + b \log(f))) dx \\ &= \frac{f^{a+bx}}{2b \log(f)} - \frac{1}{4} \exp\left(-2id + a \log(f) - \frac{i(-2ie + b \log(f))^2}{8f}\right) \int e^{\frac{i(-2ie-4ifx+b \log(f))x}{8f}} dx \\ &= \left(\frac{1}{16} + \frac{i}{16} \right) e^{2id + \frac{i(2ie+b \log(f))^2}{8f}} f^{-\frac{1}{2}+a} \sqrt{\pi} \operatorname{erf}\left(\frac{\left(\frac{1}{4} + \frac{i}{4}\right)(2ie + 4ifx + b \log(f))}{\sqrt{f}} \right) + \frac{f^{a+bx}}{2b \log(f)} \end{aligned}$$

Mathematica [A] time = 1.08, size = 244, normalized size = 1.36

$$f^{a-\frac{be+fx}{2f}} e^{-\frac{i(b^2 \log^2(f)+4e^2)}{8f}} \left(\sqrt[4]{-1} \sqrt{2\pi} b \log(f) e^{\frac{ib^2 \log^2(f)}{4f}} (\cos(2d) + i \sin(2d)) \operatorname{erf}\left(\frac{\left(\frac{1}{4} + \frac{i}{4}\right)(b \log(f) + 2i(e+2fx))}{\sqrt{f}} \right) + 8f^{b\left(\frac{e}{2f}+x\right)} \right) + \frac{f^{a+bx}}{2b \log(f)}$$

Antiderivative was successfully verified.

[In] Integrate[f^(a + b*x)*Sin[d + e*x + f*x^2]^2,x]

[Out] (f^(a - (b*e + f)/(2*f)) * (8 * E^(((I/8) * (4*e^2 + b^2 * Log[f]^2))/f)) * f^(1/2 + b * (e/(2*f) + x)) + (-1)^(1/4) * b * E^(((I/4) * b^2 * Log[f]^2)/f) * Sqrt[2*Pi] * Erf[(((1/4 + I/4) * ((2*I) * (e + 2*f*x) + b * Log[f]))/Sqrt[f]) * Log[f] * (Cos[2*d] + I * Sin[2*d]) + (-1)^(1/4) * b * E^((I * e^2)/f) * Sqrt[2*Pi] * Erf[(((1/4 + I/4) * (2*e + 4*f*x + I * b * Log[f]))/Sqrt[f]) * Log[f] * (I * Cos[2*d] + Sin[2*d])]) / (16 * b * E^(((I/8) * (4*e^2 + b^2 * Log[f]^2))/f) * Log[f])

fricas [B] time = 0.80, size = 327, normalized size = 1.83

$$2 \pi b \sqrt{\frac{f}{\pi}} e^{\left(\frac{-ib^2 \log(f)^2 + 4ie^2 - 16idf - 4(be-2af) \log(f)}{8f} \right)} C\left(\frac{(4fx + ib \log(f) + 2e) \sqrt{\frac{f}{\pi}}}{2f} \right) \log(f) - 2 \pi b \sqrt{\frac{f}{\pi}} e^{\left(\frac{ib^2 \log(f)^2 - 4ie^2 + 16idf - 4(be-2af) \log(f)}{8f} \right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(b*x+a)*sin(f*x^2+e*x+d)^2,x, algorithm="fricas")

[Out] -1/16*(2*pi*b*sqrt(f/pi))*e^(1/8*(-I*b^2*log(f)^2 + 4*I*e^2 - 16*I*d*f - 4*(b*e - 2*a*f)*log(f))/f)*fresnel_cos(1/2*(4*f*x + I*b*log(f) + 2*e)*sqrt(f/pi)/f)*log(f) - 2*pi*b*sqrt(f/pi)*e^(1/8*(I*b^2*log(f)^2 - 4*I*e^2 + 16*I*d*f - 4*(b*e - 2*a*f)*log(f))/f)*fresnel_cos(-1/2*(4*f*x - I*b*log(f) + 2*e)*sqrt(f/pi)/f)*log(f) - 2*I*pi*b*sqrt(f/pi)*e^(1/8*(-I*b^2*log(f)^2 + 4*I*e^2 - 16*I*d*f - 4*(b*e - 2*a*f)*log(f))/f)*fresnel_sin(1/2*(4*f*x + I*b*log(f) + 2*e)*sqrt(f/pi)/f)*log(f) - 2*I*pi*b*sqrt(f/pi)*e^(1/8*(I*b^2*log(f)^2 - 4*I*e^2 + 16*I*d*f - 4*(b*e - 2*a*f)*log(f))/f)*fresnel_sin(-1/2*(4*f*x - I*b*log(f) + 2*e)*sqrt(f/pi)/f)*log(f)

$$- 4*I*e^2 + 16*I*d*f - 4*(b*e - 2*a*f)*\log(f))/f)*\text{fresnel_sin}(-1/2*(4*f*x - I*b*\log(f) + 2*e)*\text{sqrt}(f/\text{pi})/f)*\log(f) - 8*f*f^(b*x + a))/(b*f*\log(f))$$

giac [B] time = 0.35, size = 605, normalized size = 3.38

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(b*x+a)*sin(f*x^2+e*x+d)^2,x, algorithm="giac")

[Out] (2*b*cos(-1/2*pi*b*x*sgn(f) + 1/2*pi*b*x - 1/2*pi*a*sgn(f) + 1/2*pi*a)*log(abs(f))/(4*b^2*log(abs(f))^2 + (pi*b*sgn(f) - pi*b)^2) - (pi*b*sgn(f) - pi*b)*sin(-1/2*pi*b*x*sgn(f) + 1/2*pi*b*x - 1/2*pi*a*sgn(f) + 1/2*pi*a)/(4*b^2*log(abs(f))^2 + (pi*b*sgn(f) - pi*b)^2))*e^(b*x*log(abs(f)) + a*log(abs(f))) - 1/2*I*(-2*I*e^(1/2*I*pi*b*x*sgn(f) - 1/2*I*pi*b*x + 1/2*I*pi*a*sgn(f) - 1/2*I*pi*a)/(2*I*pi*b*sgn(f) - 2*I*pi*b + 4*b*log(abs(f))) + 2*I*e^(-1/2*I*pi*b*x*sgn(f) + 1/2*I*pi*b*x - 1/2*I*pi*a*sgn(f) + 1/2*I*pi*a)/(-2*I*pi*b*sgn(f) + 2*I*pi*b + 4*b*log(abs(f))))*e^(b*x*log(abs(f)) + a*log(abs(f))) + 1/8*sqrt(pi)*erf(-1/8*sqrt(f)*(8*x - (pi*b*sgn(f) - pi*b + 2*I*b*log(abs(f)) - 4*e)/f)*(-I*f/abs(f) + 1))*e^(1/16*I*pi^2*b^2*sgn(f)/f + 1/8*pi*b^2*log(abs(f))*sgn(f)/f - 1/16*I*pi^2*b^2/f - 1/8*pi*b^2*log(abs(f))/f + 1/8*I*b^2*log(abs(f))^2/f - 1/2*I*pi*a*sgn(f) + 1/4*I*pi*b*e*sgn(f)/f + 1/2*I*pi*a - 1/4*I*pi*b*e/f + a*log(abs(f)) - 1/2*b*e*log(abs(f))/f + 2*I*d - 1/2*I*e^2/f)/(sqrt(f)*(-I*f/abs(f) + 1)) + 1/8*sqrt(pi)*erf(-1/8*sqrt(f)*(8*x + (pi*b*sgn(f) - pi*b + 2*I*b*log(abs(f)) + 4*e)/f)*(I*f/abs(f) + 1))*e^(-1/16*I*pi^2*b^2*sgn(f)/f - 1/8*pi*b^2*log(abs(f))*sgn(f)/f + 1/16*I*pi^2*b^2/f + 1/8*pi*b^2*log(abs(f))/f - 1/8*I*b^2*log(abs(f))^2/f - 1/2*I*pi*a*sgn(f) + 1/4*I*pi*b*e*sgn(f)/f + 1/2*I*pi*a - 1/4*I*pi*b*e/f + a*log(abs(f)) - 1/2*b*e*log(abs(f))/f - 2*I*d + 1/2*I*e^2/f)/(sqrt(f)*(I*f/abs(f) + 1))

maple [A] time = 0.69, size = 175, normalized size = 0.98

$$\frac{\sqrt{\pi} f^a e^{-\frac{i(\ln(f)^2 b^2 - 4i \ln(f) b e - 4e^2 + 16df)}{8f}} \sqrt{2} \operatorname{erf}\left(-\sqrt{2} \sqrt{if} x + \frac{(b \ln(f) - 2ie)\sqrt{2}}{4\sqrt{if}}\right)}{16\sqrt{if}} + \frac{\sqrt{\pi} f^a e^{\frac{i(\ln(f)^2 b^2 + 4i \ln(f) b e - 4e^2 + 16df)}{8f}} \operatorname{erf}\left(-\sqrt{-2if}\right)}{8\sqrt{-2if}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(f^(b*x+a)*sin(f*x^2+e*x+d)^2,x)

[Out] 1/16*Pi^(1/2)*f^a*exp(-1/8*I*(ln(f)^2*b^2-4*I*ln(f)*b*e-4*e^2+16*d*f)/f)*2^(1/2)/(I*f)^(1/2)*erf(-2^(1/2)*(I*f)^(1/2)*x+1/4*(b*ln(f)-2*I*e)*2^(1/2)/(I*f)^(1/2))+1/8*Pi^(1/2)*f^a*exp(1/8*I*(ln(f)^2*b^2+4*I*ln(f)*b*e-4*e^2+16*d*f)/f)/(-2*I*f)^(1/2)*erf(-(-2*I*f)^(1/2)*x+1/2*(2*I*e+b*ln(f))/(-2*I*f)^(1/2))+1/2*f^(b*x+a)/b/ln(f)

maxima [B] time = 0.46, size = 240, normalized size = 1.34

$$\frac{4^{\frac{1}{4}} \sqrt{2} \sqrt{\pi} \left(\left(-(i-1) b f^a \cos\left(\frac{b^2 \log(f)^2 - 4e^2 + 16df}{8f}\right) \log(f) - (i+1) b f^a \log(f) \sin\left(\frac{b^2 \log(f)^2 - 4e^2 + 16df}{8f}\right) \right) \operatorname{erf}\left(\frac{i(4ifx-b)}{8\sqrt{if}}\right) \right)}{16\sqrt{if}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(b*x+a)*sin(f*x^2+e*x+d)^2,x, algorithm="maxima")

[Out] 1/32*(4^(1/4)*sqrt(2)*sqrt(pi))*((-I - 1)*b*f^a*cos(1/8*(b^2*log(f)^2 - 4*e^2 + 16*d*f)/f)*log(f) - (I + 1)*b*f^a*log(f)*sin(1/8*(b^2*log(f)^2 - 4*e^2 + 16*d*f)/f))*erf(1/4*I*(4*I*f*x - b*log(f) + 2*I*e)*sqrt(2*I*f)/f) + ((I

+ 1)*b*f^a*cos(1/8*(b^2*log(f)^2 - 4*e^2 + 16*d*f)/f)*log(f) + (I - 1)*b*f^a*log(f)*sin(1/8*(b^2*log(f)^2 - 4*e^2 + 16*d*f)/f))*erf(1/4*I*(4*I*f*x + b*log(f) + 2*I*e)*sqrt(-2*I*f)/f))*f^(3/2) + 16*f^(a + 2)*e^(b*x*log(f) + 1/2*b*e*log(f)/f))/(b*f^2*f^(1/2*b*e/f)*log(f))

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int f^{a+bx} \sin(fx^2 + ex + d)^2 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(f^(a + b*x)*sin(d + e*x + f*x^2)^2,x)

[Out] int(f^(a + b*x)*sin(d + e*x + f*x^2)^2, x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int f^{a+bx} \sin^2(d + ex + fx^2) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f**(b*x+a)*sin(f*x**2+e*x+d)**2,x)

[Out] Integral(f**(a + b*x)*sin(d + e*x + f*x**2)**2, x)

3.84 $\int f^{a+bx} \sin^3(d + ex + fx^2) dx$

Optimal. Leaf size=340

$$\frac{3}{16}(-1)^{3/4}\sqrt{\pi}f^{a-\frac{1}{2}}e^{\frac{1}{4}i\left(4d+\frac{(b\log(f)+ie)^2}{f}\right)}\operatorname{erf}\left(\frac{\sqrt[4]{-1}(b\log(f)+ie+2ifx)}{2\sqrt{f}}\right)+\left(\frac{1}{16}-\frac{i}{16}\right)\sqrt{\frac{\pi}{6}}f^{a-\frac{1}{2}}e^{\frac{i(b\log(f)+3ie)^2}{12f}+3id}\operatorname{erf}\left(\frac{\sqrt{\frac{\pi}{6}}}{2}\right)$$

[Out] (1/96-1/96*I)*exp(3*I*d+1/12*I*(3*I*e+b*ln(f))^2/f)*f^(-1/2+a)*erf((1/12+1/12*I)*(3*I*e+6*I*f*x+b*ln(f))*6^(1/2)/f^(1/2))*6^(1/2)*Pi^(1/2)+(-1/96+1/96*I)*exp(-3*I*d+1/12*I*(3*e+I*b*ln(f))^2/f)*f^(-1/2+a)*erfi((1/12+1/12*I)*(3*I*e+6*I*f*x-b*ln(f))*6^(1/2)/f^(1/2))*6^(1/2)*Pi^(1/2)+3/16*(-1)^(3/4)*exp(1/4*I*(4*d+(I*e+b*ln(f))^2/f))*f^(-1/2+a)*erf(1/2*(-1)^(1/4)*(I*e+2*I*f*x+b*ln(f))/f^(1/2))*Pi^(1/2)-3/16*(-1)^(3/4)*exp(-I*d+1/4*I*(e+I*b*ln(f))^2/f)*f^(-1/2+a)*erfi(1/2*(-1)^(1/4)*(I*e+2*I*f*x-b*ln(f))/f^(1/2))*Pi^(1/2)

Rubi [A] time = 0.60, antiderivative size = 340, normalized size of antiderivative = 1.00, number of steps used = 14, number of rules used = 5, integrand size = 21, $\frac{\text{number of rules}}{\text{integrand size}} = 0.238$, Rules used = {4472, 2287, 2234, 2204, 2205}

$$\frac{3}{16}(-1)^{3/4}\sqrt{\pi}f^{a-\frac{1}{2}}e^{\frac{1}{4}i\left(4d+\frac{(b\log(f)+ie)^2}{f}\right)}\operatorname{Erf}\left(\frac{\sqrt[4]{-1}(b\log(f)+ie+2ifx)}{2\sqrt{f}}\right)+\left(\frac{1}{16}-\frac{i}{16}\right)\sqrt{\frac{\pi}{6}}f^{a-\frac{1}{2}}e^{\frac{i(b\log(f)+3ie)^2}{12f}+3id}\operatorname{Erf}\left(\frac{\sqrt{\frac{\pi}{6}}}{2}\right)$$

Antiderivative was successfully verified.

[In] Int[f^(a + b*x)*Sin[d + e*x + f*x^2]^3,x]

[Out] (3*(-1)^(3/4)*E^((I/4)*(4*d + (I*e + b*Log[f])^2/f))*f^(-1/2 + a)*Sqrt[Pi]*Erfi[(-1)^(1/4)*(I*e + (2*I)*f*x + b*Log[f])/(2*Sqrt[f])]/16 + (1/16 - I/16)*E^((3*I)*d + ((I/12)*((3*I)*e + b*Log[f])^2)/f)*f^(-1/2 + a)*Sqrt[Pi/6]*Erfi[((1/2 + I/2)*((3*I)*e + (6*I)*f*x + b*Log[f]))/(Sqrt[6]*Sqrt[f])] - (3*(-1)^(3/4)*E^((-I)*d + ((I/4)*(e + I*b*Log[f])^2)/f)*f^(-1/2 + a)*Sqrt[Pi]*Erfi[(-1)^(1/4)*(I*e + (2*I)*f*x - b*Log[f])/(2*Sqrt[f])]/16 - (1/16 - I/16)*E^((-3*I)*d + ((I/12)*(3*e + I*b*Log[f])^2)/f)*f^(-1/2 + a)*Sqrt[Pi/6]*Erfi[((1/2 + I/2)*((3*I)*e + (6*I)*f*x - b*Log[f]))/(Sqrt[6]*Sqrt[f])]

Rule 2204

Int[(F_)^((a_) + (b_)*((c_) + (d_)*(x_)^2), x_Symbol] := Simp[(F^a*Sqrt[Pi]*Erfi[(c + d*x)*Rt[b*Log[F], 2]]/(2*d*Rt[b*Log[F], 2]), x] /; FreeQ[{F, a, b, c, d}, x] && PosQ[b]

Rule 2205

Int[(F_)^((a_) + (b_)*((c_) + (d_)*(x_)^2), x_Symbol] := Simp[(F^a*Sqrt[Pi]*Erfi[(c + d*x)*Rt[-(b*Log[F]), 2]]/(2*d*Rt[-(b*Log[F]), 2]), x] /; FreeQ[{F, a, b, c, d}, x] && NegQ[b]

Rule 2234

Int[(F_)^((a_) + (b_)*(x_) + (c_)*(x_)^2), x_Symbol] := Dist[F^(a - b^2/(4*c)), Int[F^((b + 2*c*x)^2/(4*c)), x], x] /; FreeQ[{F, a, b, c}, x]

Rule 2287

Int[(u_)*(F_)^(v_)*(G_)^(w_), x_Symbol] := With[{z = v*Log[F] + w*Log[G]}, Int[u*NormalizeIntegrand[E^z, x], x] /; BinomialQ[z, x] || (PolynomialQ[z, x] && LeQ[Exponent[z, x], 2])] /; FreeQ[{F, G}, x]

Rule 4472

$\text{Int}[(F_)^{(u_)} \cdot \text{Sin}[v_]^{(n_.)}, x_Symbol] \rightarrow \text{Int}[\text{ExpandTrigToExp}[F^u, \text{Sin}[v]^{n}], x], x] /;$ FreeQ[F, x] && (LinearQ[u, x] || PolyQ[u, x, 2]) && (LinearQ[v, x] || PolyQ[v, x, 2]) && IGtQ[n, 0]

Rubi steps

$$\begin{aligned} \int f^{a+bx} \sin^3(d+ex+fx^2) dx &= \int \left(-\frac{1}{8} i e^{-3i(d+ex+fx^2)} f^{a+bx} + \frac{3}{8} i \exp(2id+2iex+2ifx^2-3i(d+ex+fx^2)) \right. \\ &= -\left(\frac{1}{8} i \int e^{-3i(d+ex+fx^2)} f^{a+bx} dx \right) + \frac{1}{8} i \int \exp(6id+6iex+6ifx^2-3i(d+ex+fx^2)) \\ &= -\left(\frac{1}{8} i \int \exp(-3id-3ifx^2+a \log(f)-x(3ie-b \log(f))) dx \right) + \frac{1}{8} i \int \exp(6id+6iex+6ifx^2-3i(d+ex+fx^2)) \\ &= -\left(\frac{1}{8} \left(i \exp\left(-3id+a \log(f)-\frac{i(-3ie+b \log(f))^2}{12f}\right) \right) \int e^{\frac{i(-3ie-6ifx+b \log(f))^2}{12f}} dx \right) \\ &= \frac{3}{16} (-1)^{3/4} e^{\frac{1}{4} \left(4d + \frac{(ie+b \log(f))^2}{f} \right)} f^{-\frac{1}{2}+a} \sqrt{\pi} \operatorname{erf}\left(\frac{\sqrt[4]{-1}(ie+2ifx+b \log(f))}{2\sqrt{f}}\right) + \left(\frac{1}{16}\right) \end{aligned}$$

Mathematica [A] time = 1.50, size = 323, normalized size = 0.95

$$\frac{1}{48} (-1)^{3/4} \sqrt{\pi} f^{a-\frac{be+f}{2f}} e^{-\frac{i(b^2 \log^2(f)+3e^2)}{4f}} \left(9i(\cos(d)+i \sin(d)) e^{\frac{i(b^2 \log^2(f)+e^2)}{2f}} \operatorname{erfi}\left(\frac{\sqrt[4]{-1}(-ib \log(f)+e+2fx)}{2\sqrt{f}}\right) + e^{\frac{ie^2}{f}} \right)$$

Antiderivative was successfully verified.

[In] Integrate[f^(a + b*x)*Sin[d + e*x + f*x^2]^3,x]

[Out] $((-1)^{(3/4)} f^{(a - (b * e + f) / (2 * f))} * \text{Sqrt}[\text{Pi}] * ((9 * I) * E^{((I/2) * (e^2 + b^2 * \text{Log}[f]^2)) / f} * \text{Erfi}[\frac{(-1)^{(1/4)} * (e + 2 * f * x - I * b * \text{Log}[f])}{(2 * \text{Sqrt}[f])}] * (\text{Cos}[d] + I * \text{Sin}[d]) + E^{((I * e^2) / f)} * (-9 * \text{Erfi}[\frac{(-1)^{(3/4)} * (e + 2 * f * x + I * b * \text{Log}[f])}{(2 * \text{Sqrt}[f])}] * (\text{Cos}[d] - I * \text{Sin}[d]) + \text{Sqrt}[3] * E^{((I/6) * (3 * e^2 + b^2 * \text{Log}[f]^2)) / f} * \text{Erfi}[\frac{(-1)^{(3/4)} * (3 * e + 6 * f * x + I * b * \text{Log}[f])}{(2 * \text{Sqrt}[3] * \text{Sqrt}[f])}] * (\text{Cos}[3 * d] - I * \text{Sin}[3 * d]) + \text{Sqrt}[3] * E^{((I/3) * b^2 * \text{Log}[f]^2) / f} * \text{Erfi}[\frac{(1/2 + I/2) * (3 * e + 6 * f * x - I * b * \text{Log}[f])}{(\text{Sqrt}[6] * \text{Sqrt}[f])}] * ((-I) * \text{Cos}[3 * d] + \text{Sin}[3 * d])]) / (48 * E^{((I/4) * (3 * e^2 + b^2 * \text{Log}[f]^2)) / f})$

fricas [B] time = 1.56, size = 629, normalized size = 1.85

$$-i \sqrt{6} \pi \sqrt{\frac{f}{\pi}} e^{\left(\frac{-ib^2 \log(f)^2 + 9ie^2 - 36idf - 6(be-2af) \log(f)}{12f}\right)} C\left(\frac{\sqrt{6}(6fx+ib \log(f)+3e)\sqrt{\frac{f}{\pi}}}{6f}\right) - i \sqrt{6} \pi \sqrt{\frac{f}{\pi}} e^{\left(\frac{ib^2 \log(f)^2 - 9ie^2 + 36idf - 6(be-2af)}{12f}\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(b*x+a)*sin(f*x^2+e*x+d)^3,x, algorithm="fricas")

[Out] $1/48 * (-I * \text{sqrt}(6) * \text{pi} * \text{sqrt}(f/\text{pi}) * e^{(1/12 * (-I * b^2 * \text{log}(f))^2 + 9 * I * e^2 - 36 * I * d * f - 6 * (b * e - 2 * a * f) * \text{log}(f)) / f} * \text{fresnel_cos}(1/6 * \text{sqrt}(6) * (6 * f * x + I * b * \text{log}(f) + 3 * e) * \text{sqrt}(f/\text{pi}) / f) - I * \text{sqrt}(6) * \text{pi} * \text{sqrt}(f/\text{pi}) * e^{(1/12 * (I * b^2 * \text{log}(f))^2 - 9 * I * e^2 + 36 * I * d * f - 6 * (b * e - 2 * a * f) * \text{log}(f)) / f} * \text{fresnel_cos}(-1/6 * \text{sqrt}(6) * (6 * f * x - I * b * \text{log}(f) + 3 * e) * \text{sqrt}(f/\text{pi}) / f) + 9 * I * \text{sqrt}(2) * \text{pi} * \text{sqrt}(f/\text{pi}) * e^{(1/4 * (-I * b^2 * \text{log}(f))^2 + 9 * I * e^2 - 36 * I * d * f - 6 * (b * e - 2 * a * f) * \text{log}(f)) / f} * \text{fresnel_cos}(1/6 * \text{sqrt}(6) * (6 * f * x + I * b * \text{log}(f) + 3 * e) * \text{sqrt}(f/\text{pi}) / f) - 9 * I * \text{sqrt}(2) * \text{pi} * \text{sqrt}(f/\text{pi}) * e^{(1/4 * (I * b^2 * \text{log}(f))^2 - 9 * I * e^2 + 36 * I * d * f - 6 * (b * e - 2 * a * f) * \text{log}(f)) / f} * \text{fresnel_cos}(-1/6 * \text{sqrt}(6) * (6 * f * x - I * b * \text{log}(f) + 3 * e) * \text{sqrt}(f/\text{pi}) / f)$

```
*b^2*log(f)^2 + I*e^2 - 4*I*d*f - 2*(b*e - 2*a*f)*log(f))/f)*fresnel_cos(1/
2*sqrt(2)*(2*f*x + I*b*log(f) + e)*sqrt(f/pi)/f) + 9*I*sqrt(2)*pi*sqrt(f/pi
)*e^(1/4*(I*b^2*log(f)^2 - I*e^2 + 4*I*d*f - 2*(b*e - 2*a*f)*log(f))/f)*fre
snel_cos(-1/2*sqrt(2)*(2*f*x - I*b*log(f) + e)*sqrt(f/pi)/f) - sqrt(6)*pi*s
qrt(f/pi)*e^(1/12*(-I*b^2*log(f)^2 + 9*I*e^2 - 36*I*d*f - 6*(b*e - 2*a*f)*l
og(f))/f)*fresnel_sin(1/6*sqrt(6)*(6*f*x + I*b*log(f) + 3*e)*sqrt(f/pi)/f)
+ sqrt(6)*pi*sqrt(f/pi)*e^(1/12*(I*b^2*log(f)^2 - 9*I*e^2 + 36*I*d*f - 6*(b
*e - 2*a*f)*log(f))/f)*fresnel_sin(-1/6*sqrt(6)*(6*f*x - I*b*log(f) + 3*e)*
sqrt(f/pi)/f) + 9*sqrt(2)*pi*sqrt(f/pi)*e^(1/4*(-I*b^2*log(f)^2 + I*e^2 - 4
*I*d*f - 2*(b*e - 2*a*f)*log(f))/f)*fresnel_sin(1/2*sqrt(2)*(2*f*x + I*b*lo
g(f) + e)*sqrt(f/pi)/f) - 9*sqrt(2)*pi*sqrt(f/pi)*e^(1/4*(I*b^2*log(f)^2 -
I*e^2 + 4*I*d*f - 2*(b*e - 2*a*f)*log(f))/f)*fresnel_sin(-1/2*sqrt(2)*(2*f*
x - I*b*log(f) + e)*sqrt(f/pi)/f))/f
```

giac [B] time = 0.55, size = 763, normalized size = 2.24

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(b*x+a)*sin(f*x^2+e*x+d)^3,x, algorithm="giac")

```
[Out] 3/16*I*sqrt(2)*sqrt(pi)*erf(-1/8*sqrt(2)*(4*x - (pi*b*sgn(f) - pi*b + 2*I*b
*log(abs(f)) - 2*e)/f)*(-I*f/abs(f) + 1)*sqrt(abs(f)))*e^(1/8*I*pi^2*b^2*sg
n(f)/f + 1/4*pi*b^2*log(abs(f))*sgn(f)/f - 1/8*I*pi^2*b^2/f - 1/4*pi*b^2*lo
g(abs(f))/f + 1/4*I*b^2*log(abs(f))^2/f - 1/2*I*pi*a*sgn(f) + 1/4*I*pi*b*e*
sgn(f)/f + 1/2*I*pi*a - 1/4*I*pi*b*e/f + a*log(abs(f)) - 1/2*b*e*log(abs(f)
)/f + I*d - 1/4*I*e^2/f)/((-I*f/abs(f) + 1)*sqrt(abs(f))) - 1/48*I*sqrt(6)*
sqrt(pi)*erf(-1/24*sqrt(6)*sqrt(f)*(12*x - (pi*b*sgn(f) - pi*b + 2*I*b*log(
abs(f)) - 6*e)/f)*(-I*f/abs(f) + 1))*e^(1/24*I*pi^2*b^2*sgn(f)/f + 1/12*pi*
b^2*log(abs(f))*sgn(f)/f - 1/24*I*pi^2*b^2/f - 1/12*pi*b^2*log(abs(f))/f +
1/12*I*b^2*log(abs(f))^2/f - 1/2*I*pi*a*sgn(f) + 1/4*I*pi*b*e*sgn(f)/f + 1/
2*I*pi*a - 1/4*I*pi*b*e/f + a*log(abs(f)) - 1/2*b*e*log(abs(f))/f + 3*I*d -
3/4*I*e^2/f)/(sqrt(f)*(-I*f/abs(f) + 1)) + 1/48*I*sqrt(6)*sqrt(pi)*erf(-1/
24*sqrt(6)*sqrt(f)*(12*x + (pi*b*sgn(f) - pi*b + 2*I*b*log(abs(f)) + 6*e)/f
)*(I*f/abs(f) + 1))*e^(-1/24*I*pi^2*b^2*sgn(f)/f - 1/12*pi*b^2*log(abs(f))*
sgn(f)/f + 1/24*I*pi^2*b^2/f + 1/12*pi*b^2*log(abs(f))/f - 1/12*I*b^2*log(a
bs(f))^2/f - 1/2*I*pi*a*sgn(f) + 1/4*I*pi*b*e*sgn(f)/f + 1/2*I*pi*a - 1/4*I
*pi*b*e/f + a*log(abs(f)) - 1/2*b*e*log(abs(f))/f - 3*I*d + 3/4*I*e^2/f)/(s
qrt(f)*(I*f/abs(f) + 1)) - 3/16*I*sqrt(2)*sqrt(pi)*erf(-1/8*sqrt(2)*(4*x +
(pi*b*sgn(f) - pi*b + 2*I*b*log(abs(f)) + 2*e)/f)*(I*f/abs(f) + 1)*sqrt(abs
(f)))*e^(-1/8*I*pi^2*b^2*sgn(f)/f - 1/4*pi*b^2*log(abs(f))*sgn(f)/f + 1/8*I
*pi^2*b^2/f + 1/4*pi*b^2*log(abs(f))/f - 1/4*I*b^2*log(abs(f))^2/f - 1/2*I*
pi*a*sgn(f) + 1/4*I*pi*b*e*sgn(f)/f + 1/2*I*pi*a - 1/4*I*pi*b*e/f + a*log(a
bs(f)) - 1/2*b*e*log(abs(f))/f - I*d + 1/4*I*e^2/f)/((I*f/abs(f) + 1)*sqrt(
abs(f)))
```

maple [A] time = 1.10, size = 311, normalized size = 0.91

$$\frac{i\sqrt{\pi} f^a e^{\frac{i(-9e^2+6i\ln(f)be+\ln(f)^2b^2+36df)}{12f}} \operatorname{erf}\left(-\sqrt{-3if} x + \frac{3ie+b\ln(f)}{2\sqrt{-3if}}\right)}{16\sqrt{-3if}} + \frac{i\sqrt{\pi} f^a e^{\frac{i(-9e^2-6i\ln(f)be+\ln(f)^2b^2+36df)}{12f}} \sqrt{3} \operatorname{erf}\left(-\sqrt{3} \sqrt{i} x + \frac{3ie-b\ln(f)}{2\sqrt{3if}}\right)}{48\sqrt{if}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(f^(b*x+a)*sin(f*x^2+e*x+d)^3,x)

```
[Out] -1/16*I*Pi^(1/2)*f^a*exp(1/12*I*(-9*e^2+6*I*ln(f)*b*e+ln(f)^2*b^2+36*d*f)/f
)/(-3*I*f)^(1/2)*erf(-(-3*I*f)^(1/2)*x+1/2*(3*I*e+b*ln(f))/(-3*I*f)^(1/2))+
1/48*I*Pi^(1/2)*f^a*exp(-1/12*I*(-9*e^2-6*I*ln(f)*b*e+ln(f)^2*b^2+36*d*f)/f
)*3^(1/2)/(I*f)^(1/2)*erf(-3^(1/2)*(I*f)^(1/2)*x+1/6*(b*ln(f)-3*I*e)*3^(1/2
```

$$\frac{1}{(I*f)^{(1/2)}} - \frac{3}{16} * I * \pi^{(1/2)} * f^a * \exp(-1/4 * I * (-e^2 - 2 * I * \ln(f) * b * e + \ln(f)^2 * b^2 + 4 * d * f) / f) / (I*f)^{(1/2)} * \operatorname{erf}(-I*f)^{(1/2)} * x + 1/2 * (-I*e + b*\ln(f)) / (I*f)^{(1/2)} + \frac{3}{16} * I * \pi^{(1/2)} * f^a * \exp(1/4 * I * (-e^2 + 2 * I * \ln(f) * b * e + \ln(f)^2 * b^2 + 4 * d * f) / f) / (-I*f)^{(1/2)} * \operatorname{erf}(-I*f)^{(1/2)} * x + 1/2 * (I*e + b*\ln(f)) / (-I*f)^{(1/2)}$$

maxima [A] time = 0.49, size = 377, normalized size = 1.11

$$3 \cdot 9^{\frac{1}{4}} \sqrt{2} \sqrt{\pi} \left((i+1) f^a \cos\left(\frac{b^2 \log(f)^2 - 9e^2 + 36df}{12f}\right) - (i-1) f^a \sin\left(\frac{b^2 \log(f)^2 - 9e^2 + 36df}{12f}\right) \right) \operatorname{erf}\left(\frac{i(6ifx - b \log(f) + 3ie)\sqrt{3i}}{6f}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(b*x+a)*sin(f*x^2+e*x+d)^3,x, algorithm="maxima")

[Out] $\frac{1}{288} * (3 * 9^{(1/4)} * \sqrt{2} * \sqrt{\pi}) * (((I + 1) * f^a * \cos(1/12 * (b^2 * \log(f)^2 - 9 * e^2 + 36 * d * f) / f) - (I - 1) * f^a * \sin(1/12 * (b^2 * \log(f)^2 - 9 * e^2 + 36 * d * f) / f)) * \operatorname{erf}(1/6 * I * (6 * I * f * x - b * \log(f) + 3 * I * e) * \sqrt{3 * I * f} / f) + (- (I - 1) * f^a * \cos(1/12 * (b^2 * \log(f)^2 - 9 * e^2 + 36 * d * f) / f) + (I + 1) * f^a * \sin(1/12 * (b^2 * \log(f)^2 - 9 * e^2 + 36 * d * f) / f)) * \operatorname{erf}(1/6 * I * (6 * I * f * x + b * \log(f) + 3 * I * e) * \sqrt{-3 * I * f} / f)) * f^{(3/2)} + \sqrt{2} * \sqrt{\pi} * ((- (27 * I + 27) * f^a * \cos(1/4 * (b^2 * \log(f)^2 - e^2 + 4 * d * f) / f) + (27 * I - 27) * f^a * \sin(1/4 * (b^2 * \log(f)^2 - e^2 + 4 * d * f) / f)) * \operatorname{erf}(1/2 * I * (2 * I * f * x - b * \log(f) + I * e) * \sqrt{I * f} / f) + ((27 * I - 27) * f^a * \cos(1/4 * (b^2 * \log(f)^2 - e^2 + 4 * d * f) / f) - (27 * I + 27) * f^a * \sin(1/4 * (b^2 * \log(f)^2 - e^2 + 4 * d * f) / f)) * \operatorname{erf}(1/2 * I * (2 * I * f * x + b * \log(f) + I * e) * \sqrt{-I * f} / f)) * f^{(3/2)}) / (f^2 * f^{(1/2 * b * e / f)})$

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int f^{a+bx} \sin(fx^2 + ex + d)^3 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(f^(a + b*x)*sin(d + e*x + f*x^2)^3,x)

[Out] int(f^(a + b*x)*sin(d + e*x + f*x^2)^3, x)

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f**(b*x+a)*sin(f*x**2+e*x+d)**3,x)

[Out] Timed out

3.85 $\int f^{a+cx^2} \sin(d + ex) dx$

Optimal. Leaf size=151

$$\frac{i\sqrt{\pi} f^a e^{\frac{e^2}{4c \log(f)} - id} \operatorname{erfi}\left(\frac{-2cx \log(f) + ie}{2\sqrt{c} \sqrt{\log(f)}}\right)}{4\sqrt{c} \sqrt{\log(f)}} - \frac{i\sqrt{\pi} f^a e^{\frac{e^2}{4c \log(f)} + id} \operatorname{erfi}\left(\frac{2cx \log(f) + ie}{2\sqrt{c} \sqrt{\log(f)}}\right)}{4\sqrt{c} \sqrt{\log(f)}}$$

[Out] $\frac{1}{4} I \exp(-I d + 1/4 e^2/c/\ln(f)) f^a \operatorname{erfi}(1/2 * (-I e + 2 * c * x * \ln(f))/c^{1/2}/\ln(f)^{1/2}) * \pi^{1/2}/c^{1/2}/\ln(f)^{1/2} - \frac{1}{4} I \exp(I d + 1/4 e^2/c/\ln(f)) f^a \operatorname{erfi}(1/2 * (I e + 2 * c * x * \ln(f))/c^{1/2}/\ln(f)^{1/2}) * \pi^{1/2}/c^{1/2}/\ln(f)^{1/2}$

Rubi [A] time = 0.21, antiderivative size = 151, normalized size of antiderivative = 1.00, number of steps used = 8, number of rules used = 4, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} = 0.250$, Rules used = {4472, 2287, 2234, 2204}

$$\frac{i\sqrt{\pi} f^a e^{\frac{e^2}{4c \log(f)} - id} \operatorname{Erfi}\left(\frac{-2cx \log(f) + ie}{2\sqrt{c} \sqrt{\log(f)}}\right)}{4\sqrt{c} \sqrt{\log(f)}} - \frac{i\sqrt{\pi} f^a e^{\frac{e^2}{4c \log(f)} + id} \operatorname{Erfi}\left(\frac{2cx \log(f) + ie}{2\sqrt{c} \sqrt{\log(f)}}\right)}{4\sqrt{c} \sqrt{\log(f)}}$$

Antiderivative was successfully verified.

[In] Int[f^(a + c*x^2)*Sin[d + e*x],x]

[Out] $((-I/4) * E^{((-I) * d + e^2/(4 * c * \operatorname{Log}[f]))} * f^a * \operatorname{Sqrt}[\pi] * \operatorname{Erfi}[(I * e - 2 * c * x * \operatorname{Log}[f]) / (2 * \operatorname{Sqrt}[c] * \operatorname{Sqrt}[\operatorname{Log}[f]])]) / (\operatorname{Sqrt}[c] * \operatorname{Sqrt}[\operatorname{Log}[f]]) - ((I/4) * E^{(I * d + e^2/(4 * c * \operatorname{Log}[f]))} * f^a * \operatorname{Sqrt}[\pi] * \operatorname{Erfi}[(I * e + 2 * c * x * \operatorname{Log}[f]) / (2 * \operatorname{Sqrt}[c] * \operatorname{Sqrt}[\operatorname{Log}[f]])]) / (\operatorname{Sqrt}[c] * \operatorname{Sqrt}[\operatorname{Log}[f]])$

Rule 2204

Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_)^2), x_Symbol] := Simp[(F^a * Sqrt[Pi] * Erfi[(c + d*x) * Rt[b*Log[F], 2]]) / (2*d*Rt[b*Log[F], 2]), x] /; FreeQ[{F, a, b, c, d}, x] && PosQ[b]

Rule 2234

Int[(F_)^((a_.) + (b_.)*(x_) + (c_.)*(x_)^2), x_Symbol] := Dist[F^(a - b^2/(4*c)), Int[F^((b + 2*c*x)^2/(4*c)), x], x] /; FreeQ[{F, a, b, c}, x]

Rule 2287

Int[(u_.)*(F_)^(v_.)*(G_)^(w_.), x_Symbol] := With[{z = v*Log[F] + w*Log[G]}, Int[u*NormalizeIntegrand[E^z, x], x] /; BinomialQ[z, x] || (PolynomialQ[z, x] && LeQ[Exponent[z, x], 2])] /; FreeQ[{F, G}, x]

Rule 4472

Int[(F_)^(u_.)*Sin[v_]^(n_.), x_Symbol] := Int[ExpandTrigToExp[F^u, Sin[v]^n, x], x] /; FreeQ[F, x] && (LinearQ[u, x] || PolyQ[u, x, 2]) && (LinearQ[v, x] || PolyQ[v, x, 2]) && IGtQ[n, 0]

Rubi steps

$$\begin{aligned}
\int f^{a+cx^2} \sin(d+ex) dx &= \int \left(\frac{1}{2} i e^{-id-ieux} f^{a+cx^2} - \frac{1}{2} i e^{id+ieux} f^{a+cx^2} \right) dx \\
&= \frac{1}{2} i \int e^{-id-ieux} f^{a+cx^2} dx - \frac{1}{2} i \int e^{id+ieux} f^{a+cx^2} dx \\
&= \frac{1}{2} i \int e^{-id-ieux+a \log(f)+cx^2 \log(f)} dx - \frac{1}{2} i \int e^{id+ieux+a \log(f)+cx^2 \log(f)} dx \\
&= \frac{1}{2} \left(i e^{-id+\frac{e^2}{4c \log(f)}} f^a \right) \int e^{\frac{(-ie+2cx \log(f))^2}{4c \log(f)}} dx - \frac{1}{2} \left(i e^{id+\frac{e^2}{4c \log(f)}} f^a \right) \int e^{\frac{(ie+2cx \log(f))^2}{4c \log(f)}} dx \\
&= \frac{i e^{-id+\frac{e^2}{4c \log(f)}} f^a \sqrt{\pi} \operatorname{erfi} \left(\frac{ie-2cx \log(f)}{2\sqrt{c} \sqrt{\log(f)}} \right)}{4\sqrt{c} \sqrt{\log(f)}} - \frac{i e^{id+\frac{e^2}{4c \log(f)}} f^a \sqrt{\pi} \operatorname{erfi} \left(\frac{ie+2cx \log(f)}{2\sqrt{c} \sqrt{\log(f)}} \right)}{4\sqrt{c} \sqrt{\log(f)}}
\end{aligned}$$

Mathematica [A] time = 0.15, size = 119, normalized size = 0.79

$$\frac{\sqrt{\pi} f^a e^{\frac{e^2}{4c \log(f)}} \left(i(\cos(d) + i \sin(d)) \operatorname{erfi} \left(\frac{-2cx \log(f) - ie}{2\sqrt{c} \sqrt{\log(f)}} \right) + (\sin(d) + i \cos(d)) \operatorname{erfi} \left(\frac{2cx \log(f) - ie}{2\sqrt{c} \sqrt{\log(f)}} \right) \right)}{4\sqrt{c} \sqrt{\log(f)}}$$

Antiderivative was successfully verified.

[In] Integrate[f^(a + c*x^2)*Sin[d + e*x], x]

[Out] (E^(e^2/(4*c*Log[f]))*f^a*Sqrt[Pi]*(I*Erfi[((-I)*e - 2*c*x*Log[f])/(2*Sqrt[c]*Sqrt[Log[f]])]*(Cos[d] + I*Sin[d]) + Erfi[((-I)*e + 2*c*x*Log[f])/(2*Sqrt[c]*Sqrt[Log[f]])]*(I*Cos[d] + Sin[d])))/(4*Sqrt[c]*Sqrt[Log[f]])

fricas [A] time = 0.94, size = 144, normalized size = 0.95

$$\frac{i \sqrt{\pi} \sqrt{-c \log(f)} \operatorname{erf} \left(\frac{(2cx \log(f) + ie) \sqrt{-c \log(f)}}{2c \log(f)} \right) e^{\left(\frac{4ac \log(f)^2 + 4icd \log(f) + e^2}{4c \log(f)} \right)} - i \sqrt{\pi} \sqrt{-c \log(f)} \operatorname{erf} \left(\frac{(2cx \log(f) - ie) \sqrt{-c \log(f)}}{2c \log(f)} \right)}{4c \log(f)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(c*x^2+a)*sin(e*x+d), x, algorithm="fricas")

[Out] 1/4*(I*sqrt(pi)*sqrt(-c*log(f))*erf(1/2*(2*c*x*log(f) + I*e)*sqrt(-c*log(f))/(c*log(f)))*e^(1/4*(4*a*c*log(f)^2 + 4*I*c*d*log(f) + e^2)/(c*log(f))) - I*sqrt(pi)*sqrt(-c*log(f))*erf(1/2*(2*c*x*log(f) - I*e)*sqrt(-c*log(f))/(c*log(f)))*e^(1/4*(4*a*c*log(f)^2 - 4*I*c*d*log(f) + e^2)/(c*log(f))))/(c*log(f))

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int f^{cx^2+a} \sin(ex+d) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(c*x^2+a)*sin(e*x+d), x, algorithm="giac")

[Out] integrate(f^(c*x^2 + a)*sin(e*x + d), x)

maple [A] time = 0.42, size = 123, normalized size = 0.81

$$\frac{i \sqrt{\pi} f^a e^{\frac{4id \ln(f)c + e^2}{4 \ln(f)c}} \operatorname{erf} \left(-\sqrt{-c \ln(f)} x + \frac{ie}{2\sqrt{-c \ln(f)}} \right)}{4\sqrt{-c \ln(f)}} + \frac{i \sqrt{\pi} f^a e^{-\frac{4id \ln(f)c - e^2}{4 \ln(f)c}} \operatorname{erf} \left(\sqrt{-c \ln(f)} x + \frac{ie}{2\sqrt{-c \ln(f)}} \right)}{4\sqrt{-c \ln(f)}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(f^(c*x^2+a)*sin(e*x+d),x)`

[Out] $\frac{1}{4}i\pi^{1/2}f^a\exp\left(\frac{1}{4}(4Id\ln(f)+c+e^2)/\ln(f)/c\right)/(-c\ln(f))^{1/2}\operatorname{erf}\left(\frac{-(-c\ln(f))^{1/2}x+1/2Ie}{(-c\ln(f))^{1/2}}\right)+\frac{1}{4}i\pi^{1/2}f^a\exp\left(\frac{-1}{4}(4Id\ln(f)+c-e^2)/\ln(f)/c\right)/(-c\ln(f))^{1/2}\operatorname{erf}\left(\frac{(-c\ln(f))^{1/2}x+1/2Ie}{(-c\ln(f))^{1/2}}\right)$

maxima [C] time = 0.36, size = 206, normalized size = 1.36

$$\sqrt{\pi}\left(f^a(i\cos(d)+\sin(d))\operatorname{erf}\left(x\sqrt{-c\log(f)}+\frac{1}{2}ie^{\frac{1}{\sqrt{-c\log(f)}}}\right)e^{\left(\frac{e^2}{4c\log(f)}\right)}+f^a(-i\cos(d)+\sin(d))\operatorname{erf}\left(x\sqrt{-c\log(f)}\right)\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(f^(c*x^2+a)*sin(e*x+d),x, algorithm="maxima")`

[Out] $-\frac{1}{8}\sqrt{\pi}(f^a(I\cos(d)+\sin(d))\operatorname{erf}(x\operatorname{conjugate}(\sqrt{-c\log(f)}))+\frac{1}{2}Ie\operatorname{conjugate}(1/\sqrt{-c\log(f)}))e^{1/4e^2/(c\log(f))}+f^a(-I\cos(d)+\sin(d))\operatorname{erf}(x\operatorname{conjugate}(\sqrt{-c\log(f)}))-\frac{1}{2}Ie\operatorname{conjugate}(1/\sqrt{-c\log(f)}))e^{1/4e^2/(c\log(f))}+f^a(I\cos(d)-\sin(d))\operatorname{erf}(1/2(2cx\log(f)+Ie)/\sqrt{-c\log(f)})e^{1/4e^2/(c\log(f))}+f^a(-I\cos(d)-\sin(d))\operatorname{erf}(1/2(2cx\log(f)-Ie)/\sqrt{-c\log(f)})e^{1/4e^2/(c\log(f))})\sqrt{-c\log(f)}/(c\log(f))$

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int f^{cx^2+a} \sin(d+ex) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(f^(a+c*x^2)*sin(d+e*x),x)`

[Out] `int(f^(a+c*x^2)*sin(d+e*x), x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int f^{a+cx^2} \sin(d+ex) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(f**(c*x**2+a)*sin(e*x+d),x)`

[Out] `Integral(f**(a+c*x**2)*sin(d+e*x), x)`

3.86 $\int f^{a+cx^2} \sin^2(d+ex) dx$

Optimal. Leaf size=171

$$\frac{\sqrt{\pi} f^a e^{\frac{e^2}{c \log(f)} - 2id} \operatorname{erfi}\left(\frac{-cx \log(f) + ie}{\sqrt{c} \sqrt{\log(f)}}\right)}{8\sqrt{c} \sqrt{\log(f)}} - \frac{\sqrt{\pi} f^a e^{\frac{e^2}{c \log(f)} + 2id} \operatorname{erfi}\left(\frac{cx \log(f) + ie}{\sqrt{c} \sqrt{\log(f)}}\right)}{8\sqrt{c} \sqrt{\log(f)}} + \frac{\sqrt{\pi} f^a \operatorname{erfi}\left(\sqrt{c} x \sqrt{\log(f)}\right)}{4\sqrt{c} \sqrt{\log(f)}}$$

[Out] $-1/8 \exp(-2I*d + e^2/c/\ln(f)) f^a \operatorname{erfi}((-I*e + c*x*\ln(f))/c^{(1/2)}/\ln(f)^{(1/2)}) * \pi^{(1/2)}/c^{(1/2)}/\ln(f)^{(1/2)} - 1/8 \exp(2I*d + e^2/c/\ln(f)) f^a \operatorname{erfi}((I*e + c*x*\ln(f))/c^{(1/2)}/\ln(f)^{(1/2)}) * \pi^{(1/2)}/c^{(1/2)}/\ln(f)^{(1/2)} + 1/4 f^a \operatorname{erfi}(x*c^{(1/2)*\ln(f)^{(1/2)}) * \pi^{(1/2)}/c^{(1/2)}/\ln(f)^{(1/2)}$

Rubi [A] time = 0.22, antiderivative size = 171, normalized size of antiderivative = 1.00, number of steps used = 9, number of rules used = 4, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.222$, Rules used = {4472, 2204, 2287, 2234}

$$\frac{\sqrt{\pi} f^a e^{\frac{e^2}{c \log(f)} - 2id} \operatorname{Erfi}\left(\frac{-cx \log(f) + ie}{\sqrt{c} \sqrt{\log(f)}}\right)}{8\sqrt{c} \sqrt{\log(f)}} - \frac{\sqrt{\pi} f^a e^{\frac{e^2}{c \log(f)} + 2id} \operatorname{Erfi}\left(\frac{cx \log(f) + ie}{\sqrt{c} \sqrt{\log(f)}}\right)}{8\sqrt{c} \sqrt{\log(f)}} + \frac{\sqrt{\pi} f^a \operatorname{Erfi}\left(\sqrt{c} x \sqrt{\log(f)}\right)}{4\sqrt{c} \sqrt{\log(f)}}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[f^{(a + c*x^2)} * \operatorname{Sin}[d + e*x]^2, x]$

[Out] $(f^a * \operatorname{Sqrt}[\pi] * \operatorname{Erfi}[\operatorname{Sqrt}[c] * x * \operatorname{Sqrt}[\operatorname{Log}[f]]]) / (4 * \operatorname{Sqrt}[c] * \operatorname{Sqrt}[\operatorname{Log}[f]]) + (E^{(-2*I)*d + e^2/(c*\operatorname{Log}[f])} * f^a * \operatorname{Sqrt}[\pi] * \operatorname{Erfi}[(I*e - c*x*\operatorname{Log}[f]) / (\operatorname{Sqrt}[c] * \operatorname{Sqrt}[\operatorname{Log}[f]])]) / (8 * \operatorname{Sqrt}[c] * \operatorname{Sqrt}[\operatorname{Log}[f]]) - (E^{((2*I)*d + e^2/(c*\operatorname{Log}[f])} * f^a * \operatorname{Sqrt}[\pi] * \operatorname{Erfi}[(I*e + c*x*\operatorname{Log}[f]) / (\operatorname{Sqrt}[c] * \operatorname{Sqrt}[\operatorname{Log}[f]])]) / (8 * \operatorname{Sqrt}[c] * \operatorname{Sqrt}[\operatorname{Log}[f]])$

Rule 2204

$\operatorname{Int}[(F_)^{((a_.) + (b_.)*((c_.) + (d_.)*(x_)) ^2)}, x_Symbol] := \operatorname{Simp}[(F^a * \operatorname{Sqrt}[\pi] * \operatorname{Erfi}[(c + d*x) * \operatorname{Rt}[b * \operatorname{Log}[F], 2]]) / (2*d * \operatorname{Rt}[b * \operatorname{Log}[F], 2]), x] /; \operatorname{FreeQ}\{F, a, b, c, d\}, x] \&\& \operatorname{PosQ}[b]$

Rule 2234

$\operatorname{Int}[(F_)^{((a_.) + (b_.)*(x_) + (c_.)*(x_) ^2)}, x_Symbol] := \operatorname{Dist}[F^{(a - b^2/(4*c))}, \operatorname{Int}[F^{((b + 2*c*x) ^2/(4*c))}, x], x] /; \operatorname{FreeQ}\{F, a, b, c\}, x]$

Rule 2287

$\operatorname{Int}[(u_)*(F_)^{(v_)}*(G_)^{(w_)}, x_Symbol] := \operatorname{With}\{z = v * \operatorname{Log}[F] + w * \operatorname{Log}[G]\}, \operatorname{Int}[u * \operatorname{NormalizeIntegrand}[E^z, x], x] /; \operatorname{BinomialQ}[z, x] || (\operatorname{PolynomialQ}[z, x] \&\& \operatorname{LeQ}[\operatorname{Exponent}[z, x], 2]) /; \operatorname{FreeQ}\{F, G\}, x]$

Rule 4472

$\operatorname{Int}[(F_)^{(u_)} * \operatorname{Sin}[v_]^{(n_.)}, x_Symbol] := \operatorname{Int}[\operatorname{ExpandTrigToExp}[F^u, \operatorname{Sin}[v]^n], x] /; \operatorname{FreeQ}[F, x] \&\& (\operatorname{LinearQ}[u, x] || \operatorname{PolyQ}[u, x, 2]) \&\& (\operatorname{LinearQ}[v, x] || \operatorname{PolyQ}[v, x, 2]) \&\& \operatorname{IGtQ}[n, 0]$

Rubi steps

$$\begin{aligned}
\int f^{a+cx^2} \sin^2(d+ex) dx &= \int \left(\frac{1}{2} f^{a+cx^2} - \frac{1}{4} e^{-2id-2iex} f^{a+cx^2} - \frac{1}{4} e^{2id+2iex} f^{a+cx^2} \right) dx \\
&= -\left(\frac{1}{4} \int e^{-2id-2iex} f^{a+cx^2} dx \right) - \frac{1}{4} \int e^{2id+2iex} f^{a+cx^2} dx + \frac{1}{2} \int f^{a+cx^2} dx \\
&= \frac{f^a \sqrt{\pi} \operatorname{erfi}(\sqrt{c} x \sqrt{\log(f)})}{4\sqrt{c} \sqrt{\log(f)}} - \frac{1}{4} \int e^{-2id-2iex+a \log(f)+cx^2 \log(f)} dx - \frac{1}{4} \int e^{2id+2iex+a \log(f)+cx^2 \log(f)} dx \\
&= \frac{f^a \sqrt{\pi} \operatorname{erfi}(\sqrt{c} x \sqrt{\log(f)})}{4\sqrt{c} \sqrt{\log(f)}} - \frac{1}{4} \left(e^{-2id+\frac{e^2}{c \log(f)}} f^a \right) \int e^{\frac{(-2ie+2cx \log(f))^2}{4c \log(f)}} dx - \frac{1}{4} \left(e^{2id+\frac{e^2}{c \log(f)}} f^a \right) \int e^{\frac{(2ie+2cx \log(f))^2}{4c \log(f)}} dx \\
&= \frac{f^a \sqrt{\pi} \operatorname{erfi}(\sqrt{c} x \sqrt{\log(f)})}{4\sqrt{c} \sqrt{\log(f)}} + \frac{e^{-2id+\frac{e^2}{c \log(f)}} f^a \sqrt{\pi} \operatorname{erfi}\left(\frac{ie-cx \log(f)}{\sqrt{c} \sqrt{\log(f)}}\right)}{8\sqrt{c} \sqrt{\log(f)}} - \frac{e^{2id+\frac{e^2}{c \log(f)}} f^a \sqrt{\pi} \operatorname{erfi}\left(\frac{-ie+cx \log(f)}{\sqrt{c} \sqrt{\log(f)}}\right)}{8\sqrt{c} \sqrt{\log(f)}}
\end{aligned}$$

Mathematica [A] time = 0.25, size = 132, normalized size = 0.77

$$\frac{\sqrt{\pi} f^a \left(2 \operatorname{erfi}(\sqrt{c} x \sqrt{\log(f)}) - e^{\frac{e^2}{c \log(f)}} \left((\cos(2d) - i \sin(2d)) \operatorname{erfi}\left(\frac{cx \log(f) - ie}{\sqrt{c} \sqrt{\log(f)}}\right) + (\cos(2d) + i \sin(2d)) \operatorname{erfi}\left(\frac{cx \log(f) + ie}{\sqrt{c} \sqrt{\log(f)}}\right) \right) \right)}{8\sqrt{c} \sqrt{\log(f)}}$$

Antiderivative was successfully verified.

[In] Integrate[f^(a + c*x^2)*Sin[d + e*x]^2,x]

[Out] (f^a*Sqrt[Pi]*(2*Erfi[Sqrt[c]*x*Sqrt[Log[f]]] - E^(e^2/(c*Log[f]))*(Erfi[(((-I)*e + c*x*Log[f])/(Sqrt[c]*Sqrt[Log[f]])]*(Cos[2*d] - I*Sin[2*d]) + Erfi[(I*e + c*x*Log[f])/(Sqrt[c]*Sqrt[Log[f]])]*(Cos[2*d] + I*Sin[2*d])))]/(8*Sqrt[c]*Sqrt[Log[f]]))

fricas [A] time = 0.48, size = 161, normalized size = 0.94

$$\frac{2 \sqrt{\pi} \sqrt{-c \log(f)} f^a \operatorname{erf}(\sqrt{-c \log(f)} x) - \sqrt{\pi} \sqrt{-c \log(f)} \operatorname{erf}\left(\frac{(cx \log(f) + ie) \sqrt{-c \log(f)}}{c \log(f)}\right) e^{\left(\frac{ac \log(f)^2 + 2icd \log(f) + e^2}{c \log(f)}\right)} - \sqrt{\pi} \sqrt{-c \log(f)} \operatorname{erf}\left(\frac{(cx \log(f) - ie) \sqrt{-c \log(f)}}{c \log(f)}\right) e^{\left(\frac{ac \log(f)^2 - 2icd \log(f) + e^2}{c \log(f)}\right)}}{8c \log(f)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(c*x^2+a)*sin(e*x+d)^2,x, algorithm="fricas")

[Out] -1/8*(2*sqrt(pi)*sqrt(-c*log(f))*f^a*erf(sqrt(-c*log(f))*x) - sqrt(pi)*sqrt(-c*log(f))*erf(((c*x*log(f) + I*e)*sqrt(-c*log(f))/(c*log(f)))*e^((a*c*log(f)^2 + 2*I*c*d*log(f) + e^2)/(c*log(f))) - sqrt(pi)*sqrt(-c*log(f))*erf(((c*x*log(f) - I*e)*sqrt(-c*log(f))/(c*log(f)))*e^((a*c*log(f)^2 - 2*I*c*d*log(f) + e^2)/(c*log(f))))/(c*log(f))

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int f^{cx^2+a} \sin(ex+d)^2 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(c*x^2+a)*sin(e*x+d)^2,x, algorithm="giac")

[Out] integrate(f^(c*x^2 + a)*sin(e*x + d)^2, x)

maple [A] time = 0.42, size = 145, normalized size = 0.85

$$\frac{\sqrt{\pi} f^a e^{-\frac{2id \ln(f)c - e^2}{\ln(f)c}} \operatorname{erf}\left(\sqrt{-c \ln(f)} x + \frac{ie}{\sqrt{-c \ln(f)}}\right)}{8\sqrt{-c \ln(f)}} + \frac{\sqrt{\pi} f^a e^{\frac{2id \ln(f)c + e^2}{\ln(f)c}} \operatorname{erf}\left(-\sqrt{-c \ln(f)} x + \frac{ie}{\sqrt{-c \ln(f)}}\right)}{8\sqrt{-c \ln(f)}} + \frac{f^a \sqrt{\pi} \operatorname{erf}\left(\sqrt{-c \ln(f)} x\right)}{4\sqrt{-c \ln(f)}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(f^(c*x^2+a)*sin(e*x+d)^2,x)

[Out] $-1/8*\pi^{(1/2)}*f^a*\exp(-(2*I*d*\ln(f)*c-e^2)/\ln(f)/c)/(-c*\ln(f))^{(1/2)}*\operatorname{erf}((-c*\ln(f))^{(1/2)}*x+I*e/(-c*\ln(f))^{(1/2)})+1/8*\pi^{(1/2)}*f^a*\exp((2*I*d*\ln(f)*c+e^2)/\ln(f)/c)/(-c*\ln(f))^{(1/2)}*\operatorname{erf}(-(-c*\ln(f))^{(1/2)}*x+I*e/(-c*\ln(f))^{(1/2)})+1/4*f^a*\pi^{(1/2)}/(-c*\ln(f))^{(1/2)}*\operatorname{erf}((-c*\ln(f))^{(1/2)}*x)$

maxima [C] time = 0.38, size = 236, normalized size = 1.38

$$\sqrt{\pi} \left(f^a (\cos(2d) - i \sin(2d)) \operatorname{erf}\left(x \sqrt{-c \log(f)} + i e \frac{1}{\sqrt{-c \log(f)}}\right) e^{\left(\frac{e^2}{c \log(f)}\right)} + f^a (\cos(2d) + i \sin(2d)) \operatorname{erf}\left(x \sqrt{-c \log(f)} - i e \frac{1}{\sqrt{-c \log(f)}}\right) e^{\left(\frac{e^2}{c \log(f)}\right)} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(c*x^2+a)*sin(e*x+d)^2,x, algorithm="maxima")

[Out] $-1/16*\sqrt{\pi}*(f^a*(\cos(2*d) - I*\sin(2*d))*\operatorname{erf}(x*\operatorname{conjugate}(\sqrt{-c*\log(f)}) + I*e*\operatorname{conjugate}(1/\sqrt{-c*\log(f)})))*e^{(e^2/(c*\log(f)))} + f^a*(\cos(2*d) + I*\sin(2*d))*\operatorname{erf}(x*\operatorname{conjugate}(\sqrt{-c*\log(f)}) - I*e*\operatorname{conjugate}(1/\sqrt{-c*\log(f)})))*e^{(e^2/(c*\log(f)))} - f^a*(\cos(2*d) - I*\sin(2*d))*\operatorname{erf}((c*x*\log(f) + I*e)/\sqrt{-c*\log(f)})*e^{(e^2/(c*\log(f)))} - f^a*(\cos(2*d) + I*\sin(2*d))*\operatorname{erf}((c*x*\log(f) - I*e)/\sqrt{-c*\log(f)})*e^{(e^2/(c*\log(f)))} - 2*f^a*\operatorname{erf}(x*\operatorname{conjugate}(\sqrt{-c*\log(f)}) - I*e*\operatorname{conjugate}(1/\sqrt{-c*\log(f)})))/\sqrt{-c*\log(f)}$

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int f^{cx^2+a} \sin(d+ex)^2 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(f^(a + c*x^2)*sin(d + e*x)^2,x)

[Out] int(f^(a + c*x^2)*sin(d + e*x)^2, x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int f^{a+cx^2} \sin^2(d+ex) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f**(c*x**2+a)*sin(e*x+d)**2,x)

[Out] Integral(f**(a + c*x**2)*sin(d + e*x)**2, x)

3.87 $\int f^{a+cx^2} \sin^3(d+ex) dx$

Optimal. Leaf size=301

$$\frac{3i\sqrt{\pi} f^a e^{\frac{e^2}{4c \log(f)} - id} \operatorname{erfi}\left(\frac{-2cx \log(f) + ie}{2\sqrt{c} \sqrt{\log(f)}}\right)}{16\sqrt{c} \sqrt{\log(f)}} + \frac{i\sqrt{\pi} f^a e^{\frac{9e^2}{4c \log(f)} - 3id} \operatorname{erfi}\left(\frac{-2cx \log(f) + 3ie}{2\sqrt{c} \sqrt{\log(f)}}\right)}{16\sqrt{c} \sqrt{\log(f)}} - \frac{3i\sqrt{\pi} f^a e^{\frac{e^2}{4c \log(f)} + id} \operatorname{erfi}\left(\frac{2cx \log(f) + ie}{2\sqrt{c} \sqrt{\log(f)}}\right)}{16\sqrt{c} \sqrt{\log(f)}}$$

[Out] $3/16 * I * \exp(-I * d + 1/4 * e^2 / c / \ln(f)) * f^a * \operatorname{erfi}(1/2 * (-I * e + 2 * c * x * \ln(f)) / c^{(1/2)} / \ln(f)^{(1/2)}) * \pi^{(1/2)} / c^{(1/2)} / \ln(f)^{(1/2)} - 1/16 * I * \exp(-3 * I * d + 9/4 * e^2 / c / \ln(f)) * f^a * \operatorname{erfi}(1/2 * (-3 * I * e + 2 * c * x * \ln(f)) / c^{(1/2)} / \ln(f)^{(1/2)}) * \pi^{(1/2)} / c^{(1/2)} / \ln(f)^{(1/2)} - 3/16 * I * \exp(I * d + 1/4 * e^2 / c / \ln(f)) * f^a * \operatorname{erfi}(1/2 * (I * e + 2 * c * x * \ln(f)) / c^{(1/2)} / \ln(f)^{(1/2)}) * \pi^{(1/2)} / c^{(1/2)} / \ln(f)^{(1/2)} + 1/16 * I * \exp(3 * I * d + 9/4 * e^2 / c / \ln(f)) * f^a * \operatorname{erfi}(1/2 * (3 * I * e + 2 * c * x * \ln(f)) / c^{(1/2)} / \ln(f)^{(1/2)}) * \pi^{(1/2)} / c^{(1/2)} / \ln(f)^{(1/2)}$

Rubi [A] time = 0.35, antiderivative size = 301, normalized size of antiderivative = 1.00, number of steps used = 14, number of rules used = 4, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.222$, Rules used = {4472, 2287, 2234, 2204}

$$\frac{3i\sqrt{\pi} f^a e^{\frac{e^2}{4c \log(f)} - id} \operatorname{Erfi}\left(\frac{-2cx \log(f) + ie}{2\sqrt{c} \sqrt{\log(f)}}\right)}{16\sqrt{c} \sqrt{\log(f)}} + \frac{i\sqrt{\pi} f^a e^{\frac{9e^2}{4c \log(f)} - 3id} \operatorname{Erfi}\left(\frac{-2cx \log(f) + 3ie}{2\sqrt{c} \sqrt{\log(f)}}\right)}{16\sqrt{c} \sqrt{\log(f)}} - \frac{3i\sqrt{\pi} f^a e^{\frac{e^2}{4c \log(f)} + id} \operatorname{Erfi}\left(\frac{2cx \log(f) + ie}{2\sqrt{c} \sqrt{\log(f)}}\right)}{16\sqrt{c} \sqrt{\log(f)}}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[f^{(a + c*x^2)} * \operatorname{Sin}[d + e*x]^3, x]$

[Out] $(((-3*I)/16) * E^{((-I)*d + e^2/(4*c*Log[f]))} * f^a * \operatorname{Sqrt}[\pi] * \operatorname{Erfi}[(I*e - 2*c*x*Log[f]) / (2*\operatorname{Sqrt}[c] * \operatorname{Sqrt}[Log[f]])]) / (\operatorname{Sqrt}[c] * \operatorname{Sqrt}[Log[f]]) + ((I/16) * E^{((-3*I)*d + (9*e^2)/(4*c*Log[f]))} * f^a * \operatorname{Sqrt}[\pi] * \operatorname{Erfi}[(3*I)*e - 2*c*x*Log[f]) / (2*\operatorname{Sqrt}[c] * \operatorname{Sqrt}[Log[f]])]) / (\operatorname{Sqrt}[c] * \operatorname{Sqrt}[Log[f]]) - (((3*I)/16) * E^{(I*d + e^2/(4*c*Log[f]))} * f^a * \operatorname{Sqrt}[\pi] * \operatorname{Erfi}[(I*e + 2*c*x*Log[f]) / (2*\operatorname{Sqrt}[c] * \operatorname{Sqrt}[Log[f]])]) / (\operatorname{Sqrt}[c] * \operatorname{Sqrt}[Log[f]]) + ((I/16) * E^{((3*I)*d + (9*e^2)/(4*c*Log[f]))} * f^a * \operatorname{Sqrt}[\pi] * \operatorname{Erfi}[(3*I)*e + 2*c*x*Log[f]) / (2*\operatorname{Sqrt}[c] * \operatorname{Sqrt}[Log[f]])]) / (\operatorname{Sqrt}[c] * \operatorname{Sqrt}[Log[f]])$

Rule 2204

$\operatorname{Int}[(F_)^{((a_.) + (b_.) * ((c_.) + (d_.) * (x_.)^2))}, x_Symbol] := \operatorname{Simp}[(F^a * \operatorname{Sqrt}[\pi] * \operatorname{Erfi}[(c + d*x) * \operatorname{Rt}[b * \operatorname{Log}[F], 2]]) / (2*d * \operatorname{Rt}[b * \operatorname{Log}[F], 2]), x] /; \operatorname{FreeQ}\{F, a, b, c, d\}, x] \&\& \operatorname{PosQ}[b]$

Rule 2234

$\operatorname{Int}[(F_)^{((a_.) + (b_.) * (x_.) + (c_.) * (x_.)^2)}, x_Symbol] := \operatorname{Dist}[F^{(a - b^2 / (4*c))}, \operatorname{Int}[F^{((b + 2*c*x)^2 / (4*c))}, x], x] /; \operatorname{FreeQ}\{F, a, b, c\}, x]$

Rule 2287

$\operatorname{Int}[(u_.) * (F_)^{(v_.)} * (G_)^{(w_.)}, x_Symbol] := \operatorname{With}\{z = v * \operatorname{Log}[F] + w * \operatorname{Log}[G]\}, \operatorname{Int}[u * \operatorname{NormalizeIntegrand}[E^z, x], x] /; \operatorname{BinomialQ}[z, x] \|\| (\operatorname{PolynomialQ}[z, x] \&\& \operatorname{LeQ}[\operatorname{Exponent}[z, x], 2]) /; \operatorname{FreeQ}\{F, G\}, x]$

Rule 4472

$\operatorname{Int}[(F_)^{(u_.)} * \operatorname{Sin}[v_]^{(n_.)}, x_Symbol] := \operatorname{Int}[\operatorname{ExpandTrigToExp}[F^u, \operatorname{Sin}[v]^n], x] /; \operatorname{FreeQ}[F, x] \&\& (\operatorname{LinearQ}[u, x] \|\| \operatorname{PolyQ}[u, x, 2]) \&\& (\operatorname{LinearQ}[v, x] \|\| \operatorname{PolyQ}[v, x, 2]) \&\& \operatorname{IGtQ}[n, 0]$

Rubi steps

$$\begin{aligned}
\int f^{a+cx^2} \sin^3(d+ex) dx &= \int \left(\frac{3}{8} i e^{-id-ieux} f^{a+cx^2} - \frac{3}{8} i e^{id+iex} f^{a+cx^2} - \frac{1}{8} i e^{-3id-3iex} f^{a+cx^2} + \frac{1}{8} i e^{3id+3iex} f^{a+cx^2} \right) dx \\
&= -\left(\frac{1}{8} i \int e^{-3id-3iex} f^{a+cx^2} dx \right) + \frac{1}{8} i \int e^{3id+3iex} f^{a+cx^2} dx + \frac{3}{8} i \int e^{-id-ieux} f^{a+cx^2} dx - \frac{3}{8} i \int e^{id+iex} f^{a+cx^2} dx \\
&= -\left(\frac{1}{8} i \int e^{-3id-3iex+a \log(f)+cx^2 \log(f)} dx \right) + \frac{1}{8} i \int e^{3id+3iex+a \log(f)+cx^2 \log(f)} dx + \frac{3}{8} i \int e^{-id-ieux+a \log(f)+cx^2 \log(f)} dx - \frac{3}{8} i \int e^{id+iex+a \log(f)+cx^2 \log(f)} dx \\
&= \frac{1}{8} \left(3 i e^{-id+\frac{e^2}{4c \log(f)}} f^a \right) \int e^{\frac{(-ie+2cx \log(f))^2}{4c \log(f)}} dx - \frac{1}{8} \left(3 i e^{id+\frac{e^2}{4c \log(f)}} f^a \right) \int e^{\frac{(ie+2cx \log(f))^2}{4c \log(f)}} dx - \frac{1}{8} \left(3 i e^{-id+\frac{e^2}{4c \log(f)}} f^a \right) \int e^{\frac{(-ie-2cx \log(f))^2}{4c \log(f)}} dx + \frac{1}{8} \left(3 i e^{id+\frac{e^2}{4c \log(f)}} f^a \right) \int e^{\frac{(ie-2cx \log(f))^2}{4c \log(f)}} dx \\
&= -\frac{3 i e^{-id+\frac{e^2}{4c \log(f)}} f^a \sqrt{\pi} \operatorname{erfi}\left(\frac{ie-2cx \log(f)}{2\sqrt{c} \sqrt{\log(f)}}\right)}{16\sqrt{c} \sqrt{\log(f)}} + \frac{3 i e^{id+\frac{e^2}{4c \log(f)}} f^a \sqrt{\pi} \operatorname{erfi}\left(\frac{ie+2cx \log(f)}{2\sqrt{c} \sqrt{\log(f)}}\right)}{16\sqrt{c} \sqrt{\log(f)}} - \frac{3 i e^{-id+\frac{e^2}{4c \log(f)}} f^a \sqrt{\pi} \operatorname{erfi}\left(\frac{-ie-2cx \log(f)}{2\sqrt{c} \sqrt{\log(f)}}\right)}{16\sqrt{c} \sqrt{\log(f)}} + \frac{3 i e^{id+\frac{e^2}{4c \log(f)}} f^a \sqrt{\pi} \operatorname{erfi}\left(\frac{-ie+2cx \log(f)}{2\sqrt{c} \sqrt{\log(f)}}\right)}{16\sqrt{c} \sqrt{\log(f)}}
\end{aligned}$$

Mathematica [A] time = 0.42, size = 224, normalized size = 0.74

$$\frac{\sqrt{\pi} f^a e^{\frac{e^2}{4c \log(f)}} \left(-i e^{\frac{2e^2}{c \log(f)}} \left((\cos(3d) - i \sin(3d)) \operatorname{erfi}\left(\frac{2cx \log(f) - 3ie}{2\sqrt{c} \sqrt{\log(f)}}\right) - (\cos(3d) + i \sin(3d)) \operatorname{erfi}\left(\frac{2cx \log(f) + 3ie}{2\sqrt{c} \sqrt{\log(f)}}\right) \right) + 3i \operatorname{erfi}\left(\frac{2cx \log(f)}{2\sqrt{c} \sqrt{\log(f)}}\right) \right)}{16\sqrt{c} \sqrt{\log(f)}}$$

Antiderivative was successfully verified.

[In] Integrate[f^(a + c*x^2)*Sin[d + e*x]^3,x]

[Out] (E^(e^2/(4*c*Log[f]))*f^a*Sqrt[Pi]*((3*I)*Erfi[((-I)*e - 2*c*x*Log[f])/(2*Sqrt[c]*Sqrt[Log[f]])]*(Cos[d] + I*Sin[d]) + 3*Erfi[((-I)*e + 2*c*x*Log[f])/(2*Sqrt[c]*Sqrt[Log[f]])]*(I*Cos[d] + Sin[d]) - I*E^((2*e^2)/(c*Log[f]))*(Erfi[((-3*I)*e + 2*c*x*Log[f])/(2*Sqrt[c]*Sqrt[Log[f]])]*(Cos[3*d] - I*Sin[3*d]) - Erfi[((3*I)*e + 2*c*x*Log[f])/(2*Sqrt[c]*Sqrt[Log[f]])]*(Cos[3*d] + I*Sin[3*d]))))/16*Sqrt[c]*Sqrt[Log[f]])

fricas [A] time = 0.62, size = 282, normalized size = 0.94

$$-i \sqrt{\pi} \sqrt{-c \log(f)} \operatorname{erf}\left(\frac{(2cx \log(f) + 3ie) \sqrt{-c \log(f)}}{2c \log(f)}\right) e^{\left(\frac{4ac \log(f)^2 + 12icd \log(f) + 9e^2}{4c \log(f)}\right)} + 3i \sqrt{\pi} \sqrt{-c \log(f)} \operatorname{erf}\left(\frac{(2cx \log(f) - 3ie) \sqrt{-c \log(f)}}{2c \log(f)}\right) e^{\left(\frac{4ac \log(f)^2 - 12icd \log(f) + 9e^2}{4c \log(f)}\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(c*x^2+a)*sin(e*x+d)^3,x, algorithm="fricas")

[Out] 1/16*(-I*sqrt(pi)*sqrt(-c*log(f))*erf(1/2*(2*c*x*log(f) + 3*I*e)*sqrt(-c*log(f))/(c*log(f)))*e^(1/4*(4*a*c*log(f)^2 + 12*I*c*d*log(f) + 9*e^2)/(c*log(f))) + 3*I*sqrt(pi)*sqrt(-c*log(f))*erf(1/2*(2*c*x*log(f) + I*e)*sqrt(-c*log(f))/(c*log(f)))*e^(1/4*(4*a*c*log(f)^2 + 4*I*c*d*log(f) + e^2)/(c*log(f))) - 3*I*sqrt(pi)*sqrt(-c*log(f))*erf(1/2*(2*c*x*log(f) - I*e)*sqrt(-c*log(f))/(c*log(f)))*e^(1/4*(4*a*c*log(f)^2 - 4*I*c*d*log(f) + e^2)/(c*log(f))) + I*sqrt(pi)*sqrt(-c*log(f))*erf(1/2*(2*c*x*log(f) - 3*I*e)*sqrt(-c*log(f))/(c*log(f)))*e^(1/4*(4*a*c*log(f)^2 - 12*I*c*d*log(f) + 9*e^2)/(c*log(f))))/(c*log(f))

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int f^{cx^2+a} \sin(ex+d)^3 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(c*x^2+a)*sin(e*x+d)^3,x, algorithm="giac")

[Out] integrate(f^(c*x^2 + a)*sin(e*x + d)^3, x)

maple [A] time = 0.84, size = 246, normalized size = 0.82

$$\frac{i\sqrt{\pi} f^a e^{\frac{3id\ln(f)c + \frac{9e^2}{4}}{c\ln(f)}} \operatorname{erf}\left(-\sqrt{-c\ln(f)} x + \frac{3ie}{2\sqrt{-c\ln(f)}}\right)}{16\sqrt{-c\ln(f)}} - \frac{i\sqrt{\pi} f^a e^{\frac{3(4id\ln(f)c - 3e^2)}{4\ln(f)c}} \operatorname{erf}\left(\sqrt{-c\ln(f)} x + \frac{3ie}{2\sqrt{-c\ln(f)}}\right)}{16\sqrt{-c\ln(f)}} + \frac{3i\sqrt{\pi}}{16\sqrt{-c\ln(f)}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(f^(c*x^2+a)*sin(e*x+d)^3,x)

[Out] $-1/16 * I * \pi^{(1/2)} * f^a * \exp(3/4 * (4 * I * d * \ln(f) * c + 3 * e^2) / \ln(f) / c) / (-c * \ln(f))^{(1/2)} * \operatorname{erf}(-(-c * \ln(f))^{(1/2)} * x + 3/2 * I * e / (-c * \ln(f))^{(1/2)}) - 1/16 * I * \pi^{(1/2)} * f^a * \exp(-3/4 * (4 * I * d * \ln(f) * c - 3 * e^2) / \ln(f) / c) / (-c * \ln(f))^{(1/2)} * \operatorname{erf}((-c * \ln(f))^{(1/2)} * x + 3/2 * I * e / (-c * \ln(f))^{(1/2)}) + 3/16 * I * \pi^{(1/2)} * f^a * \exp(-1/4 * (4 * I * d * \ln(f) * c - e^2) / \ln(f) / c) / (-c * \ln(f))^{(1/2)} * \operatorname{erf}((-c * \ln(f))^{(1/2)} * x + 1/2 * I * e / (-c * \ln(f))^{(1/2)}) + 3/16 * I * \pi^{(1/2)} * f^a * \exp(1/4 * (4 * I * d * \ln(f) * c + e^2) / \ln(f) / c) / (-c * \ln(f))^{(1/2)} * \operatorname{erf}(-(-c * \ln(f))^{(1/2)} * x + 1/2 * I * e / (-c * \ln(f))^{(1/2)})$

maxima [C] time = 0.42, size = 412, normalized size = 1.37

$$\sqrt{\pi} \left(f^a (i \cos(3d) + \sin(3d)) \operatorname{erf}\left(x\sqrt{-c\log(f)} + \frac{3}{2} i e \frac{1}{\sqrt{-c\log(f)}}\right) e^{\left(\frac{9e^2}{4c\log(f)}\right)} + f^a (-i \cos(3d) + \sin(3d)) \operatorname{erf}\left(x\sqrt{-c\log(f)} - \frac{3}{2} i e \frac{1}{\sqrt{-c\log(f)}}\right) e^{\left(\frac{9e^2}{4c\log(f)}\right)} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(c*x^2+a)*sin(e*x+d)^3,x, algorithm="maxima")

[Out] $1/32 * \sqrt{\pi} * (f^a * (I * \cos(3 * d) + \sin(3 * d)) * \operatorname{erf}(x * \operatorname{conjugate}(\sqrt{-c * \log(f)})) + 3/2 * I * e * \operatorname{conjugate}(1 / \sqrt{-c * \log(f)})) * e^{(9/4 * e^2 / (c * \log(f)))} + f^a * (-I * \cos(3 * d) + \sin(3 * d)) * \operatorname{erf}(x * \operatorname{conjugate}(\sqrt{-c * \log(f)}) - 3/2 * I * e * \operatorname{conjugate}(1 / \sqrt{-c * \log(f)})) * e^{(9/4 * e^2 / (c * \log(f)))} + f^a * (I * \cos(3 * d) - \sin(3 * d)) * \operatorname{erf}(1/2 * (2 * c * x * \log(f) + 3 * I * e) / \sqrt{-c * \log(f)}) * e^{(9/4 * e^2 / (c * \log(f)))} + f^a * (-I * \cos(3 * d) - \sin(3 * d)) * \operatorname{erf}(1/2 * (2 * c * x * \log(f) - 3 * I * e) / \sqrt{-c * \log(f)}) * e^{(9/4 * e^2 / (c * \log(f)))} + f^a * (-3 * I * \cos(d) - 3 * \sin(d)) * \operatorname{erf}(x * \operatorname{conjugate}(\sqrt{-c * \log(f)}) + 1/2 * I * e * \operatorname{conjugate}(1 / \sqrt{-c * \log(f)})) * e^{(1/4 * e^2 / (c * \log(f)))} + f^a * (3 * I * \cos(d) - 3 * \sin(d)) * \operatorname{erf}(x * \operatorname{conjugate}(\sqrt{-c * \log(f)}) - 1/2 * I * e * \operatorname{conjugate}(1 / \sqrt{-c * \log(f)})) * e^{(1/4 * e^2 / (c * \log(f)))} + f^a * (-3 * I * \cos(d) + 3 * \sin(d)) * \operatorname{erf}(1/2 * (2 * c * x * \log(f) + I * e) / \sqrt{-c * \log(f)}) * e^{(1/4 * e^2 / (c * \log(f)))} + f^a * (3 * I * \cos(d) + 3 * \sin(d)) * \operatorname{erf}(1/2 * (2 * c * x * \log(f) - I * e) / \sqrt{-c * \log(f)}) * e^{(1/4 * e^2 / (c * \log(f)))} * \sqrt{-c * \log(f)} / (c * \log(f)))$

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int f^{cx^2+a} \sin(d + ex)^3 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(f^(a + c*x^2)*sin(d + e*x)^3,x)

[Out] int(f^(a + c*x^2)*sin(d + e*x)^3, x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int f^{a+cx^2} \sin^3(d + ex) dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(f**(c*x**2+a)*sin(e*x+d)**3,x)
```

```
[Out] Integral(f**(a + c*x**2)*sin(d + e*x)**3, x)
```

3.88 $\int f^{a+cx^2} \sin(d + fx^2) dx$

Optimal. Leaf size=107

$$\frac{i\sqrt{\pi} e^{-id} f^a \operatorname{erf}\left(x\sqrt{-c \log(f) + if}\right)}{4\sqrt{-c \log(f) + if}} - \frac{i\sqrt{\pi} e^{id} f^a \operatorname{erfi}\left(x\sqrt{c \log(f) + if}\right)}{4\sqrt{c \log(f) + if}}$$

[Out] $1/4 * I * f^a * \operatorname{erf}(x * (I * f - c * \ln(f))^{1/2}) * \pi^{1/2} / \exp(I * d) / (I * f - c * \ln(f))^{1/2} - 1/4 * I * \exp(I * d) * f^a * \operatorname{erfi}(x * (I * f + c * \ln(f))^{1/2}) * \pi^{1/2} / (I * f + c * \ln(f))^{1/2}$

Rubi [A] time = 0.20, antiderivative size = 107, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 4, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.222$, Rules used = {4472, 2287, 2205, 2204}

$$\frac{i\sqrt{\pi} e^{-id} f^a \operatorname{Erf}\left(x\sqrt{-c \log(f) + if}\right)}{4\sqrt{-c \log(f) + if}} - \frac{i\sqrt{\pi} e^{id} f^a \operatorname{Erfi}\left(x\sqrt{c \log(f) + if}\right)}{4\sqrt{c \log(f) + if}}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[f^{(a + c * x^2)} * \operatorname{Sin}[d + f * x^2], x]$

[Out] $((I/4) * f^a * \operatorname{Sqrt}[\pi] * \operatorname{Erf}[x * \operatorname{Sqrt}[I * f - c * \operatorname{Log}[f]]]) / (E^{(I * d)} * \operatorname{Sqrt}[I * f - c * \operatorname{Log}[f]]) - ((I/4) * E^{(I * d)} * f^a * \operatorname{Sqrt}[\pi] * \operatorname{Erfi}[x * \operatorname{Sqrt}[I * f + c * \operatorname{Log}[f]]]) / \operatorname{Sqrt}[I * f + c * \operatorname{Log}[f]]$

Rule 2204

$\operatorname{Int}[(F_)^{((a_.) + (b_.) * ((c_.) + (d_.) * (x_.)^2))}, x_Symbol] := \operatorname{Simp}[(F^a * \operatorname{Sqrt}[\pi] * \operatorname{Erfi}[(c + d * x) * \operatorname{Rt}[b * \operatorname{Log}[F], 2]]) / (2 * d * \operatorname{Rt}[b * \operatorname{Log}[F], 2]), x] /;$ $\operatorname{FreeQ}\{F, a, b, c, d\}, x] \ \&\& \ \operatorname{PosQ}[b]$

Rule 2205

$\operatorname{Int}[(F_)^{((a_.) + (b_.) * ((c_.) + (d_.) * (x_.)^2))}, x_Symbol] := \operatorname{Simp}[(F^a * \operatorname{Sqrt}[\pi] * \operatorname{Erf}[(c + d * x) * \operatorname{Rt}[-(b * \operatorname{Log}[F]), 2]]) / (2 * d * \operatorname{Rt}[-(b * \operatorname{Log}[F]), 2]), x] /;$ $\operatorname{FreeQ}\{F, a, b, c, d\}, x] \ \&\& \ \operatorname{NegQ}[b]$

Rule 2287

$\operatorname{Int}[(u_.) * (F_)^{(v_.)} * (G_)^{(w_.)}, x_Symbol] := \operatorname{With}\{z = v * \operatorname{Log}[F] + w * \operatorname{Log}[G]\}, \operatorname{Int}[u * \operatorname{NormalizeIntegrand}[E^z, x], x] /;$ $\operatorname{BinomialQ}[z, x] \ || \ (\operatorname{PolynomialQ}[z, x] \ \&\& \ \operatorname{LeQ}[\operatorname{Exponent}[z, x], 2]) /;$ $\operatorname{FreeQ}\{F, G\}, x]$

Rule 4472

$\operatorname{Int}[(F_)^{(u_.)} * \operatorname{Sin}[v_]^{(n_.)}, x_Symbol] := \operatorname{Int}[\operatorname{ExpandTrigToExp}[F^u, \operatorname{Sin}[v]^n], x] /;$ $\operatorname{FreeQ}[F, x] \ \&\& \ (\operatorname{LinearQ}[u, x] \ || \ \operatorname{PolyQ}[u, x, 2]) \ \&\& \ (\operatorname{LinearQ}[v, x] \ || \ \operatorname{PolyQ}[v, x, 2]) \ \&\& \ \operatorname{IGtQ}[n, 0]$

Rubi steps

$$\begin{aligned}
\int f^{a+cx^2} \sin(d + fx^2) dx &= \int \left(\frac{1}{2} i e^{-id-ifx^2} f^{a+cx^2} - \frac{1}{2} i e^{id+ifx^2} f^{a+cx^2} \right) dx \\
&= \frac{1}{2} i \int e^{-id-ifx^2} f^{a+cx^2} dx - \frac{1}{2} i \int e^{id+ifx^2} f^{a+cx^2} dx \\
&= \frac{1}{2} i \int e^{-id+a \log(f) - x^2(if-c \log(f))} dx - \frac{1}{2} i \int e^{id+a \log(f) + x^2(if+c \log(f))} dx \\
&= \frac{i e^{-id} f^a \sqrt{\pi} \operatorname{erf}(x \sqrt{if - c \log(f)})}{4 \sqrt{if - c \log(f)}} - \frac{i e^{id} f^a \sqrt{\pi} \operatorname{erfi}(x \sqrt{if + c \log(f)})}{4 \sqrt{if + c \log(f)}}
\end{aligned}$$

Mathematica [A] time = 0.48, size = 170, normalized size = 1.59

$$\frac{\sqrt[4]{-1} \sqrt{\pi} f^a \left(\sqrt{f + ic \log(f)} \left(c \sin(d) \log(f) \operatorname{erf} \left(\frac{(1+i)x \sqrt{f+ic \log(f)}}{\sqrt{2}} \right) + \operatorname{erfi} \left((-1)^{3/4} x \sqrt{f + ic \log(f)} \right) \right) (f \sin(d) + \dots)}{4 (c^2 \log^2(f) + f^2)}$$

Antiderivative was successfully verified.

```
[In] Integrate[f^(a + c*x^2)*Sin[d + f*x^2],x]
[Out] -1/4*((-1)^(1/4)*f^a*Sqrt[Pi]*(Erfi[(-1)^(1/4)*x*Sqrt[f - I*c*Log[f]]]*Sqrt[f - I*c*Log[f]]*(f + I*c*Log[f])*(Cos[d] + I*Sin[d]) + Sqrt[f + I*c*Log[f]]*(c*Erf[((1 + I)*x*Sqrt[f + I*c*Log[f]])/Sqrt[2]]*Log[f]*Sin[d] + Erfi[(-1)^(3/4)*x*Sqrt[f + I*c*Log[f]]]*(Cos[d]*(I*f + c*Log[f]) + f*Sin[d]))) / (f^2 + c^2*Log[f]^2)
```

fricas [A] time = 0.76, size = 107, normalized size = 1.00

$$\frac{\sqrt{\pi} (ic \log(f) + f) \sqrt{-c \log(f) - if} \operatorname{erf}(\sqrt{-c \log(f) - if} x) e^{(a \log(f) + id)} + \sqrt{\pi} (-ic \log(f) + f) \sqrt{-c \log(f) + if} \operatorname{erfi}(\sqrt{-c \log(f) + if} x)}{4 (c^2 \log(f)^2 + f^2)}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(f^(c*x^2+a)*sin(f*x^2+d),x, algorithm="fricas")
[Out] 1/4*(sqrt(pi)*(I*c*log(f) + f)*sqrt(-c*log(f) - I*f)*erf(sqrt(-c*log(f) - I*f)*x)*e^(a*log(f) + I*d) + sqrt(pi)*(-I*c*log(f) + f)*sqrt(-c*log(f) + I*f)*erf(sqrt(-c*log(f) + I*f)*x)*e^(a*log(f) - I*d))/(c^2*log(f)^2 + f^2)
```

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int f^{cx^2+a} \sin(fx^2 + d) dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(f^(c*x^2+a)*sin(f*x^2+d),x, algorithm="giac")
[Out] integrate(f^(c*x^2 + a)*sin(f*x^2 + d), x)
```

maple [A] time = 0.32, size = 84, normalized size = 0.79

$$-\frac{i \sqrt{\pi} f^a e^{id} \operatorname{erf}(\sqrt{-if - c \ln(f)} x)}{4 \sqrt{-if - c \ln(f)}} + \frac{i \sqrt{\pi} f^a e^{-id} \operatorname{erf}(x \sqrt{if - c \ln(f)})}{4 \sqrt{if - c \ln(f)}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(f^(c*x^2+a)*sin(f*x^2+d),x)
```

```
[Out] -1/4*I*Pi^(1/2)*f^a*exp(I*d)/(-I*f-c*ln(f))^(1/2)*erf((-I*f-c*ln(f))^(1/2)*
x)+1/4*I*Pi^(1/2)*f^a*exp(-I*d)/(I*f-c*ln(f))^(1/2)*erf(x*(I*f-c*ln(f))^(1/
2))
```

maxima [B] time = 0.36, size = 209, normalized size = 1.95

$$\frac{\sqrt{\pi} \sqrt{2c^2 \log(f)^2 + 2f^2} \left(f^a (\cos(d) - i \sin(d)) \operatorname{erf}(\sqrt{-c \log(f) + ifx}) + f^a (\cos(d) + i \sin(d)) \operatorname{erf}(\sqrt{-c \log(f) - ifx}) \right)}{\dots}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(f^(c*x^2+a)*sin(f*x^2+d),x, algorithm="maxima")
```

```
[Out] 1/8*(sqrt(pi)*sqrt(2*c^2*log(f)^2 + 2*f^2)*(f^a*(cos(d) - I*sin(d))*erf(sqrt(-c*log(f) + I*f)*x) + f^a*(cos(d) + I*sin(d))*erf(sqrt(-c*log(f) - I*f)*x)))*sqrt(c*log(f) + sqrt(c^2*log(f)^2 + f^2)) - sqrt(pi)*sqrt(2*c^2*log(f)^2 + 2*f^2)*(f^a*(-I*cos(d) - sin(d))*erf(sqrt(-c*log(f) + I*f)*x) + f^a*(I*cos(d) - sin(d))*erf(sqrt(-c*log(f) - I*f)*x))*sqrt(-c*log(f) + sqrt(c^2*log(f)^2 + f^2)))/(c^2*log(f)^2 + f^2)
```

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int f^{cx^2+a} \sin(fx^2 + d) dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(f^(a + c*x^2)*sin(d + f*x^2),x)
```

```
[Out] int(f^(a + c*x^2)*sin(d + f*x^2), x)
```

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int f^{a+cx^2} \sin(d + fx^2) dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(f**(c*x**2+a)*sin(f*x**2+d),x)
```

```
[Out] Integral(f**(a + c*x**2)*sin(d + f*x**2), x)
```

3.89 $\int f^{a+cx^2} \sin^2(d + fx^2) dx$

Optimal. Leaf size=140

$$\frac{\sqrt{\pi} e^{-2id} f^a \operatorname{erf}(x\sqrt{-c \log(f) + 2if})}{8\sqrt{-c \log(f) + 2if}} - \frac{\sqrt{\pi} e^{2id} f^a \operatorname{erfi}(x\sqrt{c \log(f) + 2if})}{8\sqrt{c \log(f) + 2if}} + \frac{\sqrt{\pi} f^a \operatorname{erfi}(\sqrt{c} x \sqrt{\log(f)})}{4\sqrt{c} \sqrt{\log(f)}}$$

[Out] $1/4*f^a*\operatorname{erfi}(x*c^{(1/2)}*\ln(f)^{(1/2)})*\operatorname{Pi}^{(1/2)}/c^{(1/2)}/\ln(f)^{(1/2)}-1/8*f^a*\operatorname{erf}(x*(2*I*f-c*\ln(f))^{(1/2)})*\operatorname{Pi}^{(1/2)}/\exp(2*I*d)/(2*I*f-c*\ln(f))^{(1/2)}-1/8*\exp(2*I*d)*f^a*\operatorname{erfi}(x*(2*I*f+c*\ln(f))^{(1/2)})*\operatorname{Pi}^{(1/2)}/(2*I*f+c*\ln(f))^{(1/2)}$

Rubi [A] time = 0.23, antiderivative size = 140, normalized size of antiderivative = 1.00, number of steps used = 7, number of rules used = 4, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.200$, Rules used = {4472, 2204, 2287, 2205}

$$\frac{\sqrt{\pi} e^{-2id} f^a \operatorname{Erf}(x\sqrt{-c \log(f) + 2if})}{8\sqrt{-c \log(f) + 2if}} - \frac{\sqrt{\pi} e^{2id} f^a \operatorname{Erfi}(x\sqrt{c \log(f) + 2if})}{8\sqrt{c \log(f) + 2if}} + \frac{\sqrt{\pi} f^a \operatorname{Erfi}(\sqrt{c} x \sqrt{\log(f)})}{4\sqrt{c} \sqrt{\log(f)}}$$

Antiderivative was successfully verified.

[In] `Int[f^(a + c*x^2)*Sin[d + f*x^2]^2,x]`

[Out] $(f^a*\operatorname{Sqrt}[\operatorname{Pi}]*\operatorname{Erfi}[\operatorname{Sqrt}[c]*x*\operatorname{Sqrt}[\operatorname{Log}[f]]])/(4*\operatorname{Sqrt}[c]*\operatorname{Sqrt}[\operatorname{Log}[f]]) - (f^a*\operatorname{Sqrt}[\operatorname{Pi}]*\operatorname{Erf}[x*\operatorname{Sqrt}[(2*I)*f - c*\operatorname{Log}[f]])/(8*\operatorname{E}^{((2*I)*d)}*\operatorname{Sqrt}[(2*I)*f - c*\operatorname{Log}[f]]) - (\operatorname{E}^{((2*I)*d)}*f^a*\operatorname{Sqrt}[\operatorname{Pi}]*\operatorname{Erfi}[x*\operatorname{Sqrt}[(2*I)*f + c*\operatorname{Log}[f]])/(8*\operatorname{Sqrt}[(2*I)*f + c*\operatorname{Log}[f]])$

Rule 2204

`Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(2)), x_Symbol] := Simp[(F^a*Sqrt[Pi]*Erfi[(c + d*x)*Rt[b*Log[F], 2]])/(2*d*Rt[b*Log[F], 2]), x] /; FreeQ[{F, a, b, c, d}, x] && PosQ[b]`

Rule 2205

`Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(2)), x_Symbol] := Simp[(F^a*Sqrt[Pi]*Erf[(c + d*x)*Rt[-(b*Log[F]), 2]])/(2*d*Rt[-(b*Log[F]), 2]), x] /; FreeQ[{F, a, b, c, d}, x] && NegQ[b]`

Rule 2287

`Int[(u_.)*(F_)^(v_.)*(G_)^(w_.), x_Symbol] := With[{z = v*Log[F] + w*Log[G]}, Int[u*NormalizeIntegrand[E^z, x], x] /; BinomialQ[z, x] || (PolynomialQ[z, x] && LeQ[Exponent[z, x], 2])] /; FreeQ[{F, G}, x]`

Rule 4472

`Int[(F_)^(u_.)*Sin[v_]^(n_.), x_Symbol] := Int[ExpandTrigToExp[F^u, Sin[v]^n, x], x] /; FreeQ[F, x] && (LinearQ[u, x] || PolyQ[u, x, 2]) && (LinearQ[v, x] || PolyQ[v, x, 2]) && IGtQ[n, 0]`

Rubi steps

$$\begin{aligned}
\int f^{a+cx^2} \sin^2(d + fx^2) dx &= \int \left(\frac{1}{2} f^{a+cx^2} - \frac{1}{4} e^{-2id-2ifx^2} f^{a+cx^2} - \frac{1}{4} e^{2id+2ifx^2} f^{a+cx^2} \right) dx \\
&= -\left(\frac{1}{4} \int e^{-2id-2ifx^2} f^{a+cx^2} dx \right) - \frac{1}{4} \int e^{2id+2ifx^2} f^{a+cx^2} dx + \frac{1}{2} \int f^{a+cx^2} dx \\
&= \frac{f^a \sqrt{\pi} \operatorname{erfi}(\sqrt{c} x \sqrt{\log(f)})}{4\sqrt{c} \sqrt{\log(f)}} - \frac{1}{4} \int \exp(-2id + a \log(f) - x^2(2if - c \log(f))) dx - \\
&= \frac{f^a \sqrt{\pi} \operatorname{erfi}(\sqrt{c} x \sqrt{\log(f)})}{4\sqrt{c} \sqrt{\log(f)}} - \frac{e^{-2id} f^a \sqrt{\pi} \operatorname{erf}(x \sqrt{2if - c \log(f)})}{8\sqrt{2if - c \log(f)}} - \frac{e^{2id} f^a \sqrt{\pi} \operatorname{erfi}(x \sqrt{2if - c \log(f)})}{8\sqrt{2if - c \log(f)}}
\end{aligned}$$

Mathematica [A] time = 0.82, size = 188, normalized size = 1.34

$$\frac{1}{8} \sqrt{\pi} f^a \left(\frac{2 \operatorname{erfi}(\sqrt{c} x \sqrt{\log(f)})}{\sqrt{c} \sqrt{\log(f)}} + \frac{\sqrt[4]{-1} (\sqrt{2f + ic \log(f)} (c \log(f) + 2if) (\cos(2d) - i \sin(2d)) \operatorname{erf}(\sqrt[4]{-1} x \sqrt{2f + ic \log(f)}) + ((-1)^{1/4} (\operatorname{Erf}((-1)^{1/4} x \sqrt{2f + ic \log(f)}) \sqrt{2f + ic \log(f)} + ((2I)f + c \log(f)) (\cos[2*d] - I \sin[2*d]) + \operatorname{Erf}((-1)^{3/4} x \sqrt{2f - ic \log(f)}) \sqrt{2f - ic \log(f)} (2f + ic \log(f)) (\cos[2*d] + I \sin[2*d]))) / (4f^2 + c^2 \log(f)^2))}{8} \right)$$

Antiderivative was successfully verified.

[In] Integrate[f^(a + c*x^2)*Sin[d + f*x^2]^2,x]

[Out] (f^a*Sqrt[Pi]*((2*Erfi[Sqrt[c]*x*Sqrt[Log[f]]])/(Sqrt[c]*Sqrt[Log[f]])) + ((-1)^(1/4)*(Erf[(-1)^(1/4)*x*Sqrt[2*f + I*c*Log[f]]]*Sqrt[2*f + I*c*Log[f]]* ((2*I)*f + c*Log[f])*(Cos[2*d] - I*Sin[2*d]) + Erf[(-1)^(3/4)*x*Sqrt[2*f - I*c*Log[f]]]*Sqrt[2*f - I*c*Log[f]]*(2*f + I*c*Log[f])*(Cos[2*d] + I*Sin[2*d])))/(4*f^2 + c^2*Log[f]^2))/8

fricas [A] time = 0.72, size = 169, normalized size = 1.21

$$\frac{2 \sqrt{\pi} (c^2 \log(f)^2 + 4 f^2) \sqrt{-c \log(f)} f^a \operatorname{erf}(\sqrt{-c \log(f)} x) - \sqrt{\pi} (c^2 \log(f)^2 - 2i c f \log(f)) \sqrt{-c \log(f) - 2if} \operatorname{erf}(x \sqrt{-c \log(f) - 2if})}{8 (c^3 \log(f)^3 + 4 c f^2 \log(f))}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(c*x^2+a)*sin(f*x^2+d)^2,x, algorithm="fricas")

[Out] -1/8*(2*sqrt(pi)*(c^2*log(f)^2 + 4*f^2)*sqrt(-c*log(f))*f^a*erf(sqrt(-c*log(f))*x) - sqrt(pi)*(c^2*log(f)^2 - 2*I*c*f*log(f))*sqrt(-c*log(f) - 2*I*f)*erf(sqrt(-c*log(f) - 2*I*f)*x)*e^(a*log(f) + 2*I*d) - sqrt(pi)*(c^2*log(f)^2 + 2*I*c*f*log(f))*sqrt(-c*log(f) + 2*I*f)*erf(sqrt(-c*log(f) + 2*I*f)*x)*e^(a*log(f) - 2*I*d))/(c^3*log(f)^3 + 4*c*f^2*log(f))

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int f^{cx^2+a} \sin(fx^2 + d)^2 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(c*x^2+a)*sin(f*x^2+d)^2,x, algorithm="giac")

[Out] integrate(f^(c*x^2 + a)*sin(f*x^2 + d)^2, x)

maple [A] time = 0.40, size = 107, normalized size = 0.76

$$-\frac{\sqrt{\pi} f^a e^{-2id} \operatorname{erf}(x \sqrt{2if - c \ln(f)})}{8\sqrt{2if - c \ln(f)}} - \frac{\sqrt{\pi} f^a e^{2id} \operatorname{erf}(x \sqrt{-2if - c \ln(f)})}{8\sqrt{-2if - c \ln(f)}} + \frac{f^a \sqrt{\pi} \operatorname{erf}(\sqrt{-c \ln(f)} x)}{4\sqrt{-c \ln(f)}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(f^(c*x^2+a)*sin(f*x^2+d)^2,x)

[Out] $-1/8\pi^{1/2}f^a\exp(-2I*d)/(2I*f-c*\ln(f))^{1/2}\operatorname{erf}(x*(2I*f-c*\ln(f))^{1/2}) - 1/8\pi^{1/2}f^a\exp(2I*d)/(-2I*f-c*\ln(f))^{1/2}\operatorname{erf}((-2I*f-c*\ln(f))^{1/2}*x) + 1/4f^a\pi^{1/2}/(-c*\ln(f))^{1/2}\operatorname{erf}((-c*\ln(f))^{1/2}*x)$

maxima [C] time = 0.38, size = 315, normalized size = 2.25

$$\sqrt{\pi} \sqrt{2c^2 \log(f)^2 + 8f^2} \left(f^a (i \cos(2d) + \sin(2d)) \operatorname{erf}(\sqrt{-c \log(f) + 2i f x}) + f^a (-i \cos(2d) + \sin(2d)) \operatorname{erf}(\sqrt{-c \log(f) - 2i f x}) \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(c*x^2+a)*sin(f*x^2+d)^2,x, algorithm="maxima")

[Out] $1/16*(\sqrt{\pi})\sqrt{2c^2\log(f)^2 + 8f^2}*(f^a*(I*\cos(2*d) + \sin(2*d))*\operatorname{erf}(\sqrt{-c*\log(f) + 2*I*f}*x) + f^a*(-I*\cos(2*d) + \sin(2*d))*\operatorname{erf}(\sqrt{-c*\log(f) - 2*I*f}*x))*\sqrt{c*\log(f) + \sqrt{c^2*\log(f)^2 + 4*f^2}}*\sqrt{-c*\log(f)} - \sqrt{\pi}\sqrt{2c^2\log(f)^2 + 8f^2}*(f^a*(\cos(2*d) - I*\sin(2*d))*\operatorname{erf}(\sqrt{-c*\log(f) + 2*I*f}*x) + f^a*(\cos(2*d) + I*\sin(2*d))*\operatorname{erf}(\sqrt{-c*\log(f) - 2*I*f}*x))*\sqrt{-c*\log(f) + \sqrt{c^2*\log(f)^2 + 4*f^2}}*\sqrt{-c*\log(f)} + 2*\sqrt{\pi}*((c^2*f^a*\log(f)^2 + 4*f^{(a+2)})*\operatorname{erf}(x*\operatorname{conjugate}(\sqrt{-c*\log(f)}))) + (c^2*f^a*\log(f)^2 + 4*f^{(a+2)})*\operatorname{erf}(\sqrt{-c*\log(f)}*x))/((c^2*\log(f)^2 + 4*f^2)*\sqrt{-c*\log(f)})$

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int f^{c x^2+a} \sin(f x^2+d)^2 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(f^(a + c*x^2)*sin(d + f*x^2)^2,x)

[Out] int(f^(a + c*x^2)*sin(d + f*x^2)^2, x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int f^{a+cx^2} \sin^2(d + fx^2) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f**(c*x**2+a)*sin(f*x**2+d)**2,x)

[Out] Integral(f**(a + c*x**2)*sin(d + f*x**2)**2, x)

3.90 $\int f^{a+cx^2} \sin^3(d + fx^2) dx$

Optimal. Leaf size=213

$$\frac{3i\sqrt{\pi} e^{-id} f^a \operatorname{erf}(x\sqrt{-c \log(f) + if})}{16\sqrt{-c \log(f) + if}} - \frac{i\sqrt{\pi} e^{-3id} f^a \operatorname{erf}(x\sqrt{-c \log(f) + 3if})}{16\sqrt{-c \log(f) + 3if}} - \frac{3i\sqrt{\pi} e^{id} f^a \operatorname{erfi}(x\sqrt{c \log(f) + if})}{16\sqrt{c \log(f) + if}} + \dots$$

```
[Out] 3/16*I*f^a*erf(x*(I*f-c*ln(f))^(1/2))*Pi^(1/2)/exp(I*d)/(I*f-c*ln(f))^(1/2)
-1/16*I*f^a*erf(x*(3*I*f-c*ln(f))^(1/2))*Pi^(1/2)/exp(3*I*d)/(3*I*f-c*ln(f)
)^(1/2)-3/16*I*exp(I*d)*f^a*erfi(x*(I*f+c*ln(f))^(1/2))*Pi^(1/2)/(I*f+c*ln(
f))^(1/2)+1/16*I*exp(3*I*d)*f^a*erfi(x*(3*I*f+c*ln(f))^(1/2))*Pi^(1/2)/(3*I
*f+c*ln(f))^(1/2)
```

Rubi [A] time = 0.33, antiderivative size = 213, normalized size of antiderivative = 1.00, number of steps used = 10, number of rules used = 4, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.200$, Rules used = {4472, 2287, 2205, 2204}

$$\frac{3i\sqrt{\pi} e^{-id} f^a \operatorname{Erf}(x\sqrt{-c \log(f) + if})}{16\sqrt{-c \log(f) + if}} - \frac{i\sqrt{\pi} e^{-3id} f^a \operatorname{Erf}(x\sqrt{-c \log(f) + 3if})}{16\sqrt{-c \log(f) + 3if}} - \frac{3i\sqrt{\pi} e^{id} f^a \operatorname{Erfi}(x\sqrt{c \log(f) + if})}{16\sqrt{c \log(f) + if}} + \dots$$

Antiderivative was successfully verified.

```
[In] Int[f^(a + c*x^2)*Sin[d + f*x^2]^3,x]
```

```
[Out] (((3*I)/16)*f^a*Sqrt[Pi]*Erf[x*Sqrt[I*f - c*Log[f]]])/(E^(I*d)*Sqrt[I*f - c
*Log[f]]) - ((I/16)*f^a*Sqrt[Pi]*Erf[x*Sqrt[(3*I)*f - c*Log[f]]])/(E^((3*I)
*d)*Sqrt[(3*I)*f - c*Log[f]]) - (((3*I)/16)*E^(I*d)*f^a*Sqrt[Pi]*Erfi[x*Sqr
t[I*f + c*Log[f]]])/Sqrt[I*f + c*Log[f]] + ((I/16)*E^((3*I)*d)*f^a*Sqrt[Pi]
*Erfi[x*Sqrt[(3*I)*f + c*Log[f]]])/Sqrt[(3*I)*f + c*Log[f]]
```

Rule 2204

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_)^2), x_Symbol] := Simp[(F^a*Sqr
t[Pi]*Erfi[(c + d*x)*Rt[b*Log[F], 2]])/(2*d*Rt[b*Log[F], 2]), x] /; FreeQ[{
F, a, b, c, d}, x] && PosQ[b]
```

Rule 2205

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_)^2), x_Symbol] := Simp[(F^a*Sqr
t[Pi]*Erf[(c + d*x)*Rt[-(b*Log[F]), 2]])/(2*d*Rt[-(b*Log[F]), 2]), x] /; Fr
eeQ[{F, a, b, c, d}, x] && NegQ[b]
```

Rule 2287

```
Int[(u_)*(F_)^(v_)*(G_)^(w_), x_Symbol] := With[{z = v*Log[F] + w*Log[G]},
Int[u*NormalizeIntegrand[E^z, x], x] /; BinomialQ[z, x] || (PolynomialQ[z,
x] && LeQ[Exponent[z, x], 2])] /; FreeQ[{F, G}, x]
```

Rule 4472

```
Int[(F_)^(u_)*Sin[v_]^(n_), x_Symbol] := Int[ExpandTrigToExp[F^u, Sin[v]^n
, x], x] /; FreeQ[F, x] && (LinearQ[u, x] || PolyQ[u, x, 2]) && (LinearQ[v,
x] || PolyQ[v, x, 2]) && IGtQ[n, 0]
```

Rubi steps

$$\begin{aligned}
\int f^{a+cx^2} \sin^3(d+fx^2) dx &= \int \left(\frac{3}{8} i e^{-id-ifx^2} f^{a+cx^2} - \frac{3}{8} i e^{id+ifx^2} f^{a+cx^2} - \frac{1}{8} i e^{-3id-3ifx^2} f^{a+cx^2} + \frac{1}{8} i e^{3id+3ifx^2} f^{a+cx^2} \right) dx \\
&= -\left(\frac{1}{8} i \int e^{-3id-3ifx^2} f^{a+cx^2} dx \right) + \frac{1}{8} i \int e^{3id+3ifx^2} f^{a+cx^2} dx + \frac{3}{8} i \int e^{-id-ifx^2} f^{a+cx^2} dx \\
&= -\left(\frac{1}{8} i \int \exp(-3id + a \log(f) - x^2(3if - c \log(f))) dx \right) + \frac{1}{8} i \int \exp(3id + a \log(f) + x^2(3if - c \log(f))) dx \\
&= \frac{3ie^{-id} f^a \sqrt{\pi} \operatorname{erf}(x\sqrt{if - c \log(f)})}{16\sqrt{if - c \log(f)}} - \frac{ie^{-3id} f^a \sqrt{\pi} \operatorname{erf}(x\sqrt{3if - c \log(f)})}{16\sqrt{3if - c \log(f)}} - \frac{3ie^{id} f^a \sqrt{\pi} \operatorname{erf}(x\sqrt{-c \log(f) - 3if})}{16\sqrt{-c \log(f) - 3if}} + \frac{ie^{3id} f^a \sqrt{\pi} \operatorname{erf}(x\sqrt{-c \log(f) - 3if})}{16\sqrt{-c \log(f) - 3if}}
\end{aligned}$$

Mathematica [A] time = 2.31, size = 386, normalized size = 1.81

$$\frac{\sqrt[4]{-1} \sqrt{\pi} f^a \left((f - ic \log(f)) \left(\sqrt{3f - ic \log(f)} (-c^2 \log^2(f) + 4icf \log(f) + 3f^2) (\cos(3d) + i \sin(3d)) \operatorname{erfi} \left(\sqrt[4]{-1} \sqrt{3f - ic \log(f)} x \right) \right) \right)}{16 \sqrt{3f - ic \log(f)}}$$

Antiderivative was successfully verified.

[In] Integrate[f^(a + c*x^2)*Sin[d + f*x^2]^3,x]

[Out] $((-1)^{(1/4)} f^a \sqrt{\pi} (-3 \operatorname{Erfi}[-(-1)^{(1/4)} x \sqrt{f - I c \log[f]}]) \sqrt{f - I c \log[f]} (9 f^3 + (9 I) c f^2 \log[f] + c^2 f \log[f]^2 + I c^3 \log[f]^3) (\cos[d] + I \sin[d]) + (f - I c \log[f]) (\operatorname{Erfi}[-(-1)^{(1/4)} x \sqrt{3 f - I c \log[f]}]) \sqrt{3 f - I c \log[f]} (3 f^2 + (4 I) c f \log[f] - c^2 \log[f]^2) (\cos[3 d] + I \sin[3 d]) + (3 f - I c \log[f]) (3 \operatorname{Erfi}[-(-1)^{(3/4)} x \sqrt{f + I c \log[f]}]) \sqrt{f + I c \log[f]} (c \cos[d] \log[f] - 3 f \sin[d]) + 3 \operatorname{Erf}[(1 + I) x \sqrt{f + I c \log[f]}] / \sqrt{2}] \sqrt{f + I c \log[f]} (3 f \cos[d] + c \log[f] \sin[d]) + \operatorname{Erfi}[-(-1)^{(3/4)} x \sqrt{3 f + I c \log[f]}] (f + I c \log[f]) \sqrt{3 f + I c \log[f]} (I \cos[3 d] + \sin[3 d]))) / (16 (9 f^4 + 10 c^2 f^2 \log[f]^2 + c^4 \log[f]^4))$

fricas [B] time = 0.60, size = 315, normalized size = 1.48

$$\frac{\sqrt{\pi} (-ic^3 \log(f)^3 - 3c^2 f \log(f)^2 - icf^2 \log(f) - 3f^3) \sqrt{-c \log(f) - 3if} \operatorname{erf}(\sqrt{-c \log(f) - 3if} x) e^{(a \log(f) + 3id)}}{16 \sqrt{-c \log(f) - 3if}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(c*x^2+a)*sin(f*x^2+d)^3,x, algorithm="fricas")

[Out] $1/16 * (\sqrt{\pi} (-I c^3 \log(f)^3 - 3 c^2 f \log(f)^2 - I c f^2 \log(f) - 3 f^3) \sqrt{-c \log(f) - 3 I f} \operatorname{erf}(\sqrt{-c \log(f) - 3 I f} x) e^{(a \log(f) + 3 I d)} + \sqrt{\pi} (3 I c^3 \log(f)^3 + 3 c^2 f \log(f)^2 + 27 I c f^2 \log(f) + 27 f^3) \sqrt{-c \log(f) - I f} \operatorname{erf}(\sqrt{-c \log(f) - I f} x) e^{(a \log(f) + I d)} + \sqrt{\pi} (-3 I c^3 \log(f)^3 + 3 c^2 f \log(f)^2 - 27 I c f^2 \log(f) + 27 f^3) \sqrt{-c \log(f) + I f} \operatorname{erf}(\sqrt{-c \log(f) + I f} x) e^{(a \log(f) - I d)} + \sqrt{\pi} (I c^3 \log(f)^3 - 3 c^2 f \log(f)^2 + I c f^2 \log(f) - 3 f^3) \sqrt{-c \log(f) + 3 I f} \operatorname{erf}(\sqrt{-c \log(f) + 3 I f} x) e^{(a \log(f) - 3 I d)}) / (c^4 \log(f)^4 + 10 c^2 f^2 \log(f)^2 + 9 f^4)$

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int f^{cx^2+a} \sin(fx^2+d)^3 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(c*x^2+a)*sin(f*x^2+d)^3,x, algorithm="giac")

[Out] integrate(f^(c*x^2 + a)*sin(f*x^2 + d)^3, x)

maple [A] time = 0.76, size = 166, normalized size = 0.78

$$\frac{i\sqrt{\pi} f^a e^{3id} \operatorname{erf}\left(\sqrt{-c \ln(f) - 3if} x\right)}{16\sqrt{-c \ln(f) - 3if}} - \frac{i\sqrt{\pi} f^a e^{-3id} \operatorname{erf}\left(x\sqrt{3if - c \ln(f)}\right)}{16\sqrt{3if - c \ln(f)}} + \frac{3i\sqrt{\pi} f^a e^{-id} \operatorname{erf}\left(x\sqrt{if - c \ln(f)}\right)}{16\sqrt{if - c \ln(f)}} - \frac{3i\sqrt{\pi} f^a e^{id} \operatorname{erf}\left(x\sqrt{-if - c \ln(f)}\right)}{16\sqrt{-if - c \ln(f)}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(f^(c*x^2+a)*sin(f*x^2+d)^3,x)

[Out] 1/16*I*Pi^(1/2)*f^a*exp(3*I*d)/(-c*ln(f)-3*I*f)^(1/2)*erf((-c*ln(f)-3*I*f)^(1/2)*x)-1/16*I*Pi^(1/2)*f^a*exp(-3*I*d)/(3*I*f-c*ln(f))^(1/2)*erf(x*(3*I*f-c*ln(f))^(1/2))+3/16*I*Pi^(1/2)*f^a*exp(-I*d)/(I*f-c*ln(f))^(1/2)*erf(x*(I*f-c*ln(f))^(1/2))-3/16*I*Pi^(1/2)*f^a*exp(I*d)/(-I*f-c*ln(f))^(1/2)*erf((-I*f-c*ln(f))^(1/2)*x)

maxima [B] time = 0.40, size = 671, normalized size = 3.15

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(c*x^2+a)*sin(f*x^2+d)^3,x, algorithm="maxima")

[Out] -1/131072*(sqrt(pi)*sqrt(2*c^2*log(f)^2 + 18*f^2)*(((4096*c^2*cos(3*d) - 4096*I*c^2*sin(3*d))*f^a*log(f)^2 + 4096*f^(a + 2)*(cos(3*d) - I*sin(3*d)))*erf(sqrt(-c*log(f) + 3*I*f)*x) + ((4096*c^2*cos(3*d) + 4096*I*c^2*sin(3*d))*f^a*log(f)^2 + 4096*f^(a + 2)*(cos(3*d) + I*sin(3*d)))*erf(sqrt(-c*log(f) - 3*I*f)*x))*sqrt(c*log(f) + sqrt(c^2*log(f)^2 + 9*f^2)) - 12288*sqrt(pi)*sqrt(2*c^2*log(f)^2 + 2*f^2)*(((c^2*cos(d) - I*c^2*sin(d))*f^a*log(f)^2 + 9*f^(a + 2)*(cos(d) - I*sin(d)))*erf(sqrt(-c*log(f) + I*f)*x) + ((c^2*cos(d) + I*c^2*sin(d))*f^a*log(f)^2 + 9*f^(a + 2)*(cos(d) + I*sin(d)))*erf(sqrt(-c*log(f) - I*f)*x))*sqrt(c*log(f) + sqrt(c^2*log(f)^2 + f^2)) + sqrt(pi)*sqrt(2*c^2*log(f)^2 + 18*f^2)*(((4096*(I*c^2*cos(3*d) + c^2*sin(3*d))*f^a*log(f)^2 - f^(a + 2)*(-4096*I*cos(3*d) - 4096*sin(3*d)))*erf(sqrt(-c*log(f) + 3*I*f)*x) + (4096*(-I*c^2*cos(3*d) + c^2*sin(3*d))*f^a*log(f)^2 - f^(a + 2)*(4096*I*cos(3*d) - 4096*sin(3*d)))*erf(sqrt(-c*log(f) - 3*I*f)*x))*sqrt(-c*log(f) + sqrt(c^2*log(f)^2 + 9*f^2)) - sqrt(pi)*sqrt(2*c^2*log(f)^2 + 2*f^2)*(((12288*I*c^2*cos(d) + 12288*c^2*sin(d))*f^a*log(f)^2 + f^(a + 2)*(110592*I*cos(d) + 110592*sin(d)))*erf(sqrt(-c*log(f) + I*f)*x) + ((-12288*I*c^2*cos(d) + 12288*c^2*sin(d))*f^a*log(f)^2 + f^(a + 2)*(-110592*I*cos(d) + 110592*sin(d)))*erf(sqrt(-c*log(f) - I*f)*x))*sqrt(-c*log(f) + sqrt(c^2*log(f)^2 + f^2)))/(c^4*log(f)^4 + 10*c^2*f^2*log(f)^2 + 9*f^4)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int f^{cx^2+a} \sin(fx^2 + d)^3 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(f^(a + c*x^2)*sin(d + f*x^2)^3,x)

[Out] int(f^(a + c*x^2)*sin(d + f*x^2)^3, x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int f^{a+cx^2} \sin^3(d + fx^2) dx$$

Verification of antiderivative is not currently implemented for this CAS.


```
[In] integrate(f**(c*x**2+a)*sin(f*x**2+d)**3,x)
```

```
[Out] Integral(f**(a + c*x**2)*sin(d + f*x**2)**3, x)
```

3.91 $\int f^{a+cx^2} \sin(d + ex + fx^2) dx$

Optimal. Leaf size=187

$$\frac{i\sqrt{\pi} f^a e^{-\frac{e^2}{-4c \log(f)+4if} - id} \operatorname{erf}\left(\frac{2x(-c \log(f)+if)+ie}{2\sqrt{-c \log(f)+if}}\right)}{4\sqrt{-c \log(f)+if}} - \frac{i\sqrt{\pi} f^a e^{\frac{e^2}{4c \log(f)+4if} + id} \operatorname{erfi}\left(\frac{2x(c \log(f)+if)+ie}{2\sqrt{c \log(f)+if}}\right)}{4\sqrt{c \log(f)+if}}$$

[Out] $\frac{1}{4} I \exp(-I d - e^2 / (4 I f - 4 c \ln(f))) f^a \operatorname{erf}(1/2 (I e + 2 x (I f - c \ln(f)))) / (I f - c \ln(f))^{1/2} \pi^{1/2} / (I f - c \ln(f))^{1/2} - 1/4 I \exp(I d + e^2 / (4 I f + 4 c \ln(f))) f^a \operatorname{erfi}(1/2 (I e + 2 x (I f + c \ln(f)))) / (I f + c \ln(f))^{1/2} \pi^{1/2} / (I f + c \ln(f))^{1/2}$

Rubi [A] time = 0.37, antiderivative size = 187, normalized size of antiderivative = 1.00, number of steps used = 8, number of rules used = 5, integrand size = 21, $\frac{\text{number of rules}}{\text{integrand size}} = 0.238$, Rules used = {4472, 2287, 2234, 2205, 2204}

$$\frac{i\sqrt{\pi} f^a e^{-\frac{e^2}{-4c \log(f)+4if} - id} \operatorname{Erf}\left(\frac{2x(-c \log(f)+if)+ie}{2\sqrt{-c \log(f)+if}}\right)}{4\sqrt{-c \log(f)+if}} - \frac{i\sqrt{\pi} f^a e^{\frac{e^2}{4c \log(f)+4if} + id} \operatorname{Erfi}\left(\frac{2x(c \log(f)+if)+ie}{2\sqrt{c \log(f)+if}}\right)}{4\sqrt{c \log(f)+if}}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[f^{(a + c x^2)} \operatorname{Sin}[d + e x + f x^2], x]$

[Out] $((I/4) E^{((-I) d - e^2 / ((4 I) f - 4 c \operatorname{Log}[f]))} f^a \operatorname{Sqrt}[\pi] \operatorname{Erf}[(I e + 2 x (I f - c \operatorname{Log}[f])) / (2 \operatorname{Sqrt}[I f - c \operatorname{Log}[f]])] / \operatorname{Sqrt}[I f - c \operatorname{Log}[f]] - ((I/4) E^{(I d + e^2 / ((4 I) f + 4 c \operatorname{Log}[f]))} f^a \operatorname{Sqrt}[\pi] \operatorname{Erfi}[(I e + 2 x (I f + c \operatorname{Log}[f])) / (2 \operatorname{Sqrt}[I f + c \operatorname{Log}[f]])] / \operatorname{Sqrt}[I f + c \operatorname{Log}[f]]]$

Rule 2204

$\operatorname{Int}[(F_)^{((a_.) + (b_.) * ((c_.) + (d_.) * (x_)^2))}, x_Symbol] := \operatorname{Simp}[(F^a \operatorname{Sqrt}[\pi] \operatorname{Erfi}[(c + d x) \operatorname{Rt}[b \operatorname{Log}[F], 2]]) / (2 d \operatorname{Rt}[b \operatorname{Log}[F], 2]), x] /; \operatorname{FreeQ}\{F, a, b, c, d\}, x] \&\& \operatorname{PosQ}[b]$

Rule 2205

$\operatorname{Int}[(F_)^{((a_.) + (b_.) * ((c_.) + (d_.) * (x_)^2))}, x_Symbol] := \operatorname{Simp}[(F^a \operatorname{Sqrt}[\pi] \operatorname{Erf}[(c + d x) \operatorname{Rt}[-(b \operatorname{Log}[F]), 2]]) / (2 d \operatorname{Rt}[-(b \operatorname{Log}[F]), 2]), x] /; \operatorname{FreeQ}\{F, a, b, c, d\}, x] \&\& \operatorname{NegQ}[b]$

Rule 2234

$\operatorname{Int}[(F_)^{((a_.) + (b_.) * (x_) + (c_.) * (x_)^2))}, x_Symbol] := \operatorname{Dist}[F^{(a - b^2 / (4 c))}, \operatorname{Int}[F^{((b + 2 c x)^2 / (4 c))}, x], x] /; \operatorname{FreeQ}\{F, a, b, c\}, x]$

Rule 2287

$\operatorname{Int}[(u_) * (F_)^{(v_)} * (G_)^{(w_)}}, x_Symbol] := \operatorname{With}\{z = v \operatorname{Log}[F] + w \operatorname{Log}[G]\}, \operatorname{Int}[u \operatorname{NormalizeIntegrand}[E^z, x], x] /; \operatorname{BinomialQ}[z, x] \mid\mid (\operatorname{PolynomialQ}[z, x] \&\& \operatorname{LeQ}[\operatorname{Exponent}[z, x], 2]) /; \operatorname{FreeQ}\{F, G\}, x]$

Rule 4472

$\operatorname{Int}[(F_)^{(u_)} * \operatorname{Sin}[v_]^{(n_)}}, x_Symbol] := \operatorname{Int}[\operatorname{ExpandTrigToExp}[F^u, \operatorname{Sin}[v]^n], x] /; \operatorname{FreeQ}[F, x] \&\& (\operatorname{LinearQ}[u, x] \mid\mid \operatorname{PolyQ}[u, x, 2]) \&\& (\operatorname{LinearQ}[v, x] \mid\mid \operatorname{PolyQ}[v, x, 2]) \&\& \operatorname{IGtQ}[n, 0]$

Rubi steps

$$\begin{aligned}
\int f^{a+cx^2} \sin(d+ex+fx^2) dx &= \int \left(\frac{1}{2} i e^{-id-ix-ix^2} f^{a+cx^2} - \frac{1}{2} i e^{id+ix+ix^2} f^{a+cx^2} \right) dx \\
&= \frac{1}{2} i \int e^{-id-ix-ix^2} f^{a+cx^2} dx - \frac{1}{2} i \int e^{id+ix+ix^2} f^{a+cx^2} dx \\
&= \frac{1}{2} i \int \exp(-id-ix+a \log(f)-x^2(if-c \log(f))) dx - \frac{1}{2} i \int \exp(id+ix+ix^2) f^{a+cx^2} dx \\
&= \frac{1}{2} \left(i e^{-id-\frac{e^2}{4if-4c \log(f)}} f^a \right) \int \exp\left(\frac{(-ie+2x(-if+c \log(f)))^2}{4(-if+c \log(f))}\right) dx - \frac{1}{2} \left(i e^{id+\frac{e^2}{4if+4c \log(f)}} f^a \right) \int \exp\left(\frac{(-ie+2x(-if+c \log(f)))^2}{4(-if+c \log(f))}\right) dx \\
&= \frac{i e^{-id-\frac{e^2}{4if-4c \log(f)}} f^a \sqrt{\pi} \operatorname{erf}\left(\frac{ie+2x(if-c \log(f))}{2\sqrt{if-c \log(f)}}\right)}{4\sqrt{if-c \log(f)}} - \frac{i e^{id+\frac{e^2}{4if+4c \log(f)}} f^a \sqrt{\pi} \operatorname{erfi}\left(\frac{ie+2x(if+c \log(f))}{2\sqrt{if+c \log(f)}}\right)}{4\sqrt{if+c \log(f)}}
\end{aligned}$$

Mathematica [A] time = 0.96, size = 216, normalized size = 1.16

$$\frac{(-1)^{3/4} \sqrt{\pi} f^a e^{\frac{e^2}{4c \log(f)+4if}} \left((f-ic \log(f)) \sqrt{f+ic \log(f)} (\cos(d)-i \sin(d)) e^{\frac{ie^2 f}{2(c^2 \log^2(f)+f^2)}} \operatorname{erfi}\left(\frac{(-1)^{3/4}(2icx \log(f)+e+2)}{2\sqrt{f+ic \log(f)}}\right) \right)}{4(c^2 \log^2(f)+f^2)}$$

Warning: Unable to verify antiderivative.

[In] Integrate[f^(a + c*x^2)*Sin[d + e*x + f*x^2],x]

[Out] $-1/4 * ((-1)^{(3/4)} * E^{(e^2 / ((4*I)*f + 4*c*Log[f]))} * f^a * Sqrt[\pi] * (E^{((I/2)*e^2*f)/(f^2 + c^2*Log[f]^2)} * Erfi[(((-1)^{(3/4)} * (e + 2*f*x + (2*I)*c*x*Log[f])) / (2*Sqrt[f + I*c*Log[f]]))] * (f - I*c*Log[f]) * Sqrt[f + I*c*Log[f]] * (Cos[d] - I*Sin[d]) + Erfi[(((-1)^{(1/4)} * (e + 2*f*x - (2*I)*c*x*Log[f])) / (2*Sqrt[f - I*c*Log[f]]))] * Sqrt[f - I*c*Log[f]] * ((-I)*f + c*Log[f]) * (Cos[d] + I*Sin[d])) / (f^2 + c^2*Log[f]^2)$

fricas [B] time = 0.74, size = 299, normalized size = 1.60

$$\frac{\sqrt{\pi} (ic \log(f) + f) \sqrt{-c \log(f) - if} \operatorname{erf}\left(\frac{(2c^2x \log(f)^2 + 2f^2x + ice \log(f) + ef) \sqrt{-c \log(f) - if}}{2(c^2 \log(f)^2 + f^2)}\right) e^{\left(\frac{4ac^2 \log(f)^3 + 4ic^2d \log(f)^2 - ie^2f + 4id}{4(c^2 \log(f)^2 + f^2)}\right)}}{4(c^2 \log(f)^2 + f^2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(c*x^2+a)*sin(f*x^2+e*x+d),x, algorithm="fricas")

[Out] $1/4 * (\sqrt{\pi} * (I*c*\log(f) + f) * \sqrt{-c*\log(f) - I*f} * \operatorname{erf}(1/2 * (2*c^2*x*\log(f))^2 + 2*f^2*x + I*c*e*\log(f) + e*f) * \sqrt{-c*\log(f) - I*f} / (c^2*\log(f)^2 + f^2)) * e^{(1/4 * (4*a*c^2*\log(f)^3 + 4*I*c^2*d*\log(f)^2 - I*e^2*f + 4*I*d*f^2 + (c*e^2 + 4*a*f^2)*\log(f)) / (c^2*\log(f)^2 + f^2))} + \sqrt{\pi} * (-I*c*\log(f) + f) * \sqrt{-c*\log(f) + I*f} * \operatorname{erf}(1/2 * (2*c^2*x*\log(f))^2 + 2*f^2*x - I*c*e*\log(f) + e*f) * \sqrt{-c*\log(f) + I*f} / (c^2*\log(f)^2 + f^2)) * e^{(1/4 * (4*a*c^2*\log(f)^3 - 4*I*c^2*d*\log(f)^2 + I*e^2*f - 4*I*d*f^2 + (c*e^2 + 4*a*f^2)*\log(f)) / (c^2*\log(f)^2 + f^2))} / (c^2*\log(f)^2 + f^2)$

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int f^{cx^2+a} \sin(fx^2+ex+d) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(c*x^2+a)*sin(f*x^2+e*x+d),x, algorithm="giac")

[Out] integrate(f^(c*x^2 + a)*sin(f*x^2 + e*x + d), x)

maple [A] time = 0.72, size = 169, normalized size = 0.90

$$\frac{i\sqrt{\pi} f^a e^{\frac{-4df+4id \ln(f)c+e^2}{4f+4c \ln(f)}} \operatorname{erf}\left(-\sqrt{-if-c \ln(f)} x + \frac{ie}{2\sqrt{-if-c \ln(f)}}\right)}{4\sqrt{-if-c \ln(f)}} + \frac{i\sqrt{\pi} f^a e^{\frac{4df+4id \ln(f)c-e^2}{4(-if+c \ln(f))}} \operatorname{erf}\left(x\sqrt{if-c \ln(f)} + \frac{ie}{2\sqrt{if-c \ln(f)}}\right)}{4\sqrt{if-c \ln(f)}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(f^(c*x^2+a)*sin(f*x^2+e*x+d),x)

[Out] $\frac{1}{4} I \pi^{1/2} f^a \exp\left(\frac{1}{4} (-4d f + 4 I d \ln(f) c + e^2) / (I f + c \ln(f))\right) / (-I f - c \ln(f))^{1/2} \operatorname{erf}\left(-(-I f - c \ln(f))^{1/2} x + \frac{1}{2} I e / (-I f - c \ln(f))^{1/2}\right) + \frac{1}{4} I \pi^{1/2} f^a \exp\left(-\frac{1}{4} (4d f + 4 I d \ln(f) c - e^2) / (-I f + c \ln(f))\right) / (I f - c \ln(f))^{1/2} \operatorname{erf}\left(x (I f - c \ln(f))^{1/2} + \frac{1}{2} I e / (I f - c \ln(f))^{1/2}\right)$

maxima [B] time = 0.36, size = 760, normalized size = 4.06

$$\sqrt{\pi} \sqrt{2 c^2 \log(f)^2 + 2 f^2} \left(\left(f^{\frac{c^2}{4(c^2 \log(f)^2 + f^2)}} f^a \cos\left(\frac{4 c^2 d \log(f)^2 - e^2 f + 4 d f^2}{4(c^2 \log(f)^2 + f^2)}\right) - i f^{\frac{c^2}{4(c^2 \log(f)^2 + f^2)}} f^a \sin\left(\frac{4 c^2 d \log(f)^2 - e^2 f + 4 d f^2}{4(c^2 \log(f)^2 + f^2)}\right) \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(c*x^2+a)*sin(f*x^2+e*x+d),x, algorithm="maxima")

[Out] $-1/8 * (\sqrt{\pi} * \sqrt{2 * c^2 * \log(f)^2 + 2 * f^2}) * ((f^{1/4 * c * e^2 / (c^2 * \log(f)^2 + f^2)}) * f^a * \cos(1/4 * (4 * c^2 * d * \log(f)^2 - e^2 * f + 4 * d * f^2) / (c^2 * \log(f)^2 + f^2)) - I * f^{1/4 * c * e^2 / (c^2 * \log(f)^2 + f^2)}) * f^a * \sin(1/4 * (4 * c^2 * d * \log(f)^2 - e^2 * f + 4 * d * f^2) / (c^2 * \log(f)^2 + f^2))) * \operatorname{erf}(1/2 * (2 * (c * \log(f) - I * f) * x - I * e) / \sqrt{-c * \log(f) + I * f}) + (f^{1/4 * c * e^2 / (c^2 * \log(f)^2 + f^2)}) * f^a * \cos(1/4 * (4 * c^2 * d * \log(f)^2 - e^2 * f + 4 * d * f^2) / (c^2 * \log(f)^2 + f^2)) + I * f^{1/4 * c * e^2 / (c^2 * \log(f)^2 + f^2)}) * f^a * \sin(1/4 * (4 * c^2 * d * \log(f)^2 - e^2 * f + 4 * d * f^2) / (c^2 * \log(f)^2 + f^2))) * \operatorname{erf}(1/2 * (2 * (c * \log(f) + I * f) * x + I * e) / \sqrt{-c * \log(f) - I * f}) * \sqrt{c * \log(f) + \sqrt{c^2 * \log(f)^2 + f^2}} + \sqrt{\pi} * \sqrt{2 * c^2 * \log(f)^2 + 2 * f^2}) * ((I * f^{1/4 * c * e^2 / (c^2 * \log(f)^2 + f^2)}) * f^a * \cos(1/4 * (4 * c^2 * d * \log(f)^2 - e^2 * f + 4 * d * f^2) / (c^2 * \log(f)^2 + f^2)) + f^{1/4 * c * e^2 / (c^2 * \log(f)^2 + f^2)}) * f^a * \sin(1/4 * (4 * c^2 * d * \log(f)^2 - e^2 * f + 4 * d * f^2) / (c^2 * \log(f)^2 + f^2))) * \operatorname{erf}(1/2 * (2 * (c * \log(f) - I * f) * x - I * e) / \sqrt{-c * \log(f) + I * f}) + (-I * f^{1/4 * c * e^2 / (c^2 * \log(f)^2 + f^2)}) * f^a * \cos(1/4 * (4 * c^2 * d * \log(f)^2 - e^2 * f + 4 * d * f^2) / (c^2 * \log(f)^2 + f^2)) + f^{1/4 * c * e^2 / (c^2 * \log(f)^2 + f^2)}) * f^a * \sin(1/4 * (4 * c^2 * d * \log(f)^2 - e^2 * f + 4 * d * f^2) / (c^2 * \log(f)^2 + f^2))) * \operatorname{erf}(1/2 * (2 * (c * \log(f) + I * f) * x + I * e) / \sqrt{-c * \log(f) - I * f}) * \sqrt{-c * \log(f) + \sqrt{c^2 * \log(f)^2 + f^2}}) / (c^2 * \log(f)^2 + f^2)$

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int f^{c x^2 + a} \sin(f x^2 + e x + d) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(f^(a + c*x^2)*sin(d + e*x + f*x^2),x)

[Out] int(f^(a + c*x^2)*sin(d + e*x + f*x^2), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int f^{a+cx^2} \sin(d + ex + fx^2) dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(f**(c*x**2+a)*sin(f*x**2+e*x+d), x)
```

```
[Out] Integral(f**(a + c*x**2)*sin(d + e*x + f*x**2), x)
```

3.92 $\int f^{a+cx^2} \sin^2(d + ex + fx^2) dx$

Optimal. Leaf size=211

$$\frac{\sqrt{\pi} f^a e^{-\frac{e^2}{-c \log(f)+2if} - 2id} \operatorname{erf}\left(\frac{x(-c \log(f)+2if)+ie}{\sqrt{-c \log(f)+2if}}\right)}{8\sqrt{-c \log(f)+2if}} - \frac{\sqrt{\pi} f^a e^{\frac{e^2}{c \log(f)+2if} + 2id} \operatorname{erfi}\left(\frac{x(c \log(f)+2if)+ie}{\sqrt{c \log(f)+2if}}\right)}{8\sqrt{c \log(f)+2if}} + \frac{\sqrt{\pi} f^a \operatorname{erfi}\left(\sqrt{c} x \sqrt{\log(f)}\right)}{4\sqrt{c} \sqrt{\log(f)}}$$

[Out] $\frac{1}{4} f^a \operatorname{erfi}(x c^{1/2} \ln(f)^{1/2}) \pi^{1/2} / c^{1/2} / \ln(f)^{1/2} - \frac{1}{8} \exp(-2 * I * d - e^2 / (2 * I * f - c * \ln(f))) * f^a * \operatorname{erf}((I * e + x * (2 * I * f - c * \ln(f))) / (2 * I * f - c * \ln(f)))^{1/2} * \pi^{1/2} / (2 * I * f - c * \ln(f))^{1/2} - \frac{1}{8} \exp(2 * I * d + e^2 / (2 * I * f + c * \ln(f))) * f^a * \operatorname{erfi}((I * e + x * (2 * I * f + c * \ln(f))) / (2 * I * f + c * \ln(f)))^{1/2} * \pi^{1/2} / (2 * I * f + c * \ln(f))^{1/2}$

Rubi [A] time = 0.42, antiderivative size = 211, normalized size of antiderivative = 1.00, number of steps used = 9, number of rules used = 5, integrand size = 23, $\frac{\text{number of rules}}{\text{integrand size}} = 0.217$, Rules used = {4472, 2204, 2287, 2234, 2205}

$$\frac{\sqrt{\pi} f^a e^{-\frac{e^2}{-c \log(f)+2if} - 2id} \operatorname{Erf}\left(\frac{x(-c \log(f)+2if)+ie}{\sqrt{-c \log(f)+2if}}\right)}{8\sqrt{-c \log(f)+2if}} - \frac{\sqrt{\pi} f^a e^{\frac{e^2}{c \log(f)+2if} + 2id} \operatorname{Erfi}\left(\frac{x(c \log(f)+2if)+ie}{\sqrt{c \log(f)+2if}}\right)}{8\sqrt{c \log(f)+2if}} + \frac{\sqrt{\pi} f^a \operatorname{Erfi}\left(\sqrt{c} x \sqrt{\log(f)}\right)}{4\sqrt{c} \sqrt{\log(f)}}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[f^{(a + c*x^2)} * \operatorname{Sin}[d + e*x + f*x^2]^2, x]$

[Out] $(f^a * \operatorname{Sqrt}[\pi] * \operatorname{Erfi}[\operatorname{Sqrt}[c] * x * \operatorname{Sqrt}[\operatorname{Log}[f]]]) / (4 * \operatorname{Sqrt}[c] * \operatorname{Sqrt}[\operatorname{Log}[f]]) - (E^{(-2 * I) * d - e^2 / ((2 * I) * f - c * \operatorname{Log}[f])}) * f^a * \operatorname{Sqrt}[\pi] * \operatorname{Erf}[(I * e + x * ((2 * I) * f - c * \operatorname{Log}[f])) / \operatorname{Sqrt}[(2 * I) * f - c * \operatorname{Log}[f]]]) / (8 * \operatorname{Sqrt}[(2 * I) * f - c * \operatorname{Log}[f]]) - (E^{(2 * I) * d + e^2 / ((2 * I) * f + c * \operatorname{Log}[f])}) * f^a * \operatorname{Sqrt}[\pi] * \operatorname{Erfi}[(I * e + x * ((2 * I) * f + c * \operatorname{Log}[f])) / \operatorname{Sqrt}[(2 * I) * f + c * \operatorname{Log}[f]]]) / (8 * \operatorname{Sqrt}[(2 * I) * f + c * \operatorname{Log}[f]])$

Rule 2204

$\operatorname{Int}[(F_)^{((a_.) + (b_.) * ((c_.) + (d_.) * (x_)) ^ 2)}, x_Symbol] \rightarrow \operatorname{Simp}[(F^a * \operatorname{Sqrt}[\pi] * \operatorname{Erfi}[(c + d * x) * \operatorname{Rt}[b * \operatorname{Log}[F], 2]]) / (2 * d * \operatorname{Rt}[b * \operatorname{Log}[F], 2]), x] /;$ FreeQ[{F, a, b, c, d}, x] && PosQ[b]

Rule 2205

$\operatorname{Int}[(F_)^{((a_.) + (b_.) * ((c_.) + (d_.) * (x_)) ^ 2)}, x_Symbol] \rightarrow \operatorname{Simp}[(F^a * \operatorname{Sqrt}[\pi] * \operatorname{Erf}[(c + d * x) * \operatorname{Rt}[-(b * \operatorname{Log}[F]), 2]]) / (2 * d * \operatorname{Rt}[-(b * \operatorname{Log}[F]), 2]), x] /;$ FreeQ[{F, a, b, c, d}, x] && NegQ[b]

Rule 2234

$\operatorname{Int}[(F_)^{((a_.) + (b_.) * (x_) + (c_.) * (x_) ^ 2)}, x_Symbol] \rightarrow \operatorname{Dist}[F^{(a - b^2 / (4 * c))}, \operatorname{Int}[F^{((b + 2 * c * x) ^ 2 / (4 * c))}, x], x] /;$ FreeQ[{F, a, b, c}, x]

Rule 2287

$\operatorname{Int}[(u_) * (F_)^{(v_)} * (G_)^{(w_)}, x_Symbol] \rightarrow \operatorname{With}[\{z = v * \operatorname{Log}[F] + w * \operatorname{Log}[G]\}, \operatorname{Int}[u * \operatorname{NormalizeIntegrand}[E^z, x], x] /;$ BinomialQ[z, x] || (PolynomialQ[z, x] && LeQ[Exponent[z, x], 2]) /;

 FreeQ[{F, G}, x]

Rule 4472

$\operatorname{Int}[(F_)^{(u_)} * \operatorname{Sin}[v_]^{(n_.)}, x_Symbol] \rightarrow \operatorname{Int}[\operatorname{ExpandTrigToExp}[F^u, \operatorname{Sin}[v]^n], x] /;$ FreeQ[F, x] && (LinearQ[u, x] || PolyQ[u, x, 2]) && (LinearQ[v,

x] || PolyQ[v, x, 2]) && IGtQ[n, 0]

Rubi steps

$$\begin{aligned}
 \int f^{a+cx^2} \sin^2(d+ex+fx^2) dx &= \int \left(\frac{1}{2} f^{a+cx^2} - \frac{1}{4} e^{-2id-2iex-2ifx^2} f^{a+cx^2} - \frac{1}{4} e^{2id+2iex+2ifx^2} f^{a+cx^2} \right) dx \\
 &= -\left(\frac{1}{4} \int e^{-2id-2iex-2ifx^2} f^{a+cx^2} dx \right) - \frac{1}{4} \int e^{2id+2iex+2ifx^2} f^{a+cx^2} dx + \frac{1}{2} \int f^{a+cx^2} dx \\
 &= \frac{f^a \sqrt{\pi} \operatorname{erfi}(\sqrt{c} x \sqrt{\log(f)})}{4\sqrt{c} \sqrt{\log(f)}} - \frac{1}{4} \int \exp(-2id-2iex+a \log(f)-x^2(2if-c)) dx \\
 &= \frac{f^a \sqrt{\pi} \operatorname{erfi}(\sqrt{c} x \sqrt{\log(f)})}{4\sqrt{c} \sqrt{\log(f)}} - \frac{1}{4} \left(e^{-2id-\frac{e^2}{2if-c \log(f)}} f^a \right) \int \exp\left(\frac{(-2ie+2x(-2if-c))}{4(-2if-c)}\right) dx \\
 &= \frac{f^a \sqrt{\pi} \operatorname{erfi}(\sqrt{c} x \sqrt{\log(f)})}{4\sqrt{c} \sqrt{\log(f)}} - \frac{e^{-2id-\frac{e^2}{2if-c \log(f)}} f^a \sqrt{\pi} \operatorname{erf}\left(\frac{ie+x(2if-c \log(f))}{\sqrt{2if-c \log(f)}}\right)}{8\sqrt{2if-c \log(f)}} - \frac{e^{2id+\frac{e^2}{2if-c \log(f)}} f^a \sqrt{\pi} \operatorname{erf}\left(\frac{-ie+x(2if-c \log(f))}{\sqrt{2if-c \log(f)}}\right)}{8\sqrt{2if-c \log(f)}}
 \end{aligned}$$

Mathematica [A] time = 2.25, size = 251, normalized size = 1.19

$$\frac{1}{8} \sqrt{\pi} f^a \left(\frac{2 \operatorname{erfi}(\sqrt{c} x \sqrt{\log(f)})}{\sqrt{c} \sqrt{\log(f)}} + \frac{\sqrt[4]{-1} \left(\sqrt{2f-ic \log(f)} (2f+ic \log(f)) (\cos(2d) + i \sin(2d)) e^{\frac{e^2}{c \log(f)+2if}} \operatorname{erf}\left(\frac{(-1)^{3/4} (e+2fx-icx \log(f))}{\sqrt{2f-ic \log(f)}}\right)} + \sqrt{2f+ic \log(f)} (2f-ic \log(f)) (\cos(2d) - i \sin(2d)) e^{\frac{e^2}{c \log(f)+2if}} \operatorname{erf}\left(\frac{(-1)^{1/4} (e+2fx+icx \log(f))}{\sqrt{2f+ic \log(f)}}\right)} \right)}{(4f^2+c^2 \log(f)^2)} \right) / 8$$

Warning: Unable to verify antiderivative.

[In] Integrate[f^(a+c*x^2)*Sin[d+e*x+f*x^2]^2,x]

[Out] (f^a*Sqrt[Pi]*((2*Erfi[Sqrt[c]*x*Sqrt[Log[f]]])/(Sqrt[c]*Sqrt[Log[f]])) + ((-1)^(1/4)*(E^(e^2/((2*I)*f+c*Log[f]))*Erf[((-1)^(3/4)*(e+2*f*x-I*c*x*Log[f]))/Sqrt[2*f-I*c*Log[f]]]*Sqrt[2*f-I*c*Log[f]]*(2*f+I*c*Log[f])*(Cos[2*d]+I*Sin[2*d]) + E^(e^2/((-2*I)*f+c*Log[f]))*Erf[((-1)^(1/4)*(e+2*f*x+I*c*x*Log[f]))/Sqrt[2*f+I*c*Log[f]]]*(2*f-I*c*Log[f])*Sqrt[2*f+I*c*Log[f]]*(I*Cos[2*d]+Sin[2*d])))/(4*f^2+c^2*Log[f]^2)))/8

fricas [B] time = 0.70, size = 363, normalized size = 1.72

$$\frac{2\sqrt{\pi}(c^2 \log(f)^2 + 4f^2)\sqrt{-c \log(f)} f^a \operatorname{erf}(\sqrt{-c \log(f)} x) - \sqrt{\pi}(c^2 \log(f)^2 - 2icf \log(f))\sqrt{-c \log(f) - 2ifx}}{8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(c*x^2+a)*sin(f*x^2+e*x+d)^2,x, algorithm="fricas")

[Out] -1/8*(2*sqrt(pi)*(c^2*log(f)^2+4*f^2)*sqrt(-c*log(f))*f^a*erf(sqrt(-c*log(f))*x) - sqrt(pi)*(c^2*log(f)^2-2*I*c*f*log(f))*sqrt(-c*log(f)-2*I*f)*erf((c^2*x*log(f)^2+4*f^2*x+I*c*e*log(f)+2*e*f)*sqrt(-c*log(f)-2*I*f)/(c^2*log(f)^2+4*f^2))*e^((a*c^2*log(f)^3+2*I*c^2*d*log(f)^2-2*I*e^2*f+8*I*d*f^2+(c*e^2+4*a*f^2)*log(f))/(c^2*log(f)^2+4*f^2)) - sqrt(pi)*(c^2*log(f)^2+2*I*c*f*log(f))*sqrt(-c*log(f)+2*I*f)*erf((c^2*x*log(f)^2+4*f^2*x-I*c*e*log(f)+2*e*f)*sqrt(-c*log(f)+2*I*f)/(c^2*log(f)^2+4*f^2))*e^((a*c^2*log(f)^3-2*I*c^2*d*log(f)^2+2*I*e^2*f-8*I*d*f^2+(c*e^2+4*a*f^2)*log(f))/(c^2*log(f)^2+4*f^2)))/(c^3*log(f)^3+4*c*f^2*log(f))

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int f^{cx^2+a} \sin(fx^2 + ex + d)^2 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(c*x^2+a)*sin(f*x^2+e*x+d)^2,x, algorithm="giac")

[Out] integrate(f^(c*x^2 + a)*sin(f*x^2 + e*x + d)^2, x)

maple [A] time = 0.65, size = 191, normalized size = 0.91

$$\frac{\sqrt{\pi} f^a e^{-\frac{2id \ln(f)c+4df-e^2}{-2if+c \ln(f)}} \operatorname{erf}\left(x\sqrt{2if-c \ln(f)} + \frac{ie}{\sqrt{2if-c \ln(f)}}\right)}{8\sqrt{2if-c \ln(f)}} + \frac{\sqrt{\pi} f^a e^{\frac{2id \ln(f)c-4df+e^2}{2if+c \ln(f)}} \operatorname{erf}\left(-\sqrt{-2if-c \ln(f)} x + \frac{ie}{\sqrt{-2if-c \ln(f)}}\right)}{8\sqrt{-2if-c \ln(f)}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(f^(c*x^2+a)*sin(f*x^2+e*x+d)^2,x)

[Out] $-1/8*\pi^{(1/2)}*f^a*\exp(-(2*I*d*\ln(f)*c+4*d*f-e^2)/(-2*I*f+c*\ln(f)))/(2*I*f-c*\ln(f))^{(1/2)}*\operatorname{erf}(x*(2*I*f-c*\ln(f))^{(1/2)}+I*e/(2*I*f-c*\ln(f))^{(1/2)})+1/8*\pi^{(1/2)}*f^a*\exp((2*I*d*\ln(f)*c-4*d*f+e^2)/(2*I*f+c*\ln(f)))/(-2*I*f-c*\ln(f))^{(1/2)}*\operatorname{erf}(-(-2*I*f-c*\ln(f))^{(1/2)}*x+I*e/(-2*I*f-c*\ln(f))^{(1/2)})+1/4*f^a*\pi^{(1/2)}/(-c*\ln(f))^{(1/2)}*\operatorname{erf}((-c*\ln(f))^{(1/2)}*x)$

maxima [C] time = 0.38, size = 863, normalized size = 4.09

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(c*x^2+a)*sin(f*x^2+e*x+d)^2,x, algorithm="maxima")

[Out] $-1/16*(\operatorname{sqrt}(\pi)*\operatorname{sqrt}(2*c^2*\log(f)^2 + 8*f^2))*((I*f^(c*e^2/(c^2*\log(f)^2 + 4*f^2)))*f^a*\cos(2*(c^2*d*\log(f)^2 - e^2*f + 4*d*f^2)/(c^2*\log(f)^2 + 4*f^2)) + f^(c*e^2/(c^2*\log(f)^2 + 4*f^2))*f^a*\sin(2*(c^2*d*\log(f)^2 - e^2*f + 4*d*f^2)/(c^2*\log(f)^2 + 4*f^2)))*\operatorname{erf}(((c*\log(f) - 2*I*f)*x - I*e)/\operatorname{sqrt}(-c*\log(f) + 2*I*f)) + (-I*f^(c*e^2/(c^2*\log(f)^2 + 4*f^2))*f^a*\cos(2*(c^2*d*\log(f)^2 - e^2*f + 4*d*f^2)/(c^2*\log(f)^2 + 4*f^2)) + f^(c*e^2/(c^2*\log(f)^2 + 4*f^2))*f^a*\sin(2*(c^2*d*\log(f)^2 - e^2*f + 4*d*f^2)/(c^2*\log(f)^2 + 4*f^2)))*\operatorname{erf}(((c*\log(f) + 2*I*f)*x + I*e)/\operatorname{sqrt}(-c*\log(f) - 2*I*f)))*\operatorname{sqrt}(c*\log(f) + \operatorname{sqrt}(c^2*\log(f)^2 + 4*f^2))*\operatorname{sqrt}(-c*\log(f)) - \operatorname{sqrt}(\pi)*\operatorname{sqrt}(2*c^2*\log(f)^2 + 8*f^2))*((f^(c*e^2/(c^2*\log(f)^2 + 4*f^2))*f^a*\cos(2*(c^2*d*\log(f)^2 - e^2*f + 4*d*f^2)/(c^2*\log(f)^2 + 4*f^2)) - I*f^(c*e^2/(c^2*\log(f)^2 + 4*f^2))*f^a*\sin(2*(c^2*d*\log(f)^2 - e^2*f + 4*d*f^2)/(c^2*\log(f)^2 + 4*f^2)))*\operatorname{erf}(((c*\log(f) - 2*I*f)*x - I*e)/\operatorname{sqrt}(-c*\log(f) + 2*I*f)) + (f^(c*e^2/(c^2*\log(f)^2 + 4*f^2))*f^a*\cos(2*(c^2*d*\log(f)^2 - e^2*f + 4*d*f^2)/(c^2*\log(f)^2 + 4*f^2)) + I*f^(c*e^2/(c^2*\log(f)^2 + 4*f^2))*f^a*\sin(2*(c^2*d*\log(f)^2 - e^2*f + 4*d*f^2)/(c^2*\log(f)^2 + 4*f^2)))*\operatorname{erf}(((c*\log(f) + 2*I*f)*x + I*e)/\operatorname{sqrt}(-c*\log(f) - 2*I*f)))*\operatorname{sqrt}(-c*\log(f) + \operatorname{sqrt}(c^2*\log(f)^2 + 4*f^2))*\operatorname{sqrt}(-c*\log(f)) - 2*\operatorname{sqrt}(\pi))*((c^2*f^a*\log(f)^2 + 4*f^(a+2))*\operatorname{erf}(x*\operatorname{conjugate}(\operatorname{sqrt}(-c*\log(f)))) + (c^2*f^a*\log(f)^2 + 4*f^(a+2))*\operatorname{erf}(\operatorname{sqrt}(-c*\log(f))*x)))/((c^2*\log(f)^2 + 4*f^2)*\operatorname{sqrt}(-c*\log(f)))$

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int f^{cx^2+a} \sin(fx^2 + ex + d)^2 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(f^(a + c*x^2)*sin(d + e*x + f*x^2)^2,x)`

[Out] `int(f^(a + c*x^2)*sin(d + e*x + f*x^2)^2, x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int f^{a+cx^2} \sin^2(d + ex + fx^2) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(f**(c*x**2+a)*sin(f*x**2+e*x+d)**2,x)`

[Out] `Integral(f**(a + c*x**2)*sin(d + e*x + f*x**2)**2, x)`

3.93 $\int f^{a+cx^2} \sin^3(d+ex+fx^2) dx$

Optimal. Leaf size=377

$$\frac{i\sqrt{\pi} f^a \exp\left(-\frac{9e^2}{4(-c\log(f)+3if)} - 3id\right) \operatorname{erf}\left(\frac{2x(-c\log(f)+3if)+3ie}{2\sqrt{-c\log(f)+3if}}\right)}{16\sqrt{-c\log(f)+3if}} + \frac{3i\sqrt{\pi} f^a e^{-\frac{e^2}{-4c\log(f)+4if} - id} \operatorname{erf}\left(\frac{2x(-c\log(f)+if)+ie}{2\sqrt{-c\log(f)+if}}\right)}{16\sqrt{-c\log(f)+if}} - \frac{3i\sqrt{\pi}}{16\sqrt{-c\log(f)+if}}$$

[Out] $\frac{3}{16} I \exp(-I d - e^2 / (4 I f - 4 c \ln(f))) f^a \operatorname{erf}(1/2 (I e + 2 x (I f - c \ln(f)))) / (I f - c \ln(f))^{1/2} \pi^{1/2} / (I f - c \ln(f))^{1/2} - 1/16 I \exp(-3 I d - 9/4 e^2 / (3 I f - c \ln(f))) f^a \operatorname{erf}(1/2 (3 I e + 2 x (3 I f - c \ln(f)))) / (3 I f - c \ln(f))^{1/2} \pi^{1/2} / (3 I f - c \ln(f))^{1/2} - 3/16 I \exp(I d + e^2 / (4 I f + 4 c \ln(f))) f^a \operatorname{erfi}(1/2 (I e + 2 x (I f + c \ln(f)))) / (I f + c \ln(f))^{1/2} \pi^{1/2} / (I f + c \ln(f))^{1/2} + 1/16 I \exp(3 I d + 9/4 e^2 / (3 I f + c \ln(f))) f^a \operatorname{erfi}(1/2 (3 I e + 2 x (3 I f + c \ln(f)))) / (3 I f + c \ln(f))^{1/2} \pi^{1/2} / (3 I f + c \ln(f))^{1/2}$

Rubi [A] time = 0.66, antiderivative size = 377, normalized size of antiderivative = 1.00, number of steps used = 14, number of rules used = 5, integrand size = 23, $\frac{\text{number of rules}}{\text{integrand size}} = 0.217$, Rules used = {4472, 2287, 2234, 2205, 2204}

$$\frac{i\sqrt{\pi} f^a \exp\left(-\frac{9e^2}{4(-c\log(f)+3if)} - 3id\right) \operatorname{Erf}\left(\frac{2x(-c\log(f)+3if)+3ie}{2\sqrt{-c\log(f)+3if}}\right)}{16\sqrt{-c\log(f)+3if}} + \frac{3i\sqrt{\pi} f^a e^{-\frac{e^2}{-4c\log(f)+4if} - id} \operatorname{Erf}\left(\frac{2x(-c\log(f)+if)+ie}{2\sqrt{-c\log(f)+if}}\right)}{16\sqrt{-c\log(f)+if}} - \frac{3i\sqrt{\pi}}{16\sqrt{-c\log(f)+if}}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[f^{(a + c*x^2)} \operatorname{Sin}[d + e*x + f*x^2]^3, x]$

[Out] $((3 I / 16) E^{(-I) d - e^2 / ((4 I) f - 4 c \operatorname{Log}[f])} f^a \operatorname{Sqrt}[\pi] \operatorname{Erf}[(I e + 2 x (I f - c \operatorname{Log}[f])) / (2 \operatorname{Sqrt}[I f - c \operatorname{Log}[f]])] / \operatorname{Sqrt}[I f - c \operatorname{Log}[f]] - ((I / 16) E^{(-3 I) d - (9 e^2) / (4 ((3 I) f - c \operatorname{Log}[f]))} f^a \operatorname{Sqrt}[\pi] \operatorname{Erf}[(3 I) e + 2 x ((3 I) f - c \operatorname{Log}[f])) / (2 \operatorname{Sqrt}[(3 I) f - c \operatorname{Log}[f]])] / \operatorname{Sqrt}[(3 I) f - c \operatorname{Log}[f]] - ((3 I / 16) E^{I d + e^2 / ((4 I) f + 4 c \operatorname{Log}[f])} f^a \operatorname{Sqrt}[\pi] \operatorname{Erfi}[(I e + 2 x (I f + c \operatorname{Log}[f])) / (2 \operatorname{Sqrt}[I f + c \operatorname{Log}[f]])] / \operatorname{Sqrt}[I f + c \operatorname{Log}[f]] + ((I / 16) E^{(3 I) d + (9 e^2) / (4 ((3 I) f + c \operatorname{Log}[f]))} f^a \operatorname{Sqrt}[\pi] \operatorname{Erfi}[(3 I) e + 2 x ((3 I) f + c \operatorname{Log}[f])) / (2 \operatorname{Sqrt}[(3 I) f + c \operatorname{Log}[f]])] / \operatorname{Sqrt}[(3 I) f + c \operatorname{Log}[f]])$

Rule 2204

$\operatorname{Int}[(F_)^{(a_. + (b_.)((c_.) + (d_.)(x_)) ^2)}, x_Symbol] \rightarrow \operatorname{Simp}[(F^a \operatorname{Sqrt}[\pi] \operatorname{Erfi}[(c + d x) \operatorname{Rt}[b \operatorname{Log}[F], 2]]) / (2 d \operatorname{Rt}[b \operatorname{Log}[F], 2]), x] /; \operatorname{FreeQ}\{F, a, b, c, d\}, x] \&\& \operatorname{PosQ}[b]$

Rule 2205

$\operatorname{Int}[(F_)^{(a_. + (b_.)((c_.) + (d_.)(x_)) ^2)}, x_Symbol] \rightarrow \operatorname{Simp}[(F^a \operatorname{Sqrt}[\pi] \operatorname{Erf}[(c + d x) \operatorname{Rt}[-(b \operatorname{Log}[F]), 2]]) / (2 d \operatorname{Rt}[-(b \operatorname{Log}[F]), 2]), x] /; \operatorname{FreeQ}\{F, a, b, c, d\}, x] \&\& \operatorname{NegQ}[b]$

Rule 2234

$\operatorname{Int}[(F_)^{(a_. + (b_.)(x_) + (c_.)(x_) ^2)}, x_Symbol] \rightarrow \operatorname{Dist}[F^{(a - b^2 / (4 c))}, \operatorname{Int}[F^{((b + 2 c x)^2 / (4 c))}, x], x] /; \operatorname{FreeQ}\{F, a, b, c\}, x]$

Rule 2287

$\operatorname{Int}[(u_)(F_)^{(v_)}(G_)^{(w_)}, x_Symbol] \rightarrow \operatorname{With}\{z = v \operatorname{Log}[F] + w \operatorname{Log}[G]\}, \operatorname{Int}[u \operatorname{NormalizeIntegrand}[E^z, x], x] /; \operatorname{BinomialQ}[z, x] \mid\mid (\operatorname{PolynomialQ}[z,$

x] && LeQ[Exponent[z, x], 2]]) /; FreeQ[{F, G}, x]

Rule 4472

Int[(F_)^(u_)*Sin[v_]^(n_.), x_Symbol] :> Int[ExpandTrigToExp[F^u, Sin[v]^n, x], x] /; FreeQ[F, x] && (LinearQ[u, x] || PolyQ[u, x, 2]) && (LinearQ[v, x] || PolyQ[v, x, 2]) && IGtQ[n, 0]

Rubi steps

$$\begin{aligned} \int f^{a+cx^2} \sin^3(d+ex+fx^2) dx &= \int \left(-\frac{1}{8} i e^{-3i(d+ex+fx^2)} f^{a+cx^2} + \frac{3}{8} i \exp(2id+2iex+2ifx^2-3i(d+ex+fx^2)) \right. \\ &= -\left(\frac{1}{8} i \int e^{-3i(d+ex+fx^2)} f^{a+cx^2} dx \right) + \frac{1}{8} i \int \exp(6id+6iex+6ifx^2-3i(d+ex+fx^2)) dx \\ &= -\left(\frac{1}{8} i \int \exp(-3id-3iex+a \log(f)-x^2(3if-c \log(f))) dx \right) + \frac{1}{8} i \int \exp(6id+6iex+6ifx^2-3i(d+ex+fx^2)) dx \\ &= \frac{1}{8} \left(3ie^{-id-\frac{e^2}{4if-4c \log(f)}} f^a \right) \int \exp\left(\frac{(-ie+2x(-if+c \log(f)))^2}{4(-if+c \log(f))}\right) dx - \frac{1}{8} \left(ie^{-3id-\frac{9e^2}{4(3if-c \log(f))}} f^a \right) \int \exp\left(\frac{(-ie+2x(-if+c \log(f)))^2}{4(-if+c \log(f))}\right) dx \\ &= \frac{3ie^{-id-\frac{e^2}{4if-4c \log(f)}} f^a \sqrt{\pi} \operatorname{erf}\left(\frac{ie+2x(if-c \log(f))}{2\sqrt{if-c \log(f)}}\right)}{16\sqrt{if-c \log(f)}} - \frac{ie^{-3id-\frac{9e^2}{4(3if-c \log(f))}} f^a \sqrt{\pi} \operatorname{erf}\left(\frac{3ie+2x(3if-c \log(f))}{2\sqrt{3if-c \log(f)}}\right)}{16\sqrt{3if-c \log(f)}} \end{aligned}$$

Mathematica [A] time = 6.68, size = 490, normalized size = 1.30

$$\frac{\sqrt[4]{-1} \sqrt{\pi} f^a \left((f - ic \log(f)) \left(\sqrt{3f - ic \log(f)} (-c^2 \log^2(f) + 4icf \log(f) + 3f^2) (\cos(3d) + i \sin(3d)) e^{\frac{9e^2}{4(c \log(f) + 3e^2)}} \right) \right)}{16\sqrt{if-c \log(f)}} - \frac{ie^{-3id-\frac{9e^2}{4(3if-c \log(f))}} f^a \sqrt{\pi} \operatorname{erf}\left(\frac{3ie+2x(3if-c \log(f))}{2\sqrt{3if-c \log(f)}}\right)}{16\sqrt{3if-c \log(f)}}$$

Warning: Unable to verify antiderivative.

[In] Integrate[f^(a + c*x^2)*Sin[d + e*x + f*x^2]^3,x]

[Out] $((-1)^{(1/4)} f^a \sqrt{\pi} (-3E^{(e^2/((4I)f + 4c \log[f]))} \operatorname{Erfi}[\frac{(-1)^{(1/4)}(e + 2fx - (2I)c \log[f])}{2\sqrt{f - I c \log[f]}}] \sqrt{f - I c \log[f]} (9f^3 + (9I)c f^2 \log[f] + c^2 f \log[f]^2 + I c^3 \log[f]^3) (\cos[d] + I \sin[d]) + (f - I c \log[f]) (E^{((9e^2)/(4((3I)f + c \log[f]))})} \operatorname{Erfi}[\frac{(-1)^{(1/4)}(3e + 6fx - (2I)c \log[f])}{2\sqrt{3f - I c \log[f]}}] \sqrt{3f - I c \log[f]} (3f^2 + (4I)c f \log[f] - c^2 \log[f]^2) (\cos[3d] + I \sin[3d]) + (3f - I c \log[f]) (3E^{(e^2/((-4I)f + 4c \log[f]))} \operatorname{Erfi}[\frac{(-1)^{(3/4)}(e + 2fx + (2I)c \log[f])}{2\sqrt{f + I c \log[f]}}] \sqrt{f + I c \log[f]} ((-3I)f + c \log[f]) (\cos[d] - I \sin[d]) + E^{((9e^2)/(4((-3I)f + c \log[f]))})} \operatorname{Erfi}[\frac{(-1)^{(3/4)}(3e + 6fx + (2I)c \log[f])}{2\sqrt{3f + I c \log[f]}}] (f + I c \log[f]) \sqrt{3f + I c \log[f]} (I \cos[3d] + \sin[3d])))))/(16(9f^4 + 10c^2 f^2 \log[f]^2 + c^4 \log[f]^4))$

fricas [B] time = 0.76, size = 711, normalized size = 1.89

$$\frac{\sqrt{\pi} (-ic^3 \log(f)^3 - 3c^2 f \log(f)^2 - icf^2 \log(f) - 3f^3) \sqrt{-c \log(f) - 3if} \operatorname{erf}\left(\frac{(2c^2 x \log(f)^2 + 18f^2 x + 3ice \log(f) + 9ef)}{2(c^2 \log(f)^2 + 9f^2)}\right)}{16\sqrt{if-c \log(f)}} - \frac{ie^{-3id-\frac{9e^2}{4(3if-c \log(f))}} f^a \sqrt{\pi} \operatorname{erf}\left(\frac{3ie+2x(3if-c \log(f))}{2\sqrt{3if-c \log(f)}}\right)}{16\sqrt{3if-c \log(f)}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(c*x^2+a)*sin(f*x^2+e*x+d)^3,x, algorithm="fricas")

```
[Out] 1/16*(sqrt(pi)*(-I*c^3*log(f)^3 - 3*c^2*f*log(f)^2 - I*c*f^2*log(f) - 3*f^3
)*sqrt(-c*log(f) - 3*I*f)*erf(1/2*(2*c^2*x*log(f)^2 + 18*f^2*x + 3*I*c*e*lo
g(f) + 9*e*f)*sqrt(-c*log(f) - 3*I*f)/(c^2*log(f)^2 + 9*f^2))*e^(1/4*(4*a*c
^2*log(f)^3 + 12*I*c^2*d*log(f)^2 - 27*I*e^2*f + 108*I*d*f^2 + 9*(c*e^2 + 4
*a*f^2)*log(f))/(c^2*log(f)^2 + 9*f^2)) + sqrt(pi)*(I*c^3*log(f)^3 - 3*c^2*
f*log(f)^2 + I*c*f^2*log(f) - 3*f^3)*sqrt(-c*log(f) + 3*I*f)*erf(1/2*(2*c^2
*x*log(f)^2 + 18*f^2*x - 3*I*c*e*log(f) + 9*e*f)*sqrt(-c*log(f) + 3*I*f)/(c
^2*log(f)^2 + 9*f^2))*e^(1/4*(4*a*c^2*log(f)^3 - 12*I*c^2*d*log(f)^2 + 27*I
*e^2*f - 108*I*d*f^2 + 9*(c*e^2 + 4*a*f^2)*log(f))/(c^2*log(f)^2 + 9*f^2))
+ sqrt(pi)*(3*I*c^3*log(f)^3 + 3*c^2*f*log(f)^2 + 27*I*c*f^2*log(f) + 27*f^
3)*sqrt(-c*log(f) - I*f)*erf(1/2*(2*c^2*x*log(f)^2 + 2*f^2*x + I*c*e*log(f)
+ e*f)*sqrt(-c*log(f) - I*f)/(c^2*log(f)^2 + f^2))*e^(1/4*(4*a*c^2*log(f)^
3 + 4*I*c^2*d*log(f)^2 - I*e^2*f + 4*I*d*f^2 + (c*e^2 + 4*a*f^2)*log(f))/(c
^2*log(f)^2 + f^2)) + sqrt(pi)*(-3*I*c^3*log(f)^3 + 3*c^2*f*log(f)^2 - 27*I
*c*f^2*log(f) + 27*f^3)*sqrt(-c*log(f) + I*f)*erf(1/2*(2*c^2*x*log(f)^2 + 2
*f^2*x - I*c*e*log(f) + e*f)*sqrt(-c*log(f) + I*f)/(c^2*log(f)^2 + f^2))*e^
(1/4*(4*a*c^2*log(f)^3 - 4*I*c^2*d*log(f)^2 + I*e^2*f - 4*I*d*f^2 + (c*e^2
+ 4*a*f^2)*log(f))/(c^2*log(f)^2 + f^2)))/(c^4*log(f)^4 + 10*c^2*f^2*log(f)
^2 + 9*f^4)
```

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int f^{cx^2+a} \sin(fx^2 + ex + d)^3 dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(f^(c*x^2+a)*sin(f*x^2+e*x+d)^3,x, algorithm="giac")
```

```
[Out] integrate(f^(c*x^2 + a)*sin(f*x^2 + e*x + d)^3, x)
```

maple [A] time = 1.17, size = 338, normalized size = 0.90

$$\frac{i\sqrt{\pi} f^a e^{\frac{3id \ln(f)c - 9df + 9e^2}{4}} \operatorname{erf}\left(-\sqrt{-c \ln(f) - 3if} x + \frac{3ie}{2\sqrt{-c \ln(f) - 3if}}\right)}{16\sqrt{-c \ln(f) - 3if}} - \frac{i\sqrt{\pi} f^a e^{\frac{3(4id \ln(f)c + 12df - 3e^2)}{4(-3if + c \ln(f))}} \operatorname{erf}\left(x\sqrt{3if - c \ln(f)}\right)}{16\sqrt{3if - c \ln(f)}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(f^(c*x^2+a)*sin(f*x^2+e*x+d)^3,x)
```

```
[Out] -1/16*I*Pi^(1/2)*f^a*exp(3/4*(4*I*d*ln(f)*c-12*d*f+3*e^2)/(3*I*f+c*ln(f)))/
(-c*ln(f)-3*I*f)^(1/2)*erf((-c*ln(f)-3*I*f)^(1/2)*x+3/2*I*e/(-c*ln(f)-3*I*
f)^(1/2))-1/16*I*Pi^(1/2)*f^a*exp(-3/4*(4*I*d*ln(f)*c+12*d*f-3*e^2)/(-3*I*f
+c*ln(f)))/(3*I*f-c*ln(f))^(1/2)*erf(x*(3*I*f-c*ln(f))^(1/2)+3/2*I*e/(3*I*f
-c*ln(f))^(1/2))+3/16*I*Pi^(1/2)*f^a*exp(-1/4*(4*d*f+4*I*d*ln(f)*c-e^2)/(-I
*f+c*ln(f)))/(I*f-c*ln(f))^(1/2)*erf(x*(I*f-c*ln(f))^(1/2)+1/2*I*e/(I*f-c*l
n(f))^(1/2))+3/16*I*Pi^(1/2)*f^a*exp(1/4*(-4*d*f+4*I*d*ln(f)*c+e^2)/(I*f+c*
ln(f)))/(-I*f-c*ln(f))^(1/2)*erf(-(-I*f-c*ln(f))^(1/2)*x+1/2*I*e/(-I*f-c*ln
(f))^(1/2))
```

maxima [B] time = 0.44, size = 2180, normalized size = 5.78

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(f^(c*x^2+a)*sin(f*x^2+e*x+d)^3,x, algorithm="maxima")
```

```
[Out] 1/32*(sqrt(pi)*sqrt(2*c^2*log(f)^2 + 18*f^2)*(((c^2*f^(9/4*c*e^2/(c^2*log(f)
)^2 + 9*f^2))*f^a*log(f)^2 + f^(9/4*c*e^2/(c^2*log(f)^2 + 9*f^2))*f^(a + 2)
```

```

)*cos(3/4*(4*c^2*d*log(f)^2 - 9*e^2*f + 36*d*f^2)/(c^2*log(f)^2 + 9*f^2)) +
(-I*c^2*f^(9/4*c*e^2/(c^2*log(f)^2 + 9*f^2))*f^a*log(f)^2 - I*f^(9/4*c*e^2
/(c^2*log(f)^2 + 9*f^2))*f^(a + 2))*sin(3/4*(4*c^2*d*log(f)^2 - 9*e^2*f + 3
6*d*f^2)/(c^2*log(f)^2 + 9*f^2)))*erf(1/2*(2*(c*log(f) - 3*I*f)*x - 3*I*e)/
sqrt(-c*log(f) + 3*I*f)) + ((c^2*f^(9/4*c*e^2/(c^2*log(f)^2 + 9*f^2))*f^a*log
(f)^2 + f^(9/4*c*e^2/(c^2*log(f)^2 + 9*f^2))*f^(a + 2))*cos(3/4*(4*c^2*d*
log(f)^2 - 9*e^2*f + 36*d*f^2)/(c^2*log(f)^2 + 9*f^2)) + (I*c^2*f^(9/4*c*e^
2/(c^2*log(f)^2 + 9*f^2))*f^a*log(f)^2 + I*f^(9/4*c*e^2/(c^2*log(f)^2 + 9*f
^2))*f^(a + 2))*sin(3/4*(4*c^2*d*log(f)^2 - 9*e^2*f + 36*d*f^2)/(c^2*log(f)
^2 + 9*f^2)))*erf(1/2*(2*(c*log(f) + 3*I*f)*x + 3*I*e)/sqrt(-c*log(f) - 3*I
*f)))*sqrt(c*log(f) + sqrt(c^2*log(f)^2 + 9*f^2)) - sqrt(pi)*sqrt(2*c^2*log
(f)^2 + 2*f^2)*((3*(c^2*f^(1/4*c*e^2/(c^2*log(f)^2 + f^2))*f^a*log(f)^2 + 9
*f^(1/4*c*e^2/(c^2*log(f)^2 + f^2))*f^(a + 2))*cos(1/4*(4*c^2*d*log(f)^2 -
e^2*f + 4*d*f^2)/(c^2*log(f)^2 + f^2)) - (3*I*c^2*f^(1/4*c*e^2/(c^2*log(f)^
2 + f^2))*f^a*log(f)^2 + 27*I*f^(1/4*c*e^2/(c^2*log(f)^2 + f^2))*f^(a + 2))
*sin(1/4*(4*c^2*d*log(f)^2 - e^2*f + 4*d*f^2)/(c^2*log(f)^2 + f^2)))*erf(1/
2*(2*(c*log(f) - I*f)*x - I*e)/sqrt(-c*log(f) + I*f)) + (3*(c^2*f^(1/4*c*e^
2/(c^2*log(f)^2 + f^2))*f^a*log(f)^2 + 9*f^(1/4*c*e^2/(c^2*log(f)^2 + f^2))
*f^(a + 2))*cos(1/4*(4*c^2*d*log(f)^2 - e^2*f + 4*d*f^2)/(c^2*log(f)^2 + f^
2)) - (-3*I*c^2*f^(1/4*c*e^2/(c^2*log(f)^2 + f^2))*f^a*log(f)^2 - 27*I*f^(1
/4*c*e^2/(c^2*log(f)^2 + f^2))*f^(a + 2))*sin(1/4*(4*c^2*d*log(f)^2 - e^2*f
+ 4*d*f^2)/(c^2*log(f)^2 + f^2)))*erf(1/2*(2*(c*log(f) + I*f)*x + I*e)/sqr
t(-c*log(f) - I*f)))*sqrt(c*log(f) + sqrt(c^2*log(f)^2 + f^2)) + sqrt(pi)*s
qrt(2*c^2*log(f)^2 + 18*f^2)*(((I*c^2*f^(9/4*c*e^2/(c^2*log(f)^2 + 9*f^2))*
f^a*log(f)^2 + I*f^(9/4*c*e^2/(c^2*log(f)^2 + 9*f^2))*f^(a + 2))*cos(3/4*(4
*c^2*d*log(f)^2 - 9*e^2*f + 36*d*f^2)/(c^2*log(f)^2 + 9*f^2)) + (c^2*f^(9/4
*c*e^2/(c^2*log(f)^2 + 9*f^2))*f^a*log(f)^2 + f^(9/4*c*e^2/(c^2*log(f)^2 +
9*f^2))*f^(a + 2))*sin(3/4*(4*c^2*d*log(f)^2 - 9*e^2*f + 36*d*f^2)/(c^2*log
(f)^2 + 9*f^2)))*erf(1/2*(2*(c*log(f) - 3*I*f)*x - 3*I*e)/sqrt(-c*log(f) +
3*I*f)) + ((-I*c^2*f^(9/4*c*e^2/(c^2*log(f)^2 + 9*f^2))*f^a*log(f)^2 - I*f^
(9/4*c*e^2/(c^2*log(f)^2 + 9*f^2))*f^(a + 2))*cos(3/4*(4*c^2*d*log(f)^2 - 9
*e^2*f + 36*d*f^2)/(c^2*log(f)^2 + 9*f^2)) + (c^2*f^(9/4*c*e^2/(c^2*log(f)^
2 + 9*f^2))*f^a*log(f)^2 + f^(9/4*c*e^2/(c^2*log(f)^2 + 9*f^2))*f^(a + 2))*
sin(3/4*(4*c^2*d*log(f)^2 - 9*e^2*f + 36*d*f^2)/(c^2*log(f)^2 + 9*f^2)))*er
f(1/2*(2*(c*log(f) + 3*I*f)*x + 3*I*e)/sqrt(-c*log(f) - 3*I*f)))*sqrt(-c*lo
g(f) + sqrt(c^2*log(f)^2 + 9*f^2)) + sqrt(pi)*sqrt(2*c^2*log(f)^2 + 2*f^2)*
(((3*I*c^2*f^(1/4*c*e^2/(c^2*log(f)^2 + f^2))*f^a*log(f)^2 - 27*I*f^(1/4*c
*e^2/(c^2*log(f)^2 + f^2))*f^(a + 2))*cos(1/4*(4*c^2*d*log(f)^2 - e^2*f + 4
*d*f^2)/(c^2*log(f)^2 + f^2)) - 3*(c^2*f^(1/4*c*e^2/(c^2*log(f)^2 + f^2))*f
^a*log(f)^2 + 9*f^(1/4*c*e^2/(c^2*log(f)^2 + f^2))*f^(a + 2))*sin(1/4*(4*c^
2*d*log(f)^2 - e^2*f + 4*d*f^2)/(c^2*log(f)^2 + f^2)))*erf(1/2*(2*(c*log(f)
- I*f)*x - I*e)/sqrt(-c*log(f) + I*f)) + ((3*I*c^2*f^(1/4*c*e^2/(c^2*log(f)
)^2 + f^2))*f^a*log(f)^2 + 27*I*f^(1/4*c*e^2/(c^2*log(f)^2 + f^2))*f^(a + 2
))*cos(1/4*(4*c^2*d*log(f)^2 - e^2*f + 4*d*f^2)/(c^2*log(f)^2 + f^2)) - 3*(
c^2*f^(1/4*c*e^2/(c^2*log(f)^2 + f^2))*f^a*log(f)^2 + 9*f^(1/4*c*e^2/(c^2*log
(f)^2 + f^2))*f^(a + 2))*sin(1/4*(4*c^2*d*log(f)^2 - e^2*f + 4*d*f^2)/(c^
2*log(f)^2 + f^2)))*erf(1/2*(2*(c*log(f) + I*f)*x + I*e)/sqrt(-c*log(f) - I
*f)))*sqrt(-c*log(f) + sqrt(c^2*log(f)^2 + f^2)))/(c^4*log(f)^4 + 10*c^2*f^
2*log(f)^2 + 9*f^4)

```

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int f^{cx^2+a} \sin(fx^2 + ex + d)^3 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(f^(a + c*x^2)*sin(d + e*x + f*x^2)^3,x)

[Out] int(f^(a + c*x^2)*sin(d + e*x + f*x^2)^3, x)

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f**(c*x**2+a)*sin(f*x**2+e*x+d)**3,x)

[Out] Timed out

3.94 $\int f^{a+bx+cx^2} \sin(d + ex) dx$

Optimal. Leaf size=176

$$\frac{i\sqrt{\pi} f^a e^{\frac{(e+ib \log(f))^2}{4c \log(f)} - id} \operatorname{erfi}\left(\frac{-b \log(f) - 2cx \log(f) + ie}{2\sqrt{c} \sqrt{\log(f)}}\right)}{4\sqrt{c} \sqrt{\log(f)}} - \frac{i\sqrt{\pi} f^a e^{\frac{(e-ib \log(f))^2}{4c \log(f)} + id} \operatorname{erfi}\left(\frac{b \log(f) + 2cx \log(f) + ie}{2\sqrt{c} \sqrt{\log(f)}}\right)}{4\sqrt{c} \sqrt{\log(f)}}$$

[Out] $\frac{1}{4} I \exp(-I d + 1/4 (e + I b \ln(f))^2 / c / \ln(f)) f^a \operatorname{erfi}(1/2 (-I e + b \ln(f) + 2 c x \ln(f)) / c^{1/2} / \ln(f)^{1/2}) \operatorname{Pi}^{1/2} / c^{1/2} / \ln(f)^{1/2} - \frac{1}{4} I \exp(I d + 1/4 (e - I b \ln(f))^2 / c / \ln(f)) f^a \operatorname{erfi}(1/2 (I e + b \ln(f) + 2 c x \ln(f)) / c^{1/2} / \ln(f)^{1/2}) \operatorname{Pi}^{1/2} / c^{1/2} / \ln(f)^{1/2}$

Rubi [A] time = 0.33, antiderivative size = 176, normalized size of antiderivative = 1.00, number of steps used = 8, number of rules used = 4, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.210$, Rules used = {4472, 2287, 2234, 2204}

$$\frac{i\sqrt{\pi} f^a e^{\frac{(e+ib \log(f))^2}{4c \log(f)} - id} \operatorname{Erfi}\left(\frac{-b \log(f) - 2cx \log(f) + ie}{2\sqrt{c} \sqrt{\log(f)}}\right)}{4\sqrt{c} \sqrt{\log(f)}} - \frac{i\sqrt{\pi} f^a e^{\frac{(e-ib \log(f))^2}{4c \log(f)} + id} \operatorname{Erfi}\left(\frac{b \log(f) + 2cx \log(f) + ie}{2\sqrt{c} \sqrt{\log(f)}}\right)}{4\sqrt{c} \sqrt{\log(f)}}$$

Antiderivative was successfully verified.

[In] `Int[f^(a + b*x + c*x^2)*Sin[d + e*x], x]`

[Out] $((-I/4) E^{((-I)d + (e + I b \operatorname{Log}[f])^2 / (4 c \operatorname{Log}[f]))} f^a \operatorname{Sqrt}[\operatorname{Pi}] \operatorname{Erfi}[(I e - b \operatorname{Log}[f] - 2 c x \operatorname{Log}[f]) / (2 \operatorname{Sqrt}[c] \operatorname{Sqrt}[\operatorname{Log}[f]])]) / (\operatorname{Sqrt}[c] \operatorname{Sqrt}[\operatorname{Log}[f]]) - ((I/4) E^{(I d + (e - I b \operatorname{Log}[f])^2 / (4 c \operatorname{Log}[f]))} f^a \operatorname{Sqrt}[\operatorname{Pi}] \operatorname{Erfi}[(I e + b \operatorname{Log}[f] + 2 c x \operatorname{Log}[f]) / (2 \operatorname{Sqrt}[c] \operatorname{Sqrt}[\operatorname{Log}[f]])]) / (\operatorname{Sqrt}[c] \operatorname{Sqrt}[\operatorname{Log}[f]])])$

Rule 2204

`Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_.))^2), x_Symbol] := Simp[(F^a*Sqrt[Pi]*Erfi[(c + d*x)*Rt[b*Log[F], 2]])/(2*d*Rt[b*Log[F], 2]), x] /; FreeQ[{F, a, b, c, d}, x] && PosQ[b]`

Rule 2234

`Int[(F_)^((a_.) + (b_.)*(x_) + (c_.)*(x_)^2), x_Symbol] := Dist[F^(a - b^2/(4*c)), Int[F^((b + 2*c*x)^2/(4*c)), x], x] /; FreeQ[{F, a, b, c}, x]`

Rule 2287

`Int[(u_.)*(F_)^(v_.)*(G_)^(w_.), x_Symbol] := With[{z = v*Log[F] + w*Log[G]}, Int[u*NormalizeIntegrand[E^z, x], x] /; BinomialQ[z, x] || (PolynomialQ[z, x] && LeQ[Exponent[z, x], 2])] /; FreeQ[{F, G}, x]`

Rule 4472

`Int[(F_)^(u_.)*Sin[v_]^(n_.), x_Symbol] := Int[ExpandTrigToExp[F^u, Sin[v]^n, x], x] /; FreeQ[F, x] && (LinearQ[u, x] || PolyQ[u, x, 2]) && (LinearQ[v, x] || PolyQ[v, x, 2]) && IGtQ[n, 0]`

Rubi steps

$$\begin{aligned}
\int f^{a+bx+cx^2} \sin(d+ex) dx &= \int \left(\frac{1}{2} i e^{-id-ix} f^{a+bx+cx^2} - \frac{1}{2} i e^{id+ix} f^{a+bx+cx^2} \right) dx \\
&= \frac{1}{2} i \int e^{-id-ix} f^{a+bx+cx^2} dx - \frac{1}{2} i \int e^{id+ix} f^{a+bx+cx^2} dx \\
&= \frac{1}{2} i \int \exp(-id + a \log(f) + cx^2 \log(f) - x(i e - b \log(f))) dx - \frac{1}{2} i \int \exp(id + a \log(f) + cx^2 \log(f) + x(i e - b \log(f))) dx \\
&= - \left(\frac{1}{2} \left(i e^{id + \frac{(e-ib \log(f))^2}{4c \log(f)}} f^a \right) \int \exp\left(\frac{(ie + b \log(f) + 2cx \log(f))^2}{4c \log(f)}\right) dx \right) + \frac{1}{2} \left(i e^{-id + \frac{(e+ib \log(f))^2}{4c \log(f)}} f^a \right) \int \exp\left(\frac{(ie - b \log(f) - 2cx \log(f))^2}{4c \log(f)}\right) dx \\
&= - \frac{i e^{-id + \frac{(e+ib \log(f))^2}{4c \log(f)}} f^a \sqrt{\pi} \operatorname{erfi}\left(\frac{ie - b \log(f) - 2cx \log(f)}{2\sqrt{c} \sqrt{\log(f)}}\right)}{4\sqrt{c} \sqrt{\log(f)}} - \frac{i e^{id + \frac{(e-ib \log(f))^2}{4c \log(f)}} f^a \sqrt{\pi} \operatorname{erfi}\left(\frac{ie + b \log(f) + 2cx \log(f)}{2\sqrt{c} \sqrt{\log(f)}}\right)}{4\sqrt{c} \sqrt{\log(f)}}
\end{aligned}$$

Mathematica [A] time = 0.34, size = 155, normalized size = 0.88

$$\frac{\sqrt{\pi} f^{a - \frac{b^2}{4c}} e^{\frac{e(2ib \log(f))}{4c \log(f)}} \left(i(\cos(d) + i \sin(d)) \operatorname{erfi}\left(\frac{-\log(f)(b+2cx) - ie}{2\sqrt{c} \sqrt{\log(f)}}\right) + e^{\frac{ibe}{c}} (\sin(d) + i \cos(d)) \operatorname{erfi}\left(\frac{\log(f)(b+2cx) - ie}{2\sqrt{c} \sqrt{\log(f)}}\right) \right)}{4\sqrt{c} \sqrt{\log(f)}}$$

Antiderivative was successfully verified.

[In] Integrate[f^(a + b*x + c*x^2)*Sin[d + e*x], x]

[Out] (E^((e*(e - (2*I)*b*Log[f]))/(4*c*Log[f]))*f^(a - b^2/(4*c))*Sqrt[Pi]*(I*Erfi[(-I)*e - (b + 2*c*x)*Log[f]]/(2*Sqrt[c]*Sqrt[Log[f]])]*(Cos[d] + I*Sin[d]) + E^((I*b*e)/c)*Erfi[(-I)*e + (b + 2*c*x)*Log[f]]/(2*Sqrt[c]*Sqrt[Log[f]]))*(I*Cos[d] + Sin[d]))/(4*Sqrt[c]*Sqrt[Log[f]])

fricas [A] time = 1.32, size = 178, normalized size = 1.01

$$\frac{i \sqrt{\pi} \sqrt{-c \log(f)} \operatorname{erf}\left(\frac{((2cx+b) \log(f) + ie) \sqrt{-c \log(f)}}{2c \log(f)}\right) e^{\left(-\frac{(b^2-4ac) \log(f)^2 - e^2 - (4icd-2ibe) \log(f)}{4c \log(f)}\right)} - i \sqrt{\pi} \sqrt{-c \log(f)} \operatorname{erf}\left(\frac{((2cx+b) \log(f) - ie) \sqrt{-c \log(f)}}{2c \log(f)}\right) e^{\left(-\frac{(b^2-4ac) \log(f)^2 - e^2 - (4icd-2ibe) \log(f)}{4c \log(f)}\right)}}{4c \log(f)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(c*x^2+b*x+a)*sin(e*x+d), x, algorithm="fricas")

[Out] 1/4*(I*sqrt(pi)*sqrt(-c*log(f))*erf(1/2*((2*c*x + b)*log(f) + I*e)*sqrt(-c*log(f))/(c*log(f)))*e^(-1/4*((b^2 - 4*a*c)*log(f)^2 - e^2 - (4*I*c*d - 2*I*b*e)*log(f))/(c*log(f))) - I*sqrt(pi)*sqrt(-c*log(f))*erf(1/2*((2*c*x + b)*log(f) - I*e)*sqrt(-c*log(f))/(c*log(f)))*e^(-1/4*((b^2 - 4*a*c)*log(f)^2 - e^2 - (-4*I*c*d + 2*I*b*e)*log(f))/(c*log(f))))/(c*log(f))

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int f^{cx^2+bx+a} \sin(ex + d) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(c*x^2+b*x+a)*sin(e*x+d), x, algorithm="giac")

[Out] integrate(f^(c*x^2 + b*x + a)*sin(e*x + d), x)

maple [A] time = 0.52, size = 170, normalized size = 0.97

$$\frac{i \sqrt{\pi} f^a e^{-\frac{-e^2 + 2i \ln(f) b e - 4id \ln(f) c + \ln(f)^2 b^2}{4 \ln(f) c}} \operatorname{erf}\left(-\sqrt{-c \ln(f)} x + \frac{ie + b \ln(f)}{2\sqrt{-c \ln(f)}}\right)}{4\sqrt{-c \ln(f)}} - \frac{i \sqrt{\pi} f^a e^{-\frac{-e^2 - 2i \ln(f) b e + 4id \ln(f) c + \ln(f)^2 b^2}{4 \ln(f) c}} \operatorname{erf}\left(-\sqrt{-c \ln(f)} x + \frac{ie - b \ln(f)}{2\sqrt{-c \ln(f)}}\right)}{4\sqrt{-c \ln(f)}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(f^(c*x^2+b*x+a)*sin(e*x+d),x)`

[Out] $\frac{1}{4}I\pi^{1/2}f^a\exp(-1/4*(-e^2+2I*\ln(f)*b*e-4I*d*\ln(f)*c+\ln(f)^2*b^2)/\ln(f)/c)/(-c*\ln(f))^{1/2}*\operatorname{erf}(-(-c*\ln(f))^{1/2}*x+1/2*(I*e+b*\ln(f)))/(-c*\ln(f))^{1/2})-1/4I\pi^{1/2}f^a\exp(-1/4*(-e^2-2I*\ln(f)*b*e+4I*d*\ln(f)*c+\ln(f)^2*b^2)/\ln(f)/c)/(-c*\ln(f))^{1/2}*\operatorname{erf}(-(-c*\ln(f))^{1/2}*x+1/2*(-I*e+b*\ln(f)))/(-c*\ln(f))^{1/2})$

maxima [C] time = 0.40, size = 354, normalized size = 2.01

$$\sqrt{\pi} \left(f^a \left(i \cos\left(-\frac{2cd-be}{2c}\right) + \sin\left(-\frac{2cd-be}{2c}\right) \right) \operatorname{erf}\left(x\sqrt{-c\log(f)} - \frac{1}{2}(b\log(f) + ie)\frac{1}{\sqrt{-c\log(f)}}\right) e^{\left(\frac{e^2}{4c\log(f)}\right)} + f^a(-i \cos\left(-\frac{2cd-be}{2c}\right) + \sin\left(-\frac{2cd-be}{2c}\right)) \operatorname{erf}\left(x\sqrt{-c\log(f)} - \frac{1}{2}(b\log(f) - ie)\frac{1}{\sqrt{-c\log(f)}}\right) e^{\left(\frac{e^2}{4c\log(f)}\right)} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(f^(c*x^2+b*x+a)*sin(e*x+d),x, algorithm="maxima")`

[Out] $\frac{1}{8}\sqrt{\pi}*(f^a*(I*\cos(-1/2*(2*c*d - b*e)/c) + \sin(-1/2*(2*c*d - b*e)/c))*\operatorname{erf}(x*\operatorname{conjugate}(\sqrt{-c*\log(f)})) - 1/2*(b*\log(f) + I*e)*\operatorname{conjugate}(1/\sqrt{-c*\log(f)})))*e^{1/4*e^2/(c*\log(f))} + f^a*(-I*\cos(-1/2*(2*c*d - b*e)/c) + \sin(-1/2*(2*c*d - b*e)/c))*\operatorname{erf}(x*\operatorname{conjugate}(\sqrt{-c*\log(f)})) - 1/2*(b*\log(f) - I*e)*\operatorname{conjugate}(1/\sqrt{-c*\log(f)})))*e^{1/4*e^2/(c*\log(f))} + f^a*(I*\cos(-1/2*(2*c*d - b*e)/c) + \sin(-1/2*(2*c*d - b*e)/c))*\operatorname{erf}(1/2*(2*c*x*\log(f) + b*\log(f) + I*e)*\sqrt{-c*\log(f)}/(c*\log(f)))*e^{1/4*e^2/(c*\log(f))} + f^a*(-I*\cos(-1/2*(2*c*d - b*e)/c) + \sin(-1/2*(2*c*d - b*e)/c))*\operatorname{erf}(1/2*(2*c*x*\log(f) + b*\log(f) - I*e)*\sqrt{-c*\log(f)}/(c*\log(f)))*e^{1/4*e^2/(c*\log(f))})*\sqrt{-c*\log(f)}/(c*f^{1/4*b^2/c}*\log(f))$

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int f^{cx^2+bx+a} \sin(d+ex) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(f^(a + b*x + c*x^2)*sin(d + e*x),x)`

[Out] `int(f^(a + b*x + c*x^2)*sin(d + e*x), x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int f^{a+bx+cx^2} \sin(d+ex) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(f**(c*x**2+b*x+a)*sin(e*x+d),x)`

[Out] `Integral(f**(a + b*x + c*x**2)*sin(d + e*x), x)`

3.95 $\int f^{a+bx+cx^2} \sin^2(d+ex) dx$

Optimal. Leaf size=231

$$\frac{\sqrt{\pi} f^{a-\frac{b^2}{4c}} \operatorname{erfi}\left(\frac{\sqrt{\log(f)}(b+2cx)}{2\sqrt{c}}\right)}{4\sqrt{c}\sqrt{\log(f)}} + \frac{\sqrt{\pi} f^a e^{\frac{(2e+ib\log(f))^2}{4c\log(f)}-2id} \operatorname{erfi}\left(\frac{-b\log(f)-2cx\log(f)+2ie}{2\sqrt{c}\sqrt{\log(f)}}\right)}{8\sqrt{c}\sqrt{\log(f)}} - \frac{\sqrt{\pi} f^a e^{2id-\frac{(b\log(f)+2ie)^2}{4c\log(f)}} \operatorname{erfi}\left(\frac{b\log(f)+2ie}{2\sqrt{c}\sqrt{\log(f)}}\right)}{8\sqrt{c}\sqrt{\log(f)}}$$

[Out] $-1/8*\exp(-2*I*d+1/4*(2*e+I*b*\ln(f))^2/c/\ln(f))*f^a*\operatorname{erfi}(1/2*(-2*I*e+b*\ln(f)+2*c*x*\ln(f))/c^{(1/2)}/\ln(f)^{(1/2)})*\Pi^{(1/2)}/c^{(1/2)}/\ln(f)^{(1/2)}-1/8*\exp(2*I*d-1/4*(2*I*e+b*\ln(f))^2/c/\ln(f))*f^a*\operatorname{erfi}(1/2*(2*I*e+b*\ln(f)+2*c*x*\ln(f))/c^{(1/2)}/\ln(f)^{(1/2)})*\Pi^{(1/2)}/c^{(1/2)}/\ln(f)^{(1/2)}+1/4*f^{(a-1/4*b^2/c)}*\operatorname{erfi}(1/2*(2*c*x+b)*\ln(f)^{(1/2)}/c^{(1/2)})*\Pi^{(1/2)}/c^{(1/2)}/\ln(f)^{(1/2)}$

Rubi [A] time = 0.38, antiderivative size = 231, normalized size of antiderivative = 1.00, number of steps used = 10, number of rules used = 4, integrand size = 21, $\frac{\text{number of rules}}{\text{integrand size}} = 0.190$, Rules used = {4472, 2234, 2204, 2287}

$$\frac{\sqrt{\pi} f^{a-\frac{b^2}{4c}} \operatorname{Erfi}\left(\frac{\sqrt{\log(f)}(b+2cx)}{2\sqrt{c}}\right)}{4\sqrt{c}\sqrt{\log(f)}} + \frac{\sqrt{\pi} f^a e^{\frac{(2e+ib\log(f))^2}{4c\log(f)}-2id} \operatorname{Erfi}\left(\frac{-b\log(f)-2cx\log(f)+2ie}{2\sqrt{c}\sqrt{\log(f)}}\right)}{8\sqrt{c}\sqrt{\log(f)}} - \frac{\sqrt{\pi} f^a e^{2id-\frac{(b\log(f)+2ie)^2}{4c\log(f)}} \operatorname{Erfi}\left(\frac{b\log(f)+2ie}{2\sqrt{c}\sqrt{\log(f)}}\right)}{8\sqrt{c}\sqrt{\log(f)}}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[f^{(a + b*x + c*x^2)}*\operatorname{Sin}[d + e*x]^2, x]$

[Out] $(f^{(a - b^2/(4*c))}* \operatorname{Sqrt}[\Pi]* \operatorname{Erfi}[\frac{(b + 2*c*x)* \operatorname{Sqrt}[\operatorname{Log}[f]]}{(2*\operatorname{Sqrt}[c])}]) / (4*\operatorname{Sqrt}[c]* \operatorname{Sqrt}[\operatorname{Log}[f]]) + (E^{((-2*I)*d + (2*e + I*b*\operatorname{Log}[f])^2/(4*c*\operatorname{Log}[f]))} * f^a * \operatorname{Sqrt}[\Pi]* \operatorname{Erfi}[\frac{(2*I)*e - b*\operatorname{Log}[f] - 2*c*x*\operatorname{Log}[f]}{(2*\operatorname{Sqrt}[c]* \operatorname{Sqrt}[\operatorname{Log}[f]])}]) / (8*\operatorname{Sqrt}[c]* \operatorname{Sqrt}[\operatorname{Log}[f]]) - (E^{((2*I)*d - ((2*I)*e + b*\operatorname{Log}[f])^2/(4*c*\operatorname{Log}[f]))} * f^a * \operatorname{Sqrt}[\Pi]* \operatorname{Erfi}[\frac{(2*I)*e + b*\operatorname{Log}[f] + 2*c*x*\operatorname{Log}[f]}{(2*\operatorname{Sqrt}[c]* \operatorname{Sqrt}[\operatorname{Log}[f]])}]) / (8*\operatorname{Sqrt}[c]* \operatorname{Sqrt}[\operatorname{Log}[f]])$

Rule 2204

$\operatorname{Int}[(F_)^{((a_.) + (b_.)*((c_.) + (d_.)*(x_))^2)}, x_Symbol] := \operatorname{Simp}[(F^a*\operatorname{Sqrt}[\Pi]* \operatorname{Erfi}[(c + d*x)* \operatorname{Rt}[b*\operatorname{Log}[F], 2]]) / (2*d*\operatorname{Rt}[b*\operatorname{Log}[F], 2]), x] /; \operatorname{FreeQ}\{F, a, b, c, d\}, x] \&\& \operatorname{PosQ}[b]$

Rule 2234

$\operatorname{Int}[(F_)^{((a_.) + (b_.)*(x_) + (c_.)*(x_)^2)}, x_Symbol] := \operatorname{Dist}[F^{(a - b^2/(4*c))}, \operatorname{Int}[F^{((b + 2*c*x)^2/(4*c))}, x], x] /; \operatorname{FreeQ}\{F, a, b, c\}, x]$

Rule 2287

$\operatorname{Int}[(u_)*(F_)^{(v_)}*(G_)^{(w_)}, x_Symbol] := \operatorname{With}\{z = v*\operatorname{Log}[F] + w*\operatorname{Log}[G]\}, \operatorname{Int}[u*\operatorname{NormalizeIntegrand}[E^z, x], x] /; \operatorname{BinomialQ}[z, x] \|\| (\operatorname{PolynomialQ}[z, x] \&\& \operatorname{LeQ}[\operatorname{Exponent}[z, x], 2]) /; \operatorname{FreeQ}\{F, G\}, x]$

Rule 4472

$\operatorname{Int}[(F_)^{(u_)}*\operatorname{Sin}[v_]^{(n_.)}, x_Symbol] := \operatorname{Int}[\operatorname{ExpandTrigToExp}[F^u, \operatorname{Sin}[v]^n], x] /; \operatorname{FreeQ}[F, x] \&\& (\operatorname{LinearQ}[u, x] \|\| \operatorname{PolyQ}[u, x, 2]) \&\& (\operatorname{LinearQ}[v, x] \|\| \operatorname{PolyQ}[v, x, 2]) \&\& \operatorname{IGtQ}[n, 0]$

Rubi steps

$$\begin{aligned}
\int f^{a+bx+cx^2} \sin^2(d+ex) dx &= \int \left(\frac{1}{2} f^{a+bx+cx^2} - \frac{1}{4} e^{-2id-2iex} f^{a+bx+cx^2} - \frac{1}{4} e^{2id+2iex} f^{a+bx+cx^2} \right) dx \\
&= -\left(\frac{1}{4} \int e^{-2id-2iex} f^{a+bx+cx^2} dx \right) - \frac{1}{4} \int e^{2id+2iex} f^{a+bx+cx^2} dx + \frac{1}{2} \int f^{a+bx+cx^2} dx \\
&= -\left(\frac{1}{4} \int \exp(-2id + a \log(f) + cx^2 \log(f) - x(2ie - b \log(f))) dx \right) - \frac{1}{4} \int \exp \left(\dots \right) dx \\
&= \frac{f^{a-\frac{b^2}{4c}} \sqrt{\pi} \operatorname{erfi} \left(\frac{(b+2cx)\sqrt{\log(f)}}{2\sqrt{c}} \right)}{4\sqrt{c} \sqrt{\log(f)}} - \frac{1}{4} \left(\exp \left(-2id + \frac{(2e+ib \log(f))^2}{4c \log(f)} \right) f^a \right) \int \exp \left(\dots \right) dx \\
&= \frac{f^{a-\frac{b^2}{4c}} \sqrt{\pi} \operatorname{erfi} \left(\frac{(b+2cx)\sqrt{\log(f)}}{2\sqrt{c}} \right)}{4\sqrt{c} \sqrt{\log(f)}} + \frac{\exp \left(-2id + \frac{(2e+ib \log(f))^2}{4c \log(f)} \right) f^a \sqrt{\pi} \operatorname{erfi} \left(\frac{2ie-b \log(f)}{2\sqrt{c}} \right)}{8\sqrt{c} \sqrt{\log(f)}}
\end{aligned}$$

Mathematica [A] time = 0.69, size = 204, normalized size = 0.88

$$\frac{\sqrt{\pi} e^{-\frac{ibe}{c}} f^{a-\frac{b^2}{4c}} \left((\cos(2d) + i \sin(2d)) e^{\frac{e^2}{c \log(f)}} \operatorname{erfi} \left(\frac{\log(f)(b+2cx)+2ie}{2\sqrt{c} \sqrt{\log(f)}} \right) + (\cos(2d) - i \sin(2d)) e^{\frac{e(e+2ib \log(f))}{c \log(f)}} \operatorname{erfi} \left(\frac{\log(f)(2ie-b \log(f))}{2\sqrt{c} \sqrt{\log(f)}} \right) \right)}{8\sqrt{c} \sqrt{\log(f)}}$$

Antiderivative was successfully verified.

[In] Integrate[f^(a + b*x + c*x^2)*Sin[d + e*x]^2,x]

[Out] -1/8*(f^(a - b^2/(4*c))*Sqrt[Pi]*(-2*E^((I*b*e)/c)*Erfi[((b + 2*c*x)*Sqrt[Log[f]])/(2*Sqrt[c]]) + E^((e*(e + (2*I)*b*Log[f]))/(c*Log[f]))*Erfi[((-2*I)*e + (b + 2*c*x)*Log[f])/(2*Sqrt[c]*Sqrt[Log[f]])]*(Cos[2*d] - I*Sin[2*d]) + E^(e^2/(c*Log[f]))*Erfi[((2*I)*e + (b + 2*c*x)*Log[f])/(2*Sqrt[c]*Sqrt[Log[f]])]*(Cos[2*d] + I*Sin[2*d]))/(Sqrt[c]*E^((I*b*e)/c)*Sqrt[Log[f]])

fricas [A] time = 0.72, size = 224, normalized size = 0.97

$$\frac{\sqrt{\pi} \sqrt{-c \log(f)} \operatorname{erf} \left(\frac{((2cx+b) \log(f)+2ie) \sqrt{-c \log(f)}}{2c \log(f)} \right) e^{\left(-\frac{(b^2-4ac) \log(f)^2 - 4e^2 - (8icd-4ibe) \log(f)}{4c \log(f)} \right)} + \sqrt{\pi} \sqrt{-c \log(f)} \operatorname{erf} \left(\frac{((2cx+b) \log(f)-2ie) \sqrt{-c \log(f)}}{2c \log(f)} \right) e^{\left(-\frac{(b^2-4ac) \log(f)^2 - 4e^2 - (8icd-4ibe) \log(f)}{4c \log(f)} \right)}}{8c \log(f)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(c*x^2+b*x+a)*sin(e*x+d)^2,x, algorithm="fricas")

[Out] 1/8*(sqrt(pi)*sqrt(-c*log(f))*erf(1/2*((2*c*x + b)*log(f) + 2*I*e)*sqrt(-c*log(f))/(c*log(f)))*e^(-1/4*((b^2 - 4*a*c)*log(f)^2 - 4*e^2 - (8*I*c*d - 4*I*b*e)*log(f))/(c*log(f))) + sqrt(pi)*sqrt(-c*log(f))*erf(1/2*((2*c*x + b)*log(f) - 2*I*e)*sqrt(-c*log(f))/(c*log(f)))*e^(-1/4*((b^2 - 4*a*c)*log(f)^2 - 4*e^2 - (-8*I*c*d + 4*I*b*e)*log(f))/(c*log(f))) - 2*sqrt(pi)*sqrt(-c*log(f))*erf(1/2*(2*c*x + b)*sqrt(-c*log(f))/c)/f^(1/4*(b^2 - 4*a*c)/c)/(c*log(f))

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int f^{cx^2+bx+a} \sin(ex+d)^2 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(c*x^2+b*x+a)*sin(e*x+d)^2,x, algorithm="giac")

[Out] integrate(f^(c*x^2 + b*x + a)*sin(e*x + d)^2, x)

maple [A] time = 0.59, size = 217, normalized size = 0.94

$$\frac{\sqrt{\pi} f^a e^{-\frac{\ln(f)^2 b^2 - 4i \ln(f) b e + 8id \ln(f) c - 4e^2}{4 \ln(f) c}} \operatorname{erf}\left(-\sqrt{-c \ln(f)} x + \frac{b \ln(f) - 2ie}{2\sqrt{-c \ln(f)}}\right)}{8\sqrt{-c \ln(f)}} + \frac{\sqrt{\pi} f^a e^{-\frac{\ln(f)^2 b^2 + 4i \ln(f) b e - 8id \ln(f) c - 4e^2}{4 \ln(f) c}} \operatorname{erf}\left(-\sqrt{-c \ln(f)}\right)}{8\sqrt{-c \ln(f)}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(f^(c*x^2+b*x+a)*sin(e*x+d)^2,x)

[Out] 1/8*Pi^(1/2)*f^a*exp(-1/4*(ln(f)^2*b^2-4*I*ln(f)*b*e+8*I*d*ln(f)*c-4*e^2)/ln(f)/c)/(-c*ln(f))^(1/2)*erf(-(-c*ln(f))^(1/2)*x+1/2*(b*ln(f)-2*I*e)/(-c*ln(f))^(1/2))+1/8*Pi^(1/2)*f^a*exp(-1/4*(ln(f)^2*b^2+4*I*ln(f)*b*e-8*I*d*ln(f)*c-4*e^2)/ln(f)/c)/(-c*ln(f))^(1/2)*erf(-(-c*ln(f))^(1/2)*x+1/2*(2*I*e+b*ln(f)))/(-c*ln(f))^(1/2))-1/4*Pi^(1/2)*f^a*f^(-1/4*b^2/c)/(-c*ln(f))^(1/2)*erf(-(-c*ln(f))^(1/2)*x+1/2/(-c*ln(f))^(1/2)*b*ln(f))

maxima [C] time = 0.39, size = 399, normalized size = 1.73

$$\sqrt{\pi} \left(f^a \left(\cos\left(-\frac{2cd-be}{c}\right) - i \sin\left(-\frac{2cd-be}{c}\right) \right) \operatorname{erf}\left(x\sqrt{-c \log(f)} - \frac{1}{2}(b \log(f) + 2ie)\frac{1}{\sqrt{-c \log(f)}}\right) e^{\left(\frac{e^2}{c \log(f)}\right)} + f^a \left(\cos\left(-\frac{2cd-be}{c}\right) + i \sin\left(-\frac{2cd-be}{c}\right) \right) \operatorname{erf}\left(x\sqrt{-c \log(f)} - \frac{1}{2}(b \log(f) - 2ie)\frac{1}{\sqrt{-c \log(f)}}\right) e^{\left(\frac{e^2}{c \log(f)}\right)} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(c*x^2+b*x+a)*sin(e*x+d)^2,x, algorithm="maxima")

[Out] -1/16*sqrt(pi)*(f^a*(cos(-(2*c*d - b*e)/c) - I*sin(-(2*c*d - b*e)/c))*erf(x*conjugate(sqrt(-c*log(f))) - 1/2*(b*log(f) + 2*I*e)*conjugate(1/sqrt(-c*log(f))))*e^(e^2/(c*log(f))) + f^a*(cos(-(2*c*d - b*e)/c) + I*sin(-(2*c*d - b*e)/c))*erf(x*conjugate(sqrt(-c*log(f))) - 1/2*(b*log(f) - 2*I*e)*conjugate(1/sqrt(-c*log(f))))*e^(e^2/(c*log(f))) + f^a*(cos(-(2*c*d - b*e)/c) - I*sin(-(2*c*d - b*e)/c))*erf(1/2*(2*c*x*log(f) + b*log(f) + 2*I*e)*sqrt(-c*log(f))/(c*log(f)))*e^(e^2/(c*log(f))) + f^a*(cos(-(2*c*d - b*e)/c) + I*sin(-(2*c*d - b*e)/c))*erf(1/2*(2*c*x*log(f) + b*log(f) - 2*I*e)*sqrt(-c*log(f))/(c*log(f)))*e^(e^2/(c*log(f))) - 2*f^a*erf(-1/2*b*conjugate(1/sqrt(-c*log(f))))*log(f) + x*conjugate(sqrt(-c*log(f)))) + 2*f^a*erf(1/2*(2*c*x*log(f) + b*log(f))/sqrt(-c*log(f)))/sqrt(-c*log(f))*f^(1/4*b^2/c)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int f^{cx^2+bx+a} \sin(d+ex)^2 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(f^(a + b*x + c*x^2)*sin(d + e*x)^2,x)

[Out] int(f^(a + b*x + c*x^2)*sin(d + e*x)^2, x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int f^{a+bx+cx^2} \sin^2(d+ex) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f**(c*x**2+b*x+a)*sin(e*x+d)**2,x)

[Out] Integral(f**(a + b*x + c*x**2)*sin(d + e*x)**2, x)

x] || PolyQ[v, x, 2]) && IGtQ[n, 0]

Rubi steps

$$\begin{aligned}
 \int f^{a+bx+cx^2} \sin^3(d+ex) dx &= \int \left(\frac{3}{8} i e^{-id-iex} f^{a+bx+cx^2} - \frac{3}{8} i e^{id+iex} f^{a+bx+cx^2} - \frac{1}{8} i e^{-3id-3iex} f^{a+bx+cx^2} + \frac{1}{8} i e^{3id+3iex} f^{a+bx+cx^2} \right) dx \\
 &= -\left(\frac{1}{8} i \int e^{-3id-3iex} f^{a+bx+cx^2} dx \right) + \frac{1}{8} i \int e^{3id+3iex} f^{a+bx+cx^2} dx + \frac{3}{8} i \int e^{-id-iex} f^{a+bx+cx^2} dx \\
 &= -\left(\frac{1}{8} i \int \exp(-3id + a \log(f) + cx^2 \log(f) - x(3ie - b \log(f))) dx \right) + \frac{1}{8} i \int \exp(3id + 3iex + a \log(f) + cx^2 \log(f) + x(3ie - b \log(f))) dx \\
 &= -\left(\frac{1}{8} \left(3ie^{id+\frac{(e-ib \log(f))^2}{4c \log(f)}} f^a \right) \int \exp\left(\frac{(ie + b \log(f) + 2cx \log(f))^2}{4c \log(f)}\right) dx \right) + \frac{1}{8} \left(3ie^{-id+\frac{(e+ib \log(f))^2}{4c \log(f)}} f^a \right) \int \exp\left(\frac{(ie - b \log(f) + 2cx \log(f))^2}{4c \log(f)}\right) dx \\
 &= -\frac{3ie^{-id+\frac{(e+ib \log(f))^2}{4c \log(f)}} f^a \sqrt{\pi} \operatorname{erfi}\left(\frac{ie-b \log(f)-2cx \log(f)}{2\sqrt{c} \sqrt{\log(f)}}\right)}{16\sqrt{c} \sqrt{\log(f)}} + \frac{i \exp\left(-3id + \frac{(3e+ib \log(f))^2}{4c \log(f)}\right) f^a \sqrt{\pi} \operatorname{erfi}\left(\frac{ie+b \log(f)+2cx \log(f)}{2\sqrt{c} \sqrt{\log(f)}}\right)}{16\sqrt{c} \sqrt{\log(f)}}
 \end{aligned}$$

Mathematica [A] time = 0.98, size = 391, normalized size = 1.10

$$\sqrt{\pi} f^{a-\frac{b^2}{4c}} e^{\frac{e-6ib \log(f)}{4c \log(f)}} \left(-\sin(3d) e^{\frac{2e^2}{c \log(f)}} \operatorname{erfi}\left(\frac{\log(f)(b+2cx)+3ie}{2\sqrt{c} \sqrt{\log(f)}}\right) + i \cos(3d) e^{\frac{2e^2}{c \log(f)}} \operatorname{erfi}\left(\frac{\log(f)(b+2cx)+3ie}{2\sqrt{c} \sqrt{\log(f)}}\right) - \sin(3d) e^{\frac{e(2e+3ie)}{c \log(f)}} \operatorname{erfi}\left(\frac{\log(f)(b+2cx)+3ie}{2\sqrt{c} \sqrt{\log(f)}}\right) \right)$$

Antiderivative was successfully verified.

[In] Integrate[f^(a + b*x + c*x^2)*Sin[d + e*x]^3,x]

[Out] (E^((e*(e - (6*I)*b*Log[f]))/(4*c*Log[f]))*f^(a - b^2/(4*c))*Sqrt[Pi]*((-I)*E^((e*(2*e + (3*I)*b*Log[f]))/(c*Log[f]))*Cos[3*d]*Erfi[((-3*I)*e + (b + 2*c*x)*Log[f])/(2*Sqrt[c]*Sqrt[Log[f]])] + I*E^((2*e^2)/(c*Log[f]))*Cos[3*d]*Erfi[((3*I)*e + (b + 2*c*x)*Log[f])/(2*Sqrt[c]*Sqrt[Log[f]])] + (3*I)*E^((I*b*e)/c)*Erfi[((-I)*e - (b + 2*c*x)*Log[f])/(2*Sqrt[c]*Sqrt[Log[f]])]*(Cos[d] + I*Sin[d]) + 3*E^(((2*I)*b*e)/c)*Erfi[((-I)*e + (b + 2*c*x)*Log[f])/(2*Sqrt[c]*Sqrt[Log[f]])]*(I*Cos[d] + Sin[d]) - E^((e*(2*e + (3*I)*b*Log[f]))/(c*Log[f]))*Erfi[((-3*I)*e + (b + 2*c*x)*Log[f])/(2*Sqrt[c]*Sqrt[Log[f]])]*Sin[3*d] - E^((2*e^2)/(c*Log[f]))*Erfi[((3*I)*e + (b + 2*c*x)*Log[f])/(2*Sqrt[c]*Sqrt[Log[f]])]*Sin[3*d]))/(16*Sqrt[c]*Sqrt[Log[f]])

fricas [A] time = 1.04, size = 346, normalized size = 0.98

$$3i \sqrt{\pi} \sqrt{-c \log(f)} \operatorname{erf}\left(\frac{(2cx+b) \log(f)+ie}{2c \log(f)} \sqrt{-c \log(f)}\right) e^{\left(-\frac{(b^2-4ac) \log(f)^2-e^2-(4icd-2ibe) \log(f)}{4c \log(f)}\right)} - 3i \sqrt{\pi} \sqrt{-c \log(f)} \operatorname{erf}\left(\frac{(2cx+b) \log(f)-ie}{2c \log(f)} \sqrt{-c \log(f)}\right) e^{\left(-\frac{(b^2-4ac) \log(f)^2-e^2-(4icd-2ibe) \log(f)}{4c \log(f)}\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(c*x^2+b*x+a)*sin(e*x+d)^3,x, algorithm="fricas")

[Out] 1/16*(3*I*sqrt(pi)*sqrt(-c*log(f))*erf(1/2*((2*c*x + b)*log(f) + I*e)*sqrt(-c*log(f))/(c*log(f)))*e^(-1/4*((b^2 - 4*a*c)*log(f)^2 - e^2 - (4*I*c*d - 2*I*b*e)*log(f))/(c*log(f))) - 3*I*sqrt(pi)*sqrt(-c*log(f))*erf(1/2*((2*c*x + b)*log(f) - I*e)*sqrt(-c*log(f))/(c*log(f)))*e^(-1/4*((b^2 - 4*a*c)*log(f)^2 - e^2 - (-4*I*c*d + 2*I*b*e)*log(f))/(c*log(f))) - I*sqrt(pi)*sqrt(-c*log(f))*erf(1/2*((2*c*x + b)*log(f) + 3*I*e)*sqrt(-c*log(f))/(c*log(f)))*e^(-1/4*((b^2 - 4*a*c)*log(f)^2 - 9*e^2 - (12*I*c*d - 6*I*b*e)*log(f))/(c*log(f))) + I*sqrt(pi)*sqrt(-c*log(f))*erf(1/2*((2*c*x + b)*log(f) - 3*I*e)*sqrt(-c*log(f))/(c*log(f)))*e^(-1/4*((b^2 - 4*a*c)*log(f)^2 - 9*e^2 - (12*I*c*d - 6*I*b*e)*log(f))/(c*log(f)))

f))) + I*sqrt(pi)*sqrt(-c*log(f))*erf(1/2*((2*c*x + b)*log(f) - 3*I*e)*sqrt(-c*log(f))/(c*log(f)))*e^(-1/4*((b^2 - 4*a*c)*log(f)^2 - 9*e^2 - (-12*I*c*d + 6*I*b*e)*log(f))/(c*log(f)))/(c*log(f))

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int f^{cx^2+bx+a} \sin(ex+d)^3 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(c*x^2+b*x+a)*sin(e*x+d)^3,x, algorithm="giac")

[Out] integrate(f^(c*x^2 + b*x + a)*sin(e*x + d)^3, x)

maple [A] time = 0.93, size = 338, normalized size = 0.95

$$\frac{i\sqrt{\pi} f^a e^{-\frac{\ln(f)^2 b^2 + 6i \ln(f) b e - 12id \ln(f) c - 9e^2}{4 \ln(f) c}} \operatorname{erf}\left(-\sqrt{-c \ln(f)} x + \frac{3ie + b \ln(f)}{2\sqrt{-c \ln(f)}}\right)}{16\sqrt{-c \ln(f)}} + \frac{i\sqrt{\pi} f^a e^{-\frac{\ln(f)^2 b^2 - 6i \ln(f) b e + 12id \ln(f) c - 9e^2}{4 \ln(f) c}} \operatorname{erf}\left(-\sqrt{-c \ln(f)} x + \frac{3ie - b \ln(f)}{2\sqrt{-c \ln(f)}}\right)}{16\sqrt{-c \ln(f)}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(f^(c*x^2+b*x+a)*sin(e*x+d)^3,x)

[Out] -1/16*I*Pi^(1/2)*f^a*exp(-1/4*(ln(f)^2*b^2+6*I*ln(f)*b*e-12*I*d*ln(f)*c-9*e^2)/ln(f)/c)/(-c*ln(f))^(1/2)*erf(-(-c*ln(f))^(1/2)*x+1/2*(3*I*e+b*ln(f)))/(-c*ln(f))^(1/2))+1/16*I*Pi^(1/2)*f^a*exp(-1/4*(ln(f)^2*b^2-6*I*ln(f)*b*e+12*I*d*ln(f)*c-9*e^2)/ln(f)/c)/(-c*ln(f))^(1/2)*erf(-(-c*ln(f))^(1/2)*x+1/2*(b*ln(f)-3*I*e)/(-c*ln(f))^(1/2))-3/16*I*Pi^(1/2)*f^a*exp(-1/4*(-e^2-2*I*ln(f)*b*e+4*I*d*ln(f)*c+ln(f)^2*b^2)/ln(f)/c)/(-c*ln(f))^(1/2)*erf(-(-c*ln(f))^(1/2)*x+1/2*(-I*e+b*ln(f)))/(-c*ln(f))^(1/2))+3/16*I*Pi^(1/2)*f^a*exp(-1/4*(-e^2+2*I*ln(f)*b*e-4*I*d*ln(f)*c+ln(f)^2*b^2)/ln(f)/c)/(-c*ln(f))^(1/2)*erf(-(-c*ln(f))^(1/2)*x+1/2*(I*e+b*ln(f)))/(-c*ln(f))^(1/2))

maxima [C] time = 0.41, size = 684, normalized size = 1.93

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(c*x^2+b*x+a)*sin(e*x+d)^3,x, algorithm="maxima")

[Out] -1/32*sqrt(pi)*(f^a*(I*cos(-3/2*(2*c*d - b*e)/c) + sin(-3/2*(2*c*d - b*e)/c))*erf(x*conjugate(sqrt(-c*log(f))) - 1/2*(b*log(f) + 3*I*e)*conjugate(1/sqrt(-c*log(f))))*e^(9/4*e^2/(c*log(f))) + f^a*(-I*cos(-3/2*(2*c*d - b*e)/c) + sin(-3/2*(2*c*d - b*e)/c))*erf(x*conjugate(sqrt(-c*log(f))) - 1/2*(b*log(f) - 3*I*e)*conjugate(1/sqrt(-c*log(f))))*e^(9/4*e^2/(c*log(f))) + f^a*(I*cos(-3/2*(2*c*d - b*e)/c) + sin(-3/2*(2*c*d - b*e)/c))*erf(1/2*(2*c*x*log(f) + b*log(f) + 3*I*e)*sqrt(-c*log(f))/(c*log(f)))*e^(9/4*e^2/(c*log(f))) + f^a*(-I*cos(-3/2*(2*c*d - b*e)/c) + sin(-3/2*(2*c*d - b*e)/c))*erf(1/2*(2*c*x*log(f) + b*log(f) - 3*I*e)*sqrt(-c*log(f))/(c*log(f)))*e^(9/4*e^2/(c*log(f))) + f^a*(-3*I*cos(-1/2*(2*c*d - b*e)/c) - 3*sin(-1/2*(2*c*d - b*e)/c))*erf(x*conjugate(sqrt(-c*log(f))) - 1/2*(b*log(f) + I*e)*conjugate(1/sqrt(-c*log(f))))*e^(1/4*e^2/(c*log(f))) + f^a*(3*I*cos(-1/2*(2*c*d - b*e)/c) - 3*sin(-1/2*(2*c*d - b*e)/c))*erf(x*conjugate(sqrt(-c*log(f))) - 1/2*(b*log(f) - I*e)*conjugate(1/sqrt(-c*log(f))))*e^(1/4*e^2/(c*log(f))) + f^a*(-3*I*cos(-1/2*(2*c*d - b*e)/c) - 3*sin(-1/2*(2*c*d - b*e)/c))*erf(1/2*(2*c*x*log(f) + b*log(f) + I*e)*sqrt(-c*log(f))/(c*log(f)))*e^(1/4*e^2/(c*log(f))) + f^a*(3*I*cos(-1/2*(2*c*d - b*e)/c) - 3*sin(-1/2*(2*c*d - b*e)/c))*erf(1/2*(2*c*x*log(f) + b*log(f) - I*e)*sqrt(-c*log(f))/(c*log(f)))*e^(1/4*e^2/(c*log(f))))*sqrt(-c*log(f))/(c*f^(1/4*b^2/c)*log(f))

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int f^{cx^2+bx+a} \sin(dx+ex)^3 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(f^(a + b*x + c*x^2)*sin(d + e*x)^3,x)

[Out] int(f^(a + b*x + c*x^2)*sin(d + e*x)^3, x)

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f**(c*x**2+b*x+a)*sin(e*x+d)**3,x)

[Out] Timed out

3.97 $\int f^{a+bx+cx^2} \sin(d + fx^2) dx$

Optimal. Leaf size=193

$$\frac{i\sqrt{\pi} f^a e^{-\frac{b^2 \log^2(f)}{4c \log(f)+4if} - id} \operatorname{erf}\left(\frac{b \log(f) - 2x(-c \log(f) + if)}{2\sqrt{-c \log(f) + if}}\right)}{4\sqrt{-c \log(f) + if}} - \frac{i\sqrt{\pi} f^a e^{id - \frac{b^2 \log^2(f)}{4c \log(f)+4if}} \operatorname{erfi}\left(\frac{b \log(f) + 2x(c \log(f) + if)}{2\sqrt{c \log(f) + if}}\right)}{4\sqrt{c \log(f) + if}}$$

[Out] $-1/4 * I * \exp(-I * d + b^2 * \ln(f)^2 / (4 * I * f - 4 * c * \ln(f))) * f^a * \operatorname{erf}(1/2 * (b * \ln(f) - 2 * x * (I * f - c * \ln(f)))) / (I * f - c * \ln(f))^{1/2} * \Pi^{1/2} / (I * f - c * \ln(f))^{1/2} - 1/4 * I * \exp(I * d - b^2 * \ln(f)^2 / (4 * I * f + 4 * c * \ln(f))) * f^a * \operatorname{erfi}(1/2 * (b * \ln(f) + 2 * x * (I * f + c * \ln(f)))) / (I * f + c * \ln(f))^{1/2} * \Pi^{1/2} / (I * f + c * \ln(f))^{1/2}$

Rubi [A] time = 0.38, antiderivative size = 193, normalized size of antiderivative = 1.00, number of steps used = 8, number of rules used = 5, integrand size = 21, $\frac{\text{number of rules}}{\text{integrand size}} = 0.238$, Rules used = {4472, 2287, 2234, 2205, 2204}

$$\frac{i\sqrt{\pi} f^a e^{-\frac{b^2 \log^2(f)}{4c \log(f)+4if} - id} \operatorname{Erf}\left(\frac{b \log(f) - 2x(-c \log(f) + if)}{2\sqrt{-c \log(f) + if}}\right)}{4\sqrt{-c \log(f) + if}} - \frac{i\sqrt{\pi} f^a e^{id - \frac{b^2 \log^2(f)}{4c \log(f)+4if}} \operatorname{Erfi}\left(\frac{b \log(f) + 2x(c \log(f) + if)}{2\sqrt{c \log(f) + if}}\right)}{4\sqrt{c \log(f) + if}}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[f^{(a + b*x + c*x^2)} * \operatorname{Sin}[d + f*x^2], x]$

[Out] $((-I/4) * E^{((-I) * d + (b^2 * \operatorname{Log}[f]^2) / ((4 * I) * f - 4 * c * \operatorname{Log}[f]))} * f^a * \operatorname{Sqrt}[\Pi] * \operatorname{Erf}[(b * \operatorname{Log}[f] - 2 * x * (I * f - c * \operatorname{Log}[f])) / (2 * \operatorname{Sqrt}[I * f - c * \operatorname{Log}[f]])] / \operatorname{Sqrt}[I * f - c * \operatorname{Log}[f]] - ((I/4) * E^{(I * d - (b^2 * \operatorname{Log}[f]^2) / ((4 * I) * f + 4 * c * \operatorname{Log}[f]))} * f^a * \operatorname{Sqrt}[\Pi] * \operatorname{Erfi}[(b * \operatorname{Log}[f] + 2 * x * (I * f + c * \operatorname{Log}[f])) / (2 * \operatorname{Sqrt}[I * f + c * \operatorname{Log}[f]])] / \operatorname{Sqrt}[I * f + c * \operatorname{Log}[f]])$

Rule 2204

$\operatorname{Int}[(F_)^{((a_) + (b_) * ((c_) + (d_) * (x_)) ^ 2)}, x_Symbol] := \operatorname{Simp}[(F^a * \operatorname{Sqrt}[\Pi] * \operatorname{Erfi}[(c + d * x) * \operatorname{Rt}[b * \operatorname{Log}[F], 2]]) / (2 * d * \operatorname{Rt}[b * \operatorname{Log}[F], 2]), x] /;$ $\operatorname{FreeQ}\{F, a, b, c, d\}, x \} \&\& \operatorname{PosQ}[b]$

Rule 2205

$\operatorname{Int}[(F_)^{((a_) + (b_) * ((c_) + (d_) * (x_)) ^ 2)}, x_Symbol] := \operatorname{Simp}[(F^a * \operatorname{Sqrt}[\Pi] * \operatorname{Erf}[(c + d * x) * \operatorname{Rt}[-(b * \operatorname{Log}[F]), 2]]) / (2 * d * \operatorname{Rt}[-(b * \operatorname{Log}[F]), 2]), x] /;$ $\operatorname{FreeQ}\{F, a, b, c, d\}, x \} \&\& \operatorname{NegQ}[b]$

Rule 2234

$\operatorname{Int}[(F_)^{((a_) + (b_) * (x_) + (c_) * (x_) ^ 2)}, x_Symbol] := \operatorname{Dist}[F^{(a - b^2 / (4 * c))}, \operatorname{Int}[F^{((b + 2 * c * x) ^ 2 / (4 * c))}, x], x] /;$ $\operatorname{FreeQ}\{F, a, b, c\}, x \}$

Rule 2287

$\operatorname{Int}[(u_) * (F_)^{(v_)} * (G_)^{(w_)}, x_Symbol] := \operatorname{With}\{z = v * \operatorname{Log}[F] + w * \operatorname{Log}[G]\}, \operatorname{Int}[u * \operatorname{NormalizeIntegrand}[E^z, x], x] /;$ $\operatorname{BinomialQ}[z, x] \mid \mid (\operatorname{PolynomialQ}[z, x] \&\& \operatorname{LeQ}[\operatorname{Exponent}[z, x], 2]) /;$ $\operatorname{FreeQ}\{F, G\}, x \}$

Rule 4472

$\operatorname{Int}[(F_)^{(u_)} * \operatorname{Sin}[v_]^{(n_)}, x_Symbol] := \operatorname{Int}[\operatorname{ExpandTrigToExp}[F^u, \operatorname{Sin}[v]^n], x] /;$ $\operatorname{FreeQ}[F, x] \&\& (\operatorname{LinearQ}[u, x] \mid \mid \operatorname{PolyQ}[u, x, 2]) \&\& (\operatorname{LinearQ}[v, x] \mid \mid \operatorname{PolyQ}[v, x, 2]) \&\& \operatorname{IGtQ}[n, 0]$

Rubi steps

$$\begin{aligned}
\int f^{a+bx+cx^2} \sin(d + fx^2) dx &= \int \left(\frac{1}{2} i e^{-id-ifx^2} f^{a+bx+cx^2} - \frac{1}{2} i e^{id+ifx^2} f^{a+bx+cx^2} \right) dx \\
&= \frac{1}{2} i \int e^{-id-ifx^2} f^{a+bx+cx^2} dx - \frac{1}{2} i \int e^{id+ifx^2} f^{a+bx+cx^2} dx \\
&= \frac{1}{2} i \int \exp(-id + a \log(f) + bx \log(f) - x^2(if - c \log(f))) dx - \frac{1}{2} i \int \exp(id + a \log(f) + bx \log(f) + x^2(if + c \log(f))) dx \\
&= \frac{1}{2} \left(i e^{-id + \frac{b^2 \log^2(f)}{4if - 4c \log(f)}} f^a \right) \int \exp\left(\frac{(b \log(f) + 2x(-if + c \log(f)))^2}{4(-if + c \log(f))}\right) dx - \frac{1}{2} \left(i e^{id - \frac{b^2 \log^2(f)}{4if + 4c \log(f)}} f^a \right) \int \exp\left(\frac{(b \log(f) + 2x(if + c \log(f)))^2}{4(if + c \log(f))}\right) dx \\
&= -\frac{i e^{-id + \frac{b^2 \log^2(f)}{4if - 4c \log(f)}} f^a \sqrt{\pi} \operatorname{erf}\left(\frac{b \log(f) - 2x(-if - c \log(f))}{2\sqrt{if - c \log(f)}}\right)}{4\sqrt{if - c \log(f)}} - \frac{i e^{id - \frac{b^2 \log^2(f)}{4if + 4c \log(f)}} f^a \sqrt{\pi} \operatorname{erfi}\left(\frac{b \log(f) + 2x(if + c \log(f))}{2\sqrt{if + c \log(f)}}\right)}{4\sqrt{if + c \log(f)}}
\end{aligned}$$

Mathematica [A] time = 0.99, size = 230, normalized size = 1.19

$$\frac{\sqrt[4]{-1} \sqrt{\pi} f^a e^{-\frac{b^2 \log^2(f)}{4c \log(f) + 4if}} \left(\sqrt{f - ic \log(f)} (f + ic \log(f)) (\cos(d) + i \sin(d)) e^{\frac{ib^2 f \log^2(f)}{2(c^2 \log^2(f) + f^2)}} \operatorname{erfi}\left(\frac{\sqrt[4]{-1} (2fx - i \log(f)(b + 2cx))}{2\sqrt{f - ic \log(f)}}\right) \right)}{4(c^2 \log^2(f) + f^2)}$$

Antiderivative was successfully verified.

[In] Integrate[f^(a + b*x + c*x^2)*Sin[d + f*x^2],x]

[Out] -1/4*((-1)^(1/4)*E^((b^2*Log[f]^2)/((4*I)*f - 4*c*Log[f]))*f^a*Sqrt[Pi]*(Erfi[(-1)^(3/4)*(2*f*x + I*(b + 2*c*x)*Log[f])]/(2*Sqrt[f + I*c*Log[f]])]*Sqrt[f + I*c*Log[f]]*(I*f + c*Log[f])*(Cos[d] - I*Sin[d]) + E^(((I/2)*b^2*f*Log[f]^2)/(f^2 + c^2*Log[f]^2))*Erfi[(-1)^(1/4)*(2*f*x - I*(b + 2*c*x)*Log[f])]/(2*Sqrt[f - I*c*Log[f]])]*Sqrt[f - I*c*Log[f]]*(f + I*c*Log[f])*(Cos[d] + I*Sin[d]))/(f^2 + c^2*Log[f]^2)

fricas [B] time = 0.82, size = 309, normalized size = 1.60

$$\frac{\sqrt{\pi} (ic \log(f) + f) \sqrt{-c \log(f) - if} \operatorname{erf}\left(\frac{(2f^2x - ibf \log(f) + (2c^2x + bc) \log(f)^2) \sqrt{-c \log(f) - if}}{2(c^2 \log(f)^2 + f^2)}\right) e^{\left(\frac{4af^2 \log(f) - (b^2c - 4ac^2) \log(f)^3 + 4idf^2 + 4c^2 \log(f)^2 + f^2}{4(c^2 \log(f)^2 + f^2)}\right)}}{4(c^2 \log^2(f) + f^2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(c*x^2+b*x+a)*sin(f*x^2+d),x, algorithm="fricas")

[Out] 1/4*(sqrt(pi)*(I*c*log(f) + f)*sqrt(-c*log(f) - I*f)*erf(1/2*(2*f^2*x - I*b*f*log(f) + (2*c^2*x + b*c)*log(f)^2)*sqrt(-c*log(f) - I*f)/(c^2*log(f)^2 + f^2))*e^(1/4*(4*a*f^2*log(f) - (b^2*c - 4*a*c^2)*log(f)^3 + 4*I*d*f^2 + (4*I*c^2*d + I*b^2*f)*log(f)^2)/(c^2*log(f)^2 + f^2)) + sqrt(pi)*(-I*c*log(f) + f)*sqrt(-c*log(f) + I*f)*erf(1/2*(2*f^2*x + I*b*f*log(f) + (2*c^2*x + b*c)*log(f)^2)*sqrt(-c*log(f) + I*f)/(c^2*log(f)^2 + f^2))*e^(1/4*(4*a*f^2*log(f) - (b^2*c - 4*a*c^2)*log(f)^3 - 4*I*d*f^2 + (-4*I*c^2*d - I*b^2*f)*log(f)^2)/(c^2*log(f)^2 + f^2)))/(c^2*log(f)^2 + f^2)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int f^{cx^2+bx+a} \sin(fx^2 + d) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(c*x^2+b*x+a)*sin(f*x^2+d),x, algorithm="giac")

[Out] integrate(f^(c*x^2 + b*x + a)*sin(f*x^2 + d), x)

maple [A] time = 0.63, size = 180, normalized size = 0.93

$$\frac{i\sqrt{\pi} f^a e^{-\frac{4df-4id\ln(f)c+\ln(f)^2b^2}{4(if+c\ln(f))}} \operatorname{erf}\left(-\sqrt{-if-c\ln(f)} x + \frac{\ln(f)b}{2\sqrt{-if-c\ln(f)}}\right)}{4\sqrt{-if-c\ln(f)}} - \frac{i\sqrt{\pi} f^a e^{-\frac{4df+4id\ln(f)c+\ln(f)^2b^2}{4(-if+c\ln(f))}} \operatorname{erf}\left(-x\sqrt{if-c\ln(f)}\right)}{4\sqrt{if-c\ln(f)}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(f^(c*x^2+b*x+a)*sin(f*x^2+d),x)

[Out] $\frac{1}{4}I\pi^{1/2}f^a\exp(-1/4*(4*d*f-4*I*d*\ln(f)*c+\ln(f)^2*b^2)/(I*f+c*\ln(f)))/(-I*f-c*\ln(f))^{1/2}*\operatorname{erf}(-(-I*f-c*\ln(f))^{1/2}*x+1/2*\ln(f)*b/(-I*f-c*\ln(f)))^{1/2})-1/4*I\pi^{1/2}f^a\exp(-1/4*(4*d*f+4*I*d*\ln(f)*c+\ln(f)^2*b^2)/(-I*f+c*\ln(f)))/(I*f-c*\ln(f))^{1/2}*\operatorname{erf}(-x*(I*f-c*\ln(f))^{1/2}+1/2*\ln(f)*b/(I*f-c*\ln(f))^{1/2})$

maxima [B] time = 0.37, size = 647, normalized size = 3.35

$$\frac{\sqrt{\pi} \sqrt{2c^2 \log(f)^2 + 2f^2} \left(f^a \cos\left(\frac{4df^2 + (4c^2d + b^2f) \log(f)^2}{4(c^2 \log(f)^2 + f^2)}\right) - i f^a \sin\left(\frac{4df^2 + (4c^2d + b^2f) \log(f)^2}{4(c^2 \log(f)^2 + f^2)}\right) \right) \operatorname{erf}\left(\frac{2(c \log(f) - if)}{2\sqrt{-c \log(f)}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(c*x^2+b*x+a)*sin(f*x^2+d),x, algorithm="maxima")

[Out] $-1/8*(\operatorname{sqrt}(\pi)*\operatorname{sqrt}(2*c^2*\log(f)^2 + 2*f^2))*((f^a*\cos(1/4*(4*d*f^2 + (4*c^2*d + b^2*f)*\log(f)^2)/(c^2*\log(f)^2 + f^2)) - I*f^a*\sin(1/4*(4*d*f^2 + (4*c^2*d + b^2*f)*\log(f)^2)/(c^2*\log(f)^2 + f^2)))*\operatorname{erf}(1/2*(2*(c*\log(f) - I*f)*x + b*\log(f))/\operatorname{sqrt}(-c*\log(f) + I*f)) + (f^a*\cos(1/4*(4*d*f^2 + (4*c^2*d + b^2*f)*\log(f)^2)/(c^2*\log(f)^2 + f^2)) + I*f^a*\sin(1/4*(4*d*f^2 + (4*c^2*d + b^2*f)*\log(f)^2)/(c^2*\log(f)^2 + f^2)))*\operatorname{erf}(1/2*(2*(c*\log(f) + I*f)*x + b*\log(f))/\operatorname{sqrt}(-c*\log(f) - I*f)))*\operatorname{sqrt}(c*\log(f) + \operatorname{sqrt}(c^2*\log(f)^2 + f^2)) + \operatorname{sqrt}(\pi)*\operatorname{sqrt}(2*c^2*\log(f)^2 + 2*f^2))*((I*f^a*\cos(1/4*(4*d*f^2 + (4*c^2*d + b^2*f)*\log(f)^2)/(c^2*\log(f)^2 + f^2)) + f^a*\sin(1/4*(4*d*f^2 + (4*c^2*d + b^2*f)*\log(f)^2)/(c^2*\log(f)^2 + f^2)))*\operatorname{erf}(1/2*(2*(c*\log(f) - I*f)*x + b*\log(f))/\operatorname{sqrt}(-c*\log(f) + I*f)) + (-I*f^a*\cos(1/4*(4*d*f^2 + (4*c^2*d + b^2*f)*\log(f)^2)/(c^2*\log(f)^2 + f^2)) + f^a*\sin(1/4*(4*d*f^2 + (4*c^2*d + b^2*f)*\log(f)^2)/(c^2*\log(f)^2 + f^2)))*\operatorname{erf}(1/2*(2*(c*\log(f) + I*f)*x + b*\log(f))/\operatorname{sqrt}(-c*\log(f) - I*f)))*\operatorname{sqrt}(-c*\log(f) + \operatorname{sqrt}(c^2*\log(f)^2 + f^2)))/(c^2*e^{1/4*b^2*c*\log(f)^3/(c^2*\log(f)^2 + f^2)}*\log(f)^2 + f^2*e^{1/4*b^2*c*\log(f)^3/(c^2*\log(f)^2 + f^2)}))$

mapad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int f^{cx^2+bx+a} \sin(fx^2+d) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(f^(a + b*x + c*x^2)*sin(d + f*x^2),x)

[Out] int(f^(a + b*x + c*x^2)*sin(d + f*x^2), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int f^{a+bx+cx^2} \sin(d + fx^2) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f**(c*x**2+b*x+a)*sin(f*x**2+d),x)

[Out] Integral(f**(a + b*x + c*x**2)*sin(d + f*x**2), x)

3.98 $\int f^{a+bx+cx^2} \sin^2(d + fx^2) dx$

Optimal. Leaf size=245

$$\frac{\sqrt{\pi} f^a e^{-\frac{b^2 \log^2(f)}{4c \log(f)+8if} - 2id} \operatorname{erf}\left(\frac{b \log(f) - 2x(-c \log(f) + 2if)}{2\sqrt{-c \log(f) + 2if}}\right)}{8\sqrt{-c \log(f) + 2if}} - \frac{\sqrt{\pi} f^a e^{2id - \frac{b^2 \log^2(f)}{4c \log(f)+8if}} \operatorname{erfi}\left(\frac{b \log(f) + 2x(c \log(f) + 2if)}{2\sqrt{c \log(f) + 2if}}\right)}{8\sqrt{c \log(f) + 2if}} + \frac{\sqrt{\pi} f^{a - \frac{b^2}{4c}} \operatorname{erf}\left(\frac{b \log(f)}{2\sqrt{c \log(f) + 2if}}\right)}{4\sqrt{c \log(f) + 2if}}$$

[Out] $\frac{1}{4} f^{(a-1/4*b^2/c)*\operatorname{erfi}(1/2*(2*c*x+b)*\ln(f)^{(1/2)/c^{(1/2)})*\operatorname{Pi}^{(1/2)/c^{(1/2)}}/\ln(f)^{(1/2)}+1/8*\exp(-2*I*d+b^2*\ln(f)^2/(8*I*f-4*c*\ln(f)))*f^a*\operatorname{erf}(1/2*(b*\ln(f)-2*x*(2*I*f-c*\ln(f)))/(2*I*f-c*\ln(f))^{(1/2)})*\operatorname{Pi}^{(1/2)/(2*I*f-c*\ln(f))^{(1/2)}-1/8*\exp(2*I*d-b^2*\ln(f)^2/(8*I*f+4*c*\ln(f)))*f^a*\operatorname{erfi}(1/2*(b*\ln(f)+2*x*(2*I*f+c*\ln(f)))/(2*I*f+c*\ln(f))^{(1/2)})*\operatorname{Pi}^{(1/2)/(2*I*f+c*\ln(f))^{(1/2)}}$

Rubi [A] time = 0.46, antiderivative size = 245, normalized size of antiderivative = 1.00, number of steps used = 10, number of rules used = 5, integrand size = 23, $\frac{\text{number of rules}}{\text{integrand size}} = 0.217$, Rules used = {4472, 2234, 2204, 2287, 2205}

$$\frac{\sqrt{\pi} f^a e^{-\frac{b^2 \log^2(f)}{4c \log(f)+8if} - 2id} \operatorname{Erf}\left(\frac{b \log(f) - 2x(-c \log(f) + 2if)}{2\sqrt{-c \log(f) + 2if}}\right)}{8\sqrt{-c \log(f) + 2if}} - \frac{\sqrt{\pi} f^a e^{2id - \frac{b^2 \log^2(f)}{4c \log(f)+8if}} \operatorname{Erfi}\left(\frac{b \log(f) + 2x(c \log(f) + 2if)}{2\sqrt{c \log(f) + 2if}}\right)}{8\sqrt{c \log(f) + 2if}} + \frac{\sqrt{\pi} f^{a - \frac{b^2}{4c}} \operatorname{Erf}\left(\frac{b \log(f)}{2\sqrt{c \log(f) + 2if}}\right)}{4\sqrt{c \log(f) + 2if}}$$

Antiderivative was successfully verified.

[In] Int[f^(a + b*x + c*x^2)*Sin[d + f*x^2]^2,x]

[Out] $(f^{(a - b^2/(4*c))*\operatorname{Sqrt}[\operatorname{Pi}]*\operatorname{Erfi}(((b + 2*c*x)*\operatorname{Sqrt}[\operatorname{Log}[f]])/(2*\operatorname{Sqrt}[c])))/(4*\operatorname{Sqrt}[c]*\operatorname{Sqrt}[\operatorname{Log}[f]]) + (E^{((-2*I)*d + (b^2*\operatorname{Log}[f]^2)/((8*I)*f - 4*c*\operatorname{Log}[f]))}*f^a*\operatorname{Sqrt}[\operatorname{Pi}]*\operatorname{Erf}[(b*\operatorname{Log}[f] - 2*x*((2*I)*f - c*\operatorname{Log}[f]))/(2*\operatorname{Sqrt}[(2*I)*f - c*\operatorname{Log}[f]])]/(8*\operatorname{Sqrt}[(2*I)*f - c*\operatorname{Log}[f]]) - (E^{((2*I)*d - (b^2*\operatorname{Log}[f]^2)/((8*I)*f + 4*c*\operatorname{Log}[f]))}*f^a*\operatorname{Sqrt}[\operatorname{Pi}]*\operatorname{Erfi}[(b*\operatorname{Log}[f] + 2*x*((2*I)*f + c*\operatorname{Log}[f]))/(2*\operatorname{Sqrt}[(2*I)*f + c*\operatorname{Log}[f]])]/(8*\operatorname{Sqrt}[(2*I)*f + c*\operatorname{Log}[f]])$

Rule 2204

Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_)^2), x_Symbol] := Simp[(F^a*Sqrt[Pi]*Erfi[(c + d*x)*Rt[b*Log[F], 2]]/(2*d*Rt[b*Log[F], 2]), x] /; FreeQ[{F, a, b, c, d}, x] && PosQ[b]

Rule 2205

Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_)^2), x_Symbol] := Simp[(F^a*Sqrt[Pi]*Erf[(c + d*x)*Rt[-(b*Log[F]), 2]]/(2*d*Rt[-(b*Log[F]), 2]), x] /; FreeQ[{F, a, b, c, d}, x] && NegQ[b]

Rule 2234

Int[(F_)^((a_.) + (b_.)*(x_) + (c_.)*(x_)^2), x_Symbol] := Dist[F^(a - b^2/(4*c)), Int[F^((b + 2*c*x)^2/(4*c)), x], x] /; FreeQ[{F, a, b, c}, x]

Rule 2287

Int[(u_.)*(F_)^(v_.)*(G_)^(w_.), x_Symbol] := With[{z = v*Log[F] + w*Log[G]}, Int[u*NormalizeIntegrand[E^z, x], x] /; BinomialQ[z, x] || (PolynomialQ[z, x] && LeQ[Exponent[z, x], 2]) /; FreeQ[{F, G}, x]

Rule 4472

Int[(F_)^(u_.)*Sin[v_]^(n_.), x_Symbol] := Int[ExpandTrigToExp[F^u, Sin[v]^n, x], x] /; FreeQ[F, x] && (LinearQ[u, x] || PolyQ[u, x, 2]) && (LinearQ[v,

x] || PolyQ[v, x, 2]) && IGtQ[n, 0]

Rubi steps

$$\begin{aligned}
 \int f^{a+bx+cx^2} \sin^2(d + fx^2) dx &= \int \left(\frac{1}{2} f^{a+bx+cx^2} - \frac{1}{4} e^{-2id-2ifx^2} f^{a+bx+cx^2} - \frac{1}{4} e^{2id+2ifx^2} f^{a+bx+cx^2} \right) dx \\
 &= -\left(\frac{1}{4} \int e^{-2id-2ifx^2} f^{a+bx+cx^2} dx \right) - \frac{1}{4} \int e^{2id+2ifx^2} f^{a+bx+cx^2} dx + \frac{1}{2} \int f^{a+bx+cx^2} dx \\
 &= -\left(\frac{1}{4} \int \exp(-2id + a \log(f) + bx \log(f) - x^2(2if - c \log(f))) dx \right) - \frac{1}{4} \int \exp \\
 &= \frac{f^{a-\frac{b^2}{4c}} \sqrt{\pi} \operatorname{erfi}\left(\frac{(b+2cx)\sqrt{\log(f)}}{2\sqrt{c}}\right)}{4\sqrt{c}\sqrt{\log(f)}} - \frac{1}{4} \left(e^{-2id+\frac{b^2 \log^2(f)}{8if-4c \log(f)}} f^a \right) \int \exp\left(\frac{(b \log(f) + 2x(-2if + c \log(f)))}{4(-2if + c \log(f))}\right) dx \\
 &= \frac{f^{a-\frac{b^2}{4c}} \sqrt{\pi} \operatorname{erfi}\left(\frac{(b+2cx)\sqrt{\log(f)}}{2\sqrt{c}}\right)}{4\sqrt{c}\sqrt{\log(f)}} + \frac{e^{-2id+\frac{b^2 \log^2(f)}{8if-4c \log(f)}} f^a \sqrt{\pi} \operatorname{erf}\left(\frac{b \log(f) - 2x(2if - c \log(f))}{2\sqrt{2if - c \log(f)}}\right)}{8\sqrt{2if - c \log(f)}}
 \end{aligned}$$

Mathematica [A] time = 3.09, size = 299, normalized size = 1.22

$$\frac{1}{8} \sqrt{\pi} f^a \left(\frac{2f^{-\frac{b^2}{4c}} \operatorname{erfi}\left(\frac{\sqrt{\log(f)}(b+2cx)}{2\sqrt{c}}\right)}{\sqrt{c}\sqrt{\log(f)}} + \frac{\sqrt[4]{-1} e^{\frac{b^2 \log^2(f)}{-4c \log(f)+8if}} \left(\sqrt{2f - ic \log(f)} (2f + ic \log(f)) (\cos(2d) + i \sin(2d)) e^{\frac{ib^2}{c^2 \log(f)}} \right)}{\sqrt{2f - ic \log(f)} (2f + ic \log(f)) (\cos(2d) + i \sin(2d)) e^{\frac{ib^2}{c^2 \log(f)}}}} \right)$$

Warning: Unable to verify antiderivative.

[In] Integrate[f^(a + b*x + c*x^2)*Sin[d + f*x^2]^2,x]

[Out] (f^a*Sqrt[Pi]*((2*Erfi[((b + 2*c*x)*Sqrt[Log[f]])/(2*Sqrt[c])])/(Sqrt[c]*f^(b^2/(4*c))*Sqrt[Log[f]]) + ((-1)^(1/4)*E^((b^2*Log[f]^2)/((8*I)*f - 4*c*Log[f]))*(Erf[((-1)^(1/4)*(4*f*x + I*(b + 2*c*x)*Log[f]))/(2*Sqrt[2*f + I*c*Log[f]])]*Sqrt[2*f + I*c*Log[f]]*((2*I)*f + c*Log[f])*(Cos[2*d] - I*Sin[2*d]) + E^((I*b^2*f*Log[f]^2)/(4*f^2 + c^2*Log[f]^2))*Erf[((-1)^(3/4)*(4*f*x - I*(b + 2*c*x)*Log[f]))/(2*Sqrt[2*f - I*c*Log[f]])]*Sqrt[2*f - I*c*Log[f]]*(2*f + I*c*Log[f])*(Cos[2*d] + I*Sin[2*d])))/(4*f^2 + c^2*Log[f]^2))/8

fricas [B] time = 0.96, size = 400, normalized size = 1.63

$$\sqrt{\pi} (c^2 \log(f)^2 - 2icf \log(f)) \sqrt{-c \log(f) - 2if} \operatorname{erf}\left(\frac{(8f^2x - 2ibf \log(f) + (2c^2x + bc) \log(f)^2) \sqrt{-c \log(f) - 2if}}{2(c^2 \log(f)^2 + 4f^2)}\right) e^{\left(\frac{16af^2 \log(f) - (b^2c - 4ac^2) \log(f)^3 + 32Idf^2 + (8Ic^2d + 2Ib^2f) \log(f)^2}{c^2 \log(f)^2 + 4f^2}\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(c*x^2+b*x+a)*sin(f*x^2+d)^2,x, algorithm="fricas")

[Out] 1/8*(sqrt(pi)*(c^2*log(f)^2 - 2I*c*f*log(f))*sqrt(-c*log(f) - 2I*f)*erf(1/2*(8*f^2*x - 2I*b*f*log(f) + (2*c^2*x + b*c)*log(f)^2)*sqrt(-c*log(f) - 2I*f)/(c^2*log(f)^2 + 4*f^2))*e^(1/4*(16*a*f^2*log(f) - (b^2*c - 4*a*c^2)*log(f)^3 + 32*I*d*f^2 + (8*I*c^2*d + 2*I*b^2*f)*log(f)^2)/(c^2*log(f)^2 + 4*f^2)) + sqrt(pi)*(c^2*log(f)^2 + 2I*c*f*log(f))*sqrt(-c*log(f) + 2I*f)*erf(1/2*(8*f^2*x + 2I*b*f*log(f) + (2*c^2*x + b*c)*log(f)^2)*sqrt(-c*log(f) + 2I*f)/(c^2*log(f)^2 + 4*f^2))


```
+ 4*f^2))*log(f)^2 + 4*f^(a + 2)*e^(1/4*b^2*c*log(f)^3/(c^2*log(f)^2 + 4*f^2)))*erf(1/2*(2*c*x*log(f) + b*log(f))/sqrt(-c*log(f)))))/((c^2*e^(1/4*b^2*c*log(f)^3/(c^2*log(f)^2 + 4*f^2) + 1/4*b^2*log(f)/c)*log(f)^2 + 4*f^2*e^(1/4*b^2*c*log(f)^3/(c^2*log(f)^2 + 4*f^2) + 1/4*b^2*log(f)/c))*sqrt(-c*log(f))))
```

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int f^{cx^2+bx+a} \sin(fx^2+d)^2 dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(f^(a + b*x + c*x^2)*sin(d + f*x^2)^2,x)
```

```
[Out] int(f^(a + b*x + c*x^2)*sin(d + f*x^2)^2, x)
```

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int f^{a+bx+cx^2} \sin^2(d + fx^2) dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(f**(c*x**2+b*x+a)*sin(f*x**2+d)**2,x)
```

```
[Out] Integral(f**(a + b*x + c*x**2)*sin(d + f*x**2)**2, x)
```


3.99 $\int f^{a+bx+cx^2} \sin^3(d + fx^2) dx$

Optimal. Leaf size=386

$$\frac{3i\sqrt{\pi} f^a e^{\frac{b^2 \log^2(f)}{-4c \log(f)+4if} - id} \operatorname{erf}\left(\frac{b \log(f) - 2x(-c \log(f) + if)}{2\sqrt{-c \log(f) + if}}\right)}{16\sqrt{-c \log(f) + if}} + \frac{i\sqrt{\pi} f^a e^{\frac{b^2 \log^2(f)}{-4c \log(f)+12if} - 3id} \operatorname{erf}\left(\frac{b \log(f) - 2x(-c \log(f) + 3if)}{2\sqrt{-c \log(f) + 3if}}\right)}{16\sqrt{-c \log(f) + 3if}} + \frac{i\sqrt{\pi} f^a e^{\frac{b^2 \log^2(f)}{-4c \log(f)+4if} - id} \operatorname{erf}\left(\frac{b \log(f) - 2x(-c \log(f) + if)}{2\sqrt{-c \log(f) + if}}\right)}{16\sqrt{-c \log(f) + if}}$$

[Out] $-3/16*I*\exp(-I*d+b^2*\ln(f)^2/(4*I*f-4*c*\ln(f)))*f^a*\operatorname{erf}(1/2*(b*\ln(f)-2*x*(I*f-c*\ln(f)))/(I*f-c*\ln(f)))^{1/2})*\operatorname{Pi}^{1/2}/(I*f-c*\ln(f))^{1/2}+1/16*I*\exp(-3*I*d+b^2*\ln(f)^2/(12*I*f-4*c*\ln(f)))*f^a*\operatorname{erf}(1/2*(b*\ln(f)-2*x*(3*I*f-c*\ln(f)))/(3*I*f-c*\ln(f)))^{1/2})*\operatorname{Pi}^{1/2}/(3*I*f-c*\ln(f))^{1/2}-3/16*I*\exp(I*d-b^2*\ln(f)^2/(4*I*f+4*c*\ln(f)))*f^a*\operatorname{erfi}(1/2*(b*\ln(f)+2*x*(I*f+c*\ln(f)))/(I*f+c*\ln(f)))^{1/2})*\operatorname{Pi}^{1/2}/(I*f+c*\ln(f))^{1/2}+1/16*I*\exp(3*I*d-1/4*b^2*\ln(f)^2/(3*I*f+c*\ln(f)))*f^a*\operatorname{erfi}(1/2*(b*\ln(f)+2*x*(3*I*f+c*\ln(f)))/(3*I*f+c*\ln(f)))^{1/2})*\operatorname{Pi}^{1/2}/(3*I*f+c*\ln(f))^{1/2}$

Rubi [A] time = 0.57, antiderivative size = 386, normalized size of antiderivative = 1.00, number of steps used = 14, number of rules used = 5, integrand size = 23, $\frac{\text{number of rules}}{\text{integrand size}} = 0.217$, Rules used = {4472, 2287, 2234, 2205, 2204}

$$\frac{3i\sqrt{\pi} f^a e^{\frac{b^2 \log^2(f)}{-4c \log(f)+4if} - id} \operatorname{Erf}\left(\frac{b \log(f) - 2x(-c \log(f) + if)}{2\sqrt{-c \log(f) + if}}\right)}{16\sqrt{-c \log(f) + if}} + \frac{i\sqrt{\pi} f^a e^{\frac{b^2 \log^2(f)}{-4c \log(f)+12if} - 3id} \operatorname{Erf}\left(\frac{b \log(f) - 2x(-c \log(f) + 3if)}{2\sqrt{-c \log(f) + 3if}}\right)}{16\sqrt{-c \log(f) + 3if}} + \frac{i\sqrt{\pi} f^a e^{\frac{b^2 \log^2(f)}{-4c \log(f)+4if} - id} \operatorname{Erf}\left(\frac{b \log(f) - 2x(-c \log(f) + if)}{2\sqrt{-c \log(f) + if}}\right)}{16\sqrt{-c \log(f) + if}}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[f^{(a + b*x + c*x^2)}*\operatorname{Sin}[d + f*x^2]^3, x]$

[Out] $(((-3*I)/16)*E^{(-I)*d + (b^2*\operatorname{Log}[f]^2)/((4*I)*f - 4*c*\operatorname{Log}[f])})*f^a*\operatorname{Sqrt}[\operatorname{Pi}]*\operatorname{Erf}[(b*\operatorname{Log}[f] - 2*x*(I*f - c*\operatorname{Log}[f]))/(2*\operatorname{Sqrt}[I*f - c*\operatorname{Log}[f]])]/\operatorname{Sqrt}[I*f - c*\operatorname{Log}[f]] + ((I/16)*E^{(-3*I)*d + (b^2*\operatorname{Log}[f]^2)/((12*I)*f - 4*c*\operatorname{Log}[f])})*f^a*\operatorname{Sqrt}[\operatorname{Pi}]*\operatorname{Erf}[(b*\operatorname{Log}[f] - 2*x*((3*I)*f - c*\operatorname{Log}[f]))/(2*\operatorname{Sqrt}[(3*I)*f - c*\operatorname{Log}[f]])]/\operatorname{Sqrt}[(3*I)*f - c*\operatorname{Log}[f]] - (((3*I)/16)*E^{(I*d - (b^2*\operatorname{Log}[f]^2)/((4*I)*f + 4*c*\operatorname{Log}[f])})*f^a*\operatorname{Sqrt}[\operatorname{Pi}]*\operatorname{Erfi}[(b*\operatorname{Log}[f] + 2*x*(I*f + c*\operatorname{Log}[f]))/(2*\operatorname{Sqrt}[I*f + c*\operatorname{Log}[f]])]/\operatorname{Sqrt}[I*f + c*\operatorname{Log}[f]] + ((I/16)*E^{(3*I)*d - (b^2*\operatorname{Log}[f]^2)/(4*((3*I)*f + c*\operatorname{Log}[f]))})*f^a*\operatorname{Sqrt}[\operatorname{Pi}]*\operatorname{Erfi}[(b*\operatorname{Log}[f] + 2*x*((3*I)*f + c*\operatorname{Log}[f]))/(2*\operatorname{Sqrt}[(3*I)*f + c*\operatorname{Log}[f]])]/\operatorname{Sqrt}[(3*I)*f + c*\operatorname{Log}[f]])$

Rule 2204

$\operatorname{Int}[(F_)^{((a_.) + (b_.)*((c_.) + (d_.)*(x_))^2)}, x_Symbol] \rightarrow \operatorname{Simp}[(F^a*\operatorname{Sqrt}[\operatorname{Pi}]*\operatorname{Erfi}[(c + d*x)*\operatorname{Rt}[b*\operatorname{Log}[F], 2]])/(2*d*\operatorname{Rt}[b*\operatorname{Log}[F], 2]), x] /; \operatorname{FreeQ}\{F, a, b, c, d\}, x] \ \&\& \operatorname{PosQ}[b]$

Rule 2205

$\operatorname{Int}[(F_)^{((a_.) + (b_.)*((c_.) + (d_.)*(x_))^2)}, x_Symbol] \rightarrow \operatorname{Simp}[(F^a*\operatorname{Sqrt}[\operatorname{Pi}]*\operatorname{Erf}[(c + d*x)*\operatorname{Rt}[-(b*\operatorname{Log}[F]), 2]])/(2*d*\operatorname{Rt}[-(b*\operatorname{Log}[F]), 2]), x] /; \operatorname{FreeQ}\{F, a, b, c, d\}, x] \ \&\& \operatorname{NegQ}[b]$

Rule 2234

$\operatorname{Int}[(F_)^{((a_.) + (b_.)*(x_) + (c_.)*(x_)^2)}, x_Symbol] \rightarrow \operatorname{Dist}[F^{(a - b^2/(4*c))}, \operatorname{Int}[F^{((b + 2*c*x)^2/(4*c))}, x], x] /; \operatorname{FreeQ}\{F, a, b, c\}, x]$

Rule 2287

$\operatorname{Int}[(u_.)*(F_)^{(v_.)*(G_)^{(w_.)}}, x_Symbol] \rightarrow \operatorname{With}\{z = v*\operatorname{Log}[F] + w*\operatorname{Log}[G]\}, \operatorname{Int}[u*\operatorname{NormalizeIntegrand}[E^z, x], x] /; \operatorname{BinomialQ}[z, x] \ || \ (\operatorname{PolynomialQ}[z,$

x] && LeQ[Exponent[z, x], 2]]) /; FreeQ[{F, G}, x]

Rule 4472

Int[(F_)^(u_)*Sin[v_]^(n_), x_Symbol] := Int[ExpandTrigToExp[F^u, Sin[v]^n, x], x] /; FreeQ[F, x] && (LinearQ[u, x] || PolyQ[u, x, 2]) && (LinearQ[v, x] || PolyQ[v, x, 2]) && IGtQ[n, 0]

Rubi steps

$$\begin{aligned} \int f^{a+bx+cx^2} \sin^3(d+fx^2) dx &= \int \left(\frac{3}{8} i e^{-id-ifx^2} f^{a+bx+cx^2} - \frac{3}{8} i e^{id+ifx^2} f^{a+bx+cx^2} - \frac{1}{8} i e^{-3id-3ifx^2} f^{a+bx+cx^2} + \frac{1}{8} i e^{3id+3ifx^2} f^{a+bx+cx^2} \right) dx \\ &= -\left(\frac{1}{8} i \int e^{-3id-3ifx^2} f^{a+bx+cx^2} dx \right) + \frac{1}{8} i \int e^{3id+3ifx^2} f^{a+bx+cx^2} dx + \frac{3}{8} i \int e^{-id-ifx^2} f^{a+bx+cx^2} dx \\ &= -\left(\frac{1}{8} i \int \exp(-3id + a \log(f) + bx \log(f) - x^2(3if - c \log(f))) dx \right) + \frac{1}{8} i \int \exp(3id + a \log(f) + bx \log(f) - x^2(3if - c \log(f))) dx \\ &= \frac{1}{8} \left(3 i e^{-id + \frac{b^2 \log^2(f)}{4if - 4c \log(f)}} f^a \right) \int \exp\left(\frac{(b \log(f) + 2x(-if + c \log(f)))^2}{4(-if + c \log(f))}\right) dx - \frac{1}{8} \left(i e^{-3id + \frac{b^2 \log^2(f)}{4if - 4c \log(f)}} f^a \right) \int \exp\left(\frac{(b \log(f) + 2x(-if + c \log(f)))^2}{4(-if + c \log(f))}\right) dx \\ &= -\frac{3 i e^{-id + \frac{b^2 \log^2(f)}{4if - 4c \log(f)}} f^a \sqrt{\pi} \operatorname{erf}\left(\frac{b \log(f) - 2x(if - c \log(f))}{2\sqrt{if - c \log(f)}}\right)}{16\sqrt{if - c \log(f)}} + \frac{i e^{-3id + \frac{b^2 \log^2(f)}{4if - 4c \log(f)}} f^a \sqrt{\pi} \operatorname{erf}\left(\frac{b \log(f) + 2x(-if + c \log(f))}{2\sqrt{if - c \log(f)}}\right)}{16\sqrt{3if - c \log(f)}} \end{aligned}$$

Mathematica [B] time = 7.04, size = 3291, normalized size = 8.53

Result too large to show

Antiderivative was successfully verified.

[In] Integrate[f^(a + b*x + c*x^2)*Sin[d + f*x^2]^3,x]

[Out] (f^a*Sqrt[Pi]*(-27*(-1)^(3/4)*E^(((I/4)*b^2*Log[f]^2)/(f - I*c*Log[f])))*f^3*Cos[d]*Erfi[(-1)^(1/4)*(2*f*x - I*b*Log[f] - (2*I)*c*x*Log[f])]/(2*Sqrt[f - I*c*Log[f]])]*Sqrt[f - I*c*Log[f]] + 27*(-1)^(1/4)*c*E^(((I/4)*b^2*Log[f]^2)/(f - I*c*Log[f])))*f^2*Cos[d]*Erfi[(-1)^(1/4)*(2*f*x - I*b*Log[f] - (2*I)*c*x*Log[f])]/(2*Sqrt[f - I*c*Log[f]])]*Log[f]*Sqrt[f - I*c*Log[f]] - 3*(-1)^(3/4)*c^2*E^(((I/4)*b^2*Log[f]^2)/(f - I*c*Log[f])))*f*Cos[d]*Erfi[(-1)^(1/4)*(2*f*x - I*b*Log[f] - (2*I)*c*x*Log[f])]/(2*Sqrt[f - I*c*Log[f]])]*Log[f]^2*Sqrt[f - I*c*Log[f]] + 3*(-1)^(1/4)*c^3*E^(((I/4)*b^2*Log[f]^2)/(f - I*c*Log[f])))*Cos[d]*Erfi[(-1)^(1/4)*(2*f*x - I*b*Log[f] - (2*I)*c*x*Log[f])]/(2*Sqrt[f - I*c*Log[f]])]*Log[f]^3*Sqrt[f - I*c*Log[f]] + 3*(-1)^(3/4)*E^(((I/4)*b^2*Log[f]^2)/(3*f - I*c*Log[f])))*f^3*Cos[3*d]*Erfi[(-1)^(1/4)*(6*f*x - I*b*Log[f] - (2*I)*c*x*Log[f])]/(2*Sqrt[3*f - I*c*Log[f]])]*Sqrt[3*f - I*c*Log[f]] - (-1)^(1/4)*c*E^(((I/4)*b^2*Log[f]^2)/(3*f - I*c*Log[f])))*f^2*Cos[3*d]*Erfi[(-1)^(1/4)*(6*f*x - I*b*Log[f] - (2*I)*c*x*Log[f])]/(2*Sqrt[3*f - I*c*Log[f]])]*Log[f]*Sqrt[3*f - I*c*Log[f]] + 3*(-1)^(3/4)*c^2*E^(((I/4)*b^2*Log[f]^2)/(3*f - I*c*Log[f])))*f*Cos[3*d]*Erfi[(-1)^(1/4)*(6*f*x - I*b*Log[f] - (2*I)*c*x*Log[f])]/(2*Sqrt[3*f - I*c*Log[f]])]*Log[f]^2*Sqrt[3*f - I*c*Log[f]] - (-1)^(1/4)*c^3*E^(((I/4)*b^2*Log[f]^2)/(3*f - I*c*Log[f])))*Cos[3*d]*Erfi[(-1)^(1/4)*(6*f*x - I*b*Log[f] - (2*I)*c*x*Log[f])]/(2*Sqrt[3*f - I*c*Log[f]])]*Log[f]^3*Sqrt[3*f - I*c*Log[f]] + (27*(-1)^(1/4)*f^3*Cos[d]*Erfi[(-1)^(3/4)*(2*f*x + I*b*Log[f] + (2*I)*c*x*Log[f])]/(2*Sqrt[f + I*c*Log[f]])]*Sqrt[f + I*c*Log[f]])/E^(((I/4)*b^2*Log[f]^2)/(f + I*c*Log[f])) - (27*(-1)^(3/4)*c*f^2*Cos[d]*Erfi[(-1)^(3/4)*(2*f*x + I*b*Log[f] + (2*I)*c*x*Log[f])]/(2*Sqrt[f + I*c*Log[f]])]*Log[f]*Sqrt[f + I*c*Log[f]])/E^(((I/4)*b^2*Log[f]^2)/(f + I*c*Log[f])) + (3*(-1)^(1/4)*c^2*f*Cos[d]

$$\begin{aligned}
& *Erfi[(-1)^{3/4}*(2*f*x + I*b*Log[f] + (2*I)*c*x*Log[f])]/(2*sqrt[f + I*c*Log[f]])*Log[f]^2*sqrt[f + I*c*Log[f]]/E^{((I/4)*b^2*Log[f]^2)/(f + I*c*Log[f])} - (3*(-1)^{3/4}*c^3*Cos[d]*Erfi[(-1)^{3/4}*(2*f*x + I*b*Log[f] + (2*I)*c*x*Log[f])]/(2*sqrt[f + I*c*Log[f]])*Log[f]^3*sqrt[f + I*c*Log[f]])/E^{((I/4)*b^2*Log[f]^2)/(f + I*c*Log[f])} - (3*(-1)^{1/4}*f^3*Cos[3*d]*Erfi[(-1)^{3/4}*(6*f*x + I*b*Log[f] + (2*I)*c*x*Log[f])]/(2*sqrt[3*f + I*c*Log[f]])*sqrt[3*f + I*c*Log[f]]/E^{((I/4)*b^2*Log[f]^2)/(3*f + I*c*Log[f])} + ((-1)^{3/4}*c*f^2*Cos[3*d]*Erfi[(-1)^{3/4}*(6*f*x + I*b*Log[f] + (2*I)*c*x*Log[f])]/(2*sqrt[3*f + I*c*Log[f]])*Log[f]*sqrt[3*f + I*c*Log[f]])/E^{((I/4)*b^2*Log[f]^2)/(3*f + I*c*Log[f])} - (3*(-1)^{1/4}*c^2*f*Cos[3*d]*Erfi[(-1)^{3/4}*(6*f*x + I*b*Log[f] + (2*I)*c*x*Log[f])]/(2*sqrt[3*f + I*c*Log[f]])*Log[f]^2*sqrt[3*f + I*c*Log[f]])/E^{((I/4)*b^2*Log[f]^2)/(3*f + I*c*Log[f])} + ((-1)^{3/4}*c^3*Cos[3*d]*Erfi[(-1)^{3/4}*(6*f*x + I*b*Log[f] + (2*I)*c*x*Log[f])]/(2*sqrt[3*f + I*c*Log[f]])*Log[f]^3*sqrt[3*f + I*c*Log[f]])/E^{((I/4)*b^2*Log[f]^2)/(3*f + I*c*Log[f])} + 27*(-1)^{1/4}*E^{((I/4)*b^2*Log[f]^2)/(f - I*c*Log[f])}*f^3*Erfi[(-1)^{1/4}*(2*f*x - I*b*Log[f] - (2*I)*c*x*Log[f])]/(2*sqrt[f - I*c*Log[f]])*sqrt[f - I*c*Log[f]]*Sin[d] + 27*(-1)^{3/4}*c*E^{((I/4)*b^2*Log[f]^2)/(f - I*c*Log[f])}*f^2*Erfi[(-1)^{1/4}*(2*f*x - I*b*Log[f] - (2*I)*c*x*Log[f])]/(2*sqrt[f - I*c*Log[f]])*Log[f]*sqrt[f - I*c*Log[f]]*Sin[d] + 3*(-1)^{1/4}*c^2*E^{((I/4)*b^2*Log[f]^2)/(f - I*c*Log[f])}*f*Erfi[(-1)^{1/4}*(2*f*x - I*b*Log[f] - (2*I)*c*x*Log[f])]/(2*sqrt[f - I*c*Log[f]])*Log[f]^2*sqrt[f - I*c*Log[f]]*Sin[d] + 3*(-1)^{3/4}*c^3*E^{((I/4)*b^2*Log[f]^2)/(f - I*c*Log[f])}*Erfi[(-1)^{1/4}*(2*f*x - I*b*Log[f] - (2*I)*c*x*Log[f])]/(2*sqrt[f - I*c*Log[f]])*Log[f]^3*sqrt[f - I*c*Log[f]]*Sin[d] - (27*(-1)^{3/4}*f^3*Erfi[(-1)^{3/4}*(2*f*x + I*b*Log[f] + (2*I)*c*x*Log[f])]/(2*sqrt[f + I*c*Log[f]])*sqrt[f + I*c*Log[f]]*Sin[d])/E^{((I/4)*b^2*Log[f]^2)/(f + I*c*Log[f])} - (27*(-1)^{1/4}*c*f^2*Erfi[(-1)^{3/4}*(2*f*x + I*b*Log[f] + (2*I)*c*x*Log[f])]/(2*sqrt[f + I*c*Log[f]])*Log[f]*sqrt[f + I*c*Log[f]]*Sin[d])/E^{((I/4)*b^2*Log[f]^2)/(f + I*c*Log[f])} - (3*(-1)^{3/4}*c^2*f*Erfi[(-1)^{3/4}*(2*f*x + I*b*Log[f] + (2*I)*c*x*Log[f])]/(2*sqrt[f + I*c*Log[f]])*Log[f]^2*sqrt[f + I*c*Log[f]]*Sin[d])/E^{((I/4)*b^2*Log[f]^2)/(f + I*c*Log[f])} - (3*(-1)^{1/4}*c^3*Erfi[(-1)^{3/4}*(2*f*x + I*b*Log[f] + (2*I)*c*x*Log[f])]/(2*sqrt[f + I*c*Log[f]])*Log[f]^3*sqrt[f + I*c*Log[f]]*Sin[d])/E^{((I/4)*b^2*Log[f]^2)/(f + I*c*Log[f])} - 3*(-1)^{1/4}*E^{((I/4)*b^2*Log[f]^2)/(3*f - I*c*Log[f])}*f^3*Erfi[(-1)^{1/4}*(6*f*x - I*b*Log[f] - (2*I)*c*x*Log[f])]/(2*sqrt[3*f - I*c*Log[f]])*sqrt[3*f - I*c*Log[f]]*Sin[3*d] - (-1)^{3/4}*c*E^{((I/4)*b^2*Log[f]^2)/(3*f - I*c*Log[f])}*f^2*Erfi[(-1)^{1/4}*(6*f*x - I*b*Log[f] - (2*I)*c*x*Log[f])]/(2*sqrt[3*f - I*c*Log[f]])*Log[f]*sqrt[3*f - I*c*Log[f]]*Sin[3*d] - 3*(-1)^{1/4}*c^2*E^{((I/4)*b^2*Log[f]^2)/(3*f - I*c*Log[f])}*f*Erfi[(-1)^{1/4}*(6*f*x - I*b*Log[f] - (2*I)*c*x*Log[f])]/(2*sqrt[3*f - I*c*Log[f]])*Log[f]^2*sqrt[3*f - I*c*Log[f]]*Sin[3*d] - (-1)^{3/4}*c^3*E^{((I/4)*b^2*Log[f]^2)/(3*f - I*c*Log[f])}*Erfi[(-1)^{1/4}*(6*f*x - I*b*Log[f] - (2*I)*c*x*Log[f])]/(2*sqrt[3*f - I*c*Log[f]])*Log[f]^3*sqrt[3*f - I*c*Log[f]]*Sin[3*d] + (3*(-1)^{3/4}*f^3*Erfi[(-1)^{3/4}*(6*f*x + I*b*Log[f] + (2*I)*c*x*Log[f])]/(2*sqrt[3*f + I*c*Log[f]])*sqrt[3*f + I*c*Log[f]]*Sin[3*d])/E^{((I/4)*b^2*Log[f]^2)/(3*f + I*c*Log[f])} + ((-1)^{1/4}*c*f^2*Erfi[(-1)^{3/4}*(6*f*x + I*b*Log[f] + (2*I)*c*x*Log[f])]/(2*sqrt[3*f + I*c*Log[f]])*Log[f]*sqrt[3*f + I*c*Log[f]]*Sin[3*d])/E^{((I/4)*b^2*Log[f]^2)/(3*f + I*c*Log[f])} + (3*(-1)^{3/4}*c^2*f*Erfi[(-1)^{3/4}*(6*f*x + I*b*Log[f] + (2*I)*c*x*Log[f])]/(2*sqrt[3*f + I*c*Log[f]])*Log[f]^2*sqrt[3*f + I*c*Log[f]]*Sin[3*d])/E^{((I/4)*b^2*Log[f]^2)/(3*f + I*c*Log[f])} + ((-1)^{1/4}*c^3*Erfi[(-1)^{3/4}*(6*f*x + I*b*Log[f] + (2*I)*c*x*Log[f])]/(2*sqrt[3*f + I*c*Log[f]])*Log[f]^3*sqrt[3*f + I*c*Log[f]]*Sin[3*d])/E^{((I/4)*b^2*Log[f]^2)/(3*f + I*c*Log[f])}))/((16*(I*f - c*Log[f])*(f - I*c*Log[f])*(3*f - I*c*Log[f])*(3*f + I*c*Log[f]))
\end{aligned}$$

fricas [B] time = 2.00, size = 727, normalized size = 1.88

$$\frac{\sqrt{\pi} \left(-ic^3 \log(f)^3 - 3c^2 f \log(f)^2 - icf^2 \log(f) - 3f^3 \right) \sqrt{-c \log(f) - 3if} \operatorname{erf} \left(\frac{(18f^2x - 3ibf \log(f) + (2c^2x + bc) \log(f)^2) \sqrt{-c \log(f) - 3if}}{2(c^2 \log(f)^2 + 9f^2)} \right)}{1}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(c*x^2+b*x+a)*sin(f*x^2+d)^3,x, algorithm="fricas")

[Out] 1/16*(sqrt(pi)*(-I*c^3*log(f)^3 - 3*c^2*f*log(f)^2 - I*c*f^2*log(f) - 3*f^3)*sqrt(-c*log(f) - 3*I*f)*erf(1/2*(18*f^2*x - 3*I*b*f*log(f) + (2*c^2*x + b*c)*log(f)^2)*sqrt(-c*log(f) - 3*I*f)/(c^2*log(f)^2 + 9*f^2))*e^(1/4*(36*a*f^2*log(f) - (b^2*c - 4*a*c^2)*log(f)^3 + 108*I*d*f^2 + (12*I*c^2*d + 3*I*b^2*f)*log(f)^2)/(c^2*log(f)^2 + 9*f^2)) + sqrt(pi)*(I*c^3*log(f)^3 - 3*c^2*f*log(f)^2 + I*c*f^2*log(f) - 3*f^3)*sqrt(-c*log(f) + 3*I*f)*erf(1/2*(18*f^2*x + 3*I*b*f*log(f) + (2*c^2*x + b*c)*log(f)^2)*sqrt(-c*log(f) + 3*I*f)/(c^2*log(f)^2 + 9*f^2))*e^(1/4*(36*a*f^2*log(f) - (b^2*c - 4*a*c^2)*log(f)^3 - 108*I*d*f^2 + (-12*I*c^2*d - 3*I*b^2*f)*log(f)^2)/(c^2*log(f)^2 + 9*f^2)) + sqrt(pi)*(3*I*c^3*log(f)^3 + 3*c^2*f*log(f)^2 + 27*I*c*f^2*log(f) + 27*f^3)*sqrt(-c*log(f) - I*f)*erf(1/2*(2*f^2*x - I*b*f*log(f) + (2*c^2*x + b*c)*log(f)^2)*sqrt(-c*log(f) - I*f)/(c^2*log(f)^2 + f^2))*e^(1/4*(4*a*f^2*log(f) - (b^2*c - 4*a*c^2)*log(f)^3 + 4*I*d*f^2 + (4*I*c^2*d + I*b^2*f)*log(f)^2)/(c^2*log(f)^2 + f^2)) + sqrt(pi)*(-3*I*c^3*log(f)^3 + 3*c^2*f*log(f)^2 - 27*I*c*f^2*log(f) + 27*f^3)*sqrt(-c*log(f) + I*f)*erf(1/2*(2*f^2*x + I*b*f*log(f) + (2*c^2*x + b*c)*log(f)^2)*sqrt(-c*log(f) + I*f)/(c^2*log(f)^2 + f^2))*e^(1/4*(4*a*f^2*log(f) - (b^2*c - 4*a*c^2)*log(f)^3 - 4*I*d*f^2 + (-4*I*c^2*d - I*b^2*f)*log(f)^2)/(c^2*log(f)^2 + f^2)))/(c^4*log(f)^4 + 10*c^2*f^2*log(f)^2 + 9*f^4)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int f^{cx^2+bx+a} \sin(fx^2+d)^3 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(c*x^2+b*x+a)*sin(f*x^2+d)^3,x, algorithm="giac")

[Out] integrate(f^(c*x^2 + b*x + a)*sin(f*x^2 + d)^3, x)

maple [A] time = 1.17, size = 358, normalized size = 0.93

$$\frac{i\sqrt{\pi} f^a e^{-\frac{\ln(f)^2 b^2 - 12id \ln(f)c + 36df}{4(3if + c \ln(f))}} \operatorname{erf} \left(-\sqrt{-c \ln(f) - 3if} x + \frac{\ln(f)b}{2\sqrt{-c \ln(f) - 3if}} \right)}{16\sqrt{-c \ln(f) - 3if}} + \frac{i\sqrt{\pi} f^a e^{-\frac{\ln(f)^2 b^2 + 12id \ln(f)c + 36df}{4(-3if + c \ln(f))}} \operatorname{erf} \left(-x\sqrt{3if - c \ln(f)} \right)}{16\sqrt{3if - c \ln(f)}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(f^(c*x^2+b*x+a)*sin(f*x^2+d)^3,x)

[Out] -1/16*I*Pi^(1/2)*f^a*exp(-1/4*(ln(f)^2*b^2-12*I*d*ln(f)*c+36*d*f)/(3*I*f+c*ln(f)))/(-c*ln(f)-3*I*f)^(1/2)*erf(-(-c*ln(f)-3*I*f)^(1/2)*x+1/2*ln(f)*b/(-c*ln(f)-3*I*f)^(1/2))+1/16*I*Pi^(1/2)*f^a*exp(-1/4*(ln(f)^2*b^2+12*I*d*ln(f)*c+36*d*f)/(-3*I*f+c*ln(f)))/(3*I*f-c*ln(f))^(1/2)*erf(-x*(3*I*f-c*ln(f))^(1/2)+1/2*ln(f)*b/(3*I*f-c*ln(f))^(1/2))-3/16*I*Pi^(1/2)*f^a*exp(-1/4*(4*d*f+4*I*d*ln(f)*c+ln(f)^2*b^2)/(-I*f+c*ln(f)))/(I*f-c*ln(f))^(1/2)*erf(-x*(I*f-c*ln(f))^(1/2)+1/2*ln(f)*b/(I*f-c*ln(f))^(1/2))+3/16*I*Pi^(1/2)*f^a*exp(-1/4*(4*d*f-4*I*d*ln(f)*c+ln(f)^2*b^2)/(I*f+c*ln(f)))/(-I*f-c*ln(f))^(1/2)*erf(-(-I*f-c*ln(f))^(1/2)*x+1/2*ln(f)*b/(-I*f-c*ln(f))^(1/2))

maxima [B] time = 0.42, size = 2456, normalized size = 6.36

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate($f^{(c*x^2+b*x+a)} \sin(f*x^2+d)^3, x$, algorithm="maxima")

[Out] $\frac{1}{32} \sqrt{\pi} \sqrt{2c^2 \log(f)^2 + 18f^2} \left(\frac{((c^2 f^a e^{(1/4 b^2 c \log(f)^3 / (c^2 \log(f)^2 + f^2)}) \log(f)^2 + f^{(a+2)} e^{(1/4 b^2 c \log(f)^3 / (c^2 \log(f)^2 + f^2)})) \cos(3/4 (36 d f^2 + (4 c^2 d + b^2 f) \log(f)^2) / (c^2 \log(f)^2 + 9 f^2)) + (-I c^2 f^a e^{(1/4 b^2 c \log(f)^3 / (c^2 \log(f)^2 + f^2)}) \log(f)^2 - I f^{(a+2)} e^{(1/4 b^2 c \log(f)^3 / (c^2 \log(f)^2 + f^2)}) \sin(3/4 (36 d f^2 + (4 c^2 d + b^2 f) \log(f)^2) / (c^2 \log(f)^2 + 9 f^2)) \operatorname{erf}(1/2 (2 (c \log(f) - 3 I f) x + b \log(f)) / \sqrt{-c \log(f) + 3 I f}) + ((c^2 f^a e^{(1/4 b^2 c \log(f)^3 / (c^2 \log(f)^2 + f^2)}) \log(f)^2 + f^{(a+2)} e^{(1/4 b^2 c \log(f)^3 / (c^2 \log(f)^2 + f^2)})) \cos(3/4 (36 d f^2 + (4 c^2 d + b^2 f) \log(f)^2) / (c^2 \log(f)^2 + 9 f^2)) + (I c^2 f^a e^{(1/4 b^2 c \log(f)^3 / (c^2 \log(f)^2 + f^2)}) \log(f)^2 + I f^{(a+2)} e^{(1/4 b^2 c \log(f)^3 / (c^2 \log(f)^2 + f^2)}) \sin(3/4 (36 d f^2 + (4 c^2 d + b^2 f) \log(f)^2) / (c^2 \log(f)^2 + 9 f^2)) \operatorname{erf}(1/2 (2 (c \log(f) + 3 I f) x + b \log(f)) / \sqrt{-c \log(f) - 3 I f}) \right) \sqrt{c \log(f) + \sqrt{c^2 \log(f)^2 + 9 f^2}} - \sqrt{\pi} \sqrt{2c^2 \log(f)^2 + 2f^2} \left((3 (c^2 f^a e^{(1/4 b^2 c \log(f)^3 / (c^2 \log(f)^2 + 9 f^2)}) \log(f)^2 + 9 f^{(a+2)} e^{(1/4 b^2 c \log(f)^3 / (c^2 \log(f)^2 + 9 f^2)}) \cos(1/4 (4 d f^2 + (4 c^2 d + b^2 f) \log(f)^2) / (c^2 \log(f)^2 + f^2)) - (3 I c^2 f^a e^{(1/4 b^2 c \log(f)^3 / (c^2 \log(f)^2 + 9 f^2)}) \log(f)^2 + 27 I f^{(a+2)} e^{(1/4 b^2 c \log(f)^3 / (c^2 \log(f)^2 + 9 f^2)}) \sin(1/4 (4 d f^2 + (4 c^2 d + b^2 f) \log(f)^2) / (c^2 \log(f)^2 + f^2)) \operatorname{erf}(1/2 (2 (c \log(f) - I f) x + b \log(f)) / \sqrt{-c \log(f) + I f}) + (3 (c^2 f^a e^{(1/4 b^2 c \log(f)^3 / (c^2 \log(f)^2 + 9 f^2)}) \log(f)^2 + 9 f^{(a+2)} e^{(1/4 b^2 c \log(f)^3 / (c^2 \log(f)^2 + 9 f^2)}) \cos(1/4 (4 d f^2 + (4 c^2 d + b^2 f) \log(f)^2) / (c^2 \log(f)^2 + f^2)) - (-3 I c^2 f^a e^{(1/4 b^2 c \log(f)^3 / (c^2 \log(f)^2 + 9 f^2)}) \log(f)^2 - 27 I f^{(a+2)} e^{(1/4 b^2 c \log(f)^3 / (c^2 \log(f)^2 + 9 f^2)}) \sin(1/4 (4 d f^2 + (4 c^2 d + b^2 f) \log(f)^2) / (c^2 \log(f)^2 + f^2)) \operatorname{erf}(1/2 (2 (c \log(f) + I f) x + b \log(f)) / \sqrt{-c \log(f) - I f}) \right) \sqrt{c \log(f) + \sqrt{c^2 \log(f)^2 + f^2}} + \sqrt{\pi} \sqrt{2c^2 \log(f)^2 + 18f^2} \left((I c^2 f^a e^{(1/4 b^2 c \log(f)^3 / (c^2 \log(f)^2 + f^2)}) \log(f)^2 + I f^{(a+2)} e^{(1/4 b^2 c \log(f)^3 / (c^2 \log(f)^2 + f^2)}) \cos(3/4 (36 d f^2 + (4 c^2 d + b^2 f) \log(f)^2) / (c^2 \log(f)^2 + 9 f^2)) + (c^2 f^a e^{(1/4 b^2 c \log(f)^3 / (c^2 \log(f)^2 + f^2)}) \log(f)^2 + f^{(a+2)} e^{(1/4 b^2 c \log(f)^3 / (c^2 \log(f)^2 + f^2)}) \sin(3/4 (36 d f^2 + (4 c^2 d + b^2 f) \log(f)^2) / (c^2 \log(f)^2 + 9 f^2)) \operatorname{erf}(1/2 (2 (c \log(f) - 3 I f) x + b \log(f)) / \sqrt{-c \log(f) + 3 I f}) + ((-I c^2 f^a e^{(1/4 b^2 c \log(f)^3 / (c^2 \log(f)^2 + f^2)}) \log(f)^2 - I f^{(a+2)} e^{(1/4 b^2 c \log(f)^3 / (c^2 \log(f)^2 + f^2)}) \cos(3/4 (36 d f^2 + (4 c^2 d + b^2 f) \log(f)^2) / (c^2 \log(f)^2 + 9 f^2)) + (c^2 f^a e^{(1/4 b^2 c \log(f)^3 / (c^2 \log(f)^2 + f^2)}) \log(f)^2 + f^{(a+2)} e^{(1/4 b^2 c \log(f)^3 / (c^2 \log(f)^2 + f^2)}) \sin(3/4 (36 d f^2 + (4 c^2 d + b^2 f) \log(f)^2) / (c^2 \log(f)^2 + 9 f^2)) \operatorname{erf}(1/2 (2 (c \log(f) + 3 I f) x + b \log(f)) / \sqrt{-c \log(f) - 3 I f}) \right) \sqrt{-c \log(f) + \sqrt{c^2 \log(f)^2 + 9 f^2}} + \sqrt{\pi} \sqrt{2c^2 \log(f)^2 + 2f^2} \left((-3 I c^2 f^a e^{(1/4 b^2 c \log(f)^3 / (c^2 \log(f)^2 + 9 f^2)}) \log(f)^2 - 27 I f^{(a+2)} e^{(1/4 b^2 c \log(f)^3 / (c^2 \log(f)^2 + 9 f^2)}) \cos(1/4 (4 d f^2 + (4 c^2 d + b^2 f) \log(f)^2) / (c^2 \log(f)^2 + f^2)) - 3 (c^2 f^a e^{(1/4 b^2 c \log(f)^3 / (c^2 \log(f)^2 + 9 f^2)}) \log(f)^2 + 9 f^{(a+2)} e^{(1/4 b^2 c \log(f)^3 / (c^2 \log(f)^2 + 9 f^2)}) \sin(1/4 (4 d f^2 + (4 c^2 d + b^2 f) \log(f)^2) / (c^2 \log(f)^2 + f^2)) \operatorname{erf}(1/2 (2 (c \log(f) - I f) x + b \log(f)) / \sqrt{-c \log(f) + I f}) + ((3 I c^2 f^a e^{(1/4 b^2 c \log(f)^3 / (c^2 \log(f)^2 + 9 f^2)}) \log(f)^2 + 27 I f^{(a+2)} e^{(1/4 b^2 c \log(f)^3 / (c^2 \log(f)^2 + 9 f^2)}) \cos(1/4 (4 d f^2 + (4 c^2 d + b^2 f) \log(f)^2) / (c^2 \log(f)^2 + f^2)) - 3 (c^2 f^a e^{(1/4 b^2 c \log(f)^3 / (c^2 \log(f)^2 + 9 f^2)}) \log(f)^2 + 9 f^{(a+2)} e^{(1/4 b^2 c \log(f)^3 / (c^2 \log(f)^2 + 9 f^2)}) \sin(1/4 (4 d f^2 +$

```
(4*c^2*d + b^2*f)*log(f)^2)/(c^2*log(f)^2 + f^2)))*erf(1/2*(2*(c*log(f) + I
*f)*x + b*log(f))/sqrt(-c*log(f) - I*f)))*sqrt(-c*log(f) + sqrt(c^2*log(f)^
2 + f^2)))/(c^4*e^(1/4*b^2*c*log(f)^3/(c^2*log(f)^2 + 9*f^2) + 1/4*b^2*c*lo
g(f)^3/(c^2*log(f)^2 + f^2))*log(f)^4 + 10*c^2*f^2*e^(1/4*b^2*c*log(f)^3/(c
^2*log(f)^2 + 9*f^2) + 1/4*b^2*c*log(f)^3/(c^2*log(f)^2 + f^2))*log(f)^2 +
9*f^4*e^(1/4*b^2*c*log(f)^3/(c^2*log(f)^2 + 9*f^2) + 1/4*b^2*c*log(f)^3/(c^
2*log(f)^2 + f^2)))
```

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int f^{cx^2+bx+a} \sin(fx^2+d)^3 dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(f^(a + b*x + c*x^2)*sin(d + f*x^2)^3,x)
```

```
[Out] int(f^(a + b*x + c*x^2)*sin(d + f*x^2)^3, x)
```

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(f**(c*x**2+b*x+a)*sin(f*x**2+d)**3,x)
```

```
[Out] Timed out
```

3.100 $\int f^{a+bx+cx^2} \sin(d+ex+fx^2) dx$

Optimal. Leaf size=212

$$\frac{i\sqrt{\pi} f^a \exp\left(-\frac{(e+ib\log(f))^2}{-4c\log(f)+4if} - id\right) \operatorname{erf}\left(\frac{-b\log(f)+2x(-c\log(f)+if)+ie}{2\sqrt{-c\log(f)+if}}\right)}{4\sqrt{-c\log(f)+if}} - \frac{i\sqrt{\pi} f^a \exp\left(\frac{(e-ib\log(f))^2}{4c\log(f)+4if} + id\right) \operatorname{erfi}\left(\frac{b\log(f)+2x(-c\log(f)+if)+ie}{2\sqrt{c\log(f)+if}}\right)}{4\sqrt{c\log(f)+if}}$$

[Out] $\frac{1/4 * I * \exp(-I * d - (e + I * b * \ln(f))^2 / (4 * I * f - 4 * c * \ln(f))) * f^a * \operatorname{erf}(1/2 * (I * e - b * \ln(f) + 2 * x * (I * f - c * \ln(f))) / (I * f - c * \ln(f))) / (I * f - c * \ln(f))^{1/2} * \operatorname{Pi}^{1/2} / (I * f - c * \ln(f))^{1/2} - 1/4 * I * \exp(I * d + (e - I * b * \ln(f))^2 / (4 * I * f + 4 * c * \ln(f))) * f^a * \operatorname{erfi}(1/2 * (I * e + b * \ln(f) + 2 * x * (I * f + c * \ln(f))) / (I * f + c * \ln(f))) / (I * f + c * \ln(f))^{1/2} * \operatorname{Pi}^{1/2} / (I * f + c * \ln(f))^{1/2}}$

Rubi [A] time = 0.57, antiderivative size = 212, normalized size of antiderivative = 1.00, number of steps used = 8, number of rules used = 5, integrand size = 24, $\frac{\text{number of rules}}{\text{integrand size}} = 0.208$, Rules used = {4472, 2287, 2234, 2205, 2204}

$$\frac{i\sqrt{\pi} f^a \exp\left(-\frac{(e+ib\log(f))^2}{-4c\log(f)+4if} - id\right) \operatorname{Erf}\left(\frac{-b\log(f)+2x(-c\log(f)+if)+ie}{2\sqrt{-c\log(f)+if}}\right)}{4\sqrt{-c\log(f)+if}} - \frac{i\sqrt{\pi} f^a \exp\left(\frac{(e-ib\log(f))^2}{4c\log(f)+4if} + id\right) \operatorname{Erfi}\left(\frac{b\log(f)+2x(-c\log(f)+if)+ie}{2\sqrt{c\log(f)+if}}\right)}{4\sqrt{c\log(f)+if}}$$

Antiderivative was successfully verified.

[In] `Int[f^(a + b*x + c*x^2)*Sin[d + e*x + f*x^2],x]`

[Out] $((I/4) * E^{(-I) * d - (e + I * b * \operatorname{Log}[f])^2 / ((4 * I) * f - 4 * c * \operatorname{Log}[f])}) * f^a * \operatorname{Sqrt}[\operatorname{Pi}] * \operatorname{Erf}[(I * e - b * \operatorname{Log}[f] + 2 * x * (I * f - c * \operatorname{Log}[f])) / (2 * \operatorname{Sqrt}[I * f - c * \operatorname{Log}[f]])] / \operatorname{Sqrt}[I * f - c * \operatorname{Log}[f]] - ((I/4) * E^{(I * d + (e - I * b * \operatorname{Log}[f])^2 / ((4 * I) * f + 4 * c * \operatorname{Log}[f]))}) * f^a * \operatorname{Sqrt}[\operatorname{Pi}] * \operatorname{Erfi}[(I * e + b * \operatorname{Log}[f] + 2 * x * (I * f + c * \operatorname{Log}[f])) / (2 * \operatorname{Sqrt}[I * f + c * \operatorname{Log}[f]])] / \operatorname{Sqrt}[I * f + c * \operatorname{Log}[f]])$

Rule 2204

`Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_)^2), x_Symbol] := Simp[(F^a*Sqrt[Pi]*Erfi[(c + d*x)*Rt[b*Log[F], 2]]/(2*d*Rt[b*Log[F], 2]), x] /; FreeQ[{F, a, b, c, d}, x] && PosQ[b]`

Rule 2205

`Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_)^2), x_Symbol] := Simp[(F^a*Sqrt[Pi]*Erf[(c + d*x)*Rt[-(b*Log[F]), 2]]/(2*d*Rt[-(b*Log[F]), 2]), x] /; FreeQ[{F, a, b, c, d}, x] && NegQ[b]`

Rule 2234

`Int[(F_)^((a_.) + (b_.)*(x_) + (c_.)*(x_)^2), x_Symbol] := Dist[F^(a - b^2/(4*c)), Int[F^((b + 2*c*x)^2/(4*c)), x], x] /; FreeQ[{F, a, b, c}, x]`

Rule 2287

`Int[(u_.)*(F_)^(v_.)*(G_)^(w_.), x_Symbol] := With[{z = v*Log[F] + w*Log[G]}, Int[u*NormalizeIntegrand[E^z, x], x] /; BinomialQ[z, x] || (PolynomialQ[z, x] && LeQ[Exponent[z, x], 2])] /; FreeQ[{F, G}, x]`

Rule 4472

`Int[(F_)^(u_)*Sin[v_]^(n_.), x_Symbol] := Int[ExpandTrigToExp[F^u, Sin[v]^n, x], x] /; FreeQ[F, x] && (LinearQ[u, x] || PolyQ[u, x, 2]) && (LinearQ[v, x] || PolyQ[v, x, 2]) && IGtQ[n, 0]`

Rubi steps

$$\begin{aligned}
\int f^{a+bx+cx^2} \sin(d+ex+fx^2) dx &= \int \left(\frac{1}{2} i e^{-id-iex-ifx^2} f^{a+bx+cx^2} - \frac{1}{2} i e^{id+iex+ifx^2} f^{a+bx+cx^2} \right) dx \\
&= \frac{1}{2} i \int e^{-id-iex-ifx^2} f^{a+bx+cx^2} dx - \frac{1}{2} i \int e^{id+iex+ifx^2} f^{a+bx+cx^2} dx \\
&= \frac{1}{2} i \int \exp(-id + a \log(f) - x(ie - b \log(f)) - x^2(if - c \log(f))) dx - \frac{1}{2} i \int \exp(id + a \log(f) + x(ie + b \log(f)) + x^2(if + c \log(f))) dx \\
&= \frac{1}{2} \left(i \exp\left(-id - \frac{(e + ib \log(f))^2}{4if - 4c \log(f)}\right) f^a \right) \int \exp\left(\frac{(-ie + b \log(f) + 2x(-if + c \log(f)))}{4(-if + c \log(f))}\right) dx \\
&\quad - \frac{1}{2} \left(i \exp\left(id + \frac{(e - ib \log(f))^2}{4if - 4c \log(f)}\right) f^a \right) \int \exp\left(\frac{(ie + b \log(f) + 2x(if + c \log(f)))}{4(if + c \log(f))}\right) dx \\
&= \frac{i \exp\left(-id - \frac{(e + ib \log(f))^2}{4if - 4c \log(f)}\right) f^a \sqrt{\pi} \operatorname{erf}\left(\frac{ie - b \log(f) + 2x(if - c \log(f))}{2\sqrt{if - c \log(f)}}\right)}{4\sqrt{if - c \log(f)}} - \frac{i \exp\left(id + \frac{(e - ib \log(f))^2}{4if - 4c \log(f)}\right) f^a \sqrt{\pi} \operatorname{erf}\left(\frac{ie + b \log(f) + 2x(if + c \log(f))}{2\sqrt{if + c \log(f)}}\right)}{4\sqrt{if + c \log(f)}}
\end{aligned}$$

Mathematica [A] time = 2.20, size = 347, normalized size = 1.64

$$\sqrt[4]{-1} \sqrt{\pi} f^{\frac{f(af-be)+ac^2 \log^2(f)}{c^2 \log^2(f)+f^2}} \exp\left(-\frac{1}{4} i \left(\frac{b^2 \log^2(f)}{f+ic \log(f)} + \frac{e^2}{f-ic \log(f)}\right)\right) \left(\sqrt{f-ic \log(f)} (f+ic \log(f)) (\cos(d) + i \sin(d)) e^{\frac{1}{2}(d+ex+fx^2)} \right)$$

Warning: Unable to verify antiderivative.

[In] Integrate[f^(a + b*x + c*x^2)*Sin[d + e*x + f*x^2], x]

[Out]
$$\begin{aligned}
& -1/4 * ((-1)^{(1/4)} * f^{((f * (-b * e) + a * f) + a * c^2 * \text{Log}[f]^2) / (f^2 + c^2 * \text{Log}[f]^2)}) * \text{Sqrt}[\text{Pi}] * (E^{((I/2) * b^2 * f * \text{Log}[f]^2) / (f^2 + c^2 * \text{Log}[f]^2)} * f^{(b * e) / (2 * f + (2 * I) * c * \text{Log}[f])}) * \text{Erfi}[((-1)^{(1/4)} * (e + 2 * f * x - I * (b + 2 * c * x) * \text{Log}[f])) / (2 * \text{Sqrt}[f - I * c * \text{Log}[f]])] * \text{Sqrt}[f - I * c * \text{Log}[f]] * (f + I * c * \text{Log}[f]) * (\text{Cos}[d] + I * \text{Sin}[d]) + E^{((I/2) * e^2 * f) / (f^2 + c^2 * \text{Log}[f]^2)} * f^{(b * e) / (2 * f - (2 * I) * c * \text{Log}[f])}) * \text{Erfi}[((-1)^{(3/4)} * (e + 2 * f * x + I * (b + 2 * c * x) * \text{Log}[f])) / (2 * \text{Sqrt}[f + I * c * \text{Log}[f]])] * (f - I * c * \text{Log}[f]) * \text{Sqrt}[f + I * c * \text{Log}[f]] * (I * \text{Cos}[d] + \text{Sin}[d])) / (E^{((I/4) * (e^2 / (f - I * c * \text{Log}[f]) + (b^2 * \text{Log}[f]^2) / (f + I * c * \text{Log}[f]))} * (f^2 + c^2 * \text{Log}[f]^2))
\end{aligned}$$

fricas [B] time = 1.04, size = 375, normalized size = 1.77

$$\sqrt{\pi} (ic \log(f) + f) \sqrt{-c \log(f) - if} \operatorname{erf}\left(\frac{(2f^2x + (2c^2x + bc) \log(f)^2 + ef + (ice - ibf) \log(f)) \sqrt{-c \log(f) - if}}{2(c^2 \log(f)^2 + f^2)}\right) e^{\left(-\frac{(b^2c - 4ac^2) \log(f)^3 + i e^2 f - \dots}{\dots}\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(c*x^2+b*x+a)*sin(f*x^2+e*x+d), x, algorithm="fricas")

[Out]
$$\begin{aligned}
& 1/4 * (\text{sqrt}(\text{pi}) * (I * c * \log(f) + f) * \text{sqrt}(-c * \log(f) - I * f) * \text{erf}(1/2 * (2 * f^2 * x + (2 * c^2 * x + b * c) * \log(f)^2 + e * f + (I * c * e - I * b * f) * \log(f)) * \text{sqrt}(-c * \log(f) - I * f) / (c^2 * \log(f)^2 + f^2)) * e^{(-1/4 * ((b^2 * c - 4 * a * c^2) * \log(f)^3 + I * e^2 * f - 4 * I * d * f^2 - (4 * I * c^2 * d - 2 * I * b * c * e + I * b^2 * f) * \log(f)^2 - (c * e^2 - 2 * b * e * f + 4 * a * f^2) * \log(f)) / (c^2 * \log(f)^2 + f^2)} + \text{sqrt}(\text{pi}) * (-I * c * \log(f) + f) * \text{sqrt}(-c * \log(f) + I * f) * \text{erf}(1/2 * (2 * f^2 * x + (2 * c^2 * x + b * c) * \log(f)^2 + e * f + (-I * c * e + I * b * f) * \log(f)) * \text{sqrt}(-c * \log(f) + I * f) / (c^2 * \log(f)^2 + f^2)) * e^{(-1/4 * ((b^2 * c - 4 * a * c^2) * \log(f)^3 - I * e^2 * f + 4 * I * d * f^2 - (-4 * I * c^2 * d + 2 * I * b * c * e - I * b^2 * f) * \log(f)^2 - (c * e^2 - 2 * b * e * f + 4 * a * f^2) * \log(f)) / (c^2 * \log(f)^2 + f^2))} / (c^2 * \log(f)^2 + f^2)
\end{aligned}$$

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int f^{cx^2+bx+a} \sin(fx^2 + ex + d) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(c*x^2+b*x+a)*sin(f*x^2+e*x+d),x, algorithm="giac")

[Out] integrate(f^(c*x^2 + b*x + a)*sin(f*x^2 + e*x + d), x)

maple [A] time = 0.62, size = 216, normalized size = 1.02

$$\frac{i\sqrt{\pi} f^a e^{\frac{4df - e^2 + 2i \ln(f)be - 4id \ln(f)c + \ln(f)^2 b^2}{4(if + c \ln(f))}} \operatorname{erf}\left(-\sqrt{-if - c \ln(f)} x + \frac{ie + b \ln(f)}{2\sqrt{-if - c \ln(f)}}\right)}{4\sqrt{-if - c \ln(f)}} - \frac{i\sqrt{\pi} f^a e^{\frac{4df - e^2 - 2i \ln(f)be + 4id \ln(f)c + \ln(f)^2 b^2}{4(-if + c \ln(f))}}}{4\sqrt{if}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(f^(c*x^2+b*x+a)*sin(f*x^2+e*x+d),x)

[Out] $\frac{1}{4} I \pi^{1/2} f^a \exp(-1/4 * (4 * d * f - e^2 + 2 * I * \ln(f) * b * e - 4 * I * d * \ln(f) * c + \ln(f)^2 * b^2) / (I * f + c * \ln(f))) / (-I * f - c * \ln(f))^{1/2} * \operatorname{erf}(-(-I * f - c * \ln(f))^{1/2} * x + 1/2 * (I * e + b * \ln(f)) / (-I * f - c * \ln(f))) - 1/4 * I \pi^{1/2} f^a \exp(-1/4 * (4 * d * f - e^2 - 2 * I * \ln(f) * b * e + 4 * I * d * \ln(f) * c + \ln(f)^2 * b^2) / (-I * f + c * \ln(f))) / (I * f - c * \ln(f))^{1/2} * \operatorname{erf}(-x * (I * f - c * \ln(f))^{1/2} + 1/2 * (-I * e + b * \ln(f)) / (I * f - c * \ln(f)))$

maxima [B] time = 0.39, size = 1007, normalized size = 4.75

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(c*x^2+b*x+a)*sin(f*x^2+e*x+d),x, algorithm="maxima")

[Out] $\frac{1}{8} * (\sqrt{\pi}) * \sqrt{(2 * c^2 * \log(f)^2 + 2 * f^2)} * ((f^{1/4 * c * e^2 / (c^2 * \log(f)^2 + f^2)}) * f^a * \cos(-1/4 * (e^2 * f - 4 * d * f^2 - (4 * c^2 * d - 2 * b * c * e + b^2 * f) * \log(f)^2) / (c^2 * \log(f)^2 + f^2)) - I * f^{1/4 * c * e^2 / (c^2 * \log(f)^2 + f^2)}) * f^a * \sin(-1/4 * (e^2 * f - 4 * d * f^2 - (4 * c^2 * d - 2 * b * c * e + b^2 * f) * \log(f)^2) / (c^2 * \log(f)^2 + f^2))) * \operatorname{erf}(1/2 * (2 * (c * \log(f) - I * f) * x + b * \log(f) - I * e) * \sqrt{-c * \log(f) + I * f} / (c * \log(f) - I * f)) + (f^{1/4 * c * e^2 / (c^2 * \log(f)^2 + f^2)}) * f^a * \cos(-1/4 * (e^2 * f - 4 * d * f^2 - (4 * c^2 * d - 2 * b * c * e + b^2 * f) * \log(f)^2) / (c^2 * \log(f)^2 + f^2)) + I * f^{1/4 * c * e^2 / (c^2 * \log(f)^2 + f^2)}) * f^a * \sin(-1/4 * (e^2 * f - 4 * d * f^2 - (4 * c^2 * d - 2 * b * c * e + b^2 * f) * \log(f)^2) / (c^2 * \log(f)^2 + f^2))) * \operatorname{erf}(1/2 * (2 * (c * \log(f) + I * f) * x + b * \log(f) + I * e) * \sqrt{-c * \log(f) - I * f} / (c * \log(f) + I * f))) * \sqrt{(c * \log(f) + \sqrt{c^2 * \log(f)^2 + f^2}) + \sqrt{\pi}) * \sqrt{(2 * c^2 * \log(f)^2 + 2 * f^2)} * ((I * f^{1/4 * c * e^2 / (c^2 * \log(f)^2 + f^2)}) * f^a * \cos(-1/4 * (e^2 * f - 4 * d * f^2 - (4 * c^2 * d - 2 * b * c * e + b^2 * f) * \log(f)^2) / (c^2 * \log(f)^2 + f^2)) + f^{1/4 * c * e^2 / (c^2 * \log(f)^2 + f^2)}) * f^a * \sin(-1/4 * (e^2 * f - 4 * d * f^2 - (4 * c^2 * d - 2 * b * c * e + b^2 * f) * \log(f)^2) / (c^2 * \log(f)^2 + f^2))) * \operatorname{erf}(1/2 * (2 * (c * \log(f) - I * f) * x + b * \log(f) - I * e) * \sqrt{-c * \log(f) + I * f} / (c * \log(f) - I * f)) + (-I * f^{1/4 * c * e^2 / (c^2 * \log(f)^2 + f^2)}) * f^a * \cos(-1/4 * (e^2 * f - 4 * d * f^2 - (4 * c^2 * d - 2 * b * c * e + b^2 * f) * \log(f)^2) / (c^2 * \log(f)^2 + f^2)) + f^{1/4 * c * e^2 / (c^2 * \log(f)^2 + f^2)}) * f^a * \sin(-1/4 * (e^2 * f - 4 * d * f^2 - (4 * c^2 * d - 2 * b * c * e + b^2 * f) * \log(f)^2) / (c^2 * \log(f)^2 + f^2))) * \operatorname{erf}(1/2 * (2 * (c * \log(f) + I * f) * x + b * \log(f) + I * e) * \sqrt{-c * \log(f) - I * f} / (c * \log(f) + I * f))) * \sqrt{(-c * \log(f) + \sqrt{c^2 * \log(f)^2 + f^2})} / (c^2 * e^{1/4 * b^2 * c * \log(f)^3 / (c^2 * \log(f)^2 + f^2)} + 1/2 * b * e * f * \log(f) / (c^2 * \log(f)^2 + f^2)) * \log(f)^2 + f^2 * e^{1/4 * b^2 * c * \log(f)^3 / (c^2 * \log(f)^2 + f^2)} + 1/2 * b * e * f * \log(f) / (c^2 * \log(f)^2 + f^2)))$

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int f^{cx^2+bx+a} \sin(fx^2 + ex + d) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(f^(a + b*x + c*x^2)*sin(d + e*x + f*x^2), x)`

[Out] `int(f^(a + b*x + c*x^2)*sin(d + e*x + f*x^2), x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int f^{a+bx+cx^2} \sin(d+ex+fx^2) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(f**(c*x**2+b*x+a)*sin(f*x**2+e*x+d), x)`

[Out] `Integral(f**(a + b*x + c*x**2)*sin(d + e*x + f*x**2), x)`

3.101 $\int f^{a+bx+cx^2} \sin^2(d+ex+fx^2) dx$

Optimal. Leaf size=268

$$\frac{\sqrt{\pi} f^{a-\frac{b^2}{4c}} \operatorname{erfi}\left(\frac{\sqrt{\log(f)}(b+2cx)}{2\sqrt{c}}\right)}{4\sqrt{c}\sqrt{\log(f)}} - \frac{\sqrt{\pi} f^a \exp\left(-\frac{(2e+ib\log(f))^2}{-4c\log(f)+8if} - 2id\right) \operatorname{erf}\left(\frac{-b\log(f)+2x(-c\log(f)+2if)+2ie}{2\sqrt{-c\log(f)+2if}}\right)}{8\sqrt{-c\log(f)+2if}} - \frac{\sqrt{\pi} f^a \exp\left(\frac{-b\log(f)+2x(-c\log(f)+2if)+2ie}{2\sqrt{-c\log(f)+2if}}\right)}{8\sqrt{-c\log(f)+2if}}$$

```
[Out] 1/4*f^(a-1/4*b^2/c)*erfi(1/2*(2*c*x+b)*ln(f)^(1/2)/c^(1/2))*Pi^(1/2)/c^(1/2)/ln(f)^(1/2)-1/8*exp(-2*I*d-(2*e+I*b*ln(f))^2/(8*I*f-4*c*ln(f)))*f^a*erf(1/2*(2*I*e-b*ln(f)+2*x*(2*I*f-c*ln(f)))/(2*I*f-c*ln(f))^(1/2))*Pi^(1/2)/(2*I*f-c*ln(f))^(1/2)-1/8*exp(2*I*d+(2*e-I*b*ln(f))^2/(8*I*f+4*c*ln(f)))*f^a*erfi(1/2*(2*I*e+b*ln(f)+2*x*(2*I*f+c*ln(f)))/(2*I*f+c*ln(f))^(1/2))*Pi^(1/2)/(2*I*f+c*ln(f))^(1/2)
```

Rubi [A] time = 0.65, antiderivative size = 268, normalized size of antiderivative = 1.00, number of steps used = 10, number of rules used = 5, integrand size = 26, $\frac{\text{number of rules}}{\text{integrand size}} = 0.192$, Rules used = {4472, 2234, 2204, 2287, 2205}

$$\frac{\sqrt{\pi} f^{a-\frac{b^2}{4c}} \operatorname{Erfi}\left(\frac{\sqrt{\log(f)}(b+2cx)}{2\sqrt{c}}\right)}{4\sqrt{c}\sqrt{\log(f)}} - \frac{\sqrt{\pi} f^a \exp\left(-\frac{(2e+ib\log(f))^2}{-4c\log(f)+8if} - 2id\right) \operatorname{Erf}\left(\frac{-b\log(f)+2x(-c\log(f)+2if)+2ie}{2\sqrt{-c\log(f)+2if}}\right)}{8\sqrt{-c\log(f)+2if}} - \frac{\sqrt{\pi} f^a \exp\left(\frac{-b\log(f)+2x(-c\log(f)+2if)+2ie}{2\sqrt{-c\log(f)+2if}}\right)}{8\sqrt{-c\log(f)+2if}}$$

Antiderivative was successfully verified.

```
[In] Int[f^(a + b*x + c*x^2)*Sin[d + e*x + f*x^2]^2,x]
```

```
[Out] (f^(a - b^2/(4*c))*Sqrt[Pi]*Erfi[((b + 2*c*x)*Sqrt[Log[f]])/(2*Sqrt[c])])/(4*Sqrt[c]*Sqrt[Log[f]]) - (E^((-2*I)*d - (2*e + I*b*Log[f])^2/((8*I)*f - 4*c*Log[f]))*f^a*Sqrt[Pi]*Erf[((2*I)*e - b*Log[f] + 2*x*((2*I)*f - c*Log[f]))/(2*Sqrt[(2*I)*f - c*Log[f]])])/(8*Sqrt[(2*I)*f - c*Log[f]]) - (E^((2*I)*d + (2*e - I*b*Log[f])^2/((8*I)*f + 4*c*Log[f]))*f^a*Sqrt[Pi]*Erfi[((2*I)*e + b*Log[f] + 2*x*((2*I)*f + c*Log[f]))/(2*Sqrt[(2*I)*f + c*Log[f]])])/(8*Sqrt[(2*I)*f + c*Log[f]])
```

Rule 2204

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_)^2), x_Symbol] := Simp[(F^a*Sqrt[Pi]*Erfi[(c + d*x)*Rt[b*Log[F], 2]])/(2*d*Rt[b*Log[F], 2]), x] /; FreeQ[{F, a, b, c, d}, x] && PosQ[b]
```

Rule 2205

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_)^2), x_Symbol] := Simp[(F^a*Sqrt[Pi]*Erf[(c + d*x)*Rt[-(b*Log[F]), 2]])/(2*d*Rt[-(b*Log[F]), 2]), x] /; FreeQ[{F, a, b, c, d}, x] && NegQ[b]
```

Rule 2234

```
Int[(F_)^((a_.) + (b_.)*(x_) + (c_.)*(x_)^2), x_Symbol] := Dist[F^(a - b^2/(4*c)), Int[F^((b + 2*c*x)^2/(4*c)), x], x] /; FreeQ[{F, a, b, c}, x]
```

Rule 2287

```
Int[(u_.)*(F_)^(v_.)*(G_)^(w_.), x_Symbol] := With[{z = v*Log[F] + w*Log[G]}, Int[u*NormalizeIntegrand[E^z, x], x] /; BinomialQ[z, x] || (PolynomialQ[z, x] && LeQ[Exponent[z, x], 2])] /; FreeQ[{F, G}, x]
```

Rule 4472

Int[(F_)^(u_)*Sin[v_]^(n_), x_Symbol] := Int[ExpandTrigToExp[F^u, Sin[v]^n, x], x] /; FreeQ[F, x] && (LinearQ[u, x] || PolyQ[u, x, 2]) && (LinearQ[v, x] || PolyQ[v, x, 2]) && IGtQ[n, 0]

Rubi steps

$$\begin{aligned} \int f^{a+bx+cx^2} \sin^2(d+ex+fx^2) dx &= \int \left(\frac{1}{2} f^{a+bx+cx^2} - \frac{1}{4} e^{-2id-2iex-2ifx^2} f^{a+bx+cx^2} - \frac{1}{4} e^{2id+2iex+2ifx^2} f^{a+bx+cx^2} \right) dx \\ &= -\left(\frac{1}{4} \int e^{-2id-2iex-2ifx^2} f^{a+bx+cx^2} dx \right) - \frac{1}{4} \int e^{2id+2iex+2ifx^2} f^{a+bx+cx^2} dx + \frac{1}{2} \int f^{a+bx+cx^2} dx \\ &= -\left(\frac{1}{4} \int \exp(-2id + a \log(f) - x(2ie - b \log(f)) - x^2(2if - c \log(f))) dx \right) \\ &= \frac{f^{a-\frac{b^2}{4c}} \sqrt{\pi} \operatorname{erfi}\left(\frac{(b+2cx)\sqrt{\log(f)}}{2\sqrt{c}}\right)}{4\sqrt{c}\sqrt{\log(f)}} - \frac{1}{4} \left(\exp\left(-2id - \frac{(2e+ib\log(f))^2}{8if-4c\log(f)}\right) f^a \int e^{\dots} dx \right) \\ &= \frac{f^{a-\frac{b^2}{4c}} \sqrt{\pi} \operatorname{erfi}\left(\frac{(b+2cx)\sqrt{\log(f)}}{2\sqrt{c}}\right)}{4\sqrt{c}\sqrt{\log(f)}} - \frac{\exp\left(-2id - \frac{(2e+ib\log(f))^2}{8if-4c\log(f)}\right) f^a \sqrt{\pi} \operatorname{erf}\left(\frac{2ie-b\log(f)}{2\sqrt{c}}\right)}{8\sqrt{2if-c\log(f)}} \end{aligned}$$

Mathematica [B] time = 6.73, size = 1120, normalized size = 4.18

$$f^a \sqrt{\pi} \left(8\sqrt{c} \operatorname{erfi}\left(\frac{(b+2cx)\sqrt{\log(f)}}{2\sqrt{c}}\right) \sqrt{\log(f)} f^{a-\frac{b^2}{4c}} + 2c^{5/2} \operatorname{erfi}\left(\frac{(b+2cx)\sqrt{\log(f)}}{2\sqrt{c}}\right) \log^{\frac{5}{2}}(f) f^{-\frac{b^2}{4c}} + 2(-1)^{3/4} c e^{\frac{i(-4e^2+4ib\log(f)e+b^2)}{4(2f-ic\log(f))}} \right)$$

Warning: Unable to verify antiderivative.

[In] Integrate[f^(a + b*x + c*x^2)*Sin[d + e*x + f*x^2]^2,x]

[Out] (f^a*Sqrt[Pi]*(8*Sqrt[c]*f^(2 - b^2/(4*c))*Erfi[((b + 2*c*x)*Sqrt[Log[f]])/(2*Sqrt[c]])*Sqrt[Log[f]] + (2*c^(5/2)*Erfi[((b + 2*c*x)*Sqrt[Log[f]])/(2*Sqrt[c]])*Log[f]^(5/2))/f^(b^2/(4*c)) + 2*(-1)^(1/4)*c*E^(((I/4)*(-4*e^2 + (4*I)*b*e*Log[f] + b^2*Log[f]^2))/(2*f - I*c*Log[f]))*f*Cos[2*d]*Erf[(-1)^(3/4)*(2*e + 4*f*x - I*b*Log[f] - (2*I)*c*x*Log[f])]/(2*Sqrt[2*f - I*c*Log[f]])]*Log[f]*Sqrt[2*f - I*c*Log[f]] + (-1)^(3/4)*c^2*E^(((I/4)*(-4*e^2 + (4*I)*b*e*Log[f] + b^2*Log[f]^2))/(2*f - I*c*Log[f]))*Cos[2*d]*Erf[(-1)^(3/4)*(2*e + 4*f*x - I*b*Log[f] - (2*I)*c*x*Log[f])]/(2*Sqrt[2*f - I*c*Log[f]])]*Log[f]^2*Sqrt[2*f - I*c*Log[f]] + (2*(-1)^(3/4)*c*f*Cos[2*d]*Erf[(-1)^(1/4)*(2*e + 4*f*x + I*b*Log[f] + (2*I)*c*x*Log[f])]/(2*Sqrt[2*f + I*c*Log[f]])]*Log[f]*Sqrt[2*f + I*c*Log[f]])/E^(((I/4)*(-4*e^2 - (4*I)*b*e*Log[f] + b^2*Log[f]^2))/(2*f + I*c*Log[f])) + ((-1)^(1/4)*c^2*Cos[2*d]*Erf[(-1)^(1/4)*(2*e + 4*f*x + I*b*Log[f] + (2*I)*c*x*Log[f])]/(2*Sqrt[2*f + I*c*Log[f]])]*Log[f]^2*Sqrt[2*f + I*c*Log[f]])/E^(((I/4)*(-4*e^2 - (4*I)*b*e*Log[f] + b^2*Log[f]^2))/(2*f + I*c*Log[f])) + 2*(-1)^(3/4)*c*E^(((I/4)*(-4*e^2 + (4*I)*b*e*Log[f] + b^2*Log[f]^2))/(2*f - I*c*Log[f]))*f*Erf[(-1)^(3/4)*(2*e + 4*f*x - I*b*Log[f] - (2*I)*c*x*Log[f])]/(2*Sqrt[2*f - I*c*Log[f]])]*Log[f]*Sqrt[2*f - I*c*Log[f]]*Sin[2*d] - (-1)^(1/4)*c^2*E^(((I/4)*(-4*e^2 + (4*I)*b*e*Log[f] + b^2*Log[f]^2))/(2*f - I*c*Log[f]))*Erf[(-1)^(3/4)*(2*e + 4*f*x - I*b*Log[f] - (2*I)*c*x*Log[f])]/(2*Sqrt[2*f - I*c*Log[f]])]*Log[f]^2*Sqrt[2*f - I*c*Log[f]]*Sin[2*d] + (2*(-1)^(1/4)*c*f*Erf[(-1)^(1/4)*(2*e + 4*f*x + I*b*Log[f] + (2*I)*c*x*Log[f])]/(2*Sqrt[2*f + I*c*Log[f]])]*Log[f]*Sqrt[2*f + I*c*Log[f]]*Sin[2*d])/E^(((I/4)*(-4*e^2 - (4*I)*b*e*Log[f] + b^2*Log[f]^2))/(2*f + I*c*Log[f])) - ((-1)^(3/4)*c^2*Erf[(-1)^(1/4)*(2*e + 4*f*x + I*b*Log[f] + (2*I)*c*x*Log[f])]/(2*Sqrt[2*f + I*c*Log[f]])]*Log[f]^2*Sqr

$t[2*f + I*c*\text{Log}[f]]*\text{Sin}[2*d])/E^{(((I/4)*(-4*e^2 - (4*I)*b*e*\text{Log}[f] + b^2*\text{Log}[f]^2))/(2*f + I*c*\text{Log}[f]))})/(8*c*\text{Log}[f]*(2*f - I*c*\text{Log}[f])*(2*f + I*c*\text{Log}[f]))}$

fricas [B] time = 1.64, size = 468, normalized size = 1.75

$$\sqrt{\pi} (c^2 \log(f)^2 - 2icf \log(f)) \sqrt{-c \log(f) - 2if} \operatorname{erf} \left(\frac{(8f^2x + (2c^2x + bc) \log(f)^2 + 4ef + (2ice - 2ibf) \log(f)) \sqrt{-c \log(f) - 2if}}{2(c^2 \log(f)^2 + 4f^2)} \right) e$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(c*x^2+b*x+a)*sin(f*x^2+e*x+d)^2,x, algorithm="fricas")

[Out] $\frac{1}{8} * (\sqrt{\pi} * (c^2 * \log(f)^2 - 2 * I * c * f * \log(f)) * \sqrt{-c * \log(f) - 2 * I * f} * \operatorname{erf}(\frac{1}{2} * (8 * f^2 * x + (2 * c^2 * x + b * c) * \log(f)^2 + 4 * e * f + (2 * I * c * e - 2 * I * b * f) * \log(f)) * \sqrt{-c * \log(f) - 2 * I * f} / (c^2 * \log(f)^2 + 4 * f^2)) * e^{-1/4 * ((b^2 * c - 4 * a * c^2) * \log(f)^3 + 8 * I * e^2 * f - 32 * I * d * f^2 - (8 * I * c^2 * d - 4 * I * b * c * e + 2 * I * b^2 * f) * \log(f)^2 - 4 * (c * e^2 - 2 * b * e * f + 4 * a * f^2) * \log(f)) / (c^2 * \log(f)^2 + 4 * f^2)) + \sqrt{\pi} * (c^2 * \log(f)^2 + 2 * I * c * f * \log(f)) * \sqrt{-c * \log(f) + 2 * I * f} * \operatorname{erf}(\frac{1}{2} * (8 * f^2 * x + (2 * c^2 * x + b * c) * \log(f)^2 + 4 * e * f + (-2 * I * c * e + 2 * I * b * f) * \log(f)) * \sqrt{-c * \log(f) + 2 * I * f} / (c^2 * \log(f)^2 + 4 * f^2)) * e^{-1/4 * ((b^2 * c - 4 * a * c^2) * \log(f)^3 - 8 * I * e^2 * f + 32 * I * d * f^2 - (-8 * I * c^2 * d + 4 * I * b * c * e - 2 * I * b^2 * f) * \log(f)^2 - 4 * (c * e^2 - 2 * b * e * f + 4 * a * f^2) * \log(f)) / (c^2 * \log(f)^2 + 4 * f^2)) - 2 * \sqrt{\pi} * (c^2 * \log(f)^2 + 4 * f^2) * \sqrt{-c * \log(f)} * \operatorname{erf}(\frac{1}{2} * (2 * c * x + b) * \sqrt{-c * \log(f)}) / c) / f^{1/4 * (b^2 - 4 * a * c) / c} / (c^3 * \log(f)^3 + 4 * c * f^2 * \log(f))$

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int f^{cx^2+bx+a} \sin(fx^2+ex+d)^2 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(c*x^2+b*x+a)*sin(f*x^2+e*x+d)^2,x, algorithm="giac")

[Out] integrate(f^(c*x^2 + b*x + a)*sin(f*x^2 + e*x + d)^2, x)

maple [A] time = 0.70, size = 263, normalized size = 0.98

$$\frac{\sqrt{\pi} f^a e^{-\frac{\ln(f)^2 b^2 - 4i \ln(f) b e + 8id \ln(f) c + 16df - 4e^2}{4(-2if + c \ln(f))}} \operatorname{erf} \left(-x \sqrt{2if - c \ln(f)} + \frac{b \ln(f) - 2ie}{2\sqrt{2if - c \ln(f)}} \right) + \sqrt{\pi} f^a e^{-\frac{\ln(f)^2 b^2 + 4i \ln(f) b e - 8id \ln(f) c + 16df}{4(2if + c \ln(f))}}}{8\sqrt{2if - c \ln(f)}} + \frac{\sqrt{\pi} f^a e^{-\frac{\ln(f)^2 b^2 + 4i \ln(f) b e - 8id \ln(f) c + 16df}{4(2if + c \ln(f))}}}{8\sqrt{2if + c \ln(f)}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(f^(c*x^2+b*x+a)*sin(f*x^2+e*x+d)^2,x)

[Out] $\frac{1}{8} * \pi^{1/2} * f^a * \exp(-1/4 * (\ln(f)^2 * b^2 - 4 * I * \ln(f) * b * e + 8 * I * d * \ln(f) * c + 16 * d * f - 4 * e^2) / (-2 * I * f + c * \ln(f))) / (2 * I * f - c * \ln(f))^{1/2} * \operatorname{erf}(-x * (2 * I * f - c * \ln(f))^{1/2} + 1/2 * (b * \ln(f) - 2 * I * e) / (2 * I * f - c * \ln(f)))^{1/2} + 1/8 * \pi^{1/2} * f^a * \exp(-1/4 * (\ln(f)^2 * b^2 + 4 * I * \ln(f) * b * e - 8 * I * d * \ln(f) * c + 16 * d * f - 4 * e^2) / (2 * I * f + c * \ln(f))) / (-2 * I * f - c * \ln(f))^{1/2} * \operatorname{erf}(-(-2 * I * f - c * \ln(f))^{1/2} * x + 1/2 * (2 * I * e + b * \ln(f)) / (-2 * I * f - c * \ln(f)))^{1/2} - 1/4 * \pi^{1/2} * f^a * f^{-1/4 * b^2 / c} / (-c * \ln(f))^{1/2} * \operatorname{erf}(-(-c * \ln(f))^{1/2} * x + 1/2 / (-c * \ln(f))^{1/2} * b * \ln(f))$

maxima [C] time = 0.42, size = 1487, normalized size = 5.55

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(c*x^2+b*x+a)*sin(f*x^2+e*x+d)^2,x, algorithm="maxima")

[Out] 1/16*(sqrt(pi)*sqrt(2*c^2*log(f)^2 + 8*f^2)*((I*f^a*cos(-1/2*(4*e^2*f - 16*d*f^2 - (4*c^2*d - 2*b*c*e + b^2*f)*log(f)^2)/(c^2*log(f)^2 + 4*f^2))*e^(c*e^2*log(f)/(c^2*log(f)^2 + 4*f^2) + 1/4*b^2*log(f)/c) + f^a*e^(c*e^2*log(f)/(c^2*log(f)^2 + 4*f^2) + 1/4*b^2*log(f)/c)*sin(-1/2*(4*e^2*f - 16*d*f^2 - (4*c^2*d - 2*b*c*e + b^2*f)*log(f)^2)/(c^2*log(f)^2 + 4*f^2)))*erf(1/2*(2*(c*log(f) - 2*I*f)*x + b*log(f) - 2*I*e)*sqrt(-c*log(f) + 2*I*f)/(c*log(f) - 2*I*f)) + (-I*f^a*cos(-1/2*(4*e^2*f - 16*d*f^2 - (4*c^2*d - 2*b*c*e + b^2*f)*log(f)^2)/(c^2*log(f)^2 + 4*f^2))*e^(c*e^2*log(f)/(c^2*log(f)^2 + 4*f^2) + 1/4*b^2*log(f)/c) + f^a*e^(c*e^2*log(f)/(c^2*log(f)^2 + 4*f^2) + 1/4*b^2*log(f)/c)*sin(-1/2*(4*e^2*f - 16*d*f^2 - (4*c^2*d - 2*b*c*e + b^2*f)*log(f)^2)/(c^2*log(f)^2 + 4*f^2)))*erf(1/2*(2*(c*log(f) + 2*I*f)*x + b*log(f) + 2*I*e)*sqrt(-c*log(f) - 2*I*f)/(c*log(f) + 2*I*f)))*sqrt(c*log(f) + sqrt(c^2*log(f)^2 + 4*f^2))*sqrt(-c*log(f)) - sqrt(pi)*sqrt(2*c^2*log(f)^2 + 8*f^2)*((f^a*cos(-1/2*(4*e^2*f - 16*d*f^2 - (4*c^2*d - 2*b*c*e + b^2*f)*log(f)^2)/(c^2*log(f)^2 + 4*f^2))*e^(c*e^2*log(f)/(c^2*log(f)^2 + 4*f^2) + 1/4*b^2*log(f)/c) - I*f^a*e^(c*e^2*log(f)/(c^2*log(f)^2 + 4*f^2) + 1/4*b^2*log(f)/c)*sin(-1/2*(4*e^2*f - 16*d*f^2 - (4*c^2*d - 2*b*c*e + b^2*f)*log(f)^2)/(c^2*log(f)^2 + 4*f^2)))*erf(1/2*(2*(c*log(f) - 2*I*f)*x + b*log(f) - 2*I*e)*sqrt(-c*log(f) + 2*I*f)/(c*log(f) - 2*I*f)) + (f^a*cos(-1/2*(4*e^2*f - 16*d*f^2 - (4*c^2*d - 2*b*c*e + b^2*f)*log(f)^2)/(c^2*log(f)^2 + 4*f^2))*e^(c*e^2*log(f)/(c^2*log(f)^2 + 4*f^2) + 1/4*b^2*log(f)/c) + I*f^a*e^(c*e^2*log(f)/(c^2*log(f)^2 + 4*f^2) + 1/4*b^2*log(f)/c)*sin(-1/2*(4*e^2*f - 16*d*f^2 - (4*c^2*d - 2*b*c*e + b^2*f)*log(f)^2)/(c^2*log(f)^2 + 4*f^2)))*erf(1/2*(2*(c*log(f) + 2*I*f)*x + b*log(f) + 2*I*e)*sqrt(-c*log(f) - 2*I*f)/(c*log(f) + 2*I*f)))*sqrt(-c*log(f) + sqrt(c^2*log(f)^2 + 4*f^2))*sqrt(-c*log(f)) + 2*sqrt(pi)*((c^2*f^a*e^(1/4*b^2*c*log(f)^3/(c^2*log(f)^2 + 4*f^2) + 2*b*e*f*log(f)/(c^2*log(f)^2 + 4*f^2))*log(f)^2 + 4*f^(a + 2)*e^(1/4*b^2*c*log(f)^3/(c^2*log(f)^2 + 4*f^2) + 2*b*e*f*log(f)/(c^2*log(f)^2 + 4*f^2)))*erf(-1/2*b*conjugate(1/sqrt(-c*log(f)))*log(f) + x*conjugate(sqrt(-c*log(f)))) - (c^2*f^a*e^(1/4*b^2*c*log(f)^3/(c^2*log(f)^2 + 4*f^2) + 2*b*e*f*log(f)/(c^2*log(f)^2 + 4*f^2))*log(f)^2 + 4*f^(a + 2)*e^(1/4*b^2*c*log(f)^3/(c^2*log(f)^2 + 4*f^2) + 2*b*e*f*log(f)/(c^2*log(f)^2 + 4*f^2)))*erf(1/2*(2*c*x*log(f) + b*log(f))/sqrt(-c*log(f))))/((c^2*e^(1/4*b^2*c*log(f)^3/(c^2*log(f)^2 + 4*f^2) + 2*b*e*f*log(f)/(c^2*log(f)^2 + 4*f^2) + 1/4*b^2*log(f)/c)*log(f)^2 + 4*f^2*e^(1/4*b^2*c*log(f)^3/(c^2*log(f)^2 + 4*f^2) + 2*b*e*f*log(f)/(c^2*log(f)^2 + 4*f^2) + 1/4*b^2*log(f)/c))*sqrt(-c*log(f)))

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int f^{cx^2+bx+a} \sin(fx^2+ex+d)^2 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(f^(a + b*x + c*x^2)*sin(d + e*x + f*x^2)^2,x)

[Out] int(f^(a + b*x + c*x^2)*sin(d + e*x + f*x^2)^2, x)

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f**(c*x**2+b*x+a)*sin(f*x**2+e*x+d)**2,x)

[Out] Timed out


```
Int[(u_)*(F_)^(v_)*(G_)^(w_), x_Symbol] := With[{z = v*Log[F] + w*Log[G]},
  Int[u*NormalizeIntegrand[E^z, x], x] /; BinomialQ[z, x] || (PolynomialQ[z,
  x] && LeQ[Exponent[z, x], 2])] /; FreeQ[{F, G}, x]
```

Rule 4472

```
Int[(F_)^(u_)*Sin[v_]^(n_), x_Symbol] := Int[ExpandTrigToExp[F^u, Sin[v]^n
, x], x] /; FreeQ[F, x] && (LinearQ[u, x] || PolyQ[u, x, 2]) && (LinearQ[v,
x] || PolyQ[v, x, 2]) && IGtQ[n, 0]
```

Rubi steps

$$\begin{aligned} \int f^{a+bx+cx^2} \sin^3(d+ex+fx^2) dx &= \int \left(-\frac{1}{8} i e^{-3i(d+ex+fx^2)} f^{a+bx+cx^2} + \frac{3}{8} i \exp(2id + 2iex + 2ifx^2 - 3i(d+ex+fx^2)) \right. \\ &= -\left(\frac{1}{8} i \int e^{-3i(d+ex+fx^2)} f^{a+bx+cx^2} dx \right) + \frac{1}{8} i \int \exp(6id + 6iex + 6ifx^2 - 3i(d+ex+fx^2)) dx \\ &= -\left(\frac{1}{8} i \int \exp(-3id + a \log(f) - x(3ie - b \log(f)) - x^2(3if - c \log(f))) dx \right) \\ &= \frac{1}{8} \left(3i \exp\left(-id - \frac{(e+ib \log(f))^2}{4if-4c \log(f)}\right) f^a \right) \int \exp\left(\frac{(-ie+b \log(f)+2x(-if+c \log(f)))}{4(-if+c \log(f))}\right) dx \\ &= \frac{3i \exp\left(-id - \frac{(e+ib \log(f))^2}{4if-4c \log(f)}\right) f^a \sqrt{\pi} \operatorname{erf}\left(\frac{ie-b \log(f)+2x(if-c \log(f))}{2\sqrt{if-c \log(f)}}\right) - i \exp(-3id)}{16\sqrt{if-c \log(f)}} \end{aligned}$$

Mathematica [B] time = 7.26, size = 3835, normalized size = 8.92

Result too large to show

Warning: Unable to verify antiderivative.

```
[In] Integrate[f^(a + b*x + c*x^2)*Sin[d + e*x + f*x^2]^3,x]
```

```
[Out] (f^a*Sqrt[Pi]*(-27*(-1)^(3/4)*E^(((I/4)*(-e^2 + (2*I)*b*e*Log[f] + b^2*Log[f]^2)))/(f - I*c*Log[f]))*f^3*Cos[d]*Erfi[(-1)^(1/4)*(e + 2*f*x - I*b*Log[f] - (2*I)*c*x*Log[f])]/(2*Sqrt[f - I*c*Log[f]])]*Sqrt[f - I*c*Log[f]] + 27*(-1)^(1/4)*c*E^(((I/4)*(-e^2 + (2*I)*b*e*Log[f] + b^2*Log[f]^2)))/(f - I*c*Log[f]))*f^2*Cos[d]*Erfi[(-1)^(1/4)*(e + 2*f*x - I*b*Log[f] - (2*I)*c*x*Log[f])]/(2*Sqrt[f - I*c*Log[f]])]*Log[f]*Sqrt[f - I*c*Log[f]] - 3*(-1)^(3/4)*c^2*E^(((I/4)*(-e^2 + (2*I)*b*e*Log[f] + b^2*Log[f]^2)))/(f - I*c*Log[f]))*f*Cos[d]*Erfi[(-1)^(1/4)*(e + 2*f*x - I*b*Log[f] - (2*I)*c*x*Log[f])]/(2*Sqrt[f - I*c*Log[f]])]*Log[f]^2*Sqrt[f - I*c*Log[f]] + 3*(-1)^(1/4)*c^3*E^(((I/4)*(-e^2 + (2*I)*b*e*Log[f] + b^2*Log[f]^2)))/(f - I*c*Log[f]))*Cos[d]*Erfi[(-1)^(1/4)*(e + 2*f*x - I*b*Log[f] - (2*I)*c*x*Log[f])]/(2*Sqrt[f - I*c*Log[f]])]*Log[f]^3*Sqrt[f - I*c*Log[f]] + 3*(-1)^(3/4)*E^(((I/4)*(-9*e^2 + (6*I)*b*e*Log[f] + b^2*Log[f]^2)))/(3*f - I*c*Log[f]))*f^3*Cos[3*d]*Erfi[(-1)^(1/4)*(3*e + 6*f*x - I*b*Log[f] - (2*I)*c*x*Log[f])]/(2*Sqrt[3*f - I*c*Log[f]])]*Sqrt[3*f - I*c*Log[f]] - (-1)^(1/4)*c*E^(((I/4)*(-9*e^2 + (6*I)*b*e*Log[f] + b^2*Log[f]^2)))/(3*f - I*c*Log[f]))*f^2*Cos[3*d]*Erfi[(-1)^(1/4)*(3*e + 6*f*x - I*b*Log[f] - (2*I)*c*x*Log[f])]/(2*Sqrt[3*f - I*c*Log[f]])]*Log[f]*Sqrt[3*f - I*c*Log[f]] + 3*(-1)^(3/4)*c^2*E^(((I/4)*(-9*e^2 + (6*I)*b*e*Log[f] + b^2*Log[f]^2)))/(3*f - I*c*Log[f]))*f*Cos[3*d]*Erfi[(-1)^(1/4)*(3*e + 6*f*x - I*b*Log[f] - (2*I)*c*x*Log[f])]/(2*Sqrt[3*f - I*c*Log[f]])]*Log[f]^2*Sqrt[3*f - I*c*Log[f]] - (-1)^(1/4)*c^3*E^(((I/4)*(-9*e^2 + (6*I)*b*e*Log[f] + b^2*Log[f]^2)))/(3*f - I*c*Log[f]))*Cos[3*d]*Erfi[(-1)^(1/4)*(3*e + 6*f*x - I*b*Log[f] - (2*I)*c*x*Log[f])]/(2*Sqrt[3*f - I*c*Log[f]])]
```


$$\begin{aligned}
& * \text{Log}[f]^3 \text{Sqrt}[3f - I*c*\text{Log}[f]] + (27*(-1)^{(1/4)}*f^3 \text{Cos}[d]*\text{Erfi}[((-1)^{(3/4)} \\
& (e + 2*f*x + I*b*\text{Log}[f] + (2*I)*c*x*\text{Log}[f]))/(2*\text{Sqrt}[f + I*c*\text{Log}[f]])]*\text{S} \\
& \text{qrt}[f + I*c*\text{Log}[f]])/E^{((I/4)*(-e^2 - (2*I)*b*e*\text{Log}[f] + b^2*\text{Log}[f]^2))/(f \\
& + I*c*\text{Log}[f])} - (27*(-1)^{(3/4)}*c*f^2 \text{Cos}[d]*\text{Erfi}[((-1)^{(3/4)}*(e + 2*f*x + \\
& I*b*\text{Log}[f] + (2*I)*c*x*\text{Log}[f]))/(2*\text{Sqrt}[f + I*c*\text{Log}[f]])]*\text{Log}[f]*\text{Sqrt}[f + \\
& I*c*\text{Log}[f]])/E^{((I/4)*(-e^2 - (2*I)*b*e*\text{Log}[f] + b^2*\text{Log}[f]^2))/(f + I*c*\text{L} \\
& \text{og}[f])} + (3*(-1)^{(1/4)}*c^2*f*\text{Cos}[d]*\text{Erfi}[((-1)^{(3/4)}*(e + 2*f*x + I*b*\text{Log}[\\
& f] + (2*I)*c*x*\text{Log}[f]))/(2*\text{Sqrt}[f + I*c*\text{Log}[f]])]*\text{Log}[f]^2*\text{Sqrt}[f + I*c*\text{Log} \\
& [f]])/E^{((I/4)*(-e^2 - (2*I)*b*e*\text{Log}[f] + b^2*\text{Log}[f]^2))/(f + I*c*\text{Log}[f])} \\
& - (3*(-1)^{(3/4)}*c^3*\text{Cos}[d]*\text{Erfi}[((-1)^{(3/4)}*(e + 2*f*x + I*b*\text{Log}[f] + (2*I) \\
&)*c*x*\text{Log}[f]))/(2*\text{Sqrt}[f + I*c*\text{Log}[f]])]*\text{Log}[f]^3*\text{Sqrt}[f + I*c*\text{Log}[f]])/E^{(\\
& ((I/4)*(-e^2 - (2*I)*b*e*\text{Log}[f] + b^2*\text{Log}[f]^2))/(f + I*c*\text{Log}[f])} - (3*(-1) \\
&)^{(1/4)}*f^3 \text{Cos}[3*d]*\text{Erfi}[((-1)^{(3/4)}*(3*e + 6*f*x + I*b*\text{Log}[f] + (2*I)*c*x \\
& *\text{Log}[f]))/(2*\text{Sqrt}[3f + I*c*\text{Log}[f]])]*\text{Sqrt}[3f + I*c*\text{Log}[f]])/E^{((I/4)*(-9 \\
& *e^2 - (6*I)*b*e*\text{Log}[f] + b^2*\text{Log}[f]^2))/(3f + I*c*\text{Log}[f])} + ((-1)^{(3/4)}* \\
& c*f^2 \text{Cos}[3*d]*\text{Erfi}[((-1)^{(3/4)}*(3*e + 6*f*x + I*b*\text{Log}[f] + (2*I)*c*x*\text{Log}[f \\
&]))/(2*\text{Sqrt}[3f + I*c*\text{Log}[f]])]*\text{Log}[f]*\text{Sqrt}[3f + I*c*\text{Log}[f]])/E^{((I/4)*(- \\
& 9*e^2 - (6*I)*b*e*\text{Log}[f] + b^2*\text{Log}[f]^2))/(3f + I*c*\text{Log}[f])} - (3*(-1)^{(1/ \\
& 4)}*c^2*f*\text{Cos}[3*d]*\text{Erfi}[((-1)^{(3/4)}*(3*e + 6*f*x + I*b*\text{Log}[f] + (2*I)*c*x*\text{L} \\
& \text{og}[f]))/(2*\text{Sqrt}[3f + I*c*\text{Log}[f]])]*\text{Log}[f]^2*\text{Sqrt}[3f + I*c*\text{Log}[f]])/E^{((I/ \\
& 4)*(-9*e^2 - (6*I)*b*e*\text{Log}[f] + b^2*\text{Log}[f]^2))/(3f + I*c*\text{Log}[f])} + ((-1)^{ \\
& (3/4)}*c^3*\text{Cos}[3*d]*\text{Erfi}[((-1)^{(3/4)}*(3*e + 6*f*x + I*b*\text{Log}[f] + (2*I)*c*x*\text{L} \\
& \text{og}[f]))/(2*\text{Sqrt}[3f + I*c*\text{Log}[f]])]*\text{Log}[f]^3*\text{Sqrt}[3f + I*c*\text{Log}[f]])/E^{((I \\
& /4)*(-9*e^2 - (6*I)*b*e*\text{Log}[f] + b^2*\text{Log}[f]^2))/(3f + I*c*\text{Log}[f])} + 27*(- \\
& 1)^{(1/4)}*E^{((I/4)*(-e^2 + (2*I)*b*e*\text{Log}[f] + b^2*\text{Log}[f]^2))/(f - I*c*\text{Log}[f \\
&])*f^3*\text{Erfi}[((-1)^{(1/4)}*(e + 2*f*x - I*b*\text{Log}[f] - (2*I)*c*x*\text{Log}[f]))/(2*\text{S} \\
& \text{qrt}[f - I*c*\text{Log}[f]])]*\text{Sqrt}[f - I*c*\text{Log}[f]]*\text{Sin}[d] + 27*(-1)^{(3/4)}*c*E^{((I/4) \\
&)*(-e^2 + (2*I)*b*e*\text{Log}[f] + b^2*\text{Log}[f]^2))/(f - I*c*\text{Log}[f])}*f^2*\text{Erfi}[((-1) \\
&)^{(1/4)}*(e + 2*f*x - I*b*\text{Log}[f] - (2*I)*c*x*\text{Log}[f]))/(2*\text{Sqrt}[f - I*c*\text{Log}[f] \\
&])*\text{Log}[f]*\text{Sqrt}[f - I*c*\text{Log}[f]]*\text{Sin}[d] + 3*(-1)^{(1/4)}*c^2*E^{((I/4)*(-e^2 + \\
& (2*I)*b*e*\text{Log}[f] + b^2*\text{Log}[f]^2))/(f - I*c*\text{Log}[f])}*f*\text{Erfi}[((-1)^{(1/4)}*(e \\
& + 2*f*x - I*b*\text{Log}[f] - (2*I)*c*x*\text{Log}[f]))/(2*\text{Sqrt}[f - I*c*\text{Log}[f]])]*\text{Log}[f]^ \\
& 2*\text{Sqrt}[f - I*c*\text{Log}[f]]*\text{Sin}[d] + 3*(-1)^{(3/4)}*c^3*E^{((I/4)*(-e^2 + (2*I)*b* \\
& e*\text{Log}[f] + b^2*\text{Log}[f]^2))/(f - I*c*\text{Log}[f])}*Erfi}[((-1)^{(1/4)}*(e + 2*f*x - I \\
& *b*\text{Log}[f] - (2*I)*c*x*\text{Log}[f]))/(2*\text{Sqrt}[f - I*c*\text{Log}[f]])]*\text{Log}[f]^3*\text{Sqrt}[f - \\
& I*c*\text{Log}[f]]*\text{Sin}[d] - (27*(-1)^{(3/4)}*f^3*\text{Erfi}[((-1)^{(3/4)}*(e + 2*f*x + I*b*\text{L} \\
& \text{og}[f] + (2*I)*c*x*\text{Log}[f]))/(2*\text{Sqrt}[f + I*c*\text{Log}[f]])]*\text{Sqrt}[f + I*c*\text{Log}[f]]*\text{S} \\
& \text{in}[d])/E^{((I/4)*(-e^2 - (2*I)*b*e*\text{Log}[f] + b^2*\text{Log}[f]^2))/(f + I*c*\text{Log}[f])} \\
&) - (27*(-1)^{(1/4)}*c*f^2*\text{Erfi}[((-1)^{(3/4)}*(e + 2*f*x + I*b*\text{Log}[f] + (2*I)*c \\
& *x*\text{Log}[f]))/(2*\text{Sqrt}[f + I*c*\text{Log}[f]])]*\text{Log}[f]*\text{Sqrt}[f + I*c*\text{Log}[f]]*\text{Sin}[d])/E \\
& ^{((I/4)*(-e^2 - (2*I)*b*e*\text{Log}[f] + b^2*\text{Log}[f]^2))/(f + I*c*\text{Log}[f])} - (3*(- \\
& -1)^{(3/4)}*c^2*f*\text{Erfi}[((-1)^{(3/4)}*(e + 2*f*x + I*b*\text{Log}[f] + (2*I)*c*x*\text{Log}[f] \\
&))/(2*\text{Sqrt}[f + I*c*\text{Log}[f]])]*\text{Log}[f]^2*\text{Sqrt}[f + I*c*\text{Log}[f]]*\text{Sin}[d])/E^{((I/4) \\
&)*(-e^2 - (2*I)*b*e*\text{Log}[f] + b^2*\text{Log}[f]^2))/(f + I*c*\text{Log}[f])} - (3*(-1)^{(1/ \\
& 4)}*c^3*\text{Erfi}[((-1)^{(3/4)}*(e + 2*f*x + I*b*\text{Log}[f] + (2*I)*c*x*\text{Log}[f]))/(2*\text{S} \\
& \text{qrt}[f + I*c*\text{Log}[f]])]*\text{Log}[f]^3*\text{Sqrt}[f + I*c*\text{Log}[f]]*\text{Sin}[d])/E^{((I/4)*(-e^2 - \\
& (2*I)*b*e*\text{Log}[f] + b^2*\text{Log}[f]^2))/(f + I*c*\text{Log}[f])} - 3*(-1)^{(1/4)}*E^{((I/ \\
& 4)*(-9*e^2 + (6*I)*b*e*\text{Log}[f] + b^2*\text{Log}[f]^2))/(3f - I*c*\text{Log}[f])}*f^3*\text{Erfi} \\
& [((-1)^{(1/4)}*(3*e + 6*f*x - I*b*\text{Log}[f] - (2*I)*c*x*\text{Log}[f]))/(2*\text{Sqrt}[3f - I \\
& *c*\text{Log}[f]])]*\text{Sqrt}[3f - I*c*\text{Log}[f]]*\text{Sin}[3*d] - (-1)^{(3/4)}*c*E^{((I/4)*(-9*e \\
& ^2 + (6*I)*b*e*\text{Log}[f] + b^2*\text{Log}[f]^2))/(3f - I*c*\text{Log}[f])}*f^2*\text{Erfi}[((-1)^{(\\
& 1/4)}*(3*e + 6*f*x - I*b*\text{Log}[f] - (2*I)*c*x*\text{Log}[f]))/(2*\text{Sqrt}[3f - I*c*\text{Log}[f \\
&])]* \\
& \text{Log}[f]*\text{Sqrt}[3f - I*c*\text{Log}[f]]*\text{Sin}[3*d] - 3*(-1)^{(1/4)}*c^2*E^{((I/4)*(- \\
& 9*e^2 + (6*I)*b*e*\text{Log}[f] + b^2*\text{Log}[f]^2))/(3f - I*c*\text{Log}[f])}*f*\text{Erfi}[((-1)^{ \\
& (1/4)}*(3*e + 6*f*x - I*b*\text{Log}[f] - (2*I)*c*x*\text{Log}[f]))/(2*\text{Sqrt}[3f - I*c*\text{Log}[f \\
&])]* \\
& \text{Log}[f]^2*\text{Sqrt}[3f - I*c*\text{Log}[f]]*\text{Sin}[3*d] - (-1)^{(3/4)}*c^3*E^{((I/4)*(- \\
& 9*e^2 + (6*I)*b*e*\text{Log}[f] + b^2*\text{Log}[f]^2))/(3f - I*c*\text{Log}[f])}*Erfi}[((-1)^{(\\
& 1/4)}*(3*e + 6*f*x - I*b*\text{Log}[f] - (2*I)*c*x*\text{Log}[f]))/(2*\text{Sqrt}[3f - I*c*\text{Log}[f \\
&])]* \\
& \text{Log}[f]^3*\text{Sqrt}[3f - I*c*\text{Log}[f]]*\text{Sin}[3*d] + (3*(-1)^{(3/4)}*f^3*\text{Erfi}[((-1)
\end{aligned}$$

```
)^(3/4)*(3*e + 6*f*x + I*b*Log[f] + (2*I)*c*x*Log[f]))/(2*Sqrt[3*f + I*c*Log[f]])*Sqrt[3*f + I*c*Log[f]]*Sin[3*d])/E^(((I/4)*(-9*e^2 - (6*I)*b*e*Log[f] + b^2*Log[f]^2))/(3*f + I*c*Log[f])) + ((-1)^(1/4)*c*f^2*Erfi[(-1)^(3/4)*(3*e + 6*f*x + I*b*Log[f] + (2*I)*c*x*Log[f]))/(2*Sqrt[3*f + I*c*Log[f]])*Log[f]*Sqrt[3*f + I*c*Log[f]]*Sin[3*d])/E^(((I/4)*(-9*e^2 - (6*I)*b*e*Log[f] + b^2*Log[f]^2))/(3*f + I*c*Log[f])) + (3*(-1)^(3/4)*c^2*f*Erfi[(-1)^(3/4)*(3*e + 6*f*x + I*b*Log[f] + (2*I)*c*x*Log[f]))/(2*Sqrt[3*f + I*c*Log[f]])*Log[f]^2*Sqrt[3*f + I*c*Log[f]]*Sin[3*d])/E^(((I/4)*(-9*e^2 - (6*I)*b*e*Log[f] + b^2*Log[f]^2))/(3*f + I*c*Log[f])) + ((-1)^(1/4)*c^3*Erfi[(-1)^(3/4)*(3*e + 6*f*x + I*b*Log[f] + (2*I)*c*x*Log[f]))/(2*Sqrt[3*f + I*c*Log[f]])*Log[f]^3*Sqrt[3*f + I*c*Log[f]]*Sin[3*d])/E^(((I/4)*(-9*e^2 - (6*I)*b*e*Log[f] + b^2*Log[f]^2))/(3*f + I*c*Log[f])))/(16*(I*f - c*Log[f])*(f - I*c*Log[f])*(3*f - I*c*Log[f])*(3*f + I*c*Log[f]))
```

fricas [B] time = 0.87, size = 861, normalized size = 2.00

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(c*x^2+b*x+a)*sin(f*x^2+e*x+d)^3,x, algorithm="fricas")

```
[Out] 1/16*(sqrt(pi)*(-I*c^3*log(f)^3 - 3*c^2*f*log(f)^2 - I*c*f^2*log(f) - 3*f^3)*sqrt(-c*log(f) - 3*I*f)*erf(1/2*(18*f^2*x + (2*c^2*x + b*c)*log(f)^2 + 9*e*f + (3*I*c*e - 3*I*b*f)*log(f))*sqrt(-c*log(f) - 3*I*f)/(c^2*log(f)^2 + 9*f^2))*e^(-1/4*((b^2*c - 4*a*c^2)*log(f)^3 + 27*I*e^2*f - 108*I*d*f^2 - (12*I*c^2*d - 6*I*b*c*e + 3*I*b^2*f)*log(f)^2 - 9*(c*e^2 - 2*b*e*f + 4*a*f^2)*log(f))/(c^2*log(f)^2 + 9*f^2)) + sqrt(pi)*(3*I*c^3*log(f)^3 + 3*c^2*f*log(f)^2 + 27*I*c*f^2*log(f) + 27*f^3)*sqrt(-c*log(f) - I*f)*erf(1/2*(2*f^2*x + (2*c^2*x + b*c)*log(f)^2 + e*f + (I*c*e - I*b*f)*log(f))*sqrt(-c*log(f) - I*f)/(c^2*log(f)^2 + f^2))*e^(-1/4*((b^2*c - 4*a*c^2)*log(f)^3 + I*e^2*f - 4*I*d*f^2 - (4*I*c^2*d - 2*I*b*c*e + I*b^2*f)*log(f)^2 - (c*e^2 - 2*b*e*f + 4*a*f^2)*log(f))/(c^2*log(f)^2 + f^2)) + sqrt(pi)*(-3*I*c^3*log(f)^3 + 3*c^2*f*log(f)^2 - 27*I*c*f^2*log(f) + 27*f^3)*sqrt(-c*log(f) + I*f)*erf(1/2*(2*f^2*x + (2*c^2*x + b*c)*log(f)^2 + e*f + (-I*c*e + I*b*f)*log(f))*sqrt(-c*log(f) + I*f)/(c^2*log(f)^2 + f^2))*e^(-1/4*((b^2*c - 4*a*c^2)*log(f)^3 - I*e^2*f + 4*I*d*f^2 - (-4*I*c^2*d + 2*I*b*c*e - I*b^2*f)*log(f)^2 - (c*e^2 - 2*b*e*f + 4*a*f^2)*log(f))/(c^2*log(f)^2 + f^2)) + sqrt(pi)*(I*c^3*log(f)^3 - 3*c^2*f*log(f)^2 + I*c*f^2*log(f) - 3*f^3)*sqrt(-c*log(f) + 3*I*f)*erf(1/2*(18*f^2*x + (2*c^2*x + b*c)*log(f)^2 + 9*e*f + (-3*I*c*e + 3*I*b*f)*log(f))*sqrt(-c*log(f) + 3*I*f)/(c^2*log(f)^2 + 9*f^2))*e^(-1/4*((b^2*c - 4*a*c^2)*log(f)^3 - 27*I*e^2*f + 108*I*d*f^2 - (-12*I*c^2*d + 6*I*b*c*e - 3*I*b^2*f)*log(f)^2 - 9*(c*e^2 - 2*b*e*f + 4*a*f^2)*log(f))/(c^2*log(f)^2 + 9*f^2)))/(c^4*log(f)^4 + 10*c^2*f^2*log(f)^2 + 9*f^4)
```

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int f^{cx^2+bx+a} \sin(fx^2 + ex + d)^3 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(c*x^2+b*x+a)*sin(f*x^2+e*x+d)^3,x, algorithm="giac")

[Out] integrate(f^(c*x^2 + b*x + a)*sin(f*x^2 + e*x + d)^3, x)

maple [A] time = 1.25, size = 430, normalized size = 1.00

$$\frac{i\sqrt{\pi} f^a e^{-\frac{\ln(f)^2 b^2 + 6i \ln(f) b e - 12id \ln(f) c + 36df - 9e^2}{4(3if + c \ln(f))}} \operatorname{erf}\left(-\sqrt{-c \ln(f) - 3if} x + \frac{3ie + b \ln(f)}{2\sqrt{-c \ln(f) - 3if}}\right) + i\sqrt{\pi} f^a e^{-\frac{\ln(f)^2 b^2 - 6i \ln(f) b e + 12id \ln(f) c - 36df + 9e^2}{4(-3if + c \ln(f))}}}{16\sqrt{-c \ln(f) - 3if}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}(f^{(c*x^2+b*x+a)}*\sin(f*x^2+e*x+d)^3,x)$

[Out]
$$\begin{aligned} & -1/16*I*Pi^{(1/2)}*f^a*\exp(-1/4*(\ln(f)^2*b^2+6*I*\ln(f)*b*e-12*I*d*\ln(f)*c+36*d*f-9*e^2)/(3*I*f+c*\ln(f)))/(-c*\ln(f)-3*I*f)^{(1/2)}*\text{erf}(-(-c*\ln(f)-3*I*f)^{(1/2)}*x+1/2*(3*I*e+b*\ln(f)))/(-c*\ln(f)-3*I*f)^{(1/2)}+1/16*I*Pi^{(1/2)}*f^a*\exp(-1/4*(\ln(f)^2*b^2-6*I*\ln(f)*b*e+12*I*d*\ln(f)*c+36*d*f-9*e^2)/(-3*I*f+c*\ln(f)))/((3*I*f-c*\ln(f))^{(1/2)}*\text{erf}(-x*(3*I*f-c*\ln(f))^{(1/2)}+1/2*(b*\ln(f)-3*I*e)/(3*I*f-c*\ln(f))^{(1/2)}))-3/16*I*Pi^{(1/2)}*f^a*\exp(-1/4*(4*d*f-e^2-2*I*\ln(f)*b*e+4*I*d*\ln(f)*c+\ln(f)^2*b^2)/(-I*f+c*\ln(f)))/(I*f-c*\ln(f))^{(1/2)}*\text{erf}(-x*(I*f-c*\ln(f))^{(1/2)}+1/2*(-I*e+b*\ln(f))/(I*f-c*\ln(f))^{(1/2)})+3/16*I*Pi^{(1/2)}*f^a*\exp(-1/4*(4*d*f-e^2+2*I*\ln(f)*b*e-4*I*d*\ln(f)*c+\ln(f)^2*b^2)/(I*f+c*\ln(f)))/(-I*f-c*\ln(f))^{(1/2)}*\text{erf}(-(-I*f-c*\ln(f))^{(1/2)}*x+1/2*(I*e+b*\ln(f)))/(-I*f-c*\ln(f))^{(1/2)} \end{aligned}$$

maxima [B] time = 0.49, size = 4348, normalized size = 10.11

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{integrate}(f^{(c*x^2+b*x+a)}*\sin(f*x^2+e*x+d)^3,x, \text{algorithm}="maxima")$

[Out]
$$\begin{aligned} & -1/32*(\text{sqrt}(\pi)*\text{sqrt}(2*c^2*\log(f)^2 + 18*f^2))*(((c^2*f^a*e^{(1/4*b^2*c*\log(f)^3/(c^2*\log(f)^2 + f^2) + 9/4*c*e^2*\log(f)/(c^2*\log(f)^2 + 9*f^2) + 1/2*b*e*f*\log(f)/(c^2*\log(f)^2 + f^2))*\log(f)^2 + f^{(a + 2)}*e^{(1/4*b^2*c*\log(f)^3/(c^2*\log(f)^2 + f^2) + 9/4*c*e^2*\log(f)/(c^2*\log(f)^2 + 9*f^2) + 1/2*b*e*f*\log(f)/(c^2*\log(f)^2 + f^2)))*\cos(-3/4*(9*e^2*f - 36*d*f^2 - (4*c^2*d - 2*b*c*e + b^2*f)*\log(f)^2)/(c^2*\log(f)^2 + 9*f^2)) + (-I*c^2*f^a*e^{(1/4*b^2*c*\log(f)^3/(c^2*\log(f)^2 + f^2) + 9/4*c*e^2*\log(f)/(c^2*\log(f)^2 + 9*f^2) + 1/2*b*e*f*\log(f)/(c^2*\log(f)^2 + f^2))*\log(f)^2 - I*f^{(a + 2)}*e^{(1/4*b^2*c*\log(f)^3/(c^2*\log(f)^2 + f^2) + 9/4*c*e^2*\log(f)/(c^2*\log(f)^2 + 9*f^2) + 1/2*b*e*f*\log(f)/(c^2*\log(f)^2 + f^2)))*\sin(-3/4*(9*e^2*f - 36*d*f^2 - (4*c^2*d - 2*b*c*e + b^2*f)*\log(f)^2)/(c^2*\log(f)^2 + 9*f^2)))*\text{erf}(1/2*(2*(c*\log(f) - 3*I*f)*x + b*\log(f) - 3*I*e)*\text{sqrt}(-c*\log(f) + 3*I*f)/(c*\log(f) - 3*I*f)) + ((c^2*f^a*e^{(1/4*b^2*c*\log(f)^3/(c^2*\log(f)^2 + f^2) + 9/4*c*e^2*\log(f)/(c^2*\log(f)^2 + 9*f^2) + 1/2*b*e*f*\log(f)/(c^2*\log(f)^2 + f^2))*\log(f)^2 + f^{(a + 2)}*e^{(1/4*b^2*c*\log(f)^3/(c^2*\log(f)^2 + f^2) + 9/4*c*e^2*\log(f)/(c^2*\log(f)^2 + 9*f^2) + 1/2*b*e*f*\log(f)/(c^2*\log(f)^2 + f^2)))*\cos(-3/4*(9*e^2*f - 36*d*f^2 - (4*c^2*d - 2*b*c*e + b^2*f)*\log(f)^2)/(c^2*\log(f)^2 + 9*f^2)) + (I*c^2*f^a*e^{(1/4*b^2*c*\log(f)^3/(c^2*\log(f)^2 + f^2) + 9/4*c*e^2*\log(f)/(c^2*\log(f)^2 + 9*f^2) + 1/2*b*e*f*\log(f)/(c^2*\log(f)^2 + f^2))*\log(f)^2 + I*f^{(a + 2)}*e^{(1/4*b^2*c*\log(f)^3/(c^2*\log(f)^2 + f^2) + 9/4*c*e^2*\log(f)/(c^2*\log(f)^2 + 9*f^2) + 1/2*b*e*f*\log(f)/(c^2*\log(f)^2 + f^2)))*\sin(-3/4*(9*e^2*f - 36*d*f^2 - (4*c^2*d - 2*b*c*e + b^2*f)*\log(f)^2)/(c^2*\log(f)^2 + 9*f^2)))*\text{erf}(1/2*(2*(c*\log(f) + 3*I*f)*x + b*\log(f) + 3*I*e)*\text{sqrt}(-c*\log(f) - 3*I*f)/(c*\log(f) + 3*I*f)))*\text{sqrt}(c*\log(f) + \text{sqrt}(c^2*\log(f)^2 + 9*f^2)) - \text{sqrt}(\pi)*\text{sqrt}(2*c^2*\log(f)^2 + 2*f^2))*((3*(c^2*f^a*e^{(1/4*b^2*c*\log(f)^3/(c^2*\log(f)^2 + 9*f^2) + 1/4*c*e^2*\log(f)/(c^2*\log(f)^2 + f^2) + 9/2*b*e*f*\log(f)/(c^2*\log(f)^2 + 9*f^2))*\log(f)^2 + 9*f^{(a + 2)}*e^{(1/4*b^2*c*\log(f)^3/(c^2*\log(f)^2 + 9*f^2) + 1/4*c*e^2*\log(f)/(c^2*\log(f)^2 + f^2) + 9/2*b*e*f*\log(f)/(c^2*\log(f)^2 + 9*f^2)))*\cos(-1/4*(e^2*f - 4*d*f^2 - (4*c^2*d - 2*b*c*e + b^2*f)*\log(f)^2)/(c^2*\log(f)^2 + f^2)) - (3*I*c^2*f^a*e^{(1/4*b^2*c*\log(f)^3/(c^2*\log(f)^2 + 9*f^2) + 1/4*c*e^2*\log(f)/(c^2*\log(f)^2 + f^2) + 9/2*b*e*f*\log(f)/(c^2*\log(f)^2 + 9*f^2))*\log(f)^2 + 27*I*f^{(a + 2)}*e^{(1/4*b^2*c*\log(f)^3/(c^2*\log(f)^2 + 9*f^2) + 1/4*c*e^2*\log(f)/(c^2*\log(f)^2 + f^2) + 9/2*b*e*f*\log(f)/(c^2*\log(f)^2 + 9*f^2)))*\sin(-1/4*(e^2*f - 4*d*f^2 - (4*c^2*d - 2*b*c*e + b^2*f)*\log(f)^2)/(c^2*\log(f)^2 + f^2)))*\text{erf}(1/2*(2*(c*\log(f) - I*f)*x + b*\log(f) - I*e)*\text{sqrt}(-c*\log(f) + I*f)/(c*\log(f) - I*f)) + (3*(c^2*f^a*e^{(1/4*b^2*c*\log(f)^3/(c^2*\log(f)^2 + 9*f^2) + 1/4*c*e^2* \end{aligned}$$

$$\begin{aligned}
& \log(f)/(c^2 \log(f)^2 + f^2) + 9/2 * b * e * f * \log(f)/(c^2 \log(f)^2 + 9 * f^2)) * \log(f) \\
&)^2 + 9 * f^{(a+2)} * e^{(1/4 * b^2 * c * \log(f)^3 / (c^2 \log(f)^2 + 9 * f^2) + 1/4 * c * e^2 * \\
& \log(f)/(c^2 \log(f)^2 + f^2) + 9/2 * b * e * f * \log(f)/(c^2 \log(f)^2 + 9 * f^2)) * \cos \\
& (-1/4 * (e^2 * f - 4 * d * f^2 - (4 * c^2 * d - 2 * b * c * e + b^2 * f) * \log(f)^2) / (c^2 \log(f)^2 \\
& + f^2)) - (-3 * I * c^2 * f^a * e^{(1/4 * b^2 * c * \log(f)^3 / (c^2 \log(f)^2 + 9 * f^2) + 1/ \\
& 4 * c * e^2 * \log(f)/(c^2 \log(f)^2 + f^2) + 9/2 * b * e * f * \log(f)/(c^2 \log(f)^2 + 9 * f^2 \\
& 2)) * \log(f)^2 - 27 * I * f^{(a+2)} * e^{(1/4 * b^2 * c * \log(f)^3 / (c^2 \log(f)^2 + 9 * f^2) \\
& + 1/4 * c * e^2 * \log(f)/(c^2 \log(f)^2 + f^2) + 9/2 * b * e * f * \log(f)/(c^2 \log(f)^2 + \\
& 9 * f^2)) * \sin(-1/4 * (e^2 * f - 4 * d * f^2 - (4 * c^2 * d - 2 * b * c * e + b^2 * f) * \log(f)^2) / \\
& (c^2 \log(f)^2 + f^2)) * \operatorname{erf}(1/2 * (2 * (c * \log(f) + I * f) * x + b * \log(f) + I * e) * \operatorname{sqrt} \\
& (-c * \log(f) - I * f) / (c * \log(f) + I * f)) * \operatorname{sqrt}(c * \log(f) + \operatorname{sqrt}(c^2 \log(f)^2 + f^2)) \\
& + \operatorname{sqrt}(\pi) * \operatorname{sqrt}(2 * c^2 \log(f)^2 + 18 * f^2) * (((I * c^2 * f^a * e^{(1/4 * b^2 * c * \log(f) \\
&)^3 / (c^2 \log(f)^2 + f^2) + 9/4 * c * e^2 * \log(f)/(c^2 \log(f)^2 + 9 * f^2) + 1/2 * b \\
& * e * f * \log(f)/(c^2 \log(f)^2 + f^2)) * \log(f)^2 + I * f^{(a+2)} * e^{(1/4 * b^2 * c * \log(f) \\
&)^3 / (c^2 \log(f)^2 + f^2) + 9/4 * c * e^2 * \log(f)/(c^2 \log(f)^2 + 9 * f^2) + 1/2 * b * \\
& e * f * \log(f)/(c^2 \log(f)^2 + f^2)) * \cos(-3/4 * (9 * e^2 * f - 36 * d * f^2 - (4 * c^2 * d - \\
& 2 * b * c * e + b^2 * f) * \log(f)^2) / (c^2 \log(f)^2 + 9 * f^2)) + (c^2 * f^a * e^{(1/4 * b^2 * c \\
& * \log(f)^3 / (c^2 \log(f)^2 + f^2) + 9/4 * c * e^2 * \log(f)/(c^2 \log(f)^2 + 9 * f^2) + \\
& 1/2 * b * e * f * \log(f)/(c^2 \log(f)^2 + f^2)) * \log(f)^2 + f^{(a+2)} * e^{(1/4 * b^2 * c * \log \\
& (f)^3 / (c^2 \log(f)^2 + f^2) + 9/4 * c * e^2 * \log(f)/(c^2 \log(f)^2 + 9 * f^2) + 1/2 \\
& * b * e * f * \log(f)/(c^2 \log(f)^2 + f^2)) * \sin(-3/4 * (9 * e^2 * f - 36 * d * f^2 - (4 * c^2 * \\
& d - 2 * b * c * e + b^2 * f) * \log(f)^2) / (c^2 \log(f)^2 + 9 * f^2)) * \operatorname{erf}(1/2 * (2 * (c * \log(f) \\
&) - 3 * I * f) * x + b * \log(f) - 3 * I * e) * \operatorname{sqrt}(-c * \log(f) + 3 * I * f) / (c * \log(f) - 3 * I * f) \\
&) + ((-I * c^2 * f^a * e^{(1/4 * b^2 * c * \log(f)^3 / (c^2 \log(f)^2 + f^2) + 9/4 * c * e^2 * \log \\
& (f)/(c^2 \log(f)^2 + 9 * f^2) + 1/2 * b * e * f * \log(f)/(c^2 \log(f)^2 + f^2)) * \log(f)^2 \\
& - I * f^{(a+2)} * e^{(1/4 * b^2 * c * \log(f)^3 / (c^2 \log(f)^2 + f^2) + 9/4 * c * e^2 * \log(f) \\
&) / (c^2 \log(f)^2 + 9 * f^2) + 1/2 * b * e * f * \log(f)/(c^2 \log(f)^2 + f^2)) * \cos(-3/ \\
& 4 * (9 * e^2 * f - 36 * d * f^2 - (4 * c^2 * d - 2 * b * c * e + b^2 * f) * \log(f)^2) / (c^2 \log(f)^2 \\
& + 9 * f^2)) + (c^2 * f^a * e^{(1/4 * b^2 * c * \log(f)^3 / (c^2 \log(f)^2 + f^2) + 9/4 * c * e^2 * \\
& 2 * \log(f)/(c^2 \log(f)^2 + 9 * f^2) + 1/2 * b * e * f * \log(f)/(c^2 \log(f)^2 + f^2)) * \log \\
& (f)^2 + f^{(a+2)} * e^{(1/4 * b^2 * c * \log(f)^3 / (c^2 \log(f)^2 + f^2) + 9/4 * c * e^2 * \log \\
& (f)/(c^2 \log(f)^2 + 9 * f^2) + 1/2 * b * e * f * \log(f)/(c^2 \log(f)^2 + f^2)) * \sin(\\
& -3/4 * (9 * e^2 * f - 36 * d * f^2 - (4 * c^2 * d - 2 * b * c * e + b^2 * f) * \log(f)^2) / (c^2 \log(f) \\
&)^2 + 9 * f^2)) * \operatorname{erf}(1/2 * (2 * (c * \log(f) + 3 * I * f) * x + b * \log(f) + 3 * I * e) * \operatorname{sqrt}(-c * \\
& \log(f) - 3 * I * f) / (c * \log(f) + 3 * I * f)) * \operatorname{sqrt}(-c * \log(f) + \operatorname{sqrt}(c^2 \log(f)^2 + 9 \\
& * f^2)) + \operatorname{sqrt}(\pi) * \operatorname{sqrt}(2 * c^2 \log(f)^2 + 2 * f^2) * (((-3 * I * c^2 * f^a * e^{(1/4 * b^2 * c \\
& * \log(f)^3 / (c^2 \log(f)^2 + 9 * f^2) + 1/4 * c * e^2 * \log(f)/(c^2 \log(f)^2 + f^2) + \\
& 9/2 * b * e * f * \log(f)/(c^2 \log(f)^2 + 9 * f^2)) * \log(f)^2 - 27 * I * f^{(a+2)} * e^{(1/4 * b \\
& ^2 * c * \log(f)^3 / (c^2 \log(f)^2 + 9 * f^2) + 1/4 * c * e^2 * \log(f)/(c^2 \log(f)^2 + f^2 \\
&) + 9/2 * b * e * f * \log(f)/(c^2 \log(f)^2 + 9 * f^2)) * \cos(-1/4 * (e^2 * f - 4 * d * f^2 - (\\
& 4 * c^2 * d - 2 * b * c * e + b^2 * f) * \log(f)^2) / (c^2 \log(f)^2 + f^2)) - 3 * (c^2 * f^a * e^{(\\
& 1/4 * b^2 * c * \log(f)^3 / (c^2 \log(f)^2 + 9 * f^2) + 1/4 * c * e^2 * \log(f)/(c^2 \log(f)^2 \\
& + f^2) + 9/2 * b * e * f * \log(f)/(c^2 \log(f)^2 + 9 * f^2)) * \log(f)^2 + 9 * f^{(a+2)} * e^{ \\
& (1/4 * b^2 * c * \log(f)^3 / (c^2 \log(f)^2 + 9 * f^2) + 1/4 * c * e^2 * \log(f)/(c^2 \log(f)^2 \\
& + f^2) + 9/2 * b * e * f * \log(f)/(c^2 \log(f)^2 + 9 * f^2)) * \sin(-1/4 * (e^2 * f - 4 * d * f \\
& ^2 - (4 * c^2 * d - 2 * b * c * e + b^2 * f) * \log(f)^2) / (c^2 \log(f)^2 + f^2)) * \operatorname{erf}(1/2 * (\\
& 2 * (c * \log(f) - I * f) * x + b * \log(f) - I * e) * \operatorname{sqrt}(-c * \log(f) + I * f) / (c * \log(f) - I * \\
& f) + ((3 * I * c^2 * f^a * e^{(1/4 * b^2 * c * \log(f)^3 / (c^2 \log(f)^2 + 9 * f^2) + 1/4 * c * e^2 * \\
& 2 * \log(f)/(c^2 \log(f)^2 + f^2) + 9/2 * b * e * f * \log(f)/(c^2 \log(f)^2 + 9 * f^2)) * \log \\
& (f)^2 + 27 * I * f^{(a+2)} * e^{(1/4 * b^2 * c * \log(f)^3 / (c^2 \log(f)^2 + 9 * f^2) + 1/4 * \\
& c * e^2 * \log(f)/(c^2 \log(f)^2 + f^2) + 9/2 * b * e * f * \log(f)/(c^2 \log(f)^2 + 9 * f^2) \\
&)) * \cos(-1/4 * (e^2 * f - 4 * d * f^2 - (4 * c^2 * d - 2 * b * c * e + b^2 * f) * \log(f)^2) / (c^2 * \\
& \log(f)^2 + f^2)) - 3 * (c^2 * f^a * e^{(1/4 * b^2 * c * \log(f)^3 / (c^2 \log(f)^2 + 9 * f^2) + \\
& 1/4 * c * e^2 * \log(f)/(c^2 \log(f)^2 + f^2) + 9/2 * b * e * f * \log(f)/(c^2 \log(f)^2 + 9 \\
& * f^2)) * \log(f)^2 + 9 * f^{(a+2)} * e^{(1/4 * b^2 * c * \log(f)^3 / (c^2 \log(f)^2 + 9 * f^2) \\
& + 1/4 * c * e^2 * \log(f)/(c^2 \log(f)^2 + f^2) + 9/2 * b * e * f * \log(f)/(c^2 \log(f)^2 + \\
& 9 * f^2)) * \sin(-1/4 * (e^2 * f - 4 * d * f^2 - (4 * c^2 * d - 2 * b * c * e + b^2 * f) * \log(f)^2) / \\
& (c^2 \log(f)^2 + f^2)) * \operatorname{erf}(1/2 * (2 * (c * \log(f) + I * f) * x + b * \log(f) + I * e) * \operatorname{sqrt} \\
& (-c * \log(f) - I * f) / (c * \log(f) + I * f)) * \operatorname{sqrt}(-c * \log(f) + \operatorname{sqrt}(c^2 \log(f)^2 + f
\end{aligned}$$

$$\frac{\log(f)^2 + 9f^4 e^{\frac{1}{4}b^2 c \log(f)^3 / (c^2 \log(f)^2 + 9f^2)} + \frac{1}{4}b^2 c \log(f)^3 / (c^2 \log(f)^2 + f^2) + \frac{9}{2}b e f \log(f) / (c^2 \log(f)^2 + 9f^2) + \frac{1}{2}b e f \log(f) / (c^2 \log(f)^2 + f^2)) \log(f)^4 + 10c^2 f^2 e^{\frac{1}{4}b^2 c \log(f)^3 / (c^2 \log(f)^2 + 9f^2)} + \frac{1}{4}b^2 c \log(f)^3 / (c^2 \log(f)^2 + f^2) + \frac{9}{2}b e f \log(f) / (c^2 \log(f)^2 + 9f^2) + \frac{1}{2}b e f \log(f) / (c^2 \log(f)^2 + f^2)) \log(f)^2 + 9f^4 e^{\frac{1}{4}b^2 c \log(f)^3 / (c^2 \log(f)^2 + 9f^2)} + \frac{1}{4}b^2 c \log(f)^3 / (c^2 \log(f)^2 + f^2) + \frac{9}{2}b e f \log(f) / (c^2 \log(f)^2 + 9f^2) + \frac{1}{2}b e f \log(f) / (c^2 \log(f)^2 + f^2))$$

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int f^{cx^2+bx+a} \sin(fx^2+ex+d)^3 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(f^(a + b*x + c*x^2)*sin(d + e*x + f*x^2)^3,x)

[Out] int(f^(a + b*x + c*x^2)*sin(d + e*x + f*x^2)^3, x)

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f**(c*x**2+b*x+a)*sin(f*x**2+e*x+d)**3,x)

[Out] Timed out

3.103 $\int f^{a+bx+cx^2} \sin(a + bx + ex^2) dx$

Optimal. Leaf size=213

$$\frac{i\sqrt{\pi} \exp\left(-\left(-\log(f) + i\right)\left(a - \frac{b^2(-\log(f)+i)}{-4c\log(f)+4ie}\right)\right) \operatorname{erf}\left(\frac{b(-\log(f)+i)+2x(-c\log(f)+ie)}{2\sqrt{-c\log(f)+ie}}\right)}{4\sqrt{-c\log(f)+ie}} - \frac{i\sqrt{\pi} \exp\left((\log(f) + i)\left(a - \frac{b^2(\log(f))}{4c\log(f)+4ie}\right)\right)}{4\sqrt{c\log(f)+ie}}$$

[Out] $-1/4*I*\operatorname{erf}(1/2*(-b*(I-\ln(f))-2*x*(I*e-c*\ln(f)))/(I*e-c*\ln(f))^{(1/2)})*\operatorname{Pi}^{(1/2)}/\exp((I-\ln(f))*(a-b^2*(I-\ln(f)))/(4*I*e-4*c*\ln(f)))/(I*e-c*\ln(f))^{(1/2)}-1/4*I*\exp((I+\ln(f))*(a-b^2*(I+\ln(f)))/(4*I*e+4*c*\ln(f)))*\operatorname{erfi}(1/2*(b*(I+\ln(f))+2*x*(I*e+c*\ln(f)))/(I*e+c*\ln(f))^{(1/2)})*\operatorname{Pi}^{(1/2)}/(I*e+c*\ln(f))^{(1/2)}$

Rubi [A] time = 0.80, antiderivative size = 213, normalized size of antiderivative = 1.00, number of steps used = 8, number of rules used = 5, integrand size = 24, $\frac{\text{number of rules}}{\text{integrand size}} = 0.208$, Rules used = {4472, 2287, 2234, 2205, 2204}

$$\frac{i\sqrt{\pi} \exp\left(-\left(-\log(f) + i\right)\left(a - \frac{b^2(-\log(f)+i)}{-4c\log(f)+4ie}\right)\right) \operatorname{Erf}\left(\frac{b(-\log(f)+i)+2x(-c\log(f)+ie)}{2\sqrt{-c\log(f)+ie}}\right)}{4\sqrt{-c\log(f)+ie}} - \frac{i\sqrt{\pi} \exp\left((\log(f) + i)\left(a - \frac{b^2(\log(f))}{4c\log(f)+4ie}\right)\right)}{4\sqrt{c\log(f)+ie}}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[f^{(a + b*x + c*x^2)}*\operatorname{Sin}[a + b*x + e*x^2], x]$

[Out] $((I/4)*\operatorname{Sqrt}[\operatorname{Pi}]*\operatorname{Erf}[(b*(I - \operatorname{Log}[f]) + 2*x*(I*e - c*\operatorname{Log}[f]))/(2*\operatorname{Sqrt}[I*e - c*\operatorname{Log}[f]])]/(\operatorname{E}^{((I - \operatorname{Log}[f])*(a - (b^2*(I - \operatorname{Log}[f]))/(4*I)*e - 4*c*\operatorname{Log}[f]))}*\operatorname{Sqrt}[I*e - c*\operatorname{Log}[f]]) - ((I/4)*\operatorname{E}^{((I + \operatorname{Log}[f])*(a - (b^2*(I + \operatorname{Log}[f]))/(4*I)*e + 4*c*\operatorname{Log}[f]))}*\operatorname{Sqrt}[\operatorname{Pi}]*\operatorname{Erfi}[(b*(I + \operatorname{Log}[f]) + 2*x*(I*e + c*\operatorname{Log}[f]))/(2*\operatorname{Sqrt}[I*e + c*\operatorname{Log}[f]])]/\operatorname{Sqrt}[I*e + c*\operatorname{Log}[f]])$

Rule 2204

$\operatorname{Int}[(F_)^{((a_.) + (b_.)*((c_.) + (d_.)*(x_)^2))}, x_Symbol] \rightarrow \operatorname{Simp}[(F^a*\operatorname{Sqrt}[\operatorname{Pi}]*\operatorname{Erfi}[(c + d*x)*\operatorname{Rt}[b*\operatorname{Log}[F], 2]])/(2*d*\operatorname{Rt}[b*\operatorname{Log}[F], 2]), x] /; \operatorname{FreeQ}\{F, a, b, c, d\}, x] \&\& \operatorname{PosQ}[b]$

Rule 2205

$\operatorname{Int}[(F_)^{((a_.) + (b_.)*((c_.) + (d_.)*(x_)^2))}, x_Symbol] \rightarrow \operatorname{Simp}[(F^a*\operatorname{Sqrt}[\operatorname{Pi}]*\operatorname{Erf}[(c + d*x)*\operatorname{Rt}[-(b*\operatorname{Log}[F]), 2]])/(2*d*\operatorname{Rt}[-(b*\operatorname{Log}[F]), 2]), x] /; \operatorname{FreeQ}\{F, a, b, c, d\}, x] \&\& \operatorname{NegQ}[b]$

Rule 2234

$\operatorname{Int}[(F_)^{((a_.) + (b_.)*(x_) + (c_.)*(x_)^2))}, x_Symbol] \rightarrow \operatorname{Dist}[F^{(a - b^2/(4*c))}, \operatorname{Int}[F^{((b + 2*c*x)^2/(4*c))}, x], x] /; \operatorname{FreeQ}\{F, a, b, c\}, x]$

Rule 2287

$\operatorname{Int}[(u_)*(F_)^{(v_)*(G_)^{(w_)}}], x_Symbol] \rightarrow \operatorname{With}\{z = v*\operatorname{Log}[F] + w*\operatorname{Log}[G]\}, \operatorname{Int}[u*\operatorname{NormalizeIntegrand}[E^z, x], x] /; \operatorname{BinomialQ}[z, x] \mid\mid (\operatorname{PolynomialQ}[z, x] \&\& \operatorname{LeQ}[\operatorname{Exponent}[z, x], 2]) /; \operatorname{FreeQ}\{F, G\}, x]$

Rule 4472

$\operatorname{Int}[(F_)^{(u_)*\operatorname{Sin}[v_]^{(n_)}}, x_Symbol] \rightarrow \operatorname{Int}[\operatorname{ExpandTrigToExp}[F^u, \operatorname{Sin}[v]^{(n)}, x], x] /; \operatorname{FreeQ}[F, x] \&\& (\operatorname{LinearQ}[u, x] \mid\mid \operatorname{PolyQ}[u, x, 2]) \&\& (\operatorname{LinearQ}[v, x] \mid\mid \operatorname{PolyQ}[v, x, 2]) \&\& \operatorname{IGtQ}[n, 0]$

Rubi steps

$$\begin{aligned}
\int f^{a+bx+cx^2} \sin(a+bx+ex^2) dx &= \int \left(\frac{1}{2} i e^{-ia-ibx-icx^2} f^{a+bx+cx^2} - \frac{1}{2} i e^{ia+ibx+icx^2} f^{a+bx+cx^2} \right) dx \\
&= \frac{1}{2} i \int e^{-ia-ibx-icx^2} f^{a+bx+cx^2} dx - \frac{1}{2} i \int e^{ia+ibx+icx^2} f^{a+bx+cx^2} dx \\
&= \frac{1}{2} i \int \exp(-a(i-\log(f)) - bx(i-\log(f)) - x^2(ie-c\log(f))) dx - \frac{1}{2} i \int \exp(a(i-\log(f)) + bx(i-\log(f)) + x^2(ie-c\log(f))) dx \\
&= \frac{1}{2} \left(i \exp\left(-i(i-\log(f)) \left(a - \frac{b^2(i-\log(f))}{4ie-4c\log(f)}\right)\right) \int \exp\left(\frac{(-b(i-\log(f)) + ex^2)(ie-c\log(f))}{4(-ie-c\log(f))}\right) dx \right. \\
&\quad \left. - i \exp\left(-i(i-\log(f)) \left(a - \frac{b^2(i-\log(f))}{4ie-4c\log(f)}\right)\right) \int \exp\left(\frac{(b(i-\log(f)) + ex^2)(ie-c\log(f))}{4(-ie-c\log(f))}\right) dx \right) \\
&= \frac{i \exp\left(-i(i-\log(f)) \left(a - \frac{b^2(i-\log(f))}{4ie-4c\log(f)}\right)\right) \sqrt{\pi} \operatorname{erf}\left(\frac{b(i-\log(f)) + 2x(ie-c\log(f))}{2\sqrt{ie-c\log(f)}}\right)}{4\sqrt{ie-c\log(f)}} - \frac{i \exp\left(i(i-\log(f)) \left(a - \frac{b^2(i-\log(f))}{4ie-4c\log(f)}\right)\right) \sqrt{\pi} \operatorname{erf}\left(\frac{b(i-\log(f)) + 2x(ie-c\log(f))}{2\sqrt{ie-c\log(f)}}\right)}{4\sqrt{ie-c\log(f)}}
\end{aligned}$$

Mathematica [A] time = 1.85, size = 324, normalized size = 1.52

$$\sqrt{\pi} e^{-\frac{b^2 c \log^3(f)}{2(c^2 \log^2(f) + e^2)}} f^{a - \frac{b^2}{2(e - ic \log(f))}} \left((\cos(a) + i \sin(a))(e + ic \log(f)) \sqrt{c \log(f) + ie} \exp\left(\frac{1}{4} b^2 \left(\frac{\log^2(f)}{c \log(f) - ie} + \frac{1}{c \log(f) + ie}\right)\right) \right)$$

Warning: Unable to verify antiderivative.

[In] Integrate[f^(a + b*x + c*x^2)*Sin[a + b*x + e*x^2], x]

[Out] (f^(a - b^2/(2*(e - I*c*Log[f]))) * Sqrt[Pi] * (-E^((b^2*((-I)*e + c*Log[f])^(-1) + Log[f]^2/(I*e + c*Log[f])))/4) * f^((I*b^2*c*Log[f])/(e^2 + c^2*Log[f]^2)) * Erfi[((-I)*(b + 2*e*x) + (b + 2*c*x)*Log[f])/(2*Sqrt[(-I)*e + c*Log[f]])] * (e - I*c*Log[f]) * Sqrt[(-I)*e + c*Log[f]] * (Cos[a] - I*Sin[a])) + E^((b^2*(Log[f]^2/((-I)*e + c*Log[f]) + (I*e + c*Log[f])^(-1)))/4) * Erfi[((-I)*(b + 2*e*x) - (b + 2*c*x)*Log[f])/(2*Sqrt[I*e + c*Log[f]])] * (e + I*c*Log[f]) * Sqrt[I*e + c*Log[f]] * (Cos[a] + I*Sin[a])))/(4 * E^((b^2*c*Log[f]^3)/(2*(e^2 + c^2*Log[f]^2))) * (e^2 + c^2*Log[f]^2))

fricas [B] time = 0.64, size = 379, normalized size = 1.78

$$\sqrt{\pi} (ic \log(f) + e) \sqrt{-c \log(f) - ie} \operatorname{erf}\left(\frac{(2e^2x + (2c^2x + bc)\log(f)^2 + be + (bc - ibe)\log(f))\sqrt{-c \log(f) - ie}}{2(c^2 \log(f)^2 + e^2)}\right) e^{-\frac{(b^2c - 4ac^2)\log(f)^3 + ib^2e}{2(c^2 \log(f)^2 + e^2)}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(c*x^2+b*x+a)*sin(e*x^2+b*x+a), x, algorithm="fricas")

[Out] 1/4*(sqrt(pi)*(I*c*log(f) + e)*sqrt(-c*log(f) - I*e)*erf(1/2*(2*e^2*x + (2*c^2*x + b*c)*log(f)^2 + b*e + (I*b*c - I*b*e)*log(f))*sqrt(-c*log(f) - I*e)/(c^2*log(f)^2 + e^2))*e^(-1/4*((b^2*c - 4*a*c^2)*log(f)^3 + I*b^2*e - 4*I*a*e^2 - (-2*I*b^2*c + 4*I*a*c^2 + I*b^2*e)*log(f)^2 - (b^2*c - 2*b^2*e + 4*a*e^2)*log(f))/(c^2*log(f)^2 + e^2)) + sqrt(pi)*(-I*c*log(f) + e)*sqrt(-c*log(f) + I*e)*erf(1/2*(2*e^2*x + (2*c^2*x + b*c)*log(f)^2 + b*e + (-I*b*c + I*b*e)*log(f))*sqrt(-c*log(f) + I*e)/(c^2*log(f)^2 + e^2))*e^(-1/4*((b^2*c - 4*a*c^2)*log(f)^3 - I*b^2*e + 4*I*a*e^2 - (2*I*b^2*c - 4*I*a*c^2 - I*b^2*e)*log(f)^2 - (b^2*c - 2*b^2*e + 4*a*e^2)*log(f))/(c^2*log(f)^2 + e^2)))/(c^2*log(f)^2 + e^2)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int f^{cx^2+bx+a} \sin(ex^2 + bx + a) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(c*x^2+b*x+a)*sin(e*x^2+b*x+a),x, algorithm="giac")

[Out] integrate(f^(c*x^2 + b*x + a)*sin(e*x^2 + b*x + a), x)

maple [A] time = 1.04, size = 217, normalized size = 1.02

$$\frac{i\sqrt{\pi} f^a e^{\frac{-4ae+b^2+4i\ln(f)ac-2i\ln(f)b^2-\ln(f)^2b^2}{4ie+4c\ln(f)}} \operatorname{erf}\left(-\sqrt{-ie-c\ln(f)} x + \frac{ib+b\ln(f)}{2\sqrt{-ie-c\ln(f)}}\right)}{4\sqrt{-ie-c\ln(f)}} - \frac{i\sqrt{\pi} f^a e^{\frac{4ae-b^2+4i\ln(f)ac-2i\ln(f)b^2+\ln(f)^2b^2}{4(-ie+c\ln(f))}}}{4\sqrt{ie-c\ln(f)}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(f^(c*x^2+b*x+a)*sin(e*x^2+b*x+a),x)

[Out] 1/4*I*Pi^(1/2)*f^a*exp(1/4*(-4*a*e+b^2+4*I*ln(f)*a*c-2*I*ln(f)*b^2-ln(f)^2*b^2)/(I*e+c*ln(f)))/(-I*e-c*ln(f))^(1/2)*erf(-(-I*e-c*ln(f))^(1/2)*x+1/2*(I*b+b*ln(f))/(-I*e-c*ln(f))^(1/2))-1/4*I*Pi^(1/2)*f^a*exp(-1/4*(4*a*e-b^2+4*I*ln(f)*a*c-2*I*ln(f)*b^2+ln(f)^2*b^2)/(-I*e+c*ln(f)))/(I*e-c*ln(f))^(1/2)*erf(-(-I*e-c*ln(f))^(1/2)*x+1/2*(-I*b+b*ln(f))/(I*e-c*ln(f))^(1/2))

maxima [B] time = 0.39, size = 1017, normalized size = 4.77

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(c*x^2+b*x+a)*sin(e*x^2+b*x+a),x, algorithm="maxima")

[Out] 1/8*(sqrt(pi)*sqrt(2*c^2*log(f)^2 + 2*e^2))*((f^(1/4*b^2*c/(c^2*log(f)^2 + e^2)))*f^a*cos(-1/4*(b^2*e - 4*a*e^2 + (2*b^2*c - 4*a*c^2 - b^2*e)*log(f)^2)/(c^2*log(f)^2 + e^2)) - I*f^(1/4*b^2*c/(c^2*log(f)^2 + e^2))*f^a*sin(-1/4*(b^2*e - 4*a*e^2 + (2*b^2*c - 4*a*c^2 - b^2*e)*log(f)^2)/(c^2*log(f)^2 + e^2)))*erf(1/2*(2*(c*log(f) - I*e)*x + b*log(f) - I*b)*sqrt(-c*log(f) + I*e)/(c*log(f) - I*e)) + (f^(1/4*b^2*c/(c^2*log(f)^2 + e^2))*f^a*cos(-1/4*(b^2*e - 4*a*e^2 + (2*b^2*c - 4*a*c^2 - b^2*e)*log(f)^2)/(c^2*log(f)^2 + e^2)) + I*f^(1/4*b^2*c/(c^2*log(f)^2 + e^2))*f^a*sin(-1/4*(b^2*e - 4*a*e^2 + (2*b^2*c - 4*a*c^2 - b^2*e)*log(f)^2)/(c^2*log(f)^2 + e^2)))*erf(1/2*(2*(c*log(f) + I*e)*x + b*log(f) + I*b)*sqrt(-c*log(f) - I*e)/(c*log(f) + I*e)))*sqrt(c*log(f) + sqrt(c^2*log(f)^2 + e^2)) + sqrt(pi)*sqrt(2*c^2*log(f)^2 + 2*e^2)*((I*f^(1/4*b^2*c/(c^2*log(f)^2 + e^2))*f^a*cos(-1/4*(b^2*e - 4*a*e^2 + (2*b^2*c - 4*a*c^2 - b^2*e)*log(f)^2)/(c^2*log(f)^2 + e^2)) + f^(1/4*b^2*c/(c^2*log(f)^2 + e^2))*f^a*sin(-1/4*(b^2*e - 4*a*e^2 + (2*b^2*c - 4*a*c^2 - b^2*e)*log(f)^2)/(c^2*log(f)^2 + e^2)))*erf(1/2*(2*(c*log(f) - I*e)*x + b*log(f) - I*b)*sqrt(-c*log(f) + I*e)/(c*log(f) - I*e)) + (-I*f^(1/4*b^2*c/(c^2*log(f)^2 + e^2))*f^a*cos(-1/4*(b^2*e - 4*a*e^2 + (2*b^2*c - 4*a*c^2 - b^2*e)*log(f)^2)/(c^2*log(f)^2 + e^2)) + f^(1/4*b^2*c/(c^2*log(f)^2 + e^2))*f^a*sin(-1/4*(b^2*e - 4*a*e^2 + (2*b^2*c - 4*a*c^2 - b^2*e)*log(f)^2)/(c^2*log(f)^2 + e^2)))*erf(1/2*(2*(c*log(f) + I*e)*x + b*log(f) + I*b)*sqrt(-c*log(f) - I*e)/(c*log(f) + I*e)))*sqrt(-c*log(f) + sqrt(c^2*log(f)^2 + e^2)))/(c^2*e^(1/4*b^2*c*log(f)^3/(c^2*log(f)^2 + e^2) + 1/2*b^2*e*log(f)/(c^2*log(f)^2 + e^2))*log(f)^2 + e^2*e^(1/4*b^2*c*log(f)^3/(c^2*log(f)^2 + e^2) + 1/2*b^2*e*log(f)/(c^2*log(f)^2 + e^2)))

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int f^{cx^2+bx+a} \sin(ex^2 + bx + a) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(f^(a + b*x + c*x^2)*sin(a + b*x + e*x^2), x)`

[Out] `int(f^(a + b*x + c*x^2)*sin(a + b*x + e*x^2), x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int f^{a+bx+cx^2} \sin(a + bx + ex^2) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(f**(c*x**2+b*x+a)*sin(e*x**2+b*x+a), x)`

[Out] `Integral(f**(a + b*x + c*x**2)*sin(a + b*x + e*x**2), x)`

3.104 $\int e^x \cos(a + bx) dx$

Optimal. Leaf size=36

$$\frac{be^x \sin(a + bx)}{b^2 + 1} + \frac{e^x \cos(a + bx)}{b^2 + 1}$$

[Out] $\exp(x) \cdot \cos(b \cdot x + a) / (b^2 + 1) + b \cdot \exp(x) \cdot \sin(b \cdot x + a) / (b^2 + 1)$

Rubi [A] time = 0.01, antiderivative size = 36, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 10, $\frac{\text{number of rules}}{\text{integrand size}} = 0.100$, Rules used = {4433}

$$\frac{be^x \sin(a + bx)}{b^2 + 1} + \frac{e^x \cos(a + bx)}{b^2 + 1}$$

Antiderivative was successfully verified.

[In] Int[E^x * Cos[a + b * x], x]

[Out] (E^x * Cos[a + b * x]) / (1 + b^2) + (b * E^x * Sin[a + b * x]) / (1 + b^2)

Rule 4433

```
Int[Cos[(d_.) + (e_.)*(x_)]*(F_)^((c_.)*((a_.) + (b_.)*(x_))), x_Symbol] :>
Simp[(b*c*Log[F]*F^(c*(a + b*x))*Cos[d + e*x])/(e^2 + b^2*c^2*Log[F]^2), x]
+ Simp[(e*F^(c*(a + b*x))*Sin[d + e*x])/(e^2 + b^2*c^2*Log[F]^2), x] /; FreeQ[{F, a, b, c, d, e}, x] && NeQ[e^2 + b^2*c^2*Log[F]^2, 0]
```

Rubi steps

$$\int e^x \cos(a + bx) dx = \frac{e^x \cos(a + bx)}{1 + b^2} + \frac{be^x \sin(a + bx)}{1 + b^2}$$

Mathematica [A] time = 0.06, size = 26, normalized size = 0.72

$$\frac{e^x(b \sin(a + bx) + \cos(a + bx))}{b^2 + 1}$$

Antiderivative was successfully verified.

[In] Integrate[E^x * Cos[a + b * x], x]

[Out] (E^x * (Cos[a + b * x] + b * Sin[a + b * x])) / (1 + b^2)

fricas [A] time = 0.94, size = 28, normalized size = 0.78

$$\frac{be^x \sin(bx + a) + \cos(bx + a) e^x}{b^2 + 1}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(x) * cos(b * x + a), x, algorithm="fricas")

[Out] (b * e^x * sin(b * x + a) + cos(b * x + a) * e^x) / (b^2 + 1)

giac [A] time = 0.13, size = 33, normalized size = 0.92

$$\left(\frac{b \sin(bx + a)}{b^2 + 1} + \frac{\cos(bx + a)}{b^2 + 1} \right) e^x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(x)*cos(b*x+a),x, algorithm="giac")

[Out] (b*sin(b*x + a)/(b^2 + 1) + cos(b*x + a)/(b^2 + 1))*e^x

maple [A] time = 0.03, size = 35, normalized size = 0.97

$$\frac{e^x \cos(bx + a)}{b^2 + 1} + \frac{b e^x \sin(bx + a)}{b^2 + 1}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(exp(x)*cos(b*x+a),x)

[Out] exp(x)*cos(b*x+a)/(b^2+1)+b*exp(x)*sin(b*x+a)/(b^2+1)

maxima [A] time = 0.31, size = 25, normalized size = 0.69

$$\frac{(b \sin(bx + a) + \cos(bx + a))e^x}{b^2 + 1}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(x)*cos(b*x+a),x, algorithm="maxima")

[Out] (b*sin(b*x + a) + cos(b*x + a))*e^x/(b^2 + 1)

mupad [B] time = 0.09, size = 25, normalized size = 0.69

$$\frac{e^x (\cos(a + bx) + b \sin(a + bx))}{b^2 + 1}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(cos(a + b*x)*exp(x),x)

[Out] (exp(x)*(cos(a + b*x) + b*sin(a + b*x)))/(b^2 + 1)

sympy [A] time = 0.77, size = 112, normalized size = 3.11

$$\begin{cases} -\frac{ixe^x \sin(a-ix)}{2} + \frac{xe^x \cos(a-ix)}{2} + \frac{e^x \cos(a-ix)}{2} & \text{for } b = -i \\ \frac{ixe^x \sin(a+ix)}{2} + \frac{xe^x \cos(a+ix)}{2} + \frac{e^x \cos(a+ix)}{2} & \text{for } b = i \\ \frac{be^x \sin(a+bx)}{b^2+1} + \frac{e^x \cos(a+bx)}{b^2+1} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(x)*cos(b*x+a),x)

[Out] Piecewise((-I*x*exp(x)*sin(a - I*x)/2 + x*exp(x)*cos(a - I*x)/2 + exp(x)*cos(a - I*x)/2, Eq(b, -I)), (I*x*exp(x)*sin(a + I*x)/2 + x*exp(x)*cos(a + I*x)/2 + exp(x)*cos(a + I*x)/2, Eq(b, I)), (b*exp(x)*sin(a + b*x)/(b**2 + 1) + exp(x)*cos(a + b*x)/(b**2 + 1), True))

3.105 $\int e^x \cos(a + cx^2) dx$

Optimal. Leaf size=115

$$\frac{\sqrt[4]{-1} \sqrt{\pi} e^{-\frac{1}{4}i\left(4a+\frac{1}{c}\right)} \operatorname{erfi}\left(\frac{\sqrt[4]{-1}(1-2icx)}{2\sqrt{c}}\right)}{4\sqrt{c}} - \frac{\sqrt[4]{-1} \sqrt{\pi} e^{\frac{1}{4}i\left(4a+\frac{1}{c}\right)} \operatorname{erf}\left(\frac{\sqrt[4]{-1}(1+2icx)}{2\sqrt{c}}\right)}{4\sqrt{c}}$$

[Out] $-1/4*(-1)^{(1/4)}*\exp(1/4*I*(4*a+1/c))*\operatorname{erf}(1/2*(-1)^{(1/4)}*(1+2*I*c*x)/c^{(1/2)})*\operatorname{Pi}^{(1/2)}/c^{(1/2)}+1/4*(-1)^{(1/4)}*\operatorname{erfi}(1/2*(-1)^{(1/4)}*(1-2*I*c*x)/c^{(1/2)})*\operatorname{Pi}^{(1/2)}/\exp(1/4*I*(4*a+1/c))/c^{(1/2)}$

Rubi [A] time = 0.10, antiderivative size = 115, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 4, integrand size = 12, $\frac{\text{number of rules}}{\text{integrand size}} = 0.333$, Rules used = {4473, 2234, 2204, 2205}

$$\frac{\sqrt[4]{-1} \sqrt{\pi} e^{-\frac{1}{4}i\left(4a+\frac{1}{c}\right)} \operatorname{Erfi}\left(\frac{\sqrt[4]{-1}(1-2icx)}{2\sqrt{c}}\right)}{4\sqrt{c}} - \frac{\sqrt[4]{-1} \sqrt{\pi} e^{\frac{1}{4}i\left(4a+\frac{1}{c}\right)} \operatorname{Erf}\left(\frac{\sqrt[4]{-1}(1+2icx)}{2\sqrt{c}}\right)}{4\sqrt{c}}$$

Antiderivative was successfully verified.

[In] Int[E^x*Cos[a + c*x^2], x]

[Out] $-((-1)^{(1/4)}*E^{((I/4)*(4*a + c^(-1)))}*Sqrt[Pi]*Erf[(((1 + (2*I)*c*x))/(2*Sqrt[c]))]/(4*Sqrt[c]) + ((-1)^{(1/4)}*Sqrt[Pi]*Erfi[(((1 - (2*I)*c*x))/(2*Sqrt[c]))]/(4*Sqrt[c]*E^{((I/4)*(4*a + c^(-1)))}))$

Rule 2204

Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))²), x_Symbol] := Simp[(F^a*Sqrt[Pi]*Erfi[(c + d*x)*Rt[b*Log[F], 2]])/(2*d*Rt[b*Log[F], 2]), x] /; FreeQ[{F, a, b, c, d}, x] && PosQ[b]

Rule 2205

Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))²), x_Symbol] := Simp[(F^a*Sqrt[Pi]*Erf[(c + d*x)*Rt[-(b*Log[F]), 2]])/(2*d*Rt[-(b*Log[F]), 2]), x] /; FreeQ[{F, a, b, c, d}, x] && NegQ[b]

Rule 2234

Int[(F_)^((a_.) + (b_.)*x_ + (c_.)*(x_)²), x_Symbol] := Dist[F^(a - b^2/(4*c)), Int[F^((b + 2*c*x)^2/(4*c)), x], x] /; FreeQ[{F, a, b, c}, x]

Rule 4473

Int[Cos[v_]^(n_.)*(F_)^(u_), x_Symbol] := Int[ExpandTrigToExp[F^u, Cos[v]^n, x], x] /; FreeQ[F, x] && (LinearQ[u, x] || PolyQ[u, x, 2]) && (LinearQ[v, x] || PolyQ[v, x, 2]) && IGtQ[n, 0]

Rubi steps

$$\begin{aligned}
\int e^x \cos(a + cx^2) dx &= \int \left(\frac{1}{2} e^{-ia+x-icx^2} + \frac{1}{2} e^{ia+x+icx^2} \right) dx \\
&= \frac{1}{2} \int e^{-ia+x-icx^2} dx + \frac{1}{2} \int e^{ia+x+icx^2} dx \\
&= \frac{1}{2} e^{-\frac{1}{4}i\left(4a+\frac{1}{c}\right)} \int e^{\frac{i(1-2icx)^2}{4c}} dx + \frac{1}{2} e^{\frac{1}{4}i\left(4a+\frac{1}{c}\right)} \int e^{-\frac{i(1+2icx)^2}{4c}} dx \\
&= \frac{\sqrt[4]{-1} e^{\frac{1}{4}i\left(4a+\frac{1}{c}\right)} \sqrt{\pi} \operatorname{erf}\left(\frac{\sqrt[4]{-1}(1+2icx)}{2\sqrt{c}}\right) - \sqrt[4]{-1} e^{-\frac{1}{4}i\left(4a+\frac{1}{c}\right)} \sqrt{\pi} \operatorname{erfi}\left(\frac{\sqrt[4]{-1}(1-2icx)}{2\sqrt{c}}\right)}{4\sqrt{c}} + \frac{\sqrt[4]{-1} e^{-\frac{1}{4}i\left(4a+\frac{1}{c}\right)} \sqrt{\pi} \operatorname{erfi}\left(\frac{\sqrt[4]{-1}(1-2icx)}{2\sqrt{c}}\right) - \sqrt[4]{-1} e^{\frac{1}{4}i\left(4a+\frac{1}{c}\right)} \sqrt{\pi} \operatorname{erf}\left(\frac{\sqrt[4]{-1}(1+2icx)}{2\sqrt{c}}\right)}{4\sqrt{c}}
\end{aligned}$$

Mathematica [A] time = 0.17, size = 109, normalized size = 0.95

$$\frac{\sqrt[4]{-1} \sqrt{\pi} e^{-\frac{i}{4}c} \left(e^{\frac{i}{2}c} (\sin(a) - i \cos(a)) \operatorname{erfi}\left(\frac{\sqrt[4]{-1}(2cx-i)}{2\sqrt{c}}\right) - (\cos(a) - i \sin(a)) \operatorname{erfi}\left(\frac{(-1)^{3/4}(2cx+i)}{2\sqrt{c}}\right) \right)}{4\sqrt{c}}$$

Antiderivative was successfully verified.

[In] Integrate[E^x*Cos[a + c*x^2],x]

[Out] $((-1)^{1/4} \sqrt{\pi} * (-\operatorname{Erfi}[\frac{(-1)^{3/4}(I + 2cx)}{2\sqrt{c}}]) * (\cos[a] - I \sin[a])) + E^{((I/2)/c)} \operatorname{Erfi}[\frac{(-1)^{1/4}(-I + 2cx)}{2\sqrt{c}}] * ((-I) * \cos[a] + \sin[a])) / (4 \sqrt{c} * E^{(I/4)/c})$

fricas [B] time = 2.09, size = 193, normalized size = 1.68

$$\frac{\sqrt{2} \pi \sqrt{\frac{c}{\pi}} e^{\left(\frac{-4iac-i}{4c}\right)} C\left(\frac{\sqrt{2}(2cx+i)\sqrt{\frac{c}{\pi}}}{2c}\right) - \sqrt{2} \pi \sqrt{\frac{c}{\pi}} e^{\left(\frac{4iac+i}{4c}\right)} C\left(-\frac{\sqrt{2}(2cx-i)\sqrt{\frac{c}{\pi}}}{2c}\right) - i \sqrt{2} \pi \sqrt{\frac{c}{\pi}} e^{\left(\frac{-4iac-i}{4c}\right)} S\left(\frac{\sqrt{2}(2cx+i)\sqrt{\frac{c}{\pi}}}{2c}\right)}{4c}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(x)*cos(c*x^2+a),x, algorithm="fricas")

[Out] $\frac{1}{4} * (\sqrt{2} * \pi * \sqrt{c/\pi}) * e^{(1/4 * (-4 * I * a * c - I) / c)} * \operatorname{fresnel_cos}(1/2 * \sqrt{2} * (2 * c * x + I) * \sqrt{c/\pi} / c) - \sqrt{2} * \pi * \sqrt{c/\pi} * e^{(1/4 * (4 * I * a * c + I) / c)} * \operatorname{fresnel_cos}(-1/2 * \sqrt{2} * (2 * c * x - I) * \sqrt{c/\pi} / c) - I * \sqrt{2} * \pi * \sqrt{c/\pi} * e^{(1/4 * (-4 * I * a * c - I) / c)} * \operatorname{fresnel_sin}(1/2 * \sqrt{2} * (2 * c * x + I) * \sqrt{c/\pi} / c) - I * \sqrt{2} * \pi * \sqrt{c/\pi} * e^{(1/4 * (4 * I * a * c + I) / c)} * \operatorname{fresnel_sin}(-1/2 * \sqrt{2} * (2 * c * x - I) * \sqrt{c/\pi} / c) / c$

giac [A] time = 0.14, size = 127, normalized size = 1.10

$$\frac{\sqrt{2} \sqrt{\pi} \operatorname{erf}\left(-\frac{1}{4} \sqrt{2} \left(2x + \frac{i}{c}\right) \left(\frac{ic}{|c|} + 1\right) \sqrt{|c|}\right) e^{\left(-\frac{4iac+i}{4c}\right)} - \sqrt{2} \sqrt{\pi} \operatorname{erf}\left(-\frac{1}{4} \sqrt{2} \left(2x - \frac{i}{c}\right) \left(-\frac{ic}{|c|} + 1\right) \sqrt{|c|}\right) e^{\left(-\frac{-4iac-i}{4c}\right)}}{4 \left(\frac{ic}{|c|} + 1\right) \sqrt{|c|}} - \frac{\sqrt{2} \sqrt{\pi} \operatorname{erf}\left(-\frac{1}{4} \sqrt{2} \left(2x - \frac{i}{c}\right) \left(-\frac{ic}{|c|} + 1\right) \sqrt{|c|}\right) e^{\left(-\frac{-4iac-i}{4c}\right)}}{4 \left(-\frac{ic}{|c|} + 1\right) \sqrt{|c|}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(x)*cos(c*x^2+a),x, algorithm="giac")

[Out] $-1/4 * \sqrt{2} * \sqrt{\pi} * \operatorname{erf}(-1/4 * \sqrt{2} * (2 * x + I/c) * (I * c / \operatorname{abs}(c) + 1) * \sqrt{\operatorname{abs}(c)}) * e^{(-1/4 * (4 * I * a * c + I) / c)} / ((I * c / \operatorname{abs}(c) + 1) * \sqrt{\operatorname{abs}(c)}) - 1/4 * \sqrt{2} * \sqrt{\pi} * \operatorname{erf}(-1/4 * \sqrt{2} * (2 * x - I/c) * (-I * c / \operatorname{abs}(c) + 1) * \sqrt{\operatorname{abs}(c)}) * e^{(-1/4 * (-4 * I * a * c - I) / c)} / ((-I * c / \operatorname{abs}(c) + 1) * \sqrt{\operatorname{abs}(c)})$

maple [A] time = 0.13, size = 86, normalized size = 0.75

$$\frac{\sqrt{\pi} e^{-\frac{i(4ac+1)}{4c}} \operatorname{erf}\left(\sqrt{ic} x - \frac{1}{2\sqrt{ic}}\right)}{4\sqrt{ic}} + \frac{\sqrt{\pi} e^{\frac{i(4ac+1)}{4c}} \operatorname{erf}\left(\sqrt{-ic} x - \frac{1}{2\sqrt{-ic}}\right)}{4\sqrt{-ic}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(exp(x)*cos(c*x^2+a),x)`

[Out] `1/4*Pi^(1/2)*exp(-1/4*I*(4*a*c+1)/c)/(I*c)^(1/2)*erf((I*c)^(1/2)*x-1/2/(I*c)^(1/2))+1/4*Pi^(1/2)*exp(1/4*I*(4*a*c+1)/c)/(-I*c)^(1/2)*erf((-I*c)^(1/2)*x-1/2/(-I*c)^(1/2))`

maxima [A] time = 0.34, size = 100, normalized size = 0.87

$$\frac{\sqrt{2} \sqrt{\pi} \left((i-1) \cos\left(\frac{4ac+1}{4c}\right) + (i+1) \sin\left(\frac{4ac+1}{4c}\right) \right) \operatorname{erf}\left(\frac{2icx-1}{2\sqrt{ic}}\right) + \left((i+1) \cos\left(\frac{4ac+1}{4c}\right) + (i-1) \sin\left(\frac{4ac+1}{4c}\right) \right) \operatorname{erf}\left(\frac{2icx+1}{2\sqrt{-ic}}\right)}{8\sqrt{c}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(exp(x)*cos(c*x^2+a),x, algorithm="maxima")`

[Out] `-1/8*sqrt(2)*sqrt(pi)*(((I - 1)*cos(1/4*(4*a*c + 1)/c) + (I + 1)*sin(1/4*(4*a*c + 1)/c))*erf(1/2*(2*I*c*x - 1)/sqrt(I*c)) + ((I + 1)*cos(1/4*(4*a*c + 1)/c) + (I - 1)*sin(1/4*(4*a*c + 1)/c))*erf(1/2*(2*I*c*x + 1)/sqrt(-I*c)))/sqrt(c)`

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int e^x \cos(cx^2 + a) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(exp(x)*cos(a + c*x^2),x)`

[Out] `int(exp(x)*cos(a + c*x^2), x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int e^x \cos(a + cx^2) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(exp(x)*cos(c*x**2+a),x)`

[Out] `Integral(exp(x)*cos(a + c*x**2), x)`

3.106 $\int e^x \cos(a + bx + cx^2) dx$

Optimal. Leaf size=144

$$\frac{\sqrt[4]{-1} \sqrt{\pi} e^{\frac{i(b+i)^2}{4c} - ia} \operatorname{erfi}\left(\frac{\sqrt[4]{-1}(-ib-2icx+1)}{2\sqrt{c}}\right)}{4\sqrt{c}} - \frac{\sqrt[4]{-1} \sqrt{\pi} e^{\frac{1}{4}i\left(4a + \frac{(1+ib)^2}{c}\right)} \operatorname{erf}\left(\frac{\sqrt[4]{-1}(ib+2icx+1)}{2\sqrt{c}}\right)}{4\sqrt{c}}$$

[Out] $-1/4*(-1)^{(1/4)}*\exp(1/4*I*(4*a+(1+I*b)^2/c))*\operatorname{erf}(1/2*(-1)^{(1/4)}*(1+I*b+2*I*c*x)/c^{(1/2)})*\operatorname{Pi}^{(1/2)}/c^{(1/2)}+1/4*(-1)^{(1/4)}*\exp(-I*a+1/4*I*(I+b)^2/c)*\operatorname{erfi}(1/2*(-1)^{(1/4)}*(1-I*b-2*I*c*x)/c^{(1/2)})*\operatorname{Pi}^{(1/2)}/c^{(1/2)}$

Rubi [A] time = 0.17, antiderivative size = 144, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 4, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.267$, Rules used = {4473, 2234, 2204, 2205}

$$\frac{\sqrt[4]{-1} \sqrt{\pi} e^{\frac{i(b+i)^2}{4c} - ia} \operatorname{Erfi}\left(\frac{\sqrt[4]{-1}(-ib-2icx+1)}{2\sqrt{c}}\right)}{4\sqrt{c}} - \frac{\sqrt[4]{-1} \sqrt{\pi} e^{\frac{1}{4}i\left(4a + \frac{(1+ib)^2}{c}\right)} \operatorname{Erf}\left(\frac{\sqrt[4]{-1}(ib+2icx+1)}{2\sqrt{c}}\right)}{4\sqrt{c}}$$

Antiderivative was successfully verified.

[In] `Int[E^x*Cos[a + b*x + c*x^2], x]`

[Out] $-((-1)^{(1/4)}*E^{((I/4)*(4*a + (1 + I*b)^2/c))*\operatorname{Sqrt}[\operatorname{Pi}]*\operatorname{Erf}[((-1)^{(1/4)}*(1 + I*b + (2*I)*c*x))/(2*\operatorname{Sqrt}[c])]}]/(4*\operatorname{Sqrt}[c]) + ((-1)^{(1/4)}*E^{((-I)*a + ((I/4)*(I + b)^2)/c))*\operatorname{Sqrt}[\operatorname{Pi}]*\operatorname{Erfi}[((-1)^{(1/4)}*(1 - I*b - (2*I)*c*x))/(2*\operatorname{Sqrt}[c])]}]/(4*\operatorname{Sqrt}[c])$

Rule 2204

`Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_)) ^2), x_Symbol] := Simp[(F^a*Sqrt[Pi]*Erfi[(c + d*x)*Rt[b*Log[F], 2]]]/(2*d*Rt[b*Log[F], 2]), x] /; FreeQ[{F, a, b, c, d}, x] && PosQ[b]`

Rule 2205

`Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_)) ^2), x_Symbol] := Simp[(F^a*Sqrt[Pi]*Erf[(c + d*x)*Rt[-(b*Log[F]), 2]]]/(2*d*Rt[-(b*Log[F]), 2]), x] /; FreeQ[{F, a, b, c, d}, x] && NegQ[b]`

Rule 2234

`Int[(F_)^((a_.) + (b_.)*(x_) + (c_.)*(x_) ^2), x_Symbol] := Dist[F^(a - b^2/(4*c)), Int[F^((b + 2*c*x)^2/(4*c)), x], x] /; FreeQ[{F, a, b, c}, x]`

Rule 4473

`Int[Cos[v_]^(n_.)*(F_)^(u_), x_Symbol] := Int[ExpandTrigToExp[F^u, Cos[v]^n, x], x] /; FreeQ[F, x] && (LinearQ[u, x] || PolyQ[u, x, 2]) && (LinearQ[v, x] || PolyQ[v, x, 2]) && IGtQ[n, 0]`

Rubi steps

$$\begin{aligned}
\int e^x \cos(a + bx + cx^2) dx &= \int \left(\frac{1}{2} e^{-ia+(1-ib)x-icx^2} + \frac{1}{2} e^{ia+(1+ib)x+icx^2} \right) dx \\
&= \frac{1}{2} \int e^{-ia+(1-ib)x-icx^2} dx + \frac{1}{2} \int e^{ia+(1+ib)x+icx^2} dx \\
&= \frac{1}{2} e^{\frac{1}{4}i \left(4a + \frac{(1+ib)^2}{c} \right)} \int e^{-\frac{i(1+ib+2icx)^2}{4c}} dx + \frac{1}{2} e^{-\frac{i(1-2ib-b^2+4ac)}{4c}} \int e^{\frac{i(1-ib-2icx)^2}{4c}} dx \\
&= \frac{\sqrt[4]{-1} e^{\frac{1}{4}i \left(4a + \frac{(1+ib)^2}{c} \right)} \sqrt{\pi} \operatorname{erf} \left(\frac{\sqrt[4]{-1} (1+ib+2icx)}{2\sqrt{c}} \right)}{4\sqrt{c}} + \frac{\sqrt[4]{-1} e^{-\frac{i(1-2ib-b^2+4ac)}{4c}} \sqrt{\pi} \operatorname{erfi} \left(\frac{\sqrt[4]{-1} (1-ib-2icx)}{2\sqrt{c}} \right)}{4\sqrt{c}}
\end{aligned}$$

Mathematica [A] time = 0.26, size = 135, normalized size = 0.94

$$\frac{\sqrt[4]{-1} \sqrt{\pi} e^{-\frac{i(b^2-2ib+1)}{4c}} \left(e^{\frac{i}{2c}} (\sin(a) - i \cos(a)) \operatorname{erfi} \left(\frac{\sqrt[4]{-1} (b+2cx-i)}{2\sqrt{c}} \right) - e^{\frac{ib^2}{2c}} (\cos(a) - i \sin(a)) \operatorname{erfi} \left(\frac{(-1)^{3/4} (b+2cx+i)}{2\sqrt{c}} \right) \right)}{4\sqrt{c}}$$

Antiderivative was successfully verified.

[In] Integrate[E^x*Cos[a + b*x + c*x^2],x]

[Out] $((-1)^{1/4} \sqrt{\pi} * (-E^{((I/2)*b^2)/c} * \operatorname{Erfi} [((-1)^{3/4} * (I + b + 2*c*x)) / (2*\sqrt{c})] * (\cos[a] - I*\sin[a])) + E^{(I/2)/c} * \operatorname{Erfi} [((-1)^{1/4} * (-I + b + 2*c*x)) / (2*\sqrt{c})] * ((-I)*\cos[a] + \sin[a])) / (4*\sqrt{c} * E^{((I/4)*(1 - (2*I)*b + b^2))/c})$

fricas [B] time = 2.07, size = 229, normalized size = 1.59

$$\frac{\sqrt{2} \pi \sqrt{\frac{c}{\pi}} e^{\left(\frac{ib^2-4iac-2b-i}{4c} \right)} C \left(\frac{\sqrt{2} (2cx+b+i) \sqrt{\frac{c}{\pi}}}{2c} \right) - \sqrt{2} \pi \sqrt{\frac{c}{\pi}} e^{\left(\frac{-ib^2+4iac-2b+i}{4c} \right)} C \left(-\frac{\sqrt{2} (2cx+b-i) \sqrt{\frac{c}{\pi}}}{2c} \right) - i \sqrt{2} \pi \sqrt{\frac{c}{\pi}} e^{\left(\frac{ib^2-4iac-2b-i}{4c} \right)}}{4c}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(x)*cos(c*x^2+b*x+a),x, algorithm="fricas")

[Out] $1/4*(\sqrt{2}*\pi*\sqrt{c/\pi})*e^{(1/4*(I*b^2 - 4*I*a*c - 2*b - I)/c)}*\operatorname{fresnel_cos}(1/2*\sqrt{2}*(2*c*x + b + I)*\sqrt{c/\pi}/c) - \sqrt{2}*\pi*\sqrt{c/\pi}*e^{(1/4*(-I*b^2 + 4*I*a*c - 2*b + I)/c)}*\operatorname{fresnel_cos}(-1/2*\sqrt{2}*(2*c*x + b - I)*\sqrt{c/\pi}/c) - I*\sqrt{2}*\pi*\sqrt{c/\pi}*e^{(1/4*(I*b^2 - 4*I*a*c - 2*b - I)/c)}*\operatorname{fresnel_sin}(1/2*\sqrt{2}*(2*c*x + b + I)*\sqrt{c/\pi}/c) - I*\sqrt{2}*\pi*\sqrt{c/\pi}*e^{(1/4*(-I*b^2 + 4*I*a*c - 2*b + I)/c)}*\operatorname{fresnel_sin}(-1/2*\sqrt{2}*(2*c*x + b - I)*\sqrt{c/\pi}/c)/c$

giac [A] time = 0.18, size = 147, normalized size = 1.02

$$\frac{\sqrt{2} \sqrt{\pi} \operatorname{erf} \left(-\frac{1}{4} \sqrt{2} \left(2x + \frac{b-i}{c} \right) \left(-\frac{ic}{|c|} + 1 \right) \sqrt{|c|} \right) e^{\left(-\frac{ib^2-4iac+2b-i}{4c} \right)}}{4 \left(-\frac{ic}{|c|} + 1 \right) \sqrt{|c|}} - \frac{\sqrt{2} \sqrt{\pi} \operatorname{erf} \left(-\frac{1}{4} \sqrt{2} \left(2x + \frac{b+i}{c} \right) \left(\frac{ic}{|c|} + 1 \right) \sqrt{|c|} \right) e^{\left(-\frac{ib^2-4iac+2b+i}{4c} \right)}}{4 \left(\frac{ic}{|c|} + 1 \right) \sqrt{|c|}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(x)*cos(c*x^2+b*x+a),x, algorithm="giac")

[Out] $-1/4*\sqrt{2}*\sqrt{\pi}*\operatorname{erf}(-1/4*\sqrt{2}*(2*x + (b - I)/c)*(-I*c/abs(c) + 1)*\sqrt{abs(c)})*e^{(-1/4*(I*b^2 - 4*I*a*c + 2*b - I)/c)}/((-I*c/abs(c) + 1)*\sqrt{abs(c)})$

$t(\text{abs}(c)) - 1/4*\text{sqrt}(2)*\text{sqrt}(\text{pi})*\text{erf}(-1/4*\text{sqrt}(2)*(2*x + (b + I)/c)*(I*c/\text{abs}(c) + 1)*\text{sqrt}(\text{abs}(c)))*e^{(-1/4*(-I*b^2 + 4*I*a*c + 2*b + I)/c)/((I*c/\text{abs}(c) + 1)*\text{sqrt}(\text{abs}(c)))}$

maple [A] time = 0.13, size = 117, normalized size = 0.81

$$\frac{\sqrt{\pi} e^{-\frac{i(4ac-b^2-2ib+1)}{4c}} \operatorname{erf}\left(\sqrt{ic} x - \frac{-ib+1}{2\sqrt{ic}}\right)}{4\sqrt{ic}} - \frac{\sqrt{\pi} e^{\frac{i(4ac-b^2+2ib+1)}{4c}} \operatorname{erf}\left(-\sqrt{-ic} x + \frac{ib+1}{2\sqrt{-ic}}\right)}{4\sqrt{-ic}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(exp(x)*cos(c*x^2+b*x+a), x)`

[Out] $1/4*\text{Pi}^{(1/2)}*\text{exp}(-1/4*I*(-b^2-2*I*b+4*a*c+1)/c)/(I*c)^{(1/2)}*\text{erf}((I*c)^{(1/2)}*x-1/2*(-I*b+1)/(I*c)^{(1/2)})-1/4*\text{Pi}^{(1/2)}*\text{exp}(1/4*I*(-b^2+2*I*b+4*a*c+1)/c)/(-I*c)^{(1/2)}*\text{erf}(-(-I*c)^{(1/2)}*x+1/2*(1+I*b)/(-I*c)^{(1/2)})$

maxima [A] time = 0.35, size = 131, normalized size = 0.91

$$\frac{\sqrt{2} \sqrt{\pi} \left(\left(-(i-1) \cos\left(-\frac{b^2-4ac-1}{4c}\right) - (i+1) \sin\left(-\frac{b^2-4ac-1}{4c}\right) \right) \operatorname{erf}\left(\frac{i(2icx+ib-1)\sqrt{ic}}{2c}\right) + \left((i+1) \cos\left(-\frac{b^2-4ac-1}{4c}\right) - (i-1) \sin\left(-\frac{b^2-4ac-1}{4c}\right) \right) \operatorname{erf}\left(\frac{i(2icx+ib+1)\sqrt{-ic}}{2c}\right) \right)}{8\sqrt{c}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(exp(x)*cos(c*x^2+b*x+a), x, algorithm="maxima")`

[Out] $-1/8*\text{sqrt}(2)*\text{sqrt}(\text{pi})*\left(\left(-\left(I-1\right)*\cos\left(-1/4*\left(b^2-4*a*c-1\right)/c\right)-\left(I+1\right)*\sin\left(-1/4*\left(b^2-4*a*c-1\right)/c\right)\right)*\text{erf}\left(1/2*I*\left(2*I*c*x+I*b-1\right)*\text{sqrt}\left(I*c\right)/c\right)+\left(\left(I+1\right)*\cos\left(-1/4*\left(b^2-4*a*c-1\right)/c\right)+\left(I-1\right)*\sin\left(-1/4*\left(b^2-4*a*c-1\right)/c\right)\right)*\text{erf}\left(1/2*I*\left(2*I*c*x+I*b+1\right)*\text{sqrt}\left(-I*c\right)/c\right)*e^{(-1/2*b/c)/\text{sqrt}(c)}$

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int e^x \cos(cx^2 + bx + a) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(exp(x)*cos(a + b*x + c*x^2), x)`

[Out] `int(exp(x)*cos(a + b*x + c*x^2), x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int e^x \cos(a + bx + cx^2) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(exp(x)*cos(c*x**2+b*x+a), x)`

[Out] `Integral(exp(x)*cos(a + b*x + c*x**2), x)`

3.107 $\int e^{x^2} \cos(a + bx) dx$

Optimal. Leaf size=77

$$\frac{1}{4}\sqrt{\pi}e^{\frac{b^2}{4}-ia}\operatorname{erfi}\left(\frac{1}{2}(2x-ib)\right)+\frac{1}{4}\sqrt{\pi}e^{\frac{b^2}{4}+ia}\operatorname{erfi}\left(\frac{1}{2}(2x+ib)\right)$$

[Out] $-1/4*\exp(-I*a+1/4*b^2)*\operatorname{erfi}(1/2*I*b-x)*\operatorname{Pi}^{(1/2)}+1/4*\exp(I*a+1/4*b^2)*\operatorname{erfi}(1/2*I*b+x)*\operatorname{Pi}^{(1/2)}$

Rubi [A] time = 0.06, antiderivative size = 77, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 3, integrand size = 12, $\frac{\text{number of rules}}{\text{integrand size}} = 0.250$, Rules used = {4473, 2234, 2204}

$$\frac{1}{4}\sqrt{\pi}e^{\frac{b^2}{4}-ia}\operatorname{Erfi}\left(\frac{1}{2}(2x-ib)\right)+\frac{1}{4}\sqrt{\pi}e^{\frac{b^2}{4}+ia}\operatorname{Erfi}\left(\frac{1}{2}(2x+ib)\right)$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[E^{x^2}*\operatorname{Cos}[a + b*x], x]$

[Out] $(E^{((-I)*a + b^2/4)*\operatorname{Sqrt}[\operatorname{Pi}]}*\operatorname{Erfi}[((-I)*b + 2*x)/2])/4 + (E^{(I*a + b^2/4)*\operatorname{Sqrt}[\operatorname{Pi}]}*\operatorname{Erfi}[(I*b + 2*x)/2])/4$

Rule 2204

$\operatorname{Int}[(F_)^{((a_.) + (b_.)*((c_.) + (d_.)*(x_))^{2})}, x_Symbol] \rightarrow \operatorname{Simp}[(F^a*\operatorname{Sqrt}[\operatorname{Pi}]*\operatorname{Erfi}[(c + d*x)*\operatorname{Rt}[b*\operatorname{Log}[F], 2]])/(2*d*\operatorname{Rt}[b*\operatorname{Log}[F], 2]), x] /; \operatorname{FreeQ}\{F, a, b, c, d\}, x] \&\& \operatorname{PosQ}[b]$

Rule 2234

$\operatorname{Int}[(F_)^{((a_.) + (b_.)*(x_) + (c_.)*(x_)^2)}, x_Symbol] \rightarrow \operatorname{Dist}[F^{(a - b^2/(4*c))}, \operatorname{Int}[F^{((b + 2*c*x)^2/(4*c))}, x], x] /; \operatorname{FreeQ}\{F, a, b, c\}, x]$

Rule 4473

$\operatorname{Int}[\operatorname{Cos}[v_]^{(n_.)}*(F_)^{(u_)}, x_Symbol] \rightarrow \operatorname{Int}[\operatorname{ExpandTrigToExp}[F^u, \operatorname{Cos}[v]^{(n)}, x], x] /; \operatorname{FreeQ}[F, x] \&\& (\operatorname{LinearQ}[u, x] \mid\mid \operatorname{PolyQ}[u, x, 2]) \&\& (\operatorname{LinearQ}[v, x] \mid\mid \operatorname{PolyQ}[v, x, 2]) \&\& \operatorname{IGtQ}[n, 0]$

Rubi steps

$$\begin{aligned} \int e^{x^2} \cos(a + bx) dx &= \int \left(\frac{1}{2}e^{-ia-ibx+x^2} + \frac{1}{2}e^{ia+ibx+x^2} \right) dx \\ &= \frac{1}{2} \int e^{-ia-ibx+x^2} dx + \frac{1}{2} \int e^{ia+ibx+x^2} dx \\ &= \frac{1}{2}e^{-ia+\frac{b^2}{4}} \int e^{\frac{1}{4}(-ib+2x)^2} dx + \frac{1}{2}e^{ia+\frac{b^2}{4}} \int e^{\frac{1}{4}(ib+2x)^2} dx \\ &= \frac{1}{4}e^{-ia+\frac{b^2}{4}}\sqrt{\pi}\operatorname{erfi}\left(\frac{1}{2}(-ib+2x)\right) + \frac{1}{4}e^{ia+\frac{b^2}{4}}\sqrt{\pi}\operatorname{erfi}\left(\frac{1}{2}(ib+2x)\right) \end{aligned}$$

Mathematica [A] time = 0.08, size = 82, normalized size = 1.06

$$\frac{1}{4}\sqrt{\pi}e^{\frac{b^2}{4}}\left(-\sin(a)\left(\operatorname{erf}\left(\frac{b}{2}-ix\right)+\operatorname{erf}\left(\frac{b}{2}+ix\right)\right)+\cos(a)\operatorname{erfi}\left(\frac{1}{2}(2x-ib)\right)+\cos(a)\operatorname{erfi}\left(\frac{1}{2}(2x+ib)\right)\right)$$

Antiderivative was successfully verified.

[In] Integrate[E^x^2*Cos[a + b*x], x]

[Out] (E^(b^2/4)*Sqrt[Pi]*(Cos[a]*Erfi[((-I)*b + 2*x)/2] + Cos[a]*Erfi[(I*b + 2*x)/2] - (Erf[b/2 - I*x] + Erf[b/2 + I*x])*Sin[a])/4

fricas [A] time = 1.69, size = 46, normalized size = 0.60

$$\frac{1}{4} \sqrt{\pi} \left(-i \operatorname{erf} \left(-\frac{1}{2} b + i x \right) e^{\left(\frac{1}{4} b^2 + i a \right)} - i \operatorname{erf} \left(\frac{1}{2} b + i x \right) e^{\left(\frac{1}{4} b^2 - i a \right)} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(x^2)*cos(b*x+a), x, algorithm="fricas")

[Out] 1/4*sqrt(pi)*(-I*erf(-1/2*b + I*x)*e^(1/4*b^2 + I*a) - I*erf(1/2*b + I*x)*e^(1/4*b^2 - I*a))

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \cos(bx + a) e^{x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(x^2)*cos(b*x+a), x, algorithm="giac")

[Out] integrate(cos(b*x + a)*e^(x^2), x)

maple [A] time = 0.04, size = 54, normalized size = 0.70

$$-\frac{i\sqrt{\pi} e^{\frac{b^2}{4}} e^{-ia} \operatorname{erf} \left(ix + \frac{b}{2} \right)}{4} + \frac{i\sqrt{\pi} e^{\frac{b^2}{4}} e^{ia} \operatorname{erf} \left(-ix + \frac{b}{2} \right)}{4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(exp(x^2)*cos(b*x+a), x)

[Out] -1/4*I*Pi^(1/2)*exp(1/4*b^2)*exp(-I*a)*erf(I*x+1/2*b)+1/4*I*Pi^(1/2)*exp(1/4*b^2)*exp(I*a)*erf(-I*x+1/2*b)

maxima [A] time = 0.33, size = 52, normalized size = 0.68

$$-\frac{1}{4} \sqrt{\pi} \left((i \cos(a) + \sin(a)) \operatorname{erf} \left(\frac{1}{2} b + i x \right) e^{\left(\frac{1}{4} b^2 \right)} + (i \cos(a) - \sin(a)) \operatorname{erf} \left(-\frac{1}{2} b + i x \right) e^{\left(\frac{1}{4} b^2 \right)} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(x^2)*cos(b*x+a), x, algorithm="maxima")

[Out] -1/4*sqrt(pi)*((I*cos(a) + sin(a))*erf(1/2*b + I*x)*e^(1/4*b^2) + (I*cos(a) - sin(a))*erf(-1/2*b + I*x)*e^(1/4*b^2))

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \cos(a + bx) e^{x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(cos(a + b*x)*exp(x^2), x)

[Out] int(cos(a + b*x)*exp(x^2), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int e^{x^2} \cos(a + bx) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(x**2)*cos(b*x+a), x)

[Out] Integral(exp(x**2)*cos(a + b*x), x)

3.108 $\int e^{x^2} \cos(a + cx^2) dx$

Optimal. Leaf size=83

$$\frac{\sqrt{\pi} e^{-ia} \operatorname{erfi}(\sqrt{1-ic} x)}{4\sqrt{1-ic}} + \frac{\sqrt{\pi} e^{ia} \operatorname{erfi}(\sqrt{1+ic} x)}{4\sqrt{1+ic}}$$

[Out] $1/4*\operatorname{erfi}(x*(1-I*c)^{(1/2)})*Pi^{(1/2)}/\exp(I*a)/(1-I*c)^{(1/2)}+1/4*\exp(I*a)*\operatorname{erfi}(x*(1+I*c)^{(1/2)})*Pi^{(1/2)}/(1+I*c)^{(1/2)}$

Rubi [A] time = 0.08, antiderivative size = 83, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 2, integrand size = 14, $\frac{\text{number of rules}}{\text{integrand size}} = 0.143$, Rules used = {4473, 2204}

$$\frac{\sqrt{\pi} e^{-ia} \operatorname{Erfi}(\sqrt{1-ic} x)}{4\sqrt{1-ic}} + \frac{\sqrt{\pi} e^{ia} \operatorname{Erfi}(\sqrt{1+ic} x)}{4\sqrt{1+ic}}$$

Antiderivative was successfully verified.

[In] Int[E^x^2*Cos[a + c*x^2],x]

[Out] (Sqrt[Pi]*Erfi[Sqrt[1 - I*c]*x])/(4*Sqrt[1 - I*c]*E^(I*a)) + (E^(I*a)*Sqrt[Pi]*Erfi[Sqrt[1 + I*c]*x])/(4*Sqrt[1 + I*c])

Rule 2204

Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))²), x_Symbol] :> Simp[(F^a*Sqrt[Pi]*Erfi[(c + d*x)*Rt[b*Log[F], 2]])/(2*d*Rt[b*Log[F], 2]), x] /; FreeQ[{F, a, b, c, d}, x] && PosQ[b]

Rule 4473

Int[Cos[v_]^(n_.)*(F_)^(u_), x_Symbol] :> Int[ExpandTrigToExp[F^u, Cos[v]^n, x], x] /; FreeQ[F, x] && (LinearQ[u, x] || PolyQ[u, x, 2]) && (LinearQ[v, x] || PolyQ[v, x, 2]) && IGtQ[n, 0]

Rubi steps

$$\begin{aligned} \int e^{x^2} \cos(a + cx^2) dx &= \int \left(\frac{1}{2} e^{-ia+(1-ic)x^2} + \frac{1}{2} e^{ia+(1+ic)x^2} \right) dx \\ &= \frac{1}{2} \int e^{-ia+(1-ic)x^2} dx + \frac{1}{2} \int e^{ia+(1+ic)x^2} dx \\ &= \frac{e^{-ia} \sqrt{\pi} \operatorname{erfi}(\sqrt{1-ic} x)}{4\sqrt{1-ic}} + \frac{e^{ia} \sqrt{\pi} \operatorname{erfi}(\sqrt{1+ic} x)}{4\sqrt{1+ic}} \end{aligned}$$

Mathematica [A] time = 0.20, size = 107, normalized size = 1.29

$$\frac{\sqrt[4]{-1} \sqrt{\pi} \left((1-ic)\sqrt{c-i}(\cos(a) + i\sin(a))\operatorname{erfi}(\sqrt[4]{-1}\sqrt{c-i}x) - (c-i)\sqrt{c+i}(\cos(a) - i\sin(a))\operatorname{erfi}((-1)^{3/4}\sqrt{c+i}x) \right)}{4(c^2+1)}$$

Antiderivative was successfully verified.

[In] Integrate[E^x^2*Cos[a + c*x^2],x]

[Out] $((-1)^{1/4} \sqrt{\pi} * (-(-I + c) \sqrt{I + c} \operatorname{Erfi}[(-1)^{3/4} \sqrt{I + c} x] * (\cos[a] - I \sin[a])) + (1 - I c) \sqrt{-I + c} \operatorname{Erfi}[(-1)^{1/4} \sqrt{-I + c} x] * (\cos[a] + I \sin[a])) / (4 * (1 + c^2))$

fricas [A] time = 0.90, size = 70, normalized size = 0.84

$$\frac{\sqrt{\pi} (ic - 1) \sqrt{-ic - 1} \operatorname{erf}(\sqrt{-ic - 1} x) e^{ia} + \sqrt{\pi} \sqrt{ic - 1} (-ic - 1) \operatorname{erf}(\sqrt{ic - 1} x) e^{-ia}}{4(c^2 + 1)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(exp(x^2)*cos(c*x^2+a),x, algorithm="fricas")`

[Out] $1/4 * (\sqrt{\pi} * (I * c - 1) * \sqrt{-I * c - 1} * \operatorname{erf}(\sqrt{-I * c - 1} * x) * e^{I * a} + \sqrt{\pi} * \sqrt{I * c - 1} * (-I * c - 1) * \operatorname{erf}(\sqrt{I * c - 1} * x) * e^{-I * a}) / (c^2 + 1)$

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \cos(cx^2 + a) e^{x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(exp(x^2)*cos(c*x^2+a),x, algorithm="giac")`

[Out] `integrate(cos(c*x^2 + a)*e^(x^2), x)`

maple [A] time = 0.10, size = 60, normalized size = 0.72

$$\frac{\sqrt{\pi} e^{-ia} \operatorname{erf}(\sqrt{ic - 1} x)}{4\sqrt{ic - 1}} + \frac{\sqrt{\pi} e^{ia} \operatorname{erf}(\sqrt{-ic - 1} x)}{4\sqrt{-ic - 1}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(exp(x^2)*cos(c*x^2+a),x)`

[Out] $1/4 * \pi^{1/2} * \exp(-I * a) / (-1 + I * c)^{1/2} * \operatorname{erf}((-1 + I * c)^{1/2} * x) + 1/4 * \pi^{1/2} * \exp(I * a) / (-I * c - 1)^{1/2} * \operatorname{erf}((-I * c - 1)^{1/2} * x)$

maxima [B] time = 0.32, size = 133, normalized size = 1.60

$$\frac{\sqrt{\pi} \sqrt{2c^2 + 2} ((i \cos(a) + \sin(a)) \operatorname{erf}(\sqrt{ic - 1} x) + (-i \cos(a) + \sin(a)) \operatorname{erf}(\sqrt{-ic - 1} x)) \sqrt{\sqrt{c^2 + 1} + 1} - \sqrt{\pi}}{8(c^2 + 1)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(exp(x^2)*cos(c*x^2+a),x, algorithm="maxima")`

[Out] $-1/8 * (\sqrt{\pi} * \sqrt{2 * c^2 + 2} * ((I * \cos(a) + \sin(a)) * \operatorname{erf}(\sqrt{I * c - 1} * x) + (-I * \cos(a) + \sin(a)) * \operatorname{erf}(\sqrt{-I * c - 1} * x)) * \sqrt{(\sqrt{c^2 + 1} + 1)} - \sqrt{\pi} * \sqrt{2 * c^2 + 2} * ((\cos(a) - I * \sin(a)) * \operatorname{erf}(\sqrt{I * c - 1} * x) + (\cos(a) + I * \sin(a)) * \operatorname{erf}(\sqrt{-I * c - 1} * x)) * \sqrt{(\sqrt{c^2 + 1} - 1)}) / (c^2 + 1)$

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int e^{x^2} \cos(cx^2 + a) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(exp(x^2)*cos(a + c*x^2),x)`

```
[Out] int(exp(x^2)*cos(a + c*x^2), x)
```

```
sympy [F] time = 0.00, size = 0, normalized size = 0.00
```

$$\int e^{x^2} \cos(a + cx^2) dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(x**2)*cos(c*x**2+a), x)
```

```
[Out] Integral(exp(x**2)*cos(a + c*x**2), x)
```

3.109 $\int e^{x^2} \cos(a + bx + cx^2) dx$

Optimal. Leaf size=151

$$\frac{\sqrt{\pi} e^{ia + \frac{b^2}{4(1+ic)}} \operatorname{erfi}\left(\frac{ib+2(1+ic)x}{2\sqrt{1+ic}}\right)}{4\sqrt{1+ic}} - \frac{\sqrt{\pi} e^{-i\left(a - \frac{b^2}{4c+4i}\right)} \operatorname{erfi}\left(\frac{ib-2(1-ic)x}{2\sqrt{1-ic}}\right)}{4\sqrt{1-ic}}$$

[Out] $-1/4*\operatorname{erfi}(1/2*(I*b-2*(1-I*c)*x)/(1-I*c)^{(1/2)})*\operatorname{Pi}^{(1/2)}/\exp(I*(a-b^2/(4*I+4*c)))/(1-I*c)^{(1/2)}+1/4*\exp(I*a+1/4*b^2/(1+I*c))*\operatorname{erfi}(1/2*(I*b+2*(1+I*c)*x)/(1+I*c)^{(1/2)})*\operatorname{Pi}^{(1/2)}/(1+I*c)^{(1/2)}$

Rubi [A] time = 0.17, antiderivative size = 151, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 3, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.176$, Rules used = {4473, 2234, 2204}

$$\frac{\sqrt{\pi} e^{ia + \frac{b^2}{4(1+ic)}} \operatorname{Erfi}\left(\frac{ib+2(1+ic)x}{2\sqrt{1+ic}}\right)}{4\sqrt{1+ic}} - \frac{\sqrt{\pi} e^{-i\left(a - \frac{b^2}{4c+4i}\right)} \operatorname{Erfi}\left(\frac{ib-2(1-ic)x}{2\sqrt{1-ic}}\right)}{4\sqrt{1-ic}}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[E^{x^2} \operatorname{Cos}[a + b*x + c*x^2], x]$

[Out] $-(\operatorname{Sqrt}[\operatorname{Pi}]*\operatorname{Erfi}[(I*b - 2*(1 - I*c)*x)/(2*\operatorname{Sqrt}[1 - I*c]])/(4*\operatorname{Sqrt}[1 - I*c]*E^{(I*(a - b^2/(4*I + 4*c)))}) + (E^{(I*a + b^2/(4*(1 + I*c)))})*\operatorname{Sqrt}[\operatorname{Pi}]*\operatorname{Erfi}[(I*b + 2*(1 + I*c)*x)/(2*\operatorname{Sqrt}[1 + I*c]])/(4*\operatorname{Sqrt}[1 + I*c])$

Rule 2204

$\operatorname{Int}[(F_)^{((a_.) + (b_.)*((c_.) + (d_.)*(x_))^{2})}, x_Symbol] \rightarrow \operatorname{Simp}[(F^a*\operatorname{Sqrt}[\operatorname{Pi}]*\operatorname{Erfi}[(c + d*x)*\operatorname{Rt}[b*\operatorname{Log}[F], 2]])/(2*d*\operatorname{Rt}[b*\operatorname{Log}[F], 2]), x] /; \operatorname{FreeQ}\{F, a, b, c, d\}, x] \&\& \operatorname{PosQ}[b]$

Rule 2234

$\operatorname{Int}[(F_)^{((a_.) + (b_.)*(x_) + (c_.)*(x_)^2)}, x_Symbol] \rightarrow \operatorname{Dist}[F^{(a - b^2/(4*c))}, \operatorname{Int}[F^{((b + 2*c*x)^2/(4*c))}, x], x] /; \operatorname{FreeQ}\{F, a, b, c\}, x]$

Rule 4473

$\operatorname{Int}[\operatorname{Cos}[v_]^{(n_.)}*(F_)^{(u_)}, x_Symbol] \rightarrow \operatorname{Int}[\operatorname{ExpandTrigToExp}[F^u, \operatorname{Cos}[v]^{(n)}, x], x] /; \operatorname{FreeQ}[F, x] \&\& (\operatorname{LinearQ}[u, x] \parallel \operatorname{PolyQ}[u, x, 2]) \&\& (\operatorname{LinearQ}[v, x] \parallel \operatorname{PolyQ}[v, x, 2]) \&\& \operatorname{IGtQ}[n, 0]$

Rubi steps

$$\begin{aligned} \int e^{x^2} \cos(a + bx + cx^2) dx &= \int \left(\frac{1}{2} e^{-ia - ibx + (1-ic)x^2} + \frac{1}{2} e^{ia + ibx + (1+ic)x^2} \right) dx \\ &= \frac{1}{2} \int e^{-ia - ibx + (1-ic)x^2} dx + \frac{1}{2} \int e^{ia + ibx + (1+ic)x^2} dx \\ &= \frac{1}{2} e^{ia + \frac{b^2}{4(1+ic)}} \int \exp\left(\frac{(ib + 2(1+ic)x)^2}{4(1+ic)}\right) dx + \frac{1}{2} e^{-i\left(a - \frac{b^2}{4i+4c}\right)} \int \exp\left(\frac{(-ib + 2(1-ic)x)^2}{4(1-ic)}\right) dx \\ &= -\frac{e^{-i\left(a - \frac{b^2}{4i+4c}\right)} \sqrt{\pi} \operatorname{erfi}\left(\frac{ib-2(1-ic)x}{2\sqrt{1-ic}}\right)}{4\sqrt{1-ic}} + \frac{e^{ia + \frac{b^2}{4(1+ic)}} \sqrt{\pi} \operatorname{erfi}\left(\frac{ib+2(1+ic)x}{2\sqrt{1+ic}}\right)}{4\sqrt{1+ic}} \end{aligned}$$

Mathematica [A] time = 0.60, size = 166, normalized size = 1.10

$$\frac{\sqrt[4]{-1} \sqrt{\pi} e^{-\frac{ib^2}{4c+4i}} \left(\sqrt{c-i}(c+i)(\sin(a) - i \cos(a)) \operatorname{erfi} \left(\frac{\sqrt[4]{-1}(b+2(c-i)x)}{2\sqrt{c-i}} \right) - (c-i)\sqrt{c+i} e^{\frac{ib^2c}{2c^2+2}} (\cos(a) - i \sin(a)) \operatorname{erfi} \left(\frac{\sqrt[4]{-1}(b+2(c-i)x)}{2\sqrt{c-i}} \right) \right)}{4(c^2+1)}$$

Antiderivative was successfully verified.

[In] Integrate[E^x^2*Cos[a + b*x + c*x^2], x]

[Out] $((-1)^{(1/4)} * E^{((I*b^2)/(4*I - 4*c))} * \operatorname{Sqrt}[Pi] * (-((-I + c) * \operatorname{Sqrt}[I + c] * E^{((I*b^2*c)/(2 + 2*c^2))} * \operatorname{Erfi}[((-1)^{(3/4)} * (b + 2*(I + c)*x)) / (2 * \operatorname{Sqrt}[I + c])] * (\operatorname{Cos}[a] - I * \operatorname{Sin}[a])) + \operatorname{Sqrt}[-I + c] * (I + c) * \operatorname{Erfi}[((-1)^{(1/4)} * (b + 2*(-I + c)*x)) / (2 * \operatorname{Sqrt}[-I + c])] * ((-I) * \operatorname{Cos}[a] + \operatorname{Sin}[a])))) / (4 * (1 + c^2))$

fricas [A] time = 1.85, size = 164, normalized size = 1.09

$$\frac{\sqrt{\pi} (ic + 1) \sqrt{ic - 1} \operatorname{erf} \left(-\frac{(bc+2(c^2+1)x-ib)\sqrt{ic-1}}{2(c^2+1)} \right) e^{\left(\frac{ib^2c-4iac^2+b^2-4ia}{4(c^2+1)} \right)} + \sqrt{\pi} (ic - 1) \sqrt{-ic - 1} \operatorname{erf} \left(\frac{(bc+2(c^2+1)x+ib)\sqrt{-ic-1}}{2(c^2+1)} \right)}{4(c^2+1)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(x^2)*cos(c*x^2+b*x+a), x, algorithm="fricas")

[Out] $1/4 * (\operatorname{sqrt}(\pi) * (I*c + 1) * \operatorname{sqrt}(I*c - 1) * \operatorname{erf}(-1/2 * (b*c + 2*(c^2 + 1)*x - I*b) * \operatorname{sqrt}(I*c - 1) / (c^2 + 1)) * e^{(1/4 * (I*b^2*c - 4*I*a*c^2 + b^2 - 4*I*a) / (c^2 + 1))} + \operatorname{sqrt}(\pi) * (I*c - 1) * \operatorname{sqrt}(-I*c - 1) * \operatorname{erf}(1/2 * (b*c + 2*(c^2 + 1)*x + I*b) * \operatorname{sqrt}(-I*c - 1) / (c^2 + 1)) * e^{(1/4 * (-I*b^2*c + 4*I*a*c^2 + b^2 + 4*I*a) / (c^2 + 1))}) / (c^2 + 1)$

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \cos(cx^2 + bx + a) e^{(x^2)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(x^2)*cos(c*x^2+b*x+a), x, algorithm="giac")

[Out] integrate(cos(c*x^2 + b*x + a)*e^(x^2), x)

maple [A] time = 0.12, size = 127, normalized size = 0.84

$$\frac{\sqrt{\pi} e^{\frac{4ac+4ia-b^2}{4ic-4}} \operatorname{erf} \left(\sqrt{ic-1} x + \frac{ib}{2\sqrt{ic-1}} \right)}{4\sqrt{ic-1}} - \frac{\sqrt{\pi} e^{-\frac{4ac-4ia-b^2}{4(ic+1)}} \operatorname{erf} \left(-\sqrt{-ic-1} x + \frac{ib}{2\sqrt{-ic-1}} \right)}{4\sqrt{-ic-1}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(exp(x^2)*cos(c*x^2+b*x+a), x)

[Out] $1/4 * \operatorname{Pi}^{(1/2)} * \exp(1/4 * (4*a*c + 4*I*a - b^2) / (-1 + I*c)) / (-1 + I*c)^{(1/2)} * \operatorname{erf}((-1 + I*c)^{(1/2)} * x + 1/2 * I*b / (-1 + I*c)^{(1/2)}) - 1/4 * \operatorname{Pi}^{(1/2)} * \exp(-1/4 * (4*a*c - 4*I*a - b^2) / (1 + I*c)) / (-I*c - 1)^{(1/2)} * \operatorname{erf}(-(-I*c - 1)^{(1/2)} * x + 1/2 * I*b / (-I*c - 1)^{(1/2)})$

maxima [B] time = 0.34, size = 474, normalized size = 3.14

$$\sqrt{\pi} \sqrt{2c^2 + 2} \left(\left(-i \cos \left(-\frac{b^2c - 4ac^2 - 4a}{4(c^2+1)} \right) e^{\left(\frac{b^2}{4(c^2+1)} \right)} - e^{\left(\frac{b^2}{4(c^2+1)} \right)} \sin \left(-\frac{b^2c - 4ac^2 - 4a}{4(c^2+1)} \right) \right) \operatorname{erf} \left(-\frac{2(-ic+1)x-ib}{2\sqrt{ic-1}} \right) + \left(-i \cos \left(-\frac{b^2c - 4ac^2 - 4a}{4(c^2+1)} \right) e^{\left(\frac{b^2}{4(c^2+1)} \right)} - e^{\left(\frac{b^2}{4(c^2+1)} \right)} \sin \left(-\frac{b^2c - 4ac^2 - 4a}{4(c^2+1)} \right) \right) \operatorname{erf} \left(-\frac{2(-ic+1)x-ib}{2\sqrt{ic-1}} \right) \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(x^2)*cos(c*x^2+b*x+a),x, algorithm="maxima")

[Out] $\frac{1}{8}(\sqrt{\pi})\sqrt{2c^2 + 2}((-I\cos(-\frac{1}{4}(b^2c - 4ac^2 - 4a)/(c^2 + 1))e^{\frac{1}{4}b^2/(c^2 + 1)} - e^{\frac{1}{4}b^2/(c^2 + 1)})\sin(-\frac{1}{4}(b^2c - 4ac^2 - 4a)/(c^2 + 1))\operatorname{erf}(-\frac{1}{2}(2(-Ic + 1)x - Ib)/\sqrt{Ic - 1}) + (-I\cos(-\frac{1}{4}(b^2c - 4ac^2 - 4a)/(c^2 + 1))e^{\frac{1}{4}b^2/(c^2 + 1)} + e^{\frac{1}{4}b^2/(c^2 + 1)})\sin(-\frac{1}{4}(b^2c - 4ac^2 - 4a)/(c^2 + 1))\operatorname{erf}(-\frac{1}{2}(2(-Ic - 1)x - Ib)/\sqrt{-Ic - 1}))\sqrt{(\sqrt{c^2 + 1} + 1) + \sqrt{\pi})}\sqrt{2c^2 + 2}((\cos(-\frac{1}{4}(b^2c - 4ac^2 - 4a)/(c^2 + 1))e^{\frac{1}{4}b^2/(c^2 + 1)} - Ie^{\frac{1}{4}b^2/(c^2 + 1)})\sin(-\frac{1}{4}(b^2c - 4ac^2 - 4a)/(c^2 + 1))\operatorname{erf}(-\frac{1}{2}(2(-Ic + 1)x - Ib)/\sqrt{Ic - 1}) - (\cos(-\frac{1}{4}(b^2c - 4ac^2 - 4a)/(c^2 + 1))e^{\frac{1}{4}b^2/(c^2 + 1)} + Ie^{\frac{1}{4}b^2/(c^2 + 1)})\sin(-\frac{1}{4}(b^2c - 4ac^2 - 4a)/(c^2 + 1))\operatorname{erf}(-\frac{1}{2}(2(-Ic - 1)x - Ib)/\sqrt{-Ic - 1}))\sqrt{(\sqrt{c^2 + 1} - 1)})/(c^2 + 1)$

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int e^{x^2} \cos(cx^2 + bx + a) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(exp(x^2)*cos(a + b*x + c*x^2),x)

[Out] int(exp(x^2)*cos(a + b*x + c*x^2), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int e^{x^2} \cos(a + bx + cx^2) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(x**2)*cos(c*x**2+b*x+a),x)

[Out] Integral(exp(x**2)*cos(a + b*x + c*x**2), x)

3.110 $\int f^{a+bx} \cos(d + fx^2) dx$

Optimal. Leaf size=142

$$-\frac{1}{4}\sqrt[4]{-1}\sqrt{\pi}f^{a-\frac{1}{2}}e^{\frac{1}{4}i\left(\frac{b^2\log^2(f)}{f}+4d\right)}\operatorname{erf}\left(\frac{\sqrt[4]{-1}(b\log(f)+2ifx)}{2\sqrt{f}}\right)-\frac{1}{4}\sqrt[4]{-1}\sqrt{\pi}f^{a-\frac{1}{2}}e^{-\frac{1}{4}i\left(\frac{b^2\log^2(f)}{f}+4d\right)}\operatorname{erfi}\left(\frac{\sqrt[4]{-1}(-b\log(f)+2ifx)}{2\sqrt{f}}\right)$$

[Out] $-1/4*(-1)^{(1/4)}*\exp(1/4*I*(4*d+b^2*\ln(f)^2/f))*f^{(-1/2+a)}*\operatorname{erf}(1/2*(-1)^{(1/4)}*(2*I*f*x+b*\ln(f))/f^{(1/2)})*\operatorname{Pi}^{(1/2)}-1/4*(-1)^{(1/4)}*f^{(-1/2+a)}*\operatorname{erfi}(1/2*(-1)^{(1/4)}*(2*I*f*x-b*\ln(f))/f^{(1/2)})*\operatorname{Pi}^{(1/2)}/\exp(1/4*I*(4*d+b^2*\ln(f)^2/f))$

Rubi [A] time = 0.17, antiderivative size = 142, normalized size of antiderivative = 1.00, number of steps used = 8, number of rules used = 5, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} = 0.312$, Rules used = {4473, 2287, 2234, 2204, 2205}

$$-\frac{1}{4}\sqrt[4]{-1}\sqrt{\pi}f^{a-\frac{1}{2}}e^{\frac{1}{4}i\left(\frac{b^2\log^2(f)}{f}+4d\right)}\operatorname{Erf}\left(\frac{\sqrt[4]{-1}(b\log(f)+2ifx)}{2\sqrt{f}}\right)-\frac{1}{4}\sqrt[4]{-1}\sqrt{\pi}f^{a-\frac{1}{2}}e^{-\frac{1}{4}i\left(\frac{b^2\log^2(f)}{f}+4d\right)}\operatorname{Erfi}\left(\frac{\sqrt[4]{-1}(-b\log(f)+2ifx)}{2\sqrt{f}}\right)$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[f^{(a + b*x)}*\operatorname{Cos}[d + f*x^2], x]$

[Out] $-((-1)^{(1/4)}*E^{((I/4)*(4*d + (b^2*\operatorname{Log}[f]^2)/f))}*f^{(-1/2 + a)}*\operatorname{Sqrt}[\operatorname{Pi}]*\operatorname{Erf}[((-1)^{(1/4)}*((2*I)*f*x + b*\operatorname{Log}[f]))/(2*\operatorname{Sqrt}[f])])/4 - ((-1)^{(1/4)}*f^{(-1/2 + a)}*\operatorname{Sqrt}[\operatorname{Pi}]*\operatorname{Erfi}[((-1)^{(1/4)}*((2*I)*f*x - b*\operatorname{Log}[f]))/(2*\operatorname{Sqrt}[f])])/(4*E^{((I/4)*(4*d + (b^2*\operatorname{Log}[f]^2)/f))})$

Rule 2204

$\operatorname{Int}[(F_)^{((a_.) + (b_.)*((c_.) + (d_.)*(x_))^2)}, x_Symbol] \rightarrow \operatorname{Simp}[(F^a*\operatorname{Sqrt}[\operatorname{Pi}]*\operatorname{Erfi}[(c + d*x)*\operatorname{Rt}[b*\operatorname{Log}[F], 2]])/(2*d*\operatorname{Rt}[b*\operatorname{Log}[F], 2]), x] /;$ $\operatorname{FreeQ}\{F, a, b, c, d, x\} \ \&\& \ \operatorname{PosQ}[b]$

Rule 2205

$\operatorname{Int}[(F_)^{((a_.) + (b_.)*((c_.) + (d_.)*(x_))^2)}, x_Symbol] \rightarrow \operatorname{Simp}[(F^a*\operatorname{Sqrt}[\operatorname{Pi}]*\operatorname{Erf}[(c + d*x)*\operatorname{Rt}[-(b*\operatorname{Log}[F]), 2]])/(2*d*\operatorname{Rt}[-(b*\operatorname{Log}[F]), 2]), x] /;$ $\operatorname{FreeQ}\{F, a, b, c, d, x\} \ \&\& \ \operatorname{NegQ}[b]$

Rule 2234

$\operatorname{Int}[(F_)^{((a_.) + (b_.)*(x_) + (c_.)*(x_)^2)}, x_Symbol] \rightarrow \operatorname{Dist}[F^{(a - b^2/(4*c))}, \operatorname{Int}[F^{((b + 2*c*x)^2/(4*c))}, x], x] /;$ $\operatorname{FreeQ}\{F, a, b, c, x\}$

Rule 2287

$\operatorname{Int}[(u_)*(F_)^{(v_)}*(G_)^{(w_)}, x_Symbol] \rightarrow \operatorname{With}\{z = v*\operatorname{Log}[F] + w*\operatorname{Log}[G]\}, \operatorname{Int}[u*\operatorname{NormalizeIntegrand}[E^z, x], x] /;$ $\operatorname{BinomialQ}[z, x] \ \|\ \operatorname{PolynomialQ}[z, x] \ \&\& \ \operatorname{LeQ}[\operatorname{Exponent}[z, x], 2]] /;$ $\operatorname{FreeQ}\{F, G, x\}$

Rule 4473

$\operatorname{Int}[\operatorname{Cos}[v_]^{(n_.)}*(F_)^{(u_)}, x_Symbol] \rightarrow \operatorname{Int}[\operatorname{ExpandTrigToExp}[F^u, \operatorname{Cos}[v]^n], x] /;$ $\operatorname{FreeQ}[F, x] \ \&\& \ (\operatorname{LinearQ}[u, x] \ \|\ \operatorname{PolyQ}[u, x, 2]) \ \&\& \ (\operatorname{LinearQ}[v, x] \ \|\ \operatorname{PolyQ}[v, x, 2]) \ \&\& \ \operatorname{IGtQ}[n, 0]$

Rubi steps

$$\begin{aligned}
\int f^{a+bx} \cos(d + fx^2) dx &= \int \left(\frac{1}{2} e^{-id-ifx^2} f^{a+bx} + \frac{1}{2} e^{id+ifx^2} f^{a+bx} \right) dx \\
&= \frac{1}{2} \int e^{-id-ifx^2} f^{a+bx} dx + \frac{1}{2} \int e^{id+ifx^2} f^{a+bx} dx \\
&= \frac{1}{2} \int e^{-id-ifx^2+a \log(f)+bx \log(f)} dx + \frac{1}{2} \int e^{id+ifx^2+a \log(f)+bx \log(f)} dx \\
&= \frac{1}{2} \left(e^{-\frac{1}{4}i \left(4d + \frac{b^2 \log^2(f)}{f} \right)} f^a \right) \int e^{\frac{i(-2ifx+b \log(f))^2}{4f}} dx + \frac{1}{2} \left(e^{\frac{1}{4}i \left(4d + \frac{b^2 \log^2(f)}{f} \right)} f^a \right) \int e^{\frac{i(2ifx+b \log(f))^2}{4f}} dx \\
&= -\frac{1}{4} \sqrt[4]{-1} e^{\frac{1}{4}i \left(4d + \frac{b^2 \log^2(f)}{f} \right)} f^{-\frac{1}{2}+a} \sqrt{\pi} \operatorname{erf} \left(\frac{\sqrt[4]{-1} (2ifx + b \log(f))}{2\sqrt{f}} \right) - \frac{1}{4} \sqrt[4]{-1} e^{-\frac{1}{4}i \left(4d + \frac{b^2 \log^2(f)}{f} \right)} f^{-\frac{1}{2}+a} \sqrt{\pi} \operatorname{erf} \left(\frac{\sqrt[4]{-1} (2ifx + b \log(f))}{2\sqrt{f}} \right)
\end{aligned}$$

Mathematica [A] time = 0.23, size = 133, normalized size = 0.94

$$\frac{1}{4} \sqrt[4]{-1} \sqrt{\pi} f^{a-\frac{1}{2}} e^{-\frac{ib^2 \log^2(f)}{4f}} \left(e^{\frac{ib^2 \log^2(f)}{2f}} (\sin(d) - i \cos(d)) \operatorname{erfi} \left(\frac{\sqrt[4]{-1} (2fx - ib \log(f))}{2\sqrt{f}} \right) - (\cos(d) - i \sin(d)) \operatorname{erfi} \left(\frac{(-1)^{3/4} (2fx + ib \log(f))}{2\sqrt{f}} \right) \right)$$

Antiderivative was successfully verified.

[In] Integrate[f^(a + b*x)*Cos[d + f*x^2],x]

[Out] ((-1)^(1/4)*f^(-1/2 + a)*Sqrt[Pi]*(-(Erfi[(((1)^(3/4)*(2*f*x + I*b*Log[f]))/(2*Sqrt[f]))*(Cos[d] - I*Sin[d])) + E^(((I/2)*b^2*Log[f]^2)/f)*Erfi[(((1)^(1/4)*(2*f*x - I*b*Log[f]))/(2*Sqrt[f]))*((-I)*Cos[d] + Sin[d]))]/(4*E^(((I/4)*b^2*Log[f]^2)/f))

fricas [B] time = 0.69, size = 265, normalized size = 1.87

$$\sqrt{2} \pi \sqrt{\frac{f}{\pi}} e^{\left(\frac{-ib^2 \log(f)^2 + 4af \log(f) - 4idf}{4f} \right)} C \left(\frac{\sqrt{2}(2fx + ib \log(f)) \sqrt{\frac{f}{\pi}}}{2f} \right) - \sqrt{2} \pi \sqrt{\frac{f}{\pi}} e^{\left(\frac{ib^2 \log(f)^2 + 4af \log(f) + 4idf}{4f} \right)} C \left(-\frac{\sqrt{2}(2fx - ib \log(f)) \sqrt{\frac{f}{\pi}}}{2f} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(b*x+a)*cos(f*x^2+d),x, algorithm="fricas")

[Out] 1/4*(sqrt(2)*pi*sqrt(f/pi)*e^(1/4*(-I*b^2*log(f)^2 + 4*a*f*log(f) - 4*I*d*f)/f)*fresnel_cos(1/2*sqrt(2)*(2*f*x + I*b*log(f))*sqrt(f/pi)/f) - sqrt(2)*pi*sqrt(f/pi)*e^(1/4*(I*b^2*log(f)^2 + 4*a*f*log(f) + 4*I*d*f)/f)*fresnel_cos(-1/2*sqrt(2)*(2*f*x - I*b*log(f))*sqrt(f/pi)/f) - I*sqrt(2)*pi*sqrt(f/pi)*e^(1/4*(-I*b^2*log(f)^2 + 4*a*f*log(f) - 4*I*d*f)/f)*fresnel_sin(1/2*sqrt(2)*(2*f*x + I*b*log(f))*sqrt(f/pi)/f) - I*sqrt(2)*pi*sqrt(f/pi)*e^(1/4*(I*b^2*log(f)^2 + 4*a*f*log(f) + 4*I*d*f)/f)*fresnel_sin(-1/2*sqrt(2)*(2*f*x - I*b*log(f))*sqrt(f/pi)/f)/f

giac [B] time = 0.26, size = 300, normalized size = 2.11

$$\frac{\sqrt{2} \sqrt{\pi} \operatorname{erf} \left(-\frac{1}{8} \sqrt{2} \left(4x - \frac{\pi b \operatorname{sgn}(f) - \pi b + 2ib \log(|f|)}{f} \right) \left(-\frac{if}{|f|} + 1 \right) \sqrt{|f|} \right) e^{\left(\frac{i\pi^2 b^2 \operatorname{sgn}(f)}{8f} + \frac{\pi b^2 \log(|f|) \operatorname{sgn}(f)}{4f} - \frac{i\pi^2 b^2}{8f} - \frac{\pi b^2 \log(|f|)}{4f} + \frac{ib^2 \log(|f|)}{4f} \right)}}{4 \left(-\frac{if}{|f|} + 1 \right) \sqrt{|f|}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(b*x+a)*cos(f*x^2+d),x, algorithm="giac")

```
[Out] -1/4*sqrt(2)*sqrt(pi)*erf(-1/8*sqrt(2)*(4*x - (pi*b*sgn(f) - pi*b + 2*I*b*log(abs(f))))/f)*(-I*f/abs(f) + 1)*sqrt(abs(f))*e^(1/8*I*pi^2*b^2*sgn(f)/f + 1/4*pi*b^2*log(abs(f))*sgn(f)/f - 1/8*I*pi^2*b^2/f - 1/4*pi*b^2*log(abs(f))/f + 1/4*I*b^2*log(abs(f))^2/f - 1/2*I*pi*a*sgn(f) + 1/2*I*pi*a + a*log(abs(f)) + I*d)/((-I*f/abs(f) + 1)*sqrt(abs(f))) - 1/4*sqrt(2)*sqrt(pi)*erf(-1/8*sqrt(2)*(4*x + (pi*b*sgn(f) - pi*b + 2*I*b*log(abs(f))))/f)*(I*f/abs(f) + 1)*sqrt(abs(f))*e^(-1/8*I*pi^2*b^2*sgn(f)/f - 1/4*pi*b^2*log(abs(f))*sgn(f)/f + 1/8*I*pi^2*b^2/f + 1/4*pi*b^2*log(abs(f))/f - 1/4*I*b^2*log(abs(f))^2/f - 1/2*I*pi*a*sgn(f) + 1/2*I*pi*a + a*log(abs(f)) - I*d)/((I*f/abs(f) + 1)*sqrt(abs(f)))
```

maple [A] time = 0.17, size = 114, normalized size = 0.80

$$\frac{\sqrt{\pi} f^a e^{-\frac{i(\ln(f)^2 b^2 + 4df)}{4f}} \operatorname{erf}\left(-\sqrt{if} x + \frac{\ln(f)b}{2\sqrt{if}}\right)}{4\sqrt{if}} - \frac{\sqrt{\pi} f^a e^{\frac{i(\ln(f)^2 b^2 + 4df)}{4f}} \operatorname{erf}\left(-\sqrt{-if} x + \frac{\ln(f)b}{2\sqrt{-if}}\right)}{4\sqrt{-if}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(f^(b*x+a)*cos(f*x^2+d), x)
```

```
[Out] -1/4*Pi^(1/2)*f^a*exp(-1/4*I*(ln(f)^2*b^2+4*d*f)/f)/(I*f)^(1/2)*erf(-(I*f)^(1/2)*x+1/2*ln(f)*b/(I*f)^(1/2))-1/4*Pi^(1/2)*f^a*exp(1/4*I*(ln(f)^2*b^2+4*d*f)/f)/(-I*f)^(1/2)*erf(-(-I*f)^(1/2)*x+1/2*ln(f)*b/(-I*f)^(1/2))
```

maxima [A] time = 0.34, size = 147, normalized size = 1.04

$$\frac{\sqrt{2} \sqrt{\pi} \left((i-1) f^a \cos\left(\frac{b^2 \log(f)^2 + 4df}{4f}\right) + (i+1) f^a \sin\left(\frac{b^2 \log(f)^2 + 4df}{4f}\right) \right) \operatorname{erf}\left(\frac{2ifx - b \log(f)}{2\sqrt{if}}\right) + (i+1) f^a \cos\left(\frac{b^2 \log(f)^2 + 4df}{4f}\right)}{8\sqrt{f}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(f^(b*x+a)*cos(f*x^2+d), x, algorithm="maxima")
```

```
[Out] -1/8*sqrt(2)*sqrt(pi)*(((I - 1)*f^a*cos(1/4*(b^2*log(f)^2 + 4*d*f)/f) + (I + 1)*f^a*sin(1/4*(b^2*log(f)^2 + 4*d*f)/f))*erf(1/2*(2*I*f*x - b*log(f))/sqrt(I*f)) + ((I + 1)*f^a*cos(1/4*(b^2*log(f)^2 + 4*d*f)/f) + (I - 1)*f^a*sin(1/4*(b^2*log(f)^2 + 4*d*f)/f))*erf(1/2*(2*I*f*x + b*log(f))/sqrt(-I*f)))/sqrt(f)
```

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int f^{a+bx} \cos(fx^2 + d) dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(f^(a + b*x)*cos(d + f*x^2), x)
```

```
[Out] int(f^(a + b*x)*cos(d + f*x^2), x)
```

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int f^{a+bx} \cos(d + fx^2) dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(f**(b*x+a)*cos(f*x**2+d), x)
```

```
[Out] Integral(f**(a + b*x)*cos(d + f*x**2), x)
```

3.111 $\int f^{a+bx} \cos^2(d + fx^2) dx$

Optimal. Leaf size=157

$$\left(-\frac{1}{16} - \frac{i}{16}\right) \sqrt{\pi} f^{a-\frac{1}{2}} e^{\frac{ib^2 \log^2(f)}{8f} + 2id} \operatorname{erf}\left(\frac{\left(\frac{1}{4} + \frac{i}{4}\right)(b \log(f) + 4ifx)}{\sqrt{f}}\right) - \left(\frac{1}{16} + \frac{i}{16}\right) \sqrt{\pi} f^{a-\frac{1}{2}} e^{-\frac{1}{8}i\left(\frac{b^2 \log^2(f)}{f} + 16d\right)} \operatorname{erfi}\left(\frac{\left(\frac{1}{4} + \frac{i}{4}\right)(b \log(f) + 4ifx)}{\sqrt{f}}\right)$$

[Out] 1/2*f^(b*x+a)/b/ln(f)-(1/16+1/16*I)*exp(2*I*d+1/8*I*b^2*ln(f)^2/f)*f^(-1/2+a)*erf((1/4+1/4*I)*(4*I*f*x+b*ln(f))/f^(1/2))*Pi^(1/2)-(1/16+1/16*I)*f^(-1/2+a)*erfi((1/4+1/4*I)*(4*I*f*x-b*ln(f))/f^(1/2))*Pi^(1/2)/exp(1/8*I*(16*d+b^2*ln(f)^2/f))

Rubi [A] time = 0.17, antiderivative size = 157, normalized size of antiderivative = 1.00, number of steps used = 9, number of rules used = 6, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.333$, Rules used = {4473, 2194, 2287, 2234, 2204, 2205}

$$\left(-\frac{1}{16} - \frac{i}{16}\right) \sqrt{\pi} f^{a-\frac{1}{2}} e^{\frac{ib^2 \log^2(f)}{8f} + 2id} \operatorname{Erf}\left(\frac{\left(\frac{1}{4} + \frac{i}{4}\right)(b \log(f) + 4ifx)}{\sqrt{f}}\right) - \left(\frac{1}{16} + \frac{i}{16}\right) \sqrt{\pi} f^{a-\frac{1}{2}} e^{-\frac{1}{8}i\left(\frac{b^2 \log^2(f)}{f} + 16d\right)} \operatorname{Erfi}\left(\frac{\left(\frac{1}{4} + \frac{i}{4}\right)(b \log(f) + 4ifx)}{\sqrt{f}}\right)$$

Antiderivative was successfully verified.

[In] Int[f^(a + b*x)*Cos[d + f*x^2]^2,x]

[Out] (-1/16 - I/16)*E^((2*I)*d + ((I/8)*b^2*Log[f]^2)/f)*f^(-1/2 + a)*Sqrt[Pi]*Erf[((1/4 + I/4)*((4*I)*f*x + b*Log[f]))/Sqrt[f]] - ((1/16 + I/16)*f^(-1/2 + a)*Sqrt[Pi]*Erfi[((1/4 + I/4)*((4*I)*f*x - b*Log[f]))/Sqrt[f]])/E^((I/8)*(16*d + (b^2*Log[f]^2)/f)) + f^(a + b*x)/(2*b*Log[f])

Rule 2194

Int[((F_)^((c_)*(a_) + (b_)*(x_)))^(n_), x_Symbol] := Simp[(F^(c*(a + b*x)))^n/(b*c*n*Log[F]), x] /; FreeQ[{F, a, b, c, n}, x]

Rule 2204

Int[(F_)^((a_) + (b_)*((c_) + (d_)*(x_)^2)), x_Symbol] := Simp[(F^a*Sqrt[Pi]*Erfi[(c + d*x)*Rt[b*Log[F], 2]])/(2*d*Rt[b*Log[F], 2]), x] /; FreeQ[{F, a, b, c, d}, x] && PosQ[b]

Rule 2205

Int[(F_)^((a_) + (b_)*((c_) + (d_)*(x_)^2)), x_Symbol] := Simp[(F^a*Sqrt[Pi]*Erf[(c + d*x)*Rt[-(b*Log[F]), 2]])/(2*d*Rt[-(b*Log[F]), 2]), x] /; FreeQ[{F, a, b, c, d}, x] && NegQ[b]

Rule 2234

Int[(F_)^((a_) + (b_)*(x_) + (c_)*(x_)^2)), x_Symbol] := Dist[F^(a - b^2/(4*c)), Int[F^((b + 2*c*x)^2/(4*c)), x], x] /; FreeQ[{F, a, b, c}, x]

Rule 2287

Int[(u_)*(F_)^(v_)*(G_)^(w_), x_Symbol] := With[{z = v*Log[F] + w*Log[G]}, Int[u*NormalizeIntegrand[E^z, x], x] /; BinomialQ[z, x] || (PolynomialQ[z, x] && LeQ[Exponent[z, x], 2])] /; FreeQ[{F, G}, x]

Rule 4473

Int[Cos[v_]^(n_)*(F_)^(u_), x_Symbol] := Int[ExpandTrigToExp[F^u, Cos[v]^n, x], x] /; FreeQ[F, x] && (LinearQ[u, x] || PolyQ[u, x, 2]) && (LinearQ[v, x] || PolyQ[v, x, 2]) && IGtQ[n, 0]

Rubi steps

$$\begin{aligned}
 \int f^{a+bx} \cos^2(d + fx^2) dx &= \int \left(\frac{1}{2} f^{a+bx} + \frac{1}{4} e^{-2id-2ifx^2} f^{a+bx} + \frac{1}{4} e^{2id+2ifx^2} f^{a+bx} \right) dx \\
 &= \frac{1}{4} \int e^{-2id-2ifx^2} f^{a+bx} dx + \frac{1}{4} \int e^{2id+2ifx^2} f^{a+bx} dx + \frac{1}{2} \int f^{a+bx} dx \\
 &= \frac{f^{a+bx}}{2b \log(f)} + \frac{1}{4} \int e^{-2id-2ifx^2+a \log(f)+bx \log(f)} dx + \frac{1}{4} \int e^{2id+2ifx^2+a \log(f)+bx \log(f)} dx \\
 &= \frac{f^{a+bx}}{2b \log(f)} + \frac{1}{4} \left(e^{2id+\frac{ib^2 \log^2(f)}{8f}} f^a \right) \int e^{-\frac{i(4ifx+b \log(f))^2}{8f}} dx + \frac{1}{4} \left(e^{-\frac{1}{8}i \left(16d+\frac{b^2 \log^2(f)}{f} \right)} f^a \right) \int e^{\frac{i(4ifx+b \log(f))^2}{8f}} dx \\
 &= \left(-\frac{1}{16} - \frac{i}{16} \right) e^{2id+\frac{ib^2 \log^2(f)}{8f}} f^{-\frac{1}{2}+a} \sqrt{\pi} \operatorname{erf} \left(\frac{\left(\frac{1}{4} + \frac{i}{4} \right) (4ifx + b \log(f))}{\sqrt{f}} \right) - \left(\frac{1}{16} + \frac{i}{16} \right) e^{-2id-\frac{ib^2 \log^2(f)}{8f}} f^{-\frac{1}{2}+a} \sqrt{\pi} \operatorname{erf} \left(\frac{\left(\frac{1}{4} - \frac{i}{4} \right) (4ifx + b \log(f))}{\sqrt{f}} \right)
 \end{aligned}$$

Mathematica [A] time = 1.04, size = 158, normalized size = 1.01

$$\frac{1}{16} f^a \left(\frac{(1-i)\sqrt{\pi} e^{-\frac{ib^2 \log^2(f)}{8f}} (\cos(d) - i \sin(d))^2 \operatorname{erf} \left(\frac{(4+4i)fx - (1-i)b \log(f)}{4\sqrt{f}} \right)}{\sqrt{f}} + \frac{(1+i)\sqrt{\pi} e^{\frac{ib^2 \log^2(f)}{8f}} (\sin(2d) - i \cos(2d))^2 \operatorname{erf} \left(\frac{(4-4i)fx - (1+i)b \log(f)}{4\sqrt{f}} \right)}{\sqrt{f}} \right)$$

Antiderivative was successfully verified.

[In] Integrate[f^(a + b*x)*Cos[d + f*x^2]^2,x]

[Out] (f^a*((8*f^(b*x))/(b*Log[f]) + ((1 - I)*Sqrt[Pi]*Erf[((4 + 4*I)*f*x - (1 - I)*b*Log[f])/(4*Sqrt[f])])*(Cos[d] - I*Sin[d]^2)/(E^(((I/8)*b^2*Log[f]^2)/f)*Sqrt[f]) + ((1 + I)*E^(((I/8)*b^2*Log[f]^2)/f)*Sqrt[Pi]*Erfi[((4 + 4*I)*f*x + (1 - I)*b*Log[f])/(4*Sqrt[f])])*((-I)*Cos[2*d] + Sin[2*d]))/Sqrt[f])/16

fricas [B] time = 0.87, size = 271, normalized size = 1.73

$$\frac{2 \pi b \sqrt{\frac{f}{\pi}} e^{\left(\frac{-ib^2 \log(f)^2 + 8af \log(f) - 16idf}{8f} \right)} C \left(\frac{(4fx + ib \log(f)) \sqrt{\frac{f}{\pi}}}{2f} \right) \log(f) - 2 \pi b \sqrt{\frac{f}{\pi}} e^{\left(\frac{ib^2 \log(f)^2 + 8af \log(f) + 16idf}{8f} \right)} C \left(-\frac{(4fx - ib \log(f)) \sqrt{\frac{f}{\pi}}}{2f} \right)}{16}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(b*x+a)*cos(f*x^2+d)^2,x, algorithm="fricas")

[Out] 1/16*(2*pi*b*sqrt(f/pi)*e^(1/8*(-I*b^2*log(f)^2 + 8*a*f*log(f) - 16*I*d*f)/f)*fresnel_cos(1/2*(4*f*x + I*b*log(f))*sqrt(f/pi)/f)*log(f) - 2*pi*b*sqrt(f/pi)*e^(1/8*(I*b^2*log(f)^2 + 8*a*f*log(f) + 16*I*d*f)/f)*fresnel_cos(-1/2*(4*f*x - I*b*log(f))*sqrt(f/pi)/f)*log(f) - 2*I*pi*b*sqrt(f/pi)*e^(1/8*(-I*b^2*log(f)^2 + 8*a*f*log(f) - 16*I*d*f)/f)*fresnel_sin(1/2*(4*f*x + I*b*log(f))*sqrt(f/pi)/f)*log(f) - 2*I*pi*b*sqrt(f/pi)*e^(1/8*(I*b^2*log(f)^2 + 8*a*f*log(f) + 16*I*d*f)/f)*fresnel_sin(-1/2*(4*f*x - I*b*log(f))*sqrt(f/pi)/f)*log(f) + 8*f*f^(b*x + a))/(b*f*log(f))

giac [B] time = 0.30, size = 521, normalized size = 3.32

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(b*x+a)*cos(f*x^2+d)^2,x, algorithm="giac")

[Out] (2*b*cos(-1/2*pi*b*x*sgn(f) + 1/2*pi*b*x - 1/2*pi*a*sgn(f) + 1/2*pi*a)*log(abs(f))/(4*b^2*log(abs(f))^2 + (pi*b*sgn(f) - pi*b)^2) - (pi*b*sgn(f) - pi*b)*sin(-1/2*pi*b*x*sgn(f) + 1/2*pi*b*x - 1/2*pi*a*sgn(f) + 1/2*pi*a)/(4*b^2*log(abs(f))^2 + (pi*b*sgn(f) - pi*b)^2))*e^(b*x*log(abs(f)) + a*log(abs(f))) - 1/2*I*(-2*I*e^(1/2*I*pi*b*x*sgn(f) - 1/2*I*pi*b*x + 1/2*I*pi*a*sgn(f) - 1/2*I*pi*a)/(2*I*pi*b*sgn(f) - 2*I*pi*b + 4*b*log(abs(f))) + 2*I*e^(-1/2*I*pi*b*x*sgn(f) + 1/2*I*pi*b*x - 1/2*I*pi*a*sgn(f) + 1/2*I*pi*a)/(-2*I*pi*b*sgn(f) + 2*I*pi*b + 4*b*log(abs(f))))*e^(b*x*log(abs(f)) + a*log(abs(f))) - 1/8*sqrt(pi)*erf(-1/8*sqrt(f)*(8*x - (pi*b*sgn(f) - pi*b + 2*I*b*log(abs(f))))/f)*(-I*f/abs(f) + 1))*e^(1/16*I*pi^2*b^2*sgn(f)/f + 1/8*pi*b^2*log(abs(f))*sgn(f)/f - 1/16*I*pi^2*b^2/f - 1/8*pi*b^2*log(abs(f))/f + 1/8*I*b^2*log(abs(f))^2/f - 1/2*I*pi*a*sgn(f) + 1/2*I*pi*a + a*log(abs(f)) + 2*I*d)/(sqrt(f)*(-I*f/abs(f) + 1)) - 1/8*sqrt(pi)*erf(-1/8*sqrt(f)*(8*x + (pi*b*sgn(f) - pi*b + 2*I*b*log(abs(f))))/f)*(I*f/abs(f) + 1))*e^(-1/16*I*pi^2*b^2*sgn(f)/f - 1/8*pi*b^2*log(abs(f))*sgn(f)/f + 1/16*I*pi^2*b^2/f + 1/8*pi*b^2*log(abs(f))/f - 1/8*I*b^2*log(abs(f))^2/f - 1/2*I*pi*a*sgn(f) + 1/2*I*pi*a + a*log(abs(f)) - 2*I*d)/(sqrt(f)*(I*f/abs(f) + 1))

maple [A] time = 0.33, size = 139, normalized size = 0.89

$$\frac{\sqrt{\pi} f^a e^{-\frac{i(\ln(f)^2 b^2 + 16df)}{8f}} \sqrt{2} \operatorname{erf}\left(-\sqrt{2} \sqrt{if} x + \frac{\ln(f)b\sqrt{2}}{4\sqrt{if}}\right)}{16\sqrt{if}} - \frac{\sqrt{\pi} f^a e^{\frac{i(\ln(f)^2 b^2 + 16df)}{8f}} \operatorname{erf}\left(-\sqrt{-2if} x + \frac{\ln(f)b}{2\sqrt{-2if}}\right)}{8\sqrt{-2if}} + \frac{f^{bx+a}}{2b \ln(f)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(f^(b*x+a)*cos(f*x^2+d)^2,x)

[Out] -1/16*Pi^(1/2)*f^a*exp(-1/8*I*(ln(f)^2*b^2+16*d*f)/f)*2^(1/2)/(I*f)^(1/2)*erf(-2^(1/2)*(I*f)^(1/2)*x+1/4*ln(f)*b*2^(1/2)/(I*f)^(1/2))-1/8*Pi^(1/2)*f^a*exp(1/8*I*(ln(f)^2*b^2+16*d*f)/f)/(-2*I*f)^(1/2)*erf(-(-2*I*f)^(1/2)*x+1/2*ln(f)*b/(-2*I*f)^(1/2))+1/2*f^(b*x+a)/b/ln(f)

maxima [A] time = 0.44, size = 186, normalized size = 1.18

$$\frac{4^{\frac{1}{4}} \sqrt{2} \sqrt{\pi} \left((i-1) b f^a \cos\left(\frac{b^2 \log(f)^2 + 16df}{8f}\right) \log(f) + (i+1) b f^a \log(f) \sin\left(\frac{b^2 \log(f)^2 + 16df}{8f}\right) \right) \operatorname{erf}\left(\frac{4i f x - b \log(f)}{2\sqrt{2if}}\right) + \dots}{32 b f^a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(b*x+a)*cos(f*x^2+d)^2,x, algorithm="maxima")

[Out] -1/32*(4^(1/4)*sqrt(2)*sqrt(pi)*(((I - 1)*b*f^a*cos(1/8*(b^2*log(f)^2 + 16*d*f)/f)*log(f) + (I + 1)*b*f^a*log(f)*sin(1/8*(b^2*log(f)^2 + 16*d*f)/f))*erf(1/2*(4*I*f*x - b*log(f))/sqrt(2*I*f)) + ((I + 1)*b*f^a*cos(1/8*(b^2*log(f)^2 + 16*d*f)/f)*log(f) + (I - 1)*b*f^a*log(f)*sin(1/8*(b^2*log(f)^2 + 16*d*f)/f))*erf(1/2*(4*I*f*x + b*log(f))/sqrt(-2*I*f)))*f^(3/2) - 16*f^(b*x)*f^(a + 2)/(b*f^2*log(f))

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int f^{a+bx} \cos(fx^2 + d)^2 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(f^(a + b*x)*cos(d + f*x^2)^2,x)`

[Out] `int(f^(a + b*x)*cos(d + f*x^2)^2, x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int f^{a+bx} \cos^2(d + fx^2) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(f**(b*x+a)*cos(f*x**2+d)**2,x)`

[Out] `Integral(f**(a + b*x)*cos(d + f*x**2)**2, x)`

3.112 $\int f^{a+bx} \cos^3(d + fx^2) dx$

Optimal. Leaf size=298

$$-\frac{3}{16} \sqrt[4]{-1} \sqrt{\pi} f^{a-\frac{1}{2}} e^{\frac{1}{4}i\left(\frac{b^2 \log^2(f)}{f} + 4d\right)} \operatorname{erf}\left(\frac{\sqrt[4]{-1}(b \log(f) + 2ifx)}{2\sqrt{f}}\right) - \left(\frac{1}{16} + \frac{i}{16}\right) \sqrt{\frac{\pi}{6}} f^{a-\frac{1}{2}} e^{\frac{ib^2 \log^2(f)}{12f} + 3id} \operatorname{erf}\left(\frac{\left(\frac{1}{2} + \frac{i}{2}\right)(b \log(f) + 2ifx)}{\sqrt{6}}\right)$$

[Out] $(-1/96 - 1/96*I) * \exp(3*I*d + 1/12*I*b^2*\ln(f)^2/f) * f^{(-1/2+a)} * \operatorname{erf}\left(\frac{(1/12 + 1/12*I)*(6*I*f*x + b*\ln(f)) * 6^{(1/2)}/f^{(1/2)}}{2\sqrt{f}}\right) - (1/96 + 1/96*I) * f^{(-1/2+a)} * \operatorname{erfi}\left(\frac{(1/12 + 1/12*I)*(6*I*f*x - b*\ln(f)) * 6^{(1/2)}/f^{(1/2)}}{2\sqrt{f}}\right) / \exp(1/12*I*(36*d + b^2*\ln(f)^2/f)) - 3/16 * (-1)^{(1/4)} * \exp(1/4*I*(4*d + b^2*\ln(f)^2/f)) * f^{(-1/2+a)} * \operatorname{erf}\left(\frac{1/2*(-1)^{(1/4)}*(2*I*f*x + b*\ln(f))}{2\sqrt{f}}\right) * \operatorname{erfi}\left(\frac{1/2*(-1)^{(1/4)}*(2*I*f*x - b*\ln(f))}{2\sqrt{f}}\right) - 3/16 * (-1)^{(1/4)} * f^{(-1/2+a)} * \operatorname{erfi}\left(\frac{1/2*(-1)^{(1/4)}*(2*I*f*x - b*\ln(f))}{2\sqrt{f}}\right) * \operatorname{erf}\left(\frac{1/2*(-1)^{(1/4)}*(2*I*f*x + b*\ln(f))}{2\sqrt{f}}\right) / \exp(1/4*I*(4*d + b^2*\ln(f)^2/f))$

Rubi [A] time = 0.33, antiderivative size = 298, normalized size of antiderivative = 1.00, number of steps used = 14, number of rules used = 5, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.278$, Rules used = {4473, 2287, 2234, 2204, 2205}

$$-\frac{3}{16} \sqrt[4]{-1} \sqrt{\pi} f^{a-\frac{1}{2}} e^{\frac{1}{4}i\left(\frac{b^2 \log^2(f)}{f} + 4d\right)} \operatorname{Erf}\left(\frac{\sqrt[4]{-1}(b \log(f) + 2ifx)}{2\sqrt{f}}\right) - \left(\frac{1}{16} + \frac{i}{16}\right) \sqrt{\frac{\pi}{6}} f^{a-\frac{1}{2}} e^{\frac{ib^2 \log^2(f)}{12f} + 3id} \operatorname{Erf}\left(\frac{\left(\frac{1}{2} + \frac{i}{2}\right)(b \log(f) + 2ifx)}{\sqrt{6}}\right)$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[f^{(a + b*x)} * \operatorname{Cos}[d + f*x^2]^3, x]$

[Out] $(-3*(-1)^{(1/4)} * E^{((I/4)*(4*d + (b^2*\operatorname{Log}[f]^2)/f))} * f^{(-1/2 + a)} * \operatorname{Sqrt}[\operatorname{Pi}] * \operatorname{Erf}\left[\frac{((-1)^{(1/4)}*((2*I)*f*x + b*\operatorname{Log}[f]))}{(2*\operatorname{Sqrt}[f])}\right]) / 16 - (1/16 + I/16) * E^{((3*I)*d + ((I/12)*b^2*\operatorname{Log}[f]^2)/f)} * f^{(-1/2 + a)} * \operatorname{Sqrt}[\operatorname{Pi}/6] * \operatorname{Erf}\left[\frac{((1/2 + I/2)*(6*I)*f*x + b*\operatorname{Log}[f])}{(\operatorname{Sqrt}[6]*\operatorname{Sqrt}[f])}\right] - (3*(-1)^{(1/4)} * f^{(-1/2 + a)} * \operatorname{Sqrt}[\operatorname{Pi}] * \operatorname{Erfi}\left[\frac{((-1)^{(1/4)}*((2*I)*f*x - b*\operatorname{Log}[f]))}{(2*\operatorname{Sqrt}[f])}\right]) / (16 * E^{((I/4)*(4*d + (b^2*\operatorname{Log}[f]^2)/f))}) - ((1/16 + I/16) * f^{(-1/2 + a)} * \operatorname{Sqrt}[\operatorname{Pi}/6] * \operatorname{Erfi}\left[\frac{((1/2 + I/2)*((6*I)*f*x - b*\operatorname{Log}[f]))}{(\operatorname{Sqrt}[6]*\operatorname{Sqrt}[f])}\right]) / E^{((I/12)*(36*d + (b^2*\operatorname{Log}[f]^2)/f))})$

Rule 2204

$\operatorname{Int}[(F_)^{((a_.) + (b_.)*((c_.) + (d_.)*(x_.))^2)}, x_Symbol] \rightarrow \operatorname{Simp}[(F^a * \operatorname{Sqrt}[\operatorname{Pi}] * \operatorname{Erfi}[(c + d*x) * \operatorname{Rt}[b*\operatorname{Log}[F], 2]]) / (2*d*\operatorname{Rt}[b*\operatorname{Log}[F], 2]), x] /; \operatorname{FreeQ}\{F, a, b, c, d\}, x] \&\& \operatorname{PosQ}[b]$

Rule 2205

$\operatorname{Int}[(F_)^{((a_.) + (b_.)*((c_.) + (d_.)*(x_.))^2)}, x_Symbol] \rightarrow \operatorname{Simp}[(F^a * \operatorname{Sqrt}[\operatorname{Pi}] * \operatorname{Erf}[(c + d*x) * \operatorname{Rt}[-(b*\operatorname{Log}[F]), 2]]) / (2*d*\operatorname{Rt}[-(b*\operatorname{Log}[F]), 2]), x] /; \operatorname{FreeQ}\{F, a, b, c, d\}, x] \&\& \operatorname{NegQ}[b]$

Rule 2234

$\operatorname{Int}[(F_)^{((a_.) + (b_.)*(x_.) + (c_.)*(x_.)^2)}, x_Symbol] \rightarrow \operatorname{Dist}[F^{(a - b^2/(4*c))}, \operatorname{Int}[F^{((b + 2*c*x)^2/(4*c))}, x], x] /; \operatorname{FreeQ}\{F, a, b, c\}, x]$

Rule 2287

$\operatorname{Int}[(u_.)*(F_)^{(v_.)*(G_)^{(w_.)}}, x_Symbol] \rightarrow \operatorname{With}\{z = v*\operatorname{Log}[F] + w*\operatorname{Log}[G]\}, \operatorname{Int}[u*\operatorname{NormalizeIntegrand}[E^z, x], x] /; \operatorname{BinomialQ}[z, x] \|\| (\operatorname{PolynomialQ}[z, x] \&\& \operatorname{LeQ}[\operatorname{Exponent}[z, x], 2]) /; \operatorname{FreeQ}\{F, G\}, x]$


```
log(f)^2 + 12*a*f*log(f) - 36*I*d*f)/f)*fresnel_sin(1/6*sqrt(6)*(6*f*x + I*
b*log(f))*sqrt(f/pi)/f) - I*sqrt(6)*pi*sqrt(f/pi)*e^(1/12*(I*b^2*log(f)^2 +
12*a*f*log(f) + 36*I*d*f)/f)*fresnel_sin(-1/6*sqrt(6)*(6*f*x - I*b*log(f))
*sqrt(f/pi)/f) - 9*I*sqrt(2)*pi*sqrt(f/pi)*e^(1/4*(-I*b^2*log(f)^2 + 4*a*f*
log(f) - 4*I*d*f)/f)*fresnel_sin(1/2*sqrt(2)*(2*f*x + I*b*log(f))*sqrt(f/pi
)/f) - 9*I*sqrt(2)*pi*sqrt(f/pi)*e^(1/4*(I*b^2*log(f)^2 + 4*a*f*log(f) + 4*
I*d*f)/f)*fresnel_sin(-1/2*sqrt(2)*(2*f*x - I*b*log(f))*sqrt(f/pi)/f))/f
```

giac [B] time = 0.40, size = 595, normalized size = 2.00

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(b*x+a)*cos(f*x^2+d)^3,x, algorithm="giac")

```
[Out] -3/16*sqrt(2)*sqrt(pi)*erf(-1/8*sqrt(2)*(4*x - (pi*b*sgn(f) - pi*b + 2*I*b*
log(abs(f))))/f)*(-I*f/abs(f) + 1)*sqrt(abs(f)))*e^(1/8*I*pi^2*b^2*sgn(f)/f
+ 1/4*pi*b^2*log(abs(f))*sgn(f)/f - 1/8*I*pi^2*b^2/f - 1/4*pi*b^2*log(abs(f)
))/f + 1/4*I*b^2*log(abs(f))^2/f - 1/2*I*pi*a*sgn(f) + 1/2*I*pi*a + a*log(a
bs(f)) + I*d)/((-I*f/abs(f) + 1)*sqrt(abs(f))) - 1/48*sqrt(6)*sqrt(pi)*erf(
-1/24*sqrt(6)*sqrt(f)*(12*x - (pi*b*sgn(f) - pi*b + 2*I*b*log(abs(f))))/f)*(-
I*f/abs(f) + 1))*e^(1/24*I*pi^2*b^2*sgn(f)/f + 1/12*pi*b^2*log(abs(f))*sgn
(f)/f - 1/24*I*pi^2*b^2/f - 1/12*pi*b^2*log(abs(f))/f + 1/12*I*b^2*log(abs(
f))^2/f - 1/2*I*pi*a*sgn(f) + 1/2*I*pi*a + a*log(abs(f)) + 3*I*d)/(sqrt(f)*
(-I*f/abs(f) + 1)) - 1/48*sqrt(6)*sqrt(pi)*erf(-1/24*sqrt(6)*sqrt(f)*(12*x
+ (pi*b*sgn(f) - pi*b + 2*I*b*log(abs(f))))/f)*(I*f/abs(f) + 1))*e^(-1/24*I*
pi^2*b^2*sgn(f)/f - 1/12*pi*b^2*log(abs(f))*sgn(f)/f + 1/24*I*pi^2*b^2/f +
1/12*pi*b^2*log(abs(f))/f - 1/12*I*b^2*log(abs(f))^2/f - 1/2*I*pi*a*sgn(f)
+ 1/2*I*pi*a + a*log(abs(f)) - 3*I*d)/(sqrt(f)*(I*f/abs(f) + 1)) - 3/16*sq
rt(2)*sqrt(pi)*erf(-1/8*sqrt(2)*(4*x + (pi*b*sgn(f) - pi*b + 2*I*b*log(abs(f)
))))/f*(I*f/abs(f) + 1)*sqrt(abs(f)))*e^(-1/8*I*pi^2*b^2*sgn(f)/f - 1/4*pi*
b^2*log(abs(f))*sgn(f)/f + 1/8*I*pi^2*b^2/f + 1/4*pi*b^2*log(abs(f))/f - 1/
4*I*b^2*log(abs(f))^2/f - 1/2*I*pi*a*sgn(f) + 1/2*I*pi*a + a*log(abs(f)) -
I*d)/((I*f/abs(f) + 1)*sqrt(abs(f)))
```

maple [A] time = 0.63, size = 235, normalized size = 0.79

$$\frac{\sqrt{\pi} f^a e^{-\frac{i(\ln(f)^2 b^2 + 36df)}{12f}} \sqrt{3} \operatorname{erf}\left(-\sqrt{3} \sqrt{if} x + \frac{\ln(f)b\sqrt{3}}{6\sqrt{if}}\right)}{48\sqrt{if}} - \frac{3\sqrt{\pi} f^a e^{-\frac{i(\ln(f)^2 b^2 + 4df)}{4f}} \operatorname{erf}\left(-\sqrt{if} x + \frac{\ln(f)b}{2\sqrt{if}}\right)}{16\sqrt{if}} - \frac{3\sqrt{\pi} f^a e^{i(\ln(f)^2 b^2 + 36df)}}{48\sqrt{if}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(f^(b*x+a)*cos(f*x^2+d)^3,x)

```
[Out] -1/48*Pi^(1/2)*f^a*exp(-1/12*I*(ln(f)^2*b^2+36*d*f)/f)*3^(1/2)/(I*f)^(1/2)*
erf(-3^(1/2)*(I*f)^(1/2)*x+1/6*ln(f)*b*3^(1/2)/(I*f)^(1/2))-3/16*Pi^(1/2)*f
^a*exp(-1/4*I*(ln(f)^2*b^2+4*d*f)/f)/(I*f)^(1/2)*erf(-(I*f)^(1/2)*x+1/2*ln(
f)*b/(I*f)^(1/2))-3/16*Pi^(1/2)*f^a*exp(1/4*I*(ln(f)^2*b^2+4*d*f)/f)/(-I*f)
^(1/2)*erf(-(-I*f)^(1/2)*x+1/2*ln(f)*b/(-I*f)^(1/2))-1/16*Pi^(1/2)*f^a*exp(
1/12*I*(ln(f)^2*b^2+36*d*f)/f)/(-3*I*f)^(1/2)*erf(-(-3*I*f)^(1/2)*x+1/2*ln(
f)*b/(-3*I*f)^(1/2))
```

maxima [A] time = 0.45, size = 302, normalized size = 1.01

$$\frac{3 \cdot 9^{\frac{1}{4}} \sqrt{2} \sqrt{\pi} \left((i-1) f^a \cos\left(\frac{b^2 \log(f)^2 + 36df}{12f}\right) + (i+1) f^a \sin\left(\frac{b^2 \log(f)^2 + 36df}{12f}\right) \right) \operatorname{erf}\left(\frac{6ifx - b \log(f)}{2\sqrt{3if}}\right) + (i+1) f^a \cos\left(\frac{b^2 \log(f)^2 + 36df}{12f}\right)}{48\sqrt{if}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(b*x+a)*cos(f*x^2+d)^3,x, algorithm="maxima")

[Out]
$$-1/288*(3*9^{1/4}*\sqrt{2}*\sqrt{\pi})*((I - 1)*f^a*\cos(1/12*(b^2*\log(f)^2 + 36*d*f)/f) + (I + 1)*f^a*\sin(1/12*(b^2*\log(f)^2 + 36*d*f)/f))*\operatorname{erf}(1/2*(6*I*f*x - b*\log(f))/\sqrt{3*I*f}) + ((I + 1)*f^a*\cos(1/12*(b^2*\log(f)^2 + 36*d*f)/f) + (I - 1)*f^a*\sin(1/12*(b^2*\log(f)^2 + 36*d*f)/f))*\operatorname{erf}(1/2*(6*I*f*x + b*\log(f))/\sqrt{-3*I*f})) * f^{3/2} + \sqrt{2}*\sqrt{\pi}*((27*I - 27)*f^a*\cos(1/4*(b^2*\log(f)^2 + 4*d*f)/f) + (27*I + 27)*f^a*\sin(1/4*(b^2*\log(f)^2 + 4*d*f)/f))*\operatorname{erf}(1/2*(2*I*f*x - b*\log(f))/\sqrt{I*f}) + ((27*I + 27)*f^a*\cos(1/4*(b^2*\log(f)^2 + 4*d*f)/f) + (27*I - 27)*f^a*\sin(1/4*(b^2*\log(f)^2 + 4*d*f)/f))*\operatorname{erf}(1/2*(2*I*f*x + b*\log(f))/\sqrt{-I*f})) * f^{3/2})/f^2$$

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int f^{a+bx} \cos(fx^2 + d)^3 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(f^(a + b*x)*cos(d + f*x^2)^3,x)

[Out] int(f^(a + b*x)*cos(d + f*x^2)^3, x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int f^{a+bx} \cos^3(d + fx^2) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f**(b*x+a)*cos(f*x**2+d)**3,x)

[Out] Integral(f**(a + b*x)*cos(d + f*x**2)**3, x)

3.113 $\int f^{a+bx} \cos(d + ex + fx^2) dx$

Optimal. Leaf size=162

$$-\frac{1}{4} \sqrt[4]{-1} \sqrt{\pi} f^{a-\frac{1}{2}} e^{\frac{1}{4}i\left(4d + \frac{(b \log(f) + ie)^2}{f}\right)} \operatorname{erf}\left(\frac{\sqrt[4]{-1}(b \log(f) + ie + 2ifx)}{2\sqrt{f}}\right) - \frac{1}{4} \sqrt[4]{-1} \sqrt{\pi} f^{a-\frac{1}{2}} e^{\frac{i(e+ib \log(f))^2}{4f} - id} \operatorname{erfi}\left(\frac{\sqrt[4]{-1}(-b \log(f) + ie + 2ifx)}{2\sqrt{f}}\right)$$

[Out] $-1/4*(-1)^{(1/4)}*\exp(1/4*I*(4*d+(I*e+b*\ln(f))^2/f))*f^{(-1/2+a)}*\operatorname{erf}(1/2*(-1)^{(1/4)}*(I*e+2*I*f*x+b*\ln(f))/f^{(1/2)})*\operatorname{Pi}^{(1/2)}-1/4*(-1)^{(1/4)}*\exp(-I*d+1/4*I*(e+I*b*\ln(f))^2/f)*f^{(-1/2+a)}*\operatorname{erfi}(1/2*(-1)^{(1/4)}*(I*e+2*I*f*x-b*\ln(f))/f^{(1/2)})*\operatorname{Pi}^{(1/2)}$

Rubi [A] time = 0.25, antiderivative size = 162, normalized size of antiderivative = 1.00, number of steps used = 8, number of rules used = 5, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.263$, Rules used = {4473, 2287, 2234, 2204, 2205}

$$-\frac{1}{4} \sqrt[4]{-1} \sqrt{\pi} f^{a-\frac{1}{2}} e^{\frac{1}{4}i\left(4d + \frac{(b \log(f) + ie)^2}{f}\right)} \operatorname{Erf}\left(\frac{\sqrt[4]{-1}(b \log(f) + ie + 2ifx)}{2\sqrt{f}}\right) - \frac{1}{4} \sqrt[4]{-1} \sqrt{\pi} f^{a-\frac{1}{2}} e^{\frac{i(e+ib \log(f))^2}{4f} - id} \operatorname{Erfi}\left(\frac{\sqrt[4]{-1}(-b \log(f) + ie + 2ifx)}{2\sqrt{f}}\right)$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[f^{(a + b*x)}*\operatorname{Cos}[d + e*x + f*x^2], x]$

[Out] $-((-1)^{(1/4)}*E^{((I/4)*(4*d + (I*e + b*\operatorname{Log}[f])^2/f))*f^{(-1/2 + a)}*\operatorname{Sqrt}[\operatorname{Pi}]*\operatorname{Erf}(((1/4)*(I*e + (2*I)*f*x + b*\operatorname{Log}[f]))/(2*\operatorname{Sqrt}[f])))/4 - ((-1)^{(1/4)}*E^{((-I)*d + ((I/4)*(e + I*b*\operatorname{Log}[f])^2)/f))*f^{(-1/2 + a)}*\operatorname{Sqrt}[\operatorname{Pi}]*\operatorname{Erfi}(((1/4)*(I*e + (2*I)*f*x - b*\operatorname{Log}[f]))/(2*\operatorname{Sqrt}[f])))/4$

Rule 2204

$\operatorname{Int}[(F_)^{((a_.) + (b_.)*((c_.) + (d_.)*(x_))^2)}, x_Symbol] \rightarrow \operatorname{Simp}[(F^a*\operatorname{Sqrt}[\operatorname{Pi}]*\operatorname{Erfi}[(c + d*x)*\operatorname{Rt}[b*\operatorname{Log}[F], 2]])/(2*d*\operatorname{Rt}[b*\operatorname{Log}[F], 2]), x] /; \operatorname{FreeQ}\{F, a, b, c, d\}, x] \&\& \operatorname{PosQ}[b]$

Rule 2205

$\operatorname{Int}[(F_)^{((a_.) + (b_.)*((c_.) + (d_.)*(x_))^2)}, x_Symbol] \rightarrow \operatorname{Simp}[(F^a*\operatorname{Sqrt}[\operatorname{Pi}]*\operatorname{Erf}[(c + d*x)*\operatorname{Rt}[-(b*\operatorname{Log}[F]), 2]])/(2*d*\operatorname{Rt}[-(b*\operatorname{Log}[F]), 2]), x] /; \operatorname{FreeQ}\{F, a, b, c, d\}, x] \&\& \operatorname{NegQ}[b]$

Rule 2234

$\operatorname{Int}[(F_)^{((a_.) + (b_.)*(x_) + (c_.)*(x_)^2)}, x_Symbol] \rightarrow \operatorname{Dist}[F^{(a - b^2/(4*c))}, \operatorname{Int}[F^{((b + 2*c*x)^2/(4*c))}, x], x] /; \operatorname{FreeQ}\{F, a, b, c\}, x]$

Rule 2287

$\operatorname{Int}[(u_)*(F_)^{(v_)}*(G_)^{(w_)}, x_Symbol] \rightarrow \operatorname{With}\{z = v*\operatorname{Log}[F] + w*\operatorname{Log}[G]\}, \operatorname{Int}[u*\operatorname{NormalizeIntegrand}[E^z, x], x] /; \operatorname{BinomialQ}[z, x] \mid\mid (\operatorname{PolynomialQ}[z, x] \&\& \operatorname{LeQ}[\operatorname{Exponent}[z, x], 2]) /; \operatorname{FreeQ}\{F, G\}, x]$

Rule 4473

$\operatorname{Int}[\operatorname{Cos}[v_]^{(n_.)}*(F_)^{(u_)}, x_Symbol] \rightarrow \operatorname{Int}[\operatorname{ExpandTrigToExp}[F^u, \operatorname{Cos}[v]^n], x] /; \operatorname{FreeQ}[F, x] \&\& (\operatorname{LinearQ}[u, x] \mid\mid \operatorname{PolyQ}[u, x, 2]) \&\& (\operatorname{LinearQ}[v, x] \mid\mid \operatorname{PolyQ}[v, x, 2]) \&\& \operatorname{IGtQ}[n, 0]$

Rubi steps

$$\begin{aligned}
\int f^{a+bx} \cos(d+ex+fx^2) dx &= \int \left(\frac{1}{2} e^{-id-ix-ix^2} f^{a+bx} + \frac{1}{2} e^{id+ix+ix^2} f^{a+bx} \right) dx \\
&= \frac{1}{2} \int e^{-id-ix-ix^2} f^{a+bx} dx + \frac{1}{2} \int e^{id+ix+ix^2} f^{a+bx} dx \\
&= \frac{1}{2} \int \exp(-id-ix^2+a \log(f)-x(ie-b \log(f))) dx + \frac{1}{2} \int \exp(id+ix^2+a \log(f)+x(ie+b \log(f))) dx \\
&= \frac{1}{2} \left(e^{-id+\frac{i(e+ib \log(f))^2}{4f}} f^a \right) \int e^{\frac{i(-ie-2ifx+b \log(f))^2}{4f}} dx + \frac{1}{2} \left(e^{\frac{1}{4}i \left(4d+\frac{(ie+b \log(f))^2}{f} \right)} f^a \right) \int e^{-\frac{i(-ie-2ifx+b \log(f))^2}{4f}} dx \\
&= -\frac{1}{4} \sqrt[4]{-1} e^{\frac{1}{4}i \left(4d+\frac{(ie+b \log(f))^2}{f} \right)} f^{-\frac{1}{2}+a} \sqrt{\pi} \operatorname{erf} \left(\frac{\sqrt[4]{-1} (ie+2ifx+b \log(f))}{2\sqrt{f}} \right) - \frac{1}{4} \sqrt[4]{-1} e^{-\frac{1}{4}i \left(4d+\frac{(ie+b \log(f))^2}{f} \right)} f^{-\frac{1}{2}+a} \sqrt{\pi} \operatorname{erf} \left(\frac{\sqrt[4]{-1} (-ie-2ifx+b \log(f))}{2\sqrt{f}} \right)
\end{aligned}$$

Mathematica [A] time = 0.39, size = 163, normalized size = 1.01

$$\frac{1}{4} \sqrt[4]{-1} \sqrt{\pi} f^{a-\frac{be+f}{2f}} e^{-\frac{i(b^2 \log^2(f)+e^2)}{4f}} \left(e^{\frac{ib^2 \log^2(f)}{2f}} (\sin(d) - i \cos(d)) \operatorname{erfi} \left(\frac{\sqrt[4]{-1} (-ib \log(f) + e + 2fx)}{2\sqrt{f}} \right) - e^{\frac{ie^2}{2f}} (\cos(d) - i \sin(d)) \operatorname{erfi} \left(\frac{\sqrt[4]{-1} (ib \log(f) - e - 2fx)}{2\sqrt{f}} \right) \right)$$

Antiderivative was successfully verified.

[In] Integrate[f^(a + b*x)*Cos[d + e*x + f*x^2], x]

[Out] ((-1)^(1/4)*f^(a - (b*e + f)/(2*f))*Sqrt[Pi]*(-E^(((I/2)*e^2)/f)*Erfi[(((-1)^(3/4)*(e + 2*f*x + I*b*Log[f]))/(2*Sqrt[f]))*(Cos[d] - I*Sin[d])] + E^(((I/2)*b^2*Log[f]^2)/f)*Erfi[(((-1)^(1/4)*(e + 2*f*x - I*b*Log[f]))/(2*Sqrt[f]))*(Cos[d] + I*Sin[d])])/(4*E^(((I/4)*(e^2 + b^2*Log[f]^2))/f))

fricas [B] time = 1.72, size = 313, normalized size = 1.93

$$\sqrt{2} \pi \sqrt{\frac{f}{\pi}} e^{\left(\frac{-ib^2 \log(f)^2 + ie^2 - 4idf - 2(be - 2af) \log(f)}{4f} \right)} C \left(\frac{\sqrt{2} (2fx + ib \log(f) + e) \sqrt{\frac{f}{\pi}}}{2f} \right) - \sqrt{2} \pi \sqrt{\frac{f}{\pi}} e^{\left(\frac{ib^2 \log(f)^2 - ie^2 + 4idf - 2(be - 2af) \log(f)}{4f} \right)} C \left(\frac{\sqrt{2} (2fx - ib \log(f) - e) \sqrt{\frac{f}{\pi}}}{2f} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(b*x+a)*cos(f*x^2+e*x+d), x, algorithm="fricas")

[Out] 1/4*(sqrt(2)*pi*sqrt(f/pi)*e^(1/4*(-I*b^2*log(f)^2 + I*e^2 - 4*I*d*f - 2*(b*e - 2*a*f)*log(f))/f)*fresnel_cos(1/2*sqrt(2)*(2*f*x + I*b*log(f) + e)*sqrt(f/pi)/f) - sqrt(2)*pi*sqrt(f/pi)*e^(1/4*(I*b^2*log(f)^2 - I*e^2 + 4*I*d*f - 2*(b*e - 2*a*f)*log(f))/f)*fresnel_cos(-1/2*sqrt(2)*(2*f*x - I*b*log(f) + e)*sqrt(f/pi)/f) - I*sqrt(2)*pi*sqrt(f/pi)*e^(1/4*(-I*b^2*log(f)^2 + I*e^2 - 4*I*d*f - 2*(b*e - 2*a*f)*log(f))/f)*fresnel_sin(1/2*sqrt(2)*(2*f*x + I*b*log(f) + e)*sqrt(f/pi)/f) - I*sqrt(2)*pi*sqrt(f/pi)*e^(1/4*(I*b^2*log(f)^2 - I*e^2 + 4*I*d*f - 2*(b*e - 2*a*f)*log(f))/f)*fresnel_sin(-1/2*sqrt(2)*(2*f*x - I*b*log(f) + e)*sqrt(f/pi)/f)/f

giac [B] time = 0.31, size = 384, normalized size = 2.37

$$\frac{\sqrt{2} \sqrt{\pi} \operatorname{erf} \left(-\frac{1}{8} \sqrt{2} \left(4x - \frac{\pi b \operatorname{sgn}(f) - \pi b + 2i b \log(|f|) - 2e}{f} \right) \left(-\frac{if}{|f|} + 1 \right) \sqrt{|f|} \right) e^{\left(\frac{i \pi^2 b^2 \operatorname{sgn}(f)}{8f} + \frac{\pi b^2 \log(|f|) \operatorname{sgn}(f)}{4f} - \frac{i \pi^2 b^2}{8f} - \frac{\pi b^2 \log(|f|)}{4f} + \frac{ie^2}{2f} \right)}}{4 \left(-\frac{if}{|f|} + 1 \right) \sqrt{|f|}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(b*x+a)*cos(f*x^2+e*x+d),x, algorithm="giac")

[Out]
$$-1/4*\sqrt{2}*\sqrt{\pi}*\operatorname{erf}\left(-1/8*\sqrt{2}*(4*x - (\pi*b*\operatorname{sgn}(f) - \pi*b + 2*I*b*\log(\operatorname{abs}(f)) - 2*e)/f)*(-I*f/\operatorname{abs}(f) + 1)*\sqrt{\operatorname{abs}(f)}\right)*e^{(1/8*I*\pi^2*b^2*\operatorname{sgn}(f)/f + 1/4*\pi*b^2*\log(\operatorname{abs}(f))*\operatorname{sgn}(f)/f - 1/8*I*\pi^2*b^2/f - 1/4*\pi*b^2*\log(\operatorname{abs}(f))/f + 1/4*I*b^2*\log(\operatorname{abs}(f))^2/f - 1/2*I*\pi*a*\operatorname{sgn}(f) + 1/4*I*\pi*b*e*\operatorname{sgn}(f)/f + 1/2*I*\pi*a - 1/4*I*\pi*b*e/f + a*\log(\operatorname{abs}(f)) - 1/2*b*e*\log(\operatorname{abs}(f))/f + I*d - 1/4*I*e^2/f)/((-I*f/\operatorname{abs}(f) + 1)*\sqrt{\operatorname{abs}(f)})} - 1/4*\sqrt{2}*\sqrt{\pi}*\operatorname{erf}\left(-1/8*\sqrt{2}*(4*x + (\pi*b*\operatorname{sgn}(f) - \pi*b + 2*I*b*\log(\operatorname{abs}(f)) + 2*e)/f)*(I*f/\operatorname{abs}(f) + 1)*\sqrt{\operatorname{abs}(f)}\right)*e^{(-1/8*I*\pi^2*b^2*\operatorname{sgn}(f)/f - 1/4*\pi*b^2*\log(\operatorname{abs}(f))*\operatorname{sgn}(f)/f + 1/8*I*\pi^2*b^2/f + 1/4*\pi*b^2*\log(\operatorname{abs}(f))/f - 1/4*I*b^2*\log(\operatorname{abs}(f))^2/f - 1/2*I*\pi*a*\operatorname{sgn}(f) + 1/4*I*\pi*b*e*\operatorname{sgn}(f)/f + 1/2*I*\pi*a - 1/4*I*\pi*b*e/f + a*\log(\operatorname{abs}(f)) - 1/2*b*e*\log(\operatorname{abs}(f))/f - I*d + 1/4*I*e^2/f)/((I*f/\operatorname{abs}(f) + 1)*\sqrt{\operatorname{abs}(f)})}$$

maple [A] time = 0.18, size = 150, normalized size = 0.93

$$\frac{\sqrt{\pi} f^a e^{\frac{i(-e^2-2i\ln(f)be+\ln(f)^2b^2+4df)}{4f}} \operatorname{erf}\left(-\sqrt{if} x + \frac{-ie+b\ln(f)}{2\sqrt{if}}\right)}{4\sqrt{if}} - \frac{\sqrt{\pi} f^a e^{\frac{i(-e^2+2i\ln(f)be+\ln(f)^2b^2+4df)}{4f}} \operatorname{erf}\left(-\sqrt{-if} x + \frac{ie+b\ln(f)}{2\sqrt{-if}}\right)}{4\sqrt{-if}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(f^(b*x+a)*cos(f*x^2+e*x+d),x)

[Out]
$$-1/4*\pi^{(1/2)}*f^a*\exp(-1/4*I*(-e^2-2*I*\ln(f)*b*e+\ln(f)^2*b^2+4*d*f)/f)/(I*f)^{(1/2)}*\operatorname{erf}\left(-\left(I*f\right)^{(1/2)}*x+1/2*(-I*e+b*\ln(f))\right)/\left(I*f\right)^{(1/2)}-1/4*\pi^{(1/2)}*f^a*\exp(1/4*I*(-e^2+2*I*\ln(f)*b*e+\ln(f)^2*b^2+4*d*f)/f)/\left(-I*f\right)^{(1/2)}*\operatorname{erf}\left(-\left(-I*f\right)^{(1/2)}*x+1/2*(I*e+b*\ln(f))\right)/\left(-I*f\right)^{(1/2)}$$

maxima [A] time = 0.36, size = 190, normalized size = 1.17

$$\frac{\sqrt{2} \sqrt{\pi} \left(\left(-(i-1) f^a \cos\left(\frac{b^2 \log(f)^2 - e^2 + 4df}{4f}\right) - (i+1) f^a \sin\left(\frac{b^2 \log(f)^2 - e^2 + 4df}{4f}\right) \right) \operatorname{erf}\left(\frac{i(2ifx - b\log(f) + ie)\sqrt{if}}{2f}\right) + \left((i+1) f^a \cos\left(\frac{b^2 \log(f)^2 - e^2 + 4df}{4f}\right) - (i-1) f^a \sin\left(\frac{b^2 \log(f)^2 - e^2 + 4df}{4f}\right) \right) \operatorname{erf}\left(\frac{i(2ifx - b\log(f) + ie)\sqrt{-if}}{2f}\right) }{8\sqrt{f} f^{\frac{be}{2f}}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(b*x+a)*cos(f*x^2+e*x+d),x, algorithm="maxima")

[Out]
$$-1/8*\sqrt{2}*\sqrt{\pi}*\left(\left(-\left(I-1\right)*f^a*\cos\left(1/4*\left(b^2*\log(f)^2 - e^2 + 4*d*f\right)/f\right) - \left(I+1\right)*f^a*\sin\left(1/4*\left(b^2*\log(f)^2 - e^2 + 4*d*f\right)/f\right)\right)*\operatorname{erf}\left(1/2*I*\left(2*I*f*x - b*\log(f) + I*e\right)*\sqrt{I*f}/f\right) + \left(\left(I+1\right)*f^a*\cos\left(1/4*\left(b^2*\log(f)^2 - e^2 + 4*d*f\right)/f\right) + \left(I-1\right)*f^a*\sin\left(1/4*\left(b^2*\log(f)^2 - e^2 + 4*d*f\right)/f\right)\right)*\operatorname{erf}\left(1/2*I*\left(2*I*f*x + b*\log(f) + I*e\right)*\sqrt{-I*f}/f\right)\right)/\left(\sqrt{f}*f^{\left(1/2*b*e/f\right)}\right)$$

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int f^{a+bx} \cos(fx^2 + ex + d) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(f^(a + b*x)*cos(d + e*x + f*x^2),x)

[Out] int(f^(a + b*x)*cos(d + e*x + f*x^2), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int f^{a+bx} \cos(d + ex + fx^2) dx$$

Verification of antiderivative is not currently implemented for this CAS.


```
[In] integrate(f**(b*x+a)*cos(f*x**2+e*x+d),x)
```

```
[Out] Integral(f**(a + b*x)*cos(d + e*x + f*x**2), x)
```

3.114 $\int f^{a+bx} \cos^2(d + ex + fx^2) dx$

Optimal. Leaf size=179

$$\left(-\frac{1}{16} - \frac{i}{16}\right) \sqrt{\pi} f^{a-\frac{1}{2}} e^{\frac{i(b \log(f)+2ie)^2}{8f} + 2id} \operatorname{erf}\left(\frac{\left(\frac{1}{4} + \frac{i}{4}\right)(b \log(f) + 2ie + 4ifx)}{\sqrt{f}}\right) - \left(\frac{1}{16} + \frac{i}{16}\right) \sqrt{\pi} f^{a-\frac{1}{2}} e^{\frac{i(2e+ib \log(f))^2}{8f} - 2id} \operatorname{erfi}\left(\frac{\left(\frac{1}{4} + \frac{i}{4}\right)(b \log(f) + 2ie + 4ifx)}{\sqrt{f}}\right)$$

[Out] 1/2*f^(b*x+a)/b/ln(f)-(1/16+1/16*I)*exp(2*I*d+1/8*I*(2*I*e+b*ln(f))^2/f)*f^(-1/2+a)*erf((1/4+1/4*I)*(2*I*e+4*I*f*x+b*ln(f))/f^(1/2))*Pi^(1/2)-(1/16+1/16*I)*exp(-2*I*d+1/8*I*(2*e+I*b*ln(f))^2/f)*f^(-1/2+a)*erfi((1/4+1/4*I)*(2*I*e+4*I*f*x-b*ln(f))/f^(1/2))*Pi^(1/2)

Rubi [A] time = 0.28, antiderivative size = 179, normalized size of antiderivative = 1.00, number of steps used = 9, number of rules used = 6, integrand size = 21, $\frac{\text{number of rules}}{\text{integrand size}} = 0.286$, Rules used = {4473, 2194, 2287, 2234, 2204, 2205}

$$\left(-\frac{1}{16} - \frac{i}{16}\right) \sqrt{\pi} f^{a-\frac{1}{2}} e^{\frac{i(b \log(f)+2ie)^2}{8f} + 2id} \operatorname{Erf}\left(\frac{\left(\frac{1}{4} + \frac{i}{4}\right)(b \log(f) + 2ie + 4ifx)}{\sqrt{f}}\right) - \left(\frac{1}{16} + \frac{i}{16}\right) \sqrt{\pi} f^{a-\frac{1}{2}} e^{\frac{i(2e+ib \log(f))^2}{8f} - 2id} \operatorname{Erfi}\left(\frac{\left(\frac{1}{4} + \frac{i}{4}\right)(b \log(f) + 2ie + 4ifx)}{\sqrt{f}}\right)$$

Antiderivative was successfully verified.

[In] Int[f^(a + b*x)*Cos[d + e*x + f*x^2]^2,x]

[Out] (-1/16 - I/16)*E^((2*I)*d + ((I/8)*((2*I)*e + b*Log[f])^2)/f)*f^(-1/2 + a)*Sqrt[Pi]*Erf[(((1/4 + I/4)*((2*I)*e + (4*I)*f*x + b*Log[f]))/Sqrt[f]) - (1/16 + I/16)*E^((-2*I)*d + ((I/8)*(2*e + I*b*Log[f])^2)/f)*f^(-1/2 + a)*Sqrt[Pi]*Erfi[(((1/4 + I/4)*((2*I)*e + (4*I)*f*x - b*Log[f]))/Sqrt[f]) + f^(a + b*x)/(2*b*Log[f])]

Rule 2194

Int[((F_)^((c_.)*((a_.) + (b_.)*(x_))))^(n_.), x_Symbol] := Simp[(F^(c*(a + b*x)))^n/(b*c*n*Log[F]), x] /; FreeQ[{F, a, b, c, n}, x]

Rule 2204

Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^2), x_Symbol] := Simp[(F^a*Sqrt[Pi]*Erfi[(c + d*x)*Rt[b*Log[F], 2]]/(2*d*Rt[b*Log[F], 2]), x] /; FreeQ[{F, a, b, c, d}, x] && PosQ[b]

Rule 2205

Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^2), x_Symbol] := Simp[(F^a*Sqrt[Pi]*Erf[(c + d*x)*Rt[-(b*Log[F]), 2]]/(2*d*Rt[-(b*Log[F]), 2]), x] /; FreeQ[{F, a, b, c, d}, x] && NegQ[b]

Rule 2234

Int[(F_)^((a_.) + (b_.)*(x_) + (c_.)*(x_)^2), x_Symbol] := Dist[F^(a - b^2/(4*c)), Int[F^((b + 2*c*x)^2/(4*c)), x], x] /; FreeQ[{F, a, b, c}, x]

Rule 2287

Int[(u_.)*(F_)^(v_.)*(G_)^(w_.), x_Symbol] := With[{z = v*Log[F] + w*Log[G]}, Int[u*NormalizeIntegrand[E^z, x], x] /; BinomialQ[z, x] || (PolynomialQ[z, x] && LeQ[Exponent[z, x], 2]) /; FreeQ[{F, G}, x]

Rule 4473

`Int[Cos[v_]^(n_.)*(F_)^(u_), x_Symbol] := Int[ExpandTrigToExp[F^u, Cos[v]^n, x], x] /; FreeQ[F, x] && (LinearQ[u, x] || PolyQ[u, x, 2]) && (LinearQ[v, x] || PolyQ[v, x, 2]) && IGtQ[n, 0]`

Rubi steps

$$\begin{aligned} \int f^{a+bx} \cos^2(d+ex+fx^2) dx &= \int \left(\frac{1}{2} f^{a+bx} + \frac{1}{4} e^{-2id-2iex-2ifx^2} f^{a+bx} + \frac{1}{4} e^{2id+2iex+2ifx^2} f^{a+bx} \right) dx \\ &= \frac{1}{4} \int e^{-2id-2iex-2ifx^2} f^{a+bx} dx + \frac{1}{4} \int e^{2id+2iex+2ifx^2} f^{a+bx} dx + \frac{1}{2} \int f^{a+bx} dx \\ &= \frac{f^{a+bx}}{2b \log(f)} + \frac{1}{4} \int \exp(-2id - 2ifx^2 + a \log(f) - x(2ie - b \log(f))) dx + \frac{1}{4} \int \exp(2id + 2iex + 2ifx^2 + a \log(f) + x(2ie + b \log(f))) dx \\ &= \frac{f^{a+bx}}{2b \log(f)} + \frac{1}{4} \exp\left(-2id + a \log(f) - \frac{i(-2ie + b \log(f))^2}{8f}\right) \int e^{\frac{i(-2ie-4ifx+b \log(f))}{8f}} dx \\ &= \left(-\frac{1}{16} - \frac{i}{16}\right) e^{2id + \frac{i(2ie+b \log(f))^2}{8f}} f^{-\frac{1}{2}+a} \sqrt{\pi} \operatorname{erf}\left(\frac{\left(\frac{1}{4} + \frac{i}{4}\right)(2ie + 4ifx + b \log(f))}{\sqrt{f}}\right) \end{aligned}$$

Mathematica [A] time = 1.08, size = 245, normalized size = 1.37

$$f^{a-\frac{be+f}{2f}} e^{-\frac{i(b^2 \log^2(f)+4e^2)}{8f}} \left(\sqrt[4]{-1} \sqrt{2\pi} b \log(f) e^{\frac{ib^2 \log^2(f)}{4f}} (\sin(2d) - i \cos(2d)) \operatorname{erfi}\left(\frac{\left(\frac{1}{4} + \frac{i}{4}\right)(-ib \log(f) + 2e + 4fx)}{\sqrt{f}}\right) + 8f^{b\left(\frac{e}{2f} + x\right)} \right) \Big/ 16b \log(f)$$

Antiderivative was successfully verified.

[In] Integrate[f^(a + b*x)*Cos[d + e*x + f*x^2]^2, x]

[Out] (f^(a - (b*e + f)/(2*f)) * (8 * E^(((I/8) * (4*e^2 + b^2 * Log[f]^2))/f)) * f^(1/2 + b * (e/(2*f) + x)) + (-1)^(1/4) * b * E^(((I/4) * b^2 * Log[f]^2)/f) * Sqrt[2 * Pi] * Erfi[(1/4 + I/4) * (2*e + 4*f*x - I * b * Log[f])]/Sqrt[f]) * Log[f] * ((-I) * Cos[2*d] + Sin[2*d]) - (-1)^(1/4) * b * E^((I * e^2)/f) * Sqrt[2 * Pi] * Erf[(1/4 + I/4) * (2*e + 4*f*x + I * b * Log[f])]/Sqrt[f]) * Log[f] * (I * Cos[2*d] + Sin[2*d])) / (16 * b * E^(((I/8) * (4*e^2 + b^2 * Log[f]^2))/f)) * Log[f])

fricas [B] time = 0.76, size = 327, normalized size = 1.83

$$2 \pi b \sqrt{\frac{f}{\pi}} e^{\left(\frac{-ib^2 \log(f)^2 + 4ie^2 - 16idf - 4(be - 2af) \log(f)}{8f}\right)} C\left(\frac{(4fx + ib \log(f) + 2e) \sqrt{\frac{f}{\pi}}}{2f}\right) \log(f) - 2 \pi b \sqrt{\frac{f}{\pi}} e^{\left(\frac{ib^2 \log(f)^2 - 4ie^2 + 16idf - 4(be - 2af) \log(f)}{8f}\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(b*x+a)*cos(f*x^2+e*x+d)^2,x, algorithm="fricas")

[Out] 1/16*(2*pi*b*sqrt(f/pi))*e^(1/8*(-I*b^2*log(f)^2 + 4*I*e^2 - 16*I*d*f - 4*(b*e - 2*a*f)*log(f))/f)*fresnel_cos(1/2*(4*f*x + I*b*log(f) + 2*e)*sqrt(f/pi)/f)*log(f) - 2*pi*b*sqrt(f/pi)*e^(1/8*(I*b^2*log(f)^2 - 4*I*e^2 + 16*I*d*f - 4*(b*e - 2*a*f)*log(f))/f)*fresnel_cos(-1/2*(4*f*x - I*b*log(f) + 2*e)*sqrt(f/pi)/f)*log(f) - 2*I*pi*b*sqrt(f/pi)*e^(1/8*(-I*b^2*log(f)^2 + 4*I*e^2 - 16*I*d*f - 4*(b*e - 2*a*f)*log(f))/f)*fresnel_sin(1/2*(4*f*x + I*b*log(f) + 2*e)*sqrt(f/pi)/f)*log(f) - 2*I*pi*b*sqrt(f/pi)*e^(1/8*(I*b^2*log(f)^2 - 4*I*e^2 + 16*I*d*f - 4*(b*e - 2*a*f)*log(f))/f)*fresnel_sin(-1/2*(4*f*x - I*b*log(f) + 2*e)*sqrt(f/pi)/f)*log(f)

$- 4*I*e^2 + 16*I*d*f - 4*(b*e - 2*a*f)*\log(f))/f)*\text{fresnel_sin}(-1/2*(4*f*x - I*b*\log(f) + 2*e)*\sqrt{f/\pi}/f)*\log(f) + 8*f*f^{(b*x + a)}/(b*f*\log(f))$

giac [B] time = 0.36, size = 605, normalized size = 3.38

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(b*x+a)*cos(f*x^2+e*x+d)^2,x, algorithm="giac")

[Out] $(2*b*\cos(-1/2*\pi*b*x*\text{sgn}(f) + 1/2*\pi*b*x - 1/2*\pi*a*\text{sgn}(f) + 1/2*\pi*a)*\log(\text{abs}(f))/(4*b^2*\log(\text{abs}(f))^2 + (\pi*b*\text{sgn}(f) - \pi*b)^2) - (\pi*b*\text{sgn}(f) - \pi*b)*\sin(-1/2*\pi*b*x*\text{sgn}(f) + 1/2*\pi*b*x - 1/2*\pi*a*\text{sgn}(f) + 1/2*\pi*a)/(4*b^2*\log(\text{abs}(f))^2 + (\pi*b*\text{sgn}(f) - \pi*b)^2))*e^{(b*x*\log(\text{abs}(f)) + a*\log(\text{abs}(f)))} - 1/2*I*(-2*I*e^{(1/2*I*\pi*b*x*\text{sgn}(f) - 1/2*I*\pi*b*x + 1/2*I*\pi*a*\text{sgn}(f) - 1/2*I*\pi*a)/(2*I*\pi*b*\text{sgn}(f) - 2*I*\pi*b + 4*b*\log(\text{abs}(f)))} + 2*I*e^{(-1/2*I*\pi*b*x*\text{sgn}(f) + 1/2*I*\pi*b*x - 1/2*I*\pi*a*\text{sgn}(f) + 1/2*I*\pi*a)/(-2*I*\pi*b*\text{sgn}(f) + 2*I*\pi*b + 4*b*\log(\text{abs}(f)))})*e^{(b*x*\log(\text{abs}(f)) + a*\log(\text{abs}(f)))} - 1/8*\sqrt{\pi}*\text{erf}(-1/8*\sqrt{f}*(8*x - (\pi*b*\text{sgn}(f) - \pi*b + 2*I*b*\log(\text{abs}(f)) - 4*e)/f)*(-I*f/\text{abs}(f) + 1))*e^{(1/16*I*\pi^2*b^2*\text{sgn}(f)/f + 1/8*\pi*b^2*\log(\text{abs}(f))*\text{sgn}(f)/f - 1/16*I*\pi^2*b^2/f - 1/8*\pi*b^2*\log(\text{abs}(f))/f + 1/8*I*b^2*\log(\text{abs}(f))^2/f - 1/2*I*\pi*a*\text{sgn}(f) + 1/4*I*\pi*b*e*\text{sgn}(f)/f + 1/2*I*\pi*a - 1/4*I*\pi*b*e/f + a*\log(\text{abs}(f)) - 1/2*b*e*\log(\text{abs}(f))/f + 2*I*d - 1/2*I*e^2/f)/(\sqrt{f}*(-I*f/\text{abs}(f) + 1))} - 1/8*\sqrt{\pi}*\text{erf}(-1/8*\sqrt{f}*(8*x + (\pi*b*\text{sgn}(f) - \pi*b + 2*I*b*\log(\text{abs}(f)) + 4*e)/f)*(I*f/\text{abs}(f) + 1))*e^{(-1/16*I*\pi^2*b^2*\text{sgn}(f)/f - 1/8*\pi*b^2*\log(\text{abs}(f))*\text{sgn}(f)/f + 1/16*I*\pi^2*b^2/f + 1/8*\pi*b^2*\log(\text{abs}(f))/f - 1/8*I*b^2*\log(\text{abs}(f))^2/f - 1/2*I*\pi*a*\text{sgn}(f) + 1/4*I*\pi*b*e*\text{sgn}(f)/f + 1/2*I*\pi*a - 1/4*I*\pi*b*e/f + a*\log(\text{abs}(f)) - 1/2*b*e*\log(\text{abs}(f))/f - 2*I*d + 1/2*I*e^2/f)/(\sqrt{f}*(I*f/\text{abs}(f) + 1))$

maple [A] time = 0.34, size = 175, normalized size = 0.98

$$\frac{\sqrt{\pi} f^a e^{\frac{i(\ln(f)^2 b^2 - 4i \ln(f) b e - 4e^2 + 16df)}{8f}} \sqrt{2} \operatorname{erf}\left(-\sqrt{2} \sqrt{if} x + \frac{(b \ln(f) - 2ie) \sqrt{2}}{4\sqrt{if}}\right)}{16\sqrt{if}} - \frac{\sqrt{\pi} f^a e^{\frac{i(\ln(f)^2 b^2 + 4i \ln(f) b e - 4e^2 + 16df)}{8f}} \operatorname{erf}\left(-\sqrt{-2if}\right)}{8\sqrt{-2if}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(f^(b*x+a)*cos(f*x^2+e*x+d)^2,x)

[Out] $-1/16*\pi^{(1/2)}*f^a*\exp(-1/8*I*(\ln(f)^2*b^2-4*I*\ln(f)*b*e-4*e^2+16*d*f)/f)*2^{(1/2)}/(I*f)^{(1/2)}*\text{erf}(-2^{(1/2)}*(I*f)^{(1/2)}*x+1/4*(b*\ln(f)-2*I*e)*2^{(1/2)})/(I*f)^{(1/2)}-1/8*\pi^{(1/2)}*f^a*\exp(1/8*I*(\ln(f)^2*b^2+4*I*\ln(f)*b*e-4*e^2+16*d*f)/f)/(-2*I*f)^{(1/2)}*\text{erf}(-(-2*I*f)^{(1/2)}*x+1/2*(2*I*e+b*\ln(f))/(-2*I*f)^{(1/2)})+1/2*f^{(b*x+a)}/b/\ln(f)$

maxima [B] time = 0.45, size = 240, normalized size = 1.34

$$\frac{4^{\frac{1}{4}} \sqrt{2} \sqrt{\pi} \left(\left(-(i-1) b f^a \cos\left(\frac{b^2 \log(f)^2 - 4e^2 + 16df}{8f}\right) \log(f) - (i+1) b f^a \log(f) \sin\left(\frac{b^2 \log(f)^2 - 4e^2 + 16df}{8f}\right) \right) \operatorname{erf}\left(\frac{i(4ifx - (i-1) b f^a \cos\left(\frac{b^2 \log(f)^2 - 4e^2 + 16df}{8f}\right) \log(f) - (i+1) b f^a \log(f) \sin\left(\frac{b^2 \log(f)^2 - 4e^2 + 16df}{8f}\right))}{2\sqrt{2} \sqrt{\pi}}\right)}{2\sqrt{2} \sqrt{\pi}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(b*x+a)*cos(f*x^2+e*x+d)^2,x, algorithm="maxima")

[Out] $-1/32*(4^{(1/4)}*\sqrt{2}*\sqrt{\pi})*((-(I-1)*b*f^a*\cos(1/8*(b^2*\log(f))^2 - 4*e^2 + 16*d*f)/f)*\log(f) - (I+1)*b*f^a*\log(f)*\sin(1/8*(b^2*\log(f))^2 - 4*e^2 + 16*d*f)/f))*\text{erf}(1/4*I*(4*I*f*x - b*\log(f) + 2*I*e)*\sqrt{2*I*f}/f) + ((I-1)*b*f^a*\cos(1/8*(b^2*\log(f))^2 - 4*e^2 + 16*d*f)/f)*\log(f) - (I+1)*b*f^a*\log(f)*\sin(1/8*(b^2*\log(f))^2 - 4*e^2 + 16*d*f)/f)$

+ 1)*b*f^a*cos(1/8*(b^2*log(f)^2 - 4*e^2 + 16*d*f)/f)*log(f) + (I - 1)*b*f^a*log(f)*sin(1/8*(b^2*log(f)^2 - 4*e^2 + 16*d*f)/f))*erf(1/4*I*(4*I*f*x + b*log(f) + 2*I*e)*sqrt(-2*I*f)/f))*f^(3/2) - 16*f^(a + 2)*e^(b*x*log(f) + 1/2*b*e*log(f)/f))/(b*f^2*f^(1/2*b*e/f)*log(f))

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int f^{a+bx} \cos(fx^2 + ex + d)^2 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(f^(a + b*x)*cos(d + e*x + f*x^2)^2,x)

[Out] int(f^(a + b*x)*cos(d + e*x + f*x^2)^2, x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int f^{a+bx} \cos^2(d + ex + fx^2) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f**(b*x+a)*cos(f*x**2+e*x+d)**2,x)

[Out] Integral(f**(a + b*x)*cos(d + e*x + f*x**2)**2, x)

3.115 $\int f^{a+bx} \cos^3(d + ex + fx^2) dx$

Optimal. Leaf size=340

$$-\frac{3}{16} \sqrt[4]{-1} \sqrt{\pi} f^{a-\frac{1}{2}} e^{\frac{1}{4}i \left(4d + \frac{(b \log(f) + ie)^2}{f}\right)} \operatorname{erf}\left(\frac{\sqrt[4]{-1} (b \log(f) + ie + 2ifx)}{2\sqrt{f}}\right) - \left(\frac{1}{16} + \frac{i}{16}\right) \sqrt{\frac{\pi}{6}} f^{a-\frac{1}{2}} e^{\frac{i(b \log(f) + 3ie)^2}{12f} + 3id} \operatorname{erf}\left(\frac{\sqrt{\frac{\pi}{6}} (b \log(f) + ie + 2ifx)}{2\sqrt{f}}\right)$$

[Out] $(-1/96 - 1/96 * I) * \exp(3 * I * d + 1/12 * I * (3 * I * e + b * \ln(f))^2 / f) * f^{(-1/2 + a)} * \operatorname{erf}\left(\frac{(1/12 + 1/12 * I) * (3 * I * e + 6 * I * f * x + b * \ln(f)) * 6^{(1/2)} / f^{(1/2)}}{2\sqrt{f}}\right) * 6^{(1/2)} * \pi^{(1/2)} - (1/96 + 1/96 * I) * \exp(-3 * I * d + 1/12 * I * (3 * e + I * b * \ln(f))^2 / f) * f^{(-1/2 + a)} * \operatorname{erfi}\left(\frac{(1/12 + 1/12 * I) * (3 * I * e + 6 * I * f * x - b * \ln(f)) * 6^{(1/2)} / f^{(1/2)}}{2\sqrt{f}}\right) * 6^{(1/2)} * \pi^{(1/2)} - 3/16 * (-1)^{(1/4)} * \exp(1/4 * I * (4 * d + (I * e + b * \ln(f))^2 / f)) * f^{(-1/2 + a)} * \operatorname{erf}\left(\frac{1/2 * (-1)^{(1/4)} * (I * e + 2 * I * f * x + b * \ln(f)) / f^{(1/2)}}{2\sqrt{f}}\right) * \pi^{(1/2)} - 3/16 * (-1)^{(1/4)} * \exp(-I * d + 1/4 * I * (e + I * b * \ln(f))^2 / f) * f^{(-1/2 + a)} * \operatorname{erfi}\left(\frac{1/2 * (-1)^{(1/4)} * (I * e + 2 * I * f * x - b * \ln(f)) / f^{(1/2)}}{2\sqrt{f}}\right) * \pi^{(1/2)}$

Rubi [A] time = 0.52, antiderivative size = 340, normalized size of antiderivative = 1.00, number of steps used = 14, number of rules used = 5, integrand size = 21, $\frac{\text{number of rules}}{\text{integrand size}} = 0.238$, Rules used = {4473, 2287, 2234, 2204, 2205}

$$-\frac{3}{16} \sqrt[4]{-1} \sqrt{\pi} f^{a-\frac{1}{2}} e^{\frac{1}{4}i \left(4d + \frac{(b \log(f) + ie)^2}{f}\right)} \operatorname{Erf}\left(\frac{\sqrt[4]{-1} (b \log(f) + ie + 2ifx)}{2\sqrt{f}}\right) - \left(\frac{1}{16} + \frac{i}{16}\right) \sqrt{\frac{\pi}{6}} f^{a-\frac{1}{2}} e^{\frac{i(b \log(f) + 3ie)^2}{12f} + 3id} \operatorname{Erf}\left(\frac{\sqrt{\frac{\pi}{6}} (b \log(f) + ie + 2ifx)}{2\sqrt{f}}\right)$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[f^{(a + b*x)} * \operatorname{Cos}[d + e*x + f*x^2]^3, x]$

[Out] $(-3 * (-1)^{(1/4)} * E^{((I/4) * (4 * d + (I * e + b * \operatorname{Log}[f])^2 / f))} * f^{(-1/2 + a)} * \operatorname{Sqrt}[\pi] * \operatorname{Erf}\left(\frac{(-1)^{(1/4)} * (I * e + (2 * I) * f * x + b * \operatorname{Log}[f])}{2 * \operatorname{Sqrt}[f]}\right)) / 16 - (1/16 + I/16) * E^{((3 * I) * d + ((I/12) * ((3 * I) * e + b * \operatorname{Log}[f])^2 / f))} * f^{(-1/2 + a)} * \operatorname{Sqrt}[\pi/6] * \operatorname{Erf}\left(\frac{(1/2 + I/2) * ((3 * I) * e + (6 * I) * f * x + b * \operatorname{Log}[f])}{\operatorname{Sqrt}[6] * \operatorname{Sqrt}[f]}\right) - (3 * (-1)^{(1/4)} * E^{((-I) * d + ((I/4) * (e + I * b * \operatorname{Log}[f])^2 / f))} * f^{(-1/2 + a)} * \operatorname{Sqrt}[\pi] * \operatorname{Erfi}\left(\frac{(-1)^{(1/4)} * (I * e + (2 * I) * f * x - b * \operatorname{Log}[f])}{2 * \operatorname{Sqrt}[f]}\right)) / 16 - (1/16 + I/16) * E^{((-3 * I) * d + ((I/12) * (3 * e + I * b * \operatorname{Log}[f])^2 / f))} * f^{(-1/2 + a)} * \operatorname{Sqrt}[\pi/6] * \operatorname{Erfi}\left(\frac{(1/2 + I/2) * ((3 * I) * e + (6 * I) * f * x - b * \operatorname{Log}[f])}{\operatorname{Sqrt}[6] * \operatorname{Sqrt}[f]}\right)$

Rule 2204

$\operatorname{Int}[(F_)^{((a_.) + (b_.) * ((c_.) + (d_.) * (x_.)^2))}, x_Symbol] \rightarrow \operatorname{Simp}[(F^a * \operatorname{Sqrt}[\pi] * \operatorname{Erfi}[(c + d * x) * \operatorname{Rt}[b * \operatorname{Log}[F], 2]]) / (2 * d * \operatorname{Rt}[b * \operatorname{Log}[F], 2]), x] /; \operatorname{FreeQ}\{F, a, b, c, d\}, x] \&\& \operatorname{PosQ}[b]$

Rule 2205

$\operatorname{Int}[(F_)^{((a_.) + (b_.) * ((c_.) + (d_.) * (x_.)^2))}, x_Symbol] \rightarrow \operatorname{Simp}[(F^a * \operatorname{Sqrt}[\pi] * \operatorname{Erf}[(c + d * x) * \operatorname{Rt}[-(b * \operatorname{Log}[F]), 2]]) / (2 * d * \operatorname{Rt}[-(b * \operatorname{Log}[F]), 2]), x] /; \operatorname{FreeQ}\{F, a, b, c, d\}, x] \&\& \operatorname{NegQ}[b]$

Rule 2234

$\operatorname{Int}[(F_)^{((a_.) + (b_.) * (x_.) + (c_.) * (x_.)^2))}, x_Symbol] \rightarrow \operatorname{Dist}[F^{(a - b^2 / (4 * c))}, \operatorname{Int}[F^{((b + 2 * c * x)^2 / (4 * c))}, x], x] /; \operatorname{FreeQ}\{F, a, b, c\}, x]$

Rule 2287

$\operatorname{Int}[(u_.) * (F_)^{(v_.)} * (G_)^{(w_.)}, x_Symbol] \rightarrow \operatorname{With}\{z = v * \operatorname{Log}[F] + w * \operatorname{Log}[G]\}, \operatorname{Int}[u * \operatorname{NormalizeIntegrand}[E^z, x], x] /; \operatorname{BinomialQ}[z, x] \|\| (\operatorname{PolynomialQ}[z, x] \&\& \operatorname{LeQ}[\operatorname{Exponent}[z, x], 2]) /; \operatorname{FreeQ}\{F, G\}, x]$

Rule 4473

`Int[Cos[v_]^(n_.)*(F_)^(u_), x_Symbol] := Int[ExpandTrigToExp[F^u, Cos[v]^n, x], x] /; FreeQ[F, x] && (LinearQ[u, x] || PolyQ[u, x, 2]) && (LinearQ[v, x] || PolyQ[v, x, 2]) && IGtQ[n, 0]`

Rubi steps

$$\begin{aligned} \int f^{a+bx} \cos^3(d+ex+fx^2) dx &= \int \left(\frac{1}{8} e^{-3i(d+ex+fx^2)} f^{a+bx} + \frac{3}{8} \exp(2id+2iex+2ifx^2-3i(d+ex+fx^2)) f^{a+bx} \right. \\ &= \frac{1}{8} \int e^{-3i(d+ex+fx^2)} f^{a+bx} dx + \frac{1}{8} \int \exp(6id+6iex+6ifx^2-3i(d+ex+fx^2)) f^{a+bx} dx \\ &= \frac{1}{8} \int \exp(-3id-3ifx^2+a \log(f)-x(3ie-b \log(f))) dx + \frac{1}{8} \int \exp(3id+3ifx^2+a \log(f)+x(3ie-b \log(f))) dx \\ &= \frac{1}{8} \exp\left(-3id+a \log(f)-\frac{i(-3ie+b \log(f))^2}{12f}\right) \int e^{\frac{i(-3ie-6ifx+b \log(f))^2}{12f}} dx + \frac{1}{8} \exp\left(3id+a \log(f)+\frac{i(3ie-b \log(f))^2}{12f}\right) \int e^{\frac{i(3ie-6ifx+b \log(f))^2}{12f}} dx \\ &= -\frac{3}{16} \sqrt[4]{-1} e^{\frac{1}{4}i\left(4d+\frac{(ie+b \log(f))^2}{f}\right)} f^{-\frac{1}{2}+a} \sqrt{\pi} \operatorname{erf}\left(\frac{\sqrt[4]{-1}(ie+2ifx+b \log(f))}{2\sqrt{f}}\right) - \left(\frac{1}{16}\right) \sqrt[4]{-1} e^{\frac{1}{4}i\left(4d+\frac{(ie+b \log(f))^2}{f}\right)} f^{-\frac{1}{2}+a} \sqrt{\pi} \operatorname{erfi}\left(\frac{\sqrt[4]{-1}(ie+2ifx+b \log(f))}{2\sqrt{f}}\right) \end{aligned}$$

Mathematica [A] time = 1.57, size = 322, normalized size = 0.95

$$\frac{1}{48} \sqrt[4]{-1} \sqrt{\pi} f^{a-\frac{be+f}{2f}} e^{-\frac{i(b^2 \log^2(f)+3e^2)}{4f}} \left(9(\sin(d)-i \cos(d)) e^{\frac{i(b^2 \log^2(f)+e^2)}{2f}} \operatorname{erfi}\left(\frac{\sqrt[4]{-1}(-ib \log(f)+e+2fx)}{2\sqrt{f}}\right) + e^{\frac{ie^2}{f}} \left(-\frac{1}{2} \operatorname{erfi}\left(\frac{\sqrt[4]{-1}(-ib \log(f)+e+2fx)}{2\sqrt{f}}\right) + \frac{1}{2} \operatorname{erf}\left(\frac{\sqrt[4]{-1}(-ib \log(f)+e+2fx)}{2\sqrt{f}}\right) \right) \right)$$

Antiderivative was successfully verified.

[In] Integrate[f^(a + b*x)*Cos[d + e*x + f*x^2]^3,x]

[Out] $((-1)^{(1/4)} f^{(a - (b * e + f) / (2 * f))} * \operatorname{Sqrt}[\pi] * (9 * E^{((I/2) * (e^2 + b^2 * \operatorname{Log}[f]^2)) / f} * \operatorname{Erfi}[((-1)^{(1/4)} * (e + 2 * f * x - I * b * \operatorname{Log}[f])) / (2 * \operatorname{Sqrt}[f])] * ((-1) * \operatorname{Cos}[d] + \operatorname{Sin}[d]) + E^{((I * e^2) / f)} * (-9 * \operatorname{Erfi}[((-1)^{(3/4)} * (e + 2 * f * x + I * b * \operatorname{Log}[f])) / (2 * \operatorname{Sqrt}[f])] * (\operatorname{Cos}[d] - I * \operatorname{Sin}[d]) - \operatorname{Sqrt}[3] * E^{((I/6) * (3 * e^2 + b^2 * \operatorname{Log}[f]^2)) / f} * \operatorname{Erfi}[((-1)^{(3/4)} * (3 * e + 6 * f * x + I * b * \operatorname{Log}[f])) / (2 * \operatorname{Sqrt}[3] * \operatorname{Sqrt}[f])] * (\operatorname{Cos}[3 * d] - I * \operatorname{Sin}[3 * d]) + \operatorname{Sqrt}[3] * E^{((I/3) * b^2 * \operatorname{Log}[f]^2) / f} * \operatorname{Erfi}[((1/2 + I/2) * (3 * e + 6 * f * x - I * b * \operatorname{Log}[f])) / (\operatorname{Sqrt}[6] * \operatorname{Sqrt}[f])] * ((-1) * \operatorname{Cos}[3 * d] + \operatorname{Sin}[3 * d])) / (48 * E^{((I/4) * (3 * e^2 + b^2 * \operatorname{Log}[f]^2)) / f}))$

fricas [B] time = 1.56, size = 629, normalized size = 1.85

$$\sqrt{6} \pi \sqrt{\frac{f}{\pi}} e^{\left(\frac{-ib^2 \log(f)^2 + 9ie^2 - 36idf - 6(be-2af) \log(f)}{12f}\right)} C\left(\frac{\sqrt{6}(6fx+ib \log(f)+3e)\sqrt{\frac{f}{\pi}}}{6f}\right) - \sqrt{6} \pi \sqrt{\frac{f}{\pi}} e^{\left(\frac{ib^2 \log(f)^2 - 9ie^2 + 36idf - 6(be-2af) \log(f)}{12f}\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(b*x+a)*cos(f*x^2+e*x+d)^3,x, algorithm="fricas")

[Out] $1/48 * (\operatorname{sqrt}(6) * \pi * \operatorname{sqrt}(f/\pi)) * e^{(1/12 * (-I * b^2 * \log(f))^2 + 9 * I * e^2 - 36 * I * d * f - 6 * (b * e - 2 * a * f) * \log(f)) / f} * \operatorname{fresnel_cos}(1/6 * \operatorname{sqrt}(6) * (6 * f * x + I * b * \log(f) + 3 * e) * \operatorname{sqrt}(f/\pi) / f) - \operatorname{sqrt}(6) * \pi * \operatorname{sqrt}(f/\pi) * e^{(1/12 * (I * b^2 * \log(f))^2 - 9 * I * e^2 + 36 * I * d * f - 6 * (b * e - 2 * a * f) * \log(f)) / f} * \operatorname{fresnel_cos}(-1/6 * \operatorname{sqrt}(6) * (6 * f * x - I * b * \log(f) + 3 * e) * \operatorname{sqrt}(f/\pi) / f) + 9 * \operatorname{sqrt}(2) * \pi * \operatorname{sqrt}(f/\pi) * e^{(1/4 * (-I * b^2 * \log(f))^2 + I * e^2 - 4 * I * d * f - 2 * (b * e - 2 * a * f) * \log(f)) / f} * \operatorname{fresnel_cos}(1/2 * \operatorname{sqrt}(2) * (6 * f * x + I * b * \log(f) + 3 * e) * \operatorname{sqrt}(f/\pi) / f) - 9 * \operatorname{sqrt}(2) * \pi * \operatorname{sqrt}(f/\pi) * e^{(1/4 * (I * b^2 * \log(f))^2 - I * e^2 + 4 * I * d * f + 2 * (b * e - 2 * a * f) * \log(f)) / f} * \operatorname{fresnel_cos}(1/2 * \operatorname{sqrt}(2) * (-6 * f * x - I * b * \log(f) + 3 * e) * \operatorname{sqrt}(f/\pi) / f)$

```

2)*(2*f*x + I*b*log(f) + e)*sqrt(f/pi)/f) - 9*sqrt(2)*pi*sqrt(f/pi)*e^(1/4*
(I*b^2*log(f)^2 - I*e^2 + 4*I*d*f - 2*(b*e - 2*a*f)*log(f))/f)*fresnel_cos(
-1/2*sqrt(2)*(2*f*x - I*b*log(f) + e)*sqrt(f/pi)/f) - I*sqrt(6)*pi*sqrt(f/p
i)*e^(1/12*(-I*b^2*log(f)^2 + 9*I*e^2 - 36*I*d*f - 6*(b*e - 2*a*f)*log(f))/
f)*fresnel_sin(1/6*sqrt(6)*(6*f*x + I*b*log(f) + 3*e)*sqrt(f/pi)/f) - I*sq
rt(6)*pi*sqrt(f/pi)*e^(1/12*(I*b^2*log(f)^2 - 9*I*e^2 + 36*I*d*f - 6*(b*e -
2*a*f)*log(f))/f)*fresnel_sin(-1/6*sqrt(6)*(6*f*x - I*b*log(f) + 3*e)*sqrt(
f/pi)/f) - 9*I*sqrt(2)*pi*sqrt(f/pi)*e^(1/4*(-I*b^2*log(f)^2 + I*e^2 - 4*I*
d*f - 2*(b*e - 2*a*f)*log(f))/f)*fresnel_sin(1/2*sqrt(2)*(2*f*x + I*b*log(f
) + e)*sqrt(f/pi)/f) - 9*I*sqrt(2)*pi*sqrt(f/pi)*e^(1/4*(I*b^2*log(f)^2 - I
*e^2 + 4*I*d*f - 2*(b*e - 2*a*f)*log(f))/f)*fresnel_sin(-1/2*sqrt(2)*(2*f*x
- I*b*log(f) + e)*sqrt(f/pi)/f))/f

```

giac [B] time = 0.59, size = 763, normalized size = 2.24

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(b*x+a)*cos(f*x^2+e*x+d)^3,x, algorithm="giac")

```

[Out] -3/16*sqrt(2)*sqrt(pi)*erf(-1/8*sqrt(2)*(4*x - (pi*b*sgn(f) - pi*b + 2*I*b*
log(abs(f)) - 2*e)/f)*(-I*f/abs(f) + 1)*sqrt(abs(f)))*e^(1/8*I*pi^2*b^2*sgn
(f)/f + 1/4*pi*b^2*log(abs(f))*sgn(f)/f - 1/8*I*pi^2*b^2/f - 1/4*pi*b^2*log
(abs(f))/f + 1/4*I*b^2*log(abs(f))^2/f - 1/2*I*pi*a*sgn(f) + 1/4*I*pi*b*e*s
gn(f)/f + 1/2*I*pi*a - 1/4*I*pi*b*e/f + a*log(abs(f)) - 1/2*b*e*log(abs(f))
/f + I*d - 1/4*I*e^2/f)/((-I*f/abs(f) + 1)*sqrt(abs(f))) - 1/48*sqrt(6)*sq
rt(pi)*erf(-1/24*sqrt(6)*sqrt(f)*(12*x - (pi*b*sgn(f) - pi*b + 2*I*b*log(abs
(f)) - 6*e)/f)*(-I*f/abs(f) + 1))*e^(1/24*I*pi^2*b^2*sgn(f)/f + 1/12*pi*b^2
*log(abs(f))*sgn(f)/f - 1/24*I*pi^2*b^2/f - 1/12*pi*b^2*log(abs(f))/f + 1/1
2*I*b^2*log(abs(f))^2/f - 1/2*I*pi*a*sgn(f) + 1/4*I*pi*b*e*sgn(f)/f + 1/2*I
*pi*a - 1/4*I*pi*b*e/f + a*log(abs(f)) - 1/2*b*e*log(abs(f))/f + 3*I*d - 3/
4*I*e^2/f)/(sqrt(f)*(-I*f/abs(f) + 1)) - 1/48*sqrt(6)*sqrt(pi)*erf(-1/24*sq
rt(6)*sqrt(f)*(12*x + (pi*b*sgn(f) - pi*b + 2*I*b*log(abs(f)) + 6*e)/f)*(I*
f/abs(f) + 1))*e^(-1/24*I*pi^2*b^2*sgn(f)/f - 1/12*pi*b^2*log(abs(f))*sgn(f
)/f + 1/24*I*pi^2*b^2/f + 1/12*pi*b^2*log(abs(f))/f - 1/12*I*b^2*log(abs(f)
)^2/f - 1/2*I*pi*a*sgn(f) + 1/4*I*pi*b*e*sgn(f)/f + 1/2*I*pi*a - 1/4*I*pi*
b*e/f + a*log(abs(f)) - 1/2*b*e*log(abs(f))/f - 3*I*d + 3/4*I*e^2/f)/(sqrt(f
)*(I*f/abs(f) + 1)) - 3/16*sqrt(2)*sqrt(pi)*erf(-1/8*sqrt(2)*(4*x + (pi*b*s
gn(f) - pi*b + 2*I*b*log(abs(f)) + 2*e)/f)*(I*f/abs(f) + 1)*sqrt(abs(f)))*e
^(-1/8*I*pi^2*b^2*sgn(f)/f - 1/4*pi*b^2*log(abs(f))*sgn(f)/f + 1/8*I*pi^2*b
^2/f + 1/4*pi*b^2*log(abs(f))/f - 1/4*I*b^2*log(abs(f))^2/f - 1/2*I*pi*a*sg
n(f) + 1/4*I*pi*b*e*sgn(f)/f + 1/2*I*pi*a - 1/4*I*pi*b*e/f + a*log(abs(f))
- 1/2*b*e*log(abs(f))/f - I*d + 1/4*I*e^2/f)/((I*f/abs(f) + 1)*sqrt(abs(f))
)

```

maple [A] time = 0.73, size = 307, normalized size = 0.90

$$\frac{\sqrt{\pi} f^a e^{-\frac{i(-9e^2 - 6i \ln(f) b e + \ln(f)^2 b^2 + 36 d f)}{12 f}} \sqrt{3} \operatorname{erf}\left(-\sqrt{3} \sqrt{i f} x + \frac{(b \ln(f) - 3 i e) \sqrt{3}}{6 \sqrt{i f}}\right)}{48 \sqrt{i f}} - \frac{3 \sqrt{\pi} f^a e^{-\frac{i(-e^2 - 2 i \ln(f) b e + \ln(f)^2 b^2 + 4 d f)}{4 f}} \operatorname{erf}\left(-\sqrt{i f} x + \frac{(b \ln(f) - 3 i e) \sqrt{3}}{6 \sqrt{i f}}\right)}{16 \sqrt{i f}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(f^(b*x+a)*cos(f*x^2+e*x+d)^3,x)

```

[Out] -1/48*Pi^(1/2)*f^a*exp(-1/12*I*(-9*e^2-6*I*ln(f)*b*e+ln(f)^2*b^2+36*d*f)/f)
*3^(1/2)/(I*f)^(1/2)*erf(-3^(1/2)*(I*f)^(1/2)*x+1/6*(b*ln(f)-3*I*e)*3^(1/2)
/(I*f)^(1/2))-3/16*Pi^(1/2)*f^a*exp(-1/4*I*(-e^2-2*I*ln(f)*b*e+ln(f)^2*b^2+
4*d*f)/f)/(I*f)^(1/2)*erf(-I*f)^(1/2)*x+1/2*(-I*e+b*ln(f))/(I*f)^(1/2))-3/
16*Pi^(1/2)*f^a*exp(1/4*I*(-e^2+2*I*ln(f)*b*e+ln(f)^2*b^2+4*d*f)/f)/(-I*f)^(

```


$$\frac{(1/2)*\operatorname{erf}(-(-I*f)^{(1/2)*x+1/2*(I*e+b*\ln(f))}/(-I*f)^{(1/2)})-1/16*\pi^{(1/2)*f^a*\exp(1/12*I*(-9*e^2+6*I*\ln(f)*b*e+\ln(f)^2*b^2+36*d*f)/f)/(-3*I*f)^{(1/2)*\operatorname{erf}(-(-3*I*f)^{(1/2)*x+1/2*(3*I*e+b*\ln(f))}/(-3*I*f)^{(1/2)})}$$

maxima [A] time = 0.47, size = 377, normalized size = 1.11

$$3 \cdot 9^{\frac{1}{4}} \sqrt{2} \sqrt{\pi} \left((-i-1) f^a \cos\left(\frac{b^2 \log(f)^2 - 9e^2 + 36df}{12f}\right) - (i+1) f^a \sin\left(\frac{b^2 \log(f)^2 - 9e^2 + 36df}{12f}\right) \right) \operatorname{erf}\left(\frac{i(6ifx - b \log(f) + 3ie)}{6f}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(b*x+a)*cos(f*x^2+e*x+d)^3,x, algorithm="maxima")

[Out]
$$\begin{aligned} & -1/288*(3*9^{(1/4)}*\sqrt{2}*\sqrt{\pi})*((-I-1)*f^a*\cos(1/12*(b^2*\log(f)^2-9*e^2+36*d*f)/f) - (I+1)*f^a*\sin(1/12*(b^2*\log(f)^2-9*e^2+36*d*f)/f) \\ &)*\operatorname{erf}(1/6*I*(6*I*f*x-b*\log(f)+3*I*e)*\sqrt{3*I*f}/f) + ((I+1)*f^a*\cos(1/12*(b^2*\log(f)^2-9*e^2+36*d*f)/f) + (I-1)*f^a*\sin(1/12*(b^2*\log(f)^2-9*e^2+36*d*f)/f) \\ &)*\operatorname{erf}(1/6*I*(6*I*f*x+b*\log(f)+3*I*e)*\sqrt{-3*I*f}/f))*f^{(3/2)} + \sqrt{2}*\sqrt{\pi}*((-(27*I-27)*f^a*\cos(1/4*(b^2*\log(f)^2-e^2+4*d*f)/f) - (27*I+27)*f^a*\sin(1/4*(b^2*\log(f)^2-e^2+4*d*f)/f) \\ &)*\operatorname{erf}(1/2*I*(2*I*f*x-b*\log(f)+I*e)*\sqrt{I*f}/f) + ((27*I+27)*f^a*\cos(1/4*(b^2*\log(f)^2-e^2+4*d*f)/f) + (27*I-27)*f^a*\sin(1/4*(b^2*\log(f)^2-e^2+4*d*f)/f) \\ &)*\operatorname{erf}(1/2*I*(2*I*f*x+b*\log(f)+I*e)*\sqrt{-I*f}/f))*f^{(3/2)})/(f^2*f^{(1/2)*b*e/f}) \end{aligned}$$

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int f^{a+bx} \cos(fx^2 + ex + d)^3 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(f^(a + b*x)*cos(d + e*x + f*x^2)^3,x)

[Out] int(f^(a + b*x)*cos(d + e*x + f*x^2)^3, x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int f^{a+bx} \cos^3(d + ex + fx^2) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f**(b*x+a)*cos(f*x**2+e*x+d)**3,x)

[Out] Integral(f**(a + b*x)*cos(d + e*x + f*x**2)**3, x)

3.116 $\int f^{a+cx^2} \cos(d+ex) dx$

Optimal. Leaf size=147

$$\frac{\sqrt{\pi} f^a e^{\frac{e^2}{4c \log(f)} + id} \operatorname{erfi}\left(\frac{2cx \log(f) + ie}{2\sqrt{c} \sqrt{\log(f)}}\right)}{4\sqrt{c} \sqrt{\log(f)}} - \frac{\sqrt{\pi} f^a e^{\frac{e^2}{4c \log(f)} - id} \operatorname{erfi}\left(\frac{-2cx \log(f) + ie}{2\sqrt{c} \sqrt{\log(f)}}\right)}{4\sqrt{c} \sqrt{\log(f)}}$$

[Out] $\frac{1}{4} \exp(-I*d + 1/4*e^2/c/\ln(f)) * f^a * \operatorname{erfi}\left(\frac{1/2*(-I*e + 2*c*x*\ln(f))}{c^{1/2}/\ln(f)}\right) * \pi^{1/2}/c^{1/2}/\ln(f)^{1/2} + \frac{1}{4} \exp(I*d + 1/4*e^2/c/\ln(f)) * f^a * \operatorname{erfi}\left(\frac{1/2*(I*e + 2*c*x*\ln(f))}{c^{1/2}/\ln(f)}\right) * \pi^{1/2}/c^{1/2}/\ln(f)^{1/2}$

Rubi [A] time = 0.17, antiderivative size = 147, normalized size of antiderivative = 1.00, number of steps used = 8, number of rules used = 4, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} = 0.250$, Rules used = {4473, 2287, 2234, 2204}

$$\frac{\sqrt{\pi} f^a e^{\frac{e^2}{4c \log(f)} + id} \operatorname{Erfi}\left(\frac{2cx \log(f) + ie}{2\sqrt{c} \sqrt{\log(f)}}\right)}{4\sqrt{c} \sqrt{\log(f)}} - \frac{\sqrt{\pi} f^a e^{\frac{e^2}{4c \log(f)} - id} \operatorname{Erfi}\left(\frac{-2cx \log(f) + ie}{2\sqrt{c} \sqrt{\log(f)}}\right)}{4\sqrt{c} \sqrt{\log(f)}}$$

Antiderivative was successfully verified.

[In] `Int[f^(a + c*x^2)*Cos[d + e*x], x]`

[Out] $-\frac{E^{(-I)*d + e^2/(4*c*Log[f])} * f^a * \operatorname{Sqrt}[\pi] * \operatorname{Erfi}[(I*e - 2*c*x*Log[f])/(2*\operatorname{Sqrt}[c]*\operatorname{Sqrt}[Log[f]])]}{4*\operatorname{Sqrt}[c]*\operatorname{Sqrt}[Log[f]]} + \frac{E^{(I*d + e^2/(4*c*Log[f]))} * f^a * \operatorname{Sqrt}[\pi] * \operatorname{Erfi}[(I*e + 2*c*x*Log[f])/(2*\operatorname{Sqrt}[c]*\operatorname{Sqrt}[Log[f]])]}{4*\operatorname{Sqrt}[c]*\operatorname{Sqrt}[Log[f]]}$

Rule 2204

`Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_)^2), x_Symbol] := Simp[(F^a*Sqrt[Pi]*Erfi[(c + d*x)*Rt[b*Log[F], 2]])/(2*d*Rt[b*Log[F], 2]), x] /; FreeQ[{F, a, b, c, d}, x] && PosQ[b]`

Rule 2234

`Int[(F_)^((a_.) + (b_.)*(x_) + (c_.)*(x_)^2), x_Symbol] := Dist[F^(a - b^2/(4*c)), Int[F^((b + 2*c*x)^2/(4*c)), x], x] /; FreeQ[{F, a, b, c}, x]`

Rule 2287

`Int[(u_)*(F_)^(v_)*(G_)^(w_), x_Symbol] := With[{z = v*Log[F] + w*Log[G]}, Int[u*NormalizeIntegrand[E^z, x], x] /; BinomialQ[z, x] || (PolynomialQ[z, x] && LeQ[Exponent[z, x], 2])] /; FreeQ[{F, G}, x]`

Rule 4473

`Int[Cos[v_]^(n_.)*(F_)^(u_), x_Symbol] := Int[ExpandTrigToExp[F^u, Cos[v]^n, x], x] /; FreeQ[F, x] && (LinearQ[u, x] || PolyQ[u, x, 2]) && (LinearQ[v, x] || PolyQ[v, x, 2]) && IGtQ[n, 0]`

Rubi steps

$$\begin{aligned}
\int f^{a+cx^2} \cos(d+ex) dx &= \int \left(\frac{1}{2} e^{-id-ieux} f^{a+cx^2} + \frac{1}{2} e^{id+iex} f^{a+cx^2} \right) dx \\
&= \frac{1}{2} \int e^{-id-ieux} f^{a+cx^2} dx + \frac{1}{2} \int e^{id+iex} f^{a+cx^2} dx \\
&= \frac{1}{2} \int e^{-id-ieux+a \log(f)+cx^2 \log(f)} dx + \frac{1}{2} \int e^{id+iex+a \log(f)+cx^2 \log(f)} dx \\
&= \frac{1}{2} \left(e^{-id+\frac{e^2}{4c \log(f)}} f^a \right) \int e^{\frac{(-ie+2cx \log(f))^2}{4c \log(f)}} dx + \frac{1}{2} \left(e^{id+\frac{e^2}{4c \log(f)}} f^a \right) \int e^{\frac{(ie+2cx \log(f))^2}{4c \log(f)}} dx \\
&= \frac{e^{-id+\frac{e^2}{4c \log(f)}} f^a \sqrt{\pi} \operatorname{erfi} \left(\frac{ie-2cx \log(f)}{2\sqrt{c} \sqrt{\log(f)}} \right)}{4\sqrt{c} \sqrt{\log(f)}} + \frac{e^{id+\frac{e^2}{4c \log(f)}} f^a \sqrt{\pi} \operatorname{erfi} \left(\frac{ie+2cx \log(f)}{2\sqrt{c} \sqrt{\log(f)}} \right)}{4\sqrt{c} \sqrt{\log(f)}}
\end{aligned}$$

Mathematica [A] time = 0.16, size = 116, normalized size = 0.79

$$\frac{\sqrt{\pi} f^a e^{\frac{e^2}{4c \log(f)}} \left((\cos(d) - i \sin(d)) \operatorname{erfi} \left(\frac{2cx \log(f) - ie}{2\sqrt{c} \sqrt{\log(f)}} \right) + (\cos(d) + i \sin(d)) \operatorname{erfi} \left(\frac{2cx \log(f) + ie}{2\sqrt{c} \sqrt{\log(f)}} \right) \right)}{4\sqrt{c} \sqrt{\log(f)}}$$

Antiderivative was successfully verified.

[In] Integrate[f^(a + c*x^2)*Cos[d + e*x], x]

[Out] (E^(e^2/(4*c*Log[f]))*f^a*Sqrt[Pi]*(Erfi[((-I)*e + 2*c*x*Log[f])/(2*Sqrt[c]*Sqrt[Log[f]])]*(Cos[d] - I*Sin[d]) + Erfi[(I*e + 2*c*x*Log[f])/(2*Sqrt[c]*Sqrt[Log[f]])]*(Cos[d] + I*Sin[d])))/(4*Sqrt[c]*Sqrt[Log[f]])

fricas [A] time = 0.82, size = 142, normalized size = 0.97

$$\frac{\sqrt{\pi} \sqrt{-c \log(f)} \operatorname{erf} \left(\frac{(2cx \log(f) + ie) \sqrt{-c \log(f)}}{2c \log(f)} \right) e^{\left(\frac{4ac \log(f)^2 + 4icd \log(f) + e^2}{4c \log(f)} \right)} + \sqrt{\pi} \sqrt{-c \log(f)} \operatorname{erf} \left(\frac{(2cx \log(f) - ie) \sqrt{-c \log(f)}}{2c \log(f)} \right)}{4c \log(f)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(c*x^2+a)*cos(e*x+d), x, algorithm="fricas")

[Out] -1/4*(sqrt(pi)*sqrt(-c*log(f))*erf(1/2*(2*c*x*log(f) + I*e)*sqrt(-c*log(f))/(c*log(f)))*e^(1/4*(4*a*c*log(f)^2 + 4*I*c*d*log(f) + e^2)/(c*log(f))) + sqrt(pi)*sqrt(-c*log(f))*erf(1/2*(2*c*x*log(f) - I*e)*sqrt(-c*log(f))/(c*log(f)))*e^(1/4*(4*a*c*log(f)^2 - 4*I*c*d*log(f) + e^2)/(c*log(f))))/(c*log(f))

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int f^{cx^2+a} \cos(ex+d) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(c*x^2+a)*cos(e*x+d), x, algorithm="giac")

[Out] integrate(f^(c*x^2 + a)*cos(e*x + d), x)

maple [A] time = 0.17, size = 121, normalized size = 0.82

$$\frac{\sqrt{\pi} f^a e^{-\frac{4id \ln(f)c - e^2}{4 \ln(f)c}} \operatorname{erf} \left(\sqrt{-c \ln(f)} x + \frac{ie}{2\sqrt{-c \ln(f)}} \right)}{4\sqrt{-c \ln(f)}} - \frac{\sqrt{\pi} f^a e^{\frac{4id \ln(f)c + e^2}{4 \ln(f)c}} \operatorname{erf} \left(-\sqrt{-c \ln(f)} x + \frac{ie}{2\sqrt{-c \ln(f)}} \right)}{4\sqrt{-c \ln(f)}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(f^(c*x^2+a)*cos(e*x+d),x)`

[Out] $\frac{1}{4}\pi^{1/2}f^a\exp(-1/4*(4I*d*\ln(f)*c-e^2)/\ln(f)/c)/(-c*\ln(f))^{1/2}*\operatorname{erf}((-c*\ln(f))^{1/2}*x+1/2*I*e/(-c*\ln(f))^{1/2})-1/4*\pi^{1/2}f^a*\exp(1/4*(4I*d*\ln(f)*c+e^2)/\ln(f)/c)/(-c*\ln(f))^{1/2}*\operatorname{erf}(-(-c*\ln(f))^{1/2}*x+1/2*I*e/(-c*\ln(f))^{1/2})$

maxima [C] time = 0.35, size = 204, normalized size = 1.39

$$\sqrt{\pi}\left(f^a(\cos(d)-i\sin(d))\operatorname{erf}\left(x\sqrt{-c\log(f)}+\frac{1}{2}ie\frac{1}{\sqrt{-c\log(f)}}\right)e^{\left(\frac{e^2}{4c\log(f)}\right)}+f^a(\cos(d)+i\sin(d))\operatorname{erf}\left(x\sqrt{-c\log(f)}\right)\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(f^(c*x^2+a)*cos(e*x+d),x, algorithm="maxima")`

[Out] $-1/8*\sqrt{\pi}*(f^a*(\cos(d)-I*\sin(d))*\operatorname{erf}(x*\operatorname{conjugate}(\sqrt{-c*\log(f)}))+1/2*I*e*\operatorname{conjugate}(1/\sqrt{-c*\log(f)}))*e^{1/4*e^2/(c*\log(f))}+f^a*(\cos(d)+I*\sin(d))*\operatorname{erf}(x*\operatorname{conjugate}(\sqrt{-c*\log(f)}))-1/2*I*e*\operatorname{conjugate}(1/\sqrt{-c*\log(f)}))*e^{1/4*e^2/(c*\log(f))}-f^a*(\cos(d)+I*\sin(d))*\operatorname{erf}(1/2*(2*c*x*\log(f)+I*e)/\sqrt{-c*\log(f)})*e^{1/4*e^2/(c*\log(f))}-f^a*(\cos(d)-I*\sin(d))*\operatorname{erf}(1/2*(2*c*x*\log(f)-I*e)/\sqrt{-c*\log(f)})*e^{1/4*e^2/(c*\log(f))})*\sqrt{-c*\log(f)}/(c*\log(f))$

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int f^{cx^2+a} \cos(d+ex) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(f^(a+c*x^2)*cos(d+e*x),x)`

[Out] `int(f^(a+c*x^2)*cos(d+e*x),x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int f^{a+cx^2} \cos(d+ex) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(f**(c*x**2+a)*cos(e*x+d),x)`

[Out] `Integral(f**(a+c*x**2)*cos(d+e*x),x)`

3.117 $\int f^{a+cx^2} \cos^2(d+ex) dx$

Optimal. Leaf size=171

$$\frac{\sqrt{\pi} f^a e^{\frac{e^2}{c \log(f)}}^{-2id} \operatorname{erfi}\left(\frac{-cx \log(f)+ie}{\sqrt{c} \sqrt{\log(f)}}\right)}{8\sqrt{c} \sqrt{\log(f)}} + \frac{\sqrt{\pi} f^a e^{\frac{e^2}{c \log(f)}}^{+2id} \operatorname{erfi}\left(\frac{cx \log(f)+ie}{\sqrt{c} \sqrt{\log(f)}}\right)}{8\sqrt{c} \sqrt{\log(f)}} + \frac{\sqrt{\pi} f^a \operatorname{erfi}\left(\sqrt{c} x \sqrt{\log(f)}\right)}{4\sqrt{c} \sqrt{\log(f)}}$$

[Out] $1/8 \cdot \exp(-2 \cdot I \cdot d + e^2/c/\ln(f)) \cdot f^a \cdot \operatorname{erfi}((-I \cdot e + c \cdot x \cdot \ln(f))/c^{1/2}/\ln(f)^{1/2}) \cdot \pi^{1/2}/c^{1/2}/\ln(f)^{1/2} + 1/8 \cdot \exp(2 \cdot I \cdot d + e^2/c/\ln(f)) \cdot f^a \cdot \operatorname{erfi}(I \cdot e + c \cdot x \cdot \ln(f))/c^{1/2}/\ln(f)^{1/2} \cdot \pi^{1/2}/c^{1/2}/\ln(f)^{1/2} + 1/4 \cdot f^a \cdot \operatorname{erfi}(x \cdot c^{1/2} \cdot \ln(f)^{1/2}) \cdot \pi^{1/2}/c^{1/2}/\ln(f)^{1/2}$

Rubi [A] time = 0.20, antiderivative size = 171, normalized size of antiderivative = 1.00, number of steps used = 9, number of rules used = 4, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.222$, Rules used = {4473, 2204, 2287, 2234}

$$\frac{\sqrt{\pi} f^a e^{\frac{e^2}{c \log(f)}}^{-2id} \operatorname{Erfi}\left(\frac{-cx \log(f)+ie}{\sqrt{c} \sqrt{\log(f)}}\right)}{8\sqrt{c} \sqrt{\log(f)}} + \frac{\sqrt{\pi} f^a e^{\frac{e^2}{c \log(f)}}^{+2id} \operatorname{Erfi}\left(\frac{cx \log(f)+ie}{\sqrt{c} \sqrt{\log(f)}}\right)}{8\sqrt{c} \sqrt{\log(f)}} + \frac{\sqrt{\pi} f^a \operatorname{Erfi}\left(\sqrt{c} x \sqrt{\log(f)}\right)}{4\sqrt{c} \sqrt{\log(f)}}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[f^{(a + c \cdot x^2)} \cdot \operatorname{Cos}[d + e \cdot x]^2, x]$

[Out] $(f^a \cdot \operatorname{Sqrt}[\pi] \cdot \operatorname{Erfi}[\operatorname{Sqrt}[c] \cdot x \cdot \operatorname{Sqrt}[\operatorname{Log}[f]]]) / (4 \cdot \operatorname{Sqrt}[c] \cdot \operatorname{Sqrt}[\operatorname{Log}[f]]) - (E^{(-2 \cdot I) \cdot d + e^2/(c \cdot \operatorname{Log}[f])} \cdot f^a \cdot \operatorname{Sqrt}[\pi] \cdot \operatorname{Erfi}[(I \cdot e - c \cdot x \cdot \operatorname{Log}[f]) / (\operatorname{Sqrt}[c] \cdot \operatorname{Sqrt}[\operatorname{Log}[f]])]) / (8 \cdot \operatorname{Sqrt}[c] \cdot \operatorname{Sqrt}[\operatorname{Log}[f]]) + (E^{((2 \cdot I) \cdot d + e^2/(c \cdot \operatorname{Log}[f])} \cdot f^a \cdot \operatorname{Sqrt}[\pi] \cdot \operatorname{Erfi}[(I \cdot e + c \cdot x \cdot \operatorname{Log}[f]) / (\operatorname{Sqrt}[c] \cdot \operatorname{Sqrt}[\operatorname{Log}[f]])]) / (8 \cdot \operatorname{Sqrt}[c] \cdot \operatorname{Sqrt}[\operatorname{Log}[f]])$

Rule 2204

$\operatorname{Int}[(F_)^{((a_.) + (b_.) \cdot ((c_.) + (d_.) \cdot (x_.))^2)}, x_Symbol] \rightarrow \operatorname{Simp}[(F^a \cdot \operatorname{Sqrt}[\pi] \cdot \operatorname{Erfi}[(c + d \cdot x) \cdot \operatorname{Rt}[b \cdot \operatorname{Log}[F], 2]]) / (2 \cdot d \cdot \operatorname{Rt}[b \cdot \operatorname{Log}[F], 2]), x] /; \operatorname{FreeQ}\{F, a, b, c, d\}, x] \ \&\& \operatorname{PosQ}[b]$

Rule 2234

$\operatorname{Int}[(F_)^{((a_.) + (b_.) \cdot (x_.) + (c_.) \cdot (x_.)^2)}, x_Symbol] \rightarrow \operatorname{Dist}[F^{(a - b^2/(4 \cdot c))}, \operatorname{Int}[F^{((b + 2 \cdot c \cdot x)^2/(4 \cdot c))}, x], x] /; \operatorname{FreeQ}\{F, a, b, c\}, x]$

Rule 2287

$\operatorname{Int}[(u_.) \cdot (F_)^{(v_.)} \cdot (G_)^{(w_.)}, x_Symbol] \rightarrow \operatorname{With}\{z = v \cdot \operatorname{Log}[F] + w \cdot \operatorname{Log}[G]\}, \operatorname{Int}[u \cdot \operatorname{NormalizeIntegrand}[E^z, x], x] /; \operatorname{BinomialQ}[z, x] \ || \ (\operatorname{PolynomialQ}[z, x] \ \&\& \operatorname{LeQ}[\operatorname{Exponent}[z, x], 2]) /; \operatorname{FreeQ}\{F, G\}, x]$

Rule 4473

$\operatorname{Int}[\operatorname{Cos}[v_]^{(n_.)} \cdot (F_)^{(u_.)}, x_Symbol] \rightarrow \operatorname{Int}[\operatorname{ExpandTrigToExp}[F^u, \operatorname{Cos}[v]^n, x], x] /; \operatorname{FreeQ}[F, x] \ \&\& \ (\operatorname{LinearQ}[u, x] \ || \ \operatorname{PolyQ}[u, x, 2]) \ \&\& \ (\operatorname{LinearQ}[v, x] \ || \ \operatorname{PolyQ}[v, x, 2]) \ \&\& \ \operatorname{IGtQ}[n, 0]$

Rubi steps

$$\begin{aligned}
\int f^{a+cx^2} \cos^2(d+ex) dx &= \int \left(\frac{1}{2} f^{a+cx^2} + \frac{1}{4} e^{-2id-2iex} f^{a+cx^2} + \frac{1}{4} e^{2id+2iex} f^{a+cx^2} \right) dx \\
&= \frac{1}{4} \int e^{-2id-2iex} f^{a+cx^2} dx + \frac{1}{4} \int e^{2id+2iex} f^{a+cx^2} dx + \frac{1}{2} \int f^{a+cx^2} dx \\
&= \frac{f^a \sqrt{\pi} \operatorname{erfi}(\sqrt{c} x \sqrt{\log(f)})}{4\sqrt{c} \sqrt{\log(f)}} + \frac{1}{4} \int e^{-2id-2iex+a \log(f)+cx^2 \log(f)} dx + \frac{1}{4} \int e^{2id+2iex+a \log(f)+cx^2 \log(f)} dx \\
&= \frac{f^a \sqrt{\pi} \operatorname{erfi}(\sqrt{c} x \sqrt{\log(f)})}{4\sqrt{c} \sqrt{\log(f)}} + \frac{1}{4} \left(e^{-2id+\frac{e^2}{c \log(f)}} f^a \right) \int e^{\frac{(-2ie+2cx \log(f))^2}{4c \log(f)}} dx + \frac{1}{4} \left(e^{2id+\frac{e^2}{c \log(f)}} f^a \right) \int e^{\frac{(2ie+2cx \log(f))^2}{4c \log(f)}} dx \\
&= \frac{f^a \sqrt{\pi} \operatorname{erfi}(\sqrt{c} x \sqrt{\log(f)})}{4\sqrt{c} \sqrt{\log(f)}} - \frac{e^{-2id+\frac{e^2}{c \log(f)}} f^a \sqrt{\pi} \operatorname{erfi}\left(\frac{ie-cx \log(f)}{\sqrt{c} \sqrt{\log(f)}}\right)}{8\sqrt{c} \sqrt{\log(f)}} + \frac{e^{2id+\frac{e^2}{c \log(f)}} f^a \sqrt{\pi} \operatorname{erfi}\left(\frac{ie+cx \log(f)}{\sqrt{c} \sqrt{\log(f)}}\right)}{8\sqrt{c} \sqrt{\log(f)}}
\end{aligned}$$

Mathematica [A] time = 0.25, size = 131, normalized size = 0.77

$$\frac{\sqrt{\pi} f^a \left(2 \operatorname{erfi}(\sqrt{c} x \sqrt{\log(f)}) + e^{\frac{e^2}{c \log(f)}} \left((\cos(2d) - i \sin(2d)) \operatorname{erfi}\left(\frac{cx \log(f) - ie}{\sqrt{c} \sqrt{\log(f)}}\right) + (\cos(2d) + i \sin(2d)) \operatorname{erfi}\left(\frac{cx \log(f) + ie}{\sqrt{c} \sqrt{\log(f)}}\right) \right) \right)}{8\sqrt{c} \sqrt{\log(f)}}$$

Antiderivative was successfully verified.

[In] Integrate[f^(a + c*x^2)*Cos[d + e*x]^2,x]

[Out] (f^a*Sqrt[Pi]*(2*Erfi[Sqrt[c]*x*Sqrt[Log[f]]] + E^(e^2/(c*Log[f]))*(Erfi[(-I)*e + c*x*Log[f]]/(Sqrt[c]*Sqrt[Log[f]])*(Cos[2*d] - I*Sin[2*d]) + Erfi[(I*e + c*x*Log[f]]/(Sqrt[c]*Sqrt[Log[f]])*(Cos[2*d] + I*Sin[2*d])))]/(8*Sqrt[c]*Sqrt[Log[f]]))

fricas [A] time = 0.62, size = 159, normalized size = 0.93

$$\frac{2 \sqrt{\pi} \sqrt{-c \log(f)} f^a \operatorname{erf}(\sqrt{-c \log(f)} x) + \sqrt{\pi} \sqrt{-c \log(f)} \operatorname{erf}\left(\frac{(cx \log(f) + ie) \sqrt{-c \log(f)}}{c \log(f)}\right) e^{\left(\frac{ac \log(f)^2 + 2icd \log(f) + e^2}{c \log(f)}\right)} + \sqrt{\pi} \sqrt{-c \log(f)} \operatorname{erf}\left(\frac{(cx \log(f) - ie) \sqrt{-c \log(f)}}{c \log(f)}\right) e^{\left(\frac{ac \log(f)^2 - 2icd \log(f) + e^2}{c \log(f)}\right)}}{8c \log(f)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(c*x^2+a)*cos(e*x+d)^2,x, algorithm="fricas")

[Out] -1/8*(2*sqrt(pi)*sqrt(-c*log(f))*f^a*erf(sqrt(-c*log(f))*x) + sqrt(pi)*sqrt(-c*log(f))*erf((c*x*log(f) + I*e)*sqrt(-c*log(f))/(c*log(f)))*e^((a*c*log(f)^2 + 2*I*c*d*log(f) + e^2)/(c*log(f))) + sqrt(pi)*sqrt(-c*log(f))*erf((c*x*log(f) - I*e)*sqrt(-c*log(f))/(c*log(f)))*e^((a*c*log(f)^2 - 2*I*c*d*log(f) + e^2)/(c*log(f))))/(c*log(f))

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int f^{cx^2+a} \cos(ex+d)^2 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(c*x^2+a)*cos(e*x+d)^2,x, algorithm="giac")

[Out] integrate(f^(c*x^2 + a)*cos(e*x + d)^2, x)

maple [A] time = 0.24, size = 145, normalized size = 0.85

$$\frac{\sqrt{\pi} f^a e^{-\frac{2id \ln(f)c - e^2}{\ln(f)c}} \operatorname{erf}\left(\sqrt{-c \ln(f)} x + \frac{ie}{\sqrt{-c \ln(f)}}\right)}{8\sqrt{-c \ln(f)}} - \frac{\sqrt{\pi} f^a e^{\frac{2id \ln(f)c + e^2}{\ln(f)c}} \operatorname{erf}\left(-\sqrt{-c \ln(f)} x + \frac{ie}{\sqrt{-c \ln(f)}}\right)}{8\sqrt{-c \ln(f)}} + \frac{f^a \sqrt{\pi} \operatorname{erf}\left(\sqrt{-c \ln(f)} x\right)}{4\sqrt{-c \ln(f)}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(f^(c*x^2+a)*cos(e*x+d)^2,x)

[Out] 1/8*Pi^(1/2)*f^a*exp(-(2*I*d*ln(f)*c-e^2)/ln(f)/c)/(-c*ln(f))^(1/2)*erf((-c*ln(f))^(1/2)*x+I*e/(-c*ln(f))^(1/2))-1/8*Pi^(1/2)*f^a*exp((2*I*d*ln(f)*c+e^2)/ln(f)/c)/(-c*ln(f))^(1/2)*erf(-(-c*ln(f))^(1/2)*x+I*e/(-c*ln(f))^(1/2))+1/4*f^a*Pi^(1/2)/(-c*ln(f))^(1/2)*erf((-c*ln(f))^(1/2)*x)

maxima [C] time = 0.36, size = 236, normalized size = 1.38

$$\sqrt{\pi} \left(f^a (\cos(2d) - i \sin(2d)) \operatorname{erf}\left(x\sqrt{-c \log(f)} + ie \frac{1}{\sqrt{-c \log(f)}}\right) e^{\left(\frac{e^2}{c \log(f)}\right)} + f^a (\cos(2d) + i \sin(2d)) \operatorname{erf}\left(x\sqrt{-c \log(f)} - ie \frac{1}{\sqrt{-c \log(f)}}\right) e^{\left(\frac{e^2}{c \log(f)}\right)} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(c*x^2+a)*cos(e*x+d)^2,x, algorithm="maxima")

[Out] 1/16*sqrt(pi)*(f^a*(cos(2*d) - I*sin(2*d))*erf(x*conjugate(sqrt(-c*log(f)))) + I*e*conjugate(1/sqrt(-c*log(f))))*e^(e^2/(c*log(f))) + f^a*(cos(2*d) + I*sin(2*d))*erf(x*conjugate(sqrt(-c*log(f))) - I*e*conjugate(1/sqrt(-c*log(f))))*e^(e^2/(c*log(f))) - f^a*(cos(2*d) + I*sin(2*d))*erf((c*x*log(f) + I*e)/sqrt(-c*log(f)))*e^(e^2/(c*log(f))) - f^a*(cos(2*d) - I*sin(2*d))*erf((c*x*log(f) - I*e)/sqrt(-c*log(f)))*e^(e^2/(c*log(f))) + 2*f^a*erf(x*conjugate(sqrt(-c*log(f)))) + 2*f^a*erf(sqrt(-c*log(f))*x)/sqrt(-c*log(f))

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int f^{cx^2+a} \cos(d + ex)^2 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(f^(a + c*x^2)*cos(d + e*x)^2,x)

[Out] int(f^(a + c*x^2)*cos(d + e*x)^2, x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int f^{a+cx^2} \cos^2(d + ex) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f**(c*x**2+a)*cos(e*x+d)**2,x)

[Out] Integral(f**(a + c*x**2)*cos(d + e*x)**2, x)

3.118 $\int f^{a+cx^2} \cos^3(d+ex) dx$

Optimal. Leaf size=293

$$\frac{3\sqrt{\pi} f^a e^{\frac{e^2}{4c \log(f)} - id} \operatorname{erfi}\left(\frac{-2cx \log(f) + ie}{2\sqrt{c} \sqrt{\log(f)}}\right) - \sqrt{\pi} f^a e^{\frac{9e^2}{4c \log(f)} - 3id} \operatorname{erfi}\left(\frac{-2cx \log(f) + 3ie}{2\sqrt{c} \sqrt{\log(f)}}\right) + 3\sqrt{\pi} f^a e^{\frac{e^2}{4c \log(f)} + id} \operatorname{erfi}\left(\frac{2cx \log(f) + ie}{2\sqrt{c} \sqrt{\log(f)}}\right)}{16\sqrt{c} \sqrt{\log(f)} - 16\sqrt{c} \sqrt{\log(f)} + 16\sqrt{c} \sqrt{\log(f)}}$$

[Out] $3/16 \cdot \exp(-I \cdot d + 1/4 \cdot e^2/c/\ln(f)) \cdot f^a \cdot \operatorname{erfi}(1/2 \cdot (-I \cdot e + 2 \cdot c \cdot x \cdot \ln(f))/c^{(1/2)}/\ln(f)^{(1/2)}) \cdot \pi^{(1/2)}/c^{(1/2)}/\ln(f)^{(1/2)} + 1/16 \cdot \exp(-3 \cdot I \cdot d + 9/4 \cdot e^2/c/\ln(f)) \cdot f^a \cdot \operatorname{erfi}(1/2 \cdot (-3 \cdot I \cdot e + 2 \cdot c \cdot x \cdot \ln(f))/c^{(1/2)}/\ln(f)^{(1/2)}) \cdot \pi^{(1/2)}/c^{(1/2)}/\ln(f)^{(1/2)} + 3/16 \cdot \exp(I \cdot d + 1/4 \cdot e^2/c/\ln(f)) \cdot f^a \cdot \operatorname{erfi}(1/2 \cdot (I \cdot e + 2 \cdot c \cdot x \cdot \ln(f))/c^{(1/2)}/\ln(f)^{(1/2)}) \cdot \pi^{(1/2)}/c^{(1/2)}/\ln(f)^{(1/2)} + 1/16 \cdot \exp(3 \cdot I \cdot d + 9/4 \cdot e^2/c/\ln(f)) \cdot f^a \cdot \operatorname{erfi}(1/2 \cdot (3 \cdot I \cdot e + 2 \cdot c \cdot x \cdot \ln(f))/c^{(1/2)}/\ln(f)^{(1/2)}) \cdot \pi^{(1/2)}/c^{(1/2)}/\ln(f)^{(1/2)}$

Rubi [A] time = 0.33, antiderivative size = 293, normalized size of antiderivative = 1.00, number of steps used = 14, number of rules used = 4, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.222$, Rules used = {4473, 2287, 2234, 2204}

$$\frac{3\sqrt{\pi} f^a e^{\frac{e^2}{4c \log(f)} - id} \operatorname{Erfi}\left(\frac{-2cx \log(f) + ie}{2\sqrt{c} \sqrt{\log(f)}}\right) - \sqrt{\pi} f^a e^{\frac{9e^2}{4c \log(f)} - 3id} \operatorname{Erfi}\left(\frac{-2cx \log(f) + 3ie}{2\sqrt{c} \sqrt{\log(f)}}\right) + 3\sqrt{\pi} f^a e^{\frac{e^2}{4c \log(f)} + id} \operatorname{Erfi}\left(\frac{2cx \log(f) + ie}{2\sqrt{c} \sqrt{\log(f)}}\right)}{16\sqrt{c} \sqrt{\log(f)} - 16\sqrt{c} \sqrt{\log(f)} + 16\sqrt{c} \sqrt{\log(f)}}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[f^{(a + c \cdot x^2)} \cdot \operatorname{Cos}[d + e \cdot x]^3, x]$

[Out] $(-3 \cdot E^{((-I) \cdot d + e^2/(4 \cdot c \cdot \operatorname{Log}[f]))} \cdot f^a \cdot \operatorname{Sqrt}[\pi] \cdot \operatorname{Erfi}[(I \cdot e - 2 \cdot c \cdot x \cdot \operatorname{Log}[f])/(2 \cdot \operatorname{Sqrt}[c] \cdot \operatorname{Sqrt}[\operatorname{Log}[f]])]) / (16 \cdot \operatorname{Sqrt}[c] \cdot \operatorname{Sqrt}[\operatorname{Log}[f]]) - (E^{((-3 \cdot I) \cdot d + (9 \cdot e^2)/(4 \cdot c \cdot \operatorname{Log}[f]))} \cdot f^a \cdot \operatorname{Sqrt}[\pi] \cdot \operatorname{Erfi}[(3 \cdot I \cdot e - 2 \cdot c \cdot x \cdot \operatorname{Log}[f])/(2 \cdot \operatorname{Sqrt}[c] \cdot \operatorname{Sqrt}[\operatorname{Log}[f]])]) / (16 \cdot \operatorname{Sqrt}[c] \cdot \operatorname{Sqrt}[\operatorname{Log}[f]]) + (3 \cdot E^{(I \cdot d + e^2/(4 \cdot c \cdot \operatorname{Log}[f]))} \cdot f^a \cdot \operatorname{Sqrt}[\pi] \cdot \operatorname{Erfi}[(I \cdot e + 2 \cdot c \cdot x \cdot \operatorname{Log}[f])/(2 \cdot \operatorname{Sqrt}[c] \cdot \operatorname{Sqrt}[\operatorname{Log}[f]])]) / (16 \cdot \operatorname{Sqrt}[c] \cdot \operatorname{Sqrt}[\operatorname{Log}[f]]) + (E^{((3 \cdot I) \cdot d + (9 \cdot e^2)/(4 \cdot c \cdot \operatorname{Log}[f]))} \cdot f^a \cdot \operatorname{Sqrt}[\pi] \cdot \operatorname{Erfi}[(3 \cdot I \cdot e + 2 \cdot c \cdot x \cdot \operatorname{Log}[f])/(2 \cdot \operatorname{Sqrt}[c] \cdot \operatorname{Sqrt}[\operatorname{Log}[f]])]) / (16 \cdot \operatorname{Sqrt}[c] \cdot \operatorname{Sqrt}[\operatorname{Log}[f]])$

Rule 2204

$\operatorname{Int}[(F_)^{((a_.) + (b_.) \cdot ((c_.) + (d_.) \cdot (x_.)^2))}, x_Symbol] := \operatorname{Simp}[(F^a \cdot \operatorname{Sqrt}[\pi] \cdot \operatorname{Erfi}[(c + d \cdot x) \cdot \operatorname{Rt}[b \cdot \operatorname{Log}[F], 2]]) / (2 \cdot d \cdot \operatorname{Rt}[b \cdot \operatorname{Log}[F], 2]), x] /; \operatorname{FreeQ}\{F, a, b, c, d\}, x] \ \&\& \ \operatorname{PosQ}[b]$

Rule 2234

$\operatorname{Int}[(F_)^{((a_.) + (b_.) \cdot (x_.) + (c_.) \cdot (x_.)^2))}, x_Symbol] := \operatorname{Dist}[F^{(a - b^2/(4 \cdot c))}, \operatorname{Int}[F^{((b + 2 \cdot c \cdot x)^2/(4 \cdot c))}, x], x] /; \operatorname{FreeQ}\{F, a, b, c\}, x]$

Rule 2287

$\operatorname{Int}[(u_.) \cdot (F_)^{(v_.)} \cdot (G_)^{(w_.)}, x_Symbol] := \operatorname{With}\{z = v \cdot \operatorname{Log}[F] + w \cdot \operatorname{Log}[G]\}, \operatorname{Int}[u \cdot \operatorname{NormalizeIntegrand}[E^z, x], x] /; \operatorname{BinomialQ}[z, x] \ || \ (\operatorname{PolynomialQ}[z, x] \ \&\& \ \operatorname{LeQ}[\operatorname{Exponent}[z, x], 2]) /; \operatorname{FreeQ}\{F, G\}, x]$

Rule 4473

$\operatorname{Int}[\operatorname{Cos}[v_]^{(n_.)} \cdot (F_)^{(u_.)}, x_Symbol] := \operatorname{Int}[\operatorname{ExpandTrigToExp}[F^u \cdot \operatorname{Cos}[v]^n], x] /; \operatorname{FreeQ}[F, x] \ \&\& \ (\operatorname{LinearQ}[u, x] \ || \ \operatorname{PolyQ}[u, x, 2]) \ \&\& \ (\operatorname{LinearQ}[v, x] \ || \ \operatorname{PolyQ}[v, x, 2]) \ \&\& \ \operatorname{IGtQ}[n, 0]$

Rubi steps

$$\begin{aligned}
\int f^{a+cx^2} \cos^3(d+ex) dx &= \int \left(\frac{3}{8} e^{-id-3iex} f^{a+cx^2} + \frac{3}{8} e^{id+3iex} f^{a+cx^2} + \frac{1}{8} e^{-3id-3iex} f^{a+cx^2} + \frac{1}{8} e^{3id+3iex} f^{a+cx^2} \right) dx \\
&= \frac{1}{8} \int e^{-3id-3iex} f^{a+cx^2} dx + \frac{1}{8} \int e^{3id+3iex} f^{a+cx^2} dx + \frac{3}{8} \int e^{-id-3iex} f^{a+cx^2} dx + \frac{3}{8} \int e^{id+3iex} f^{a+cx^2} dx \\
&= \frac{1}{8} \int e^{-3id-3iex+a \log(f)+cx^2 \log(f)} dx + \frac{1}{8} \int e^{3id+3iex+a \log(f)+cx^2 \log(f)} dx + \frac{3}{8} \int e^{-id-3iex+a \log(f)+cx^2 \log(f)} dx + \frac{3}{8} \int e^{id+3iex+a \log(f)+cx^2 \log(f)} dx \\
&= \frac{1}{8} \left(3e^{-id+\frac{e^2}{4c \log(f)}} f^a \right) \int e^{\frac{(-ie+2cx \log(f))^2}{4c \log(f)}} dx + \frac{1}{8} \left(3e^{id+\frac{e^2}{4c \log(f)}} f^a \right) \int e^{\frac{(ie+2cx \log(f))^2}{4c \log(f)}} dx + \frac{1}{8} \left(3e^{-id+\frac{e^2}{4c \log(f)}} f^a \right) \int e^{\frac{(ie-2cx \log(f))^2}{4c \log(f)}} dx + \frac{1}{8} \left(3e^{id+\frac{e^2}{4c \log(f)}} f^a \right) \int e^{\frac{(-ie-2cx \log(f))^2}{4c \log(f)}} dx \\
&= -\frac{3e^{-id+\frac{e^2}{4c \log(f)}} f^a \sqrt{\pi} \operatorname{erfi}\left(\frac{ie-2cx \log(f)}{2\sqrt{c} \sqrt{\log(f)}}\right)}{16\sqrt{c} \sqrt{\log(f)}} - \frac{3e^{-3id+\frac{9e^2}{4c \log(f)}} f^a \sqrt{\pi} \operatorname{erfi}\left(\frac{3ie-2cx \log(f)}{2\sqrt{c} \sqrt{\log(f)}}\right)}{16\sqrt{c} \sqrt{\log(f)}} + \frac{3e^{id+\frac{e^2}{4c \log(f)}} f^a \sqrt{\pi} \operatorname{erfi}\left(\frac{ie+2cx \log(f)}{2\sqrt{c} \sqrt{\log(f)}}\right)}{16\sqrt{c} \sqrt{\log(f)}} + \frac{3e^{3id+\frac{9e^2}{4c \log(f)}} f^a \sqrt{\pi} \operatorname{erfi}\left(\frac{3ie+2cx \log(f)}{2\sqrt{c} \sqrt{\log(f)}}\right)}{16\sqrt{c} \sqrt{\log(f)}}
\end{aligned}$$

Mathematica [A] time = 0.42, size = 218, normalized size = 0.74

$$\frac{\sqrt{\pi} f^a e^{\frac{e^2}{4c \log(f)}} \left(e^{\frac{2e^2}{c \log(f)}} \left((\cos(3d) - i \sin(3d)) \operatorname{erfi}\left(\frac{2cx \log(f) - 3ie}{2\sqrt{c} \sqrt{\log(f)}}\right) + (\cos(3d) + i \sin(3d)) \operatorname{erfi}\left(\frac{2cx \log(f) + 3ie}{2\sqrt{c} \sqrt{\log(f)}}\right) \right) + 3 \left(e^{-id+\frac{e^2}{4c \log(f)}} f^a \sqrt{\pi} \operatorname{erfi}\left(\frac{ie-2cx \log(f)}{2\sqrt{c} \sqrt{\log(f)}}\right) + e^{id+\frac{e^2}{4c \log(f)}} f^a \sqrt{\pi} \operatorname{erfi}\left(\frac{ie+2cx \log(f)}{2\sqrt{c} \sqrt{\log(f)}}\right) \right)}{16\sqrt{c} \sqrt{\log(f)}}$$

Antiderivative was successfully verified.

[In] Integrate[f^(a + c*x^2)*Cos[d + e*x]^3,x]

[Out] (E^(e^2/(4*c*Log[f]))*f^a*Sqrt[Pi]*(3*Erfi[((-I)*e + 2*c*x*Log[f])/(2*Sqrt[c]*Sqrt[Log[f]])]*(Cos[d] - I*Sin[d]) + 3*Erfi[(I*e + 2*c*x*Log[f])/(2*Sqrt[c]*Sqrt[Log[f]])]*(Cos[d] + I*Sin[d]) + E^((2*e^2)/(c*Log[f]))*(Erfi[((-3*I)*e + 2*c*x*Log[f])/(2*Sqrt[c]*Sqrt[Log[f]])]*(Cos[3*d] - I*Sin[3*d]) + Erfi[((3*I)*e + 2*c*x*Log[f])/(2*Sqrt[c]*Sqrt[Log[f]])]*(Cos[3*d] + I*Sin[3*d])))/(16*Sqrt[c]*Sqrt[Log[f]])

fricas [A] time = 1.36, size = 280, normalized size = 0.96

$$\frac{\sqrt{\pi} \sqrt{-c \log(f)} \operatorname{erf}\left(\frac{(2cx \log(f) + 3ie) \sqrt{-c \log(f)}}{2c \log(f)}\right) e^{\left(\frac{4ac \log(f)^2 + 12icd \log(f) + 9e^2}{4c \log(f)}\right)} + 3 \sqrt{\pi} \sqrt{-c \log(f)} \operatorname{erf}\left(\frac{(2cx \log(f) + ie) \sqrt{-c \log(f)}}{2c \log(f)}\right)}{16\sqrt{c} \sqrt{\log(f)}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(c*x^2+a)*cos(e*x+d)^3,x, algorithm="fricas")

[Out] -1/16*(sqrt(pi)*sqrt(-c*log(f))*erf(1/2*(2*c*x*log(f) + 3*I*e)*sqrt(-c*log(f))/(c*log(f)))*e^(1/4*(4*a*c*log(f)^2 + 12*I*c*d*log(f) + 9*e^2)/(c*log(f))) + 3*sqrt(pi)*sqrt(-c*log(f))*erf(1/2*(2*c*x*log(f) + I*e)*sqrt(-c*log(f))/(c*log(f)))*e^(1/4*(4*a*c*log(f)^2 + 4*I*c*d*log(f) + e^2)/(c*log(f))) + 3*sqrt(pi)*sqrt(-c*log(f))*erf(1/2*(2*c*x*log(f) - I*e)*sqrt(-c*log(f))/(c*log(f)))*e^(1/4*(4*a*c*log(f)^2 - 4*I*c*d*log(f) + e^2)/(c*log(f))) + sqrt(pi)*sqrt(-c*log(f))*erf(1/2*(2*c*x*log(f) - 3*I*e)*sqrt(-c*log(f))/(c*log(f)))*e^(1/4*(4*a*c*log(f)^2 - 12*I*c*d*log(f) + 9*e^2)/(c*log(f)))/(c*log(f))

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int f^{cx^2+a} \cos(ex+d)^3 dx$$

Verification of antiderivative is not currently implemented for this CAS.

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(f**(c*x**2+a)*cos(e*x+d)**3,x)
```

```
[Out] Integral(f**(a + c*x**2)*cos(d + e*x)**3, x)
```

3.119 $\int f^{a+cx^2} \cos(d + fx^2) dx$

Optimal. Leaf size=103

$$\frac{\sqrt{\pi} e^{-id} f^a \operatorname{erf}\left(x\sqrt{-c \log(f) + if}\right)}{4\sqrt{-c \log(f) + if}} + \frac{\sqrt{\pi} e^{id} f^a \operatorname{erfi}\left(x\sqrt{c \log(f) + if}\right)}{4\sqrt{c \log(f) + if}}$$

[Out] $1/4*f^a*\operatorname{erf}(x*(I*f-c*\ln(f))^{(1/2)})*\operatorname{Pi}^{(1/2)}/\exp(I*d)/(I*f-c*\ln(f))^{(1/2)}+1/4*\exp(I*d)*f^a*\operatorname{erfi}(x*(I*f+c*\ln(f))^{(1/2)})*\operatorname{Pi}^{(1/2)}/(I*f+c*\ln(f))^{(1/2)}$

Rubi [A] time = 0.15, antiderivative size = 103, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 4, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.222$, Rules used = {4473, 2287, 2205, 2204}

$$\frac{\sqrt{\pi} e^{-id} f^a \operatorname{Erf}\left(x\sqrt{-c \log(f) + if}\right)}{4\sqrt{-c \log(f) + if}} + \frac{\sqrt{\pi} e^{id} f^a \operatorname{Erfi}\left(x\sqrt{c \log(f) + if}\right)}{4\sqrt{c \log(f) + if}}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[f^{(a + c*x^2)}*\operatorname{Cos}[d + f*x^2], x]$

[Out] $(f^a*\operatorname{Sqrt}[\operatorname{Pi}]*\operatorname{Erf}[x*\operatorname{Sqrt}[I*f - c*\operatorname{Log}[f]])]/(4*E^{(I*d)}*\operatorname{Sqrt}[I*f - c*\operatorname{Log}[f]]) + (E^{(I*d)}*f^a*\operatorname{Sqrt}[\operatorname{Pi}]*\operatorname{Erfi}[x*\operatorname{Sqrt}[I*f + c*\operatorname{Log}[f]])]/(4*\operatorname{Sqrt}[I*f + c*\operatorname{Log}[f]])$

Rule 2204

$\operatorname{Int}[(F_)^{((a_.) + (b_.)*((c_.) + (d_.)*(x_.))^2)}, x_Symbol] := \operatorname{Simp}[(F^a*\operatorname{Sqrt}[\operatorname{Pi}]*\operatorname{Erfi}[(c + d*x)*\operatorname{Rt}[b*\operatorname{Log}[F], 2]])/(2*d*\operatorname{Rt}[b*\operatorname{Log}[F], 2]), x] /; \operatorname{FreeQ}\{F, a, b, c, d\}, x] \&\& \operatorname{PosQ}[b]$

Rule 2205

$\operatorname{Int}[(F_)^{((a_.) + (b_.)*((c_.) + (d_.)*(x_.))^2)}, x_Symbol] := \operatorname{Simp}[(F^a*\operatorname{Sqrt}[\operatorname{Pi}]*\operatorname{Erf}[(c + d*x)*\operatorname{Rt}[-(b*\operatorname{Log}[F]), 2]])/(2*d*\operatorname{Rt}[-(b*\operatorname{Log}[F]), 2]), x] /; \operatorname{FreeQ}\{F, a, b, c, d\}, x] \&\& \operatorname{NegQ}[b]$

Rule 2287

$\operatorname{Int}[(u_.)*(F_)^{(v_.)}*(G_)^{(w_.)}, x_Symbol] := \operatorname{With}\{z = v*\operatorname{Log}[F] + w*\operatorname{Log}[G]\}, \operatorname{Int}[u*\operatorname{NormalizeIntegrand}[E^z, x], x] /; \operatorname{BinomialQ}[z, x] \|\| (\operatorname{PolynomialQ}[z, x] \&\& \operatorname{LeQ}[\operatorname{Exponent}[z, x], 2]) /; \operatorname{FreeQ}\{F, G\}, x]$

Rule 4473

$\operatorname{Int}[\operatorname{Cos}[v_]^{(n_.)}*(F_)^{(u_.)}, x_Symbol] := \operatorname{Int}[\operatorname{ExpandTrigToExp}[F^u, \operatorname{Cos}[v]^n, x], x] /; \operatorname{FreeQ}[F, x] \&\& (\operatorname{LinearQ}[u, x] \|\| \operatorname{PolyQ}[u, x, 2]) \&\& (\operatorname{LinearQ}[v, x] \|\| \operatorname{PolyQ}[v, x, 2]) \&\& \operatorname{IGtQ}[n, 0]$

Rubi steps

$$\begin{aligned}
\int f^{a+cx^2} \cos(d + fx^2) dx &= \int \left(\frac{1}{2} e^{-id-ifx^2} f^{a+cx^2} + \frac{1}{2} e^{id+ifx^2} f^{a+cx^2} \right) dx \\
&= \frac{1}{2} \int e^{-id-ifx^2} f^{a+cx^2} dx + \frac{1}{2} \int e^{id+ifx^2} f^{a+cx^2} dx \\
&= \frac{1}{2} \int e^{-id+a \log(f)-x^2(if-c \log(f))} dx + \frac{1}{2} \int e^{id+a \log(f)+x^2(if+c \log(f))} dx \\
&= \frac{e^{-id} f^a \sqrt{\pi} \operatorname{erf}(x \sqrt{if - c \log(f)})}{4 \sqrt{if - c \log(f)}} + \frac{e^{id} f^a \sqrt{\pi} \operatorname{erfi}(x \sqrt{if + c \log(f)})}{4 \sqrt{if + c \log(f)}}
\end{aligned}$$

Mathematica [A] time = 0.49, size = 170, normalized size = 1.65

$$\frac{(-1)^{3/4} \sqrt{\pi} f^a \left(\sqrt{f + ic \log(f)} \left(f \cos(d) \operatorname{erf} \left(\frac{(1+i)x \sqrt{f+ic \log(f)}}{\sqrt{2}} \right) - \operatorname{erfi} \left((-1)^{3/4} x \sqrt{f + ic \log(f)} \right) \right) (c \cos(d) \log(f) + (f - ic \log(f)) \sin(d)) \right)}{4 (c^2 \log^2(f) + f^2)}$$

Antiderivative was successfully verified.

```
[In] Integrate[f^(a + c*x^2)*Cos[d + f*x^2],x]
[Out] -1/4*((-1)^(3/4)*f^a*Sqrt[Pi]*(Erfi[(-1)^(1/4)*x*Sqrt[f - I*c*Log[f]]]*Sqrt[f - I*c*Log[f]]*(f + I*c*Log[f])*(Cos[d] + I*Sin[d]) + Sqrt[f + I*c*Log[f]]*(f*cos[d]*Erf[((1 + I)*x*Sqrt[f + I*c*Log[f]])/Sqrt[2]] - Erfi[(-1)^(3/4)*x*Sqrt[f + I*c*Log[f]]]*(c*cos[d]*Log[f] + (f - I*c*Log[f])*Sin[d]))) / (f^2 + c^2*Log[f]^2)
```

fricas [A] time = 2.29, size = 109, normalized size = 1.06

$$\frac{\sqrt{\pi} (c \log(f) - if) \sqrt{-c \log(f) - if} \operatorname{erf}(\sqrt{-c \log(f) - if} x) e^{(a \log(f) + id)} + \sqrt{\pi} (c \log(f) + if) \sqrt{-c \log(f) + if} \operatorname{erfi}(\sqrt{-c \log(f) + if} x)}{4 (c^2 \log^2(f) + f^2)}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(f^(c*x^2+a)*cos(f*x^2+d),x, algorithm="fricas")
[Out] -1/4*(sqrt(pi)*(c*log(f) - I*f)*sqrt(-c*log(f) - I*f)*erf(sqrt(-c*log(f) - I*f)*x)*e^(a*log(f) + I*d) + sqrt(pi)*(c*log(f) + I*f)*sqrt(-c*log(f) + I*f)*erf(sqrt(-c*log(f) + I*f)*x)*e^(a*log(f) - I*d))/(c^2*log(f)^2 + f^2)
```

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int f^{cx^2+a} \cos(fx^2 + d) dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(f^(c*x^2+a)*cos(f*x^2+d),x, algorithm="giac")
[Out] integrate(f^(c*x^2 + a)*cos(f*x^2 + d), x)
```

maple [A] time = 0.15, size = 82, normalized size = 0.80

$$\frac{\sqrt{\pi} f^a e^{-id} \operatorname{erf}(x \sqrt{if - c \ln(f)})}{4 \sqrt{if - c \ln(f)}} + \frac{\sqrt{\pi} f^a e^{id} \operatorname{erf}(\sqrt{-if - c \ln(f)} x)}{4 \sqrt{-if - c \ln(f)}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(f^(c*x^2+a)*cos(f*x^2+d),x)
```

[Out] $\frac{1}{4}\pi^{1/2}f^a\exp(-I*d)/(I*f-c*\ln(f))^{1/2}*\operatorname{erf}(x*(I*f-c*\ln(f))^{1/2})+1/4*\pi^{1/2}f^a\exp(I*d)/(-I*f-c*\ln(f))^{1/2}*\operatorname{erf}((-I*f-c*\ln(f))^{1/2}*x)$

maxima [B] time = 0.35, size = 205, normalized size = 1.99

$$\frac{\sqrt{\pi} \sqrt{2c^2 \log(f)^2 + 2f^2} (f^a (i \cos(d) + \sin(d)) \operatorname{erf}(\sqrt{-c \log(f) + ifx}) + f^a (-i \cos(d) + \sin(d)) \operatorname{erf}(\sqrt{-c \log(f) - ifx}))}{c^2 \log(f)^2 + f^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(f^(c*x^2+a)*cos(f*x^2+d),x, algorithm="maxima")`

[Out] $-1/8*(\sqrt{\pi}*\sqrt{2*c^2*\log(f)^2 + 2*f^2}*(f^a*(I*\cos(d) + \sin(d))*\operatorname{erf}(\sqrt{-c*\log(f) + I*f}*x) + f^a*(-I*\cos(d) + \sin(d))*\operatorname{erf}(\sqrt{-c*\log(f) - I*f}*x))*\sqrt{c*\log(f) + \sqrt{c^2*\log(f)^2 + f^2}} - \sqrt{\pi}*\sqrt{2*c^2*\log(f)^2 + 2*f^2}*(f^a*(\cos(d) - I*\sin(d))*\operatorname{erf}(\sqrt{-c*\log(f) + I*f}*x) + f^a*(\cos(d) + I*\sin(d))*\operatorname{erf}(\sqrt{-c*\log(f) - I*f}*x))*\sqrt{-c*\log(f) + \sqrt{c^2*\log(f)^2 + f^2}})/(c^2*\log(f)^2 + f^2)$

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int f^{cx^2+a} \cos(fx^2 + d) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(f^(a + c*x^2)*cos(d + f*x^2),x)`

[Out] `int(f^(a + c*x^2)*cos(d + f*x^2), x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int f^{a+cx^2} \cos(d + fx^2) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(f**(c*x**2+a)*cos(f*x**2+d),x)`

[Out] `Integral(f**(a + c*x**2)*cos(d + f*x**2), x)`

3.120 $\int f^{a+cx^2} \cos^2(d + fx^2) dx$

Optimal. Leaf size=140

$$\frac{\sqrt{\pi} e^{-2id} f^a \operatorname{erf}\left(x\sqrt{-c \log(f) + 2if}\right)}{8\sqrt{-c \log(f) + 2if}} + \frac{\sqrt{\pi} e^{2id} f^a \operatorname{erfi}\left(x\sqrt{c \log(f) + 2if}\right)}{8\sqrt{c \log(f) + 2if}} + \frac{\sqrt{\pi} f^a \operatorname{erfi}\left(\sqrt{c} x \sqrt{\log(f)}\right)}{4\sqrt{c} \sqrt{\log(f)}}$$

[Out] $1/4*f^a*\operatorname{erfi}(x*c^{(1/2)}*\ln(f)^{(1/2)})*\operatorname{Pi}^{(1/2)}/c^{(1/2)}/\ln(f)^{(1/2)}+1/8*f^a*\operatorname{erf}(x*(2*I*f-c*\ln(f))^{(1/2)})*\operatorname{Pi}^{(1/2)}/\exp(2*I*d)/(2*I*f-c*\ln(f))^{(1/2)}+1/8*\exp(2*I*d)*f^a*\operatorname{erfi}(x*(2*I*f+c*\ln(f))^{(1/2)})*\operatorname{Pi}^{(1/2)}/(2*I*f+c*\ln(f))^{(1/2)}$

Rubi [A] time = 0.19, antiderivative size = 140, normalized size of antiderivative = 1.00, number of steps used = 7, number of rules used = 4, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.200$, Rules used = {4473, 2204, 2287, 2205}

$$\frac{\sqrt{\pi} e^{-2id} f^a \operatorname{Erf}\left(x\sqrt{-c \log(f) + 2if}\right)}{8\sqrt{-c \log(f) + 2if}} + \frac{\sqrt{\pi} e^{2id} f^a \operatorname{Erfi}\left(x\sqrt{c \log(f) + 2if}\right)}{8\sqrt{c \log(f) + 2if}} + \frac{\sqrt{\pi} f^a \operatorname{Erfi}\left(\sqrt{c} x \sqrt{\log(f)}\right)}{4\sqrt{c} \sqrt{\log(f)}}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[f^{(a + c*x^2)}*\operatorname{Cos}[d + f*x^2]^2, x]$

[Out] $(f^a*\operatorname{Sqrt}[\operatorname{Pi}]*\operatorname{Erfi}[\operatorname{Sqrt}[c]*x*\operatorname{Sqrt}[\operatorname{Log}[f]]])/(4*\operatorname{Sqrt}[c]*\operatorname{Sqrt}[\operatorname{Log}[f]]) + (f^a*\operatorname{Sqrt}[\operatorname{Pi}]*\operatorname{Erf}[x*\operatorname{Sqrt}[(2*I)*f - c*\operatorname{Log}[f]])/(8*\operatorname{E}^{((2*I)*d)}*\operatorname{Sqrt}[(2*I)*f - c*\operatorname{Log}[f]]) + (\operatorname{E}^{((2*I)*d)}*f^a*\operatorname{Sqrt}[\operatorname{Pi}]*\operatorname{Erfi}[x*\operatorname{Sqrt}[(2*I)*f + c*\operatorname{Log}[f]])/(8*\operatorname{Sqrt}[(2*I)*f + c*\operatorname{Log}[f]])$

Rule 2204

$\operatorname{Int}[(F_)^{((a_.) + (b_.)*((c_.) + (d_.)*(x_))^{2})}, x_Symbol] \rightarrow \operatorname{Simp}[(F^a*\operatorname{Sqrt}[\operatorname{Pi}]*\operatorname{Erfi}[(c + d*x)*\operatorname{Rt}[b*\operatorname{Log}[F], 2]])/(2*d*\operatorname{Rt}[b*\operatorname{Log}[F], 2]), x] /; \operatorname{FreeQ}\{F, a, b, c, d\}, x] \&\& \operatorname{PosQ}[b]$

Rule 2205

$\operatorname{Int}[(F_)^{((a_.) + (b_.)*((c_.) + (d_.)*(x_))^{2})}, x_Symbol] \rightarrow \operatorname{Simp}[(F^a*\operatorname{Sqrt}[\operatorname{Pi}]*\operatorname{Erf}[(c + d*x)*\operatorname{Rt}[-(b*\operatorname{Log}[F]), 2]])/(2*d*\operatorname{Rt}[-(b*\operatorname{Log}[F]), 2]), x] /; \operatorname{FreeQ}\{F, a, b, c, d\}, x] \&\& \operatorname{NegQ}[b]$

Rule 2287

$\operatorname{Int}[(u_)*(F_)^{(v_)}*(G_)^{(w_)}, x_Symbol] \rightarrow \operatorname{With}\{z = v*\operatorname{Log}[F] + w*\operatorname{Log}[G]\}, \operatorname{Int}[u*\operatorname{NormalizeIntegrand}[\operatorname{E}^z, x], x] /; \operatorname{BinomialQ}[z, x] \mid\mid (\operatorname{PolynomialQ}[z, x] \&\& \operatorname{LeQ}[\operatorname{Exponent}[z, x], 2]) /; \operatorname{FreeQ}\{F, G\}, x]$

Rule 4473

$\operatorname{Int}[\operatorname{Cos}[v_]^{(n_)}*(F_)^{(u_)}, x_Symbol] \rightarrow \operatorname{Int}[\operatorname{ExpandTrigToExp}[F^u, \operatorname{Cos}[v]^{n_}], x] /; \operatorname{FreeQ}[F, x] \&\& (\operatorname{LinearQ}[u, x] \mid\mid \operatorname{PolyQ}[u, x, 2]) \&\& (\operatorname{LinearQ}[v, x] \mid\mid \operatorname{PolyQ}[v, x, 2]) \&\& \operatorname{IGtQ}[n, 0]$

Rubi steps

$$\begin{aligned}
\int f^{a+cx^2} \cos^2(d + fx^2) dx &= \int \left(\frac{1}{2} f^{a+cx^2} + \frac{1}{4} e^{-2id-2ifx^2} f^{a+cx^2} + \frac{1}{4} e^{2id+2ifx^2} f^{a+cx^2} \right) dx \\
&= \frac{1}{4} \int e^{-2id-2ifx^2} f^{a+cx^2} dx + \frac{1}{4} \int e^{2id+2ifx^2} f^{a+cx^2} dx + \frac{1}{2} \int f^{a+cx^2} dx \\
&= \frac{f^a \sqrt{\pi} \operatorname{erfi}(\sqrt{c} x \sqrt{\log(f)})}{4\sqrt{c} \sqrt{\log(f)}} + \frac{1}{4} \int \exp(-2id + a \log(f) - x^2(2if - c \log(f))) dx + \\
&= \frac{f^a \sqrt{\pi} \operatorname{erfi}(\sqrt{c} x \sqrt{\log(f)})}{4\sqrt{c} \sqrt{\log(f)}} + \frac{e^{-2id} f^a \sqrt{\pi} \operatorname{erf}(x \sqrt{2if - c \log(f)})}{8\sqrt{2if - c \log(f)}} + \frac{e^{2id} f^a \sqrt{\pi} \operatorname{erfi}(x \sqrt{2if - c \log(f)})}{8\sqrt{2if - c \log(f)}}
\end{aligned}$$

Mathematica [A] time = 0.83, size = 189, normalized size = 1.35

$$\frac{1}{8} \sqrt{\pi} f^a \left(\frac{2 \operatorname{erfi}(\sqrt{c} x \sqrt{\log(f)})}{\sqrt{c} \sqrt{\log(f)}} + \frac{\sqrt[4]{-1} (\sqrt{2f - ic \log(f)} (c \log(f) - 2if) (\cos(2d) + i \sin(2d)) \operatorname{erfi}(\sqrt[4]{-1} x \sqrt{2f - ic \log(f)}) + (-1)^{1/4} (-\operatorname{erfi}((-1)^{3/4} x \sqrt{2f + I c \log(f)}) * (2f - I c \log(f)) * \operatorname{Sqrt}[2f + I c \log(f)] * (\cos[2d] - I \sin[2d])) + \operatorname{erfi}((-1)^{1/4} x \sqrt{2f - I c \log(f)}) * \operatorname{Sqrt}[2f - I c \log(f)] * ((-2I) f + c \log(f)) * (\cos[2d] + I \sin[2d]))}{(4f^2 + c^2 \log(f)^2)} \right) / 8$$

Antiderivative was successfully verified.

[In] Integrate[f^(a + c*x^2)*Cos[d + f*x^2]^2,x]

[Out] (f^a*Sqrt[Pi]*((2*Erfi[Sqrt[c]*x*Sqrt[Log[f]]])/(Sqrt[c]*Sqrt[Log[f]])) + ((-1)^(1/4)*(-Erfi[(-1)^(3/4)*x*Sqrt[2*f + I*c*Log[f]]]*(2*f - I*c*Log[f])*Sqrt[2*f + I*c*Log[f]]*(Cos[2*d] - I*Sin[2*d])) + Erfi[(-1)^(1/4)*x*Sqrt[2*f - I*c*Log[f]]]*Sqrt[2*f - I*c*Log[f]]*((-2*I)*f + c*Log[f])*(Cos[2*d] + I*Sin[2*d])))/(4*f^2 + c^2*Log[f]^2))/8

fricas [A] time = 1.71, size = 167, normalized size = 1.19

$$\frac{2 \sqrt{\pi} (c^2 \log(f)^2 + 4 f^2) \sqrt{-c \log(f)} f^a \operatorname{erf}(\sqrt{-c \log(f)} x) + \sqrt{\pi} (c^2 \log(f)^2 - 2i c f \log(f)) \sqrt{-c \log(f) - 2if} \operatorname{erf}(x \sqrt{-c \log(f) - 2if})}{8 (c^3 \log(f)^3 + 4 c^2 f \log(f)^2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(c*x^2+a)*cos(f*x^2+d)^2,x, algorithm="fricas")

[Out] -1/8*(2*sqrt(pi)*(c^2*log(f)^2 + 4*f^2)*sqrt(-c*log(f))*f^a*erf(sqrt(-c*log(f))*x) + sqrt(pi)*(c^2*log(f)^2 - 2*I*c*f*log(f))*sqrt(-c*log(f) - 2*I*f)*erf(sqrt(-c*log(f) - 2*I*f)*x)*e^(a*log(f) + 2*I*d) + sqrt(pi)*(c^2*log(f)^2 + 2*I*c*f*log(f))*sqrt(-c*log(f) + 2*I*f)*erf(sqrt(-c*log(f) + 2*I*f)*x)*e^(a*log(f) - 2*I*d))/(c^3*log(f)^3 + 4*c*f^2*log(f))

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int f^{cx^2+a} \cos(fx^2 + d)^2 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(c*x^2+a)*cos(f*x^2+d)^2,x, algorithm="giac")

[Out] integrate(f^(c*x^2 + a)*cos(f*x^2 + d)^2, x)

maple [A] time = 0.25, size = 107, normalized size = 0.76

$$\frac{\sqrt{\pi} f^a e^{-2id} \operatorname{erf}(x \sqrt{2if - c \ln(f)})}{8\sqrt{2if - c \ln(f)}} + \frac{\sqrt{\pi} f^a e^{2id} \operatorname{erf}(x \sqrt{-2if - c \ln(f)})}{8\sqrt{-2if - c \ln(f)}} + \frac{f^a \sqrt{\pi} \operatorname{erf}(\sqrt{-c \ln(f)} x)}{4\sqrt{-c \ln(f)}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(f^(c*x^2+a)*cos(f*x^2+d)^2,x)

[Out] $\frac{1}{8}\pi^{1/2}f^a\exp(-2I*d)/(2I*f-c*\ln(f))^{1/2}\operatorname{erf}(x*(2I*f-c*\ln(f))^{1/2})+\frac{1}{8}\pi^{1/2}f^a\exp(2I*d)/(-2I*f-c*\ln(f))^{1/2}\operatorname{erf}((-2I*f-c*\ln(f))^{1/2}*x)+\frac{1}{4}f^a\pi^{1/2}/(-c*\ln(f))^{1/2}\operatorname{erf}((-c*\ln(f))^{1/2}*x)$

maxima [C] time = 0.35, size = 315, normalized size = 2.25

$$\sqrt{\pi}\sqrt{2c^2\log(f)^2+8f^2}\left(f^a(i\cos(2d)+\sin(2d))\operatorname{erf}\left(\sqrt{-c\log(f)+2ifx}\right)+f^a(-i\cos(2d)+\sin(2d))\operatorname{erf}\left(\sqrt{-c\log(f)-2ifx}\right)\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(c*x^2+a)*cos(f*x^2+d)^2,x, algorithm="maxima")

[Out] $-1/16*(\sqrt{\pi})\sqrt{(2c^2\log(f)^2+8f^2)}*(f^a*(I*\cos(2*d)+\sin(2*d))*\operatorname{erf}(\sqrt{-c*\log(f)+2I*f}*x)+f^a*(-I*\cos(2*d)+\sin(2*d))*\operatorname{erf}(\sqrt{-c*\log(f)-2I*f}*x))*\sqrt{c*\log(f)+\sqrt{c^2*\log(f)^2+4*f^2}}*\sqrt{-c*\log(f)}-\sqrt{\pi}\sqrt{(2c^2\log(f)^2+8f^2)}*(f^a*(\cos(2*d)-I*\sin(2*d))*\operatorname{erf}(\sqrt{-c*\log(f)+2I*f}*x)+f^a*(\cos(2*d)+I*\sin(2*d))*\operatorname{erf}(\sqrt{-c*\log(f)-2I*f}*x))*\sqrt{-c*\log(f)+\sqrt{c^2*\log(f)^2+4*f^2}}*\sqrt{-c*\log(f)}-2*\sqrt{\pi}*((c^2*f^a*\log(f)^2+4*f^{(a+2)})*\operatorname{erf}(x*\operatorname{conjugate}(\sqrt{-c*\log(f)})))+(c^2*f^a*\log(f)^2+4*f^{(a+2)})*\operatorname{erf}(\sqrt{-c*\log(f)}*x))/((c^2*\log(f)^2+4*f^2)*\sqrt{-c*\log(f)})$

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int f^{cx^2+a} \cos(fx^2+d)^2 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(f^(a+c*x^2)*cos(d+f*x^2)^2,x)

[Out] int(f^(a+c*x^2)*cos(d+f*x^2)^2, x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int f^{a+cx^2} \cos^2(d+fx^2) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f**(c*x**2+a)*cos(f*x**2+d)**2,x)

[Out] Integral(f**(a+c*x**2)*cos(d+f*x**2)**2, x)

3.121 $\int f^{a+cx^2} \cos^3(d + fx^2) dx$

Optimal. Leaf size=205

$$\frac{3\sqrt{\pi} e^{-id} f^a \operatorname{erf}(x\sqrt{-c \log(f) + if})}{16\sqrt{-c \log(f) + if}} + \frac{\sqrt{\pi} e^{-3id} f^a \operatorname{erf}(x\sqrt{-c \log(f) + 3if})}{16\sqrt{-c \log(f) + 3if}} + \frac{3\sqrt{\pi} e^{id} f^a \operatorname{erfi}(x\sqrt{c \log(f) + if})}{16\sqrt{c \log(f) + if}} + \frac{\sqrt{\pi} e^{3id} f^a \operatorname{erfi}(x\sqrt{c \log(f) + 3if})}{16\sqrt{c \log(f) + 3if}}$$

[Out] $3/16*f^a*\operatorname{erf}(x*(I*f-c*\ln(f))^{(1/2)})*\operatorname{Pi}^{(1/2)}/\exp(I*d)/(I*f-c*\ln(f))^{(1/2)+1}$
 $/16*f^a*\operatorname{erf}(x*(3*I*f-c*\ln(f))^{(1/2)})*\operatorname{Pi}^{(1/2)}/\exp(3*I*d)/(3*I*f-c*\ln(f))^{(1/2)+3}$
 $+3/16*\exp(I*d)*f^a*\operatorname{erfi}(x*(I*f+c*\ln(f))^{(1/2)})*\operatorname{Pi}^{(1/2)/(I*f+c*\ln(f))^{(1/2)+1}$
 $+1/16*\exp(3*I*d)*f^a*\operatorname{erfi}(x*(3*I*f+c*\ln(f))^{(1/2)})*\operatorname{Pi}^{(1/2)/(3*I*f+c*\ln(f))^{(1/2)+1}$

Rubi [A] time = 0.29, antiderivative size = 205, normalized size of antiderivative = 1.00, number of steps used = 10, number of rules used = 4, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.200$, Rules used = {4473, 2287, 2205, 2204}

$$\frac{3\sqrt{\pi} e^{-id} f^a \operatorname{Erf}(x\sqrt{-c \log(f) + if})}{16\sqrt{-c \log(f) + if}} + \frac{\sqrt{\pi} e^{-3id} f^a \operatorname{Erf}(x\sqrt{-c \log(f) + 3if})}{16\sqrt{-c \log(f) + 3if}} + \frac{3\sqrt{\pi} e^{id} f^a \operatorname{Erfi}(x\sqrt{c \log(f) + if})}{16\sqrt{c \log(f) + if}} + \frac{\sqrt{\pi} e^{3id} f^a \operatorname{Erfi}(x\sqrt{c \log(f) + 3if})}{16\sqrt{c \log(f) + 3if}}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[f^{(a + c*x^2)}*\operatorname{Cos}[d + f*x^2]^3, x]$

[Out] $(3*f^a*\operatorname{Sqrt}[\operatorname{Pi}]*\operatorname{Erf}[x*\operatorname{Sqrt}[I*f - c*\operatorname{Log}[f]]])/(16*E^{(I*d)}*\operatorname{Sqrt}[I*f - c*\operatorname{Log}[f]]) + (f^a*\operatorname{Sqrt}[\operatorname{Pi}]*\operatorname{Erf}[x*\operatorname{Sqrt}[(3*I)*f - c*\operatorname{Log}[f]]])/(16*E^{((3*I)*d)}*\operatorname{Sqrt}[(3*I)*f - c*\operatorname{Log}[f]]) + (3*E^{(I*d)}*f^a*\operatorname{Sqrt}[\operatorname{Pi}]*\operatorname{Erfi}[x*\operatorname{Sqrt}[I*f + c*\operatorname{Log}[f]]])/(16*\operatorname{Sqrt}[I*f + c*\operatorname{Log}[f]]) + (E^{((3*I)*d)}*f^a*\operatorname{Sqrt}[\operatorname{Pi}]*\operatorname{Erfi}[x*\operatorname{Sqrt}[(3*I)*f + c*\operatorname{Log}[f]]])/(16*\operatorname{Sqrt}[(3*I)*f + c*\operatorname{Log}[f]])$

Rule 2204

$\operatorname{Int}[(F_)^{((a_.) + (b_.)*((c_.) + (d_.)*(x_.))^2)}, x_Symbol] := \operatorname{Simp}[(F^a*\operatorname{Sqrt}[\operatorname{Pi}]*\operatorname{Erfi}[(c + d*x)*\operatorname{Rt}[b*\operatorname{Log}[F], 2]])/(2*d*\operatorname{Rt}[b*\operatorname{Log}[F], 2]), x] /; \operatorname{FreeQ}\{F, a, b, c, d\}, x] \ \&\& \operatorname{PosQ}[b]$

Rule 2205

$\operatorname{Int}[(F_)^{((a_.) + (b_.)*((c_.) + (d_.)*(x_.))^2)}, x_Symbol] := \operatorname{Simp}[(F^a*\operatorname{Sqrt}[\operatorname{Pi}]*\operatorname{Erf}[(c + d*x)*\operatorname{Rt}[-(b*\operatorname{Log}[F]), 2]])/(2*d*\operatorname{Rt}[-(b*\operatorname{Log}[F]), 2]), x] /; \operatorname{FreeQ}\{F, a, b, c, d\}, x] \ \&\& \operatorname{NegQ}[b]$

Rule 2287

$\operatorname{Int}[(u_)*(F_)^{(v_)}*(G_)^{(w_)}], x_Symbol] := \operatorname{With}\{z = v*\operatorname{Log}[F] + w*\operatorname{Log}[G]\}, \operatorname{Int}[u*\operatorname{NormalizeIntegrand}[E^z, x], x] /; \operatorname{BinomialQ}[z, x] \ \|\ (\operatorname{PolynomialQ}[z, x] \ \&\& \operatorname{LeQ}[\operatorname{Exponent}[z, x], 2]) /; \operatorname{FreeQ}\{F, G\}, x]$

Rule 4473

$\operatorname{Int}[\operatorname{Cos}[v_]^{(n_.)}*(F_)^{(u_)}], x_Symbol] := \operatorname{Int}[\operatorname{ExpandTrigToExp}[F^u, \operatorname{Cos}[v]^n], x] /; \operatorname{FreeQ}[F, x] \ \&\& (\operatorname{LinearQ}[u, x] \ \|\ \operatorname{PolyQ}[u, x, 2]) \ \&\& (\operatorname{LinearQ}[v, x] \ \|\ \operatorname{PolyQ}[v, x, 2]) \ \&\& \operatorname{IGtQ}[n, 0]$

Rubi steps

$$\begin{aligned}
\int f^{a+cx^2} \cos^3(d + fx^2) dx &= \int \left(\frac{3}{8} e^{-id-ifx^2} f^{a+cx^2} + \frac{3}{8} e^{id+ifx^2} f^{a+cx^2} + \frac{1}{8} e^{-3id-3ifx^2} f^{a+cx^2} + \frac{1}{8} e^{3id+3ifx^2} f^{a+cx^2} \right) dx \\
&= \frac{1}{8} \int e^{-3id-3ifx^2} f^{a+cx^2} dx + \frac{1}{8} \int e^{3id+3ifx^2} f^{a+cx^2} dx + \frac{3}{8} \int e^{-id-ifx^2} f^{a+cx^2} dx + \frac{3}{8} \int e^{id+ifx^2} f^{a+cx^2} dx \\
&= \frac{1}{8} \int \exp(-3id + a \log(f) - x^2(3if - c \log(f))) dx + \frac{1}{8} \int \exp(3id + a \log(f) - x^2(3if - c \log(f))) dx \\
&= \frac{3e^{-id} f^a \sqrt{\pi} \operatorname{erf}(x\sqrt{if - c \log(f)})}{16\sqrt{if - c \log(f)}} + \frac{e^{-3id} f^a \sqrt{\pi} \operatorname{erf}(x\sqrt{3if - c \log(f)})}{16\sqrt{3if - c \log(f)}} + \frac{3e^{id} f^a \sqrt{\pi} \operatorname{erf}(x\sqrt{-if + c \log(f)})}{16\sqrt{-if + c \log(f)}}
\end{aligned}$$

Mathematica [A] time = 2.19, size = 389, normalized size = 1.90

$$\frac{\sqrt[4]{-1} \sqrt{\pi} f^a \left((f - ic \log(f)) \left(\sqrt{3f - ic \log(f)} (ic^2 \log^2(f) + 4cf \log(f) - 3if^2) (\cos(3d) + i \sin(3d)) \operatorname{erfi} \left(\sqrt[4]{-1} \sqrt{f - ic \log(f)} \right) \right) \right)}{16\sqrt{if - c \log(f)}} + \frac{e^{-3id} f^a \sqrt{\pi} \operatorname{erf}(x\sqrt{3if - c \log(f)})}{16\sqrt{3if - c \log(f)}} + \frac{3e^{id} f^a \sqrt{\pi} \operatorname{erf}(x\sqrt{-if + c \log(f)})}{16\sqrt{-if + c \log(f)}}$$

Antiderivative was successfully verified.

[In] Integrate[f^(a + c*x^2)*Cos[d + f*x^2]^3,x]

[Out] $((-1)^{1/4} f^a \sqrt{\pi} (3 \operatorname{Erfi}[-(1/4) x \sqrt{f - I c \log(f)}]) \sqrt{f - I c \log(f)} ((-9I) f^3 + 9 c f^2 \log(f) - I c^2 f \log(f)^2 + c^3 \log(f)^3) (\cos(d) + I \sin(d)) + (f - I c \log(f)) (-((3f - I c \log(f)) (9 f \operatorname{Erfi}[(1 + I) x \sqrt{f + I c \log(f)}]) / \sqrt{2}) \sqrt{f + I c \log(f)} \sin(d) + 3 \operatorname{Erfi}[-(1/4) x \sqrt{f + I c \log(f)}]) \sqrt{f + I c \log(f)} (\cos(d) (3f + I c \log(f)) + c \log(f) \sin(d)) + \operatorname{Erfi}[-(3/4) x \sqrt{3f + I c \log(f)}]) (f + I c \log(f)) \sqrt{3f + I c \log(f)} (\cos(3d) - I \sin(3d))) + \operatorname{Erfi}[-(1/4) x \sqrt{3f - I c \log(f)}]) \sqrt{3f - I c \log(f)} ((-3I) f^2 + 4 c f \log(f) + I c^2 \log(f)^2) (\cos(3d) + I \sin(3d))) / (16 (9 f^4 + 10 c^2 f^2 \log(f)^2 + c^4 \log(f)^4))$

fricas [B] time = 0.63, size = 311, normalized size = 1.52

$$\frac{\sqrt{\pi} (c^3 \log(f)^3 - 3i c^2 f \log(f)^2 + c f^2 \log(f) - 3i f^3) \sqrt{-c \log(f) - 3i f} \operatorname{erf}(\sqrt{-c \log(f) - 3i f} x) e^{(a \log(f) + 3i d)}}{16\sqrt{if - c \log(f)}} + \frac{e^{-3id} f^a \sqrt{\pi} \operatorname{erf}(x\sqrt{3if - c \log(f)})}{16\sqrt{3if - c \log(f)}} + \frac{3e^{id} f^a \sqrt{\pi} \operatorname{erf}(x\sqrt{-if + c \log(f)})}{16\sqrt{-if + c \log(f)}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(c*x^2+a)*cos(f*x^2+d)^3,x, algorithm="fricas")

[Out] $-1/16 (\sqrt{\pi} (c^3 \log(f)^3 - 3I c^2 f \log(f)^2 + c f^2 \log(f) - 3I f^3) \sqrt{-c \log(f) - 3I f} \operatorname{erf}(\sqrt{-c \log(f) - 3I f} x) e^{(a \log(f) + 3I d)} + \sqrt{\pi} (3c^3 \log(f)^3 - 3I c^2 f \log(f)^2 + 27c f^2 \log(f) - 27I f^3) \sqrt{-c \log(f) - I f} \operatorname{erf}(\sqrt{-c \log(f) - I f} x) e^{(a \log(f) + I d)} + \sqrt{\pi} (3c^3 \log(f)^3 + 3I c^2 f \log(f)^2 + 27c f^2 \log(f) + 27I f^3) \sqrt{-c \log(f) + I f} \operatorname{erf}(\sqrt{-c \log(f) + I f} x) e^{(a \log(f) - I d)} + \sqrt{\pi} (c^3 \log(f)^3 + 3I c^2 f \log(f)^2 + c f^2 \log(f) + 3I f^3) \sqrt{-c \log(f) + 3I f} \operatorname{erf}(\sqrt{-c \log(f) + 3I f} x) e^{(a \log(f) - 3I d)}) / (c^4 \log(f)^4 + 10c^2 f^2 \log(f)^2 + 9f^4)$

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int f^{cx^2+a} \cos(fx^2 + d)^3 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(c*x^2+a)*cos(f*x^2+d)^3,x, algorithm="giac")

[Out] integrate(f^(c*x^2 + a)*cos(f*x^2 + d)^3, x)

maple [A] time = 0.55, size = 162, normalized size = 0.79

$$\frac{\sqrt{\pi} f^a e^{-3id} \operatorname{erf}\left(x\sqrt{3if - c \ln(f)}\right)}{16\sqrt{3if - c \ln(f)}} + \frac{3\sqrt{\pi} f^a e^{-id} \operatorname{erf}\left(x\sqrt{if - c \ln(f)}\right)}{16\sqrt{if - c \ln(f)}} + \frac{3\sqrt{\pi} f^a e^{id} \operatorname{erf}\left(\sqrt{-if - c \ln(f)} x\right)}{16\sqrt{-if - c \ln(f)}} + \frac{\sqrt{\pi} f^a}{16\sqrt{-if - c \ln(f)}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(f^(c*x^2+a)*cos(f*x^2+d)^3,x)

[Out] 1/16*Pi^(1/2)*f^a*exp(-3*I*d)/(3*I*f-c*ln(f))^(1/2)*erf(x*(3*I*f-c*ln(f))^(1/2))+3/16*Pi^(1/2)*f^a*exp(-I*d)/(I*f-c*ln(f))^(1/2)*erf(x*(I*f-c*ln(f))^(1/2))+3/16*Pi^(1/2)*f^a*exp(I*d)/(-I*f-c*ln(f))^(1/2)*erf((-I*f-c*ln(f))^(1/2)*x)+1/16*Pi^(1/2)*f^a*exp(3*I*d)/(-c*ln(f)-3*I*f)^(1/2)*erf((-c*ln(f)-3*I*f)^(1/2)*x)

maxima [B] time = 0.35, size = 673, normalized size = 3.28

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(c*x^2+a)*cos(f*x^2+d)^3,x, algorithm="maxima")

[Out] 1/4096*(sqrt(pi)*sqrt(2*c^2*log(f)^2 + 18*f^2)*((128*(-I*c^2*cos(3*d) - c^2*sin(3*d))*f^a*log(f)^2 - f^(a + 2)*(128*I*cos(3*d) + 128*sin(3*d)))*erf(sqrt(-c*log(f) + 3*I*f)*x) + (128*(I*c^2*cos(3*d) - c^2*sin(3*d))*f^a*log(f)^2 - f^(a + 2)*(-128*I*cos(3*d) + 128*sin(3*d)))*erf(sqrt(-c*log(f) - 3*I*f)*x))*sqrt(c*log(f) + sqrt(c^2*log(f)^2 + 9*f^2)) - sqrt(pi)*sqrt(2*c^2*log(f)^2 + 2*f^2)*(((384*I*c^2*cos(d) + 384*c^2*sin(d))*f^a*log(f)^2 + f^(a + 2)*(3456*I*cos(d) + 3456*sin(d)))*erf(sqrt(-c*log(f) + I*f)*x) + ((-384*I*c^2*cos(d) + 384*c^2*sin(d))*f^a*log(f)^2 + f^(a + 2)*(-3456*I*cos(d) + 3456*sin(d)))*erf(sqrt(-c*log(f) - I*f)*x))*sqrt(c*log(f) + sqrt(c^2*log(f)^2 + f^2)) + sqrt(pi)*sqrt(2*c^2*log(f)^2 + 18*f^2)*(((128*c^2*cos(3*d) - 128*I*c^2*sin(3*d))*f^a*log(f)^2 + 128*f^(a + 2)*(cos(3*d) - I*sin(3*d)))*erf(sqrt(-c*log(f) + 3*I*f)*x) + ((128*c^2*cos(3*d) + 128*I*c^2*sin(3*d))*f^a*log(f)^2 + 128*f^(a + 2)*(cos(3*d) + I*sin(3*d)))*erf(sqrt(-c*log(f) - 3*I*f)*x))*sqrt(-c*log(f) + sqrt(c^2*log(f)^2 + 9*f^2)) + 384*sqrt(pi)*sqrt(2*c^2*log(f)^2 + 2*f^2)*(((c^2*cos(d) - I*c^2*sin(d))*f^a*log(f)^2 + 9*f^(a + 2)*(cos(d) - I*sin(d)))*erf(sqrt(-c*log(f) + I*f)*x) + ((c^2*cos(d) + I*c^2*sin(d))*f^a*log(f)^2 + 9*f^(a + 2)*(cos(d) + I*sin(d)))*erf(sqrt(-c*log(f) - I*f)*x))*sqrt(-c*log(f) + sqrt(c^2*log(f)^2 + f^2)))/(c^4*log(f)^4 + 10*c^2*f^2*log(f)^2 + 9*f^4)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int f^{cx^2+a} \cos(fx^2 + d)^3 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(f^(a + c*x^2)*cos(d + f*x^2)^3,x)

[Out] int(f^(a + c*x^2)*cos(d + f*x^2)^3, x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int f^{a+cx^2} \cos^3(d + fx^2) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f**(c*x**2+a)*cos(f*x**2+d)**3,x)

[Out] Integral(f**(a + c*x**2)*cos(d + f*x**2)**3, x)

3.122 $\int f^{a+cx^2} \cos(d + ex + fx^2) dx$

Optimal. Leaf size=183

$$\frac{\sqrt{\pi} f^a e^{-\frac{e^2}{-4c \log(f) + 4if} - id} \operatorname{erf}\left(\frac{2x(-c \log(f) + if) + ie}{2\sqrt{-c \log(f) + if}}\right)}{4\sqrt{-c \log(f) + if}} + \frac{\sqrt{\pi} f^a e^{\frac{e^2}{4c \log(f) + 4if} + id} \operatorname{erfi}\left(\frac{2x(c \log(f) + if) + ie}{2\sqrt{c \log(f) + if}}\right)}{4\sqrt{c \log(f) + if}}$$

[Out] $1/4 * \exp(-I * d - e^2 / (4 * I * f - 4 * c * \ln(f))) * f^a * \operatorname{erf}(1/2 * (I * e + 2 * x * (I * f - c * \ln(f)))) / (I * f - c * \ln(f))^{(1/2)} * \pi^{(1/2)} / (I * f - c * \ln(f))^{(1/2)} + 1/4 * \exp(I * d + e^2 / (4 * I * f + 4 * c * \ln(f))) * f^a * \operatorname{erfi}(1/2 * (I * e + 2 * x * (I * f + c * \ln(f)))) / (I * f + c * \ln(f))^{(1/2)} * \pi^{(1/2)} / (I * f + c * \ln(f))^{(1/2)}$

Rubi [A] time = 0.30, antiderivative size = 183, normalized size of antiderivative = 1.00, number of steps used = 8, number of rules used = 5, integrand size = 21, $\frac{\text{number of rules}}{\text{integrand size}} = 0.238$, Rules used = {4473, 2287, 2234, 2205, 2204}

$$\frac{\sqrt{\pi} f^a e^{-\frac{e^2}{-4c \log(f) + 4if} - id} \operatorname{Erf}\left(\frac{2x(-c \log(f) + if) + ie}{2\sqrt{-c \log(f) + if}}\right)}{4\sqrt{-c \log(f) + if}} + \frac{\sqrt{\pi} f^a e^{\frac{e^2}{4c \log(f) + 4if} + id} \operatorname{Erfi}\left(\frac{2x(c \log(f) + if) + ie}{2\sqrt{c \log(f) + if}}\right)}{4\sqrt{c \log(f) + if}}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[f^{(a + c * x^2)} * \operatorname{Cos}[d + e * x + f * x^2], x]$

[Out] $(E^{((-I) * d - e^2 / ((4 * I) * f - 4 * c * \operatorname{Log}[f]))} * f^a * \operatorname{Sqrt}[\pi] * \operatorname{Erf}[(I * e + 2 * x * (I * f - c * \operatorname{Log}[f])) / (2 * \operatorname{Sqrt}[I * f - c * \operatorname{Log}[f]])]) / (4 * \operatorname{Sqrt}[I * f - c * \operatorname{Log}[f]]) + (E^{(I * d + e^2 / ((4 * I) * f + 4 * c * \operatorname{Log}[f]))} * f^a * \operatorname{Sqrt}[\pi] * \operatorname{Erfi}[(I * e + 2 * x * (I * f + c * \operatorname{Log}[f])) / (2 * \operatorname{Sqrt}[I * f + c * \operatorname{Log}[f]])]) / (4 * \operatorname{Sqrt}[I * f + c * \operatorname{Log}[f]])$

Rule 2204

$\operatorname{Int}[(F_)^{(a_)} + (b_)*((c_)+ (d_)*(x_))^2], x_Symbol] := \operatorname{Simp}[(F^a * \operatorname{Sqrt}[\pi] * \operatorname{Erfi}[(c + d * x) * \operatorname{Rt}[b * \operatorname{Log}[F], 2]]) / (2 * d * \operatorname{Rt}[b * \operatorname{Log}[F], 2]), x] /; \operatorname{FreeQ}\{F, a, b, c, d\}, x] \&\& \operatorname{PosQ}[b]$

Rule 2205

$\operatorname{Int}[(F_)^{(a_)} + (b_)*((c_)+ (d_)*(x_))^2], x_Symbol] := \operatorname{Simp}[(F^a * \operatorname{Sqrt}[\pi] * \operatorname{Erf}[(c + d * x) * \operatorname{Rt}[-(b * \operatorname{Log}[F]), 2]]) / (2 * d * \operatorname{Rt}[-(b * \operatorname{Log}[F]), 2]), x] /; \operatorname{FreeQ}\{F, a, b, c, d\}, x] \&\& \operatorname{NegQ}[b]$

Rule 2234

$\operatorname{Int}[(F_)^{(a_)} + (b_)*(x_)+ (c_)*(x_)^2], x_Symbol] := \operatorname{Dist}[F^{(a - b^2 / (4 * c))}, \operatorname{Int}[F^{((b + 2 * c * x)^2 / (4 * c))}, x], x] /; \operatorname{FreeQ}\{F, a, b, c\}, x]$

Rule 2287

$\operatorname{Int}[(u_)*(F_)^{(v_)}*(G_)^{(w_)}], x_Symbol] := \operatorname{With}\{z = v * \operatorname{Log}[F] + w * \operatorname{Log}[G]\}, \operatorname{Int}[u * \operatorname{NormalizeIntegrand}[E^z, x], x] /; \operatorname{BinomialQ}[z, x] || (\operatorname{PolynomialQ}[z, x] \&\& \operatorname{LeQ}[\operatorname{Exponent}[z, x], 2]) /; \operatorname{FreeQ}\{F, G\}, x]$

Rule 4473

$\operatorname{Int}[\operatorname{Cos}[v_]^{(n_)} * (F_)^{(u_)}], x_Symbol] := \operatorname{Int}[\operatorname{ExpandTrigToExp}[F^u, \operatorname{Cos}[v]^{(n)}, x], x] /; \operatorname{FreeQ}[F, x] \&\& (\operatorname{LinearQ}[u, x] || \operatorname{PolyQ}[u, x, 2]) \&\& (\operatorname{LinearQ}[v, x] || \operatorname{PolyQ}[v, x, 2]) \&\& \operatorname{IGtQ}[n, 0]$

Rubi steps

$$\begin{aligned}
\int f^{a+cx^2} \cos(d+ex+fx^2) dx &= \int \left(\frac{1}{2} e^{-id-ix-ix^2} f^{a+cx^2} + \frac{1}{2} e^{id+ix+ix^2} f^{a+cx^2} \right) dx \\
&= \frac{1}{2} \int e^{-id-ix-ix^2} f^{a+cx^2} dx + \frac{1}{2} \int e^{id+ix+ix^2} f^{a+cx^2} dx \\
&= \frac{1}{2} \int \exp(-id-ix+a \log(f)-x^2(if-c \log(f))) dx + \frac{1}{2} \int \exp(id+ix+a \log(f)+x^2(if+c \log(f))) dx \\
&= \frac{1}{2} \left(e^{-id-\frac{e^2}{4if-4c \log(f)}} f^a \right) \int \exp\left(\frac{(-ie+2x(-if+c \log(f)))^2}{4(-if+c \log(f))}\right) dx + \frac{1}{2} \left(e^{id+\frac{e^2}{4if+4c \log(f)}} f^a \right) \int \exp\left(\frac{(ie+2x(if+c \log(f)))^2}{4(if+c \log(f))}\right) dx \\
&= \frac{e^{-id-\frac{e^2}{4if-4c \log(f)}} f^a \sqrt{\pi} \operatorname{erf}\left(\frac{ie+2x(if-c \log(f))}{2\sqrt{if-c \log(f)}}\right)}{4\sqrt{if-c \log(f)}} + \frac{e^{id+\frac{e^2}{4if+4c \log(f)}} f^a \sqrt{\pi} \operatorname{erfi}\left(\frac{ie+2x(if+c \log(f))}{2\sqrt{if+c \log(f)}}\right)}{4\sqrt{if+c \log(f)}}
\end{aligned}$$

Mathematica [A] time = 0.95, size = 217, normalized size = 1.19

$$\frac{\sqrt[4]{-1} \sqrt{\pi} f^a e^{\frac{e^2}{4c \log(f)+4if}} \left(\sqrt{f-ic \log(f)} (c \log(f)-if)(\cos(d)+i \sin(d)) \operatorname{erfi}\left(\frac{\sqrt[4]{-1}(-2icx \log(f)+e+2fx)}{2\sqrt{f-ic \log(f)}}\right) - (f-ic \log(f)) \right)}{4(c^2 \log^2(f)+f^2)}$$

Warning: Unable to verify antiderivative.

[In] Integrate[f^(a+c*x^2)*Cos[d+e*x+f*x^2],x]

[Out] $((-1)^{(1/4)} * E^{(e^2/((4*I)*f + 4*c*Log[f]))} * f^a * Sqrt[\pi] * (-E^{((I/2)*e^2*f)} / (f^2 + c^2*Log[f]^2)) * \operatorname{Erfi}[\frac{(-1)^{(3/4)}*(e + 2*f*x + (2*I)*c*x*Log[f])}{(2*Sqrt[f + I*c*Log[f]])}] * (f - I*c*Log[f]) * Sqrt[f + I*c*Log[f]] * (\cos[d] - I*\sin[d]) + \operatorname{Erfi}[\frac{(-1)^{(1/4)}*(e + 2*f*x - (2*I)*c*x*Log[f])}{(2*Sqrt[f - I*c*Log[f]])}] * Sqrt[f - I*c*Log[f]] * ((-I)*f + c*Log[f]) * (\cos[d] + I*\sin[d])]) / (4*(f^2 + c^2*Log[f]^2))$

fricas [B] time = 0.82, size = 301, normalized size = 1.64

$$\frac{\sqrt{\pi} (c \log(f) - if) \sqrt{-c \log(f) - if} \operatorname{erf}\left(\frac{(2c^2x \log(f)^2 + 2f^2x + ice \log(f) + ef) \sqrt{-c \log(f) - if}}{2(c^2 \log(f)^2 + f^2)}\right)}{4(c^2 \log(f)^2 + f^2)} e^{\left(\frac{4ac^2 \log(f)^3 + 4ic^2d \log(f)^2 - ie^2f + 4idf^2}{4(c^2 \log(f)^2 + f^2)}\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(c*x^2+a)*cos(f*x^2+e*x+d),x, algorithm="fricas")

[Out] $-1/4*(\sqrt{\pi})*(c*\log(f) - I*f)*\sqrt{-c*\log(f) - I*f}*\operatorname{erf}(1/2*(2*c^2*x*\log(f)^2 + 2*f^2*x + I*c*e*\log(f) + e*f)*\sqrt{-c*\log(f) - I*f}/(c^2*\log(f)^2 + f^2))*e^{(1/4*(4*a*c^2*\log(f)^3 + 4*I*c^2*d*\log(f)^2 - I*e^2*f + 4*I*d*f^2 + (c*e^2 + 4*a*f^2)*\log(f))/(c^2*\log(f)^2 + f^2))} + \sqrt{\pi}*(c*\log(f) + I*f)*\sqrt{-c*\log(f) + I*f}*\operatorname{erf}(1/2*(2*c^2*x*\log(f)^2 + 2*f^2*x - I*c*e*\log(f) + e*f)*\sqrt{-c*\log(f) + I*f}/(c^2*\log(f)^2 + f^2))*e^{(1/4*(4*a*c^2*\log(f)^3 - 4*I*c^2*d*\log(f)^2 + I*e^2*f - 4*I*d*f^2 + (c*e^2 + 4*a*f^2)*\log(f))/(c^2*\log(f)^2 + f^2))}/(c^2*\log(f)^2 + f^2)$

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int f^{cx^2+a} \cos(fx^2 + ex + d) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(c*x^2+a)*cos(f*x^2+e*x+d),x, algorithm="giac")

[Out] integrate(f^(c*x^2 + a)*cos(f*x^2 + e*x + d), x)

maple [A] time = 0.17, size = 167, normalized size = 0.91

$$\frac{\sqrt{\pi} f^a e^{-\frac{4df+4id \ln(f)c-e^2}{4(-if+c \ln(f))}} \operatorname{erf}\left(x\sqrt{if-c \ln(f)} + \frac{ie}{2\sqrt{if-c \ln(f)}}\right)}{4\sqrt{if-c \ln(f)}} - \frac{\sqrt{\pi} f^a e^{-\frac{4df+4id \ln(f)c+e^2}{4if+4c \ln(f)}} \operatorname{erf}\left(-\sqrt{-if-c \ln(f)} x + \frac{ie}{2\sqrt{-if-c \ln(f)}}\right)}{4\sqrt{-if-c \ln(f)}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(f^(c*x^2+a)*cos(f*x^2+e*x+d),x)

[Out] $\frac{1}{4}\pi^{1/2} f^a \exp(-1/4*(4*d*f+4*I*d*\ln(f)*c-e^2)/(-I*f+c*\ln(f)))/(I*f-c*\ln(f))^{1/2} \operatorname{erf}(x*(I*f-c*\ln(f))^{1/2}+1/2*I*e/(I*f-c*\ln(f))^{1/2})-1/4*\pi^{1/2} f^a \exp(1/4*(-4*d*f+4*I*d*\ln(f)*c+e^2)/(I*f+c*\ln(f)))/(-I*f-c*\ln(f))^{1/2} \operatorname{erf}(-(-I*f-c*\ln(f))^{1/2}*x+1/2*I*e/(-I*f-c*\ln(f))^{1/2})$

maxima [B] time = 0.37, size = 761, normalized size = 4.16

$$\sqrt{\pi} \sqrt{2c^2 \log(f)^2 + 2f^2} \left(i f^{\frac{c^2}{4(c^2 \log(f)^2 + f^2)}} f^a \cos\left(\frac{4c^2 d \log(f)^2 - e^2 f + 4df^2}{4(c^2 \log(f)^2 + f^2)}\right) + f^{\frac{c^2}{4(c^2 \log(f)^2 + f^2)}} f^a \sin\left(\frac{4c^2 d \log(f)^2 - e^2 f + 4df^2}{4(c^2 \log(f)^2 + f^2)}\right) \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(c*x^2+a)*cos(f*x^2+e*x+d),x, algorithm="maxima")

[Out] $\frac{1}{8}*(\sqrt{\pi}*\sqrt{2*c^2*\log(f)^2 + 2*f^2})*((I*f^{1/4*c*e^2/(c^2*\log(f)^2 + f^2)})*f^a*\cos(1/4*(4*c^2*d*\log(f)^2 - e^2*f + 4*d*f^2)/(c^2*\log(f)^2 + f^2)) + f^{1/4*c*e^2/(c^2*\log(f)^2 + f^2)}*f^a*\sin(1/4*(4*c^2*d*\log(f)^2 - e^2*f + 4*d*f^2)/(c^2*\log(f)^2 + f^2)))*\operatorname{erf}(1/2*(2*(c*\log(f) - I*f)*x - I*e)/\sqrt{-c*\log(f) + I*f}) + (-I*f^{1/4*c*e^2/(c^2*\log(f)^2 + f^2)})*f^a*\cos(1/4*(4*c^2*d*\log(f)^2 - e^2*f + 4*d*f^2)/(c^2*\log(f)^2 + f^2)) + f^{1/4*c*e^2/(c^2*\log(f)^2 + f^2)}*f^a*\sin(1/4*(4*c^2*d*\log(f)^2 - e^2*f + 4*d*f^2)/(c^2*\log(f)^2 + f^2)))*\operatorname{erf}(1/2*(2*(c*\log(f) + I*f)*x + I*e)/\sqrt{-c*\log(f) - I*f}) + \sqrt{c*\log(f) + \sqrt{c^2*\log(f)^2 + f^2}} - \sqrt{\pi}*\sqrt{2*c^2*\log(f)^2 + 2*f^2}*((f^{1/4*c*e^2/(c^2*\log(f)^2 + f^2)})*f^a*\cos(1/4*(4*c^2*d*\log(f)^2 - e^2*f + 4*d*f^2)/(c^2*\log(f)^2 + f^2)) - I*f^{1/4*c*e^2/(c^2*\log(f)^2 + f^2)}*f^a*\sin(1/4*(4*c^2*d*\log(f)^2 - e^2*f + 4*d*f^2)/(c^2*\log(f)^2 + f^2)))*\operatorname{erf}(1/2*(2*(c*\log(f) - I*f)*x - I*e)/\sqrt{-c*\log(f) + I*f}) + (f^{1/4*c*e^2/(c^2*\log(f)^2 + f^2)})*f^a*\cos(1/4*(4*c^2*d*\log(f)^2 - e^2*f + 4*d*f^2)/(c^2*\log(f)^2 + f^2)) + I*f^{1/4*c*e^2/(c^2*\log(f)^2 + f^2)}*f^a*\sin(1/4*(4*c^2*d*\log(f)^2 - e^2*f + 4*d*f^2)/(c^2*\log(f)^2 + f^2)))*\operatorname{erf}(1/2*(2*(c*\log(f) + I*f)*x + I*e)/\sqrt{-c*\log(f) - I*f}) + \sqrt{-c*\log(f) + \sqrt{c^2*\log(f)^2 + f^2}})/(c^2*\log(f)^2 + f^2)$

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int f^{cx^2+a} \cos(fx^2 + ex + d) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(f^(a + c*x^2)*cos(d + e*x + f*x^2),x)

[Out] int(f^(a + c*x^2)*cos(d + e*x + f*x^2), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int f^{a+cx^2} \cos(d + ex + fx^2) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f**(c*x**2+a)*cos(f*x**2+e*x+d),x)

[Out] Integral(f**(a + c*x**2)*cos(d + e*x + f*x**2), x)

3.123 $\int f^{a+cx^2} \cos^2(d + ex + fx^2) dx$

Optimal. Leaf size=211

$$\frac{\sqrt{\pi} f^a e^{-\frac{e^2}{-c \log(f)+2if} - 2id} \operatorname{erf}\left(\frac{x(-c \log(f)+2if)+ie}{\sqrt{-c \log(f)+2if}}\right)}{8\sqrt{-c \log(f)+2if}} + \frac{\sqrt{\pi} f^a e^{\frac{e^2}{c \log(f)+2if} + 2id} \operatorname{erfi}\left(\frac{x(c \log(f)+2if)+ie}{\sqrt{c \log(f)+2if}}\right)}{8\sqrt{c \log(f)+2if}} + \frac{\sqrt{\pi} f^a \operatorname{erfi}\left(\sqrt{c} x \sqrt{\log(f)}\right)}{4\sqrt{c} \sqrt{\log(f)}}$$

[Out] $\frac{1}{4} f^a \operatorname{erfi}\left(x \sqrt{c} \ln(f)^{1/2}\right) \frac{\pi^{1/2}}{c^{1/2} \ln(f)^{1/2}} + \frac{1}{8} \exp(-2 * I * d - e^2 / (2 * I * f - c * \ln(f))) * f^a * \operatorname{erf}\left(\frac{I * e + x * (2 * I * f - c * \ln(f))}{(2 * I * f - c * \ln(f))^{1/2}}\right) \frac{\pi^{1/2}}{(2 * I * f - c * \ln(f))^{1/2}} + \frac{1}{8} \exp(2 * I * d + e^2 / (2 * I * f + c * \ln(f))) * f^a * \operatorname{erfi}\left(\frac{I * e + x * (2 * I * f + c * \ln(f))}{(2 * I * f + c * \ln(f))^{1/2}}\right) \frac{\pi^{1/2}}{(2 * I * f + c * \ln(f))^{1/2}}$

Rubi [A] time = 0.36, antiderivative size = 211, normalized size of antiderivative = 1.00, number of steps used = 9, number of rules used = 5, integrand size = 23, $\frac{\text{number of rules}}{\text{integrand size}} = 0.217$, Rules used = {4473, 2204, 2287, 2234, 2205}

$$\frac{\sqrt{\pi} f^a e^{-\frac{e^2}{-c \log(f)+2if} - 2id} \operatorname{Erf}\left(\frac{x(-c \log(f)+2if)+ie}{\sqrt{-c \log(f)+2if}}\right)}{8\sqrt{-c \log(f)+2if}} + \frac{\sqrt{\pi} f^a e^{\frac{e^2}{c \log(f)+2if} + 2id} \operatorname{Erfi}\left(\frac{x(c \log(f)+2if)+ie}{\sqrt{c \log(f)+2if}}\right)}{8\sqrt{c \log(f)+2if}} + \frac{\sqrt{\pi} f^a \operatorname{Erfi}\left(\sqrt{c} x \sqrt{\log(f)}\right)}{4\sqrt{c} \sqrt{\log(f)}}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[f^{(a + c*x^2)} * \operatorname{Cos}[d + e*x + f*x^2]^2, x]$

[Out] $\frac{(f^a \sqrt{\pi} \operatorname{Erfi}[\sqrt{c} x \sqrt{\log(f)}]) / (4 \sqrt{c} \sqrt{\log(f)}) + (E^{(-2 * I * d - e^2 / ((2 * I * f - c * \log(f))))} * f^a \sqrt{\pi} \operatorname{Erf}[(I * e + x * ((2 * I * f - c * \log(f))) / \sqrt{(2 * I * f - c * \log(f))}] / (8 \sqrt{(2 * I * f - c * \log(f))}) + (E^{(2 * I * d + e^2 / ((2 * I * f + c * \log(f))))} * f^a \sqrt{\pi} \operatorname{Erfi}[(I * e + x * ((2 * I * f + c * \log(f))) / \sqrt{(2 * I * f + c * \log(f))}] / (8 \sqrt{(2 * I * f + c * \log(f))})$

Rule 2204

$\operatorname{Int}[(F_)^{((a_.) + (b_.) * ((c_.) + (d_.) * (x_)^2))}, x_Symbol] \rightarrow \operatorname{Simp}[(F^a \sqrt{\pi} \operatorname{Erfi}[(c + d * x) \operatorname{Rt}[b * \log[F], 2]]) / (2 * d * \operatorname{Rt}[b * \log[F], 2]), x] /;$ $\operatorname{FreeQ}\{F, a, b, c, d\}, x\} \&\& \operatorname{PosQ}[b]$

Rule 2205

$\operatorname{Int}[(F_)^{((a_.) + (b_.) * ((c_.) + (d_.) * (x_)^2))}, x_Symbol] \rightarrow \operatorname{Simp}[(F^a \sqrt{\pi} \operatorname{Erf}[(c + d * x) \operatorname{Rt}[-(b * \log[F]), 2]]) / (2 * d * \operatorname{Rt}[-(b * \log[F]), 2]), x] /;$ $\operatorname{FreeQ}\{F, a, b, c, d\}, x\} \&\& \operatorname{NegQ}[b]$

Rule 2234

$\operatorname{Int}[(F_)^{((a_.) + (b_.) * (x_) + (c_.) * (x_)^2))}, x_Symbol] \rightarrow \operatorname{Dist}[F^{(a - b^2 / (4 * c))}, \operatorname{Int}[F^{((b + 2 * c * x)^2 / (4 * c))}, x], x] /;$ $\operatorname{FreeQ}\{F, a, b, c\}, x\}$

Rule 2287

$\operatorname{Int}[(u_.) * (F_)^{(v_.) * (G_)^{(w_.)}}, x_Symbol] \rightarrow \operatorname{With}\{z = v * \log[F] + w * \log[G]\}, \operatorname{Int}[u * \operatorname{NormalizeIntegrand}[E^z, x], x] /;$ $\operatorname{BinomialQ}[z, x] \mid \mid (\operatorname{PolynomialQ}[z, x] \&\& \operatorname{LeQ}[\operatorname{Exponent}[z, x], 2]) /;$ $\operatorname{FreeQ}\{F, G\}, x\}$

Rule 4473

$\operatorname{Int}[\operatorname{Cos}[v_]^{(n_.)} * (F_)^{(u_.)}, x_Symbol] \rightarrow \operatorname{Int}[\operatorname{ExpandTrigToExp}[F^u, \operatorname{Cos}[v]^n], x] /;$ $\operatorname{FreeQ}[F, x] \&\& (\operatorname{LinearQ}[u, x] \mid \mid \operatorname{PolyQ}[u, x, 2]) \&\& (\operatorname{LinearQ}[v,$

x] || PolyQ[v, x, 2]) && IGtQ[n, 0]

Rubi steps

$$\begin{aligned}
 \int f^{a+cx^2} \cos^2(d+ex+fx^2) dx &= \int \left(\frac{1}{2} f^{a+cx^2} + \frac{1}{4} e^{-2id-2iex-2ifx^2} f^{a+cx^2} + \frac{1}{4} e^{2id+2iex+2ifx^2} f^{a+cx^2} \right) dx \\
 &= \frac{1}{4} \int e^{-2id-2iex-2ifx^2} f^{a+cx^2} dx + \frac{1}{4} \int e^{2id+2iex+2ifx^2} f^{a+cx^2} dx + \frac{1}{2} \int f^{a+cx^2} dx \\
 &= \frac{f^a \sqrt{\pi} \operatorname{erfi}(\sqrt{c} x \sqrt{\log(f)})}{4\sqrt{c} \sqrt{\log(f)}} + \frac{1}{4} \int \exp(-2id-2iex+a \log(f)-x^2(2if-c \log(f))) f^{a+cx^2} dx \\
 &= \frac{f^a \sqrt{\pi} \operatorname{erfi}(\sqrt{c} x \sqrt{\log(f)})}{4\sqrt{c} \sqrt{\log(f)}} + \frac{1}{4} \left(e^{-2id-\frac{e^2}{2if-c \log(f)}} f^a \right) \int \exp\left(\frac{(-2ie+2x(-2if+c \log(f)))}{4(-2if+c \log(f))}\right) f^{a+cx^2} dx \\
 &= \frac{f^a \sqrt{\pi} \operatorname{erfi}(\sqrt{c} x \sqrt{\log(f)})}{4\sqrt{c} \sqrt{\log(f)}} + \frac{e^{-2id-\frac{e^2}{2if-c \log(f)}} f^a \sqrt{\pi} \operatorname{erf}\left(\frac{ie+x(2if-c \log(f))}{\sqrt{2if-c \log(f)}}\right)}{8\sqrt{2if-c \log(f)}} + \frac{e^{2id+\frac{e^2}{2if-c \log(f)}} f^a \sqrt{\pi} \operatorname{erf}\left(\frac{ie+x(2if-c \log(f))}{\sqrt{2if-c \log(f)}}\right)}{8\sqrt{2if-c \log(f)}}
 \end{aligned}$$

Mathematica [A] time = 2.32, size = 252, normalized size = 1.19

$$\frac{1}{8} \sqrt{\pi} f^a \left(\frac{2 \operatorname{erfi}(\sqrt{c} x \sqrt{\log(f)})}{\sqrt{c} \sqrt{\log(f)}} + \frac{\sqrt[4]{-1} \left(\sqrt{2f-ic \log(f)} (2f+ic \log(f)) (\sin(2d)-i \cos(2d)) e^{\frac{e^2}{c \log(f)+2if}} \operatorname{erfi}\left(\frac{\sqrt[4]{-1} (2f+ic \log(f))}{\sqrt{2f-ic \log(f)}}\right) \right)}{8 \sqrt{2f-ic \log(f)}} \right)$$

Warning: Unable to verify antiderivative.

[In] Integrate[f^(a + c*x^2)*Cos[d + e*x + f*x^2]^2,x]

[Out] (f^a*Sqrt[Pi]*((2*Erfi[Sqrt[c]*x*Sqrt[Log[f]]])/(Sqrt[c]*Sqrt[Log[f]])) + ((-1)^(1/4)*(-E^(e^2/((-2*I)*f + c*Log[f]))*Erfi[(((-1)^(3/4)*(e + 2*f*x + I*c*x*Log[f]))/Sqrt[2*f + I*c*Log[f]])*(2*f - I*c*Log[f])*Sqrt[2*f + I*c*Log[f]]*(Cos[2*d] - I*Sin[2*d])) + E^(e^2/((2*I)*f + c*Log[f]))*Erfi[(((-1)^(1/4)*(e + 2*f*x - I*c*x*Log[f]))/Sqrt[2*f - I*c*Log[f]])*(2*f + I*c*Log[f])*Sqrt[2*f - I*c*Log[f]]*(Cos[2*d] + I*Sin[2*d]))]/(4*f^2 + c^2*Log[f]^2)))/8

fricas [B] time = 1.51, size = 361, normalized size = 1.71

$$\frac{2 \sqrt{\pi} (c^2 \log(f)^2 + 4 f^2) \sqrt{-c \log(f)} f^a \operatorname{erf}(\sqrt{-c \log(f)} x) + \sqrt{\pi} (c^2 \log(f)^2 - 2 i c f \log(f)) \sqrt{-c \log(f) - 2 i f} \operatorname{erf}\left(\frac{\sqrt{-c \log(f) - 2 i f} x}{\sqrt{-c \log(f)}}\right)}{8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(c*x^2+a)*cos(f*x^2+e*x+d)^2,x, algorithm="fricas")

[Out] -1/8*(2*sqrt(pi)*(c^2*log(f)^2 + 4*f^2)*sqrt(-c*log(f))*f^a*erf(sqrt(-c*log(f))*x) + sqrt(pi)*(c^2*log(f)^2 - 2*I*c*f*log(f))*sqrt(-c*log(f) - 2*I*f)*erf((c^2*x*log(f)^2 + 4*f^2*x + I*c*e*log(f) + 2*e*f)*sqrt(-c*log(f) - 2*I*f)/(c^2*log(f)^2 + 4*f^2))*e^((a*c^2*log(f)^3 + 2*I*c^2*d*log(f)^2 - 2*I*e^2*f + 8*I*d*f^2 + (c*e^2 + 4*a*f^2)*log(f))/(c^2*log(f)^2 + 4*f^2)) + sqrt(pi)*(c^2*log(f)^2 + 2*I*c*f*log(f))*sqrt(-c*log(f) + 2*I*f)*erf((c^2*x*log(f)^2 + 4*f^2*x - I*c*e*log(f) + 2*e*f)*sqrt(-c*log(f) + 2*I*f)/(c^2*log(f)^2 + 4*f^2))*e^((a*c^2*log(f)^3 - 2*I*c^2*d*log(f)^2 + 2*I*e^2*f - 8*I*d*f^2 + (c*e^2 + 4*a*f^2)*log(f))/(c^2*log(f)^2 + 4*f^2)))/8

+ (c*e^2 + 4*a*f^2)*log(f))/(c^2*log(f)^2 + 4*f^2)))/(c^3*log(f)^3 + 4*c*f^2*log(f))

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int f^{cx^2+a} \cos(fx^2 + ex + d)^2 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(c*x^2+a)*cos(f*x^2+e*x+d)^2,x, algorithm="giac")

[Out] integrate(f^(c*x^2 + a)*cos(f*x^2 + e*x + d)^2, x)

maple [A] time = 0.31, size = 191, normalized size = 0.91

$$\frac{\sqrt{\pi} f^a e^{-\frac{2id \ln(f)c+4df-e^2}{-2if+c \ln(f)}} \operatorname{erf}\left(x\sqrt{2if-c \ln(f)} + \frac{ie}{\sqrt{2if-c \ln(f)}}\right)}{8\sqrt{2if-c \ln(f)}} - \frac{\sqrt{\pi} f^a e^{\frac{2id \ln(f)c-4df+e^2}{2if+c \ln(f)}} \operatorname{erf}\left(-\sqrt{-2if-c \ln(f)} x + \frac{ie}{\sqrt{-2if-c \ln(f)}}\right)}{8\sqrt{-2if-c \ln(f)}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(f^(c*x^2+a)*cos(f*x^2+e*x+d)^2,x)

[Out] 1/8*Pi^(1/2)*f^a*exp(-(2*I*d*ln(f)*c+4*d*f-e^2)/(-2*I*f+c*ln(f)))/(2*I*f-c*ln(f))^(1/2)*erf(x*(2*I*f-c*ln(f))^(1/2)+I*e/(2*I*f-c*ln(f))^(1/2))-1/8*Pi^(1/2)*f^a*exp((2*I*d*ln(f)*c-4*d*f+e^2)/(2*I*f+c*ln(f)))/(-2*I*f-c*ln(f))^(1/2)*erf(-(-2*I*f-c*ln(f))^(1/2)*x+I*e/(-2*I*f-c*ln(f))^(1/2))+1/4*f^a*Pi^(1/2)/(-c*ln(f))^(1/2)*erf((-c*ln(f))^(1/2)*x)

maxima [C] time = 0.36, size = 863, normalized size = 4.09

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(c*x^2+a)*cos(f*x^2+e*x+d)^2,x, algorithm="maxima")

[Out] 1/16*(sqrt(pi)*sqrt(2*c^2*log(f)^2 + 8*f^2)*((I*f^(c*e^2/(c^2*log(f)^2 + 4*f^2))*f^a*cos(2*(c^2*d*log(f)^2 - e^2*f + 4*d*f^2)/(c^2*log(f)^2 + 4*f^2)) + f^(c*e^2/(c^2*log(f)^2 + 4*f^2))*f^a*sin(2*(c^2*d*log(f)^2 - e^2*f + 4*d*f^2)/(c^2*log(f)^2 + 4*f^2)))*erf(((c*log(f) - 2*I*f)*x - I*e)/sqrt(-c*log(f) + 2*I*f)) + (-I*f^(c*e^2/(c^2*log(f)^2 + 4*f^2))*f^a*cos(2*(c^2*d*log(f)^2 - e^2*f + 4*d*f^2)/(c^2*log(f)^2 + 4*f^2)) + f^(c*e^2/(c^2*log(f)^2 + 4*f^2))*f^a*sin(2*(c^2*d*log(f)^2 - e^2*f + 4*d*f^2)/(c^2*log(f)^2 + 4*f^2)))*erf(((c*log(f) + 2*I*f)*x + I*e)/sqrt(-c*log(f) - 2*I*f)))*sqrt(c*log(f) + sqrt(c^2*log(f)^2 + 4*f^2))*sqrt(-c*log(f)) - sqrt(pi)*sqrt(2*c^2*log(f)^2 + 8*f^2)*((f^(c*e^2/(c^2*log(f)^2 + 4*f^2))*f^a*cos(2*(c^2*d*log(f)^2 - e^2*f + 4*d*f^2)/(c^2*log(f)^2 + 4*f^2)) - I*f^(c*e^2/(c^2*log(f)^2 + 4*f^2))*f^a*sin(2*(c^2*d*log(f)^2 - e^2*f + 4*d*f^2)/(c^2*log(f)^2 + 4*f^2)))*erf(((c*log(f) - 2*I*f)*x - I*e)/sqrt(-c*log(f) + 2*I*f)) + (f^(c*e^2/(c^2*log(f)^2 + 4*f^2))*f^a*cos(2*(c^2*d*log(f)^2 - e^2*f + 4*d*f^2)/(c^2*log(f)^2 + 4*f^2)) + I*f^(c*e^2/(c^2*log(f)^2 + 4*f^2))*f^a*sin(2*(c^2*d*log(f)^2 - e^2*f + 4*d*f^2)/(c^2*log(f)^2 + 4*f^2)))*erf(((c*log(f) + 2*I*f)*x + I*e)/sqrt(-c*log(f) - 2*I*f)))*sqrt(-c*log(f) + sqrt(c^2*log(f)^2 + 4*f^2))*sqrt(-c*log(f)) + 2*sqrt(pi)*((c^2*f^a*log(f)^2 + 4*f^(a + 2))*erf(x*conjugate(sqrt(-c*log(f)))) + (c^2*f^a*log(f)^2 + 4*f^(a + 2))*erf(sqrt(-c*log(f))*x)))/((c^2*log(f)^2 + 4*f^2)*sqrt(-c*log(f)))

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int f^{cx^2+a} \cos(fx^2 + ex + d)^2 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(f^(a + c*x^2)*cos(d + e*x + f*x^2)^2,x)`

[Out] `int(f^(a + c*x^2)*cos(d + e*x + f*x^2)^2, x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int f^{a+cx^2} \cos^2(d + ex + fx^2) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(f**(c*x**2+a)*cos(f*x**2+e*x+d)**2,x)`

[Out] `Integral(f**(a + c*x**2)*cos(d + e*x + f*x**2)**2, x)`

3.124 $\int f^{a+cx^2} \cos^3(d + ex + fx^2) dx$

Optimal. Leaf size=369

$$\frac{\sqrt{\pi} f^a \exp\left(-\frac{9e^2}{4(-c \log(f)+3if)} - 3id\right) \operatorname{erf}\left(\frac{2x(-c \log(f)+3if)+3ie}{2\sqrt{-c \log(f)+3if}}\right)}{16\sqrt{-c \log(f)+3if}} + \frac{3\sqrt{\pi} f^a e^{-\frac{e^2}{-4c \log(f)+4if} - id} \operatorname{erf}\left(\frac{2x(-c \log(f)+if)+ie}{2\sqrt{-c \log(f)+if}}\right)}{16\sqrt{-c \log(f)+if}} + \frac{3\sqrt{\pi} f^a e^{-\frac{e^2}{-4c \log(f)+4if} - id} \operatorname{erf}\left(\frac{2x(-c \log(f)+if)+ie}{2\sqrt{-c \log(f)+if}}\right)}{16\sqrt{-c \log(f)+if}}$$

[Out] $3/16*\exp(-I*d-e^2/(4*I*f-4*c*\ln(f)))*f^a*\operatorname{erf}(1/2*(I*e+2*x*(I*f-c*\ln(f))))/(I*f-c*\ln(f))^{(1/2)}*\operatorname{Pi}^{(1/2)}/(I*f-c*\ln(f))^{(1/2)}+1/16*\exp(-3*I*d-9/4*e^2/(3*I*f-c*\ln(f)))*f^a*\operatorname{erf}(1/2*(3*I*e+2*x*(3*I*f-c*\ln(f))))/(3*I*f-c*\ln(f))^{(1/2)}*\operatorname{Pi}^{(1/2)}/(3*I*f-c*\ln(f))^{(1/2)}+3/16*\exp(I*d+e^2/(4*I*f+4*c*\ln(f)))*f^a*\operatorname{erfi}(1/2*(I*e+2*x*(I*f+c*\ln(f))))/(I*f+c*\ln(f))^{(1/2)}*\operatorname{Pi}^{(1/2)}/(I*f+c*\ln(f))^{(1/2)}+1/16*\exp(3*I*d+9/4*e^2/(3*I*f+c*\ln(f)))*f^a*\operatorname{erfi}(1/2*(3*I*e+2*x*(3*I*f+c*\ln(f))))/(3*I*f+c*\ln(f))^{(1/2)}*\operatorname{Pi}^{(1/2)}/(3*I*f+c*\ln(f))^{(1/2)}$

Rubi [A] time = 0.58, antiderivative size = 369, normalized size of antiderivative = 1.00, number of steps used = 14, number of rules used = 5, integrand size = 23, $\frac{\text{number of rules}}{\text{integrand size}} = 0.217$, Rules used = {4473, 2287, 2234, 2205, 2204}

$$\frac{\sqrt{\pi} f^a \exp\left(-\frac{9e^2}{4(-c \log(f)+3if)} - 3id\right) \operatorname{Erf}\left(\frac{2x(-c \log(f)+3if)+3ie}{2\sqrt{-c \log(f)+3if}}\right)}{16\sqrt{-c \log(f)+3if}} + \frac{3\sqrt{\pi} f^a e^{-\frac{e^2}{-4c \log(f)+4if} - id} \operatorname{Erf}\left(\frac{2x(-c \log(f)+if)+ie}{2\sqrt{-c \log(f)+if}}\right)}{16\sqrt{-c \log(f)+if}} + \frac{3\sqrt{\pi} f^a e^{-\frac{e^2}{-4c \log(f)+4if} - id} \operatorname{Erf}\left(\frac{2x(-c \log(f)+if)+ie}{2\sqrt{-c \log(f)+if}}\right)}{16\sqrt{-c \log(f)+if}}$$

Antiderivative was successfully verified.

[In] `Int[f^(a + c*x^2)*Cos[d + e*x + f*x^2]^3,x]`

[Out] $(3*E^{((-I)*d - e^2/((4*I)*f - 4*c*\operatorname{Log}[f]))}*f^a*\operatorname{Sqrt}[\operatorname{Pi}]*\operatorname{Erf}[(I*e + 2*x*(I*f - c*\operatorname{Log}[f]))/(2*\operatorname{Sqrt}[I*f - c*\operatorname{Log}[f]])])/(16*\operatorname{Sqrt}[I*f - c*\operatorname{Log}[f]]) + (E^{((-3*I)*d - (9*e^2)/(4*((3*I)*f - c*\operatorname{Log}[f])))*f^a*\operatorname{Sqrt}[\operatorname{Pi}]*\operatorname{Erf}[(3*I)*e + 2*x*((3*I)*f - c*\operatorname{Log}[f]))/(2*\operatorname{Sqrt}[(3*I)*f - c*\operatorname{Log}[f]])])/(16*\operatorname{Sqrt}[(3*I)*f - c*\operatorname{Log}[f]]) + (3*E^{(I*d + e^2/((4*I)*f + 4*c*\operatorname{Log}[f]))}*f^a*\operatorname{Sqrt}[\operatorname{Pi}]*\operatorname{Erfi}[(I*e + 2*x*(I*f + c*\operatorname{Log}[f]))/(2*\operatorname{Sqrt}[I*f + c*\operatorname{Log}[f]])])/(16*\operatorname{Sqrt}[I*f + c*\operatorname{Log}[f]]) + (E^{((3*I)*d + (9*e^2)/(4*((3*I)*f + c*\operatorname{Log}[f])))*f^a*\operatorname{Sqrt}[\operatorname{Pi}]*\operatorname{Erfi}[(3*I)*e + 2*x*((3*I)*f + c*\operatorname{Log}[f]))/(2*\operatorname{Sqrt}[(3*I)*f + c*\operatorname{Log}[f]])])/(16*\operatorname{Sqrt}[(3*I)*f + c*\operatorname{Log}[f]])$

Rule 2204

`Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_)^2), x_Symbol] := Simp[(F^a*Sqrt[Pi]*Erfi[(c + d*x)*Rt[b*Log[F], 2]])/(2*d*Rt[b*Log[F], 2]), x] /; FreeQ[{F, a, b, c, d}, x] && PosQ[b]`

Rule 2205

`Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_)^2), x_Symbol] := Simp[(F^a*Sqrt[Pi]*Erf[(c + d*x)*Rt[-(b*Log[F]), 2]])/(2*d*Rt[-(b*Log[F]), 2]), x] /; FreeQ[{F, a, b, c, d}, x] && NegQ[b]`

Rule 2234

`Int[(F_)^((a_.) + (b_.)*(x_) + (c_.)*(x_)^2), x_Symbol] := Dist[F^(a - b^2/(4*c)), Int[F^((b + 2*c*x)^2/(4*c)), x], x] /; FreeQ[{F, a, b, c}, x]`

Rule 2287

`Int[(u_.)*(F_)^(v_.)*(G_)^(w_.), x_Symbol] := With[{z = v*Log[F] + w*Log[G]}, Int[u*NormalizeIntegrand[E^z, x], x] /; BinomialQ[z, x] || (PolynomialQ[z,`

x] && LeQ[Exponent[z, x], 2]]) /; FreeQ[{F, G}, x]

Rule 4473

Int[Cos[v_]^(n_.)*(F_)^(u_), x_Symbol] := Int[ExpandTrigToExp[F^u, Cos[v]^n, x], x] /; FreeQ[F, x] && (LinearQ[u, x] || PolyQ[u, x, 2]) && (LinearQ[v, x] || PolyQ[v, x, 2]) && IGtQ[n, 0]

Rubi steps

$$\begin{aligned} \int f^{a+cx^2} \cos^3(d+ex+fx^2) dx &= \int \left(\frac{1}{8} e^{-3i(d+ex+fx^2)} f^{a+cx^2} + \frac{3}{8} \exp(2id+2iex+2ifx^2-3i(d+ex+fx^2)) f^{a+cx^2} \right) dx \\ &= \frac{1}{8} \int e^{-3i(d+ex+fx^2)} f^{a+cx^2} dx + \frac{1}{8} \int \exp(6id+6iex+6ifx^2-3i(d+ex+fx^2)) f^{a+cx^2} dx \\ &= \frac{1}{8} \int \exp(-3id-3iex+a \log(f)-x^2(3if-c \log(f))) dx + \frac{1}{8} \int \exp(3id+3iex+3ifx^2-3i(d+ex+fx^2)) f^{a+cx^2} dx \\ &= \frac{1}{8} \left(3e^{-id-\frac{e^2}{4if-4c \log(f)}} f^a \right) \int \exp\left(\frac{(-ie+2x(-if+c \log(f)))^2}{4(-if+c \log(f))}\right) dx + \frac{1}{8} \left(e^{-3id-\frac{9e^2}{4(3if-c \log(f))}} f^a \right) \int \exp\left(\frac{(3ie+2x(-if+c \log(f)))^2}{4(-if+c \log(f))}\right) dx \\ &= \frac{3e^{-id-\frac{e^2}{4if-4c \log(f)}} f^a \sqrt{\pi} \operatorname{erf}\left(\frac{ie+2x(if-c \log(f))}{2\sqrt{if-c \log(f)}}\right)}{16\sqrt{if-c \log(f)}} + \frac{e^{-3id-\frac{9e^2}{4(3if-c \log(f))}} f^a \sqrt{\pi} \operatorname{erf}\left(\frac{3ie+2x(-if+c \log(f))}{2\sqrt{3if-c \log(f)}}\right)}{16\sqrt{3if-c \log(f)}} \end{aligned}$$

Mathematica [B] time = 6.95, size = 2997, normalized size = 8.12

Result too large to show

Warning: Unable to verify antiderivative.

[In] Integrate[f^(a + c*x^2)*Cos[d + e*x + f*x^2]^3,x]

[Out] (f^a*Sqrt[Pi]*((-27*(-1)^(3/4)*f^3*Cos[d]*Erfi[((-1)^(1/4)*(e + 2*f*x - (2*I)*c*x*Log[f]))/(2*Sqrt[f - I*c*Log[f]])]*Sqrt[f - I*c*Log[f]])/E^(((I/4)*e^2)/(f - I*c*Log[f])) + (27*(-1)^(1/4)*c*f^2*Cos[d]*Erfi[((-1)^(1/4)*(e + 2*f*x - (2*I)*c*x*Log[f]))/(2*Sqrt[f - I*c*Log[f]])]*Log[f]*Sqrt[f - I*c*Log[f]])/E^(((I/4)*e^2)/(f - I*c*Log[f])) - (3*(-1)^(3/4)*c^2*f*Cos[d]*Erfi[((-1)^(1/4)*(e + 2*f*x - (2*I)*c*x*Log[f]))/(2*Sqrt[f - I*c*Log[f]])]*Log[f]^2*Sqrt[f - I*c*Log[f]])/E^(((I/4)*e^2)/(f - I*c*Log[f])) + (3*(-1)^(1/4)*c^3*Cos[d]*Erfi[((-1)^(1/4)*(e + 2*f*x - (2*I)*c*x*Log[f]))/(2*Sqrt[f - I*c*Log[f]])]*Log[f]^3*Sqrt[f - I*c*Log[f]])/E^(((I/4)*e^2)/(f - I*c*Log[f])) - (3*(-1)^(3/4)*f^3*Cos[3*d]*Erfi[((-1)^(1/4)*(3*e + 6*f*x - (2*I)*c*x*Log[f]))/(2*Sqrt[3*f - I*c*Log[f]])]*Sqrt[3*f - I*c*Log[f]])/E^(((9*I)/4)*e^2)/(3*f - I*c*Log[f])) + ((-1)^(1/4)*c*f^2*Cos[3*d]*Erfi[((-1)^(1/4)*(3*e + 6*f*x - (2*I)*c*x*Log[f]))/(2*Sqrt[3*f - I*c*Log[f]])]*Log[f]*Sqrt[3*f - I*c*Log[f]])/E^(((9*I)/4)*e^2)/(3*f - I*c*Log[f])) - (3*(-1)^(3/4)*c^2*f*Cos[3*d]*Erfi[((-1)^(1/4)*(3*e + 6*f*x - (2*I)*c*x*Log[f]))/(2*Sqrt[3*f - I*c*Log[f]])]*Log[f]^2*Sqrt[3*f - I*c*Log[f]])/E^(((9*I)/4)*e^2)/(3*f - I*c*Log[f])) + ((-1)^(1/4)*c^3*Cos[3*d]*Erfi[((-1)^(1/4)*(3*e + 6*f*x - (2*I)*c*x*Log[f]))/(2*Sqrt[3*f - I*c*Log[f]])]*Log[f]^3*Sqrt[3*f - I*c*Log[f]])/E^(((9*I)/4)*e^2)/(3*f - I*c*Log[f])) - 27*(-1)^(1/4)*E^(((I/4)*e^2)/(f + I*c*Log[f]))*f^3*Cos[d]*Erfi[((-1)^(3/4)*(e + 2*f*x + (2*I)*c*x*Log[f]))/(2*Sqrt[f + I*c*Log[f]])]*Sqrt[f + I*c*Log[f]] + 27*(-1)^(3/4)*c*E^(((I/4)*e^2)/(f + I*c*Log[f]))*f^2*Cos[d]*Erfi[((-1)^(3/4)*(e + 2*f*x + (2*I)*c*x*Log[f]))/(2*Sqrt[f + I*c*Log[f]])]*Log[f]*Sqrt[f + I*c*Log[f]] - 3*(-1)^(1/4)*c^2*E^(((I/4)*e^2)/(f + I*c*Log[f]))*f*Cos[d]*Erfi[((-1)^(3/4)*(e + 2*f*x + (2*I)*c*x*Log[f]))/(2*Sqrt[f + I*c*Log[f]])]*Log[f]^2*Sqrt[f + I*c*Log[f]] + 3*(-1)^(3/4)*c^3*E^(((I/4)*e^2)/(f + I*c*Log[f]))*Cos[d]*Erfi[((-1)^(3/4)*(e + 2*f*x + (2*I)*c*x*Log[f]))/(2*Sqrt[f + I*c*Log[f]])]*Log[f]^3*Sqrt[f + I*c*Log[f]]

$$\begin{aligned}
& 2*f*x + (2*I)*c*x*\text{Log}[f]))/(2*\text{Sqrt}[f + I*c*\text{Log}[f]])*\text{Log}[f]^3*\text{Sqrt}[f + I*c* \\
& \text{Log}[f] - 3*(-1)^{(1/4)}*E^{(((9*I)/4)*e^2)/(3*f + I*c*\text{Log}[f])}*f^3*\text{Cos}[3*d]* \\
& \text{Erfi}[((-1)^{(3/4)}*(3*e + 6*f*x + (2*I)*c*x*\text{Log}[f]))/(2*\text{Sqrt}[3*f + I*c*\text{Log}[f] \\
&])]*\text{Sqrt}[3*f + I*c*\text{Log}[f]] + (-1)^{(3/4)}*c*E^{(((9*I)/4)*e^2)/(3*f + I*c*\text{Log} \\
& [f])}*f^2*\text{Cos}[3*d]*\text{Erfi}[((-1)^{(3/4)}*(3*e + 6*f*x + (2*I)*c*x*\text{Log}[f]))/(2*\text{Sqr} \\
& \text{rt}[3*f + I*c*\text{Log}[f]])]*\text{Log}[f]*\text{Sqrt}[3*f + I*c*\text{Log}[f]] - 3*(-1)^{(1/4)}*c^2*E^{(\\
& (((9*I)/4)*e^2)/(3*f + I*c*\text{Log}[f])}*f*\text{Cos}[3*d]*\text{Erfi}[((-1)^{(3/4)}*(3*e + 6*f*x \\
& x + (2*I)*c*x*\text{Log}[f]))/(2*\text{Sqrt}[3*f + I*c*\text{Log}[f]])]*\text{Log}[f]^2*\text{Sqrt}[3*f + I*c* \\
& \text{Log}[f]] + (-1)^{(3/4)}*c^3*E^{(((9*I)/4)*e^2)/(3*f + I*c*\text{Log}[f])}*c*\text{Cos}[3*d]*\text{Er} \\
& \text{fi}[((-1)^{(3/4)}*(3*e + 6*f*x + (2*I)*c*x*\text{Log}[f]))/(2*\text{Sqrt}[3*f + I*c*\text{Log}[f]])] \\
&]*\text{Log}[f]^3*\text{Sqrt}[3*f + I*c*\text{Log}[f]] + (27*(-1)^{(1/4)}*f^3*\text{Erfi}[((-1)^{(1/4)}*(e \\
& + 2*f*x - (2*I)*c*x*\text{Log}[f]))/(2*\text{Sqrt}[f - I*c*\text{Log}[f]])]*\text{Sqrt}[f - I*c*\text{Log}[f]] \\
& *\text{Sin}[d])/E^{((I/4)*e^2)/(f - I*c*\text{Log}[f])} + (27*(-1)^{(3/4)}*c*f^2*\text{Erfi}[((-1) \\
& ^{(1/4)}*(e + 2*f*x - (2*I)*c*x*\text{Log}[f]))/(2*\text{Sqrt}[f - I*c*\text{Log}[f]])]*\text{Log}[f]*\text{Sqr} \\
& \text{t}[f - I*c*\text{Log}[f]]*\text{Sin}[d])/E^{((I/4)*e^2)/(f - I*c*\text{Log}[f])} + (3*(-1)^{(1/4)}* \\
& c^2*f*\text{Erfi}[((-1)^{(1/4)}*(e + 2*f*x - (2*I)*c*x*\text{Log}[f]))/(2*\text{Sqrt}[f - I*c*\text{Log}[f] \\
&])]*\text{Log}[f]^2*\text{Sqrt}[f - I*c*\text{Log}[f]]*\text{Sin}[d])/E^{((I/4)*e^2)/(f - I*c*\text{Log}[f])} \\
&) + (3*(-1)^{(3/4)}*c^3*\text{Erfi}[((-1)^{(1/4)}*(e + 2*f*x - (2*I)*c*x*\text{Log}[f]))/(2*S \\
& \text{qrt}[f - I*c*\text{Log}[f]])]*\text{Log}[f]^3*\text{Sqrt}[f - I*c*\text{Log}[f]]*\text{Sin}[d])/E^{((I/4)*e^2)/ \\
& (f - I*c*\text{Log}[f])} + 27*(-1)^{(3/4)}*E^{((I/4)*e^2)/(f + I*c*\text{Log}[f])}*f^3*\text{Erfi} \\
& [((-1)^{(3/4)}*(e + 2*f*x + (2*I)*c*x*\text{Log}[f]))/(2*\text{Sqrt}[f + I*c*\text{Log}[f]])]*\text{Sqrt} \\
& [f + I*c*\text{Log}[f]]*\text{Sin}[d] + 27*(-1)^{(1/4)}*c*E^{((I/4)*e^2)/(f + I*c*\text{Log}[f])}* \\
& f^2*\text{Erfi}[((-1)^{(3/4)}*(e + 2*f*x + (2*I)*c*x*\text{Log}[f]))/(2*\text{Sqrt}[f + I*c*\text{Log}[f] \\
&])]*\text{Log}[f]*\text{Sqrt}[f + I*c*\text{Log}[f]]*\text{Sin}[d] + 3*(-1)^{(3/4)}*c^2*E^{((I/4)*e^2)/(f \\
& + I*c*\text{Log}[f])}*f*\text{Erfi}[((-1)^{(3/4)}*(e + 2*f*x + (2*I)*c*x*\text{Log}[f]))/(2*\text{Sqrt}[\\
& f + I*c*\text{Log}[f]])]*\text{Log}[f]^2*\text{Sqrt}[f + I*c*\text{Log}[f]]*\text{Sin}[d] + 3*(-1)^{(1/4)}*c^3*E \\
& ^{((I/4)*e^2)/(f + I*c*\text{Log}[f])}*Erfi[((-1)^{(3/4)}*(e + 2*f*x + (2*I)*c*x*\text{Log} \\
& [f]))/(2*\text{Sqrt}[f + I*c*\text{Log}[f]])]*\text{Log}[f]^3*\text{Sqrt}[f + I*c*\text{Log}[f]]*\text{Sin}[d] + (3*(\\
& -1)^{(1/4)}*f^3*\text{Erfi}[((-1)^{(1/4)}*(3*e + 6*f*x - (2*I)*c*x*\text{Log}[f]))/(2*\text{Sqrt}[3*f \\
& - I*c*\text{Log}[f]])]*\text{Sqrt}[3*f - I*c*\text{Log}[f]]*\text{Sin}[3*d])/E^{(((9*I)/4)*e^2)/(3*f \\
& - I*c*\text{Log}[f])} + ((-1)^{(3/4)}*c*f^2*\text{Erfi}[((-1)^{(1/4)}*(3*e + 6*f*x - (2*I)*c* \\
& x*\text{Log}[f]))/(2*\text{Sqrt}[3*f - I*c*\text{Log}[f]])]*\text{Log}[f]*\text{Sqrt}[3*f - I*c*\text{Log}[f]]*\text{Sin}[3* \\
& d])/E^{(((9*I)/4)*e^2)/(3*f - I*c*\text{Log}[f])} + (3*(-1)^{(1/4)}*c^2*f*\text{Erfi}[((-1) \\
& ^{(1/4)}*(3*e + 6*f*x - (2*I)*c*x*\text{Log}[f]))/(2*\text{Sqrt}[3*f - I*c*\text{Log}[f]])]*\text{Log}[f] \\
& ^2*\text{Sqrt}[3*f - I*c*\text{Log}[f]]*\text{Sin}[3*d])/E^{(((9*I)/4)*e^2)/(3*f - I*c*\text{Log}[f])} \\
& + ((-1)^{(3/4)}*c^3*\text{Erfi}[((-1)^{(1/4)}*(3*e + 6*f*x - (2*I)*c*x*\text{Log}[f]))/(2*\text{Sqr} \\
& \text{t}[3*f - I*c*\text{Log}[f]])]*\text{Log}[f]^3*\text{Sqrt}[3*f - I*c*\text{Log}[f]]*\text{Sin}[3*d])/E^{(((9*I)/ \\
& 4)*e^2)/(3*f - I*c*\text{Log}[f])} + 3*(-1)^{(3/4)}*E^{(((9*I)/4)*e^2)/(3*f + I*c*Lo \\
& g[f])}*f^3*\text{Erfi}[((-1)^{(3/4)}*(3*e + 6*f*x + (2*I)*c*x*\text{Log}[f]))/(2*\text{Sqrt}[3*f + \\
& I*c*\text{Log}[f]])]*\text{Sqrt}[3*f + I*c*\text{Log}[f]]*\text{Sin}[3*d] + (-1)^{(1/4)}*c*E^{(((9*I)/4) \\
& *e^2)/(3*f + I*c*\text{Log}[f])}*f^2*\text{Erfi}[((-1)^{(3/4)}*(3*e + 6*f*x + (2*I)*c*x*\text{Log} \\
& [f]))/(2*\text{Sqrt}[3*f + I*c*\text{Log}[f]])]*\text{Log}[f]*\text{Sqrt}[3*f + I*c*\text{Log}[f]]*\text{Sin}[3*d] + \\
& 3*(-1)^{(3/4)}*c^2*E^{(((9*I)/4)*e^2)/(3*f + I*c*\text{Log}[f])}*f*\text{Erfi}[((-1)^{(3/4)}* \\
& (3*e + 6*f*x + (2*I)*c*x*\text{Log}[f]))/(2*\text{Sqrt}[3*f + I*c*\text{Log}[f]])]*\text{Log}[f]^2*\text{Sqrt} \\
& [3*f + I*c*\text{Log}[f]]*\text{Sin}[3*d] + (-1)^{(1/4)}*c^3*E^{(((9*I)/4)*e^2)/(3*f + I*c* \\
& \text{Log}[f])}*Erfi[((-1)^{(3/4)}*(3*e + 6*f*x + (2*I)*c*x*\text{Log}[f]))/(2*\text{Sqrt}[3*f + I \\
& *c*\text{Log}[f]])]*\text{Log}[f]^3*\text{Sqrt}[3*f + I*c*\text{Log}[f]]*\text{Sin}[3*d]))/(16*(f - I*c*\text{Log}[f] \\
&)*(3*f - I*c*\text{Log}[f])*(f + I*c*\text{Log}[f])*(3*f + I*c*\text{Log}[f]))
\end{aligned}$$

fricas [B] time = 0.93, size = 707, normalized size = 1.92

$$\frac{\sqrt{\pi} (c^3 \log(f)^3 - 3i c^2 f \log(f)^2 + c f^2 \log(f) - 3i f^3) \sqrt{-c \log(f) - 3i f} \operatorname{erf}\left(\frac{(2c^2 x \log(f)^2 + 18 f^2 x + 3i c e \log(f) + 9 e f)}{2(c^2 \log(f)^2 + 9 f^2)}\right)}{1}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(c*x^2+a)*cos(f*x^2+e*x+d)^3,x, algorithm="fricas")

[Out] -1/16*(sqrt(pi)*(c^3*log(f)^3 - 3*I*c^2*f*log(f)^2 + c*f^2*log(f) - 3*I*f^3

```
)*sqrt(-c*log(f) - 3*I*f)*erf(1/2*(2*c^2*x*log(f)^2 + 18*f^2*x + 3*I*c*e*log(f) + 9*e*f)*sqrt(-c*log(f) - 3*I*f)/(c^2*log(f)^2 + 9*f^2))*e^(1/4*(4*a*c^2*log(f)^3 + 12*I*c^2*d*log(f)^2 - 27*I*e^2*f + 108*I*d*f^2 + 9*(c*e^2 + 4*a*f^2)*log(f))/(c^2*log(f)^2 + 9*f^2)) + sqrt(pi)*(c^3*log(f)^3 + 3*I*c^2*f*log(f)^2 + c*f^2*log(f) + 3*I*f^3)*sqrt(-c*log(f) + 3*I*f)*erf(1/2*(2*c^2*x*log(f)^2 + 18*f^2*x - 3*I*c*e*log(f) + 9*e*f)*sqrt(-c*log(f) + 3*I*f)/(c^2*log(f)^2 + 9*f^2))*e^(1/4*(4*a*c^2*log(f)^3 - 12*I*c^2*d*log(f)^2 + 27*I*e^2*f - 108*I*d*f^2 + 9*(c*e^2 + 4*a*f^2)*log(f))/(c^2*log(f)^2 + 9*f^2)) + sqrt(pi)*(3*c^3*log(f)^3 - 3*I*c^2*f*log(f)^2 + 27*c*f^2*log(f) - 27*I*f^3)*sqrt(-c*log(f) - I*f)*erf(1/2*(2*c^2*x*log(f)^2 + 2*f^2*x + I*c*e*log(f) + e*f)*sqrt(-c*log(f) - I*f)/(c^2*log(f)^2 + f^2))*e^(1/4*(4*a*c^2*log(f)^3 + 4*I*c^2*d*log(f)^2 - I*e^2*f + 4*I*d*f^2 + (c*e^2 + 4*a*f^2)*log(f))/(c^2*log(f)^2 + f^2)) + sqrt(pi)*(3*c^3*log(f)^3 + 3*I*c^2*f*log(f)^2 + 27*c*f^2*log(f) + 27*I*f^3)*sqrt(-c*log(f) + I*f)*erf(1/2*(2*c^2*x*log(f)^2 + 2*f^2*x - I*c*e*log(f) + e*f)*sqrt(-c*log(f) + I*f)/(c^2*log(f)^2 + f^2))*e^(1/4*(4*a*c^2*log(f)^3 - 4*I*c^2*d*log(f)^2 + I*e^2*f - 4*I*d*f^2 + (c*e^2 + 4*a*f^2)*log(f))/(c^2*log(f)^2 + f^2)))/(c^4*log(f)^4 + 10*c^2*f^2*log(f)^2 + 9*f^4)
```

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int f^{cx^2+a} \cos(fx^2 + ex + d)^3 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(c*x^2+a)*cos(f*x^2+e*x+d)^3,x, algorithm="giac")

[Out] integrate(f^(c*x^2 + a)*cos(f*x^2 + e*x + d)^3, x)

maple [A] time = 0.70, size = 334, normalized size = 0.91

$$\frac{\sqrt{\pi} f^a e^{\frac{3(4id \ln(f)c+12df-3e^2)}{4(-3if+c \ln(f))}} \operatorname{erf}\left(x\sqrt{3if-c \ln(f)} + \frac{3ie}{2\sqrt{3if-c \ln(f)}}\right)}{16\sqrt{3if-c \ln(f)}} + \frac{3\sqrt{\pi} f^a e^{\frac{4df+4id \ln(f)c-e^2}{4(-if+c \ln(f))}} \operatorname{erf}\left(x\sqrt{if-c \ln(f)} + \frac{e}{2\sqrt{if-c \ln(f)}}\right)}{16\sqrt{if-c \ln(f)}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(f^(c*x^2+a)*cos(f*x^2+e*x+d)^3,x)

```
[Out] 1/16*Pi^(1/2)*f^a*exp(-3/4*(4*I*d*ln(f)*c+12*d*f-3*e^2)/(-3*I*f+c*ln(f)))/((3*I*f-c*ln(f))^(1/2)*erf(x*(3*I*f-c*ln(f))^(1/2)+3/2*I*e/(3*I*f-c*ln(f))^(1/2))+3/16*Pi^(1/2)*f^a*exp(-1/4*(4*d*f+4*I*d*ln(f)*c-e^2)/(-I*f+c*ln(f)))/(I*f-c*ln(f))^(1/2)*erf(x*(I*f-c*ln(f))^(1/2)+1/2*I*e/(I*f-c*ln(f))^(1/2))-3/16*Pi^(1/2)*f^a*exp(1/4*(-4*d*f+4*I*d*ln(f)*c+e^2)/(I*f+c*ln(f)))/(-I*f-c*ln(f))^(1/2)*erf(-(-I*f-c*ln(f))^(1/2)*x+1/2*I*e/(-I*f-c*ln(f))^(1/2))-1/16*Pi^(1/2)*f^a*exp(3/4*(4*I*d*ln(f)*c-12*d*f+3*e^2)/(3*I*f+c*ln(f)))/(-c*ln(f)-3*I*f)^(1/2)*erf(-(-c*ln(f)-3*I*f)^(1/2)*x+3/2*I*e/(-c*ln(f)-3*I*f)^(1/2)))
```

maxima [B] time = 0.41, size = 2183, normalized size = 5.92

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(c*x^2+a)*cos(f*x^2+e*x+d)^3,x, algorithm="maxima")

```
[Out] 1/32*(sqrt(pi)*sqrt(2*c^2*log(f)^2 + 18*f^2)*(((I*c^2*f^(9/4*c*e^2/(c^2*log(f)^2 + 9*f^2))*f^a*log(f)^2 + I*f^(9/4*c*e^2/(c^2*log(f)^2 + 9*f^2))*f^(a + 2))*cos(3/4*(4*c^2*d*log(f)^2 - 9*e^2*f + 36*d*f^2)/(c^2*log(f)^2 + 9*f^2
```



```

)) + (c^2*f^(9/4*c*e^2/(c^2*log(f)^2 + 9*f^2))*f^a*log(f)^2 + f^(9/4*c*e^2/
(c^2*log(f)^2 + 9*f^2))*f^(a + 2))*sin(3/4*(4*c^2*d*log(f)^2 - 9*e^2*f + 36
*d*f^2)/(c^2*log(f)^2 + 9*f^2))*erf(1/2*(2*(c*log(f) - 3*I*f)*x - 3*I*e)/s
qrt(-c*log(f) + 3*I*f)) + ((-I*c^2*f^(9/4*c*e^2/(c^2*log(f)^2 + 9*f^2))*f^a
*log(f)^2 - I*f^(9/4*c*e^2/(c^2*log(f)^2 + 9*f^2))*f^(a + 2))*cos(3/4*(4*c^
2*d*log(f)^2 - 9*e^2*f + 36*d*f^2)/(c^2*log(f)^2 + 9*f^2)) + (c^2*f^(9/4*c*
e^2/(c^2*log(f)^2 + 9*f^2))*f^a*log(f)^2 + f^(9/4*c*e^2/(c^2*log(f)^2 + 9*f
^2))*f^(a + 2))*sin(3/4*(4*c^2*d*log(f)^2 - 9*e^2*f + 36*d*f^2)/(c^2*log(f)
^2 + 9*f^2))*erf(1/2*(2*(c*log(f) + 3*I*f)*x + 3*I*e)/sqrt(-c*log(f) - 3*I
*f)))*sqrt(c*log(f) + sqrt(c^2*log(f)^2 + 9*f^2)) + sqrt(pi)*sqrt(2*c^2*log
(f)^2 + 2*f^2)*(((3*I*c^2*f^(1/4*c*e^2/(c^2*log(f)^2 + f^2))*f^a*log(f)^2 +
27*I*f^(1/4*c*e^2/(c^2*log(f)^2 + f^2))*f^(a + 2))*cos(1/4*(4*c^2*d*log(f)
^2 - e^2*f + 4*d*f^2)/(c^2*log(f)^2 + f^2)) + 3*(c^2*f^(1/4*c*e^2/(c^2*log(
f)^2 + f^2))*f^a*log(f)^2 + 9*f^(1/4*c*e^2/(c^2*log(f)^2 + f^2))*f^(a + 2))
*sin(1/4*(4*c^2*d*log(f)^2 - e^2*f + 4*d*f^2)/(c^2*log(f)^2 + f^2))*erf(1/
2*(2*(c*log(f) - I*f)*x - I*e)/sqrt(-c*log(f) + I*f)) + ((-3*I*c^2*f^(1/4*c
*e^2/(c^2*log(f)^2 + f^2))*f^a*log(f)^2 - 27*I*f^(1/4*c*e^2/(c^2*log(f)^2 +
f^2))*f^(a + 2))*cos(1/4*(4*c^2*d*log(f)^2 - e^2*f + 4*d*f^2)/(c^2*log(f)^
2 + f^2)) + 3*(c^2*f^(1/4*c*e^2/(c^2*log(f)^2 + f^2))*f^a*log(f)^2 + 9*f^(1
/4*c*e^2/(c^2*log(f)^2 + f^2))*f^(a + 2))*sin(1/4*(4*c^2*d*log(f)^2 - e^2*f
+ 4*d*f^2)/(c^2*log(f)^2 + f^2))*erf(1/2*(2*(c*log(f) + I*f)*x + I*e)/sqr
t(-c*log(f) - I*f))*sqrt(c*log(f) + sqrt(c^2*log(f)^2 + f^2)) - sqrt(pi)*s
qrt(2*c^2*log(f)^2 + 18*f^2)*(((c^2*f^(9/4*c*e^2/(c^2*log(f)^2 + 9*f^2))*f^
a*log(f)^2 + f^(9/4*c*e^2/(c^2*log(f)^2 + 9*f^2))*f^(a + 2))*cos(3/4*(4*c^2
*d*log(f)^2 - 9*e^2*f + 36*d*f^2)/(c^2*log(f)^2 + 9*f^2)) - (I*c^2*f^(9/4*c
*e^2/(c^2*log(f)^2 + 9*f^2))*f^a*log(f)^2 + I*f^(9/4*c*e^2/(c^2*log(f)^2 +
9*f^2))*f^(a + 2))*sin(3/4*(4*c^2*d*log(f)^2 - 9*e^2*f + 36*d*f^2)/(c^2*log
(f)^2 + 9*f^2))*erf(1/2*(2*(c*log(f) - 3*I*f)*x - 3*I*e)/sqrt(-c*log(f) +
3*I*f)) + ((c^2*f^(9/4*c*e^2/(c^2*log(f)^2 + 9*f^2))*f^a*log(f)^2 + f^(9/4*
c*e^2/(c^2*log(f)^2 + 9*f^2))*f^(a + 2))*cos(3/4*(4*c^2*d*log(f)^2 - 9*e^2*
f + 36*d*f^2)/(c^2*log(f)^2 + 9*f^2)) - (-I*c^2*f^(9/4*c*e^2/(c^2*log(f)^2
+ 9*f^2))*f^a*log(f)^2 - I*f^(9/4*c*e^2/(c^2*log(f)^2 + 9*f^2))*f^(a + 2))*
sin(3/4*(4*c^2*d*log(f)^2 - 9*e^2*f + 36*d*f^2)/(c^2*log(f)^2 + 9*f^2))*er
f(1/2*(2*(c*log(f) + 3*I*f)*x + 3*I*e)/sqrt(-c*log(f) - 3*I*f))*sqrt(-c*lo
g(f) + sqrt(c^2*log(f)^2 + 9*f^2)) - sqrt(pi)*sqrt(2*c^2*log(f)^2 + 2*f^2)*
(((3*(c^2*f^(1/4*c*e^2/(c^2*log(f)^2 + f^2))*f^a*log(f)^2 + 9*f^(1/4*c*e^2/(
c^2*log(f)^2 + f^2))*f^(a + 2))*cos(1/4*(4*c^2*d*log(f)^2 - e^2*f + 4*d*f^2
)/(c^2*log(f)^2 + f^2)) - (3*I*c^2*f^(1/4*c*e^2/(c^2*log(f)^2 + f^2))*f^a*l
og(f)^2 + 27*I*f^(1/4*c*e^2/(c^2*log(f)^2 + f^2))*f^(a + 2))*sin(1/4*(4*c^2
*d*log(f)^2 - e^2*f + 4*d*f^2)/(c^2*log(f)^2 + f^2))*erf(1/2*(2*(c*log(f)
- I*f)*x - I*e)/sqrt(-c*log(f) + I*f)) + (3*(c^2*f^(1/4*c*e^2/(c^2*log(f)^2
+ f^2))*f^a*log(f)^2 + 9*f^(1/4*c*e^2/(c^2*log(f)^2 + f^2))*f^(a + 2))*cos
(1/4*(4*c^2*d*log(f)^2 - e^2*f + 4*d*f^2)/(c^2*log(f)^2 + f^2)) - (-3*I*c^2
*f^(1/4*c*e^2/(c^2*log(f)^2 + f^2))*f^a*log(f)^2 - 27*I*f^(1/4*c*e^2/(c^2*l
og(f)^2 + f^2))*f^(a + 2))*sin(1/4*(4*c^2*d*log(f)^2 - e^2*f + 4*d*f^2)/(c^
2*log(f)^2 + f^2))*erf(1/2*(2*(c*log(f) + I*f)*x + I*e)/sqrt(-c*log(f) - I
*f))*sqrt(-c*log(f) + sqrt(c^2*log(f)^2 + f^2)))/(c^4*log(f)^4 + 10*c^2*f^
2*log(f)^2 + 9*f^4)

```

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int f^{cx^2+a} \cos(fx^2 + ex + d)^3 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(f^(a + c*x^2)*cos(d + e*x + f*x^2)^3,x)

[Out] int(f^(a + c*x^2)*cos(d + e*x + f*x^2)^3, x)

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f**(c*x**2+a)*cos(f*x**2+e*x+d)**3,x)

[Out] Timed out

3.125 $\int f^{a+bx+cx^2} \cos(d + ex) dx$

Optimal. Leaf size=172

$$\frac{\sqrt{\pi} f^a e^{\frac{(e-ib \log(f))^2}{4c \log(f)} + id} \operatorname{erfi}\left(\frac{b \log(f) + 2cx \log(f) + ie}{2\sqrt{c} \sqrt{\log(f)}}\right)}{4\sqrt{c} \sqrt{\log(f)}} - \frac{\sqrt{\pi} f^a e^{\frac{(e+ib \log(f))^2}{4c \log(f)} - id} \operatorname{erfi}\left(\frac{-b \log(f) - 2cx \log(f) + ie}{2\sqrt{c} \sqrt{\log(f)}}\right)}{4\sqrt{c} \sqrt{\log(f)}}$$

[Out] $\frac{1}{4} \exp(-I*d + 1/4*(e + I*b*\ln(f))^2/c/\ln(f)) * f^a * \operatorname{erfi}(1/2*(-I*e + b*\ln(f) + 2*c*x*\ln(f))/c^{(1/2)}/\ln(f)^{(1/2)}) * \pi^{(1/2)}/c^{(1/2)}/\ln(f)^{(1/2)} + 1/4 * \exp(I*d + 1/4*(e - I*b*\ln(f))^2/c/\ln(f)) * f^a * \operatorname{erfi}(1/2*(I*e + b*\ln(f) + 2*c*x*\ln(f))/c^{(1/2)}/\ln(f)^{(1/2)}) * \pi^{(1/2)}/c^{(1/2)}/\ln(f)^{(1/2)}$

Rubi [A] time = 0.26, antiderivative size = 172, normalized size of antiderivative = 1.00, number of steps used = 8, number of rules used = 4, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.210$, Rules used = {4473, 2287, 2234, 2204}

$$\frac{\sqrt{\pi} f^a e^{\frac{(e-ib \log(f))^2}{4c \log(f)} + id} \operatorname{Erfi}\left(\frac{b \log(f) + 2cx \log(f) + ie}{2\sqrt{c} \sqrt{\log(f)}}\right)}{4\sqrt{c} \sqrt{\log(f)}} - \frac{\sqrt{\pi} f^a e^{\frac{(e+ib \log(f))^2}{4c \log(f)} - id} \operatorname{Erfi}\left(\frac{-b \log(f) - 2cx \log(f) + ie}{2\sqrt{c} \sqrt{\log(f)}}\right)}{4\sqrt{c} \sqrt{\log(f)}}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[f^{(a + b*x + c*x^2)} * \operatorname{Cos}[d + e*x], x]$

[Out] $-(E^{((-I)*d + (e + I*b*\operatorname{Log}[f])^2/(4*c*\operatorname{Log}[f]))} * f^a * \operatorname{Sqrt}[\pi] * \operatorname{Erfi}[(I*e - b*\operatorname{Log}[f] - 2*c*x*\operatorname{Log}[f])/(2*\operatorname{Sqrt}[c]*\operatorname{Sqrt}[\operatorname{Log}[f]])]) / (4*\operatorname{Sqrt}[c]*\operatorname{Sqrt}[\operatorname{Log}[f]]) + (E^{(I*d + (e - I*b*\operatorname{Log}[f])^2/(4*c*\operatorname{Log}[f]))} * f^a * \operatorname{Sqrt}[\pi] * \operatorname{Erfi}[(I*e + b*\operatorname{Log}[f] + 2*c*x*\operatorname{Log}[f])/(2*\operatorname{Sqrt}[c]*\operatorname{Sqrt}[\operatorname{Log}[f]])]) / (4*\operatorname{Sqrt}[c]*\operatorname{Sqrt}[\operatorname{Log}[f]])$

Rule 2204

$\operatorname{Int}[(F_)^{((a_.) + (b_.)*((c_.) + (d_.)*(x_)^2))}, x_Symbol] := \operatorname{Simp}[(F^a * \operatorname{Sqrt}[\pi] * \operatorname{Erfi}[(c + d*x)*\operatorname{Rt}[b*\operatorname{Log}[F], 2]]) / (2*d*\operatorname{Rt}[b*\operatorname{Log}[F], 2]), x] /; \operatorname{FreeQ}\{F, a, b, c, d\}, x] \ \&\& \operatorname{PosQ}[b]$

Rule 2234

$\operatorname{Int}[(F_)^{((a_.) + (b_.)*(x_) + (c_.)*(x_)^2))}, x_Symbol] := \operatorname{Dist}[F^{(a - b^2/(4*c))}, \operatorname{Int}[F^{((b + 2*c*x)^2/(4*c))}, x], x] /; \operatorname{FreeQ}\{F, a, b, c\}, x]$

Rule 2287

$\operatorname{Int}[(u_)*(F_)^{(v_)*(G_)^{(w_)}}, x_Symbol] := \operatorname{With}\{z = v*\operatorname{Log}[F] + w*\operatorname{Log}[G]\}, \operatorname{Int}[u*\operatorname{NormalizeIntegrand}[E^z, x], x] /; \operatorname{BinomialQ}[z, x] \ || \ (\operatorname{PolynomialQ}[z, x] \ \&\& \operatorname{LeQ}[\operatorname{Exponent}[z, x], 2]) /; \operatorname{FreeQ}\{F, G\}, x]$

Rule 4473

$\operatorname{Int}[\operatorname{Cos}[v_]^{(n_.)}*(F_)^{(u_)}, x_Symbol] := \operatorname{Int}[\operatorname{ExpandTrigToExp}[F^u, \operatorname{Cos}[v]^n], x] /; \operatorname{FreeQ}[F, x] \ \&\& \ (\operatorname{LinearQ}[u, x] \ || \ \operatorname{PolyQ}[u, x, 2]) \ \&\& \ (\operatorname{LinearQ}[v, x] \ || \ \operatorname{PolyQ}[v, x, 2]) \ \&\& \operatorname{IGtQ}[n, 0]$

Rubi steps

$$\begin{aligned}
\int f^{a+bx+cx^2} \cos(d+ex) dx &= \int \left(\frac{1}{2} e^{-id-iex} f^{a+bx+cx^2} + \frac{1}{2} e^{id+iex} f^{a+bx+cx^2} \right) dx \\
&= \frac{1}{2} \int e^{-id-iex} f^{a+bx+cx^2} dx + \frac{1}{2} \int e^{id+iex} f^{a+bx+cx^2} dx \\
&= \frac{1}{2} \int \exp(-id + a \log(f) + cx^2 \log(f) - x(ie - b \log(f))) dx + \frac{1}{2} \int \exp(id + a \log(f) + cx^2 \log(f) + x(ie - b \log(f))) dx \\
&= \frac{1}{2} \left(e^{id + \frac{(e-ib \log(f))^2}{4c \log(f)}} f^a \right) \int \exp\left(\frac{(ie + b \log(f) + 2cx \log(f))^2}{4c \log(f)}\right) dx + \frac{1}{2} \left(e^{-id + \frac{(e+ib \log(f))^2}{4c \log(f)}} f^a \right) \int \exp\left(\frac{(ie - b \log(f) + 2cx \log(f))^2}{4c \log(f)}\right) dx \\
&= -\frac{e^{-id + \frac{(e+ib \log(f))^2}{4c \log(f)}} f^a \sqrt{\pi} \operatorname{erfi}\left(\frac{ie - b \log(f) - 2cx \log(f)}{2\sqrt{c} \sqrt{\log(f)}}\right)}{4\sqrt{c} \sqrt{\log(f)}} + \frac{e^{id + \frac{(e-ib \log(f))^2}{4c \log(f)}} f^a \sqrt{\pi} \operatorname{erfi}\left(\frac{ie + b \log(f) + 2cx \log(f)}{2\sqrt{c} \sqrt{\log(f)}}\right)}{4\sqrt{c} \sqrt{\log(f)}}
\end{aligned}$$

Mathematica [A] time = 0.33, size = 151, normalized size = 0.88

$$\frac{\sqrt{\pi} f^{a-\frac{b^2}{4c}} e^{\frac{e(2ib \log(f))}{4c \log(f)}} \left(e^{\frac{ibe}{c}} (\cos(d) - i \sin(d)) \operatorname{erfi}\left(\frac{\log(f)(b+2cx)-ie}{2\sqrt{c} \sqrt{\log(f)}}\right) + (\cos(d) + i \sin(d)) \operatorname{erfi}\left(\frac{\log(f)(b+2cx)+ie}{2\sqrt{c} \sqrt{\log(f)}}\right) \right)}{4\sqrt{c} \sqrt{\log(f)}}$$

Antiderivative was successfully verified.

[In] Integrate[f^(a + b*x + c*x^2)*Cos[d + e*x], x]

[Out] (E^((e*(e - (2*I)*b*Log[f]))/(4*c*Log[f])))*f^(a - b^2/(4*c))*Sqrt[Pi]*(E^((I*b*e)/c)*Erfi[((-I)*e + (b + 2*c*x)*Log[f])/(2*Sqrt[c]*Sqrt[Log[f]])]*(Cos[d] - I*Sin[d]) + Erfi[(I*e + (b + 2*c*x)*Log[f])/(2*Sqrt[c]*Sqrt[Log[f]])]*(Cos[d] + I*Sin[d]))/(4*Sqrt[c]*Sqrt[Log[f]])

fricas [A] time = 0.72, size = 176, normalized size = 1.02

$$\frac{\sqrt{\pi} \sqrt{-c \log(f)} \operatorname{erf}\left(\frac{((2cx+b) \log(f)+ie) \sqrt{-c \log(f)}}{2c \log(f)}\right) e^{\left(-\frac{(b^2-4ac) \log(f)^2 - e^2 - (4icd-2ibe) \log(f)}{4c \log(f)}\right)} + \sqrt{\pi} \sqrt{-c \log(f)} \operatorname{erf}\left(\frac{((2cx+b) \log(f)-ie) \sqrt{-c \log(f)}}{2c \log(f)}\right) e^{\left(-\frac{(b^2-4ac) \log(f)^2 - e^2 - (4icd-2ibe) \log(f)}{4c \log(f)}\right)}}{4c \log(f)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(c*x^2+b*x+a)*cos(e*x+d), x, algorithm="fricas")

[Out] -1/4*(sqrt(pi)*sqrt(-c*log(f))*erf(1/2*((2*c*x + b)*log(f) + I*e)*sqrt(-c*log(f))/(c*log(f)))*e^(-1/4*((b^2 - 4*a*c)*log(f)^2 - e^2 - (4*I*c*d - 2*I*b*e)*log(f))/(c*log(f))) + sqrt(pi)*sqrt(-c*log(f))*erf(1/2*((2*c*x + b)*log(f) - I*e)*sqrt(-c*log(f))/(c*log(f)))*e^(-1/4*((b^2 - 4*a*c)*log(f)^2 - e^2 - (-4*I*c*d + 2*I*b*e)*log(f))/(c*log(f)))/(c*log(f))

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int f^{cx^2+bx+a} \cos(ex+d) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(c*x^2+b*x+a)*cos(e*x+d), x, algorithm="giac")

[Out] integrate(f^(c*x^2 + b*x + a)*cos(e*x + d), x)

maple [A] time = 0.17, size = 168, normalized size = 0.98

$$\frac{\sqrt{\pi} f^a e^{-\frac{-e^2-2i \ln(f)be+4id \ln(f)c+\ln(f)^2b^2}{4 \ln(f)c}} \operatorname{erf}\left(-\sqrt{-c \ln(f)} x + \frac{-ie+b \ln(f)}{2\sqrt{-c \ln(f)}}\right) + \sqrt{\pi} f^a e^{-\frac{-e^2+2i \ln(f)be-4id \ln(f)c+\ln(f)^2b^2}{4 \ln(f)c}} \operatorname{erf}\left(-\sqrt{-c \ln(f)} x + \frac{ie-b \ln(f)}{2\sqrt{-c \ln(f)}}\right)}{4\sqrt{-c \ln(f)}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(f^(c*x^2+b*x+a)*cos(e*x+d), x)`

[Out]
$$-1/4*\text{Pi}^{(1/2)}*f^a*\exp(-1/4*(-e^2-2*I*\ln(f)*b*e+4*I*d*\ln(f)*c+\ln(f)^2*b^2)/\ln(f)/c)/(-c*\ln(f))^{(1/2)}*\text{erf}(-(-c*\ln(f))^{(1/2)}*x+1/2*(-I*e+b*\ln(f)))/(-c*\ln(f))^{(1/2)}-1/4*\text{Pi}^{(1/2)}*f^a*\exp(-1/4*(-e^2+2*I*\ln(f)*b*e-4*I*d*\ln(f)*c+\ln(f)^2*b^2)/\ln(f)/c)/(-c*\ln(f))^{(1/2)}*\text{erf}(-(-c*\ln(f))^{(1/2)}*x+1/2*(I*e+b*\ln(f)))/(-c*\ln(f))^{(1/2)}$$

maxima [C] time = 0.38, size = 354, normalized size = 2.06

$$\sqrt{\pi} \left(f^a \left(\cos\left(-\frac{2cd-be}{2c}\right) - i \sin\left(-\frac{2cd-be}{2c}\right) \right) \text{erf}\left(x\sqrt{-c\log(f)} - \frac{1}{2}(b\log(f) + ie)\frac{1}{\sqrt{-c\log(f)}}\right) e^{\left(\frac{e^2}{4c\log(f)}\right)} + f^a \left(\cos\right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(f^(c*x^2+b*x+a)*cos(e*x+d), x, algorithm="maxima")`

[Out]
$$-1/8*\text{sqrt}(\text{pi})*(f^a*(\cos(-1/2*(2*c*d - b*e)/c) - I*\sin(-1/2*(2*c*d - b*e)/c))*\text{erf}(x*\text{conjugate}(\text{sqrt}(-c*\log(f)))) - 1/2*(b*\log(f) + I*e)*\text{conjugate}(1/\text{sqrt}(-c*\log(f)))*e^{(1/4*e^2/(c*\log(f)))} + f^a*(\cos(-1/2*(2*c*d - b*e)/c) + I*\sin(-1/2*(2*c*d - b*e)/c))*\text{erf}(x*\text{conjugate}(\text{sqrt}(-c*\log(f)))) - 1/2*(b*\log(f) - I*e)*\text{conjugate}(1/\text{sqrt}(-c*\log(f)))*e^{(1/4*e^2/(c*\log(f)))} + f^a*(\cos(-1/2*(2*c*d - b*e)/c) - I*\sin(-1/2*(2*c*d - b*e)/c))*\text{erf}(1/2*(2*c*x*\log(f) + b*\log(f) + I*e)*\text{sqrt}(-c*\log(f))/(c*\log(f)))*e^{(1/4*e^2/(c*\log(f)))} + f^a*(\cos(-1/2*(2*c*d - b*e)/c) + I*\sin(-1/2*(2*c*d - b*e)/c))*\text{erf}(1/2*(2*c*x*\log(f) + b*\log(f) - I*e)*\text{sqrt}(-c*\log(f))/(c*\log(f)))*e^{(1/4*e^2/(c*\log(f)))})*\text{sqrt}(-c*\log(f))/(c*f^{(1/4*b^2/c)*\log(f)})$$

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int f^{cx^2+bx+a} \cos(d+ex) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(f^(a + b*x + c*x^2)*cos(d + e*x), x)`

[Out] `int(f^(a + b*x + c*x^2)*cos(d + e*x), x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int f^{a+bx+cx^2} \cos(d+ex) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(f**(c*x**2+b*x+a)*cos(e*x+d), x)`

[Out] `Integral(f**(a + b*x + c*x**2)*cos(d + e*x), x)`

3.126 $\int f^{a+bx+cx^2} \cos^2(d+ex) dx$

Optimal. Leaf size=231

$$\frac{\sqrt{\pi} f^{a-\frac{b^2}{4c}} \operatorname{erfi}\left(\frac{\sqrt{\log(f)}(b+2cx)}{2\sqrt{c}}\right)}{4\sqrt{c}\sqrt{\log(f)}} - \frac{\sqrt{\pi} f^a e^{\frac{(2e+ib\log(f))^2}{4c\log(f)}-2id} \operatorname{erfi}\left(\frac{-b\log(f)-2cx\log(f)+2ie}{2\sqrt{c}\sqrt{\log(f)}}\right)}{8\sqrt{c}\sqrt{\log(f)}} + \frac{\sqrt{\pi} f^a e^{2id-\frac{(b\log(f)+2ie)^2}{4c\log(f)}} \operatorname{erfi}\left(\frac{b\log(f)+2ie}{2\sqrt{c}\sqrt{\log(f)}}\right)}{8\sqrt{c}\sqrt{\log(f)}}$$

[Out] $1/8*\exp(-2*I*d+1/4*(2*e+I*b*\ln(f))^2/c/\ln(f))*f^a*\operatorname{erfi}(1/2*(-2*I*e+b*\ln(f)+2*c*x*\ln(f))/c^{(1/2)}/\ln(f)^{(1/2)})*\operatorname{Pi}^{(1/2)}/c^{(1/2)}/\ln(f)^{(1/2)}+1/8*\exp(2*I*d-1/4*(2*I*e+b*\ln(f))^2/c/\ln(f))*f^a*\operatorname{erfi}(1/2*(2*I*e+b*\ln(f)+2*c*x*\ln(f))/c^{(1/2)}/\ln(f)^{(1/2)})*\operatorname{Pi}^{(1/2)}/c^{(1/2)}/\ln(f)^{(1/2)}+1/4*f^{(a-1/4*b^2/c)}*\operatorname{erfi}(1/2*(2*c*x+b)*\ln(f)^{(1/2)}/c^{(1/2)})*\operatorname{Pi}^{(1/2)}/c^{(1/2)}/\ln(f)^{(1/2)}$

Rubi [A] time = 0.28, antiderivative size = 231, normalized size of antiderivative = 1.00, number of steps used = 10, number of rules used = 4, integrand size = 21, $\frac{\text{number of rules}}{\text{integrand size}} = 0.190$, Rules used = {4473, 2234, 2204, 2287}

$$\frac{\sqrt{\pi} f^{a-\frac{b^2}{4c}} \operatorname{Erfi}\left(\frac{\sqrt{\log(f)}(b+2cx)}{2\sqrt{c}}\right)}{4\sqrt{c}\sqrt{\log(f)}} - \frac{\sqrt{\pi} f^a e^{\frac{(2e+ib\log(f))^2}{4c\log(f)}-2id} \operatorname{Erfi}\left(\frac{-b\log(f)-2cx\log(f)+2ie}{2\sqrt{c}\sqrt{\log(f)}}\right)}{8\sqrt{c}\sqrt{\log(f)}} + \frac{\sqrt{\pi} f^a e^{2id-\frac{(b\log(f)+2ie)^2}{4c\log(f)}} \operatorname{Erfi}\left(\frac{b\log(f)+2ie}{2\sqrt{c}\sqrt{\log(f)}}\right)}{8\sqrt{c}\sqrt{\log(f)}}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[f^{(a+b*x+c*x^2)}*\operatorname{Cos}[d+e*x]^2, x]$

[Out] $(f^{(a-b^2/(4*c))*\operatorname{Sqrt}[\operatorname{Pi}]*\operatorname{Erfi}[(b+2*c*x)*\operatorname{Sqrt}[\operatorname{Log}[f]]/(2*\operatorname{Sqrt}[c])])/(4*\operatorname{Sqrt}[c]*\operatorname{Sqrt}[\operatorname{Log}[f]]) - (E^{((-2*I)*d+(2*e+I*b*\operatorname{Log}[f])^2/(4*c*\operatorname{Log}[f]))}*f^a*\operatorname{Sqrt}[\operatorname{Pi}]*\operatorname{Erfi}[(2*I)*e-b*\operatorname{Log}[f]-2*c*x*\operatorname{Log}[f]]/(2*\operatorname{Sqrt}[c]*\operatorname{Sqrt}[\operatorname{Log}[f]])])/(8*\operatorname{Sqrt}[c]*\operatorname{Sqrt}[\operatorname{Log}[f]]) + (E^{((2*I)*d-((2*I)*e+b*\operatorname{Log}[f])^2/(4*c*\operatorname{Log}[f]))}*f^a*\operatorname{Sqrt}[\operatorname{Pi}]*\operatorname{Erfi}[(2*I)*e+b*\operatorname{Log}[f]+2*c*x*\operatorname{Log}[f]]/(2*\operatorname{Sqrt}[c]*\operatorname{Sqrt}[\operatorname{Log}[f]])])/(8*\operatorname{Sqrt}[c]*\operatorname{Sqrt}[\operatorname{Log}[f]])$

Rule 2204

$\operatorname{Int}[(F_)^{((a_.)+(b_.)*((c_.)+(d_.)*(x_))^2)}, x_Symbol] \rightarrow \operatorname{Simp}[(F^a*\operatorname{Sqrt}[\operatorname{Pi}]*\operatorname{Erfi}[(c+d*x)*\operatorname{Rt}[b*\operatorname{Log}[F], 2]])/(2*d*\operatorname{Rt}[b*\operatorname{Log}[F], 2]), x] /; \operatorname{FreeQ}\{F, a, b, c, d\}, x] \&\& \operatorname{PosQ}[b]$

Rule 2234

$\operatorname{Int}[(F_)^{((a_.)+(b_.)*(x_)+(c_.)*(x_)^2)}, x_Symbol] \rightarrow \operatorname{Dist}[F^{(a-b^2/(4*c))}, \operatorname{Int}[F^{((b+2*c*x)^2/(4*c))}, x], x] /; \operatorname{FreeQ}\{F, a, b, c\}, x]$

Rule 2287

$\operatorname{Int}[(u_)*(F_)^{(v_)*(G_)^{(w_)}}, x_Symbol] \rightarrow \operatorname{With}\{z = v*\operatorname{Log}[F] + w*\operatorname{Log}[G]\}, \operatorname{Int}[u*\operatorname{NormalizeIntegrand}[E^z, x], x] /; \operatorname{BinomialQ}[z, x] \|\| (\operatorname{PolynomialQ}[z, x] \&\& \operatorname{LeQ}[\operatorname{Exponent}[z, x], 2]) /; \operatorname{FreeQ}\{F, G\}, x]$

Rule 4473

$\operatorname{Int}[\operatorname{Cos}[v_]^{(n_.)*(F_)^{(u_)}}, x_Symbol] \rightarrow \operatorname{Int}[\operatorname{ExpandTrigToExp}[F^u, \operatorname{Cos}[v]^{(n)}, x], x] /; \operatorname{FreeQ}[F, x] \&\& (\operatorname{LinearQ}[u, x] \|\| \operatorname{PolyQ}[u, x, 2]) \&\& (\operatorname{LinearQ}[v, x] \|\| \operatorname{PolyQ}[v, x, 2]) \&\& \operatorname{IGtQ}[n, 0]$

Rubi steps

$$\begin{aligned}
\int f^{a+bx+cx^2} \cos^2(d+ex) dx &= \int \left(\frac{1}{2} f^{a+bx+cx^2} + \frac{1}{4} e^{-2id-2iex} f^{a+bx+cx^2} + \frac{1}{4} e^{2id+2iex} f^{a+bx+cx^2} \right) dx \\
&= \frac{1}{4} \int e^{-2id-2iex} f^{a+bx+cx^2} dx + \frac{1}{4} \int e^{2id+2iex} f^{a+bx+cx^2} dx + \frac{1}{2} \int f^{a+bx+cx^2} dx \\
&= \frac{1}{4} \int \exp(-2id + a \log(f) + cx^2 \log(f) - x(2ie - b \log(f))) dx + \frac{1}{4} \int \exp(2id + a \log(f) + cx^2 \log(f) + x(2ie - b \log(f))) dx \\
&= \frac{f^{a-\frac{b^2}{4c}} \sqrt{\pi} \operatorname{erfi}\left(\frac{(b+2cx)\sqrt{\log(f)}}{2\sqrt{c}}\right)}{4\sqrt{c}\sqrt{\log(f)}} + \frac{1}{4} \left(\exp\left(-2id + \frac{(2e+ib\log(f))^2}{4c\log(f)}\right) f^a \right) \int \exp\left(-2id + a \log(f) + cx^2 \log(f) - x(2ie - b \log(f))\right) dx \\
&= \frac{f^{a-\frac{b^2}{4c}} \sqrt{\pi} \operatorname{erfi}\left(\frac{(b+2cx)\sqrt{\log(f)}}{2\sqrt{c}}\right)}{4\sqrt{c}\sqrt{\log(f)}} - \frac{\exp\left(-2id + \frac{(2e+ib\log(f))^2}{4c\log(f)}\right) f^a \sqrt{\pi} \operatorname{erfi}\left(\frac{2ie-b\log(f)}{2\sqrt{c}\sqrt{\log(f)}}\right)}{8\sqrt{c}\sqrt{\log(f)}}
\end{aligned}$$

Mathematica [A] time = 0.61, size = 204, normalized size = 0.88

$$\frac{\sqrt{\pi} e^{-\frac{ibe}{c}} f^{a-\frac{b^2}{4c}} \left((\cos(2d) + i \sin(2d)) e^{\frac{e^2}{c \log(f)}} \operatorname{erfi}\left(\frac{\log(f)(b+2cx)+2ie}{2\sqrt{c}\sqrt{\log(f)}}\right) + (\cos(2d) - i \sin(2d)) e^{\frac{e(e+2ib\log(f))}{c \log(f)}} \operatorname{erfi}\left(\frac{\log(f)(b+2cx)+2ie}{2\sqrt{c}\sqrt{\log(f)}}\right) \right)}{8\sqrt{c}\sqrt{\log(f)}}$$

Antiderivative was successfully verified.

[In] Integrate[f^(a + b*x + c*x^2)*Cos[d + e*x]^2,x]

[Out] (f^(a - b^2/(4*c))*Sqrt[Pi]*(2*E^((I*b*e)/c)*Erfi[((b + 2*c*x)*Sqrt[Log[f]])/(2*Sqrt[c])]) + E^((e*(e + (2*I)*b*Log[f]))/(c*Log[f]))*Erfi[((-2*I)*e + (b + 2*c*x)*Log[f])/(2*Sqrt[c]*Sqrt[Log[f]])])*(Cos[2*d] - I*Sin[2*d]) + E^(e^2/(c*Log[f]))*Erfi[((2*I)*e + (b + 2*c*x)*Log[f])/(2*Sqrt[c]*Sqrt[Log[f]])])*(Cos[2*d] + I*Sin[2*d]))/(8*Sqrt[c]*E^((I*b*e)/c)*Sqrt[Log[f]])

fricas [A] time = 0.78, size = 224, normalized size = 0.97

$$\frac{\sqrt{\pi} \sqrt{-c \log(f)} \operatorname{erf}\left(\frac{((2cx+b)\log(f)+2ie)\sqrt{-c \log(f)}}{2c \log(f)}\right) e^{\left(-\frac{(b^2-4ac)\log(f)^2-4e^2-(8icd-4ibe)\log(f)}{4c \log(f)}\right)} + \sqrt{\pi} \sqrt{-c \log(f)} \operatorname{erf}\left(\frac{((2cx+b)\log(f)+2ie)\sqrt{-c \log(f)}}{2c \log(f)}\right)}{8c \log(f)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(c*x^2+b*x+a)*cos(e*x+d)^2,x, algorithm="fricas")

[Out] -1/8*(sqrt(pi)*sqrt(-c*log(f))*erf(1/2*((2*c*x + b)*log(f) + 2*I*e)*sqrt(-c*log(f))/(c*log(f)))*e^(-1/4*((b^2 - 4*a*c)*log(f)^2 - 4*e^2 - (8*I*c*d - 4*I*b*e)*log(f))/(c*log(f))) + sqrt(pi)*sqrt(-c*log(f))*erf(1/2*((2*c*x + b)*log(f) - 2*I*e)*sqrt(-c*log(f))/(c*log(f)))*e^(-1/4*((b^2 - 4*a*c)*log(f)^2 - 4*e^2 - (-8*I*c*d + 4*I*b*e)*log(f))/(c*log(f))) + 2*sqrt(pi)*sqrt(-c*log(f))*erf(1/2*(2*c*x + b)*sqrt(-c*log(f))/c)/f^(1/4*(b^2 - 4*a*c)/c))/(c*log(f))

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int f^{cx^2+bx+a} \cos(ex+d)^2 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(c*x^2+b*x+a)*cos(e*x+d)^2,x, algorithm="giac")

[Out] integrate(f^(c*x^2 + b*x + a)*cos(e*x + d)^2, x)

maple [A] time = 0.26, size = 217, normalized size = 0.94

$$\frac{\sqrt{\pi} f^a e^{-\frac{\ln(f)^2 b^2 - 4i \ln(f) b e + 8id \ln(f) c - 4e^2}{4 \ln(f) c}} \operatorname{erf}\left(-\sqrt{-c \ln(f)} x + \frac{b \ln(f) - 2ie}{2\sqrt{-c \ln(f)}}\right)}{8\sqrt{-c \ln(f)}} - \frac{\sqrt{\pi} f^a e^{-\frac{\ln(f)^2 b^2 + 4i \ln(f) b e - 8id \ln(f) c - 4e^2}{4 \ln(f) c}} \operatorname{erf}\left(-\sqrt{-c \ln(f)} x + \frac{b \ln(f) - 2ie}{2\sqrt{-c \ln(f)}}\right)}{8\sqrt{-c \ln(f)}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(f^(c*x^2+b*x+a)*cos(e*x+d)^2,x)

[Out] $-1/8*\pi^{(1/2)}*f^a*\exp(-1/4*(\ln(f)^2*b^2-4*I*\ln(f)*b*e+8*I*d*\ln(f)*c-4*e^2)/\ln(f)/c)/(-c*\ln(f))^{(1/2)}*\operatorname{erf}(-(-c*\ln(f))^{(1/2)}*x+1/2*(b*\ln(f)-2*I*e)/(-c*\ln(f))^{(1/2)})-1/8*\pi^{(1/2)}*f^a*\exp(-1/4*(\ln(f)^2*b^2+4*I*\ln(f)*b*e-8*I*d*\ln(f)*c-4*e^2)/\ln(f)/c)/(-c*\ln(f))^{(1/2)}*\operatorname{erf}(-(-c*\ln(f))^{(1/2)}*x+1/2*(2*I*e+b*\ln(f))/(-c*\ln(f))^{(1/2)})-1/4*\pi^{(1/2)}*f^a*f^{(-1/4*b^2/c)/(-c*\ln(f))^{(1/2)}}*\operatorname{erf}(-(-c*\ln(f))^{(1/2)}*x+1/2/(-c*\ln(f))^{(1/2)}*b*\ln(f))$

maxima [C] time = 0.38, size = 399, normalized size = 1.73

$$\sqrt{\pi} \left(f^a \left(\cos\left(-\frac{2cd-be}{c}\right) - i \sin\left(-\frac{2cd-be}{c}\right) \right) \operatorname{erf}\left(x\sqrt{-c \log(f)} - \frac{1}{2} (b \log(f) + 2ie) \frac{1}{\sqrt{-c \log(f)}}\right) e^{\left(\frac{e^2}{c \log(f)}\right)} + f^a \left(\cos\left(-\frac{2cd-be}{c}\right) + i \sin\left(-\frac{2cd-be}{c}\right) \right) \operatorname{erf}\left(x\sqrt{-c \log(f)} + \frac{1}{2} (b \log(f) - 2ie) \frac{1}{\sqrt{-c \log(f)}}\right) e^{\left(\frac{e^2}{c \log(f)}\right)} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(c*x^2+b*x+a)*cos(e*x+d)^2,x, algorithm="maxima")

[Out] $1/16*\sqrt{\pi}*(f^a*(\cos(-(2*c*d - b*e)/c) - I*\sin(-(2*c*d - b*e)/c))*\operatorname{erf}(x*\operatorname{conjugate}(\sqrt{-c*\log(f)}) - 1/2*(b*\log(f) + 2*I*e)*\operatorname{conjugate}(1/\sqrt{-c*\log(f)})) + f^a*(\cos(-(2*c*d - b*e)/c) + I*\sin(-(2*c*d - b*e)/c))*\operatorname{erf}(x*\operatorname{conjugate}(\sqrt{-c*\log(f)}) - 1/2*(b*\log(f) - 2*I*e)*\operatorname{conjugate}(1/\sqrt{-c*\log(f)})) + f^a*(\cos(-(2*c*d - b*e)/c) - I*\sin(-(2*c*d - b*e)/c))*\operatorname{erf}(1/2*(2*c*x*\log(f) + b*\log(f) + 2*I*e)*\sqrt{-c*\log(f)})/(c*\log(f)) + f^a*(\cos(-(2*c*d - b*e)/c) + I*\sin(-(2*c*d - b*e)/c))*\operatorname{erf}(1/2*(2*c*x*\log(f) + b*\log(f) - 2*I*e)*\sqrt{-c*\log(f)})/(c*\log(f)) + 2*f^a*\operatorname{erf}(-1/2*b*\operatorname{conjugate}(1/\sqrt{-c*\log(f)})*\log(f) + x*\operatorname{conjugate}(\sqrt{-c*\log(f)})) - 2*f^a*\operatorname{erf}(1/2*(2*c*x*\log(f) + b*\log(f))/\sqrt{-c*\log(f)})/(\sqrt{-c*\log(f)})*f^{(1/4*b^2/c)})$

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int f^{cx^2+bx+a} \cos(d+ex)^2 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(f^(a + b*x + c*x^2)*cos(d + e*x)^2,x)

[Out] int(f^(a + b*x + c*x^2)*cos(d + e*x)^2, x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int f^{a+bx+cx^2} \cos^2(d+ex) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f**(c*x**2+b*x+a)*cos(e*x+d)**2,x)

[Out] Integral(f**(a + b*x + c*x**2)*cos(d + e*x)**2, x)

3.127 $\int f^{a+bx+cx^2} \cos^3(d+ex) dx$

Optimal. Leaf size=346

$$\frac{3\sqrt{\pi} f^a e^{\frac{(e+ib \log(f))^2}{4c \log(f)} - id} \operatorname{erfi}\left(\frac{-b \log(f) - 2cx \log(f) + ie}{2\sqrt{c} \sqrt{\log(f)}}\right)}{16\sqrt{c} \sqrt{\log(f)}} - \frac{\sqrt{\pi} f^a e^{\frac{(3e+ib \log(f))^2}{4c \log(f)} - 3id} \operatorname{erfi}\left(\frac{-b \log(f) - 2cx \log(f) + 3ie}{2\sqrt{c} \sqrt{\log(f)}}\right)}{16\sqrt{c} \sqrt{\log(f)}} + \frac{3\sqrt{\pi} f^a e^{\frac{(e-ib \log(f))^2}{4c \log(f)} - id} \operatorname{erfi}\left(\frac{-b \log(f) - 2cx \log(f) + ie}{2\sqrt{c} \sqrt{\log(f)}}\right)}{16\sqrt{c} \sqrt{\log(f)}} - \frac{\sqrt{\pi} f^a e^{\frac{(3e-ib \log(f))^2}{4c \log(f)} - 3id} \operatorname{erfi}\left(\frac{-b \log(f) - 2cx \log(f) + 3ie}{2\sqrt{c} \sqrt{\log(f)}}\right)}{16\sqrt{c} \sqrt{\log(f)}} + \dots$$

[Out] $3/16 \exp(-I*d + 1/4*(e + I*b*\ln(f))^2/c/\ln(f)) * f^a * \operatorname{erfi}(1/2*(-I*e + b*\ln(f) + 2*c*x*\ln(f))/c^{(1/2)}/\ln(f)^{(1/2)}) * \Pi^{(1/2)}/c^{(1/2)}/\ln(f)^{(1/2)} + 1/16 \exp(-3*I*d + 1/4*(3e + I*b*\ln(f))^2/c/\ln(f)) * f^a * \operatorname{erfi}(1/2*(-3*I*e + b*\ln(f) + 2*c*x*\ln(f))/c^{(1/2)}/\ln(f)^{(1/2)}) * \Pi^{(1/2)}/c^{(1/2)}/\ln(f)^{(1/2)} + 3/16 \exp(I*d + 1/4*(e - I*b*\ln(f))^2/c/\ln(f)) * f^a * \operatorname{erfi}(1/2*(I*e + b*\ln(f) + 2*c*x*\ln(f))/c^{(1/2)}/\ln(f)^{(1/2)}) * \Pi^{(1/2)}/c^{(1/2)}/\ln(f)^{(1/2)} + 1/16 \exp(3*I*d - 1/4*(3e - I*b*\ln(f))^2/c/\ln(f)) * f^a * \operatorname{erfi}(1/2*(3*I*e + b*\ln(f) + 2*c*x*\ln(f))/c^{(1/2)}/\ln(f)^{(1/2)}) * \Pi^{(1/2)}/c^{(1/2)}/\ln(f)^{(1/2)}$

Rubi [A] time = 0.42, antiderivative size = 346, normalized size of antiderivative = 1.00, number of steps used = 14, number of rules used = 4, integrand size = 21, number of rules / integrand size = 0.190, Rules used = {4473, 2287, 2234, 2204}

$$\frac{3\sqrt{\pi} f^a e^{\frac{(e+ib \log(f))^2}{4c \log(f)} - id} \operatorname{Erfi}\left(\frac{-b \log(f) - 2cx \log(f) + ie}{2\sqrt{c} \sqrt{\log(f)}}\right)}{16\sqrt{c} \sqrt{\log(f)}} - \frac{\sqrt{\pi} f^a e^{\frac{(3e+ib \log(f))^2}{4c \log(f)} - 3id} \operatorname{Erfi}\left(\frac{-b \log(f) - 2cx \log(f) + 3ie}{2\sqrt{c} \sqrt{\log(f)}}\right)}{16\sqrt{c} \sqrt{\log(f)}} + \frac{3\sqrt{\pi} f^a e^{\frac{(e-ib \log(f))^2}{4c \log(f)} - id} \operatorname{Erfi}\left(\frac{-b \log(f) - 2cx \log(f) + ie}{2\sqrt{c} \sqrt{\log(f)}}\right)}{16\sqrt{c} \sqrt{\log(f)}} - \frac{\sqrt{\pi} f^a e^{\frac{(3e-ib \log(f))^2}{4c \log(f)} - 3id} \operatorname{Erfi}\left(\frac{-b \log(f) - 2cx \log(f) + 3ie}{2\sqrt{c} \sqrt{\log(f)}}\right)}{16\sqrt{c} \sqrt{\log(f)}} + \dots$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[f^{(a + b*x + c*x^2)} * \operatorname{Cos}[d + e*x]^3, x]$

[Out] $(-3 * E^{((-I)*d + (e + I*b*Log[f])^2/(4*c*Log[f]))} * f^a * \operatorname{Sqrt}[\Pi] * \operatorname{Erfi}[(I*e - b*Log[f] - 2*c*x*Log[f])/(2*\operatorname{Sqrt}[c]*\operatorname{Sqrt}[Log[f]])]) / (16*\operatorname{Sqrt}[c]*\operatorname{Sqrt}[Log[f]]) - (E^{((-3*I)*d + (3e + I*b*Log[f])^2/(4*c*Log[f]))} * f^a * \operatorname{Sqrt}[\Pi] * \operatorname{Erfi}[(3*I)*e - b*Log[f] - 2*c*x*Log[f])/(2*\operatorname{Sqrt}[c]*\operatorname{Sqrt}[Log[f]])]) / (16*\operatorname{Sqrt}[c]*\operatorname{Sqrt}[Log[f]]) + (3 * E^{(I*d + (e - I*b*Log[f])^2/(4*c*Log[f]))} * f^a * \operatorname{Sqrt}[\Pi] * \operatorname{Erfi}[(I*e + b*Log[f] + 2*c*x*Log[f])/(2*\operatorname{Sqrt}[c]*\operatorname{Sqrt}[Log[f]])]) / (16*\operatorname{Sqrt}[c]*\operatorname{Sqrt}[Log[f]]) + (E^{((3*I)*d - ((3*I)*e + b*Log[f])^2/(4*c*Log[f]))} * f^a * \operatorname{Sqrt}[\Pi] * \operatorname{Erfi}[(3*I)*e + b*Log[f] + 2*c*x*Log[f])/(2*\operatorname{Sqrt}[c]*\operatorname{Sqrt}[Log[f]])]) / (16*\operatorname{Sqrt}[c]*\operatorname{Sqrt}[Log[f]])$

Rule 2204

$\operatorname{Int}[(F_)^{((a_.) + (b_.)*((c_.) + (d_.)*(x_.))^2)}, x_Symbol] \rightarrow \operatorname{Simp}[(F^a * \operatorname{Sqrt}[\Pi] * \operatorname{Erfi}[(c + d*x)*\operatorname{Rt}[b*Log[F], 2]]) / (2*d*\operatorname{Rt}[b*Log[F], 2]), x] /; \operatorname{FreeQ}\{F, a, b, c, d\}, x] \ \&\& \ \operatorname{PosQ}[b]$

Rule 2234

$\operatorname{Int}[(F_)^{((a_.) + (b_.)*(x_.) + (c_.)*(x_.)^2)}, x_Symbol] \rightarrow \operatorname{Dist}[F^{(a - b^2/(4*c))}, \operatorname{Int}[F^{((b + 2*c*x)^2/(4*c))}, x], x] /; \operatorname{FreeQ}\{F, a, b, c\}, x]$

Rule 2287

$\operatorname{Int}[(u_.)*(F_)^{(v_.)*(G_)^{(w_.)}}, x_Symbol] \rightarrow \operatorname{With}\{z = v*\operatorname{Log}[F] + w*\operatorname{Log}[G]\}, \operatorname{Int}[u*\operatorname{NormalizeIntegrand}[E^z, x], x] /; \operatorname{BinomialQ}[z, x] \ || \ (\operatorname{PolynomialQ}[z, x] \ \&\& \ \operatorname{LeQ}[\operatorname{Exponent}[z, x], 2]) /; \operatorname{FreeQ}\{F, G\}, x]$

Rule 4473

$\operatorname{Int}[\operatorname{Cos}[v_]^{(n_.)}*(F_)^{(u_.)}, x_Symbol] \rightarrow \operatorname{Int}[\operatorname{ExpandTrigToExp}[F^u, \operatorname{Cos}[v]^n], x] /; \operatorname{FreeQ}[F, x] \ \&\& \ (\operatorname{LinearQ}[u, x] \ || \ \operatorname{PolyQ}[u, x, 2]) \ \&\& \ (\operatorname{LinearQ}[v,$

x] || PolyQ[v, x, 2]) && IGtQ[n, 0]

Rubi steps

$$\begin{aligned}
 \int f^{a+bx+cx^2} \cos^3(d+ex) dx &= \int \left(\frac{3}{8} e^{-id-ix} f^{a+bx+cx^2} + \frac{3}{8} e^{id+ix} f^{a+bx+cx^2} + \frac{1}{8} e^{-3id-3iex} f^{a+bx+cx^2} + \frac{1}{8} e^{3id+3iex} f^{a+bx+cx^2} \right) dx \\
 &= \frac{1}{8} \int e^{-3id-3iex} f^{a+bx+cx^2} dx + \frac{1}{8} \int e^{3id+3iex} f^{a+bx+cx^2} dx + \frac{3}{8} \int e^{-id-ix} f^{a+bx+cx^2} dx + \frac{3}{8} \int e^{id+ix} f^{a+bx+cx^2} dx \\
 &= \frac{1}{8} \int \exp(-3id + a \log(f) + cx^2 \log(f) - x(3ie - b \log(f))) dx + \frac{1}{8} \int \exp(3id + a \log(f) + cx^2 \log(f) + x(3ie - b \log(f))) dx \\
 &= \frac{1}{8} \left(3e^{id + \frac{(e-ib \log(f))^2}{4c \log(f)}} f^a \right) \int \exp\left(\frac{(ie + b \log(f) + 2cx \log(f))^2}{4c \log(f)}\right) dx + \frac{1}{8} \left(3e^{-id + \frac{(e+ib \log(f))^2}{4c \log(f)}} f^a \right) \int \exp\left(\frac{(ie - b \log(f) - 2cx \log(f))^2}{4c \log(f)}\right) dx \\
 &= -\frac{3e^{-id + \frac{(e+ib \log(f))^2}{4c \log(f)}} f^a \sqrt{\pi} \operatorname{erfi}\left(\frac{ie - b \log(f) - 2cx \log(f)}{2\sqrt{c} \sqrt{\log(f)}}\right)}{16\sqrt{c} \sqrt{\log(f)}} - \frac{\exp(-3id + \frac{(3e+ib \log(f))^2}{4c \log(f)}) f^a \sqrt{\pi}}{16\sqrt{c} \sqrt{\log(f)}}
 \end{aligned}$$

Mathematica [A] time = 0.95, size = 386, normalized size = 1.12

$$\sqrt{\pi} f^{a-\frac{b^2}{4c}} e^{\frac{e-6ib \log(f)}{4c \log(f)}} \left(i \sin(3d) e^{\frac{2e^2}{c \log(f)}} \operatorname{erfi}\left(\frac{\log(f)(b+2cx)+3ie}{2\sqrt{c} \sqrt{\log(f)}}\right) + \cos(3d) e^{\frac{2e^2}{c \log(f)}} \operatorname{erfi}\left(\frac{\log(f)(b+2cx)+3ie}{2\sqrt{c} \sqrt{\log(f)}}\right) - i \sin(3d) e^{\frac{e(2e+3ib)}{c \log(f)}} \right)$$

Antiderivative was successfully verified.

[In] Integrate[f^(a + b*x + c*x^2)*Cos[d + e*x]^3,x]

[Out] (E^((e*(e - (6*I)*b*Log[f]))/(4*c*Log[f]))*f^(a - b^2/(4*c))*Sqrt[Pi]*(E^((e*(2*e + (3*I)*b*Log[f]))/(c*Log[f]))*Cos[3*d]*Erfi[((-3*I)*e + (b + 2*c*x)*Log[f])/(2*Sqrt[c]*Sqrt[Log[f]])] + E^((2*e^2)/(c*Log[f]))*Cos[3*d]*Erfi[((3*I)*e + (b + 2*c*x)*Log[f])/(2*Sqrt[c]*Sqrt[Log[f]])] + 3*E^(((2*I)*b*e)/c)*Erfi[((-I)*e + (b + 2*c*x)*Log[f])/(2*Sqrt[c]*Sqrt[Log[f]])]*(Cos[d] - I*Sin[d]) + 3*E^(((I*b*e)/c)*Erfi[(I*e + (b + 2*c*x)*Log[f])/(2*Sqrt[c]*Sqrt[Log[f]])]*(Cos[d] + I*Sin[d]) - I*E^((e*(2*e + (3*I)*b*Log[f]))/(c*Log[f]))*Erfi[((-3*I)*e + (b + 2*c*x)*Log[f])/(2*Sqrt[c]*Sqrt[Log[f]])]*Sin[3*d] + I*E^((2*e^2)/(c*Log[f]))*Erfi[((3*I)*e + (b + 2*c*x)*Log[f])/(2*Sqrt[c]*Sqrt[Log[f]])]*Sin[3*d]))/(16*Sqrt[c]*Sqrt[Log[f]])

fricas [A] time = 0.77, size = 344, normalized size = 0.99

$$3 \sqrt{\pi} \sqrt{-c \log(f)} \operatorname{erf}\left(\frac{((2cx+b) \log(f)+ie) \sqrt{-c \log(f)}}{2c \log(f)}\right) e^{\left(-\frac{(b^2-4ac) \log(f)^2 - e^2 - (4icd-2ibe) \log(f)}{4c \log(f)}\right)} + 3 \sqrt{\pi} \sqrt{-c \log(f)} \operatorname{erf}\left(\frac{((2cx+b) \log(f)-ie) \sqrt{-c \log(f)}}{2c \log(f)}\right) e^{\left(-\frac{(b^2-4ac) \log(f)^2 - e^2 - (4icd-2ibe) \log(f)}{4c \log(f)}\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(c*x^2+b*x+a)*cos(e*x+d)^3,x, algorithm="fricas")

[Out] -1/16*(3*sqrt(pi)*sqrt(-c*log(f))*erf(1/2*((2*c*x + b)*log(f) + I*e)*sqrt(-c*log(f))/(c*log(f)))*e^(-1/4*((b^2 - 4*a*c)*log(f)^2 - e^2 - (4*I*c*d - 2*I*b*e)*log(f))/(c*log(f))) + 3*sqrt(pi)*sqrt(-c*log(f))*erf(1/2*((2*c*x + b)*log(f) - I*e)*sqrt(-c*log(f))/(c*log(f)))*e^(-1/4*((b^2 - 4*a*c)*log(f)^2 - e^2 - (-4*I*c*d + 2*I*b*e)*log(f))/(c*log(f))) + sqrt(pi)*sqrt(-c*log(f))*erf(1/2*((2*c*x + b)*log(f) + 3*I*e)*sqrt(-c*log(f))/(c*log(f)))*e^(-1/4*((b^2 - 4*a*c)*log(f)^2 - 9*e^2 - (12*I*c*d - 6*I*b*e)*log(f))/(c*log(f))) + sqrt(pi)*sqrt(-c*log(f))*erf(1/2*((2*c*x + b)*log(f) - 3*I*e)*sqrt(-c*log(f))/(c*log(f)))*e^(-1/4*((b^2 - 4*a*c)*log(f)^2 - 9*e^2 - (12*I*c*d - 6*I*b*e)*log(f))/(c*log(f)))

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int f^{cx^2+bx+a} \cos(dx+ex)^3 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(f^(a + b*x + c*x^2)*cos(d + e*x)^3,x)

[Out] int(f^(a + b*x + c*x^2)*cos(d + e*x)^3, x)

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f**(c*x**2+b*x+a)*cos(e*x+d)**3,x)

[Out] Timed out

3.128 $\int f^{a+bx+cx^2} \cos(d + fx^2) dx$

Optimal. Leaf size=189

$$\frac{\sqrt{\pi} f^a e^{id - \frac{b^2 \log^2(f)}{4c \log(f) + 4if}} \operatorname{erfi}\left(\frac{b \log(f) + 2x(c \log(f) + if)}{2\sqrt{c \log(f) + if}}\right)}{4\sqrt{c \log(f) + if}} - \frac{\sqrt{\pi} f^a e^{-\frac{b^2 \log^2(f)}{4c \log(f) + 4if} - id} \operatorname{erf}\left(\frac{b \log(f) - 2x(-c \log(f) + if)}{2\sqrt{-c \log(f) + if}}\right)}{4\sqrt{-c \log(f) + if}}$$

[Out] $-1/4 * \exp(-I * d + b^2 * \ln(f)^2 / (4 * I * f - 4 * c * \ln(f))) * f^a * \operatorname{erf}(1/2 * (b * \ln(f) - 2 * x * (I * f - c * \ln(f)))) / (I * f - c * \ln(f))^{1/2} * \pi^{1/2} / (I * f - c * \ln(f))^{1/2} + 1/4 * \exp(I * d - b^2 * \ln(f)^2 / (4 * I * f + 4 * c * \ln(f))) * f^a * \operatorname{erfi}(1/2 * (b * \ln(f) + 2 * x * (I * f + c * \ln(f)))) / (I * f + c * \ln(f))^{1/2} * \pi^{1/2} / (I * f + c * \ln(f))^{1/2}$

Rubi [A] time = 0.27, antiderivative size = 189, normalized size of antiderivative = 1.00, number of steps used = 8, number of rules used = 5, integrand size = 21, $\frac{\text{number of rules}}{\text{integrand size}} = 0.238$, Rules used = {4473, 2287, 2234, 2205, 2204}

$$\frac{\sqrt{\pi} f^a e^{id - \frac{b^2 \log^2(f)}{4c \log(f) + 4if}} \operatorname{Erfi}\left(\frac{b \log(f) + 2x(c \log(f) + if)}{2\sqrt{c \log(f) + if}}\right)}{4\sqrt{c \log(f) + if}} - \frac{\sqrt{\pi} f^a e^{-\frac{b^2 \log^2(f)}{4c \log(f) + 4if} - id} \operatorname{Erf}\left(\frac{b \log(f) - 2x(-c \log(f) + if)}{2\sqrt{-c \log(f) + if}}\right)}{4\sqrt{-c \log(f) + if}}$$

Antiderivative was successfully verified.

[In] `Int[f^(a + b*x + c*x^2)*Cos[d + f*x^2], x]`

[Out] $-(E^{((-I)*d + (b^2 * \operatorname{Log}[f]^2) / ((4 * I) * f - 4 * c * \operatorname{Log}[f]))} * f^a * \operatorname{Sqrt}[\pi] * \operatorname{Erf}[(b * \operatorname{Log}[f] - 2 * x * (I * f - c * \operatorname{Log}[f])) / (2 * \operatorname{Sqrt}[I * f - c * \operatorname{Log}[f]])]) / (4 * \operatorname{Sqrt}[I * f - c * \operatorname{Log}[f]]) + (E^{(I * d - (b^2 * \operatorname{Log}[f]^2) / ((4 * I) * f + 4 * c * \operatorname{Log}[f]))} * f^a * \operatorname{Sqrt}[\pi] * \operatorname{Erfi}[(b * \operatorname{Log}[f] + 2 * x * (I * f + c * \operatorname{Log}[f])) / (2 * \operatorname{Sqrt}[I * f + c * \operatorname{Log}[f]])]) / (4 * \operatorname{Sqrt}[I * f + c * \operatorname{Log}[f]])$

Rule 2204

`Int[(F_)^((a_) + (b_)*((c_) + (d_)*(x_)^2), x_Symbol] := Simp[(F^a * Sqrt[Pi] * Erfi[(c + d*x) * Rt[b * Log[F], 2]]) / (2 * d * Rt[b * Log[F], 2]), x] /; FreeQ[{F, a, b, c, d}, x] && PosQ[b]`

Rule 2205

`Int[(F_)^((a_) + (b_)*((c_) + (d_)*(x_)^2), x_Symbol] := Simp[(F^a * Sqrt[Pi] * Erf[(c + d*x) * Rt[-(b * Log[F]), 2]]) / (2 * d * Rt[-(b * Log[F]), 2]), x] /; FreeQ[{F, a, b, c, d}, x] && NegQ[b]`

Rule 2234

`Int[(F_)^((a_) + (b_)*(x_) + (c_)*(x_)^2), x_Symbol] := Dist[F^(a - b^2 / (4 * c)), Int[F^((b + 2 * c * x)^2 / (4 * c)), x], x] /; FreeQ[{F, a, b, c}, x]`

Rule 2287

`Int[(u_)*(F_)^(v_)*(G_)^(w_), x_Symbol] := With[{z = v * Log[F] + w * Log[G]}, Int[u * NormalizeIntegrand[E^z, x], x] /; BinomialQ[z, x] || (PolynomialQ[z, x] && LeQ[Exponent[z, x], 2])] /; FreeQ[{F, G}, x]`

Rule 4473

`Int[Cos[v_]^(n_)*(F_)^(u_), x_Symbol] := Int[ExpandTrigToExp[F^u, Cos[v]^n, x], x] /; FreeQ[F, x] && (LinearQ[u, x] || PolyQ[u, x, 2]) && (LinearQ[v, x] || PolyQ[v, x, 2]) && IGtQ[n, 0]`

Rubi steps

$$\begin{aligned}
\int f^{a+bx+cx^2} \cos(d + fx^2) dx &= \int \left(\frac{1}{2} e^{-id-ifx^2} f^{a+bx+cx^2} + \frac{1}{2} e^{id+ifx^2} f^{a+bx+cx^2} \right) dx \\
&= \frac{1}{2} \int e^{-id-ifx^2} f^{a+bx+cx^2} dx + \frac{1}{2} \int e^{id+ifx^2} f^{a+bx+cx^2} dx \\
&= \frac{1}{2} \int \exp(-id + a \log(f) + bx \log(f) - x^2(if - c \log(f))) dx + \frac{1}{2} \int \exp(id + a \log(f) + bx \log(f) - x^2(if + c \log(f))) dx \\
&= \frac{1}{2} \left(e^{-id + \frac{b^2 \log^2(f)}{4if-4c \log(f)}} f^a \right) \int \exp\left(\frac{(b \log(f) + 2x(-if + c \log(f)))^2}{4(-if + c \log(f))}\right) dx + \frac{1}{2} \left(e^{id - \frac{b^2 \log^2(f)}{4if+4c \log(f)}} f^a \right) \int \exp\left(\frac{(b \log(f) + 2x(-if - c \log(f)))^2}{4(-if - c \log(f))}\right) dx \\
&= -\frac{e^{-id + \frac{b^2 \log^2(f)}{4if-4c \log(f)}} f^a \sqrt{\pi} \operatorname{erf}\left(\frac{b \log(f) - 2x(-if - c \log(f))}{2\sqrt{if - c \log(f)}}\right)}{4\sqrt{if - c \log(f)}} + \frac{e^{id - \frac{b^2 \log^2(f)}{4if+4c \log(f)}} f^a \sqrt{\pi} \operatorname{erfi}\left(\frac{b \log(f) + 2x(-if + c \log(f))}{2\sqrt{if + c \log(f)}}\right)}{4\sqrt{if + c \log(f)}}
\end{aligned}$$

Mathematica [A] time = 1.00, size = 231, normalized size = 1.22

$$(-1)^{3/4} \sqrt{\pi} f^a e^{-\frac{b^2 \log^2(f)}{4c \log(f) + 4if}} \left(\sqrt{f - ic \log(f)} (f + ic \log(f)) (\cos(d) + i \sin(d)) e^{\frac{ib^2 f \log^2(f)}{2(c^2 \log^2(f) + f^2)}} \operatorname{erfi}\left(\frac{\sqrt[4]{-1} (2fx - i \log(f)(b + 2cx))}{2\sqrt{f - ic \log(f)}}\right) \right)$$

$$4(c^2 \log^2(f) + f^2)$$

Antiderivative was successfully verified.

[In] Integrate[f^(a + b*x + c*x^2)*Cos[d + f*x^2],x]

[Out] -1/4*((-1)^(3/4)*E^((b^2*Log[f]^2)/((4*I)*f - 4*c*Log[f]))*f^a*Sqrt[Pi]*(Erfi[(-1)^(3/4)*(2*f*x + I*(b + 2*c*x)*Log[f])]/(2*Sqrt[f + I*c*Log[f]])]*(f - I*c*Log[f])*Sqrt[f + I*c*Log[f]]*((-I)*Cos[d] - Sin[d]) + E^(((I/2)*b^2*f*Log[f]^2)/(f^2 + c^2*Log[f]^2))*Erfi[(-1)^(1/4)*(2*f*x - I*(b + 2*c*x)*Log[f])]/(2*Sqrt[f - I*c*Log[f]])*Sqrt[f - I*c*Log[f]]*(f + I*c*Log[f]))*(Cos[d] + I*Sin[d]))/(f^2 + c^2*Log[f]^2)

fricas [B] time = 0.72, size = 311, normalized size = 1.65

$$\sqrt{\pi} (c \log(f) - if) \sqrt{-c \log(f) - if} \operatorname{erf}\left(\frac{(2f^2x - if \log(f) + (2c^2x + bc) \log(f)^2) \sqrt{-c \log(f) - if}}{2(c^2 \log(f)^2 + f^2)}\right) e^{\left(\frac{4af^2 \log(f) - (b^2c - 4ac^2) \log(f)^3 + 4idf^2}{4(c^2 \log(f)^2 + f^2)}\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(c*x^2+b*x+a)*cos(f*x^2+d),x, algorithm="fricas")

[Out] -1/4*(sqrt(pi)*(c*log(f) - I*f)*sqrt(-c*log(f) - I*f)*erf(1/2*(2*f^2*x - I*b*f*log(f) + (2*c^2*x + b*c)*log(f)^2)*sqrt(-c*log(f) - I*f)/(c^2*log(f)^2 + f^2))*e^(1/4*(4*a*f^2*log(f) - (b^2*c - 4*a*c^2)*log(f)^3 + 4*I*d*f^2 + (4*I*c^2*d + I*b^2*f)*log(f)^2)/(c^2*log(f)^2 + f^2)) + sqrt(pi)*(c*log(f) + I*f)*sqrt(-c*log(f) + I*f)*erf(1/2*(2*f^2*x + I*b*f*log(f) + (2*c^2*x + b*c)*log(f)^2)*sqrt(-c*log(f) + I*f)/(c^2*log(f)^2 + f^2))*e^(1/4*(4*a*f^2*log(f) - (b^2*c - 4*a*c^2)*log(f)^3 - 4*I*d*f^2 + (-4*I*c^2*d - I*b^2*f)*log(f)^2)/(c^2*log(f)^2 + f^2)))/(c^2*log(f)^2 + f^2)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int f^{cx^2+bx+a} \cos(fx^2 + d) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(c*x^2+b*x+a)*cos(f*x^2+d),x, algorithm="giac")

[Out] integrate(f^(c*x^2 + b*x + a)*cos(f*x^2 + d), x)

maple [A] time = 0.18, size = 178, normalized size = 0.94

$$\frac{\sqrt{\pi} f^a e^{-\frac{4df+4id\ln(f)c+\ln(f)^2b^2}{4(-if+c\ln(f))}} \operatorname{erf}\left(-x\sqrt{if-c\ln(f)} + \frac{\ln(f)b}{2\sqrt{if-c\ln(f)}}\right)}{4\sqrt{if-c\ln(f)}} - \frac{\sqrt{\pi} f^a e^{-\frac{4df-4id\ln(f)c+\ln(f)^2b^2}{4(if+c\ln(f))}} \operatorname{erf}\left(-\sqrt{-if-c\ln(f)}\right)}{4\sqrt{-if-c\ln(f)}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(f^(c*x^2+b*x+a)*cos(f*x^2+d),x)

[Out]
$$\frac{-1/4\pi^{1/2}f^a\exp(-1/4(4df+4id\ln(f)c+\ln(f)^2b^2)/(-If+c\ln(f)))}{(If-c\ln(f))^{1/2}}\operatorname{erf}(-x(If-c\ln(f))^{1/2}+1/2\ln(f)b/(If-c\ln(f))^{1/2}) - 1/4\pi^{1/2}f^a\exp(-1/4(4df-4id\ln(f)c+\ln(f)^2b^2)/(If+c\ln(f)))}{(-If-c\ln(f))^{1/2}}\operatorname{erf}(-(-If-c\ln(f))^{1/2}x+1/2\ln(f)b/(-If-c\ln(f))^{1/2})$$

maxima [B] time = 0.36, size = 648, normalized size = 3.43

$$\sqrt{\pi} \sqrt{2c^2 \log(f)^2 + 2f^2} \left(i f^a \cos\left(\frac{4df^2 + (4c^2d + b^2f)\log(f)^2}{4(c^2\log(f)^2 + f^2)}\right) + f^a \sin\left(\frac{4df^2 + (4c^2d + b^2f)\log(f)^2}{4(c^2\log(f)^2 + f^2)}\right) \right) \operatorname{erf}\left(\frac{2(c\log(f) - if)x + b\log(f)}{2\sqrt{-c\log(f)}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(c*x^2+b*x+a)*cos(f*x^2+d),x, algorithm="maxima")

[Out]
$$\frac{1}{8}\sqrt{\pi}\sqrt{2c^2\log(f)^2 + 2f^2}\left(\frac{f^a\cos\left(\frac{1}{4}(4df^2 + (4c^2d + b^2f)\log(f)^2)/(c^2\log(f)^2 + f^2)\right)}{(c^2\log(f)^2 + f^2)} + \frac{f^a\sin\left(\frac{1}{4}(4df^2 + (4c^2d + b^2f)\log(f)^2)/(c^2\log(f)^2 + f^2)\right)}{(c^2\log(f)^2 + f^2)}\right)\operatorname{erf}\left(\frac{1}{2}(2(c\log(f) - If)x + b\log(f))/\sqrt{-c\log(f) + If}\right) + \frac{(-1)f^a\cos\left(\frac{1}{4}(4df^2 + (4c^2d + b^2f)\log(f)^2)/(c^2\log(f)^2 + f^2)\right)}{(c^2\log(f)^2 + f^2)} + \frac{f^a\sin\left(\frac{1}{4}(4df^2 + (4c^2d + b^2f)\log(f)^2)/(c^2\log(f)^2 + f^2)\right)}{(c^2\log(f)^2 + f^2)}\operatorname{erf}\left(\frac{1}{2}(2(c\log(f) + If)x + b\log(f))/\sqrt{-c\log(f) - If}\right)\sqrt{c\log(f) + \sqrt{c^2\log(f)^2 + f^2}} - \sqrt{\pi}\sqrt{2c^2\log(f)^2 + 2f^2}\left(\frac{f^a\cos\left(\frac{1}{4}(4df^2 + (4c^2d + b^2f)\log(f)^2)/(c^2\log(f)^2 + f^2)\right)}{(c^2\log(f)^2 + f^2)} - \frac{If^a\sin\left(\frac{1}{4}(4df^2 + (4c^2d + b^2f)\log(f)^2)/(c^2\log(f)^2 + f^2)\right)}{(c^2\log(f)^2 + f^2)}\right)\operatorname{erf}\left(\frac{1}{2}(2(c\log(f) - If)x + b\log(f))/\sqrt{-c\log(f) + If}\right) + \left(\frac{f^a\cos\left(\frac{1}{4}(4df^2 + (4c^2d + b^2f)\log(f)^2)/(c^2\log(f)^2 + f^2)\right)}{(c^2\log(f)^2 + f^2)} + \frac{If^a\sin\left(\frac{1}{4}(4df^2 + (4c^2d + b^2f)\log(f)^2)/(c^2\log(f)^2 + f^2)\right)}{(c^2\log(f)^2 + f^2)}\right)\operatorname{erf}\left(\frac{1}{2}(2(c\log(f) + If)x + b\log(f))/\sqrt{-c\log(f) - If}\right)\sqrt{-c\log(f) + \sqrt{c^2\log(f)^2 + f^2}}\right)/(c^2e^{1/4b^2c\log(f)}(c^2\log(f)^2 + f^2)\log(f)^2 + f^2e^{1/4b^2c\log(f)}(c^2\log(f)^2 + f^2))$$

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int f^{cx^2+bx+a} \cos(fx^2+d) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(f^(a + b*x + c*x^2)*cos(d + f*x^2),x)

[Out] int(f^(a + b*x + c*x^2)*cos(d + f*x^2), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int f^{a+bx+cx^2} \cos(d + fx^2) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f**(c*x**2+b*x+a)*cos(f*x**2+d),x)

[Out] Integral(f**(a + b*x + c*x**2)*cos(d + f*x**2), x)

$$3.129 \quad \int f^{a+bx+cx^2} \cos^2(d + fx^2) dx$$

Optimal. Leaf size=245

$$\frac{\sqrt{\pi} f^a e^{-\frac{b^2 \log^2(f)}{4c \log(f)+8if} - 2id} \operatorname{erf}\left(\frac{b \log(f) - 2x(-c \log(f) + 2if)}{2\sqrt{-c \log(f) + 2if}}\right)}{8\sqrt{-c \log(f) + 2if}} + \frac{\sqrt{\pi} f^a e^{2id - \frac{b^2 \log^2(f)}{4c \log(f)+8if}} \operatorname{erfi}\left(\frac{b \log(f) + 2x(c \log(f) + 2if)}{2\sqrt{c \log(f) + 2if}}\right)}{8\sqrt{c \log(f) + 2if}} + \frac{\sqrt{\pi} f^{a - \frac{b^2}{4c}}}{4\sqrt{c}}$$

[Out] $\frac{1}{4} f^{(a-1/4*b^2/c)} \operatorname{erfi}\left(\frac{1/2*(2*c*x+b)*\ln(f)^{(1/2)/c^{(1/2)}}*\Pi^{(1/2)/c^{(1/2)}}}{\ln(f)^{(1/2)}-1/8*\exp(-2*I*d+b^2*\ln(f)^2/(8*I*f-4*c*\ln(f)))} * f^a * \operatorname{erf}\left(\frac{1/2*(b*\ln(f)-2*x*(2*I*f-c*\ln(f)))}{(2*I*f-c*\ln(f))^{(1/2)}}*\Pi^{(1/2)/(2*I*f-c*\ln(f))^{(1/2)}}+1/8*\exp(2*I*d-b^2*\ln(f)^2/(8*I*f+4*c*\ln(f)))} * f^a * \operatorname{erfi}\left(\frac{1/2*(b*\ln(f)+2*x*(2*I*f+c*\ln(f)))}{(2*I*f+c*\ln(f))^{(1/2)}}*\Pi^{(1/2)/(2*I*f+c*\ln(f))^{(1/2)}}\right)\right)$

Rubi [A] time = 0.41, antiderivative size = 245, normalized size of antiderivative = 1.00, number of steps used = 10, number of rules used = 5, integrand size = 23, $\frac{\text{number of rules}}{\text{integrand size}} = 0.217$, Rules used = {4473, 2234, 2204, 2287, 2205}

$$\frac{\sqrt{\pi} f^a e^{-\frac{b^2 \log^2(f)}{4c \log(f)+8if} - 2id} \operatorname{Erf}\left(\frac{b \log(f) - 2x(-c \log(f) + 2if)}{2\sqrt{-c \log(f) + 2if}}\right)}{8\sqrt{-c \log(f) + 2if}} + \frac{\sqrt{\pi} f^a e^{2id - \frac{b^2 \log^2(f)}{4c \log(f)+8if}} \operatorname{Erfi}\left(\frac{b \log(f) + 2x(c \log(f) + 2if)}{2\sqrt{c \log(f) + 2if}}\right)}{8\sqrt{c \log(f) + 2if}} + \frac{\sqrt{\pi} f^{a - \frac{b^2}{4c}}}{4\sqrt{c}}$$

Antiderivative was successfully verified.

[In] Int[f^(a + b*x + c*x^2)*Cos[d + f*x^2]^2,x]

[Out] $(f^{(a - b^2/(4*c))} * \operatorname{Sqrt}[\Pi] * \operatorname{Erfi}\left(\frac{(b + 2*c*x) * \operatorname{Sqrt}[\operatorname{Log}[f]]}{2 * \operatorname{Sqrt}[c]}\right)) / (4 * \operatorname{Sqrt}[c] * \operatorname{Sqrt}[\operatorname{Log}[f]]) - (E^{((-2*I)*d + (b^2 * \operatorname{Log}[f]^2) / ((8*I)*f - 4*c * \operatorname{Log}[f]))} * f^a * \operatorname{Sqrt}[\Pi] * \operatorname{Erf}\left(\frac{(b * \operatorname{Log}[f] - 2*x * ((2*I)*f - c * \operatorname{Log}[f]))}{2 * \operatorname{Sqrt}[(2*I)*f - c * \operatorname{Log}[f]]}\right)) / (8 * \operatorname{Sqrt}[(2*I)*f - c * \operatorname{Log}[f]]) + (E^{((2*I)*d - (b^2 * \operatorname{Log}[f]^2) / ((8*I)*f + 4*c * \operatorname{Log}[f]))} * f^a * \operatorname{Sqrt}[\Pi] * \operatorname{Erfi}\left(\frac{(b * \operatorname{Log}[f] + 2*x * ((2*I)*f + c * \operatorname{Log}[f]))}{2 * \operatorname{Sqrt}[(2*I)*f + c * \operatorname{Log}[f]]}\right)) / (8 * \operatorname{Sqrt}[(2*I)*f + c * \operatorname{Log}[f]])$

Rule 2204

Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_)^2), x_Symbol] := Simp[(F^a*Sqrt[Pi]*Erfi[(c + d*x)*Rt[b*Log[F], 2]]/(2*d*Rt[b*Log[F], 2]), x] /; FreeQ[{F, a, b, c, d}, x] && PosQ[b]

Rule 2205

Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_)^2), x_Symbol] := Simp[(F^a*Sqrt[Pi]*Erf[(c + d*x)*Rt[-(b*Log[F]), 2]]/(2*d*Rt[-(b*Log[F]), 2]), x] /; FreeQ[{F, a, b, c, d}, x] && NegQ[b]

Rule 2234

Int[(F_)^((a_.) + (b_.)*(x_) + (c_.)*(x_)^2), x_Symbol] := Dist[F^(a - b^2/(4*c)), Int[F^((b + 2*c*x)^2/(4*c)), x], x] /; FreeQ[{F, a, b, c}, x]

Rule 2287

Int[(u_.)*(F_)^(v_.)*(G_)^(w_.), x_Symbol] := With[{z = v*Log[F] + w*Log[G]}, Int[u*NormalizeIntegrand[E^z, x], x] /; BinomialQ[z, x] || (PolynomialQ[z, x] && LeQ[Exponent[z, x], 2]) /; FreeQ[{F, G}, x]

Rule 4473

Int[Cos[v_]^(n_.)*(F_)^(u_), x_Symbol] := Int[ExpandTrigToExp[F^u, Cos[v]^n, x], x] /; FreeQ[F, x] && (LinearQ[u, x] || PolyQ[u, x, 2]) && (LinearQ[v,

x] || PolyQ[v, x, 2]) && IGtQ[n, 0]

Rubi steps

$$\begin{aligned}
 \int f^{a+bx+cx^2} \cos^2(d + fx^2) dx &= \int \left(\frac{1}{2} f^{a+bx+cx^2} + \frac{1}{4} e^{-2id-2ifx^2} f^{a+bx+cx^2} + \frac{1}{4} e^{2id+2ifx^2} f^{a+bx+cx^2} \right) dx \\
 &= \frac{1}{4} \int e^{-2id-2ifx^2} f^{a+bx+cx^2} dx + \frac{1}{4} \int e^{2id+2ifx^2} f^{a+bx+cx^2} dx + \frac{1}{2} \int f^{a+bx+cx^2} dx \\
 &= \frac{1}{4} \int \exp(-2id + a \log(f) + bx \log(f) - x^2(2if - c \log(f))) dx + \frac{1}{4} \int \exp(2id + a \log(f) + bx \log(f) - x^2(2if - c \log(f))) dx \\
 &= \frac{f^{a-\frac{b^2}{4c}} \sqrt{\pi} \operatorname{erfi}\left(\frac{(b+2cx)\sqrt{\log(f)}}{2\sqrt{c}}\right)}{4\sqrt{c}\sqrt{\log(f)}} + \frac{1}{4} \left(e^{-2id + \frac{b^2 \log^2(f)}{8if-4c \log(f)}} f^a \right) \int \exp\left(\frac{(b \log(f) + 2x(-2if + c \log(f)))}{4(-2if + c \log(f))}\right) dx \\
 &= \frac{f^{a-\frac{b^2}{4c}} \sqrt{\pi} \operatorname{erfi}\left(\frac{(b+2cx)\sqrt{\log(f)}}{2\sqrt{c}}\right)}{4\sqrt{c}\sqrt{\log(f)}} - \frac{e^{-2id + \frac{b^2 \log^2(f)}{8if-4c \log(f)}} f^a \sqrt{\pi} \operatorname{erf}\left(\frac{(b \log(f) - 2x(2if - c \log(f)))}{2\sqrt{2if - c \log(f)}}\right)}{8\sqrt{2if - c \log(f)}}
 \end{aligned}$$

Mathematica [A] time = 3.10, size = 301, normalized size = 1.23

$$\frac{1}{8} \sqrt{\pi} f^a \left(\frac{2f^{-\frac{b^2}{4c}} \operatorname{erfi}\left(\frac{\sqrt{\log(f)}(b+2cx)}{2\sqrt{c}}\right)}{\sqrt{c}\sqrt{\log(f)}} + \frac{\sqrt[4]{-1} e^{-\frac{b^2 \log^2(f)}{4c \log(f)+8if}} \left(\sqrt{2f - ic \log(f)} (2f + ic \log(f)) (\sin(2d) - i \cos(2d)) \right) e^{\frac{ib^2}{c^2 \log(f)}}}{\sqrt{2f - ic \log(f)} (2f + ic \log(f)) (\sin(2d) - i \cos(2d)) e^{\frac{ib^2}{c^2 \log(f)}}}} \right)$$

Warning: Unable to verify antiderivative.

[In] Integrate[f^(a + b*x + c*x^2)*Cos[d + f*x^2]^2,x]

[Out] (f^a*Sqrt[Pi]*((2*Erfi[((b + 2*c*x)*Sqrt[Log[f]])/(2*Sqrt[c])])/(Sqrt[c]*f^(b^2/(4*c))*Sqrt[Log[f]]) + ((-1)^(1/4)*E^((b^2*Log[f]^2)/((8*I)*f - 4*c*Log[f]))*(-(Erfi[((-1)^(3/4)*(4*f*x + I*(b + 2*c*x)*Log[f])]/(2*Sqrt[2*f + I*c*Log[f]])]*(2*f - I*c*Log[f])*Sqrt[2*f + I*c*Log[f]]*(Cos[2*d] - I*Sin[2*d])) + E^((I*b^2*f*Log[f]^2)/(4*f^2 + c^2*Log[f]^2))*Erfi[((-1)^(1/4)*(4*f*x - I*(b + 2*c*x)*Log[f])]/(2*Sqrt[2*f - I*c*Log[f]])]*Sqrt[2*f - I*c*Log[f]]*(2*f + I*c*Log[f])*(-I)*Cos[2*d] + Sin[2*d]))/(4*f^2 + c^2*Log[f]^2)))/8

fricas [B] time = 0.72, size = 400, normalized size = 1.63

$$\sqrt{\pi} (c^2 \log(f)^2 - 2icf \log(f)) \sqrt{-c \log(f) - 2if} \operatorname{erf}\left(\frac{(8f^2x - 2ibf \log(f) + (2c^2x + bc) \log(f)^2) \sqrt{-c \log(f) - 2if}}{2(c^2 \log(f)^2 + 4f^2)}\right) e^{\frac{16af^2 \log(f) - (b^2c - 4ac^2) \log(f)^3 + 32I*d*f^2 + (8*I*c^2*d + 2*I*b^2*f) \log(f)^2}{(c^2 \log(f)^2 + 4f^2)}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(c*x^2+b*x+a)*cos(f*x^2+d)^2,x, algorithm="fricas")

[Out] -1/8*(sqrt(pi)*(c^2*log(f)^2 - 2I*c*f*log(f))*sqrt(-c*log(f) - 2I*f)*erf(1/2*(8*f^2*x - 2*I*b*f*log(f) + (2*c^2*x + b*c)*log(f)^2)*sqrt(-c*log(f) - 2I*f)/(c^2*log(f)^2 + 4*f^2))*e^(1/4*(16*a*f^2*log(f) - (b^2*c - 4*a*c^2)*log(f)^3 + 32*I*d*f^2 + (8*I*c^2*d + 2*I*b^2*f)*log(f)^2)/(c^2*log(f)^2 + 4*f^2)) + sqrt(pi)*(c^2*log(f)^2 + 2I*c*f*log(f))*sqrt(-c*log(f) + 2I*f)*e^(1/4*(16*a*f^2*log(f) - (b^2*c - 4*a*c^2)*log(f)^3 + 32*I*d*f^2 + (8*I*c^2*d + 2*I*b^2*f)*log(f)^2)/(c^2*log(f)^2 + 4*f^2))

$$\frac{\operatorname{rf}\left(\frac{1}{2}\left(8f^2x + 2Ibf\log(f) + (2c^2x + bc)\log(f)^2\right)\sqrt{-c\log(f)} + 2If\right)}{\left(c^2\log(f)^2 + 4f^2\right)} e^{\frac{1}{4}\left(16a^2f^2\log(f) - (b^2c - 4a^2c^2)\log(f)^3 - 32Idf^2 + (-8Ic^2d - 2Ib^2f)\log(f)^2\right)} \frac{2\sqrt{\pi}\left(c^2\log(f)^2 + 4f^2\right)\sqrt{-c\log(f)}\operatorname{erf}\left(\frac{1}{2}\left(2cx + b\right)\sqrt{-c\log(f)}\right)/c}{f^{\frac{1}{4}\left(b^2 - 4ac\right)}/c} \frac{1}{\left(c^3\log(f)^3 + 4c^2f^2\log(f)\right)}$$

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int f^{cx^2+bx+a} \cos(fx^2 + d)^2 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(c*x^2+b*x+a)*cos(f*x^2+d)^2,x, algorithm="giac")

[Out] integrate(f^(c*x^2 + b*x + a)*cos(f*x^2 + d)^2, x)

maple [A] time = 0.31, size = 227, normalized size = 0.93

$$\frac{\sqrt{\pi} f^a e^{-\frac{\ln(f)^2 b^2 + 8id \ln(f) c + 16df}{4(-2if + c \ln(f))}} \operatorname{erf}\left(-x\sqrt{2if - c \ln(f)} + \frac{\ln(f)b}{2\sqrt{2if - c \ln(f)}}\right)}{8\sqrt{2if - c \ln(f)}} \frac{\sqrt{\pi} f^a e^{-\frac{\ln(f)^2 b^2 - 8id \ln(f) c + 16df}{4(2if + c \ln(f))}} \operatorname{erf}\left(-\sqrt{-2if - c \ln(f)}\right)}{8\sqrt{-2if - c \ln(f)}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(f^(c*x^2+b*x+a)*cos(f*x^2+d)^2,x)

[Out]
$$\frac{-1/8\pi^{1/2}f^a \exp(-1/4(\ln(f)^2 b^2 + 8Id \ln(f) c + 16df)) / (-2If + c \ln(f))^{1/2} \operatorname{erf}(-x(2If - c \ln(f))^{1/2} + 1/2 \ln(f) b / (2If - c \ln(f))^{1/2}) - 1/8\pi^{1/2}f^a \exp(-1/4(\ln(f)^2 b^2 - 8Id \ln(f) c + 16df)) / (2If + c \ln(f))^{1/2} \operatorname{erf}(-(-2If - c \ln(f))^{1/2} x + 1/2 \ln(f) b / (-2If - c \ln(f))^{1/2}) - 1/4\pi^{1/2}f^a f^{(-1/4 b^2/c)} / (-c \ln(f))^{1/2} \operatorname{erf}(-(-c \ln(f))^{1/2} x + 1/2 / (-c \ln(f))^{1/2} b \ln(f))}{8\sqrt{2if - c \ln(f)}} \frac{\sqrt{\pi} f^a e^{-\frac{\ln(f)^2 b^2 - 8id \ln(f) c + 16df}{4(2if + c \ln(f))}} \operatorname{erf}\left(-\sqrt{-2if - c \ln(f)}\right)}{8\sqrt{-2if - c \ln(f)}}$$

maxima [C] time = 0.38, size = 997, normalized size = 4.07

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(c*x^2+b*x+a)*cos(f*x^2+d)^2,x, algorithm="maxima")

[Out]
$$\frac{1}{16} \left(\sqrt{\pi} \sqrt{2c^2 \log(f)^2 + 8f^2} \left((If^a f^{1/4 b^2/c}) \cos\left(\frac{1}{2} \left(16d^2 f^2 + (4c^2 d + b^2 f) \log(f)^2 \right) / (c^2 \log(f)^2 + 4f^2) \right) + f^a f^{1/4 b^2/c} \sin\left(\frac{1}{2} \left(16d^2 f^2 + (4c^2 d + b^2 f) \log(f)^2 \right) / (c^2 \log(f)^2 + 4f^2) \right) \right) \operatorname{erf}\left(\frac{1}{2} \left(2(c \log(f) - 2If) x + b \log(f) \right) / \sqrt{-c \log(f) + 2If} \right) \right. \\ \left. + (-If^a f^{1/4 b^2/c}) \cos\left(\frac{1}{2} \left(16d^2 f^2 + (4c^2 d + b^2 f) \log(f)^2 \right) / (c^2 \log(f)^2 + 4f^2) \right) + f^a f^{1/4 b^2/c} \sin\left(\frac{1}{2} \left(16d^2 f^2 + (4c^2 d + b^2 f) \log(f)^2 \right) / (c^2 \log(f)^2 + 4f^2) \right) \right) \operatorname{erf}\left(\frac{1}{2} \left(2(c \log(f) + 2If) x + b \log(f) \right) / \sqrt{-c \log(f) - 2If} \right) \right) \sqrt{c \log(f) + \sqrt{c^2 \log(f)^2 + 4f^2}} \\ \left(\sqrt{-c \log(f)} - \sqrt{\pi} \sqrt{2c^2 \log(f)^2 + 8f^2} \left((f^a f^{1/4 b^2/c}) \cos\left(\frac{1}{2} \left(16d^2 f^2 + (4c^2 d + b^2 f) \log(f)^2 \right) / (c^2 \log(f)^2 + 4f^2) \right) \right. \right. \\ \left. \left. - If^a f^{1/4 b^2/c} \sin\left(\frac{1}{2} \left(16d^2 f^2 + (4c^2 d + b^2 f) \log(f)^2 \right) / (c^2 \log(f)^2 + 4f^2) \right) \right) \operatorname{erf}\left(\frac{1}{2} \left(2(c \log(f) - 2If) x + b \log(f) \right) / \sqrt{-c \log(f) + 2If} \right) \right. \\ \left. + (f^a f^{1/4 b^2/c}) \cos\left(\frac{1}{2} \left(16d^2 f^2 + (4c^2 d + b^2 f) \log(f)^2 \right) / (c^2 \log(f)^2 + 4f^2) \right) + If^a f^{1/4 b^2/c} \sin\left(\frac{1}{2} \left(16d^2 f^2 + (4c^2 d + b^2 f) \log(f)^2 \right) / (c^2 \log(f)^2 + 4f^2) \right) \right) \operatorname{erf}\left(\frac{1}{2} \left(2(c \log(f) + 2If) x + b \log(f) \right) / \sqrt{-c \log(f) - 2If} \right) \right) \sqrt{-c \log(f) + \sqrt{c^2 \log(f)^2 + 4f^2}} \\ \left(\sqrt{-c \log(f)} + 2\sqrt{\pi} \left((c^2 f^a e^{1/4 b^2 c \log(f)})^3 / (c^2 \log(f)^2 + 4f^2) \right) \log(f)^2 + 4f^{\ln(f)} \right) e^{1/4 b^2 c \log(f)} \sqrt{c^2 \log(f)^2 + 4f^2} \right) \operatorname{erf}\left(-\frac{1}{2} b \operatorname{conjugate}\left(\frac{1}{\sqrt{-c \log(f)}}\right)\right) \log(f) + x^c$$

```
onjugate(sqrt(-c*log(f)))) - (c^2*f^a*e^(1/4*b^2*c*log(f)^3/(c^2*log(f)^2 +
4*f^2))*log(f)^2 + 4*f^(a + 2)*e^(1/4*b^2*c*log(f)^3/(c^2*log(f)^2 + 4*f^2
)))*erf(1/2*(2*c*x*log(f) + b*log(f))/sqrt(-c*log(f))))/((c^2*e^(1/4*b^2*c
*log(f)^3/(c^2*log(f)^2 + 4*f^2) + 1/4*b^2*log(f)/c)*log(f)^2 + 4*f^2*e^(1/
4*b^2*c*log(f)^3/(c^2*log(f)^2 + 4*f^2) + 1/4*b^2*log(f)/c))*sqrt(-c*log(f)
))
```

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int f^{cx^2+bx+a} \cos(fx^2+d)^2 dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(f^(a + b*x + c*x^2)*cos(d + f*x^2)^2,x)
```

```
[Out] int(f^(a + b*x + c*x^2)*cos(d + f*x^2)^2, x)
```

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int f^{a+bx+cx^2} \cos^2(d + fx^2) dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(f**(c*x**2+b*x+a)*cos(f*x**2+d)**2,x)
```

```
[Out] Integral(f**(a + b*x + c*x**2)*cos(d + f*x**2)**2, x)
```


x] && LeQ[Exponent[z, x], 2]]) /; FreeQ[{F, G}, x]

Rule 4473

Int[Cos[v_]^(n_.)*(F_)^(u_), x_Symbol] := Int[ExpandTrigToExp[F^u, Cos[v]^n, x], x] /; FreeQ[F, x] && (LinearQ[u, x] || PolyQ[u, x, 2]) && (LinearQ[v, x] || PolyQ[v, x, 2]) && IGtQ[n, 0]

Rubi steps

$$\begin{aligned} \int f^{a+bx+cx^2} \cos^3(d+fx^2) dx &= \int \left(\frac{3}{8} e^{-id-ifx^2} f^{a+bx+cx^2} + \frac{3}{8} e^{id+ifx^2} f^{a+bx+cx^2} + \frac{1}{8} e^{-3id-3ifx^2} f^{a+bx+cx^2} + \frac{1}{8} e^{3id+3ifx^2} f^{a+bx+cx^2} \right) dx \\ &= \frac{1}{8} \int e^{-3id-3ifx^2} f^{a+bx+cx^2} dx + \frac{1}{8} \int e^{3id+3ifx^2} f^{a+bx+cx^2} dx + \frac{3}{8} \int e^{-id-ifx^2} f^{a+bx+cx^2} dx \\ &= \frac{1}{8} \int \exp(-3id + a \log(f) + bx \log(f) - x^2(3if - c \log(f))) dx + \frac{1}{8} \int \exp(3id + a \log(f) + bx \log(f) - x^2(3if - c \log(f))) dx \\ &= \frac{1}{8} \left(3e^{-id + \frac{b^2 \log^2(f)}{4if - 4c \log(f)}} f^a \right) \int \exp\left(\frac{(b \log(f) + 2x(-if + c \log(f)))^2}{4(-if + c \log(f))}\right) dx + \frac{1}{8} \left(e^{-3id + \frac{b^2 \log^2(f)}{4if - 4c \log(f)}} f^a \right) \int \exp\left(\frac{(b \log(f) + 2x(-if + c \log(f)))^2}{4(-if + c \log(f))}\right) dx \\ &= -\frac{3e^{-id + \frac{b^2 \log^2(f)}{4if - 4c \log(f)}} f^a \sqrt{\pi} \operatorname{erf}\left(\frac{b \log(f) - 2x(if - c \log(f))}{2\sqrt{if - c \log(f)}}\right)}{16\sqrt{if - c \log(f)}} - \frac{e^{-3id + \frac{b^2 \log^2(f)}{12if - 4c \log(f)}} f^a \sqrt{\pi} \operatorname{erf}\left(\frac{b \log(f) - 2x(if - c \log(f))}{2\sqrt{3if - c \log(f)}}\right)}{16\sqrt{3if - c \log(f)}} \end{aligned}$$

Mathematica [B] time = 7.00, size = 3285, normalized size = 8.69

Result too large to show

Antiderivative was successfully verified.

[In] Integrate[f^(a + b*x + c*x^2)*Cos[d + f*x^2]^3,x]

[Out] (f^a*Sqrt[Pi]*(-27*(-1)^(3/4)*E^(((I/4)*b^2*Log[f]^2)/(f - I*c*Log[f])))*f^3 *Cos[d]*Erfi[(((-1)^(1/4)*(2*f*x - I*b*Log[f] - (2*I)*c*x*Log[f]))/(2*Sqrt[f - I*c*Log[f]]))]*Sqrt[f - I*c*Log[f]] + 27*(-1)^(1/4)*c*E^(((I/4)*b^2*Log[f]^2)/(f - I*c*Log[f]))*f^2 *Cos[d]*Erfi[(((-1)^(1/4)*(2*f*x - I*b*Log[f] - (2*I)*c*x*Log[f]))/(2*Sqrt[f - I*c*Log[f]]))]*Log[f]*Sqrt[f - I*c*Log[f]] - 3*(-1)^(3/4)*c^2 *E^(((I/4)*b^2*Log[f]^2)/(f - I*c*Log[f]))*f *Cos[d]*Erfi[(((-1)^(1/4)*(2*f*x - I*b*Log[f] - (2*I)*c*x*Log[f]))/(2*Sqrt[f - I*c*Log[f]]))]*Log[f]^2 *Sqrt[f - I*c*Log[f]] + 3*(-1)^(1/4)*c^3 *E^(((I/4)*b^2*Log[f]^2)/(f - I*c*Log[f])) *Cos[d]*Erfi[(((-1)^(1/4)*(2*f*x - I*b*Log[f] - (2*I)*c*x*Log[f]))/(2*Sqrt[f - I*c*Log[f]]))]*Log[f]^3 *Sqrt[f - I*c*Log[f]] - 3*(-1)^(3/4) *E^(((I/4)*b^2*Log[f]^2)/(3*f - I*c*Log[f]))*f^3 *Cos[3*d]*Erfi[(((-1)^(1/4) * (6*f*x - I*b*Log[f] - (2*I)*c*x*Log[f]))/(2*Sqrt[3*f - I*c*Log[f]]))]*Sqrt[3*f - I*c*Log[f]] + (-1)^(1/4)*c *E^(((I/4)*b^2*Log[f]^2)/(3*f - I*c*Log[f])) *f^2 *Cos[3*d]*Erfi[(((-1)^(1/4)*(6*f*x - I*b*Log[f] - (2*I)*c*x*Log[f]))/(2 *Sqrt[3*f - I*c*Log[f]]))]*Log[f]*Sqrt[3*f - I*c*Log[f]] - 3*(-1)^(3/4) *E^(((I/4)*b^2*Log[f]^2)/(3*f - I*c*Log[f]))*f *Cos[3*d]*Erfi[(((-1)^(1/4) * (6*f*x - I*b*Log[f] - (2*I)*c*x*Log[f]))/(2*Sqrt[3*f - I*c*Log[f]]))]*Log[f]^2 *Sqrt[3*f - I*c*Log[f]] + (-1)^(1/4)*c^3 *E^(((I/4)*b^2*Log[f]^2)/(3*f - I*c*Log[f])) *Cos[3*d]*Erfi[(((-1)^(1/4)*(6*f*x - I*b*Log[f] - (2*I)*c*x*Log[f]))/(2*Sqrt[3*f - I*c*Log[f]]))]*Log[f]^3 *Sqrt[3*f - I*c*Log[f]] - (27*(-1)^(1/4) *f^3 *Cos[d]*Erfi[(((-1)^(3/4)*(2*f*x + I*b*Log[f] + (2*I)*c*x*Log[f]))/(2 *Sqrt[f + I*c*Log[f]]))]*Sqrt[f + I*c*Log[f]])/E^(((I/4)*b^2*Log[f]^2)/(f + I *c*Log[f])) + (27*(-1)^(3/4)*c*f^2 *Cos[d]*Erfi[(((-1)^(3/4)*(2*f*x + I*b*Log[f] + (2*I)*c*x*Log[f]))/(2*Sqrt[f + I*c*Log[f]]))]*Log[f]*Sqrt[f + I*c*Log[f]])/E^(((I/4)*b^2*Log[f]^2)/(f + I*c*Log[f])) - (3*(-1)^(1/4)*c^2 *f *Cos[d]

fricas [B] time = 0.93, size = 723, normalized size = 1.91

$$\frac{\sqrt{\pi} \left(c^3 \log(f)^3 - 3ic^2f \log(f)^2 + cf^2 \log(f) - 3if^3 \right) \sqrt{-c \log(f) - 3if} \operatorname{erf} \left(\frac{(18f^2x - 3ibf \log(f) + (2c^2x + bc) \log(f)^2) \sqrt{-c}}{2(c^2 \log(f)^2 + 9f^2)} \right)}{1}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(c*x^2+b*x+a)*cos(f*x^2+d)^3,x, algorithm="fricas")

[Out] -1/16*(sqrt(pi)*(c^3*log(f)^3 - 3I*c^2*f*log(f)^2 + c*f^2*log(f) - 3I*f^3)*sqrt(-c*log(f) - 3I*f)*erf(1/2*(18*f^2*x - 3I*b*f*log(f) + (2*c^2*x + b*c)*log(f)^2)*sqrt(-c*log(f) - 3I*f)/(c^2*log(f)^2 + 9*f^2))*e^(1/4*(36*a*f^2*log(f) - (b^2*c - 4*a*c^2)*log(f)^3 + 108*I*d*f^2 + (12*I*c^2*d + 3*I*b^2*f)*log(f)^2)/(c^2*log(f)^2 + 9*f^2)) + sqrt(pi)*(c^3*log(f)^3 + 3I*c^2*f*log(f)^2 + c*f^2*log(f) + 3I*f^3)*sqrt(-c*log(f) + 3I*f)*erf(1/2*(18*f^2*x + 3I*b*f*log(f) + (2*c^2*x + b*c)*log(f)^2)*sqrt(-c*log(f) + 3I*f)/(c^2*log(f)^2 + 9*f^2))*e^(1/4*(36*a*f^2*log(f) - (b^2*c - 4*a*c^2)*log(f)^3 - 108*I*d*f^2 + (-12*I*c^2*d - 3*I*b^2*f)*log(f)^2)/(c^2*log(f)^2 + 9*f^2)) + sqrt(pi)*(3*c^3*log(f)^3 - 3I*c^2*f*log(f)^2 + 27*c*f^2*log(f) - 27*I*f^3)*sqrt(-c*log(f) - I*f)*erf(1/2*(2*f^2*x - I*b*f*log(f) + (2*c^2*x + b*c)*log(f)^2)*sqrt(-c*log(f) - I*f)/(c^2*log(f)^2 + f^2))*e^(1/4*(4*a*f^2*log(f) - (b^2*c - 4*a*c^2)*log(f)^3 + 4*I*d*f^2 + (4*I*c^2*d + I*b^2*f)*log(f)^2)/(c^2*log(f)^2 + f^2)) + sqrt(pi)*(3*c^3*log(f)^3 + 3I*c^2*f*log(f)^2 + 27*c*f^2*log(f) + 27*I*f^3)*sqrt(-c*log(f) + I*f)*erf(1/2*(2*f^2*x + I*b*f*log(f) + (2*c^2*x + b*c)*log(f)^2)*sqrt(-c*log(f) + I*f)/(c^2*log(f)^2 + f^2))*e^(1/4*(4*a*f^2*log(f) - (b^2*c - 4*a*c^2)*log(f)^3 - 4*I*d*f^2 + (-4*I*c^2*d - I*b^2*f)*log(f)^2)/(c^2*log(f)^2 + f^2)))/(c^4*log(f)^4 + 10*c^2*f^2*log(f)^2 + 9*f^4)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int f^{cx^2+bx+a} \cos(fx^2+d)^3 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(c*x^2+b*x+a)*cos(f*x^2+d)^3,x, algorithm="giac")

[Out] integrate(f^(c*x^2 + b*x + a)*cos(f*x^2 + d)^3, x)

maple [A] time = 0.70, size = 354, normalized size = 0.94

$$\frac{\sqrt{\pi} f^a e^{\frac{\ln(f)^2 b^2 + 12id \ln(f) c + 36df}{4(-3if + c \ln(f))}} \operatorname{erf} \left(-x \sqrt{3if - c \ln(f)} + \frac{\ln(f)b}{2\sqrt{3if - c \ln(f)}} \right)}{16\sqrt{3if - c \ln(f)}} \frac{3\sqrt{\pi} f^a e^{\frac{4df + 4id \ln(f) c + \ln(f)^2 b^2}{4(-if + c \ln(f))}} \operatorname{erf} \left(-x \sqrt{if - c \ln(f)} \right)}{16\sqrt{if - c \ln(f)}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(f^(c*x^2+b*x+a)*cos(f*x^2+d)^3,x)

[Out] -1/16*Pi^(1/2)*f^a*exp(-1/4*(ln(f)^2*b^2+12*I*d*ln(f)*c+36*d*f)/(-3*I*f+c*ln(f)))/(3*I*f-c*ln(f))^(1/2)*erf(-x*(3*I*f-c*ln(f))^(1/2)+1/2*ln(f)*b/(3*I*f-c*ln(f))^(1/2))-3/16*Pi^(1/2)*f^a*exp(-1/4*(4*d*f+4*I*d*ln(f)*c+ln(f)^2*b^2)/(-I*f+c*ln(f)))/(I*f-c*ln(f))^(1/2)*erf(-x*(I*f-c*ln(f))^(1/2)+1/2*ln(f)*b/(I*f-c*ln(f))^(1/2))-3/16*Pi^(1/2)*f^a*exp(-1/4*(4*d*f-4*I*d*ln(f)*c+ln(f)^2*b^2)/(I*f+c*ln(f)))/(-I*f-c*ln(f))^(1/2)*erf(-(-I*f-c*ln(f))^(1/2)*x+1/2*ln(f)*b/(-I*f-c*ln(f))^(1/2))-1/16*Pi^(1/2)*f^a*exp(-1/4*(ln(f)^2*b^2-12*I*d*ln(f)*c+36*d*f)/(3*I*f+c*ln(f)))/(-c*ln(f)-3*I*f)^(1/2)*erf(-(-c*ln(f)-3*I*f)^(1/2)*x+1/2*ln(f)*b/(-c*ln(f)-3*I*f)^(1/2))

maxima [B] time = 0.42, size = 2459, normalized size = 6.51

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate($f^{(c*x^2+b*x+a)}*\cos(f*x^2+d)^3,x$, algorithm="maxima")

[Out] $\frac{1}{32}*\sqrt{\pi}*\sqrt{2*c^2*\log(f)^2 + 18*f^2}*\left(\left(I*c^2*f^a*e^{(1/4*b^2*c*\log(f)^3/(c^2*\log(f)^2 + f^2))*\log(f)^2 + I*f^{(a + 2)}*e^{(1/4*b^2*c*\log(f)^3/(c^2*\log(f)^2 + f^2))}\right)*\cos\left(\frac{3/4*(36*d*f^2 + (4*c^2*d + b^2*f)*\log(f)^2)}{(c^2*\log(f)^2 + 9*f^2)}\right) + (c^2*f^a*e^{(1/4*b^2*c*\log(f)^3/(c^2*\log(f)^2 + f^2))*\log(f)^2 + f^{(a + 2)}*e^{(1/4*b^2*c*\log(f)^3/(c^2*\log(f)^2 + f^2))}\right)*\sin\left(\frac{3/4*(36*d*f^2 + (4*c^2*d + b^2*f)*\log(f)^2)}{(c^2*\log(f)^2 + 9*f^2)}\right)*\operatorname{erf}\left(\frac{1/2*(2*(c*\log(f) - 3*I*f)*x + b*\log(f))}{\sqrt{-c*\log(f) + 3*I*f}}\right) + \left(-I*c^2*f^a*e^{(1/4*b^2*c*\log(f)^3/(c^2*\log(f)^2 + f^2))*\log(f)^2 - I*f^{(a + 2)}*e^{(1/4*b^2*c*\log(f)^3/(c^2*\log(f)^2 + f^2))}\right)*\cos\left(\frac{3/4*(36*d*f^2 + (4*c^2*d + b^2*f)*\log(f)^2)}{(c^2*\log(f)^2 + 9*f^2)}\right) + (c^2*f^a*e^{(1/4*b^2*c*\log(f)^3/(c^2*\log(f)^2 + f^2))*\log(f)^2 + f^{(a + 2)}*e^{(1/4*b^2*c*\log(f)^3/(c^2*\log(f)^2 + f^2))}\right)*\sin\left(\frac{3/4*(36*d*f^2 + (4*c^2*d + b^2*f)*\log(f)^2)}{(c^2*\log(f)^2 + 9*f^2)}\right)*\operatorname{erf}\left(\frac{1/2*(2*(c*\log(f) + 3*I*f)*x + b*\log(f))}{\sqrt{-c*\log(f) - 3*I*f}}\right)*\sqrt{c*\log(f) + \sqrt{c^2*\log(f)^2 + 9*f^2}} + \sqrt{\pi}*\sqrt{2*c^2*\log(f)^2 + 2*f^2}\right)*\left(\left(3*I*c^2*f^a*e^{(1/4*b^2*c*\log(f)^3/(c^2*\log(f)^2 + 9*f^2))*\log(f)^2 + 2*7*I*f^{(a + 2)}*e^{(1/4*b^2*c*\log(f)^3/(c^2*\log(f)^2 + 9*f^2))}\right)*\cos\left(\frac{1/4*(4*d*f^2 + (4*c^2*d + b^2*f)*\log(f)^2)}{(c^2*\log(f)^2 + f^2)}\right) + 3*(c^2*f^a*e^{(1/4*b^2*c*\log(f)^3/(c^2*\log(f)^2 + 9*f^2))*\log(f)^2 + 9*f^{(a + 2)}*e^{(1/4*b^2*c*\log(f)^3/(c^2*\log(f)^2 + 9*f^2))}\right)*\sin\left(\frac{1/4*(4*d*f^2 + (4*c^2*d + b^2*f)*\log(f)^2)}{(c^2*\log(f)^2 + f^2)}\right)*\operatorname{erf}\left(\frac{1/2*(2*(c*\log(f) - I*f)*x + b*\log(f))}{\sqrt{-c*\log(f) + I*f}}\right) + \left(-3*I*c^2*f^a*e^{(1/4*b^2*c*\log(f)^3/(c^2*\log(f)^2 + 9*f^2))*\log(f)^2 - 27*I*f^{(a + 2)}*e^{(1/4*b^2*c*\log(f)^3/(c^2*\log(f)^2 + 9*f^2))}\right)*\cos\left(\frac{1/4*(4*d*f^2 + (4*c^2*d + b^2*f)*\log(f)^2)}{(c^2*\log(f)^2 + f^2)}\right) + 3*(c^2*f^a*e^{(1/4*b^2*c*\log(f)^3/(c^2*\log(f)^2 + 9*f^2))*\log(f)^2 + 9*f^{(a + 2)}*e^{(1/4*b^2*c*\log(f)^3/(c^2*\log(f)^2 + 9*f^2))}\right)*\sin\left(\frac{1/4*(4*d*f^2 + (4*c^2*d + b^2*f)*\log(f)^2)}{(c^2*\log(f)^2 + f^2)}\right)*\operatorname{erf}\left(\frac{1/2*(2*(c*\log(f) + I*f)*x + b*\log(f))}{\sqrt{-c*\log(f) - I*f}}\right)*\sqrt{c*\log(f) + \sqrt{c^2*\log(f)^2 + f^2}} - \sqrt{\pi}*\sqrt{2*c^2*\log(f)^2 + 18*f^2}\right)*\left(\left(c^2*f^a*e^{(1/4*b^2*c*\log(f)^3/(c^2*\log(f)^2 + f^2))*\log(f)^2 + f^{(a + 2)}*e^{(1/4*b^2*c*\log(f)^3/(c^2*\log(f)^2 + f^2))}\right)*\cos\left(\frac{3/4*(36*d*f^2 + (4*c^2*d + b^2*f)*\log(f)^2)}{(c^2*\log(f)^2 + 9*f^2)}\right) - (I*c^2*f^a*e^{(1/4*b^2*c*\log(f)^3/(c^2*\log(f)^2 + f^2))*\log(f)^2 + I*f^{(a + 2)}*e^{(1/4*b^2*c*\log(f)^3/(c^2*\log(f)^2 + f^2))}\right)*\sin\left(\frac{3/4*(36*d*f^2 + (4*c^2*d + b^2*f)*\log(f)^2)}{(c^2*\log(f)^2 + 9*f^2)}\right)*\operatorname{erf}\left(\frac{1/2*(2*(c*\log(f) - 3*I*f)*x + b*\log(f))}{\sqrt{-c*\log(f) + 3*I*f}}\right) + \left((c^2*f^a*e^{(1/4*b^2*c*\log(f)^3/(c^2*\log(f)^2 + f^2))*\log(f)^2 + f^{(a + 2)}*e^{(1/4*b^2*c*\log(f)^3/(c^2*\log(f)^2 + f^2))}\right)*\cos\left(\frac{3/4*(36*d*f^2 + (4*c^2*d + b^2*f)*\log(f)^2)}{(c^2*\log(f)^2 + 9*f^2)}\right) - (-I*c^2*f^a*e^{(1/4*b^2*c*\log(f)^3/(c^2*\log(f)^2 + f^2))*\log(f)^2 - I*f^{(a + 2)}*e^{(1/4*b^2*c*\log(f)^3/(c^2*\log(f)^2 + f^2))}\right)*\sin\left(\frac{3/4*(36*d*f^2 + (4*c^2*d + b^2*f)*\log(f)^2)}{(c^2*\log(f)^2 + 9*f^2)}\right)*\operatorname{erf}\left(\frac{1/2*(2*(c*\log(f) + 3*I*f)*x + b*\log(f))}{\sqrt{-c*\log(f) - 3*I*f}}\right)*\sqrt{-c*\log(f) + \sqrt{c^2*\log(f)^2 + 9*f^2}} - \sqrt{\pi}*\sqrt{2*c^2*\log(f)^2 + 2*f^2}\right)*\left(\left(3*(c^2*f^a*e^{(1/4*b^2*c*\log(f)^3/(c^2*\log(f)^2 + 9*f^2))*\log(f)^2 + 9*f^{(a + 2)}*e^{(1/4*b^2*c*\log(f)^3/(c^2*\log(f)^2 + 9*f^2))}\right)*\cos\left(\frac{1/4*(4*d*f^2 + (4*c^2*d + b^2*f)*\log(f)^2)}{(c^2*\log(f)^2 + f^2)}\right) - (3*I*c^2*f^a*e^{(1/4*b^2*c*\log(f)^3/(c^2*\log(f)^2 + 9*f^2))*\log(f)^2 + 27*I*f^{(a + 2)}*e^{(1/4*b^2*c*\log(f)^3/(c^2*\log(f)^2 + 9*f^2))}\right)*\sin\left(\frac{1/4*(4*d*f^2 + (4*c^2*d + b^2*f)*\log(f)^2)}{(c^2*\log(f)^2 + f^2)}\right)*\operatorname{erf}\left(\frac{1/2*(2*(c*\log(f) - I*f)*x + b*\log(f))}{\sqrt{-c*\log(f) + I*f}}\right) + (3*(c^2*f^a*e^{(1/4*b^2*c*\log(f)^3/(c^2*\log(f)^2 + 9*f^2))*\log(f)^2 + 9*f^{(a + 2)}*e^{(1/4*b^2*c*\log(f)^3/(c^2*\log(f)^2 + 9*f^2))}\right)*\cos\left(\frac{1/4*(4*d*f^2 + (4*c^2*d + b^2*f)*\log(f)^2)}{(c^2*\log(f)^2 + f^2)}\right) - (-3*I*c^2*f^a*e^{(1/4*b^2*c*\log(f)^3/(c^2*\log(f)^2 + 9*f^2))*\log(f)^2 - 27*I*f^{(a + 2)}*e^{(1/4*b^2*c*\log(f)^3/(c^2*\log(f)^2 + 9*f^2))}\right)*\sin\left(\frac{1/4*(4*d*f^2 +$

```
(4*c^2*d + b^2*f)*log(f)^2)/(c^2*log(f)^2 + f^2))*erf(1/2*(2*(c*log(f) + I
*f)*x + b*log(f))/sqrt(-c*log(f) - I*f)))*sqrt(-c*log(f) + sqrt(c^2*log(f)^
2 + f^2)))/(c^4*e^(1/4*b^2*c*log(f)^3/(c^2*log(f)^2 + 9*f^2) + 1/4*b^2*c*lo
g(f)^3/(c^2*log(f)^2 + f^2))*log(f)^4 + 10*c^2*f^2*e^(1/4*b^2*c*log(f)^3/(c
^2*log(f)^2 + 9*f^2) + 1/4*b^2*c*log(f)^3/(c^2*log(f)^2 + f^2))*log(f)^2 +
9*f^4*e^(1/4*b^2*c*log(f)^3/(c^2*log(f)^2 + 9*f^2) + 1/4*b^2*c*log(f)^3/(c^
2*log(f)^2 + f^2)))
```

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int f^{cx^2+bx+a} \cos(fx^2+d)^3 dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(f^(a + b*x + c*x^2)*cos(d + f*x^2)^3,x)
```

```
[Out] int(f^(a + b*x + c*x^2)*cos(d + f*x^2)^3, x)
```

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(f**(c*x**2+b*x+a)*cos(f*x**2+d)**3,x)
```

```
[Out] Timed out
```

3.131 $\int f^{a+bx+cx^2} \cos(d+ex+fx^2) dx$

Optimal. Leaf size=208

$$\frac{\sqrt{\pi} f^a \exp\left(-\frac{(e+ib \log(f))^2}{-4c \log(f)+4if} - id\right) \operatorname{erf}\left(\frac{-b \log(f)+2x(-c \log(f)+if)+ie}{2\sqrt{-c \log(f)+if}}\right)}{4\sqrt{-c \log(f)+if}} + \frac{\sqrt{\pi} f^a \exp\left(\frac{(e-ib \log(f))^2}{4c \log(f)+4if} + id\right) \operatorname{erfi}\left(\frac{b \log(f)+2x(c \log(f)+if)+ie}{2\sqrt{c \log(f)+if}}\right)}{4\sqrt{c \log(f)+if}}$$

[Out] $1/4*\exp(-I*d-(e+I*b*\ln(f))^2/(4*I*f-4*c*\ln(f)))*f^a*\operatorname{erf}(1/2*(I*e-b*\ln(f)+2*x*(I*f-c*\ln(f)))/(I*f-c*\ln(f)))^{(1/2)}*\operatorname{Pi}^{(1/2)}/(I*f-c*\ln(f))^{(1/2)}+1/4*\exp(I*d+(e-I*b*\ln(f))^2/(4*I*f+4*c*\ln(f)))*f^a*\operatorname{erfi}(1/2*(I*e+b*\ln(f)+2*x*(I*f+c*\ln(f)))/(I*f+c*\ln(f)))^{(1/2)}*\operatorname{Pi}^{(1/2)}/(I*f+c*\ln(f))^{(1/2)}$

Rubi [A] time = 0.39, antiderivative size = 208, normalized size of antiderivative = 1.00, number of steps used = 8, number of rules used = 5, integrand size = 24, $\frac{\text{number of rules}}{\text{integrand size}} = 0.208$, Rules used = {4473, 2287, 2234, 2205, 2204}

$$\frac{\sqrt{\pi} f^a \exp\left(-\frac{(e+ib \log(f))^2}{-4c \log(f)+4if} - id\right) \operatorname{Erf}\left(\frac{-b \log(f)+2x(-c \log(f)+if)+ie}{2\sqrt{-c \log(f)+if}}\right)}{4\sqrt{-c \log(f)+if}} + \frac{\sqrt{\pi} f^a \exp\left(\frac{(e-ib \log(f))^2}{4c \log(f)+4if} + id\right) \operatorname{Erfi}\left(\frac{b \log(f)+2x(c \log(f)+if)+ie}{2\sqrt{c \log(f)+if}}\right)}{4\sqrt{c \log(f)+if}}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[f^{(a + b*x + c*x^2)}*\operatorname{Cos}[d + e*x + f*x^2], x]$

[Out] $(E^{((-I)*d - (e + I*b*\operatorname{Log}[f])^2/((4*I)*f - 4*c*\operatorname{Log}[f]))}*f^a*\operatorname{Sqrt}[\operatorname{Pi}]*\operatorname{Erf}[(I*e - b*\operatorname{Log}[f] + 2*x*(I*f - c*\operatorname{Log}[f]))/(2*\operatorname{Sqrt}[I*f - c*\operatorname{Log}[f]])])/(4*\operatorname{Sqrt}[I*f - c*\operatorname{Log}[f]]) + (E^{(I*d + (e - I*b*\operatorname{Log}[f])^2/((4*I)*f + 4*c*\operatorname{Log}[f]))}*f^a*\operatorname{Sqrt}[\operatorname{Pi}]*\operatorname{Erfi}[(I*e + b*\operatorname{Log}[f] + 2*x*(I*f + c*\operatorname{Log}[f]))/(2*\operatorname{Sqrt}[I*f + c*\operatorname{Log}[f]])])/(4*\operatorname{Sqrt}[I*f + c*\operatorname{Log}[f]])$

Rule 2204

$\operatorname{Int}[(F_)^{((a_.) + (b_.)*((c_.) + (d_.)*(x_.))^2)}, x_Symbol] \rightarrow \operatorname{Simp}[(F^a*\operatorname{Sqrt}[\operatorname{Pi}]*\operatorname{Erfi}[(c + d*x)*\operatorname{Rt}[b*\operatorname{Log}[F], 2]])/(2*d*\operatorname{Rt}[b*\operatorname{Log}[F], 2]), x] /; \operatorname{FreeQ}\{F, a, b, c, d\}, x] \&\& \operatorname{PosQ}[b]$

Rule 2205

$\operatorname{Int}[(F_)^{((a_.) + (b_.)*((c_.) + (d_.)*(x_.))^2)}, x_Symbol] \rightarrow \operatorname{Simp}[(F^a*\operatorname{Sqrt}[\operatorname{Pi}]*\operatorname{Erf}[(c + d*x)*\operatorname{Rt}[-(b*\operatorname{Log}[F]), 2]])/(2*d*\operatorname{Rt}[-(b*\operatorname{Log}[F]), 2]), x] /; \operatorname{FreeQ}\{F, a, b, c, d\}, x] \&\& \operatorname{NegQ}[b]$

Rule 2234

$\operatorname{Int}[(F_)^{((a_.) + (b_.)*(x_.) + (c_.)*(x_.)^2)}, x_Symbol] \rightarrow \operatorname{Dist}[F^{(a - b^2/(4*c))}, \operatorname{Int}[F^{((b + 2*c*x)^2/(4*c))}, x], x] /; \operatorname{FreeQ}\{F, a, b, c\}, x]$

Rule 2287

$\operatorname{Int}[(u_.)*(F_)^{(v_.)*(G_)^{(w_.)}}, x_Symbol] \rightarrow \operatorname{With}\{z = v*\operatorname{Log}[F] + w*\operatorname{Log}[G]\}, \operatorname{Int}[u*\operatorname{NormalizeIntegrand}[E^z, x], x] /; \operatorname{BinomialQ}[z, x] \mid\mid (\operatorname{PolynomialQ}[z, x] \&\& \operatorname{LeQ}[\operatorname{Exponent}[z, x], 2]) /; \operatorname{FreeQ}\{F, G\}, x]$

Rule 4473

$\operatorname{Int}[\operatorname{Cos}[v_]^{(n_.)}*(F_)^{(u_.)}, x_Symbol] \rightarrow \operatorname{Int}[\operatorname{ExpandTrigToExp}[F^u, \operatorname{Cos}[v]^{(n)}, x], x] /; \operatorname{FreeQ}[F, x] \&\& (\operatorname{LinearQ}[u, x] \mid\mid \operatorname{PolyQ}[u, x, 2]) \&\& (\operatorname{LinearQ}[v, x] \mid\mid \operatorname{PolyQ}[v, x, 2]) \&\& \operatorname{IGtQ}[n, 0]$

Rubi steps

$$\begin{aligned}
\int f^{a+bx+cx^2} \cos(d+ex+fx^2) dx &= \int \left(\frac{1}{2} e^{-id-iex-ifx^2} f^{a+bx+cx^2} + \frac{1}{2} e^{id+iex+ifx^2} f^{a+bx+cx^2} \right) dx \\
&= \frac{1}{2} \int e^{-id-iex-ifx^2} f^{a+bx+cx^2} dx + \frac{1}{2} \int e^{id+iex+ifx^2} f^{a+bx+cx^2} dx \\
&= \frac{1}{2} \int \exp(-id+a \log(f)-x(ie-b \log(f))-x^2(if-c \log(f))) dx + \frac{1}{2} \int e^{id+ix+ifx^2} f^{a+bx+cx^2} dx \\
&= \frac{1}{2} \left(\exp\left(-id - \frac{(e+ib \log(f))^2}{4if-4c \log(f)}\right) f^a \int \exp\left(\frac{(-ie+b \log(f)+2x(-if+c \log(f)))}{4(-if+c \log(f))}\right) dx \right. \\
&\quad \left. + \exp\left(-id - \frac{(e+ib \log(f))^2}{4if-4c \log(f)}\right) f^a \sqrt{\pi} \operatorname{erf}\left(\frac{ie-b \log(f)+2x(if-c \log(f))}{2\sqrt{if-c \log(f)}}\right) \right) \\
&= \frac{\exp\left(-id - \frac{(e+ib \log(f))^2}{4if-4c \log(f)}\right) f^a \sqrt{\pi} \operatorname{erf}\left(\frac{ie-b \log(f)+2x(if-c \log(f))}{2\sqrt{if-c \log(f)}}\right)}{4\sqrt{if-c \log(f)}} + \frac{\exp\left(id + \frac{(e-ib \log(f))^2}{4if-4c \log(f)}\right) f^a \sqrt{\pi} \operatorname{erf}\left(\frac{-ie+b \log(f)+2x(-if+c \log(f))}{2\sqrt{-if+c \log(f)}}\right)}{4\sqrt{-if+c \log(f)}}
\end{aligned}$$

Mathematica [A] time = 2.10, size = 348, normalized size = 1.67

$$\sqrt[4]{-1} \sqrt{\pi} f^{\frac{f(af-be)+ac^2 \log^2(f)}{c^2 \log^2(f)+f^2}} \exp\left(-\frac{1}{4} i \left(\frac{b^2 \log^2(f)}{f+ic \log(f)} + \frac{e^2}{f-ic \log(f)}\right)\right) \left(\sqrt{f-ic \log(f)} (f+ic \log(f)) (\sin(d) - i \cos(d)) e^{\frac{ib^2 \log^2(f)}{2(c^2 \log^2(f)+f^2)}} \right)$$

Warning: Unable to verify antiderivative.

[In] Integrate[f^(a + b*x + c*x^2)*Cos[d + e*x + f*x^2], x]

[Out] $((-1)^{1/4} f^{((f*(-(b*e) + a*f) + a*c^2*Log[f]^2)/(f^2 + c^2*Log[f]^2))} * \operatorname{Sqrt}[\pi] * (-E^{(((I/2)*e^2*f)/(f^2 + c^2*Log[f]^2))} * f^{((b*e)/(2*f - (2*I)*c*Log[f])} * \operatorname{Erfi}[((-1)^{3/4}*(e + 2*f*x + I*(b + 2*c*x)*Log[f]))/(2*\operatorname{Sqrt}[f + I*c*Log[f]])] * (f - I*c*Log[f]) * \operatorname{Sqrt}[f + I*c*Log[f]] * (\operatorname{Cos}[d] - I*\operatorname{Sin}[d])) + E^{(((I/2)*b^2*f*Log[f]^2)/(f^2 + c^2*Log[f]^2))} * f^{((b*e)/(2*f + (2*I)*c*Log[f])} * \operatorname{Erfi}[((-1)^{1/4}*(e + 2*f*x - I*(b + 2*c*x)*Log[f]))/(2*\operatorname{Sqrt}[f - I*c*Log[f]])] * \operatorname{Sqrt}[f - I*c*Log[f]] * (f + I*c*Log[f]) * ((-I)*\operatorname{Cos}[d] + \operatorname{Sin}[d])))/(4*E^{(((I/4)*(e^2/(f - I*c*Log[f]) + (b^2*Log[f]^2)/(f + I*c*Log[f]))*(f^2 + c^2*Log[f]^2))})$

fricas [B] time = 0.71, size = 377, normalized size = 1.81

$$\sqrt{\pi} (c \log(f) - if) \sqrt{-c \log(f) - if} \operatorname{erf}\left(\frac{(2f^2x + (2c^2x + bc) \log(f)^2 + ef + (ice - ibf) \log(f)) \sqrt{-c \log(f) - if}}{2(c^2 \log(f)^2 + f^2)}\right) e^{\left(-\frac{(b^2c - 4ac^2) \log(f)^3 + ie^2f}{2(c^2 \log(f)^2 + f^2)}\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(c*x^2+b*x+a)*cos(f*x^2+e*x+d), x, algorithm="fricas")

[Out] $-1/4*(\operatorname{sqrt}(\pi)*(c*\log(f) - I*f)*\operatorname{sqrt}(-c*\log(f) - I*f)*\operatorname{erf}(1/2*(2*f^2*x + (2*c^2*x + b*c)*\log(f)^2 + e*f + (I*c*e - I*b*f)*\log(f))*\operatorname{sqrt}(-c*\log(f) - I*f)/(c^2*\log(f)^2 + f^2)) * e^{-1/4*((b^2*c - 4*a*c^2)*\log(f)^3 + I*e^2*f - 4*I*d*f^2 - (4*I*c^2*d - 2*I*b*c*e + I*b^2*f)*\log(f)^2 - (c*e^2 - 2*b*e*f + 4*a*f^2)*\log(f))/(c^2*\log(f)^2 + f^2)} + \operatorname{sqrt}(\pi)*(c*\log(f) + I*f)*\operatorname{sqrt}(-c*\log(f) + I*f)*\operatorname{erf}(1/2*(2*f^2*x + (2*c^2*x + b*c)*\log(f)^2 + e*f + (-I*c*e + I*b*f)*\log(f))*\operatorname{sqrt}(-c*\log(f) + I*f)/(c^2*\log(f)^2 + f^2)) * e^{-1/4*((b^2*c - 4*a*c^2)*\log(f)^3 - I*e^2*f + 4*I*d*f^2 - (-4*I*c^2*d + 2*I*b*c*e - I*b^2*f)*\log(f)^2 - (c*e^2 - 2*b*e*f + 4*a*f^2)*\log(f))/(c^2*\log(f)^2 + f^2)))/(c^2*\log(f)^2 + f^2)$

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int f^{cx^2+bx+a} \cos(fx^2 + ex + d) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(c*x^2+b*x+a)*cos(f*x^2+e*x+d),x, algorithm="giac")

[Out] integrate(f^(c*x^2 + b*x + a)*cos(f*x^2 + e*x + d), x)

maple [A] time = 0.19, size = 214, normalized size = 1.03

$$\frac{\sqrt{\pi} f^a e^{\frac{4df - e^2 - 2i \ln(f) b e + 4id \ln(f) c + \ln(f)^2 b^2}{4(-if + c \ln(f))}} \operatorname{erf}\left(-x \sqrt{if - c \ln(f)} + \frac{-ie + b \ln(f)}{2\sqrt{if - c \ln(f)}}\right)}{4\sqrt{if - c \ln(f)}} \frac{\sqrt{\pi} f^a e^{\frac{4df - e^2 + 2i \ln(f) b e - 4id \ln(f) c + \ln(f)^2 b^2}{4(if + c \ln(f))}}}{4\sqrt{-if}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(f^(c*x^2+b*x+a)*cos(f*x^2+e*x+d),x)

[Out] $-1/4 * \pi^{(1/2)} * f^a * \exp(-1/4 * (4 * d * f - e^2 - 2 * I * \ln(f) * b * e + 4 * I * d * \ln(f) * c + \ln(f)^2 * b^2) / (-I * f + c * \ln(f))) / (I * f - c * \ln(f))^{(1/2)} * \operatorname{erf}(-x * (I * f - c * \ln(f))^{(1/2)} + 1/2 * (-I * e + b * \ln(f)) / (I * f - c * \ln(f))) - 1/4 * \pi^{(1/2)} * f^a * \exp(-1/4 * (4 * d * f - e^2 + 2 * I * \ln(f) * b * e - 4 * I * d * \ln(f) * c + \ln(f)^2 * b^2) / (I * f + c * \ln(f))) / (-I * f - c * \ln(f))^{(1/2)} * \operatorname{erf}(-(-I * f - c * \ln(f))^{(1/2)} * x + 1/2 * (I * e + b * \ln(f)) / (-I * f - c * \ln(f)))^{(1/2)}$

maxima [B] time = 0.39, size = 1008, normalized size = 4.85

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(c*x^2+b*x+a)*cos(f*x^2+e*x+d),x, algorithm="maxima")

[Out] $-1/8 * (\sqrt{\pi}) * \sqrt{(2 * c^2 * \log(f)^2 + 2 * f^2)} * ((I * f^{(1/4) * c * e^2 / (c^2 * \log(f)^2 + f^2)}) * f^a * \cos(-1/4 * (e^2 * f - 4 * d * f^2 - (4 * c^2 * d - 2 * b * c * e + b^2 * f) * \log(f)^2) / (c^2 * \log(f)^2 + f^2)) + f^{(1/4) * c * e^2 / (c^2 * \log(f)^2 + f^2)}) * f^a * \sin(-1/4 * (e^2 * f - 4 * d * f^2 - (4 * c^2 * d - 2 * b * c * e + b^2 * f) * \log(f)^2) / (c^2 * \log(f)^2 + f^2))) * \operatorname{erf}(1/2 * (2 * (c * \log(f) - I * f) * x + b * \log(f) - I * e) * \sqrt{-c * \log(f) + I * f} / (c * \log(f) - I * f)) + (-I * f^{(1/4) * c * e^2 / (c^2 * \log(f)^2 + f^2)}) * f^a * \cos(-1/4 * (e^2 * f - 4 * d * f^2 - (4 * c^2 * d - 2 * b * c * e + b^2 * f) * \log(f)^2) / (c^2 * \log(f)^2 + f^2)) + f^{(1/4) * c * e^2 / (c^2 * \log(f)^2 + f^2)}) * f^a * \sin(-1/4 * (e^2 * f - 4 * d * f^2 - (4 * c^2 * d - 2 * b * c * e + b^2 * f) * \log(f)^2) / (c^2 * \log(f)^2 + f^2))) * \operatorname{erf}(1/2 * (2 * (c * \log(f) + I * f) * x + b * \log(f) + I * e) * \sqrt{-c * \log(f) - I * f} / (c * \log(f) + I * f))) * \sqrt{(c * \log(f) + \sqrt{c^2 * \log(f)^2 + f^2}) - \sqrt{\pi}) * \sqrt{(2 * c^2 * \log(f)^2 + 2 * f^2)} * ((f^{(1/4) * c * e^2 / (c^2 * \log(f)^2 + f^2)}) * f^a * \cos(-1/4 * (e^2 * f - 4 * d * f^2 - (4 * c^2 * d - 2 * b * c * e + b^2 * f) * \log(f)^2) / (c^2 * \log(f)^2 + f^2)) - I * f^{(1/4) * c * e^2 / (c^2 * \log(f)^2 + f^2)}) * f^a * \sin(-1/4 * (e^2 * f - 4 * d * f^2 - (4 * c^2 * d - 2 * b * c * e + b^2 * f) * \log(f)^2) / (c^2 * \log(f)^2 + f^2))) * \operatorname{erf}(1/2 * (2 * (c * \log(f) - I * f) * x + b * \log(f) - I * e) * \sqrt{-c * \log(f) + I * f} / (c * \log(f) - I * f)) + (f^{(1/4) * c * e^2 / (c^2 * \log(f)^2 + f^2)}) * f^a * \cos(-1/4 * (e^2 * f - 4 * d * f^2 - (4 * c^2 * d - 2 * b * c * e + b^2 * f) * \log(f)^2) / (c^2 * \log(f)^2 + f^2)) + I * f^{(1/4) * c * e^2 / (c^2 * \log(f)^2 + f^2)}) * f^a * \sin(-1/4 * (e^2 * f - 4 * d * f^2 - (4 * c^2 * d - 2 * b * c * e + b^2 * f) * \log(f)^2) / (c^2 * \log(f)^2 + f^2))) * \operatorname{erf}(1/2 * (2 * (c * \log(f) + I * f) * x + b * \log(f) + I * e) * \sqrt{-c * \log(f) - I * f} / (c * \log(f) + I * f))) * \sqrt{(-c * \log(f) + \sqrt{c^2 * \log(f)^2 + f^2})} / (c^2 * e^{(1/4) * b^2 * c * \log(f)^3 / (c^2 * \log(f)^2 + f^2)} + 1/2 * b * e * f * \log(f) / (c^2 * \log(f)^2 + f^2)) * \log(f)^2 + f^2 * e^{(1/4) * b^2 * c * \log(f)^3 / (c^2 * \log(f)^2 + f^2)} + 1/2 * b * e * f * \log(f) / (c^2 * \log(f)^2 + f^2)))$

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int f^{cx^2+bx+a} \cos(fx^2 + ex + d) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(f^(a + b*x + c*x^2)*cos(d + e*x + f*x^2), x)`

[Out] `int(f^(a + b*x + c*x^2)*cos(d + e*x + f*x^2), x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int f^{a+bx+cx^2} \cos(d + ex + fx^2) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(f**(c*x**2+b*x+a)*cos(f*x**2+e*x+d), x)`

[Out] `Integral(f**(a + b*x + c*x**2)*cos(d + e*x + f*x**2), x)`

$$3.132 \quad \int f^{a+bx+cx^2} \cos^2(d + ex + fx^2) dx$$

Optimal. Leaf size=268

$$\frac{\sqrt{\pi} f^{a-\frac{b^2}{4c}} \operatorname{erfi}\left(\frac{\sqrt{\log(f)}(b+2cx)}{2\sqrt{c}}\right)}{4\sqrt{c}\sqrt{\log(f)}} + \frac{\sqrt{\pi} f^a \exp\left(-\frac{(2e+ib\log(f))^2}{-4c\log(f)+8if} - 2id\right) \operatorname{erf}\left(\frac{-b\log(f)+2x(-c\log(f)+2if)+2ie}{2\sqrt{-c\log(f)+2if}}\right)}{8\sqrt{-c\log(f)+2if}} + \frac{\sqrt{\pi} f^a \exp\left(\frac{-b\log(f)+2x(-c\log(f)+2if)+2ie}{2\sqrt{-c\log(f)+2if}}\right)}{8\sqrt{-c\log(f)+2if}}$$

```
[Out] 1/4*f^(a-1/4*b^2/c)*erfi(1/2*(2*c*x+b)*ln(f)^(1/2)/c^(1/2))*Pi^(1/2)/c^(1/2)/ln(f)^(1/2)+1/8*exp(-2*I*d-(2*e+I*b*ln(f))^2/(8*I*f-4*c*ln(f)))*f^a*erf(1/2*(2*I*e-b*ln(f)+2*x*(2*I*f-c*ln(f)))/(2*I*f-c*ln(f))^(1/2))*Pi^(1/2)/(2*I*f-c*ln(f))^(1/2)+1/8*exp(2*I*d+(2*e-I*b*ln(f))^2/(8*I*f+4*c*ln(f)))*f^a*erfi(1/2*(2*I*e+b*ln(f)+2*x*(2*I*f+c*ln(f)))/(2*I*f+c*ln(f))^(1/2))*Pi^(1/2)/(2*I*f+c*ln(f))^(1/2)
```

Rubi [A] time = 0.46, antiderivative size = 268, normalized size of antiderivative = 1.00, number of steps used = 10, number of rules used = 5, integrand size = 26, $\frac{\text{number of rules}}{\text{integrand size}} = 0.192$, Rules used = {4473, 2234, 2204, 2287, 2205}

$$\frac{\sqrt{\pi} f^{a-\frac{b^2}{4c}} \operatorname{Erfi}\left(\frac{\sqrt{\log(f)}(b+2cx)}{2\sqrt{c}}\right)}{4\sqrt{c}\sqrt{\log(f)}} + \frac{\sqrt{\pi} f^a \exp\left(-\frac{(2e+ib\log(f))^2}{-4c\log(f)+8if} - 2id\right) \operatorname{Erf}\left(\frac{-b\log(f)+2x(-c\log(f)+2if)+2ie}{2\sqrt{-c\log(f)+2if}}\right)}{8\sqrt{-c\log(f)+2if}} + \frac{\sqrt{\pi} f^a \exp\left(\frac{-b\log(f)+2x(-c\log(f)+2if)+2ie}{2\sqrt{-c\log(f)+2if}}\right)}{8\sqrt{-c\log(f)+2if}}$$

Antiderivative was successfully verified.

```
[In] Int[f^(a + b*x + c*x^2)*Cos[d + e*x + f*x^2]^2, x]
```

```
[Out] (f^(a - b^2/(4*c))*Sqrt[Pi]*Erfi[((b + 2*c*x)*Sqrt[Log[f]])/(2*Sqrt[c])])/(4*Sqrt[c]*Sqrt[Log[f]]) + (E^((-2*I)*d - (2*e + I*b*Log[f])^2/((8*I)*f - 4*c*Log[f]))*f^a*Sqrt[Pi]*Erf[((2*I)*e - b*Log[f] + 2*x*((2*I)*f - c*Log[f]))/(2*Sqrt[(2*I)*f - c*Log[f]])])/(8*Sqrt[(2*I)*f - c*Log[f]]) + (E^((2*I)*d + (2*e - I*b*Log[f])^2/((8*I)*f + 4*c*Log[f]))*f^a*Sqrt[Pi]*Erfi[((2*I)*e + b*Log[f] + 2*x*((2*I)*f + c*Log[f]))/(2*Sqrt[(2*I)*f + c*Log[f]])])/(8*Sqrt[(2*I)*f + c*Log[f]])
```

Rule 2204

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^2), x_Symbol] := Simp[(F^a*Sqrt[Pi]*Erfi[(c + d*x)*Rt[b*Log[F], 2]]/(2*d*Rt[b*Log[F], 2]), x] /; FreeQ[{F, a, b, c, d}, x] && PosQ[b]
```

Rule 2205

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^2), x_Symbol] := Simp[(F^a*Sqrt[Pi]*Erf[(c + d*x)*Rt[-(b*Log[F]), 2]]/(2*d*Rt[-(b*Log[F]), 2]), x] /; FreeQ[{F, a, b, c, d}, x] && NegQ[b]
```

Rule 2234

```
Int[(F_)^((a_.) + (b_.)*(x_) + (c_.)*(x_)^2), x_Symbol] := Dist[F^(a - b^2/(4*c)), Int[F^((b + 2*c*x)^2/(4*c)), x], x] /; FreeQ[{F, a, b, c}, x]
```

Rule 2287

```
Int[(u_.)*(F_)^(v_.)*(G_)^(w_.), x_Symbol] := With[{z = v*Log[F] + w*Log[G]}, Int[u*NormalizeIntegrand[E^z, x], x] /; BinomialQ[z, x] || (PolynomialQ[z, x] && LeQ[Exponent[z, x], 2])] /; FreeQ[{F, G}, x]
```

Rule 4473

$f]^2 \sqrt{2f + I \cdot c \cdot \text{Log}[f]} \cdot \text{Sin}[2 \cdot d]) / E^{(((I/4) \cdot (-4 \cdot e^2 - (4 \cdot I) \cdot b \cdot e \cdot \text{Log}[f] + b^2 \cdot \text{Log}[f]^2)) / (2f + I \cdot c \cdot \text{Log}[f]))} / (8 \cdot c \cdot \text{Log}[f] \cdot (2f - I \cdot c \cdot \text{Log}[f]) \cdot (2f + I \cdot c \cdot \text{Log}[f]))$

fricas [B] time = 0.68, size = 468, normalized size = 1.75

$$\sqrt{\pi} (c^2 \log(f)^2 - 2icf \log(f)) \sqrt{-c \log(f) - 2if} \operatorname{erf} \left(\frac{(8f^2x + (2c^2x + bc) \log(f)^2 + 4ef + (2ice - 2ibf) \log(f)) \sqrt{-c \log(f) - 2if}}{2(c^2 \log(f)^2 + 4f^2)} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(c*x^2+b*x+a)*cos(f*x^2+e*x+d)^2,x, algorithm="fricas")

[Out] $-1/8 \cdot (\sqrt{\pi}) \cdot (c^2 \log(f)^2 - 2I \cdot c \cdot f \cdot \log(f)) \cdot \sqrt{-c \log(f) - 2I \cdot f} \cdot \operatorname{erf} \left(\frac{1/2 \cdot (8f^2x + (2c^2x + bc) \log(f)^2 + 4e \cdot f + (2I \cdot c \cdot e - 2I \cdot b \cdot f) \log(f)) \cdot \sqrt{-c \log(f) - 2I \cdot f}}{(c^2 \log(f)^2 + 4f^2)} \right) \cdot e^{-1/4 \cdot ((b^2 \cdot c - 4 \cdot a \cdot c^2) \log(f)^3 + 8I \cdot e^2 \cdot f - 32I \cdot d \cdot f^2 - (8I \cdot c^2 \cdot d - 4I \cdot b \cdot c \cdot e + 2I \cdot b^2 \cdot f) \log(f)^2 - 4 \cdot (c \cdot e^2 - 2 \cdot b \cdot e \cdot f + 4 \cdot a \cdot f^2) \log(f)) / (c^2 \log(f)^2 + 4f^2)} + \sqrt{\pi} \cdot (c^2 \log(f)^2 + 2I \cdot c \cdot f \cdot \log(f)) \cdot \sqrt{-c \log(f) + 2I \cdot f} \cdot \operatorname{erf} \left(\frac{1/2 \cdot (8f^2x + (2c^2x + bc) \log(f)^2 + 4e \cdot f + (-2I \cdot c \cdot e + 2I \cdot b \cdot f) \log(f)) \cdot \sqrt{-c \log(f) + 2I \cdot f}}{(c^2 \log(f)^2 + 4f^2)} \right) \cdot e^{-1/4 \cdot ((b^2 \cdot c - 4 \cdot a \cdot c^2) \log(f)^3 - 8I \cdot e^2 \cdot f + 32I \cdot d \cdot f^2 - (-8I \cdot c^2 \cdot d + 4I \cdot b \cdot c \cdot e - 2I \cdot b^2 \cdot f) \log(f)^2 - 4 \cdot (c \cdot e^2 - 2 \cdot b \cdot e \cdot f + 4 \cdot a \cdot f^2) \log(f)) / (c^2 \log(f)^2 + 4f^2)} + 2 \cdot \sqrt{\pi} \cdot (c^2 \log(f)^2 + 4f^2) \cdot \sqrt{-c \log(f)} \cdot \operatorname{erf} \left(\frac{1/2 \cdot (2c \cdot x + b) \cdot \sqrt{-c \log(f)}}{c} \right) / f^{1/4 \cdot (b^2 - 4 \cdot a \cdot c) / c} / (c^3 \log(f)^3 + 4 \cdot c \cdot f^2 \cdot \log(f))$

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int f^{cx^2+bx+a} \cos(fx^2+ex+d)^2 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(c*x^2+b*x+a)*cos(f*x^2+e*x+d)^2,x, algorithm="giac")

[Out] integrate(f^(c*x^2 + b*x + a)*cos(f*x^2 + e*x + d)^2, x)

maple [A] time = 0.33, size = 263, normalized size = 0.98

$$\frac{\sqrt{\pi} f^a e^{-\frac{\ln(f)^2 b^2 - 4i \ln(f) b e + 8id \ln(f) c + 16df - 4e^2}{4(-2if + c \ln(f))}} \operatorname{erf} \left(-x \sqrt{2if - c \ln(f)} + \frac{b \ln(f) - 2ie}{2\sqrt{2if - c \ln(f)}} \right) \sqrt{\pi} f^a e^{-\frac{\ln(f)^2 b^2 + 4i \ln(f) b e - 8id \ln(f) c + 16df}{4(2if + c \ln(f))}}}{8\sqrt{2if - c \ln(f)}} \quad 8\sqrt{2if + c \ln(f)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(f^(c*x^2+b*x+a)*cos(f*x^2+e*x+d)^2,x)

[Out] $-1/8 \cdot \text{Pi}^{(1/2)} \cdot f^a \cdot \exp(-1/4 \cdot (\ln(f)^2 \cdot b^2 - 4I \cdot \ln(f) \cdot b \cdot e + 8I \cdot d \cdot \ln(f) \cdot c + 16 \cdot d \cdot f - 4 \cdot e^2) / (-2I \cdot f + c \cdot \ln(f))) / (2I \cdot f - c \cdot \ln(f))^{(1/2)} \cdot \operatorname{erf}(-x \cdot (2I \cdot f - c \cdot \ln(f))^{(1/2)} + 1/2 \cdot (b \cdot \ln(f) - 2I \cdot e) / (2I \cdot f - c \cdot \ln(f))^{(1/2)}) - 1/8 \cdot \text{Pi}^{(1/2)} \cdot f^a \cdot \exp(-1/4 \cdot (\ln(f)^2 \cdot b^2 + 4I \cdot \ln(f) \cdot b \cdot e - 8I \cdot d \cdot \ln(f) \cdot c + 16 \cdot d \cdot f - 4 \cdot e^2) / (2I \cdot f + c \cdot \ln(f))) / (-2I \cdot f - c \cdot \ln(f))^{(1/2)} \cdot \operatorname{erf}(-(-2I \cdot f - c \cdot \ln(f))^{(1/2)} \cdot x + 1/2 \cdot (2I \cdot e + b \cdot \ln(f)) / (-2I \cdot f - c \cdot \ln(f))^{(1/2)}) - 1/4 \cdot \text{Pi}^{(1/2)} \cdot f^a \cdot f^{-1/4 \cdot b^2 / c} / (-c \cdot \ln(f))^{(1/2)} \cdot \operatorname{erf}(-(-c \cdot \ln(f))^{(1/2)} \cdot x + 1/2 / (-c \cdot \ln(f))^{(1/2)} \cdot b \cdot \ln(f))$

maxima [C] time = 0.42, size = 1487, normalized size = 5.55

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(c*x^2+b*x+a)*cos(f*x^2+e*x+d)^2,x, algorithm="maxima")

[Out]
$$-1/16*(\sqrt{\pi})\sqrt{2*c^2*\log(f)^2 + 8*f^2}*((I*f^a*\cos(-1/2*(4*e^2*f - 16*d*f^2 - 4*c^2*d - 2*b*c*e + b^2*f)*\log(f)^2)/(c^2*\log(f)^2 + 4*f^2))*e^{(c*e^2*\log(f)/(c^2*\log(f)^2 + 4*f^2) + 1/4*b^2*\log(f)/c) + f^a*e^{(c*e^2*\log(f)/(c^2*\log(f)^2 + 4*f^2) + 1/4*b^2*\log(f)/c)*\sin(-1/2*(4*e^2*f - 16*d*f^2 - 4*c^2*d - 2*b*c*e + b^2*f)*\log(f)^2)/(c^2*\log(f)^2 + 4*f^2)))*\operatorname{erf}(1/2*(2*(c*\log(f) - 2*I*f)*x + b*\log(f) - 2*I*e)*\sqrt{-c*\log(f) + 2*I*f})/(c*\log(f) - 2*I*f)) + (-I*f^a*\cos(-1/2*(4*e^2*f - 16*d*f^2 - 4*c^2*d - 2*b*c*e + b^2*f)*\log(f)^2)/(c^2*\log(f)^2 + 4*f^2))*e^{(c*e^2*\log(f)/(c^2*\log(f)^2 + 4*f^2) + 1/4*b^2*\log(f)/c) + f^a*e^{(c*e^2*\log(f)/(c^2*\log(f)^2 + 4*f^2) + 1/4*b^2*\log(f)/c)*\sin(-1/2*(4*e^2*f - 16*d*f^2 - 4*c^2*d - 2*b*c*e + b^2*f)*\log(f)^2)/(c^2*\log(f)^2 + 4*f^2)))*\operatorname{erf}(1/2*(2*(c*\log(f) + 2*I*f)*x + b*\log(f) + 2*I*e)*\sqrt{-c*\log(f) - 2*I*f})/(c*\log(f) + 2*I*f)))*\sqrt{c*\log(f) + \sqrt{c^2*\log(f)^2 + 4*f^2}}*\sqrt{-c*\log(f)} - \sqrt{\pi})\sqrt{2*c^2*\log(f)^2 + 8*f^2}*((f^a*\cos(-1/2*(4*e^2*f - 16*d*f^2 - 4*c^2*d - 2*b*c*e + b^2*f)*\log(f)^2)/(c^2*\log(f)^2 + 4*f^2))*e^{(c*e^2*\log(f)/(c^2*\log(f)^2 + 4*f^2) + 1/4*b^2*\log(f)/c) - I*f^a*e^{(c*e^2*\log(f)/(c^2*\log(f)^2 + 4*f^2) + 1/4*b^2*\log(f)/c)*\sin(-1/2*(4*e^2*f - 16*d*f^2 - 4*c^2*d - 2*b*c*e + b^2*f)*\log(f)^2)/(c^2*\log(f)^2 + 4*f^2)))*\operatorname{erf}(1/2*(2*(c*\log(f) - 2*I*f)*x + b*\log(f) - 2*I*e)*\sqrt{-c*\log(f) + 2*I*f})/(c*\log(f) - 2*I*f)) + (f^a*\cos(-1/2*(4*e^2*f - 16*d*f^2 - 4*c^2*d - 2*b*c*e + b^2*f)*\log(f)^2)/(c^2*\log(f)^2 + 4*f^2))*e^{(c*e^2*\log(f)/(c^2*\log(f)^2 + 4*f^2) + 1/4*b^2*\log(f)/c) + I*f^a*e^{(c*e^2*\log(f)/(c^2*\log(f)^2 + 4*f^2) + 1/4*b^2*\log(f)/c)*\sin(-1/2*(4*e^2*f - 16*d*f^2 - 4*c^2*d - 2*b*c*e + b^2*f)*\log(f)^2)/(c^2*\log(f)^2 + 4*f^2)))*\operatorname{erf}(1/2*(2*(c*\log(f) + 2*I*f)*x + b*\log(f) + 2*I*e)*\sqrt{-c*\log(f) - 2*I*f})/(c*\log(f) + 2*I*f)))*\sqrt{-c*\log(f) + \sqrt{c^2*\log(f)^2 + 4*f^2}}*\sqrt{-c*\log(f)} - 2*\sqrt{\pi}*((c^2*f^a*e^{(1/4*b^2*c*\log(f)^3/(c^2*\log(f)^2 + 4*f^2) + 2*b*e*f*\log(f)/(c^2*\log(f)^2 + 4*f^2))*\log(f)^2 + 4*f^a*(a + 2)*e^{(1/4*b^2*c*\log(f)^3/(c^2*\log(f)^2 + 4*f^2) + 2*b*e*f*\log(f)/(c^2*\log(f)^2 + 4*f^2)))*\operatorname{erf}(-1/2*b*\operatorname{conjugate}(1/\sqrt{-c*\log(f)})*\log(f) + x*\operatorname{conjugate}(\sqrt{-c*\log(f)})) - (c^2*f^a*e^{(1/4*b^2*c*\log(f)^3/(c^2*\log(f)^2 + 4*f^2) + 2*b*e*f*\log(f)/(c^2*\log(f)^2 + 4*f^2))*\log(f)^2 + 4*f^a*(a + 2)*e^{(1/4*b^2*c*\log(f)^3/(c^2*\log(f)^2 + 4*f^2) + 2*b*e*f*\log(f)/(c^2*\log(f)^2 + 4*f^2)))*\operatorname{erf}(1/2*(2*c*x*\log(f) + b*\log(f))/\sqrt{-c*\log(f)})))/((c^2*e^{(1/4*b^2*c*\log(f)^3/(c^2*\log(f)^2 + 4*f^2) + 2*b*e*f*\log(f)/(c^2*\log(f)^2 + 4*f^2) + 1/4*b^2*\log(f)/c)*\log(f)^2 + 4*f^2*e^{(1/4*b^2*c*\log(f)^3/(c^2*\log(f)^2 + 4*f^2) + 2*b*e*f*\log(f)/(c^2*\log(f)^2 + 4*f^2) + 1/4*b^2*\log(f)/c)}*\sqrt{-c*\log(f)}))$$

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int f^{cx^2+bx+a} \cos(fx^2+ex+d)^2 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(f^(a + b*x + c*x^2)*cos(d + e*x + f*x^2)^2,x)

[Out] int(f^(a + b*x + c*x^2)*cos(d + e*x + f*x^2)^2, x)

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f**(c*x**2+b*x+a)*cos(f*x**2+e*x+d)**2,x)

[Out] Timed out

3.133 $\int f^{a+bx+cx^2} \cos^3(d+ex+fx^2) dx$

Optimal. Leaf size=422

$$\frac{3\sqrt{\pi} f^a \exp\left(-\frac{(e+ib \log(f))^2}{-4c \log(f)+4if} - id\right) \operatorname{erf}\left(\frac{-b \log(f)+2x(-c \log(f)+if)+ie}{2\sqrt{-c \log(f)+if}}\right)}{16\sqrt{-c \log(f)+if}} + \frac{\sqrt{\pi} f^a \exp\left(-\frac{(3e+ib \log(f))^2}{4(-c \log(f)+3if)} - 3id\right) \operatorname{erf}\left(\frac{-b \log(f)+2x(-c \log(f)+if)+ie}{2\sqrt{-c \log(f)+if}}\right)}{16\sqrt{-c \log(f)+3if}}$$

```
[Out] 3/16*exp(-I*d-(e+I*b*ln(f))^2/(4*I*f-4*c*ln(f)))*f^a*erf(1/2*(I*e-b*ln(f)+2*x*(I*f-c*ln(f)))/(I*f-c*ln(f))^(1/2))*Pi^(1/2)/(I*f-c*ln(f))^(1/2)+1/16*exp(-3*I*d-1/4*(3*e+I*b*ln(f))^2/(3*I*f-c*ln(f)))*f^a*erf(1/2*(3*I*e-b*ln(f)+2*x*(3*I*f-c*ln(f)))/(3*I*f-c*ln(f))^(1/2))*Pi^(1/2)/(3*I*f-c*ln(f))^(1/2)+3/16*exp(I*d+(e-I*b*ln(f))^2/(4*I*f+4*c*ln(f)))*f^a*erfi(1/2*(I*e+b*ln(f)+2*x*(I*f+c*ln(f)))/(I*f+c*ln(f))^(1/2))*Pi^(1/2)/(I*f+c*ln(f))^(1/2)+1/16*exp(3*I*d-1/4*(3*I*e+b*ln(f))^2/(3*I*f+c*ln(f)))*f^a*erfi(1/2*(3*I*e+b*ln(f)+2*x*(3*I*f+c*ln(f)))/(3*I*f+c*ln(f))^(1/2))*Pi^(1/2)/(3*I*f+c*ln(f))^(1/2)
```

Rubi [A] time = 0.66, antiderivative size = 422, normalized size of antiderivative = 1.00, number of steps used = 14, number of rules used = 5, integrand size = 26, $\frac{\text{number of rules}}{\text{integrand size}} = 0.192$, Rules used = {4473, 2287, 2234, 2205, 2204}

$$\frac{3\sqrt{\pi} f^a \exp\left(-\frac{(e+ib \log(f))^2}{-4c \log(f)+4if} - id\right) \operatorname{Erf}\left(\frac{-b \log(f)+2x(-c \log(f)+if)+ie}{2\sqrt{-c \log(f)+if}}\right)}{16\sqrt{-c \log(f)+if}} + \frac{\sqrt{\pi} f^a \exp\left(-\frac{(3e+ib \log(f))^2}{4(-c \log(f)+3if)} - 3id\right) \operatorname{Erf}\left(\frac{-b \log(f)+2x(-c \log(f)+if)+ie}{2\sqrt{-c \log(f)+if}}\right)}{16\sqrt{-c \log(f)+3if}}$$

Antiderivative was successfully verified.

```
[In] Int[f^(a + b*x + c*x^2)*Cos[d + e*x + f*x^2]^3, x]
```

```
[Out] (3*E^((-I)*d - (e + I*b*Log[f])^2/((4*I)*f - 4*c*Log[f]))*f^a*Sqrt[Pi]*Erf[(I*e - b*Log[f] + 2*x*(I*f - c*Log[f]))/(2*Sqrt[I*f - c*Log[f]])]/(16*Sqrt[I*f - c*Log[f]]) + (E^((-3*I)*d - (3*e + I*b*Log[f])^2/(4*((3*I)*f - c*Log[f]))) * f^a * Sqrt[Pi] * Erf[((3*I)*e - b*Log[f] + 2*x*((3*I)*f - c*Log[f]))/(2*Sqrt[(3*I)*f - c*Log[f]])]/(16*Sqrt[(3*I)*f - c*Log[f]]) + (3*E^(I*d + (e - I*b*Log[f])^2/((4*I)*f + 4*c*Log[f])) * f^a * Sqrt[Pi] * Erfi[(I*e + b*Log[f] + 2*x*(I*f + c*Log[f]))/(2*Sqrt[I*f + c*Log[f]])]/(16*Sqrt[I*f + c*Log[f]]) + (E^((3*I)*d - ((3*I)*e + b*Log[f])^2/(4*((3*I)*f + c*Log[f]))) * f^a * Sqrt[Pi] * Erfi[((3*I)*e + b*Log[f] + 2*x*((3*I)*f + c*Log[f]))/(2*Sqrt[(3*I)*f + c*Log[f]])]/(16*Sqrt[(3*I)*f + c*Log[f]])
```

Rule 2204

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_)^2), x_Symbol] := Simp[(F^a*Sqrt[Pi]*Erfi[(c + d*x)*Rt[b*Log[F], 2]]/(2*d*Rt[b*Log[F], 2]), x] /; FreeQ[{F, a, b, c, d}, x] && PosQ[b]
```

Rule 2205

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_)^2), x_Symbol] := Simp[(F^a*Sqrt[Pi]*Erf[(c + d*x)*Rt[-(b*Log[F]), 2]]/(2*d*Rt[-(b*Log[F]), 2]), x] /; FreeQ[{F, a, b, c, d}, x] && NegQ[b]
```

Rule 2234

```
Int[(F_)^((a_.) + (b_.)*(x_) + (c_.)*(x_)^2), x_Symbol] := Dist[F^(a - b^2/(4*c)), Int[F^((b + 2*c*x)^2/(4*c)), x], x] /; FreeQ[{F, a, b, c}, x]
```

Rule 2287

```
Int[(u_.)*(F_)^(v_.)*(G_)^(w_.), x_Symbol] := With[{z = v*Log[F] + w*Log[G]}, Int[u*NormalizeIntegrand[E^z, x], x] /; BinomialQ[z, x] || (PolynomialQ[z,
```

x] && LeQ[Exponent[z, x], 2]]) /; FreeQ[{F, G}, x]

Rule 4473

Int[Cos[v_]^(n_.)*(F_)^(u_), x_Symbol] := Int[ExpandTrigToExp[F^u, Cos[v]^n, x], x] /; FreeQ[F, x] && (LinearQ[u, x] || PolyQ[u, x, 2]) && (LinearQ[v, x] || PolyQ[v, x, 2]) && IGtQ[n, 0]

Rubi steps

$$\begin{aligned} \int f^{a+bx+cx^2} \cos^3(d+ex+fx^2) dx &= \int \left(\frac{1}{8} e^{-3i(d+ex+fx^2)} f^{a+bx+cx^2} + \frac{3}{8} \exp(2id+2iex+2ifx^2-3i(d+ex+fx^2)) \right. \\ &= \frac{1}{8} \int e^{-3i(d+ex+fx^2)} f^{a+bx+cx^2} dx + \frac{1}{8} \int \exp(6id+6iex+6ifx^2-3i(d+ex+fx^2)) \\ &= \frac{1}{8} \int \exp(-3id+a \log(f)-x(3ie-b \log(f))-x^2(3if-c \log(f))) dx + \frac{1}{8} \int \exp\left(\frac{(-ie+b \log(f)+2x(-if+c \log(f))}{4(-if+c \log(f))}\right) \\ &= \frac{1}{8} \left(3 \exp\left(-id-\frac{(e+ib \log(f))^2}{4if-4c \log(f)}\right) f^a \int \exp\left(\frac{(-ie+b \log(f)+2x(-if+c \log(f))}{4(-if+c \log(f))}\right) \right. \\ &= \frac{3 \exp\left(-id-\frac{(e+ib \log(f))^2}{4if-4c \log(f)}\right) f^a \sqrt{\pi} \operatorname{erf}\left(\frac{ie-b \log(f)+2x(if-c \log(f))}{2\sqrt{if-c \log(f)}}\right) \exp(-3id-} \\ &= \frac{\phantom{3 \exp\left(-id-\frac{(e+ib \log(f))^2}{4if-4c \log(f)}\right) f^a \sqrt{\pi} \operatorname{erf}\left(\frac{ie-b \log(f)+2x(if-c \log(f))}{2\sqrt{if-c \log(f)}}\right) \exp(-3id-}}{16\sqrt{if-c \log(f)}} + \frac{\phantom{3 \exp\left(-id-\frac{(e+ib \log(f))^2}{4if-4c \log(f)}\right) f^a \sqrt{\pi} \operatorname{erf}\left(\frac{ie-b \log(f)+2x(if-c \log(f))}{2\sqrt{if-c \log(f)}}\right) \exp(-3id-}}{16\sqrt{if-c \log(f)}} \end{aligned}$$

Mathematica [B] time = 7.28, size = 3829, normalized size = 9.07

Result too large to show

Warning: Unable to verify antiderivative.

[In] Integrate[f^(a + b*x + c*x^2)*Cos[d + e*x + f*x^2]^3,x]

[Out] (f^a*Sqrt[Pi]*(-27*(-1)^(3/4)*E^(((I/4)*(-e^2 + (2*I)*b*e*Log[f] + b^2*Log[f]^2))/(f - I*c*Log[f]))*f^3*Cos[d]*Erfi[((-1)^(1/4)*(e + 2*f*x - I*b*Log[f] - (2*I)*c*x*Log[f]))/(2*Sqrt[f - I*c*Log[f]])]*Sqrt[f - I*c*Log[f]] + 27*(-1)^(1/4)*c*E^(((I/4)*(-e^2 + (2*I)*b*e*Log[f] + b^2*Log[f]^2))/(f - I*c*Log[f]))*f^2*Cos[d]*Erfi[((-1)^(1/4)*(e + 2*f*x - I*b*Log[f] - (2*I)*c*x*Log[f]))/(2*Sqrt[f - I*c*Log[f]])]*Log[f]*Sqrt[f - I*c*Log[f]] - 3*(-1)^(3/4)*c^2*E^(((I/4)*(-e^2 + (2*I)*b*e*Log[f] + b^2*Log[f]^2))/(f - I*c*Log[f]))*f*Cos[d]*Erfi[((-1)^(1/4)*(e + 2*f*x - I*b*Log[f] - (2*I)*c*x*Log[f]))/(2*Sqrt[f - I*c*Log[f]])]*Log[f]^2*Sqrt[f - I*c*Log[f]] + 3*(-1)^(1/4)*c^3*E^(((I/4)*(-e^2 + (2*I)*b*e*Log[f] + b^2*Log[f]^2))/(f - I*c*Log[f]))*Cos[d]*Erfi[((-1)^(1/4)*(e + 2*f*x - I*b*Log[f] - (2*I)*c*x*Log[f]))/(2*Sqrt[f - I*c*Log[f]])]*Log[f]^3*Sqrt[f - I*c*Log[f]] - 3*(-1)^(3/4)*E^(((I/4)*(-9*e^2 + (6*I)*b*e*Log[f] + b^2*Log[f]^2))/(3*f - I*c*Log[f]))*f^3*Cos[3*d]*Erfi[((-1)^(1/4)*(3*e + 6*f*x - I*b*Log[f] - (2*I)*c*x*Log[f]))/(2*Sqrt[3*f - I*c*Log[f]])]*Sqrt[3*f - I*c*Log[f]] + (-1)^(1/4)*c*E^(((I/4)*(-9*e^2 + (6*I)*b*e*Log[f] + b^2*Log[f]^2))/(3*f - I*c*Log[f]))*f^2*Cos[3*d]*Erfi[((-1)^(1/4)*(3*e + 6*f*x - I*b*Log[f] - (2*I)*c*x*Log[f]))/(2*Sqrt[3*f - I*c*Log[f]])]*Log[f]*Sqrt[3*f - I*c*Log[f]] - 3*(-1)^(3/4)*c^2*E^(((I/4)*(-9*e^2 + (6*I)*b*e*Log[f] + b^2*Log[f]^2))/(3*f - I*c*Log[f]))*f*Cos[3*d]*Erfi[((-1)^(1/4)*(3*e + 6*f*x - I*b*Log[f] - (2*I)*c*x*Log[f]))/(2*Sqrt[3*f - I*c*Log[f]])]*Log[f]^2*Sqrt[3*f - I*c*Log[f]] + (-1)^(1/4)*c^3*E^(((I/4)*(-9*e^2 + (6*I)*b*e*Log[f] + b^2*Log[f]^2))/(3*f - I*c*Log[f]))*Cos[3*d]*Erfi[((-1)^(1/4)*(3*e + 6*f*x - I*b*Log[f] - (2*I)*c*x*Log[f]))/(2*Sqrt[3*f - I*c*Log[f]])]*Log[f]^3*Sqrt[3*f - I*c*Log[f]] - (27*(-1)^(1/4)*f^3*Cos[d]*Erfi[((-1)^(3/4)*(e + 2*f*x + I*b*Log[f] + (2*I)*c*x*Log[f]))/(2*Sqrt[f + I*c*Log[f]])]*Sqrt[f + I*c*Log[f]])/E^(((I/4)*(-e^2 - (2*I)*b*e*Log[f] + b^2*Log[f]^2))/(f


```

)*(3*e + 6*f*x + I*b*Log[f] + (2*I)*c*x*Log[f]))/(2*Sqrt[3*f + I*c*Log[f]])
]*Log[f]*Sqrt[3*f + I*c*Log[f]]*Sin[3*d])/E^(((I/4)*(-9*e^2 - (6*I)*b*e*Log
[f] + b^2*Log[f]^2))/(3*f + I*c*Log[f])) + (3*(-1)^(3/4)*c^2*f*Erfi[(-1)^(
3/4)*(3*e + 6*f*x + I*b*Log[f] + (2*I)*c*x*Log[f]))/(2*Sqrt[3*f + I*c*Log[f
]])]*Log[f]^2*Sqrt[3*f + I*c*Log[f]]*Sin[3*d])/E^(((I/4)*(-9*e^2 - (6*I)*b*
e*Log[f] + b^2*Log[f]^2))/(3*f + I*c*Log[f])) + ((-1)^(1/4)*c^3*Erfi[(-1)^(
3/4)*(3*e + 6*f*x + I*b*Log[f] + (2*I)*c*x*Log[f]))/(2*Sqrt[3*f + I*c*Log[
f]])]*Log[f]^3*Sqrt[3*f + I*c*Log[f]]*Sin[3*d])/E^(((I/4)*(-9*e^2 - (6*I)*b
*e*Log[f] + b^2*Log[f]^2))/(3*f + I*c*Log[f])))/(16*(f - I*c*Log[f])*(3*f
- I*c*Log[f])*(f + I*c*Log[f])*(3*f + I*c*Log[f]))

```

fricas [B] time = 0.93, size = 857, normalized size = 2.03

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(c*x^2+b*x+a)*cos(f*x^2+e*x+d)^3,x, algorithm="fricas")

```

[Out] -1/16*(sqrt(pi)*(c^3*log(f)^3 - 3*I*c^2*f*log(f)^2 + c*f^2*log(f) - 3*I*f^3
)*sqrt(-c*log(f) - 3*I*f)*erf(1/2*(18*f^2*x + (2*c^2*x + b*c)*log(f)^2 + 9*
e*f + (3*I*c*e - 3*I*b*f)*log(f))*sqrt(-c*log(f) - 3*I*f)/(c^2*log(f)^2 + 9
*f^2))*e^(-1/4*((b^2*c - 4*a*c^2)*log(f)^3 + 27*I*e^2*f - 108*I*d*f^2 - (12
*I*c^2*d - 6*I*b*c*e + 3*I*b^2*f)*log(f)^2 - 9*(c*e^2 - 2*b*e*f + 4*a*f^2)*
log(f))/(c^2*log(f)^2 + 9*f^2)) + sqrt(pi)*(3*c^3*log(f)^3 - 3*I*c^2*f*log(
f)^2 + 27*c*f^2*log(f) - 27*I*f^3)*sqrt(-c*log(f) - I*f)*erf(1/2*(2*f^2*x +
(2*c^2*x + b*c)*log(f)^2 + e*f + (I*c*e - I*b*f)*log(f))*sqrt(-c*log(f) -
I*f)/(c^2*log(f)^2 + f^2))*e^(-1/4*((b^2*c - 4*a*c^2)*log(f)^3 + I*e^2*f -
4*I*d*f^2 - (4*I*c^2*d - 2*I*b*c*e + I*b^2*f)*log(f)^2 - (c*e^2 - 2*b*e*f +
4*a*f^2)*log(f))/(c^2*log(f)^2 + f^2)) + sqrt(pi)*(3*c^3*log(f)^3 + 3*I*c^
2*f*log(f)^2 + 27*c*f^2*log(f) + 27*I*f^3)*sqrt(-c*log(f) + I*f)*erf(1/2*(2
*f^2*x + (2*c^2*x + b*c)*log(f)^2 + e*f + (-I*c*e + I*b*f)*log(f))*sqrt(-c*
log(f) + I*f)/(c^2*log(f)^2 + f^2))*e^(-1/4*((b^2*c - 4*a*c^2)*log(f)^3 - I
*e^2*f + 4*I*d*f^2 - (-4*I*c^2*d + 2*I*b*c*e - I*b^2*f)*log(f)^2 - (c*e^2 -
2*b*e*f + 4*a*f^2)*log(f))/(c^2*log(f)^2 + f^2)) + sqrt(pi)*(c^3*log(f)^3
+ 3*I*c^2*f*log(f)^2 + c*f^2*log(f) + 3*I*f^3)*sqrt(-c*log(f) + 3*I*f)*erf(
1/2*(18*f^2*x + (2*c^2*x + b*c)*log(f)^2 + 9*e*f + (-3*I*c*e + 3*I*b*f)*log
(f))*sqrt(-c*log(f) + 3*I*f)/(c^2*log(f)^2 + 9*f^2))*e^(-1/4*((b^2*c - 4*a*
c^2)*log(f)^3 - 27*I*e^2*f + 108*I*d*f^2 - (-12*I*c^2*d + 6*I*b*c*e - 3*I*b
^2*f)*log(f)^2 - 9*(c*e^2 - 2*b*e*f + 4*a*f^2)*log(f))/(c^2*log(f)^2 + 9*f^
2)))/(c^4*log(f)^4 + 10*c^2*f^2*log(f)^2 + 9*f^4)

```

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int f^{cx^2+bx+a} \cos(fx^2 + ex + d)^3 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(c*x^2+b*x+a)*cos(f*x^2+e*x+d)^3,x, algorithm="giac")

[Out] integrate(f^(c*x^2 + b*x + a)*cos(f*x^2 + e*x + d)^3, x)

maple [A] time = 0.81, size = 426, normalized size = 1.01

$$\frac{\sqrt{\pi} f^a e^{-\frac{\ln(f)^2 b^2 - 6i \ln(f) b e + 12id \ln(f) c + 36df - 9e^2}{4(-3if + c \ln(f))}} \operatorname{erf}\left(-x\sqrt{3if - c \ln(f)} + \frac{b \ln(f) - 3ie}{2\sqrt{3if - c \ln(f)}}\right) 3\sqrt{\pi} f^a e^{-\frac{4df - e^2 - 2i \ln(f) b e + 4id \ln(f) c + \ln(f)^2}{4(-if + c \ln(f))}}}{16\sqrt{3if - c \ln(f)}} \quad 16\sqrt{if}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(f^(c*x^2+b*x+a)*cos(f*x^2+e*x+d)^3,x)

```
[Out] -1/16*Pi^(1/2)*f^a*exp(-1/4*(ln(f)^2*b^2-6*I*ln(f)*b*e+12*I*d*ln(f)*c+36*d*
f-9*e^2)/(-3*I*f+c*ln(f)))/(3*I*f-c*ln(f))^(1/2)*erf(-x*(3*I*f-c*ln(f))^(1/
2)+1/2*(b*ln(f)-3*I*e)/(3*I*f-c*ln(f))^(1/2))-3/16*Pi^(1/2)*f^a*exp(-1/4*(4
*d*f-e^2-2*I*ln(f)*b*e+4*I*d*ln(f)*c+ln(f)^2*b^2)/(-I*f+c*ln(f)))/(I*f-c*ln
(f))^(1/2)*erf(-x*(I*f-c*ln(f))^(1/2)+1/2*(-I*e+b*ln(f))/(I*f-c*ln(f))^(1/2
))-3/16*Pi^(1/2)*f^a*exp(-1/4*(4*d*f-e^2+2*I*ln(f)*b*e-4*I*d*ln(f)*c+ln(f)^
2*b^2)/(I*f+c*ln(f)))/(-I*f-c*ln(f))^(1/2)*erf(-(-I*f-c*ln(f))^(1/2)*x+1/2*
(I*e+b*ln(f))/(-I*f-c*ln(f))^(1/2))-1/16*Pi^(1/2)*f^a*exp(-1/4*(ln(f)^2*b^2
+6*I*ln(f)*b*e-12*I*d*ln(f)*c+36*d*f-9*e^2)/(3*I*f+c*ln(f)))/(-c*ln(f)-3*I*
f)^(1/2)*erf(-(-c*ln(f)-3*I*f)^(1/2)*x+1/2*(3*I*e+b*ln(f))/(-c*ln(f)-3*I*f)
^(1/2))
```

maxima [B] time = 0.50, size = 4351, normalized size = 10.31

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(f^(c*x^2+b*x+a)*cos(f*x^2+e*x+d)^3,x, algorithm="maxima")
```

```
[Out] -1/32*(sqrt(pi)*sqrt(2*c^2*log(f)^2 + 18*f^2))*(((I*c^2*f^a*e^(1/4*b^2*c*log
(f)^3/(c^2*log(f)^2 + f^2) + 9/4*c*e^2*log(f)/(c^2*log(f)^2 + 9*f^2) + 1/2*
b*e*f*log(f)/(c^2*log(f)^2 + f^2))*log(f)^2 + I*f^(a + 2)*e^(1/4*b^2*c*log(
f)^3/(c^2*log(f)^2 + f^2) + 9/4*c*e^2*log(f)/(c^2*log(f)^2 + 9*f^2) + 1/2*b
*e*f*log(f)/(c^2*log(f)^2 + f^2)))*cos(-3/4*(9*e^2*f - 36*d*f^2 - (4*c^2*d
- 2*b*c*e + b^2*f)*log(f)^2)/(c^2*log(f)^2 + 9*f^2)) + (c^2*f^a*e^(1/4*b^2*
c*log(f)^3/(c^2*log(f)^2 + f^2) + 9/4*c*e^2*log(f)/(c^2*log(f)^2 + 9*f^2) +
1/2*b*e*f*log(f)/(c^2*log(f)^2 + f^2))*log(f)^2 + f^(a + 2)*e^(1/4*b^2*c*1
og(f)^3/(c^2*log(f)^2 + f^2) + 9/4*c*e^2*log(f)/(c^2*log(f)^2 + 9*f^2) + 1/
2*b*e*f*log(f)/(c^2*log(f)^2 + f^2)))*sin(-3/4*(9*e^2*f - 36*d*f^2 - (4*c^2
*d - 2*b*c*e + b^2*f)*log(f)^2)/(c^2*log(f)^2 + 9*f^2)))*erf(1/2*(2*(c*log(
f) - 3*I*f)*x + b*log(f) - 3*I*e)*sqrt(-c*log(f) + 3*I*f)/(c*log(f) - 3*I*f
)) + ((-I*c^2*f^a*e^(1/4*b^2*c*log(f)^3/(c^2*log(f)^2 + f^2) + 9/4*c*e^2*lo
g(f)/(c^2*log(f)^2 + 9*f^2) + 1/2*b*e*f*log(f)/(c^2*log(f)^2 + f^2))*log(f)
^2 - I*f^(a + 2)*e^(1/4*b^2*c*log(f)^3/(c^2*log(f)^2 + f^2) + 9/4*c*e^2*log
(f)/(c^2*log(f)^2 + 9*f^2) + 1/2*b*e*f*log(f)/(c^2*log(f)^2 + f^2)))*cos(-3
/4*(9*e^2*f - 36*d*f^2 - (4*c^2*d - 2*b*c*e + b^2*f)*log(f)^2)/(c^2*log(f)^
2 + 9*f^2)) + (c^2*f^a*e^(1/4*b^2*c*log(f)^3/(c^2*log(f)^2 + f^2) + 9/4*c*e
^2*log(f)/(c^2*log(f)^2 + 9*f^2) + 1/2*b*e*f*log(f)/(c^2*log(f)^2 + f^2))*l
og(f)^2 + f^(a + 2)*e^(1/4*b^2*c*log(f)^3/(c^2*log(f)^2 + f^2) + 9/4*c*e^2*
log(f)/(c^2*log(f)^2 + 9*f^2) + 1/2*b*e*f*log(f)/(c^2*log(f)^2 + f^2)))*sin
(-3/4*(9*e^2*f - 36*d*f^2 - (4*c^2*d - 2*b*c*e + b^2*f)*log(f)^2)/(c^2*log(
f)^2 + 9*f^2)))*erf(1/2*(2*(c*log(f) + 3*I*f)*x + b*log(f) + 3*I*e)*sqrt(-c
*log(f) - 3*I*f)/(c*log(f) + 3*I*f)))*sqrt(c*log(f) + sqrt(c^2*log(f)^2 + 9
*f^2)) + sqrt(pi)*sqrt(2*c^2*log(f)^2 + 2*f^2))*(((3*I*c^2*f^a*e^(1/4*b^2*c*
log(f)^3/(c^2*log(f)^2 + 9*f^2) + 1/4*c*e^2*log(f)/(c^2*log(f)^2 + f^2) + 9
/2*b*e*f*log(f)/(c^2*log(f)^2 + 9*f^2))*log(f)^2 + 27*I*f^(a + 2)*e^(1/4*b^
2*c*log(f)^3/(c^2*log(f)^2 + 9*f^2) + 1/4*c*e^2*log(f)/(c^2*log(f)^2 + f^2)
+ 9/2*b*e*f*log(f)/(c^2*log(f)^2 + 9*f^2)))*cos(-1/4*(e^2*f - 4*d*f^2 - (4
*c^2*d - 2*b*c*e + b^2*f)*log(f)^2)/(c^2*log(f)^2 + f^2)) + 3*(c^2*f^a*e^(1
/4*b^2*c*log(f)^3/(c^2*log(f)^2 + 9*f^2) + 1/4*c*e^2*log(f)/(c^2*log(f)^2 +
f^2) + 9/2*b*e*f*log(f)/(c^2*log(f)^2 + 9*f^2))*log(f)^2 + 9*f^(a + 2)*e^(
1/4*b^2*c*log(f)^3/(c^2*log(f)^2 + 9*f^2) + 1/4*c*e^2*log(f)/(c^2*log(f)^2
+ f^2) + 9/2*b*e*f*log(f)/(c^2*log(f)^2 + 9*f^2)))*sin(-1/4*(e^2*f - 4*d*f^
2 - (4*c^2*d - 2*b*c*e + b^2*f)*log(f)^2)/(c^2*log(f)^2 + f^2)))*erf(1/2*(2
*(c*log(f) - I*f)*x + b*log(f) - I*e)*sqrt(-c*log(f) + I*f)/(c*log(f) - I*f
)) + ((-3*I*c^2*f^a*e^(1/4*b^2*c*log(f)^3/(c^2*log(f)^2 + 9*f^2) + 1/4*c*e^
2*log(f)/(c^2*log(f)^2 + f^2) + 9/2*b*e*f*log(f)/(c^2*log(f)^2 + 9*f^2))*l
og(f)^2 - 27*I*f^(a + 2)*e^(1/4*b^2*c*log(f)^3/(c^2*log(f)^2 + 9*f^2) + 1/4*
c*e^2*log(f)/(c^2*log(f)^2 + f^2) + 9/2*b*e*f*log(f)/(c^2*log(f)^2 + 9*f^2)
))*cos(-1/4*(e^2*f - 4*d*f^2 - (4*c^2*d - 2*b*c*e + b^2*f)*log(f)^2)/(c^2*1
```

$$\begin{aligned}
& \log(f)^2 + f^2)) + 3*(c^2*f^a*e^{(1/4*b^2*c*\log(f))^3/(c^2*\log(f)^2 + 9*f^2)} + \\
& 1/4*c*e^2*\log(f)/(c^2*\log(f)^2 + f^2) + 9/2*b*e*f*\log(f)/(c^2*\log(f)^2 + 9* \\
& *f^2))*\log(f)^2 + 9*f^{(a + 2)}*e^{(1/4*b^2*c*\log(f))^3/(c^2*\log(f)^2 + 9*f^2)} \\
& + 1/4*c*e^2*\log(f)/(c^2*\log(f)^2 + f^2) + 9/2*b*e*f*\log(f)/(c^2*\log(f)^2 + \\
& 9*f^2)))*\sin(-1/4*(e^2*f - 4*d*f^2 - (4*c^2*d - 2*b*c*e + b^2*f)*\log(f)^2)/ \\
& (c^2*\log(f)^2 + f^2)))*\operatorname{erf}(1/2*(2*(c*\log(f) + I*f)*x + b*\log(f) + I*e)*\operatorname{sqrt} \\
& (-c*\log(f) - I*f)/(c*\log(f) + I*f))*\operatorname{sqrt}(c*\log(f) + \operatorname{sqrt}(c^2*\log(f)^2 + f^ \\
& 2)) - \operatorname{sqrt}(\pi)*\operatorname{sqrt}(2*c^2*\log(f)^2 + 18*f^2)*(((c^2*f^a*e^{(1/4*b^2*c*\log(f) \\
& ^3/(c^2*\log(f)^2 + f^2) + 9/4*c*e^2*\log(f)/(c^2*\log(f)^2 + 9*f^2) + 1/2*b*e \\
& *f*\log(f)/(c^2*\log(f)^2 + f^2))*\log(f)^2 + f^{(a + 2)}*e^{(1/4*b^2*c*\log(f))^3/ \\
& (c^2*\log(f)^2 + f^2) + 9/4*c*e^2*\log(f)/(c^2*\log(f)^2 + 9*f^2) + 1/2*b*e*f* \\
& \log(f)/(c^2*\log(f)^2 + f^2)))*\cos(-3/4*(9*e^2*f - 36*d*f^2 - (4*c^2*d - 2*b \\
& *c*e + b^2*f)*\log(f)^2)/(c^2*\log(f)^2 + 9*f^2)) - (I*c^2*f^a*e^{(1/4*b^2*c*1 \\
& \log(f)^3/(c^2*\log(f)^2 + f^2) + 9/4*c*e^2*\log(f)/(c^2*\log(f)^2 + 9*f^2) + 1/ \\
& 2*b*e*f*\log(f)/(c^2*\log(f)^2 + f^2))*\log(f)^2 + I*f^{(a + 2)}*e^{(1/4*b^2*c*lo \\
& \log(f))^3/(c^2*\log(f)^2 + f^2) + 9/4*c*e^2*\log(f)/(c^2*\log(f)^2 + 9*f^2) + 1/2 \\
& *b*e*f*\log(f)/(c^2*\log(f)^2 + f^2)))*\sin(-3/4*(9*e^2*f - 36*d*f^2 - (4*c^2* \\
& d - 2*b*c*e + b^2*f)*\log(f)^2)/(c^2*\log(f)^2 + 9*f^2)))*\operatorname{erf}(1/2*(2*(c*\log(f) \\
&) - 3*I*f)*x + b*\log(f) - 3*I*e)*\operatorname{sqrt}(-c*\log(f) + 3*I*f)/(c*\log(f) - 3*I*f) \\
&) + ((c^2*f^a*e^{(1/4*b^2*c*\log(f))^3/(c^2*\log(f)^2 + f^2) + 9/4*c*e^2*\log(f) \\
& / (c^2*\log(f)^2 + 9*f^2) + 1/2*b*e*f*\log(f)/(c^2*\log(f)^2 + f^2))*\log(f)^2 + \\
& f^{(a + 2)}*e^{(1/4*b^2*c*\log(f))^3/(c^2*\log(f)^2 + f^2) + 9/4*c*e^2*\log(f)/(c \\
& ^2*\log(f)^2 + 9*f^2) + 1/2*b*e*f*\log(f)/(c^2*\log(f)^2 + f^2)))*\cos(-3/4*(9* \\
& e^2*f - 36*d*f^2 - (4*c^2*d - 2*b*c*e + b^2*f)*\log(f)^2)/(c^2*\log(f)^2 + 9* \\
& f^2)) - (-I*c^2*f^a*e^{(1/4*b^2*c*\log(f))^3/(c^2*\log(f)^2 + f^2) + 9/4*c*e^2* \\
& \log(f)/(c^2*\log(f)^2 + 9*f^2) + 1/2*b*e*f*\log(f)/(c^2*\log(f)^2 + f^2))*\log(\\
& f)^2 - I*f^{(a + 2)}*e^{(1/4*b^2*c*\log(f))^3/(c^2*\log(f)^2 + f^2) + 9/4*c*e^2*1 \\
& \log(f)/(c^2*\log(f)^2 + 9*f^2) + 1/2*b*e*f*\log(f)/(c^2*\log(f)^2 + f^2)))*\sin(\\
& -3/4*(9*e^2*f - 36*d*f^2 - (4*c^2*d - 2*b*c*e + b^2*f)*\log(f)^2)/(c^2*\log(f) \\
&)^2 + 9*f^2)))*\operatorname{erf}(1/2*(2*(c*\log(f) + 3*I*f)*x + b*\log(f) + 3*I*e)*\operatorname{sqrt}(-c* \\
& \log(f) - 3*I*f)/(c*\log(f) + 3*I*f))*\operatorname{sqrt}(-c*\log(f) + \operatorname{sqrt}(c^2*\log(f)^2 + 9 \\
& *f^2)) - \operatorname{sqrt}(\pi)*\operatorname{sqrt}(2*c^2*\log(f)^2 + 2*f^2)*((3*(c^2*f^a*e^{(1/4*b^2*c*lo \\
& \log(f))^3/(c^2*\log(f)^2 + 9*f^2) + 1/4*c*e^2*\log(f)/(c^2*\log(f)^2 + f^2) + 9/2 \\
& *b*e*f*\log(f)/(c^2*\log(f)^2 + 9*f^2))*\log(f)^2 + 9*f^{(a + 2)}*e^{(1/4*b^2*c*1 \\
& \log(f))^3/(c^2*\log(f)^2 + 9*f^2) + 1/4*c*e^2*\log(f)/(c^2*\log(f)^2 + f^2) + 9/ \\
& 2*b*e*f*\log(f)/(c^2*\log(f)^2 + 9*f^2)))*\cos(-1/4*(e^2*f - 4*d*f^2 - (4*c^2* \\
& d - 2*b*c*e + b^2*f)*\log(f)^2)/(c^2*\log(f)^2 + f^2)) - (3*I*c^2*f^a*e^{(1/4* \\
& b^2*c*\log(f))^3/(c^2*\log(f)^2 + 9*f^2) + 1/4*c*e^2*\log(f)/(c^2*\log(f)^2 + f^ \\
& 2) + 9/2*b*e*f*\log(f)/(c^2*\log(f)^2 + 9*f^2))*\log(f)^2 + 27*I*f^{(a + 2)}*e^{(\\
& 1/4*b^2*c*\log(f))^3/(c^2*\log(f)^2 + 9*f^2) + 1/4*c*e^2*\log(f)/(c^2*\log(f)^2 \\
& + f^2) + 9/2*b*e*f*\log(f)/(c^2*\log(f)^2 + 9*f^2)))*\sin(-1/4*(e^2*f - 4*d*f^ \\
& 2 - (4*c^2*d - 2*b*c*e + b^2*f)*\log(f)^2)/(c^2*\log(f)^2 + f^2)))*\operatorname{erf}(1/2*(2 \\
& *(c*\log(f) - I*f)*x + b*\log(f) - I*e)*\operatorname{sqrt}(-c*\log(f) + I*f)/(c*\log(f) - I*f \\
&)) + (3*(c^2*f^a*e^{(1/4*b^2*c*\log(f))^3/(c^2*\log(f)^2 + 9*f^2) + 1/4*c*e^2*1 \\
& \log(f)/(c^2*\log(f)^2 + f^2) + 9/2*b*e*f*\log(f)/(c^2*\log(f)^2 + 9*f^2))*\log(f) \\
&)^2 + 9*f^{(a + 2)}*e^{(1/4*b^2*c*\log(f))^3/(c^2*\log(f)^2 + 9*f^2) + 1/4*c*e^2* \\
& \log(f)/(c^2*\log(f)^2 + f^2) + 9/2*b*e*f*\log(f)/(c^2*\log(f)^2 + 9*f^2)))*\cos \\
& (-1/4*(e^2*f - 4*d*f^2 - (4*c^2*d - 2*b*c*e + b^2*f)*\log(f)^2)/(c^2*\log(f)^ \\
& 2 + f^2)) - (-3*I*c^2*f^a*e^{(1/4*b^2*c*\log(f))^3/(c^2*\log(f)^2 + 9*f^2) + 1/ \\
& 4*c*e^2*\log(f)/(c^2*\log(f)^2 + f^2) + 9/2*b*e*f*\log(f)/(c^2*\log(f)^2 + 9*f^ \\
& 2))*\log(f)^2 - 27*I*f^{(a + 2)}*e^{(1/4*b^2*c*\log(f))^3/(c^2*\log(f)^2 + 9*f^2) \\
& + 1/4*c*e^2*\log(f)/(c^2*\log(f)^2 + f^2) + 9/2*b*e*f*\log(f)/(c^2*\log(f)^2 + \\
& 9*f^2)))*\sin(-1/4*(e^2*f - 4*d*f^2 - (4*c^2*d - 2*b*c*e + b^2*f)*\log(f)^2)/ \\
& (c^2*\log(f)^2 + f^2)))*\operatorname{erf}(1/2*(2*(c*\log(f) + I*f)*x + b*\log(f) + I*e)*\operatorname{sqrt} \\
& (-c*\log(f) - I*f)/(c*\log(f) + I*f))*\operatorname{sqrt}(-c*\log(f) + \operatorname{sqrt}(c^2*\log(f)^2 + f \\
& ^2)))/(c^4*e^{(1/4*b^2*c*\log(f))^3/(c^2*\log(f)^2 + 9*f^2) + 1/4*b^2*c*\log(f)^ \\
& 3/(c^2*\log(f)^2 + f^2) + 9/2*b*e*f*\log(f)/(c^2*\log(f)^2 + 9*f^2) + 1/2*b*e* \\
& f*\log(f)/(c^2*\log(f)^2 + f^2))*\log(f)^4 + 10*c^2*f^2*e^{(1/4*b^2*c*\log(f))^3/ \\
& (c^2*\log(f)^2 + 9*f^2) + 1/4*b^2*c*\log(f)^3/(c^2*\log(f)^2 + f^2) + 9/2*b*e*
\end{aligned}$$


```
f*log(f)/(c^2*log(f)^2 + 9*f^2) + 1/2*b*e*f*log(f)/(c^2*log(f)^2 + f^2))*lo
g(f)^2 + 9*f^4*e^(1/4*b^2*c*log(f)^3/(c^2*log(f)^2 + 9*f^2) + 1/4*b^2*c*log
(f)^3/(c^2*log(f)^2 + f^2) + 9/2*b*e*f*log(f)/(c^2*log(f)^2 + 9*f^2) + 1/2*
b*e*f*log(f)/(c^2*log(f)^2 + f^2)))
```

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int f^{cx^2+bx+a} \cos(fx^2 + ex + d)^3 dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(f^(a + b*x + c*x^2)*cos(d + e*x + f*x^2)^3,x)
```

```
[Out] int(f^(a + b*x + c*x^2)*cos(d + e*x + f*x^2)^3, x)
```

sympy [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(f**(c*x**2+b*x+a)*cos(f*x**2+e*x+d)**3,x)
```

```
[Out] Timed out
```

3.134 $\int f^{a+bx+cx^2} \cos(a + bx + ex^2) dx$

Optimal. Leaf size=209

$$\frac{\sqrt{\pi} \exp\left(-\left(-\log(f) + i\right)\left(a - \frac{b^2(-\log(f)+i)}{-4c\log(f)+4ie}\right)\right) \operatorname{erf}\left(\frac{b(-\log(f)+i)+2x(-c\log(f)+ie)}{2\sqrt{-c\log(f)+ie}}\right)}{4\sqrt{-c\log(f)+ie}} + \frac{\sqrt{\pi} \exp\left((\log(f) + i)\left(a - \frac{b^2(\log(f)+i)}{4c\log(f)+4ie}\right)\right) \operatorname{erfi}\left(\frac{b(\log(f)+i)+2x(c\log(f)+ie)}{2\sqrt{c\log(f)+ie}}\right)}{4\sqrt{c\log(f)+ie}}$$

[Out] $-1/4*\operatorname{erf}(1/2*(-b*(I-\ln(f))-2*x*(I*e-c*\ln(f)))/(I*e-c*\ln(f))^{(1/2)})*\operatorname{Pi}^{(1/2)}/\exp((I-\ln(f))*(a-b^2*(I-\ln(f)))/(4*I*e-4*c*\ln(f)))/(I*e-c*\ln(f))^{(1/2)+1/4}* \exp((I+\ln(f))*(a-b^2*(I+\ln(f)))/(4*I*e+4*c*\ln(f)))*\operatorname{erfi}(1/2*(b*(I+\ln(f))+2*x*(I*e+c*\ln(f)))/(I*e+c*\ln(f))^{(1/2)})*\operatorname{Pi}^{(1/2)}/(I*e+c*\ln(f))^{(1/2)}$

Rubi [A] time = 0.48, antiderivative size = 209, normalized size of antiderivative = 1.00, number of steps used = 8, number of rules used = 5, integrand size = 24, $\frac{\text{number of rules}}{\text{integrand size}} = 0.208$, Rules used = {4473, 2287, 2234, 2205, 2204}

$$\frac{\sqrt{\pi} \exp\left(-\left(-\log(f) + i\right)\left(a - \frac{b^2(-\log(f)+i)}{-4c\log(f)+4ie}\right)\right) \operatorname{Erf}\left(\frac{b(-\log(f)+i)+2x(-c\log(f)+ie)}{2\sqrt{-c\log(f)+ie}}\right)}{4\sqrt{-c\log(f)+ie}} + \frac{\sqrt{\pi} \exp\left((\log(f) + i)\left(a - \frac{b^2(\log(f)+i)}{4c\log(f)+4ie}\right)\right) \operatorname{Erfi}\left(\frac{b(\log(f)+i)+2x(c\log(f)+ie)}{2\sqrt{c\log(f)+ie}}\right)}{4\sqrt{c\log(f)+ie}}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[f^{(a + b*x + c*x^2)}*\operatorname{Cos}[a + b*x + e*x^2], x]$

[Out] $(\operatorname{Sqrt}[\operatorname{Pi}]*\operatorname{Erf}[(b*(I - \operatorname{Log}[f]) + 2*x*(I*e - c*\operatorname{Log}[f]))/(2*\operatorname{Sqrt}[I*e - c*\operatorname{Log}[f]])])/(4*E^{((I - \operatorname{Log}[f])*(a - (b^2*(I - \operatorname{Log}[f]))/((4*I)*e - 4*c*\operatorname{Log}[f])))*\operatorname{Sqrt}[I*e - c*\operatorname{Log}[f]]}) + (E^{((I + \operatorname{Log}[f])*(a - (b^2*(I + \operatorname{Log}[f]))/((4*I)*e + 4*c*\operatorname{Log}[f])))*\operatorname{Sqrt}[I*e + c*\operatorname{Log}[f]]})*\operatorname{Sqrt}[\operatorname{Pi}]*\operatorname{Erfi}[(b*(I + \operatorname{Log}[f]) + 2*x*(I*e + c*\operatorname{Log}[f]))/(2*\operatorname{Sqrt}[I*e + c*\operatorname{Log}[f]])])/(4*\operatorname{Sqrt}[I*e + c*\operatorname{Log}[f]])]$

Rule 2204

$\operatorname{Int}[(F_)^{((a_.) + (b_.)*((c_.) + (d_.)*(x_)^2))}, x_Symbol] := \operatorname{Simp}[(F^a*\operatorname{Sqrt}[\operatorname{Pi}]*\operatorname{Erfi}[(c + d*x)*\operatorname{Rt}[b*\operatorname{Log}[F], 2]])/(2*d*\operatorname{Rt}[b*\operatorname{Log}[F], 2]), x] /; \operatorname{FreeQ}\{F, a, b, c, d\}, x] \&\& \operatorname{PosQ}[b]$

Rule 2205

$\operatorname{Int}[(F_)^{((a_.) + (b_.)*((c_.) + (d_.)*(x_)^2))}, x_Symbol] := \operatorname{Simp}[(F^a*\operatorname{Sqrt}[\operatorname{Pi}]*\operatorname{Erf}[(c + d*x)*\operatorname{Rt}[-(b*\operatorname{Log}[F]), 2]])/(2*d*\operatorname{Rt}[-(b*\operatorname{Log}[F]), 2]), x] /; \operatorname{FreeQ}\{F, a, b, c, d\}, x] \&\& \operatorname{NegQ}[b]$

Rule 2234

$\operatorname{Int}[(F_)^{((a_.) + (b_.)*(x_) + (c_.)*(x_)^2))}, x_Symbol] := \operatorname{Dist}[F^{(a - b^2/(4*c))}, \operatorname{Int}[F^{((b + 2*c*x)^2/(4*c))}, x], x] /; \operatorname{FreeQ}\{F, a, b, c\}, x]$

Rule 2287

$\operatorname{Int}[(u_)*(F_)^{(v_)*(G_)^{(w_)}}], x_Symbol] := \operatorname{With}\{z = v*\operatorname{Log}[F] + w*\operatorname{Log}[G]\}, \operatorname{Int}[u*\operatorname{NormalizeIntegrand}[E^z, x], x] /; \operatorname{BinomialQ}[z, x] \|\| (\operatorname{PolynomialQ}[z, x] \&\& \operatorname{LeQ}[\operatorname{Exponent}[z, x], 2]) /; \operatorname{FreeQ}\{F, G\}, x]$

Rule 4473

$\operatorname{Int}[\operatorname{Cos}[v_]^{(n_.)*(F_)^{(u_)}}], x_Symbol] := \operatorname{Int}[\operatorname{ExpandTrigToExp}[F^u, \operatorname{Cos}[v]^{(n)}, x], x] /; \operatorname{FreeQ}[F, x] \&\& (\operatorname{LinearQ}[u, x] \|\| \operatorname{PolyQ}[u, x, 2]) \&\& (\operatorname{LinearQ}[v, x] \|\| \operatorname{PolyQ}[v, x, 2]) \&\& \operatorname{IGtQ}[n, 0]$

Rubi steps

$$\begin{aligned}
\int f^{a+bx+cx^2} \cos(a+bx+ex^2) dx &= \int \left(\frac{1}{2} e^{-ia-ibx-ix^2} f^{a+bx+cx^2} + \frac{1}{2} e^{ia+ibx+ix^2} f^{a+bx+cx^2} \right) dx \\
&= \frac{1}{2} \int e^{-ia-ibx-ix^2} f^{a+bx+cx^2} dx + \frac{1}{2} \int e^{ia+ibx+ix^2} f^{a+bx+cx^2} dx \\
&= \frac{1}{2} \int \exp(-a(i-\log(f)) - bx(i-\log(f)) - x^2(ie-c\log(f))) dx + \frac{1}{2} \int \exp(a(i-\log(f)) + bx(i-\log(f)) + x^2(ie-c\log(f))) dx \\
&= \frac{1}{2} \exp\left(-i(i-\log(f))\left(a - \frac{b^2(i-\log(f))}{4ie-4c\log(f)}\right)\right) \int \exp\left(\frac{(-b(i-\log(f)) + 2cx(i-\log(f)) - x^2(ie-c\log(f)))}{4(-ie+c\log(f))}\right) dx \\
&\quad + \frac{1}{2} \exp\left(i(i-\log(f))\left(a - \frac{b^2(i-\log(f))}{4ie-4c\log(f)}\right)\right) \int \exp\left(\frac{(b(i-\log(f)) + 2cx(i-\log(f)) - x^2(ie-c\log(f)))}{4(-ie+c\log(f))}\right) dx \\
&= \frac{\exp\left(-i(i-\log(f))\left(a - \frac{b^2(i-\log(f))}{4ie-4c\log(f)}\right)\right) \sqrt{\pi} \operatorname{erf}\left(\frac{b(i-\log(f)) + 2cx(i-\log(f)) - x^2(ie-c\log(f))}{2\sqrt{ie-c\log(f)}}\right) e^{-a(i-\log(f)) - bx(i-\log(f)) - x^2(ie-c\log(f))}}{4\sqrt{ie-c\log(f)}} + \frac{\exp\left(i(i-\log(f))\left(a - \frac{b^2(i-\log(f))}{4ie-4c\log(f)}\right)\right) \sqrt{\pi} \operatorname{erf}\left(\frac{b(i-\log(f)) + 2cx(i-\log(f)) - x^2(ie-c\log(f))}{2\sqrt{ie-c\log(f)}}\right) e^{a(i-\log(f)) + bx(i-\log(f)) + x^2(ie-c\log(f))}}{4\sqrt{ie-c\log(f)}}
\end{aligned}$$

Mathematica [A] time = 1.81, size = 325, normalized size = 1.56

$$i\sqrt{\pi} e^{-\frac{b^2 c \log^3(f)}{2(c^2 \log^2(f) + e^2)}} f^{a - \frac{b^2}{2(e - ic \log(f))}} \left((\cos(a) + i \sin(a))(e + ic \log(f)) \sqrt{c \log(f) + ie} \exp\left(\frac{1}{4} b^2 \left(\frac{\log^2(f)}{c \log(f) - ie} + \frac{1}{c \log(f) + ie}\right)\right) \right)$$

Warning: Unable to verify antiderivative.

[In] Integrate[f^(a + b*x + c*x^2)*Cos[a + b*x + e*x^2], x]

[Out] $((-1/4*I)*f^{(a - b^2/(2*(e - I*c*Log[f])))*Sqrt[Pi]*(-(E^{((b^2*((-I)*e + c*Log[f])^{-1} + Log[f]^2/(I*e + c*Log[f])))/4)*f^{((I*b^2*c*Log[f])/(e^2 + c^2*Log[f]^2))*Erfi[((-I)*(b + 2*e*x) + (b + 2*c*x)*Log[f])/(2*Sqrt[(-I)*e + c*Log[f]])]*(e - I*c*Log[f])*Sqrt[(-I)*e + c*Log[f]]*(Cos[a] - I*Sin[a]))} + E^{((b^2*(Log[f]^2/((-I)*e + c*Log[f]) + (I*e + c*Log[f])^{-1}))/4}*Erfi[(I*(b + 2*e*x) + (b + 2*c*x)*Log[f])/(2*Sqrt[I*e + c*Log[f]])]*(e + I*c*Log[f])*Sqrt[I*e + c*Log[f]]*(Cos[a] + I*Sin[a]))})/(E^{(b^2*c*Log[f]^3)/(2*(e^2 + c^2*Log[f]^2))})*(e^2 + c^2*Log[f]^2))$

fricas [B] time = 2.13, size = 381, normalized size = 1.82

$$\sqrt{\pi} (c \log(f) - ie) \sqrt{-c \log(f) - ie} \operatorname{erf}\left(\frac{(2e^2x + (2c^2x + bc) \log(f)^2 + be + (bc - ibe) \log(f)) \sqrt{-c \log(f) - ie}}{2(c^2 \log(f)^2 + e^2)}\right) e^{-\frac{(b^2c - 4ac^2) \log(f)^3 + ib^2}{2(c^2 \log(f)^2 + e^2)}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(c*x^2+b*x+a)*cos(e*x^2+b*x+a), x, algorithm="fricas")

[Out] $-1/4*(\operatorname{sqrt}(\pi)*(c*\log(f) - I*e)*\operatorname{sqrt}(-c*\log(f) - I*e)*\operatorname{erf}(1/2*(2*e^2*x + (2*c^2*x + b*c)*\log(f)^2 + b*e + (I*b*c - I*b*e)*\log(f))*\operatorname{sqrt}(-c*\log(f) - I*e))/(c^2*\log(f)^2 + e^2))*e^{-1/4*((b^2*c - 4*a*c^2)*\log(f)^3 + I*b^2*e - 4*I*a*e^2 - (-2*I*b^2*c + 4*I*a*c^2 + I*b^2*e)*\log(f)^2 - (b^2*c - 2*b^2*e + 4*a*e^2)*\log(f))/(c^2*\log(f)^2 + e^2)} + \operatorname{sqrt}(\pi)*(c*\log(f) + I*e)*\operatorname{sqrt}(-c*\log(f) + I*e)*\operatorname{erf}(1/2*(2*e^2*x + (2*c^2*x + b*c)*\log(f)^2 + b*e + (-I*b*c + I*b*e)*\log(f))*\operatorname{sqrt}(-c*\log(f) + I*e))/(c^2*\log(f)^2 + e^2))*e^{-1/4*((b^2*c - 4*a*c^2)*\log(f)^3 - I*b^2*e + 4*I*a*e^2 - (2*I*b^2*c - 4*I*a*c^2 - I*b^2*e)*\log(f)^2 - (b^2*c - 2*b^2*e + 4*a*e^2)*\log(f))/(c^2*\log(f)^2 + e^2)))/(c^2*\log(f)^2 + e^2)$

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int f^{cx^2+bx+a} \cos(ex^2 + bx + a) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(c*x^2+b*x+a)*cos(e*x^2+b*x+a),x, algorithm="giac")

[Out] integrate(f^(c*x^2 + b*x + a)*cos(e*x^2 + b*x + a), x)

maple [A] time = 0.20, size = 215, normalized size = 1.03

$$\frac{\sqrt{\pi} f^a e^{\frac{4ae-b^2+4i\ln(f)ac-2i\ln(f)b^2+\ln(f)^2b^2}{4(-ie+c\ln(f))}} \operatorname{erf}\left(-\sqrt{ie-c\ln(f)} x + \frac{-ib+b\ln(f)}{2\sqrt{ie-c\ln(f)}}\right)}{4\sqrt{ie-c\ln(f)}} - \frac{\sqrt{\pi} f^a e^{\frac{-4ae+b^2+4i\ln(f)ac-2i\ln(f)b^2-\ln(f)^2b^2}{4ie+4c\ln(f)}} \operatorname{erf}\left(\dots\right)}{4\sqrt{-ie-c\ln(f)}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(f^(c*x^2+b*x+a)*cos(e*x^2+b*x+a),x)

[Out] $-1/4*\text{Pi}^{(1/2)}*f^a*\exp(-1/4*(4*a*e-b^2+4*I*\ln(f)*a*c-2*I*\ln(f)*b^2+\ln(f)^2*b^2)/(-I*e+c*\ln(f)))/(I*e-c*\ln(f))^{(1/2)}*\operatorname{erf}(- (I*e-c*\ln(f))^{(1/2)}*x+1/2*(-I*b+b*\ln(f))/(I*e-c*\ln(f))) - 1/4*\text{Pi}^{(1/2)}*f^a*\exp(1/4*(-4*a*e+b^2+4*I*\ln(f)*a*c-2*I*\ln(f)*b^2-\ln(f)^2*b^2)/(I*e+c*\ln(f)))/(-I*e-c*\ln(f))^{(1/2)}*\operatorname{erf}(- (I*e-c*\ln(f))^{(1/2)}*x+1/2*(I*b+b*\ln(f))/(-I*e-c*\ln(f)))$

maxima [B] time = 0.39, size = 1018, normalized size = 4.87

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(f^(c*x^2+b*x+a)*cos(e*x^2+b*x+a),x, algorithm="maxima")

[Out] $-1/8*(\sqrt{\pi}*\sqrt{2*c^2*\log(f)^2 + 2*e^2})*((I*f^{(1/4*b^2*c/(c^2*\log(f)^2 + e^2)}*f^a*\cos(-1/4*(b^2*e - 4*a*e^2 + (2*b^2*c - 4*a*c^2 - b^2*e)*\log(f)^2)/(c^2*\log(f)^2 + e^2)) + f^{(1/4*b^2*c/(c^2*\log(f)^2 + e^2)}*f^a*\sin(-1/4*(b^2*e - 4*a*e^2 + (2*b^2*c - 4*a*c^2 - b^2*e)*\log(f)^2)/(c^2*\log(f)^2 + e^2))))*\operatorname{erf}(1/2*(2*(c*\log(f) - I*e)*x + b*\log(f) - I*b)*\sqrt{-c*\log(f) + I*e}/(c*\log(f) - I*e)) + (-I*f^{(1/4*b^2*c/(c^2*\log(f)^2 + e^2)}*f^a*\cos(-1/4*(b^2*e - 4*a*e^2 + (2*b^2*c - 4*a*c^2 - b^2*e)*\log(f)^2)/(c^2*\log(f)^2 + e^2)) + f^{(1/4*b^2*c/(c^2*\log(f)^2 + e^2)}*f^a*\sin(-1/4*(b^2*e - 4*a*e^2 + (2*b^2*c - 4*a*c^2 - b^2*e)*\log(f)^2)/(c^2*\log(f)^2 + e^2))))*\operatorname{erf}(1/2*(2*(c*\log(f) + I*e)*x + b*\log(f) + I*b)*\sqrt{-c*\log(f) - I*e}/(c*\log(f) + I*e)))*\sqrt{c*\log(f) + \sqrt{c^2*\log(f)^2 + e^2}} - \sqrt{\pi}*\sqrt{2*c^2*\log(f)^2 + 2*e^2})*((f^{(1/4*b^2*c/(c^2*\log(f)^2 + e^2)}*f^a*\cos(-1/4*(b^2*e - 4*a*e^2 + (2*b^2*c - 4*a*c^2 - b^2*e)*\log(f)^2)/(c^2*\log(f)^2 + e^2)) - I*f^{(1/4*b^2*c/(c^2*\log(f)^2 + e^2)}*f^a*\sin(-1/4*(b^2*e - 4*a*e^2 + (2*b^2*c - 4*a*c^2 - b^2*e)*\log(f)^2)/(c^2*\log(f)^2 + e^2))))*\operatorname{erf}(1/2*(2*(c*\log(f) - I*e)*x + b*\log(f) - I*b)*\sqrt{-c*\log(f) + I*e}/(c*\log(f) - I*e)) + (f^{(1/4*b^2*c/(c^2*\log(f)^2 + e^2)}*f^a*\cos(-1/4*(b^2*e - 4*a*e^2 + (2*b^2*c - 4*a*c^2 - b^2*e)*\log(f)^2)/(c^2*\log(f)^2 + e^2)) + I*f^{(1/4*b^2*c/(c^2*\log(f)^2 + e^2)}*f^a*\sin(-1/4*(b^2*e - 4*a*e^2 + (2*b^2*c - 4*a*c^2 - b^2*e)*\log(f)^2)/(c^2*\log(f)^2 + e^2))))*\operatorname{erf}(1/2*(2*(c*\log(f) + I*e)*x + b*\log(f) + I*b)*\sqrt{-c*\log(f) - I*e}/(c*\log(f) + I*e)))*\sqrt{-c*\log(f) + \sqrt{c^2*\log(f)^2 + e^2}})/(c^2*e^{(1/4*b^2*c*\log(f)^3/(c^2*\log(f)^2 + e^2) + 1/2*b^2*e*\log(f)/(c^2*\log(f)^2 + e^2))*\log(f)^2 + e^2}*e^{(1/4*b^2*c*\log(f)^3/(c^2*\log(f)^2 + e^2) + 1/2*b^2*e*\log(f)/(c^2*\log(f)^2 + e^2))})$

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int f^{cx^2+bx+a} \cos(ex^2 + bx + a) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(f^(a + b*x + c*x^2)*cos(a + b*x + e*x^2), x)`

[Out] `int(f^(a + b*x + c*x^2)*cos(a + b*x + e*x^2), x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int f^{a+bx+cx^2} \cos(a + bx + ex^2) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(f**(c*x**2+b*x+a)*cos(e*x**2+b*x+a), x)`

[Out] `Integral(f**(a + b*x + c*x**2)*cos(a + b*x + e*x**2), x)`

3.135 $\int F^{c(a+bx)}(f + f \sin(d + ex))^2 dx$

Optimal. Leaf size=245

$$\frac{bcf^2 \log(F) \sin^2(d + ex)F^{ac+bcx}}{b^2c^2 \log^2(F) + 4e^2} + \frac{2bcf^2 \log(F) \sin(d + ex)F^{ac+bcx}}{b^2c^2 \log^2(F) + e^2} - \frac{2ef^2 \cos(d + ex)F^{ac+bcx}}{b^2c^2 \log^2(F) + e^2} - \frac{2ef^2 \sin(d + ex) \cos(d + ex)F^{ac+bcx}}{b^2c^2 \log^2(F)}$$

[Out] $f^2 F^{(b*c*x+a*c)}/b/c/\ln(F) - 2*e*f^2 F^{(b*c*x+a*c)} * \cos(e*x+d) / (e^2 + b^2*c^2*\ln(F)^2) + 2*e^2*f^2 F^{(b*c*x+a*c)}/b/c/\ln(F) / (4*e^2 + b^2*c^2*\ln(F)^2) + 2*b*c*f^2 F^{(b*c*x+a*c)} * \ln(F) * \sin(e*x+d) / (e^2 + b^2*c^2*\ln(F)^2) - 2*e*f^2 F^{(b*c*x+a*c)} * \cos(e*x+d) * \sin(e*x+d) / (4*e^2 + b^2*c^2*\ln(F)^2) + b*c*f^2 F^{(b*c*x+a*c)} * \ln(F) * \sin(e*x+d)^2 / (4*e^2 + b^2*c^2*\ln(F)^2)$

Rubi [A] time = 0.36, antiderivative size = 245, normalized size of antiderivative = 1.00, number of steps used = 8, number of rules used = 6, integrand size = 22, $\frac{\text{number of rules}}{\text{integrand size}} = 0.273$, Rules used = {6741, 12, 6742, 2194, 4432, 4434}

$$\frac{bcf^2 \log(F) \sin^2(d + ex)F^{ac+bcx}}{b^2c^2 \log^2(F) + 4e^2} + \frac{2bcf^2 \log(F) \sin(d + ex)F^{ac+bcx}}{b^2c^2 \log^2(F) + e^2} - \frac{2ef^2 \cos(d + ex)F^{ac+bcx}}{b^2c^2 \log^2(F) + e^2} - \frac{2ef^2 \sin(d + ex) \cos(d + ex)F^{ac+bcx}}{b^2c^2 \log^2(F)}$$

Antiderivative was successfully verified.

[In] Int[F^(c*(a + b*x))*(f + f*Sin[d + e*x])^2, x]

[Out] $(f^2 F^{(a*c + b*c*x)}) / (b*c*Log[F]) - (2*e*f^2 F^{(a*c + b*c*x)} * Cos[d + e*x]) / (e^2 + b^2*c^2*Log[F]^2) + (2*e^2*f^2 F^{(a*c + b*c*x)}) / (b*c*Log[F] * (4*e^2 + b^2*c^2*Log[F]^2)) + (2*b*c*f^2 F^{(a*c + b*c*x)} * Log[F] * Sin[d + e*x]) / (e^2 + b^2*c^2*Log[F]^2) - (2*e*f^2 F^{(a*c + b*c*x)} * Cos[d + e*x] * Sin[d + e*x]) / (4*e^2 + b^2*c^2*Log[F]^2) + (b*c*f^2 F^{(a*c + b*c*x)} * Log[F] * Sin[d + e*x]^2) / (4*e^2 + b^2*c^2*Log[F]^2)$

Rule 12

Int[(a_)*(u_), x_Symbol] := Dist[a, Int[u, x], x] /; FreeQ[a, x] && !MatchQ[u, (b_)*(v_)] /; FreeQ[b, x]

Rule 2194

Int[((F_)^((c_)*((a_) + (b_)*(x_))))^(n_), x_Symbol] := Simp[(F^(c*(a + b*x)))^n/(b*c*n*Log[F]), x] /; FreeQ[{F, a, b, c, n}, x]

Rule 4432

Int[(F_)^((c_)*((a_) + (b_)*(x_)))*Sin[(d_) + (e_)*(x_)], x_Symbol] := Simp[(b*c*Log[F]*F^(c*(a + b*x))*Sin[d + e*x]/(e^2 + b^2*c^2*Log[F]^2), x] - Simp[(e*f^(c*(a + b*x))*Cos[d + e*x]/(e^2 + b^2*c^2*Log[F]^2), x] /; FreeQ[{F, a, b, c, d, e}, x] && NeQ[e^2 + b^2*c^2*Log[F]^2, 0]

Rule 4434

Int[(F_)^((c_)*((a_) + (b_)*(x_)))*Sin[(d_) + (e_)*(x_)]^(n_), x_Symbol] := Simp[(b*c*Log[F]*F^(c*(a + b*x))*Sin[d + e*x]^n/(e^2*n^2 + b^2*c^2*Log[F]^2), x] + (Dist[(n*(n - 1)*e^2)/(e^2*n^2 + b^2*c^2*Log[F]^2), Int[F^(c*(a + b*x))*Sin[d + e*x]^(n - 2), x], x] - Simp[(e*n*f^(c*(a + b*x))*Cos[d + e*x]*Sin[d + e*x]^(n - 1)/(e^2*n^2 + b^2*c^2*Log[F]^2), x]) /; FreeQ[{F, a, b, c, d, e}, x] && NeQ[e^2*n^2 + b^2*c^2*Log[F]^2, 0] && GtQ[n, 1]

Rule 6741

Int[u_, x_Symbol] :=> With[{v = NormalizeIntegrand[u, x]}, Int[v, x] /; v != u]

Rule 6742

Int[u_, x_Symbol] :=> With[{v = ExpandIntegrand[u, x]}, Int[v, x] /; SumQ[v]

Rubi steps

$$\begin{aligned}
 \int F^{c(a+bx)}(f + f \sin(d + ex))^2 dx &= \int f^2 F^{ac+bcx}(1 + \sin(d + ex))^2 dx \\
 &= f^2 \int F^{ac+bcx}(1 + \sin(d + ex))^2 dx \\
 &= f^2 \int (F^{ac+bcx} + 2F^{ac+bcx} \sin(d + ex) + F^{ac+bcx} \sin^2(d + ex)) dx \\
 &= f^2 \int F^{ac+bcx} dx + f^2 \int F^{ac+bcx} \sin^2(d + ex) dx + (2f^2) \int F^{ac+bcx} \sin(d + ex) dx \\
 &= \frac{f^2 F^{ac+bcx}}{bc \log(F)} - \frac{2ef^2 F^{ac+bcx} \cos(d + ex)}{e^2 + b^2 c^2 \log^2(F)} + \frac{2bc f^2 F^{ac+bcx} \log(F) \sin(d + ex)}{e^2 + b^2 c^2 \log^2(F)} - \frac{2bc^2 f^2 F^{ac+bcx} \log^2(F) \cos(d + ex)}{e^2 + b^2 c^2 \log^2(F)} \\
 &= \frac{f^2 F^{ac+bcx}}{bc \log(F)} - \frac{2ef^2 F^{ac+bcx} \cos(d + ex)}{e^2 + b^2 c^2 \log^2(F)} + \frac{2e^2 f^2 F^{ac+bcx}}{bc \log(F) (4e^2 + b^2 c^2 \log^2(F))} + \frac{2bc^2 f^2 F^{ac+bcx} \log^2(F) \cos(d + ex)}{e^2 + b^2 c^2 \log^2(F)}
 \end{aligned}$$

Mathematica [A] time = 1.63, size = 180, normalized size = 0.73

$$\frac{f^2 (\sin(d + ex) + 1)^2 F^{c(a+bx)} \left(\frac{4bc \log(F) \sin(d+ex)}{b^2 c^2 \log^2(F) + e^2} - \frac{2e \sin(2(d+ex))}{b^2 c^2 \log^2(F) + 4e^2} - \frac{4e \cos(d+ex)}{b^2 c^2 \log^2(F) + e^2} - \frac{bc \log(F) \cos(2(d+ex))}{b^2 c^2 \log^2(F) + 4e^2} + \frac{3}{bc \log(F)} \right)}{2 \left(\sin\left(\frac{1}{2}(d + ex)\right) + \cos\left(\frac{1}{2}(d + ex)\right) \right)^4}$$

Antiderivative was successfully verified.

[In] Integrate[F^(c*(a + b*x))*(f + f*Sin[d + e*x])^2,x]

[Out] (f^2 F^(c*(a + b*x))*(1 + Sin[d + e*x])^2*(3/(b*c*Log[F]) - (4*e*Cos[d + e*x])/(e^2 + b^2*c^2*Log[F]^2) - (b*c*Cos[2*(d + e*x)]*Log[F])/(4*e^2 + b^2*c^2*Log[F]^2) + (4*b*c*Log[F]*Sin[d + e*x])/(e^2 + b^2*c^2*Log[F]^2) - (2*e*Sin[2*(d + e*x)])/(4*e^2 + b^2*c^2*Log[F]^2)))/(2*(Cos[(d + e*x)/2] + Sin[(d + e*x)/2])^4)

fricas [A] time = 0.71, size = 256, normalized size = 1.04

$$\frac{(2 b^3 c^3 e f^2 \cos(ex + d) \log(F)^3 + 8 b c e^3 f^2 \cos(ex + d) \log(F) - 6 e^4 f^2 + (b^4 c^4 f^2 \cos(ex + d)^2 - 2 b^4 c^4 f^2) \log(F))}{2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(F^(c*(b*x+a))*(f+f*sin(e*x+d))^2,x, algorithm="fricas")

[Out] -(2*b^3*c^3*e*f^2*cos(e*x + d)*log(F)^3 + 8*b*c*e^3*f^2*cos(e*x + d)*log(F) - 6*e^4*f^2 + (b^4*c^4*f^2*cos(e*x + d)^2 - 2*b^4*c^4*f^2)*log(F)^4 + (b^2*c^2*e^2*f^2*cos(e*x + d)^2 - 8*b^2*c^2*e^2*f^2)*log(F)^2 - 2*(b^4*c^4*f^2*log(F)^4 - b^3*c^3*e*f^2*cos(e*x + d)*log(F)^3 + 4*b^2*c^2*e^2*f^2*log(F)^2 - b*c*e^3*f^2*cos(e*x + d)*log(F))*sin(e*x + d))*F^(b*c*x + a*c)/(b^5*c^5*log(F)^5 + 5*b^3*c^3*e^2*log(F)^3 + 4*b*c*e^4*log(F))

giac [C] time = 0.38, size = 1774, normalized size = 7.24

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(F^(c*(b*x+a))*(f+f*sin(e*x+d))^2,x, algorithm="giac")

[Out]
$$-1/2*(2*b*c*f^2*\cos(1/2*\pi*b*c*x*\operatorname{sgn}(F) - 1/2*\pi*b*c*x + 1/2*\pi*a*c*\operatorname{sgn}(F) - 1/2*\pi*a*c + 2*x*e + 2*d)*\log(\operatorname{abs}(F))/(4*b^2*c^2*\log(\operatorname{abs}(F))^2 + (\pi*b*c*\operatorname{sgn}(F) - \pi*b*c + 4*e)^2) + (\pi*b*c*\operatorname{sgn}(F) - \pi*b*c + 4*e)*f^2*\sin(1/2*\pi*b*c*x*\operatorname{sgn}(F) - 1/2*\pi*b*c*x + 1/2*\pi*a*c*\operatorname{sgn}(F) - 1/2*\pi*a*c + 2*x*e + 2*d)/(4*b^2*c^2*\log(\operatorname{abs}(F))^2 + (\pi*b*c*\operatorname{sgn}(F) - \pi*b*c + 4*e)^2)*e^{(b*c*x*\log(\operatorname{abs}(F)) + a*c*\log(\operatorname{abs}(F)))} - 1/2*(2*b*c*f^2*\cos(1/2*\pi*b*c*x*\operatorname{sgn}(F) - 1/2*\pi*b*c*x + 1/2*\pi*a*c*\operatorname{sgn}(F) - 1/2*\pi*a*c - 2*x*e - 2*d)*\log(\operatorname{abs}(F))/(4*b^2*c^2*\log(\operatorname{abs}(F))^2 + (\pi*b*c*\operatorname{sgn}(F) - \pi*b*c - 4*e)^2) + (\pi*b*c*\operatorname{sgn}(F) - \pi*b*c - 4*e)*f^2*\sin(1/2*\pi*b*c*x*\operatorname{sgn}(F) - 1/2*\pi*b*c*x + 1/2*\pi*a*c*\operatorname{sgn}(F) - 1/2*\pi*a*c - 2*x*e - 2*d)/(4*b^2*c^2*\log(\operatorname{abs}(F))^2 + (\pi*b*c*\operatorname{sgn}(F) - \pi*b*c - 4*e)^2)*e^{(b*c*x*\log(\operatorname{abs}(F)) + a*c*\log(\operatorname{abs}(F)))} + 3*(2*b*c*f^2*\cos(-1/2*\pi*b*c*x*\operatorname{sgn}(F) + 1/2*\pi*b*c*x - 1/2*\pi*a*c*\operatorname{sgn}(F) + 1/2*\pi*a*c)*\log(\operatorname{abs}(F))/(4*b^2*c^2*\log(\operatorname{abs}(F))^2 + (\pi*b*c*\operatorname{sgn}(F) - \pi*b*c)^2) - (\pi*b*c*\operatorname{sgn}(F) - \pi*b*c)*f^2*\sin(-1/2*\pi*b*c*x*\operatorname{sgn}(F) + 1/2*\pi*b*c*x - 1/2*\pi*a*c*\operatorname{sgn}(F) + 1/2*\pi*a*c)/(4*b^2*c^2*\log(\operatorname{abs}(F))^2 + (\pi*b*c*\operatorname{sgn}(F) - \pi*b*c)^2)*e^{(b*c*x*\log(\operatorname{abs}(F)) + a*c*\log(\operatorname{abs}(F)))} + 2*(2*b*c*f^2*\log(\operatorname{abs}(F))*\sin(1/2*\pi*b*c*x*\operatorname{sgn}(F) - 1/2*\pi*b*c*x + 1/2*\pi*a*c*\operatorname{sgn}(F) - 1/2*\pi*a*c + x*e + d)/(4*b^2*c^2*\log(\operatorname{abs}(F))^2 + (\pi*b*c*\operatorname{sgn}(F) - \pi*b*c + 2*e)^2) - (\pi*b*c*\operatorname{sgn}(F) - \pi*b*c + 2*e)*f^2*\cos(1/2*\pi*b*c*x*\operatorname{sgn}(F) - 1/2*\pi*b*c*x + 1/2*\pi*a*c*\operatorname{sgn}(F) - 1/2*\pi*a*c + x*e + d)/(4*b^2*c^2*\log(\operatorname{abs}(F))^2 + (\pi*b*c*\operatorname{sgn}(F) - \pi*b*c + 2*e)^2)*e^{(b*c*x*\log(\operatorname{abs}(F)) + a*c*\log(\operatorname{abs}(F)))} - 2*(2*b*c*f^2*\log(\operatorname{abs}(F))*\sin(1/2*\pi*b*c*x*\operatorname{sgn}(F) - 1/2*\pi*b*c*x + 1/2*\pi*a*c*\operatorname{sgn}(F) - 1/2*\pi*a*c - x*e - d)/(4*b^2*c^2*\log(\operatorname{abs}(F))^2 + (\pi*b*c*\operatorname{sgn}(F) - \pi*b*c - 2*e)^2) - (\pi*b*c*\operatorname{sgn}(F) - \pi*b*c - 2*e)*f^2*\cos(1/2*\pi*b*c*x*\operatorname{sgn}(F) - 1/2*\pi*b*c*x + 1/2*\pi*a*c*\operatorname{sgn}(F) - 1/2*\pi*a*c - x*e - d)/(4*b^2*c^2*\log(\operatorname{abs}(F))^2 + (\pi*b*c*\operatorname{sgn}(F) - \pi*b*c - 2*e)^2)*e^{(b*c*x*\log(\operatorname{abs}(F)) + a*c*\log(\operatorname{abs}(F)))} - 1/2*I*(2*I*f^2*e^{(1/2*I*\pi*b*c*x*\operatorname{sgn}(F) - 1/2*I*\pi*b*c*x + 1/2*I*\pi*a*c*\operatorname{sgn}(F) - 1/2*I*\pi*a*c + 2*I*x*e + 2*I*d)/(4*I*\pi*b*c*\operatorname{sgn}(F) - 4*I*\pi*b*c + 8*b*c*\log(\operatorname{abs}(F)) + 16*I*e) - 2*I*f^2*e^{(-1/2*I*\pi*b*c*x*\operatorname{sgn}(F) + 1/2*I*\pi*b*c*x - 1/2*I*\pi*a*c*\operatorname{sgn}(F) + 1/2*I*\pi*a*c - 2*I*x*e - 2*I*d)/(-4*I*\pi*b*c*\operatorname{sgn}(F) + 4*I*\pi*b*c + 8*b*c*\log(\operatorname{abs}(F)) - 16*I*e)})*e^{(b*c*x*\log(\operatorname{abs}(F)) + a*c*\log(\operatorname{abs}(F)))} + 1/2*(2*I*f^2*e^{(1/2*I*\pi*b*c*x*\operatorname{sgn}(F) - 1/2*I*\pi*b*c*x + 1/2*I*\pi*a*c*\operatorname{sgn}(F) - 1/2*I*\pi*a*c + I*x*e + I*d)/(I*\pi*b*c*\operatorname{sgn}(F) - I*\pi*b*c + 2*b*c*\log(\operatorname{abs}(F)) + 2*I*e) + 2*I*f^2*e^{(-1/2*I*\pi*b*c*x*\operatorname{sgn}(F) + 1/2*I*\pi*b*c*x - 1/2*I*\pi*a*c*\operatorname{sgn}(F) + 1/2*I*\pi*a*c - I*x*e - I*d)/(-I*\pi*b*c*\operatorname{sgn}(F) + I*\pi*b*c + 2*b*c*\log(\operatorname{abs}(F)) - 2*I*e)})*e^{(b*c*x*\log(\operatorname{abs}(F)) + a*c*\log(\operatorname{abs}(F)))} + 1/2*(-2*I*f^2*e^{(1/2*I*\pi*b*c*x*\operatorname{sgn}(F) - 1/2*I*\pi*b*c*x + 1/2*I*\pi*a*c*\operatorname{sgn}(F) - 1/2*I*\pi*a*c - I*x*e - I*d)/(I*\pi*b*c*\operatorname{sgn}(F) - I*\pi*b*c + 2*b*c*\log(\operatorname{abs}(F)) - 2*I*e) - 2*I*f^2*e^{(-1/2*I*\pi*b*c*x*\operatorname{sgn}(F) + 1/2*I*\pi*b*c*x - 1/2*I*\pi*a*c*\operatorname{sgn}(F) + 1/2*I*\pi*a*c + I*x*e + I*d)/(-I*\pi*b*c*\operatorname{sgn}(F) + I*\pi*b*c + 2*b*c*\log(\operatorname{abs}(F)) + 2*I*e)})*e^{(b*c*x*\log(\operatorname{abs}(F)) + a*c*\log(\operatorname{abs}(F)))} - 1/2*I*(2*I*f^2*e^{(1/2*I*\pi*b*c*x*\operatorname{sgn}(F) - 1/2*I*\pi*b*c*x + 1/2*I*\pi*a*c*\operatorname{sgn}(F) - 1/2*I*\pi*a*c - 2*I*x*e - 2*I*d)/(4*I*\pi*b*c*\operatorname{sgn}(F) - 4*I*\pi*b*c + 8*b*c*\log(\operatorname{abs}(F)) - 16*I*e) - 2*I*f^2*e^{(-1/2*I*\pi*b*c*x*\operatorname{sgn}(F) + 1/2*I*\pi*b*c*x - 1/2*I*\pi*a*c*\operatorname{sgn}(F) + 1/2*I*\pi*a*c + 2*I*x*e + 2*I*d)/(-4*I*\pi*b*c*\operatorname{sgn}(F) + 4*I*\pi*b*c + 8*b*c*\log(\operatorname{abs}(F)) + 16*I*e)})*e^{(b*c*x*\log(\operatorname{abs}(F)) + a*c*\log(\operatorname{abs}(F)))} - 1/2*I*(-2*I*f^2*e^{(1/2*I*\pi*b*c*x*\operatorname{sgn}(F) - 1/2*I*\pi*b*c*x + 1/2*I*\pi*a*c*\operatorname{sgn}(F) - 1/2*I*\pi*b*c*x + 1/2*I*\pi*a*c)/(2*I*\pi*b*c*\operatorname{sgn}(F) - 2*I*\pi*b*c + 4*b*c*\log(\operatorname{abs}(F)))} + 2*I*f^2*e^{(-1/2*I*\pi*b*c*x*\operatorname{sgn}(F) + 1/2*I*\pi*b*c*x - 1/2*I*\pi*a*c*\operatorname{sgn}(F) + 1/2*I*\pi*a*c)/(-2*I*\pi*b*c*\operatorname{sgn}(F) + 2*I*\pi*b*c + 4*b*c*\log(\operatorname{abs}(F)))})*e^{(b*c*x*\log(\operatorname{abs}(F)) + a*c*\log(\operatorname{abs}(F)))} - 1/2*I*(-2*I*f^2*e^{(1/2*I*\pi*b*c*x*\operatorname{sgn}(F) - 1/2*I*\pi*b*c*x + 1/2*I*\pi*a*c*\operatorname{sgn}(F) - 1/2*I*\pi*a*c)/(I*\pi*b*c*\operatorname{sgn}(F) - I*\pi*b*c + 2*b*c*\log(\operatorname{abs}(F)))} + 2*I*f^2*e^{(-1/2*I*\pi*b*c*x*\operatorname{sgn}(F) + 1/2*I*\pi*b*c*x - 1/2*I*\pi*a*c*\operatorname{sgn}(F) + 1/2*I*\pi*a*c)/(-I*\pi*b*c*\operatorname{sgn}(F) + I*\pi*b*c + 2*b*c*\log(\operatorname{abs}(F)))})*e^{(b*c*x*\log(\operatorname{abs}(F)) + a*c*\log(\operatorname{abs}(F)))}$$

maple [A] time = 0.42, size = 368, normalized size = 1.50

$$\frac{3F^{ac} f^2 F^{bcx}}{2bc \ln(F)} - \frac{F^{ac} f^2 bc \ln(F) e^{bcx \ln(F)}}{2(1 + \tan^2(ex + d))(4e^2 + b^2 c^2 \ln(F)^2)} - \frac{2F^{ac} f^2 e^{bcx \ln(F)} \tan(ex + d)}{(1 + \tan^2(ex + d))(4e^2 + b^2 c^2 \ln(F)^2)} + \frac{F^{ac} f^2 bc \ln(F)}{2(1 + \tan^2(ex + d))}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(F^(c*(b*x+a))*(f+f*sin(e*x+d))^2,x)

[Out] $\frac{3}{2} F^{(a*c)} f^2 / b / c / \ln(F) F^{(b*c*x)} - \frac{1}{2} F^{(a*c)} f^2 / (1 + \tan^2(e*x + d)) / (4e^2 + b^2 c^2 \ln(F)^2) * b*c*\ln(F) * \exp(b*c*x*\ln(F)) - 2 F^{(a*c)} f^2 / (1 + \tan^2(e*x + d)) / (4e^2 + b^2 c^2 \ln(F)^2) * e * \exp(b*c*x*\ln(F)) * \tan(e*x + d) + \frac{1}{2} F^{(a*c)} f^2 / (1 + \tan^2(e*x + d)) / (4e^2 + b^2 c^2 \ln(F)^2) * b*c*\ln(F) * \exp(b*c*x*\ln(F)) * \tan(e*x + d)^2 - 2 F^{(a*c)} f^2 / (1 + \tan^2(1/2*d + 1/2*e*x)^2) / (e^2 + b^2 c^2 \ln(F)^2) * e * \exp(b*c*x*\ln(F)) + 2 F^{(a*c)} f^2 / (1 + \tan^2(1/2*d + 1/2*e*x)^2) / (e^2 + b^2 c^2 \ln(F)^2) * e * \exp(b*c*x*\ln(F)) * \tan(1/2*d + 1/2*e*x)^2 + 4 F^{(a*c)} f^2 / (1 + \tan^2(1/2*d + 1/2*e*x)^2) * b*c*\ln(F) / (e^2 + b^2 c^2 \ln(F)^2) * \exp(b*c*x*\ln(F)) * \tan(1/2*d + 1/2*e*x)$

maxima [B] time = 0.39, size = 581, normalized size = 2.37

$$\frac{\left((F^{ac} b^2 c^2 \cos(2d) \log(F)^2 + 2 F^{ac} b c e \log(F) \sin(2d)) F^{bcx} \cos(2ex) + (F^{ac} b^2 c^2 \cos(2d) \log(F)^2 - 2 F^{ac} b c e \log(F) \sin(2d)) F^{bcx} \sin(2ex) \right)}{2(1 + \tan^2(ex + d))(4e^2 + b^2 c^2 \ln(F)^2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(F^(c*(b*x+a))*(f+f*sin(e*x+d))^2,x, algorithm="maxima")

[Out] $-1/4 * ((F^{(a*c)} * b^2 * c^2 * \cos(2*d) * \log(F)^2 + 2 * F^{(a*c)} * b * c * e * \log(F) * \sin(2*d)) * F^{(b*c*x)} * \cos(2*e*x) + (F^{(a*c)} * b^2 * c^2 * \cos(2*d) * \log(F)^2 - 2 * F^{(a*c)} * b * c * e * \log(F) * \sin(2*d)) * F^{(b*c*x)} * \cos(2*e*x + 4*d) - (F^{(a*c)} * b^2 * c^2 * \log(F)^2 * \sin(2*d) - 2 * F^{(a*c)} * b * c * e * \cos(2*d) * \log(F)) * F^{(b*c*x)} * \sin(2*e*x) + (F^{(a*c)} * b^2 * c^2 * \log(F)^2 * \sin(2*d) + 2 * F^{(a*c)} * b * c * e * \cos(2*d) * \log(F)) * F^{(b*c*x)} * \sin(2*e*x + 4*d) - 2 * (F^{(a*c)} * b^2 * c^2 * \cos(2*d)^2 * \log(F)^2 + F^{(a*c)} * b^2 * c^2 * \log(F)^2 * \sin(2*d)^2 + 4 * (F^{(a*c)} * \cos(2*d)^2 + F^{(a*c)} * \sin(2*d)^2) * e^2) * F^{(b*c*x)} * f^2 / (b^3 * c^3 * \cos(2*d)^2 * \log(F)^3 + b^3 * c^3 * \log(F)^3 * \sin(2*d)^2 + 4 * (b * c * \cos(2*d)^2 * \log(F) + b * c * \log(F) * \sin(2*d)^2) * e^2) - ((F^{(a*c)} * b * c * \log(F) * \sin(d) + F^{(a*c)} * e * \cos(d)) * F^{(b*c*x)} * \cos(e*x + 2*d) - (F^{(a*c)} * b * c * \log(F) * \sin(d) - F^{(a*c)} * e * \cos(d)) * F^{(b*c*x)} * \cos(e*x) - (F^{(a*c)} * b * c * \cos(d) * \log(F) - F^{(a*c)} * e * \sin(d)) * F^{(b*c*x)} * \sin(e*x + 2*d) - (F^{(a*c)} * b * c * \cos(d) * \log(F) + F^{(a*c)} * e * \sin(d)) * F^{(b*c*x)} * \sin(e*x)) * f^2 / (b^2 * c^2 * \cos(d)^2 * \log(F)^2 + b^2 * c^2 * \log(F)^2 * \sin(d)^2 + (\cos(d)^2 + \sin(d)^2) * e^2) + F^{(b*c*x + a*c)} * f^2 / (b * c * \log(F))$

mupad [B] time = 3.42, size = 248, normalized size = 1.01

$$\frac{F^{ac+bcx} f^2 \left(\frac{b^4 c^4 \ln(F)^4 \cos(2d+2ex)}{2} - \frac{3 b^4 c^4 \ln(F)^4}{2} - 2 b^4 c^4 \sin(d+ex) \ln(F)^4 - 6 e^4 - \frac{15 b^2 c^2 e^2 \ln(F)^2}{2} + b^3 c^3 e \ln(F) \right)}{2(1 + \tan^2(ex + d))(4e^2 + b^2 c^2 \ln(F)^2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(F^(c*(a + b*x))*(f + f*sin(d + e*x))^2,x)

[Out] $-(F^{(a*c + b*c*x)} * f^2 * ((b^4 * c^4 * \log(F)^4 * \cos(2*d + 2*e*x)) / 2 - (3 * b^4 * c^4 * \log(F)^4) / 2 - 2 * b^4 * c^4 * \sin(d + e*x) * \log(F)^4 - 6 * e^4 - (15 * b^2 * c^2 * e^2 * \log(F)^2) / 2 + b^3 * c^3 * e * \log(F)^3 * \sin(2*d + 2*e*x) - 8 * b^2 * c^2 * e^2 * \sin(d + e*x) * \log(F)^2 + b * c * e^3 * \log(F) * \sin(2*d + 2*e*x) + (b^2 * c^2 * e^2 * \log(F)^2 * \cos(2*d + 2*e*x)) / 2 + 2 * b^3 * c^3 * e * \cos(d + e*x) * \log(F)^3 + 8 * b * c * e^3 * \cos(d + e*x) * \log(F))) / (b * c * \log(F) * (4 * e^4 + b^4 * c^4 * \log(F)^4 + 5 * b^2 * c^2 * e^2 * \log(F)^2))$

sympy [A] time = 58.62, size = 1760, normalized size = 7.18

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(F**(c*(b*x+a))*(f+f*sin(e*x+d))**2,x)

[Out] Piecewise((f**2*x*sin(d + e*x)**2/2 + f**2*x*cos(d + e*x)**2/2 + f**2*x - f**2*sin(d + e*x)*cos(d + e*x)/(2*e) - 2*f**2*cos(d + e*x)/e, Eq(F, 1)), (zoo*e**4*f**2*exp(-2*I*e/(b*c))**(a*c)*exp(-2*I*e/(b*c))**(b*c*x)*sin(d + e*x)**2 + zoo*e**4*f**2*exp(-2*I*e/(b*c))**(a*c)*exp(-2*I*e/(b*c))**(b*c*x)*sin(d + e*x)*cos(d + e*x) + zoo*e**4*f**2*exp(-2*I*e/(b*c))**(a*c)*exp(-2*I*e/(b*c))**(b*c*x)*cos(d + e*x)**2, Eq(F, exp(-2*I*e/(b*c)))), (zoo*e**4*f**2*exp(-I*e/(b*c))**(a*c)*exp(-I*e/(b*c))**(b*c*x)*sin(d + e*x) + zoo*e**4*f**2*exp(-I*e/(b*c))**(a*c)*exp(-I*e/(b*c))**(b*c*x)*cos(d + e*x), Eq(F, exp(-I*e/(b*c)))), (zoo*e**4*f**2*exp(I*e/(b*c))**(a*c)*exp(I*e/(b*c))**(b*c*x)*sin(d + e*x) + zoo*e**4*f**2*exp(I*e/(b*c))**(a*c)*exp(I*e/(b*c))**(b*c*x)*cos(d + e*x), Eq(F, exp(I*e/(b*c)))), (zoo*e**4*f**2*exp(2*I*e/(b*c))**(a*c)*exp(2*I*e/(b*c))**(b*c*x)*sin(d + e*x)**2 + zoo*e**4*f**2*exp(2*I*e/(b*c))**(a*c)*exp(2*I*e/(b*c))**(b*c*x)*sin(d + e*x)*cos(d + e*x) + zoo*e**4*f**2*exp(2*I*e/(b*c))**(a*c)*exp(2*I*e/(b*c))**(b*c*x)*cos(d + e*x)**2, Eq(F, exp(2*I*e/(b*c)))), (F**(a*c)*(f**2*x*sin(d + e*x)**2/2 + f**2*x*cos(d + e*x)**2/2 + f**2*x - f**2*sin(d + e*x)*cos(d + e*x)/(2*e) - 2*f**2*cos(d + e*x)/e), Eq(b, 0)), (f**2*x*sin(d + e*x)**2/2 + f**2*x*cos(d + e*x)**2/2 + f**2*x - f**2*sin(d + e*x)*cos(d + e*x)/(2*e) - 2*f**2*cos(d + e*x)/e, Eq(c, 0)), (F**(a*c)*F**(b*c*x)*b**4*c**4*f**2*log(F)**4*sin(d + e*x)**2/(b**5*c**5*log(F)**5 + 5*b**3*c**3*e**2*log(F)**3 + 4*b*c*e**4*log(F)) + 2*F**(a*c)*F**(b*c*x)*b**4*c**4*f**2*log(F)**4*sin(d + e*x)/(b**5*c**5*log(F)**5 + 5*b**3*c**3*e**2*log(F)**3 + 4*b*c*e**4*log(F)) + F**(a*c)*F**(b*c*x)*b**4*c**4*f**2*log(F)**4/(b**5*c**5*log(F)**5 + 5*b**3*c**3*e**2*log(F)**3 + 4*b*c*e**4*log(F)) - 2*F**(a*c)*F**(b*c*x)*b**3*c**3*e**2*log(F)**3*sin(d + e*x)*cos(d + e*x)/(b**5*c**5*log(F)**5 + 5*b**3*c**3*e**2*log(F)**3 + 4*b*c*e**4*log(F)) - 2*F**(a*c)*F**(b*c*x)*b**3*c**3*e**2*log(F)**3*cos(d + e*x)/(b**5*c**5*log(F)**5 + 5*b**3*c**3*e**2*log(F)**3 + 4*b*c*e**4*log(F)) + 3*F**(a*c)*F**(b*c*x)*b**2*c**2*e**2*f**2*log(F)**2*sin(d + e*x)**2/(b**5*c**5*log(F)**5 + 5*b**3*c**3*e**2*log(F)**3 + 4*b*c*e**4*log(F)) + 8*F**(a*c)*F**(b*c*x)*b**2*c**2*e**2*f**2*log(F)**2*sin(d + e*x)/(b**5*c**5*log(F)**5 + 5*b**3*c**3*e**2*log(F)**3 + 4*b*c*e**4*log(F)) + 2*F**(a*c)*F**(b*c*x)*b**2*c**2*e**2*f**2*log(F)**2*cos(d + e*x)**2/(b**5*c**5*log(F)**5 + 5*b**3*c**3*e**2*log(F)**3 + 4*b*c*e**4*log(F)) - 2*F**(a*c)*F**(b*c*x)*b*c*e**3*f**2*log(F)*sin(d + e*x)*cos(d + e*x)/(b**5*c**5*log(F)**5 + 5*b**3*c**3*e**2*log(F)**3 + 4*b*c*e**4*log(F)) - 8*F**(a*c)*F**(b*c*x)*b*c*e**3*f**2*log(F)*cos(d + e*x)/(b**5*c**5*log(F)**5 + 5*b**3*c**3*e**2*log(F)**3 + 4*b*c*e**4*log(F)) + 2*F**(a*c)*F**(b*c*x)*e**4*f**2*sin(d + e*x)**2/(b**5*c**5*log(F)**5 + 5*b**3*c**3*e**2*log(F)**3 + 4*b*c*e**4*log(F)) + 2*F**(a*c)*F**(b*c*x)*e**4*f**2*cos(d + e*x)**2/(b**5*c**5*log(F)**5 + 5*b**3*c**3*e**2*log(F)**3 + 4*b*c*e**4*log(F)) + 4*F**(a*c)*F**(b*c*x)*e**4*f**2/(b**5*c**5*log(F)**5 + 5*b**3*c**3*e**2*log(F)**3 + 4*b*c*e**4*log(F)), True))

3.136 $\int F^{c(a+bx)}(f + f \sin(d + ex)) dx$

Optimal. Leaf size=99

$$\frac{bcf \log(F) \sin(d + ex) F^{ac+bcx}}{b^2 c^2 \log^2(F) + e^2} - \frac{ef \cos(d + ex) F^{ac+bcx}}{b^2 c^2 \log^2(F) + e^2} + \frac{f F^{ac+bcx}}{bc \log(F)}$$

[Out] $f F^{(b c x + a c) / b / c / \ln(F)} - e f F^{(b c x + a c) / b / c / \ln(F)} \cos(e x + d) / (e^2 + b^2 c^2 \ln(F)^2) + b c f F^{(b c x + a c) / b / c / \ln(F)} \ln(F) \sin(e x + d) / (e^2 + b^2 c^2 \ln(F)^2)$

Rubi [A] time = 0.16, antiderivative size = 99, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 5, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.250$, Rules used = {6741, 12, 6742, 2194, 4432}

$$\frac{bcf \log(F) \sin(d + ex) F^{ac+bcx}}{b^2 c^2 \log^2(F) + e^2} - \frac{ef \cos(d + ex) F^{ac+bcx}}{b^2 c^2 \log^2(F) + e^2} + \frac{f F^{ac+bcx}}{bc \log(F)}$$

Antiderivative was successfully verified.

[In] `Int[F^(c*(a + b*x))*(f + f*Sin[d + e*x]),x]`

[Out] $(f F^{(a c + b c x)}) / (b c \log[F]) - (e f F^{(a c + b c x)} \cos[d + e x]) / (e^2 + b^2 c^2 \log[F]^2) + (b c f F^{(a c + b c x)} \log[F] \sin[d + e x]) / (e^2 + b^2 c^2 \log[F]^2)$

Rule 12

`Int[(a_)*(u_), x_Symbol] := Dist[a, Int[u, x], x] /; FreeQ[a, x] && !MatchQ[u, (b_)*(v_) /; FreeQ[b, x]]`

Rule 2194

`Int[((F_)^((c_.)*((a_.) + (b_.)*(x_))))^(n_.), x_Symbol] := Simp[(F^(c*(a + b*x)))^n/(b*c*n*Log[F]), x] /; FreeQ[{F, a, b, c, n}, x]`

Rule 4432

`Int[(F_)^((c_.)*((a_.) + (b_.)*(x_)))*Sin[(d_.) + (e_.)*(x_)], x_Symbol] := Simp[(b*c*Log[F]*F^(c*(a + b*x))*Sin[d + e*x]/(e^2 + b^2*c^2*Log[F]^2), x] - Simp[(e*F^(c*(a + b*x))*Cos[d + e*x]/(e^2 + b^2*c^2*Log[F]^2), x] /; FreeQ[{F, a, b, c, d, e}, x] && NeQ[e^2 + b^2*c^2*Log[F]^2, 0]`

Rule 6741

`Int[u_, x_Symbol] := With[{v = NormalizeIntegrand[u, x]}, Int[v, x] /; v != u]`

Rule 6742

`Int[u_, x_Symbol] := With[{v = ExpandIntegrand[u, x]}, Int[v, x] /; SumQ[v]`

Rubi steps

$$\begin{aligned}
\int F^{c(a+bx)}(f + f \sin(d + ex)) dx &= \int f F^{ac+bcx}(1 + \sin(d + ex)) dx \\
&= f \int F^{ac+bcx}(1 + \sin(d + ex)) dx \\
&= f \int (F^{ac+bcx} + F^{ac+bcx} \sin(d + ex)) dx \\
&= f \int F^{ac+bcx} dx + f \int F^{ac+bcx} \sin(d + ex) dx \\
&= \frac{f F^{ac+bcx}}{bc \log(F)} - \frac{ef F^{ac+bcx} \cos(d + ex)}{e^2 + b^2 c^2 \log^2(F)} + \frac{bc f F^{ac+bcx} \log(F) \sin(d + ex)}{e^2 + b^2 c^2 \log^2(F)}
\end{aligned}$$

Mathematica [A] time = 0.57, size = 83, normalized size = 0.84

$$\frac{f F^{c(a+bx)} (b^2 c^2 \log^2(F) \sin(d + ex) + b^2 c^2 \log^2(F) - bce \log(F) \cos(d + ex) + e^2)}{bc \log(F) (b^2 c^2 \log^2(F) + e^2)}$$

Antiderivative was successfully verified.

[In] Integrate[F^(c*(a + b*x))*(f + f*Sin[d + e*x]),x]

[Out] (f*F^(c*(a + b*x))*(e^2 - b*c*e*Cos[d + e*x]*Log[F] + b^2*c^2*Log[F]^2 + b^2*c^2*Log[F]^2*Sin[d + e*x]))/(b*c*Log[F]*(e^2 + b^2*c^2*Log[F]^2))

fricas [A] time = 0.65, size = 83, normalized size = 0.84

$$\frac{(b^2 c^2 f \log(F)^2 \sin(ex + d) + b^2 c^2 f \log(F)^2 - bce f \cos(ex + d) \log(F) + e^2 f) F^{bcx+ac}}{b^3 c^3 \log(F)^3 + bce^2 \log(F)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(F^(c*(b*x+a))*(f+f*sin(e*x+d)),x, algorithm="fricas")

[Out] (b^2*c^2*f*log(F)^2*sin(e*x + d) + b^2*c^2*f*log(F)^2 - b*c*e*f*cos(e*x + d)*log(F) + e^2*f)*F^(b*c*x + a*c)/(b^3*c^3*log(F)^3 + b*c*e^2*log(F))

giac [C] time = 0.26, size = 941, normalized size = 9.51

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(F^(c*(b*x+a))*(f+f*sin(e*x+d)),x, algorithm="giac")

[Out] 2*(2*b*c*f*cos(-1/2*pi*b*c*x*sgn(F) + 1/2*pi*b*c*x - 1/2*pi*a*c*sgn(F) + 1/2*pi*a*c)*log(abs(F))/(4*b^2*c^2*log(abs(F))^2 + (pi*b*c*sgn(F) - pi*b*c)^2) - (pi*b*c*sgn(F) - pi*b*c)*f*sin(-1/2*pi*b*c*x*sgn(F) + 1/2*pi*b*c*x - 1/2*pi*a*c*sgn(F) + 1/2*pi*a*c)/(4*b^2*c^2*log(abs(F))^2 + (pi*b*c*sgn(F) - pi*b*c)^2))*e^(b*c*x*log(abs(F)) + a*c*log(abs(F))) + (2*b*c*f*log(abs(F))*sin(1/2*pi*b*c*x*sgn(F) - 1/2*pi*b*c*x + 1/2*pi*a*c*sgn(F) - 1/2*pi*a*c + x*e + d)/(4*b^2*c^2*log(abs(F))^2 + (pi*b*c*sgn(F) - pi*b*c + 2*e)^2) - (pi*b*c*sgn(F) - pi*b*c + 2*e)*f*cos(1/2*pi*b*c*x*sgn(F) - 1/2*pi*b*c*x + 1/2*pi*a*c*sgn(F) - 1/2*pi*a*c + x*e + d)/(4*b^2*c^2*log(abs(F))^2 + (pi*b*c*sgn(F) - pi*b*c + 2*e)^2))*e^(b*c*x*log(abs(F)) + a*c*log(abs(F))) - (2*b*c*f*log(abs(F))*sin(1/2*pi*b*c*x*sgn(F) - 1/2*pi*b*c*x + 1/2*pi*a*c*sgn(F) - 1/2*pi*a*c - x*e - d)/(4*b^2*c^2*log(abs(F))^2 + (pi*b*c*sgn(F) - pi*b*c - 2*e)^2) - (pi*b*c*sgn(F) - pi*b*c - 2*e)*f*cos(1/2*pi*b*c*x*sgn(F) - 1/2*pi*b*c*x + 1/2*pi*a*c*sgn(F) - 1/2*pi*a*c - x*e - d)/(4*b^2*c^2*log(abs(F))^2 + (pi*b*c*sgn(F) - pi*b*c - 2*e)^2))*e^(b*c*x*log(abs(F)) + a*c*log(abs(F)))

$$\begin{aligned}
& + 1/2*(2*I*f*e^{(1/2*I*pi*b*c*x*sgn(F) - 1/2*I*pi*b*c*x + 1/2*I*pi*a*c*sgn(F)} \\
&) - 1/2*I*pi*a*c + I*x*e + I*d)/(2*I*pi*b*c*sgn(F) - 2*I*pi*b*c + 4*b*c*log \\
& (abs(F)) + 4*I*e) + 2*I*f*e^{(-1/2*I*pi*b*c*x*sgn(F) + 1/2*I*pi*b*c*x - 1/2* \\
& I*pi*a*c*sgn(F) + 1/2*I*pi*a*c - I*x*e - I*d)/(-2*I*pi*b*c*sgn(F) + 2*I*pi* \\
& b*c + 4*b*c*log(abs(F)) - 4*I*e))e^{(b*c*x*log(abs(F)) + a*c*log(abs(F)))} + \\
& 1/2*(-2*I*f*e^{(1/2*I*pi*b*c*x*sgn(F) - 1/2*I*pi*b*c*x + 1/2*I*pi*a*c*sgn(F)} \\
&) - 1/2*I*pi*a*c - I*x*e - I*d)/(2*I*pi*b*c*sgn(F) - 2*I*pi*b*c + 4*b*c*log \\
& (abs(F)) - 4*I*e) - 2*I*f*e^{(-1/2*I*pi*b*c*x*sgn(F) + 1/2*I*pi*b*c*x - 1/2* \\
& I*pi*a*c*sgn(F) + 1/2*I*pi*a*c + I*x*e + I*d)/(-2*I*pi*b*c*sgn(F) + 2*I*pi* \\
& b*c + 4*b*c*log(abs(F)) + 4*I*e))e^{(b*c*x*log(abs(F)) + a*c*log(abs(F)))} - \\
& 1/2*I*(-2*I*f*e^{(1/2*I*pi*b*c*x*sgn(F) - 1/2*I*pi*b*c*x + 1/2*I*pi*a*c*sgn \\
& (F) - 1/2*I*pi*a*c)/(I*pi*b*c*sgn(F) - I*pi*b*c + 2*b*c*log(abs(F)))} + 2*I* \\
& f*e^{(-1/2*I*pi*b*c*x*sgn(F) + 1/2*I*pi*b*c*x - 1/2*I*pi*a*c*sgn(F) + 1/2*I* \\
& pi*a*c)/(-I*pi*b*c*sgn(F) + I*pi*b*c + 2*b*c*log(abs(F)))})e^{(b*c*x*log(abs \\
& (F)) + a*c*log(abs(F)))}
\end{aligned}$$

maple [A] time = 0.05, size = 183, normalized size = 1.85

$$\frac{f F^{c(bx+a)}}{bc \ln(F)} + \frac{f e^{c(bx+a) \ln(F)} \left(\tan^2 \left(\frac{d}{2} + \frac{ex}{2} \right) \right)}{\left(1 + \tan^2 \left(\frac{d}{2} + \frac{ex}{2} \right) \right) (e^2 + b^2 c^2 \ln(F)^2)} - \frac{f e^{c(bx+a) \ln(F)}}{\left(1 + \tan^2 \left(\frac{d}{2} + \frac{ex}{2} \right) \right) (e^2 + b^2 c^2 \ln(F)^2)} + \frac{2 f b c \ln(F) e^{c(bx+a)}}{\left(1 + \tan^2 \left(\frac{d}{2} + \frac{ex}{2} \right) \right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(F^(c*(b*x+a))*(f+f*sin(e*x+d)),x)

[Out] f/b/c/ln(F)*F^(c*(b*x+a))+f/(1+tan(1/2*d+1/2*e*x)^2)/(e^2+b^2*c^2*ln(F)^2)*e*exp(c*(b*x+a)*ln(F))*tan(1/2*d+1/2*e*x)^2-f/(1+tan(1/2*d+1/2*e*x)^2)/(e^2+b^2*c^2*ln(F)^2)*e*exp(c*(b*x+a)*ln(F))+2*f/(1+tan(1/2*d+1/2*e*x)^2)*b*c*ln(F)/(e^2+b^2*c^2*ln(F)^2)*exp(c*(b*x+a)*ln(F))*tan(1/2*d+1/2*e*x)

maxima [B] time = 0.34, size = 218, normalized size = 2.20

$$\frac{\left(F^{ac} b c \log(F) \sin(d) + F^{ac} e \cos(d) \right) F^{bcx} \cos(ex + 2d) - \left(F^{ac} b c \log(F) \sin(d) - F^{ac} e \cos(d) \right) F^{bcx} \cos(ex) - \left(F^{ac} b c \log(F) \sin(d) + F^{ac} e \cos(d) \right) F^{bcx} \cos(ex + 2d) + \left(F^{ac} b c \log(F) \sin(d) - F^{ac} e \cos(d) \right) F^{bcx} \cos(ex)}{2 \left(b^2 c^2 \cos(d)^2 \log(F)^2 + b^2 c^2 \log(F)^2 \sin(d)^2 \right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(F^(c*(b*x+a))*(f+f*sin(e*x+d)),x, algorithm="maxima")

[Out] -1/2*((F^(a*c)*b*c*log(F)*sin(d) + F^(a*c)*e*cos(d))*F^(b*c*x)*cos(e*x + 2*d) - (F^(a*c)*b*c*log(F)*sin(d) - F^(a*c)*e*cos(d))*F^(b*c*x)*cos(e*x) - (F^(a*c)*b*c*cos(d)*log(F) - F^(a*c)*e*sin(d))*F^(b*c*x)*sin(e*x + 2*d) - (F^(a*c)*b*c*cos(d)*log(F) + F^(a*c)*e*sin(d))*F^(b*c*x)*sin(e*x))*f/(b^2*c^2*cos(d)^2*log(F)^2 + b^2*c^2*log(F)^2*sin(d)^2 + (cos(d)^2 + sin(d)^2)*e^2) + F^(b*c*x + a*c)*f/(b*c*log(F))

mupad [B] time = 2.59, size = 84, normalized size = 0.85

$$\frac{F^{ac+bcx} f \left(e^2 + b^2 c^2 \ln(F)^2 + b^2 c^2 \sin(d + ex) \ln(F)^2 - b c e \cos(d + ex) \ln(F) \right)}{b c \ln(F) \left(b^2 c^2 \ln(F)^2 + e^2 \right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(F^(c*(a + b*x))*(f + f*sin(d + e*x)),x)

[Out] (F^(a*c + b*c*x)*f*(e^2 + b^2*c^2*log(F)^2 + b^2*c^2*sin(d + e*x)*log(F)^2 - b*c*e*cos(d + e*x)*log(F)))/(b*c*log(F)*(e^2 + b^2*c^2*log(F)^2))

sympy [A] time = 7.37, size = 408, normalized size = 4.12

$$\left\{ \begin{array}{ll}
 f x - \frac{f \cos(d+ex)}{e} & \text{for } F = 1 \\
 \tilde{\omega} e^2 f \left(e^{-\frac{ie}{bc}} \right)^{ac} \left(e^{-\frac{ie}{bc}} \right)^{bcx} \sin(d+ex) + \tilde{\omega} e^2 f \left(e^{-\frac{ie}{bc}} \right)^{ac} \left(e^{-\frac{ie}{bc}} \right)^{bcx} \cos(d+ex) & \text{for } F = e^{-\frac{ie}{bc}} \\
 \tilde{\omega} e^2 f \left(e^{\frac{ie}{bc}} \right)^{ac} \left(e^{\frac{ie}{bc}} \right)^{bcx} \sin(d+ex) + \tilde{\omega} e^2 f \left(e^{\frac{ie}{bc}} \right)^{ac} \left(e^{\frac{ie}{bc}} \right)^{bcx} \cos(d+ex) & \text{for } F = e^{\frac{ie}{bc}} \\
 F^{ac} \left(f x - \frac{f \cos(d+ex)}{e} \right) & \text{for } b = 0 \\
 f x - \frac{f \cos(d+ex)}{e} & \text{for } c = 0 \\
 \frac{F^{ac} F^{bcx} b^2 c^2 f \log(F)^2 \sin(d+ex)}{b^3 c^3 \log(F)^3 + b c e^2 \log(F)} + \frac{F^{ac} F^{bcx} b^2 c^2 f \log(F)^2}{b^3 c^3 \log(F)^3 + b c e^2 \log(F)} - \frac{F^{ac} F^{bcx} b c e f \log(F) \cos(d+ex)}{b^3 c^3 \log(F)^3 + b c e^2 \log(F)} + \frac{F^{ac} F^{bcx} e^2 f}{b^3 c^3 \log(F)^3 + b c e^2 \log(F)} & \text{otherwise}
 \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

```

[In] integrate(F**(c*(b*x+a))*(f+f*sin(e*x+d)),x)
[Out] Piecewise((f*x - f*cos(d + e*x)/e, Eq(F, 1)), (zoo*e**2*f*exp(-I*e/(b*c))**
(a*c)*exp(-I*e/(b*c))**(b*c*x)*sin(d + e*x) + zoo*e**2*f*exp(-I*e/(b*c))**
(a*c)*exp(-I*e/(b*c))**(b*c*x)*cos(d + e*x), Eq(F, exp(-I*e/(b*c)))), (zoo*e
**2*f*exp(I*e/(b*c))**(a*c)*exp(I*e/(b*c))**(b*c*x)*sin(d + e*x) + zoo*e**2
*f*exp(I*e/(b*c))**(a*c)*exp(I*e/(b*c))**(b*c*x)*cos(d + e*x), Eq(F, exp(I*
e/(b*c)))), (F**(a*c)*(f*x - f*cos(d + e*x)/e), Eq(b, 0)), (f*x - f*cos(d +
e*x)/e, Eq(c, 0)), (F**(a*c)*F**(b*c*x)*b**2*c**2*f*log(F)**2*sin(d + e*x)
/(b**3*c**3*log(F)**3 + b*c*e**2*log(F)) + F**(a*c)*F**(b*c*x)*b**2*c**2*f*
log(F)**2/(b**3*c**3*log(F)**3 + b*c*e**2*log(F)) - F**(a*c)*F**(b*c*x)*b*c
*e*f*log(F)*cos(d + e*x)/(b**3*c**3*log(F)**3 + b*c*e**2*log(F)) + F**(a*c)
*F**(b*c*x)*e**2*f/(b**3*c**3*log(F)**3 + b*c*e**2*log(F)), True))

```

$$3.137 \quad \int \frac{F^{c(a+bx)}}{f+f \sin(d+ex)} dx$$

Optimal. Leaf size=80

$$\frac{2e^{i(d+ex)}F^{c(a+bx)} {}_2F_1\left(2, 1 - \frac{ibc \log(F)}{e}; 2 - \frac{ibc \log(F)}{e}; ie^{i(d+ex)}\right)}{f(e - ibc \log(F))}$$

[Out] $-2*\exp(I*(e*x+d))*F^{(c*(b*x+a))*\text{hypergeom}([2, 1-I*b*c*\ln(F)/e], [2-I*b*c*\ln(F)/e], I*\exp(I*(e*x+d)))/f/(e-I*b*c*\ln(F))$

Rubi [A] time = 0.07, antiderivative size = 80, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 22, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {4456, 4450}

$$\frac{2e^{i(d+ex)}F^{c(a+bx)} {}_2F_1\left(2, 1 - \frac{ibc \log(F)}{e}; 2 - \frac{ibc \log(F)}{e}; ie^{i(d+ex)}\right)}{f(e - ibc \log(F))}$$

Antiderivative was successfully verified.

[In] Int[F^(c*(a + b*x))/(f + f*Sin[d + e*x]),x]

[Out] $(-2*E^{(I*(d + e*x))*F^{(c*(a + b*x))*\text{Hypergeometric2F1}[2, 1 - (I*b*c*\text{Log}[F])/e, 2 - (I*b*c*\text{Log}[F])/e, I*E^{(I*(d + e*x))}]/(f*(e - I*b*c*\text{Log}[F]))$

Rule 4450

Int[(F_)^((c_.)*((a_.) + (b_.)*(x_)))*Sec[(d_.) + Pi*(k_.) + (e_.)*(x_)]^(n_.), x_Symbol] := Simp[(2^n*E^(I*k*n*Pi)*E^(I*n*(d + e*x))*F^(c*(a + b*x))*Hypergeometric2F1[n, n/2 - (I*b*c*Log[F])/(2*e), 1 + n/2 - (I*b*c*Log[F])/(2*e), -(E^(2*I*k*Pi)*E^(2*I*(d + e*x)))]/(I*e*n + b*c*Log[F]), x] /; FreeQ[{F, a, b, c, d, e}, x] && IntegerQ[4*k] && IntegerQ[n]

Rule 4456

Int[(F_)^((c_.)*((a_.) + (b_.)*(x_)))*((f_) + (g_.)*Sin[(d_.) + (e_.)*(x_)]^(n_.), x_Symbol] := Dist[2^n*f^n, Int[F^(c*(a + b*x))*Cos[d/2 + (e*x)/2 - (f*Pi)/(4*g)]^(2*n), x], x] /; FreeQ[{F, a, b, c, d, e, f, g}, x] && EqQ[f^2 - g^2, 0] && ILtQ[n, 0]

Rubi steps

$$\begin{aligned} \int \frac{F^{c(a+bx)}}{f+f \sin(d+ex)} dx &= \frac{\int F^{c(a+bx)} \sec^2\left(\frac{d}{2} - \frac{\pi}{4} + \frac{ex}{2}\right) dx}{2f} \\ &= -\frac{2e^{i(d+ex)}F^{c(a+bx)} {}_2F_1\left(2, 1 - \frac{ibc \log(F)}{e}; 2 - \frac{ibc \log(F)}{e}; ie^{i(d+ex)}\right)}{f(e - ibc \log(F))} \end{aligned}$$

Mathematica [A] time = 1.69, size = 128, normalized size = 1.60

$$\frac{2F^{c(a+bx)} \left(-i {}_2F_1\left(1, -\frac{ibc \log(F)}{e}; 1 - \frac{ibc \log(F)}{e}; i \cos(d+ex) - \sin(d+ex)\right) + \frac{\sin\left(\frac{ex}{2}\right)}{\left(\sin\left(\frac{d}{2}\right) + \cos\left(\frac{d}{2}\right)\right) \left(\sin\left(\frac{1}{2}(d+ex)\right) + \cos\left(\frac{1}{2}(d+ex)\right)\right)} \right)}{ef}$$

Antiderivative was successfully verified.

[In] Integrate[F^(c*(a + b*x))/(f + f*Sin[d + e*x]),x]

[Out] (2*F^(c*(a + b*x))*((-I)*Hypergeometric2F1[1, ((-I)*b*c*Log[F])/e, 1 - (I*b*c*Log[F])/e, I*Cos[d + e*x] - Sin[d + e*x]] - (Cos[d] + I*(1 + Sin[d]))^(-1) + Sin[(e*x)/2]/((Cos[d/2] + Sin[d/2])*(Cos[(d + e*x)/2] + Sin[(d + e*x)/2]))))/(e*f)

fricas [F] time = 0.77, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{F^{bcx+ac}}{f \sin(ex+d) + f}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(F^(c*(b*x+a))/(f+f*sin(e*x+d)),x, algorithm="fricas")

[Out] integral(F^(b*c*x + a*c)/(f*sin(e*x + d) + f), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{F^{(bx+a)c}}{f \sin(ex+d) + f} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(F^(c*(b*x+a))/(f+f*sin(e*x+d)),x, algorithm="giac")

[Out] integrate(F^((b*x + a)*c)/(f*sin(e*x + d) + f), x)

maple [F] time = 0.20, size = 0, normalized size = 0.00

$$\int \frac{F^{c(bx+a)}}{f + f \sin(ex+d)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(F^(c*(b*x+a))/(f+f*sin(e*x+d)),x)

[Out] int(F^(c*(b*x+a))/(f+f*sin(e*x+d)),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(F^(c*(b*x+a))/(f+f*sin(e*x+d)),x, algorithm="maxima")

[Out] 2*(6*F^(b*c*x)*F^(a*c)*b*c*e^2*log(F) + 2*(F^(a*c)*b^3*c^3*log(F)^3 + 4*F^(a*c)*b*c*e^2*log(F))*F^(b*c*x)*cos(e*x + d)^2 + 2*(F^(a*c)*b^3*c^3*log(F)^3 + 4*F^(a*c)*b*c*e^2*log(F))*F^(b*c*x)*sin(e*x + d)^2 + (5*F^(a*c)*b^2*c^2*e*log(F)^2 - 4*F^(a*c)*e^3)*F^(b*c*x)*cos(e*x + d) + (F^(a*c)*b^3*c^3*log(F)^3 + 16*F^(a*c)*b*c*e^2*log(F))*F^(b*c*x)*sin(e*x + d) - (6*F^(b*c*x)*F^(a*c)*b*c*e^2*log(F) + (F^(a*c)*b^2*c^2*e*log(F)^2 + 4*F^(a*c)*e^3)*F^(b*c*x)*cos(e*x + d) + (F^(a*c)*b^3*c^3*log(F)^3 + 4*F^(a*c)*b*c*e^2*log(F))*F^(b*c*x)*sin(e*x + d))*cos(2*e*x + 2*d) - 2*((F^(a*c)*b^5*c^5*e*log(F)^5 + 5*F^(a*c)*b^3*c^3*e^3*log(F)^3 + 4*F^(a*c)*b*c*e^5*log(F))*f*cos(2*e*x + 2*d)^2 + 4*(F^(a*c)*b^5*c^5*e*log(F)^5 + 5*F^(a*c)*b^3*c^3*e^3*log(F)^3 + 4*F^(a*c)*b*c*e^5*log(F))*f*cos(e*x + d)^2 + 4*(F^(a*c)*b^5*c^5*e*log(F)^5 + 5*F^(a*c)*b^3*c^3*e^3*log(F)^3 + 4*F^(a*c)*b*c*e^5*log(F))*f*cos(e*x + d)*sin(2*e*x + 2*d) + (F^(a*c)*b^5*c^5*e*log(F)^5 + 5*F^(a*c)*b^3*c^3*e^3*log(F)^3 + 4*F^(a*c)*b*c*e^5*log(F))*f*sin(2*e*x + 2*d)^2 + 4*(F^(a*c)*b^5*c^5*e*log(F)^5 + 5*F^(a*c)*b^3*c^3*e^3*log(F)^3 + 4*F^(a*c)*b*c*e^5*log(F))*f*sin(e*x

+ d)^2 + 4*(F^(a*c)*b^5*c^5*e*log(F)^5 + 5*F^(a*c)*b^3*c^3*e^3*log(F)^3 + 4*F^(a*c)*b*c*e^5*log(F))*f*sin(e*x + d) + (F^(a*c)*b^5*c^5*e*log(F)^5 + 5*F^(a*c)*b^3*c^3*e^3*log(F)^3 + 4*F^(a*c)*b*c*e^5*log(F))*f - 2*(2*(F^(a*c)*b^5*c^5*e*log(F)^5 + 5*F^(a*c)*b^3*c^3*e^3*log(F)^3 + 4*F^(a*c)*b*c*e^5*log(F))*f*sin(e*x + d) + (F^(a*c)*b^5*c^5*e*log(F)^5 + 5*F^(a*c)*b^3*c^3*e^3*log(F)^3 + 4*F^(a*c)*b*c*e^5*log(F))*f*cos(2*e*x + 2*d))*integrate((3*F^(b*c*x)*b*c*e*cos(3*e*x + 3*d)*log(F) - 9*F^(b*c*x)*b*c*e*cos(e*x + d)*log(F) - 9*F^(b*c*x)*b*c*e*log(F)*sin(2*e*x + 2*d) - 3*(b^2*c^2*log(F)^2 - 2*e^2)*F^(b*c*x)*cos(2*e*x + 2*d) - (b^2*c^2*log(F)^2 - 2*e^2)*F^(b*c*x)*sin(3*e*x + 3*d) + 3*(b^2*c^2*log(F)^2 - 2*e^2)*F^(b*c*x)*sin(e*x + d) + (b^2*c^2*log(F)^2 - 2*e^2)*F^(b*c*x))/((b^4*c^4*log(F)^4 + 5*b^2*c^2*e^2*log(F)^2 + 4*e^4)*f*cos(3*e*x + 3*d)^2 + 9*(b^4*c^4*log(F)^4 + 5*b^2*c^2*e^2*log(F)^2 + 4*e^4)*f*cos(2*e*x + 2*d)^2 + 9*(b^4*c^4*log(F)^4 + 5*b^2*c^2*e^2*log(F)^2 + 4*e^4)*f*cos(e*x + d)^2 + (b^4*c^4*log(F)^4 + 5*b^2*c^2*e^2*log(F)^2 + 4*e^4)*f*sin(3*e*x + 3*d)^2 + 18*(b^4*c^4*log(F)^4 + 5*b^2*c^2*e^2*log(F)^2 + 4*e^4)*f*cos(e*x + d)*sin(2*e*x + 2*d) + 9*(b^4*c^4*log(F)^4 + 5*b^2*c^2*e^2*log(F)^2 + 4*e^4)*f*sin(2*e*x + 2*d)^2 + 9*(b^4*c^4*log(F)^4 + 5*b^2*c^2*e^2*log(F)^2 + 4*e^4)*f*sin(e*x + d)^2 + 6*(b^4*c^4*log(F)^4 + 5*b^2*c^2*e^2*log(F)^2 + 4*e^4)*f*sin(e*x + d) + (b^4*c^4*log(F)^4 + 5*b^2*c^2*e^2*log(F)^2 + 4*e^4)*f - 6*((b^4*c^4*log(F)^4 + 5*b^2*c^2*e^2*log(F)^2 + 4*e^4)*f*cos(e*x + d) + (b^4*c^4*log(F)^4 + 5*b^2*c^2*e^2*log(F)^2 + 4*e^4)*f*sin(2*e*x + 2*d))*cos(3*e*x + 3*d) - 6*(3*(b^4*c^4*log(F)^4 + 5*b^2*c^2*e^2*log(F)^2 + 4*e^4)*f*sin(e*x + d) + (b^4*c^4*log(F)^4 + 5*b^2*c^2*e^2*log(F)^2 + 4*e^4)*f*cos(2*e*x + 2*d) + 2*(3*(b^4*c^4*log(F)^4 + 5*b^2*c^2*e^2*log(F)^2 + 4*e^4)*f*cos(2*e*x + 2*d) - 3*(b^4*c^4*log(F)^4 + 5*b^2*c^2*e^2*log(F)^2 + 4*e^4)*f*sin(e*x + d) - (b^4*c^4*log(F)^4 + 5*b^2*c^2*e^2*log(F)^2 + 4*e^4)*f)*sin(3*e*x + 3*d)), x) + ((F^(a*c)*b^3*c^3*log(F)^3 + 4*F^(a*c)*b*c*e^2*log(F))*F^(b*c*x)*cos(e*x + d) - (F^(a*c)*b^2*c^2*e*log(F)^2 + 4*F^(a*c)*e^3)*F^(b*c*x)*sin(e*x + d) + 2*(F^(a*c)*b^2*c^2*e*log(F)^2 - 2*F^(a*c)*e^3)*F^(b*c*x))*sin(2*e*x + 2*d))/((b^4*c^4*log(F)^4 + 5*b^2*c^2*e^2*log(F)^2 + 4*e^4)*f*cos(2*e*x + 2*d)^2 + 4*(b^4*c^4*log(F)^4 + 5*b^2*c^2*e^2*log(F)^2 + 4*e^4)*f*cos(e*x + d)^2 + 4*(b^4*c^4*log(F)^4 + 5*b^2*c^2*e^2*log(F)^2 + 4*e^4)*f*cos(e*x + d)*sin(2*e*x + 2*d) + (b^4*c^4*log(F)^4 + 5*b^2*c^2*e^2*log(F)^2 + 4*e^4)*f*sin(2*e*x + 2*d)^2 + 4*(b^4*c^4*log(F)^4 + 5*b^2*c^2*e^2*log(F)^2 + 4*e^4)*f*sin(e*x + d)^2 + 4*(b^4*c^4*log(F)^4 + 5*b^2*c^2*e^2*log(F)^2 + 4*e^4)*f*sin(e*x + d) + (b^4*c^4*log(F)^4 + 5*b^2*c^2*e^2*log(F)^2 + 4*e^4)*f - 2*(2*(b^4*c^4*log(F)^4 + 5*b^2*c^2*e^2*log(F)^2 + 4*e^4)*f*sin(e*x + d) + (b^4*c^4*log(F)^4 + 5*b^2*c^2*e^2*log(F)^2 + 4*e^4)*f*cos(2*e*x + 2*d))

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{F^{c(a+bx)}}{f + f \sin(d + ex)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(F^(c*(a + b*x))/(f + f*sin(d + e*x)), x)

[Out] int(F^(c*(a + b*x))/(f + f*sin(d + e*x)), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\frac{\int \frac{F^{ac} F^{bcx}}{\sin(d+ex)+1} dx}{f}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(F**(c*(b*x+a))/(f+f*sin(e*x+d)), x)

[Out] Integral(F**(a*c)*F**(b*c*x)/(sin(d + e*x) + 1), x)/f

$$3.138 \quad \int \frac{F^{c(a+bx)}}{(f+f \sin(d+ex))^2} dx$$

Optimal. Leaf size=184

$$\frac{2e^{i(d+ex)Fc(a+bx)}(e + ibc \log(F)) {}_2F_1\left(2, 1 - \frac{ibc \log(F)}{e}; 2 - \frac{ibc \log(F)}{e}; ie^{i(d+ex)}\right)}{3e^2 f^2} - \frac{bc \log(F) \csc^2\left(\frac{d}{2} + \frac{ex}{2} + \frac{\pi}{4}\right) F^{c(a+bx)}}{6e^2 f^2}$$

[Out] $-1/6 * F^{(c*(b*x+a))} * \cot(1/2*d+1/4*Pi+1/2*e*x) * \csc(1/2*d+1/4*Pi+1/2*e*x)^2 / e / f^2 - 1/6 * b * c * F^{(c*(b*x+a))} * \csc(1/2*d+1/4*Pi+1/2*e*x)^2 * \ln(F) / e^2 / f^2 - 2/3 * \exp(I*(e*x+d)) * F^{(c*(b*x+a))} * \text{hypergeom}([2, 1-I*b*c*\ln(F)/e], [2-I*b*c*\ln(F)/e], I*\exp(I*(e*x+d))) * (e+I*b*c*\ln(F)) / e^2 / f^2$

Rubi [A] time = 0.10, antiderivative size = 184, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 3, integrand size = 22, $\frac{\text{number of rules}}{\text{integrand size}} = 0.136$, Rules used = {4456, 4448, 4450}

$$\frac{2e^{i(d+ex)Fc(a+bx)}(e + ibc \log(F)) {}_2F_1\left(2, 1 - \frac{ibc \log(F)}{e}; 2 - \frac{ibc \log(F)}{e}; ie^{i(d+ex)}\right)}{3e^2 f^2} - \frac{bc \log(F) \csc^2\left(\frac{d}{2} + \frac{ex}{2} + \frac{\pi}{4}\right) F^{c(a+bx)}}{6e^2 f^2}$$

Antiderivative was successfully verified.

[In] Int[F^(c*(a + b*x))/(f + f*Sin[d + e*x])^2, x]

[Out] $-(F^{(c*(a + b*x))} * \cot[d/2 + Pi/4 + (e*x)/2] * \csc[d/2 + Pi/4 + (e*x)/2]^2) / (6 * e * f^2) - (b * c * F^{(c*(a + b*x))} * \csc[d/2 + Pi/4 + (e*x)/2]^2 * \log[F]) / (6 * e^2 * f^2) - (2 * E^{(I*(d + e*x))} * F^{(c*(a + b*x))} * \text{Hypergeometric2F1}[2, 1 - (I*b*c*\log[F])/e, 2 - (I*b*c*\log[F])/e, I * E^{(I*(d + e*x))}] * (e + I*b*c*\log[F])) / (3 * e^2 * f^2)$

Rule 4448

Int[(F_)^((c_.)*((a_.) + (b_.)*(x_)))*Sec[(d_.) + (e_.)*(x_)]^(n_), x_Symbol] :> -Simp[(b*c*Log[F]*F^(c*(a + b*x))*Sec[d + e*x]^(n - 2))/(e^2*(n - 1)*(n - 2)), x] + (Dist[(e^2*(n - 2)^2 + b^2*c^2*Log[F]^2)/(e^2*(n - 1)*(n - 2)), Int[F^(c*(a + b*x))*Sec[d + e*x]^(n - 2), x], x] + Simp[(F^(c*(a + b*x))*Sec[d + e*x]^(n - 1)*Sin[d + e*x]/(e*(n - 1)), x]) /; FreeQ[{F, a, b, c, d, e}, x] && NeQ[b^2*c^2*Log[F]^2 + e^2*(n - 2)^2, 0] && GtQ[n, 1] && NeQ[n, 2]

Rule 4450

Int[(F_)^((c_.)*((a_.) + (b_.)*(x_)))*Sec[(d_.) + Pi*(k_.) + (e_.)*(x_)]^(n_.), x_Symbol] :> Simp[(2^n * E^(I*k*n*Pi) * E^(I*n*(d + e*x)) * F^(c*(a + b*x)) * Hypergeometric2F1[n, n/2 - (I*b*c*Log[F])/(2*e), 1 + n/2 - (I*b*c*Log[F])/(2*e), -(E^(2*I*k*Pi) * E^(2*I*(d + e*x)))] / (I * e^n + b*c*Log[F]), x] /; FreeQ[{F, a, b, c, d, e}, x] && IntegerQ[4*k] && IntegerQ[n]

Rule 4456

Int[(F_)^((c_.)*((a_.) + (b_.)*(x_)))*((f_.) + (g_.)*Sin[(d_.) + (e_.)*(x_)]^(n_.), x_Symbol] :> Dist[2^n * f^n, Int[F^(c*(a + b*x))*Cos[d/2 + (e*x)/2 - (f*Pi)/(4*g)]^(2*n), x], x] /; FreeQ[{F, a, b, c, d, e, f, g}, x] && EqQ[f^2 - g^2, 0] && ILtQ[n, 0]

Rubi steps

$$\int \frac{F^{c(a+bx)}}{(f + f \sin(d + ex))^2} dx = \frac{\int F^{c(a+bx)} \sec^4\left(\frac{d}{2} - \frac{\pi}{4} + \frac{ex}{2}\right) dx}{4f^2}$$

$$= -\frac{F^{c(a+bx)} \cot\left(\frac{d}{2} + \frac{\pi}{4} + \frac{ex}{2}\right) \csc^2\left(\frac{d}{2} + \frac{\pi}{4} + \frac{ex}{2}\right)}{6ef^2} - \frac{bcF^{c(a+bx)} \csc^2\left(\frac{d}{2} + \frac{\pi}{4} + \frac{ex}{2}\right) \log(F)}{6e^2f^2}$$

$$= -\frac{F^{c(a+bx)} \cot\left(\frac{d}{2} + \frac{\pi}{4} + \frac{ex}{2}\right) \csc^2\left(\frac{d}{2} + \frac{\pi}{4} + \frac{ex}{2}\right)}{6ef^2} - \frac{bcF^{c(a+bx)} \csc^2\left(\frac{d}{2} + \frac{\pi}{4} + \frac{ex}{2}\right) \log(F)}{6e^2f^2}$$

Mathematica [A] time = 3.20, size = 240, normalized size = 1.30

$$F^{c(a+bx)} \left(\sin\left(\frac{1}{2}(d + ex)\right) + \cos\left(\frac{1}{2}(d + ex)\right) \right) \left((-1 + i) (b^2 c^2 \log^2(F) + e^2) \left(\sin\left(\frac{1}{2}(d + ex)\right) + \cos\left(\frac{1}{2}(d + ex)\right) \right) \right)^3$$

Antiderivative was successfully verified.

[In] Integrate[F^(c*(a + b*x))/(f + f*Sin[d + e*x])^2,x]

[Out] (F^(c*(a + b*x))*(Cos[(d + e*x)/2] + Sin[(d + e*x)/2])*(2*e^2*Sin[(d + e*x)/2] - e*(e + b*c*Log[F])*(Cos[(d + e*x)/2] + Sin[(d + e*x)/2]) + 2*(e^2 + b^2*c^2*Log[F]^2)*Sin[(d + e*x)/2]*(Cos[(d + e*x)/2] + Sin[(d + e*x)/2])^2 - (1 - I)*(1 - (1 - I)*Hypergeometric2F1[1, ((-I)*b*c*Log[F])/e, 1 - (I*b*c*Log[F])/e, I*Cos[d + e*x] - Sin[d + e*x]])*(e^2 + b^2*c^2*Log[F]^2)*(Cos[(d + e*x)/2] + Sin[(d + e*x)/2])^3)/(3*e^3*f^2*(1 + Sin[d + e*x])^2)

fricas [F] time = 0.60, size = 0, normalized size = 0.00

$$\text{integral}\left(-\frac{F^{bcx+ac}}{f^2 \cos(ex + d)^2 - 2f^2 \sin(ex + d) - 2f^2}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(F^(c*(b*x+a))/(f+f*sin(e*x+d))^2,x, algorithm="fricas")

[Out] integral(-F^(b*c*x + a*c)/(f^2*cos(e*x + d)^2 - 2*f^2*sin(e*x + d) - 2*f^2), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{F^{(bx+a)c}}{(f \sin(ex + d) + f)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(F^(c*(b*x+a))/(f+f*sin(e*x+d))^2,x, algorithm="giac")

[Out] integrate(F^((b*x + a)*c)/(f*sin(e*x + d) + f)^2, x)

maple [F] time = 0.95, size = 0, normalized size = 0.00

$$\int \frac{F^{c(bx+a)}}{(f + f \sin(ex + d))^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(F^(c*(b*x+a))/(f+f*sin(e*x+d))^2,x)

[Out] int(F^(c*(b*x+a))/(f+f*sin(e*x+d))^2,x)

maxima [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(F^(c*(b*x+a))/(f+f*sin(e*x+d))^2,x, algorithm="maxima")

[Out] Timed out

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{F^{c(a+bx)}}{(f + f \sin(d + ex))^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(F^(c*(a + b*x))/(f + f*sin(d + e*x))^2,x)

[Out] int(F^(c*(a + b*x))/(f + f*sin(d + e*x))^2, x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{F^{ac} F^{bcx}}{\frac{\sin^2(d+ex) + 2 \sin(d+ex) + 1}{f^2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(F**(c*(b*x+a))/(f+f*sin(e*x+d))**2,x)

[Out] Integral(F**(a*c)*F**(b*c*x)/(sin(d + e*x)**2 + 2*sin(d + e*x) + 1), x)/f**2

3.139 $\int F^{c(a+bx)}(f + f \cos(d + ex))^2 dx$

Optimal. Leaf size=245

$$\frac{2ef^2 \sin(d + ex)F^{ac+bcx}}{b^2c^2 \log^2(F) + e^2} + \frac{bcf^2 \log(F) \cos^2(d + ex)F^{ac+bcx}}{b^2c^2 \log^2(F) + 4e^2} + \frac{2bcf^2 \log(F) \cos(d + ex)F^{ac+bcx}}{b^2c^2 \log^2(F) + e^2} + \frac{2ef^2 \sin(d + ex)F^{ac+bcx}}{b^2c^2 \log^2(F) + e^2}$$

[Out] $f^2 F^{(b*c*x+a*c)}/b/c/\ln(F)+2*b*c*f^2 F^{(b*c*x+a*c)}*\cos(e*x+d)*\ln(F)/(e^2+b^2*c^2*\ln(F)^2)+2*e^2*f^2 F^{(b*c*x+a*c)}/b/c/\ln(F)/(4*e^2+b^2*c^2*\ln(F)^2)+b*c*f^2 F^{(b*c*x+a*c)}*\cos(e*x+d)^2*\ln(F)/(4*e^2+b^2*c^2*\ln(F)^2)+2*e*f^2 F^{(b*c*x+a*c)}*\sin(e*x+d)/(e^2+b^2*c^2*\ln(F)^2)+2*e*f^2 F^{(b*c*x+a*c)}*\cos(e*x+d)*\sin(e*x+d)/(4*e^2+b^2*c^2*\ln(F)^2)$

Rubi [A] time = 0.33, antiderivative size = 245, normalized size of antiderivative = 1.00, number of steps used = 8, number of rules used = 6, integrand size = 22, $\frac{\text{number of rules}}{\text{integrand size}} = 0.273$, Rules used = {6741, 12, 6742, 2194, 4433, 4435}

$$\frac{2ef^2 \sin(d + ex)F^{ac+bcx}}{b^2c^2 \log^2(F) + e^2} + \frac{bcf^2 \log(F) \cos^2(d + ex)F^{ac+bcx}}{b^2c^2 \log^2(F) + 4e^2} + \frac{2bcf^2 \log(F) \cos(d + ex)F^{ac+bcx}}{b^2c^2 \log^2(F) + e^2} + \frac{2ef^2 \sin(d + ex)F^{ac+bcx}}{b^2c^2 \log^2(F) + e^2}$$

Antiderivative was successfully verified.

[In] Int[F^(c*(a + b*x))*(f + f*Cos[d + e*x])^2, x]

[Out] $(f^2 F^{(a*c + b*c*x)})/(b*c*\text{Log}[F]) + (2*b*c*f^2 F^{(a*c + b*c*x)}*\text{Cos}[d + e*x]*\text{Log}[F])/(e^2 + b^2*c^2*\text{Log}[F]^2) + (2*e^2*f^2 F^{(a*c + b*c*x)})/(b*c*\text{Log}[F]*(4*e^2 + b^2*c^2*\text{Log}[F]^2)) + (b*c*f^2 F^{(a*c + b*c*x)}*\text{Cos}[d + e*x]^2*\text{Log}[F])/(4*e^2 + b^2*c^2*\text{Log}[F]^2) + (2*e*f^2 F^{(a*c + b*c*x)}*\text{Sin}[d + e*x])/(e^2 + b^2*c^2*\text{Log}[F]^2) + (2*e*f^2 F^{(a*c + b*c*x)}*\text{Cos}[d + e*x]*\text{Sin}[d + e*x])/(4*e^2 + b^2*c^2*\text{Log}[F]^2)$

Rule 12

Int[(a_)*(u_), x_Symbol] := Dist[a, Int[u, x], x] /; FreeQ[a, x] && !MatchQ[u, (b_)*(v_)] /; FreeQ[b, x]

Rule 2194

Int[((F_)^((c_)*((a_) + (b_)*(x_))))^(n_), x_Symbol] := Simp[(F^(c*(a + b*x)))^n/(b*c*n*Log[F]), x] /; FreeQ[{F, a, b, c, n}, x]

Rule 4433

Int[Cos[(d_) + (e_)*(x_)]*(F_)^((c_)*((a_) + (b_)*(x_))), x_Symbol] := Simp[(b*c*Log[F]*F^(c*(a + b*x))*Cos[d + e*x]/(e^2 + b^2*c^2*Log[F]^2), x] + Simp[(e*F^(c*(a + b*x))*Sin[d + e*x]/(e^2 + b^2*c^2*Log[F]^2), x] /; FreeQ[{F, a, b, c, d, e}, x] && NeQ[e^2 + b^2*c^2*Log[F]^2, 0]

Rule 4435

Int[Cos[(d_) + (e_)*(x_)]^(m_)*(F_)^((c_)*((a_) + (b_)*(x_))), x_Symbol] := Simp[(b*c*Log[F]*F^(c*(a + b*x))*Cos[d + e*x]^m/(e^2*m^2 + b^2*c^2*Log[F]^2), x] + (Dist[(m*(m - 1)*e^2)/(e^2*m^2 + b^2*c^2*Log[F]^2), Int[F^(c*(a + b*x))*Cos[d + e*x]^(m - 2), x], x] + Simp[(e*m*F^(c*(a + b*x))*Sin[d + e*x]*Cos[d + e*x]^(m - 1)/(e^2*m^2 + b^2*c^2*Log[F]^2), x]) /; FreeQ[{F, a, b, c, d, e}, x] && NeQ[e^2*m^2 + b^2*c^2*Log[F]^2, 0] && GtQ[m, 1]

Rule 6741

Int[u_, x_Symbol] := With[{v = NormalizeIntegrand[u, x]}, Int[v, x] /; v != u]

Rule 6742

Int[u_, x_Symbol] := With[{v = ExpandIntegrand[u, x]}, Int[v, x] /; SumQ[v]]

Rubi steps

$$\begin{aligned}
 \int F^{c(a+bx)}(f + f \cos(d + ex))^2 dx &= \int f^2 F^{ac+bcx} (1 + \cos(d + ex))^2 dx \\
 &= f^2 \int F^{ac+bcx} (1 + \cos(d + ex))^2 dx \\
 &= f^2 \int (F^{ac+bcx} + 2F^{ac+bcx} \cos(d + ex) + F^{ac+bcx} \cos^2(d + ex)) dx \\
 &= f^2 \int F^{ac+bcx} dx + f^2 \int F^{ac+bcx} \cos^2(d + ex) dx + (2f^2) \int F^{ac+bcx} \cos(d + ex) dx \\
 &= \frac{f^2 F^{ac+bcx}}{bc \log(F)} + \frac{2bc f^2 F^{ac+bcx} \cos(d + ex) \log(F)}{e^2 + b^2 c^2 \log^2(F)} + \frac{bc f^2 F^{ac+bcx} \cos^2(d + ex) \log(F)}{4e^2 + b^2 c^2 \log^2(F)} \\
 &= \frac{f^2 F^{ac+bcx}}{bc \log(F)} + \frac{2bc f^2 F^{ac+bcx} \cos(d + ex) \log(F)}{e^2 + b^2 c^2 \log^2(F)} + \frac{2e^2 f^2 F^{ac+bcx}}{bc \log(F) (4e^2 + b^2 c^2 \log^2(F))}
 \end{aligned}$$

Mathematica [A] time = 0.64, size = 228, normalized size = 0.93

$$\frac{f^2 F^{c(a+bx)} (3b^4 c^4 \log^4(F) + 4b^3 c^3 e \log^3(F) \sin(d + ex) + 2b^3 c^3 e \log^3(F) \sin(2(d + ex)) + b^2 c^2 \log^2(F) \cos(2(d + ex)))}{2(b^5 c^5 \log^5(F) + 5b^3 c^3 e^2 \log^3(F) + 4b^3 c^3 e \log^3(F) \sin(2(d + ex)) + 16b^2 c^2 e \log^2(F) \cos(2(d + ex)) + 15b^2 c^2 e^2 \log^2(F) \sin^2(d + ex) + 12e^4 + 3b^4 c^4 \log^4(F))}$$

Antiderivative was successfully verified.

[In] Integrate[F^(c*(a + b*x))*(f + f*Cos[d + e*x])^2,x]

[Out] (f^2 F^(c*(a + b*x))*(12*e^4 + 15*b^2*c^2*e^2*Log[F]^2 + 3*b^4*c^4*Log[F]^4 + b^2*c^2*Cos[2*(d + e*x)]*Log[F]^2*(e^2 + b^2*c^2*Log[F]^2) + 4*b^2*c^2*Cos[d + e*x]*Log[F]^2*(4*e^2 + b^2*c^2*Log[F]^2) + 16*b*c*e^3*Log[F]*Sin[d + e*x] + 4*b^3*c^3*e*Log[F]^3*Sin[d + e*x] + 2*b*c*e^3*Log[F]*Sin[2*(d + e*x)]) + 2*b^3*c^3*e*Log[F]^3*Sin[2*(d + e*x)])/(2*(4*b*c*e^4*Log[F] + 5*b^3*c^3*e^2*Log[F]^3 + b^5*c^5*Log[F]^5))

fricas [A] time = 1.39, size = 242, normalized size = 0.99

$$\frac{(6e^4 f^2 + (b^4 c^4 f^2 \cos(ex + d))^2 + 2b^4 c^4 f^2 \cos(ex + d) + b^4 c^4 f^2) \log(F)^4 + (b^2 c^2 e^2 f^2 \cos(ex + d))^2 + 8b^2 c^2 e^2 f^2 \cos(ex + d)}{b^5 c^5 \log^5(F) + 5b^3 c^3 e^2 \log^3(F) + 4b^3 c^3 e \log^3(F) \sin(2(d + ex)) + 16b^2 c^2 e \log^2(F) \cos(2(d + ex)) + 15b^2 c^2 e^2 \log^2(F) \sin^2(d + ex) + 12e^4 + 3b^4 c^4 \log^4(F)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(F^(c*(b*x+a))*(f+f*cos(e*x+d))^2,x, algorithm="fricas")

[Out] (6*e^4*f^2 + (b^4*c^4*f^2*cos(e*x + d))^2 + 2*b^4*c^4*f^2*cos(e*x + d) + b^4*c^4*f^2)*log(F)^4 + (b^2*c^2*e^2*f^2*cos(e*x + d))^2 + 8*b^2*c^2*e^2*f^2*cos(e*x + d) + 7*b^2*c^2*e^2*f^2*log(F)^2 + 2*((b^3*c^3*e*f^2*cos(e*x + d) + b^3*c^3*e*f^2)*log(F)^3 + (b*c*e^3*f^2*cos(e*x + d) + 4*b*c*e^3*f^2)*log(F))*sin(e*x + d)*F^(b*c*x + a*c)/(b^5*c^5*log(F)^5 + 5*b^3*c^3*e^2*log(F)^3 + 4*b*c*e^4*log(F))

giac [C] time = 0.37, size = 1772, normalized size = 7.23

result too large to display

maple [A] time = 0.31, size = 371, normalized size = 1.51

$$\frac{3F^{ac} f^2 F^{bcx}}{2bc \ln(F)} + \frac{4F^{ac} f^2 e^{bcx \ln(F)} \tan\left(\frac{d}{2} + \frac{ex}{2}\right)}{\left(1 + \tan^2\left(\frac{d}{2} + \frac{ex}{2}\right)\right) (e^2 + b^2 c^2 \ln(F)^2)} + \frac{2F^{ac} f^2 bc \ln(F) e^{bcx \ln(F)}}{\left(1 + \tan^2\left(\frac{d}{2} + \frac{ex}{2}\right)\right) (e^2 + b^2 c^2 \ln(F)^2)} - \frac{2F^{ac} f^2 bc \ln(F) e^{bcx \ln(F)}}{\left(1 + \tan^2\left(\frac{d}{2} + \frac{ex}{2}\right)\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(F^(c*(b*x+a))*(f+f*cos(e*x+d))^2,x)

[Out] $\frac{3}{2} F^{(a*c)} * f^2 / b / c / \ln(F) * F^{(b*c*x)} + 4 * F^{(a*c)} * f^2 / (1 + \tan(1/2*d + 1/2*e*x)^2) / (e^2 + b^2*c^2*\ln(F)^2) * e * \exp(b*c*x*\ln(F)) * \tan(1/2*d + 1/2*e*x) + 2 * F^{(a*c)} * f^2 / (1 + \tan(1/2*d + 1/2*e*x)^2) * b*c*\ln(F) / (e^2 + b^2*c^2*\ln(F)^2) * \exp(b*c*x*\ln(F)) - 2 * F^{(a*c)} * f^2 / (1 + \tan(1/2*d + 1/2*e*x)^2) * b*c*\ln(F) / (e^2 + b^2*c^2*\ln(F)^2) * \exp(b*c*x*\ln(F)) * \tan(1/2*d + 1/2*e*x)^2 + 1/2 * F^{(a*c)} * f^2 / (1 + \tan(e*x+d)^2) / (4 * e^2 + b^2*c^2*\ln(F)^2) * b*c*\ln(F) * \exp(b*c*x*\ln(F)) + 2 * F^{(a*c)} * f^2 / (1 + \tan(e*x+d)^2) / (4 * e^2 + b^2*c^2*\ln(F)^2) * e * \exp(b*c*x*\ln(F)) * \tan(e*x+d) - 1/2 * F^{(a*c)} * f^2 / (1 + \tan(e*x+d)^2) / (4 * e^2 + b^2*c^2*\ln(F)^2) * b*c*\ln(F) * \exp(b*c*x*\ln(F)) * \tan(e*x+d)^2$

maxima [B] time = 0.45, size = 578, normalized size = 2.36

$$\frac{\left(F^{ac} b^2 c^2 \cos(2d) \log(F)^2 + 2 F^{ac} b c e \log(F) \sin(2d)\right) F^{bcx} \cos(2ex) + \left(F^{ac} b^2 c^2 \cos(2d) \log(F)^2 - 2 F^{ac} b c e \log(F)\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(F^(c*(b*x+a))*(f+f*cos(e*x+d))^2,x, algorithm="maxima")

[Out] $\frac{1}{4} * ((F^{(a*c)} * b^2 * c^2 * \cos(2*d) * \log(F)^2 + 2 * F^{(a*c)} * b * c * e * \log(F) * \sin(2*d)) * F^{(b*c*x)} * \cos(2*e*x) + (F^{(a*c)} * b^2 * c^2 * \cos(2*d) * \log(F)^2 - 2 * F^{(a*c)} * b * c * e * \log(F) * \sin(2*d)) * F^{(b*c*x)} * \cos(2*e*x + 4*d) - (F^{(a*c)} * b^2 * c^2 * \log(F)^2 * \sin(2*d) - 2 * F^{(a*c)} * b * c * e * \cos(2*d) * \log(F)) * F^{(b*c*x)} * \sin(2*e*x) + (F^{(a*c)} * b^2 * c^2 * \log(F)^2 * \sin(2*d) + 2 * F^{(a*c)} * b * c * e * \cos(2*d) * \log(F)) * F^{(b*c*x)} * \sin(2*e*x + 4*d) + 2 * (F^{(a*c)} * b^2 * c^2 * \cos(2*d)^2 * \log(F)^2 + F^{(a*c)} * b^2 * c^2 * \log(F)^2 * \sin(2*d)^2 + 4 * (F^{(a*c)} * \cos(2*d)^2 + F^{(a*c)} * \sin(2*d)^2) * e^2) * F^{(b*c*x)}) * f^2 / (b^3 * c^3 * \cos(2*d)^2 * \log(F)^3 + b^3 * c^3 * \log(F)^3 * \sin(2*d)^2 + 4 * (b * c * \cos(2*d)^2 * \log(F) + b * c * \log(F) * \sin(2*d)^2) * e^2) + ((F^{(a*c)} * b * c * \cos(d) * \log(F) - F^{(a*c)} * e * \sin(d)) * F^{(b*c*x)} * \cos(e*x + 2*d) + (F^{(a*c)} * b * c * \cos(d) * \log(F) + F^{(a*c)} * e * \sin(d)) * F^{(b*c*x)} * \cos(e*x) + (F^{(a*c)} * b * c * \log(F) * \sin(d) + F^{(a*c)} * e * \cos(d)) * F^{(b*c*x)} * \sin(e*x + 2*d) - (F^{(a*c)} * b * c * \log(F) * \sin(d) - F^{(a*c)} * e * \cos(d)) * F^{(b*c*x)} * \sin(e*x)) * f^2 / (b^2 * c^2 * \cos(d)^2 * \log(F)^2 + b^2 * c^2 * \log(F)^2 * \sin(d)^2 + (\cos(d)^2 + \sin(d)^2) * e^2) + F^{(b*c*x + a*c)} * f^2 / (b * c * \log(F))$

mupad [B] time = 3.31, size = 247, normalized size = 1.01

$$\frac{F^{a+c} f^2 \left(6e^4 + \frac{3b^4 c^4 \ln(F)^4}{2} + 2b^4 c^4 \cos(d+ex) \ln(F)^4 + \frac{b^4 c^4 \ln(F)^4 \cos(2d+2ex)}{2} + \frac{15b^2 c^2 e^2 \ln(F)^2}{2} + 8bce^3 \sin(d)\right)}{b^2 c^2 \ln(F)^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(F^(c*(a + b*x))*(f + f*cos(d + e*x))^2,x)

[Out] $(F^{(a*c + b*c*x)} * f^2 * (6 * e^4 + (3 * b^4 * c^4 * \log(F)^4) / 2 + 2 * b^4 * c^4 * \cos(d + e*x) * \log(F)^4 + (b^4 * c^4 * \log(F)^4 * \cos(2*d + 2*e*x)) / 2 + (15 * b^2 * c^2 * e^2 * \log(F)^2) / 2 + 8 * b * c * e^3 * \sin(d + e*x) * \log(F) + 8 * b^2 * c^2 * e^2 * \cos(d + e*x) * \log(F)^2 + b^3 * c^3 * e * \log(F)^3 * \sin(2*d + 2*e*x) + b * c * e^3 * \log(F) * \sin(2*d + 2*e*x) + (b^2 * c^2 * e^2 * \log(F)^2 * \cos(2*d + 2*e*x)) / 2 + 2 * b^3 * c^3 * e * \sin(d + e*x) * \log(F)^3) / (b * c * \log(F) * (4 * e^4 + b^4 * c^4 * \log(F)^4 + 5 * b^2 * c^2 * e^2 * \log(F)^2))$

sympy [A] time = 58.63, size = 1760, normalized size = 7.18

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(F**(c*(b*x+a))*(f+f*cos(e*x+d))**2,x)

[Out] Piecewise((f**2*x*sin(d + e*x)**2/2 + f**2*x*cos(d + e*x)**2/2 + f**2*x + f**2*sin(d + e*x)*cos(d + e*x)/(2*e) + 2*f**2*sin(d + e*x)/e, Eq(F, 1)), (zoo**4*f**2*exp(-2*I*e/(b*c))**(a*c)*exp(-2*I*e/(b*c))**(b*c*x)*sin(d + e*x)**2 + zoo**4*f**2*exp(-2*I*e/(b*c))**(a*c)*exp(-2*I*e/(b*c))**(b*c*x)*sin(d + e*x)*cos(d + e*x) + zoo**4*f**2*exp(-2*I*e/(b*c))**(a*c)*exp(-2*I*e/(b*c))**(b*c*x)*cos(d + e*x)**2, Eq(F, exp(-2*I*e/(b*c)))), (zoo**4*f**2*exp(-I*e/(b*c))**(a*c)*exp(-I*e/(b*c))**(b*c*x)*sin(d + e*x) + zoo**4*f**2*exp(-I*e/(b*c))**(a*c)*exp(-I*e/(b*c))**(b*c*x)*cos(d + e*x), Eq(F, exp(-I*e/(b*c)))), (zoo**4*f**2*exp(I*e/(b*c))**(a*c)*exp(I*e/(b*c))**(b*c*x)*sin(d + e*x) + zoo**4*f**2*exp(I*e/(b*c))**(a*c)*exp(I*e/(b*c))**(b*c*x)*cos(d + e*x), Eq(F, exp(I*e/(b*c)))), (zoo**4*f**2*exp(2*I*e/(b*c))**(a*c)*exp(2*I*e/(b*c))**(b*c*x)*sin(d + e*x)**2 + zoo**4*f**2*exp(2*I*e/(b*c))**(a*c)*exp(2*I*e/(b*c))**(b*c*x)*sin(d + e*x)*cos(d + e*x) + zoo**4*f**2*exp(2*I*e/(b*c))**(a*c)*exp(2*I*e/(b*c))**(b*c*x)*cos(d + e*x)**2, Eq(F, exp(2*I*e/(b*c)))), (F**(a*c)*(f**2*x*sin(d + e*x)**2/2 + f**2*x*cos(d + e*x)**2/2 + f**2*x + f**2*sin(d + e*x)*cos(d + e*x)/(2*e) + 2*f**2*sin(d + e*x)/e), Eq(b, 0)), (f**2*x*sin(d + e*x)**2/2 + f**2*x*cos(d + e*x)**2/2 + f**2*x + f**2*sin(d + e*x)*cos(d + e*x)/(2*e) + 2*f**2*sin(d + e*x)/e, Eq(c, 0)), (F**(a*c)*F**(b*c*x)*b**4*c**4*f**2*log(F)**4*cos(d + e*x)**2/(b**5*c**5*log(F)**5 + 5*b**3*c**3*e**2*log(F)**3 + 4*b*c*e**4*log(F)) + 2*F**(a*c)*F**(b*c*x)*b**4*c**4*f**2*log(F)**4*cos(d + e*x)/(b**5*c**5*log(F)**5 + 5*b**3*c**3*e**2*log(F)**3 + 4*b*c*e**4*log(F)) + F**(a*c)*F**(b*c*x)*b**4*c**4*f**2*log(F)**4/(b**5*c**5*log(F)**5 + 5*b**3*c**3*e**2*log(F)**3 + 4*b*c*e**4*log(F)) + 2*F**(a*c)*F**(b*c*x)*b**3*c**3*e*f**2*log(F)**3*sin(d + e*x)*cos(d + e*x)/(b**5*c**5*log(F)**5 + 5*b**3*c**3*e**2*log(F)**3 + 4*b*c*e**4*log(F)) + 2*F**(a*c)*F**(b*c*x)*b**3*c**3*e*f**2*log(F)**3*sin(d + e*x)/(b**5*c**5*log(F)**5 + 5*b**3*c**3*e**2*log(F)**3 + 4*b*c*e**4*log(F)) + 2*F**(a*c)*F**(b*c*x)*b**2*c**2*e**2*f**2*log(F)**2*sin(d + e*x)**2/(b**5*c**5*log(F)**5 + 5*b**3*c**3*e**2*log(F)**3 + 4*b*c*e**4*log(F)) + 3*F**(a*c)*F**(b*c*x)*b**2*c**2*e**2*f**2*log(F)**2*cos(d + e*x)**2/(b**5*c**5*log(F)**5 + 5*b**3*c**3*e**2*log(F)**3 + 4*b*c*e**4*log(F)) + 8*F**(a*c)*F**(b*c*x)*b**2*c**2*e**2*f**2*log(F)**2*cos(d + e*x)/(b**5*c**5*log(F)**5 + 5*b**3*c**3*e**2*log(F)**3 + 4*b*c*e**4*log(F)) + 5*F**(a*c)*F**(b*c*x)*b**2*c**2*e**2*f**2*log(F)**2/(b**5*c**5*log(F)**5 + 5*b**3*c**3*e**2*log(F)**3 + 4*b*c*e**4*log(F)) + 2*F**(a*c)*F**(b*c*x)*b*c*e**3*f**2*log(F)*sin(d + e*x)*cos(d + e*x)/(b**5*c**5*log(F)**5 + 5*b**3*c**3*e**2*log(F)**3 + 4*b*c*e**4*log(F)) + 8*F**(a*c)*F**(b*c*x)*b*c*e**3*f**2*log(F)*sin(d + e*x)/(b**5*c**5*log(F)**5 + 5*b**3*c**3*e**2*log(F)**3 + 4*b*c*e**4*log(F)) + 2*F**(a*c)*F**(b*c*x)*e**4*f**2*sin(d + e*x)**2/(b**5*c**5*log(F)**5 + 5*b**3*c**3*e**2*log(F)**3 + 4*b*c*e**4*log(F)) + 2*F**(a*c)*F**(b*c*x)*e**4*f**2*cos(d + e*x)**2/(b**5*c**5*log(F)**5 + 5*b**3*c**3*e**2*log(F)**3 + 4*b*c*e**4*log(F)) + 4*F**(a*c)*F**(b*c*x)*e**4*f**2/(b**5*c**5*log(F)**5 + 5*b**3*c**3*e**2*log(F)**3 + 4*b*c*e**4*log(F)), True))

3.140 $\int F^{c(a+bx)}(f + f \cos(d + ex)) dx$

Optimal. Leaf size=98

$$\frac{ef \sin(d + ex)F^{ac+bcx}}{b^2c^2 \log^2(F) + e^2} + \frac{bcf \log(F) \cos(d + ex)F^{ac+bcx}}{b^2c^2 \log^2(F) + e^2} + \frac{fF^{ac+bcx}}{bc \log(F)}$$

[Out] $f * F^{(b * c * x + a * c)} / b / c / \ln(F) + b * c * f * F^{(b * c * x + a * c)} * \cos(e * x + d) * \ln(F) / (e^2 + b^2 * c^2 * \ln(F)^2) + e * f * F^{(b * c * x + a * c)} * \sin(e * x + d) / (e^2 + b^2 * c^2 * \ln(F)^2)$

Rubi [A] time = 0.15, antiderivative size = 98, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 5, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.250$, Rules used = {6741, 12, 6742, 2194, 4433}

$$\frac{ef \sin(d + ex)F^{ac+bcx}}{b^2c^2 \log^2(F) + e^2} + \frac{bcf \log(F) \cos(d + ex)F^{ac+bcx}}{b^2c^2 \log^2(F) + e^2} + \frac{fF^{ac+bcx}}{bc \log(F)}$$

Antiderivative was successfully verified.

[In] Int[F^(c*(a + b*x))*(f + f*Cos[d + e*x]),x]

[Out] $(f * F^{(a * c + b * c * x)}) / (b * c * \text{Log}[F]) + (b * c * f * F^{(a * c + b * c * x)} * \text{Cos}[d + e * x] * \text{Log}[F]) / (e^2 + b^2 * c^2 * \text{Log}[F]^2) + (e * f * F^{(a * c + b * c * x)} * \text{Sin}[d + e * x]) / (e^2 + b^2 * c^2 * \text{Log}[F]^2)$

Rule 12

Int[(a_)*(u_), x_Symbol] := Dist[a, Int[u, x], x] /; FreeQ[a, x] && !MatchQ[u, (b_)*(v_)] /; FreeQ[b, x]

Rule 2194

Int[((F_)^((c_.)*((a_.) + (b_.)*(x_))))^(n_.), x_Symbol] := Simp[(F^(c*(a + b*x)))^n/(b*c*n*Log[F]), x] /; FreeQ[{F, a, b, c, n}, x]

Rule 4433

Int[Cos[(d_.) + (e_.)*(x_)]*(F_)^((c_.)*((a_.) + (b_.)*(x_))), x_Symbol] := Simp[(b*c*Log[F]*F^(c*(a + b*x))*Cos[d + e*x]/(e^2 + b^2*c^2*Log[F]^2), x] + Simp[(e*F^(c*(a + b*x))*Sin[d + e*x]/(e^2 + b^2*c^2*Log[F]^2), x] /; FreeQ[{F, a, b, c, d, e}, x] && NeQ[e^2 + b^2*c^2*Log[F]^2, 0]

Rule 6741

Int[u_, x_Symbol] := With[{v = NormalizeIntegrand[u, x]}, Int[v, x] /; v != u]

Rule 6742

Int[u_, x_Symbol] := With[{v = ExpandIntegrand[u, x]}, Int[v, x] /; SumQ[v]

Rubi steps

$$\begin{aligned}
\int F^{c(a+bx)}(f + f \cos(d + ex)) dx &= \int f F^{ac+bcx}(1 + \cos(d + ex)) dx \\
&= f \int F^{ac+bcx}(1 + \cos(d + ex)) dx \\
&= f \int (F^{ac+bcx} + F^{ac+bcx} \cos(d + ex)) dx \\
&= f \int F^{ac+bcx} dx + f \int F^{ac+bcx} \cos(d + ex) dx \\
&= \frac{f F^{ac+bcx}}{bc \log(F)} + \frac{bc f F^{ac+bcx} \cos(d + ex) \log(F)}{e^2 + b^2 c^2 \log^2(F)} + \frac{ef F^{ac+bcx} \sin(d + ex)}{e^2 + b^2 c^2 \log^2(F)}
\end{aligned}$$

Mathematica [A] time = 0.24, size = 82, normalized size = 0.84

$$\frac{f F^{c(a+bx)} (b^2 c^2 \log^2(F) \cos(d + ex) + b^2 c^2 \log^2(F) + b c e \log(F) \sin(d + ex) + e^2)}{bc \log(F) (b^2 c^2 \log^2(F) + e^2)}$$

Antiderivative was successfully verified.

[In] Integrate[F^(c*(a + b*x))*(f + f*Cos[d + e*x]),x]

[Out] (f*F^(c*(a + b*x))*(e^2 + b^2*c^2*Log[F]^2 + b^2*c^2*Cos[d + e*x]*Log[F]^2 + b*c*e*Log[F]*Sin[d + e*x]))/(b*c*Log[F]*(e^2 + b^2*c^2*Log[F]^2))

fricas [A] time = 0.70, size = 80, normalized size = 0.82

$$\frac{(bc e f \log(F) \sin(ex + d) + e^2 f + (b^2 c^2 f \cos(ex + d) + b^2 c^2 f) \log(F)^2) F^{bcx+ac}}{b^3 c^3 \log(F)^3 + b c e^2 \log(F)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(F^(c*(b*x+a))*(f+f*cos(e*x+d)),x, algorithm="fricas")

[Out] (b*c*e*f*log(F)*sin(e*x + d) + e^2*f + (b^2*c^2*f*cos(e*x + d) + b^2*c^2*f)*log(F)^2)*F^(b*c*x + a*c)/(b^3*c^3*log(F)^3 + b*c*e^2*log(F))

giac [C] time = 0.25, size = 938, normalized size = 9.57

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(F^(c*(b*x+a))*(f+f*cos(e*x+d)),x, algorithm="giac")

[Out] (2*b*c*f*cos(1/2*pi*b*c*x*sgn(F) - 1/2*pi*b*c*x + 1/2*pi*a*c*sgn(F) - 1/2*pi*a*c + x*e + d)*log(abs(F))/(4*b^2*c^2*log(abs(F))^2 + (pi*b*c*sgn(F) - pi*b*c + 2*e)^2) + (pi*b*c*sgn(F) - pi*b*c + 2*e)*f*sin(1/2*pi*b*c*x*sgn(F) - 1/2*pi*b*c*x + 1/2*pi*a*c*sgn(F) - 1/2*pi*a*c + x*e + d)/(4*b^2*c^2*log(abs(F))^2 + (pi*b*c*sgn(F) - pi*b*c + 2*e)^2))*e^(b*c*x*log(abs(F)) + a*c*log(abs(F))) + (2*b*c*f*cos(1/2*pi*b*c*x*sgn(F) - 1/2*pi*b*c*x + 1/2*pi*a*c*sgn(F) - 1/2*pi*a*c - x*e - d)*log(abs(F))/(4*b^2*c^2*log(abs(F))^2 + (pi*b*c*sgn(F) - pi*b*c - 2*e)^2) + (pi*b*c*sgn(F) - pi*b*c - 2*e)*f*sin(1/2*pi*b*c*x*sgn(F) - 1/2*pi*b*c*x + 1/2*pi*a*c*sgn(F) - 1/2*pi*a*c - x*e - d)/(4*b^2*c^2*log(abs(F))^2 + (pi*b*c*sgn(F) - pi*b*c - 2*e)^2))*e^(b*c*x*log(abs(F)) + a*c*log(abs(F))) + 2*(2*b*c*f*cos(-1/2*pi*b*c*x*sgn(F) + 1/2*pi*b*c*x - 1/2*pi*a*c*sgn(F) + 1/2*pi*a*c)*log(abs(F))/(4*b^2*c^2*log(abs(F))^2 + (pi*b*c*sgn(F) - pi*b*c)^2) - (pi*b*c*sgn(F) - pi*b*c)*f*sin(-1/2*pi*b*c*x*sgn(F) + 1/2*pi*b*c*x - 1/2*pi*a*c*sgn(F) + 1/2*pi*a*c)/(4*b^2*c^2*log(abs(F))^2 + (pi*b*c*sgn(F) - pi*b*c)^2))*e^(b*c*x*log(abs(F)) + a*c*log(abs(F)))

$$- \frac{1}{2} I \left(-2 I f e^{\left(\frac{1}{2} I \pi b c x \operatorname{sgn}(F) - \frac{1}{2} I \pi b c x + \frac{1}{2} I \pi a c \operatorname{sgn}(F) - \frac{1}{2} I \pi a c + I x e + I d \right) / \left(2 I \pi b c \operatorname{sgn}(F) - 2 I \pi b c + 4 b c \log(\operatorname{abs}(F)) + 4 I e \right)} + 2 I f e^{\left(-\frac{1}{2} I \pi b c x \operatorname{sgn}(F) + \frac{1}{2} I \pi b c x - \frac{1}{2} I \pi a c \operatorname{sgn}(F) + \frac{1}{2} I \pi a c - I x e - I d \right) / \left(-2 I \pi b c \operatorname{sgn}(F) + 2 I \pi b c + 4 b c \log(\operatorname{abs}(F)) - 4 I e \right)} \right) e^{(b c x \log(\operatorname{abs}(F)) + a c \log(\operatorname{abs}(F)))} - \frac{1}{2} I \left(-2 I f e^{\left(\frac{1}{2} I \pi b c x \operatorname{sgn}(F) - \frac{1}{2} I \pi b c x + \frac{1}{2} I \pi a c \operatorname{sgn}(F) - \frac{1}{2} I \pi a c - I x e - I d \right) / \left(2 I \pi b c \operatorname{sgn}(F) - 2 I \pi b c + 4 b c \log(\operatorname{abs}(F)) - 4 I e \right)} + 2 I f e^{\left(-\frac{1}{2} I \pi b c x \operatorname{sgn}(F) + \frac{1}{2} I \pi b c x - \frac{1}{2} I \pi a c \operatorname{sgn}(F) + \frac{1}{2} I \pi a c + I x e + I d \right) / \left(-2 I \pi b c \operatorname{sgn}(F) + 2 I \pi b c + 4 b c \log(\operatorname{abs}(F)) + 4 I e \right)} \right) e^{(b c x \log(\operatorname{abs}(F)) + a c \log(\operatorname{abs}(F)))} - \frac{1}{2} I \left(-2 I f e^{\left(\frac{1}{2} I \pi b c x \operatorname{sgn}(F) - \frac{1}{2} I \pi b c x + \frac{1}{2} I \pi a c \operatorname{sgn}(F) - \frac{1}{2} I \pi a c \right) / \left(I \pi b c \operatorname{sgn}(F) - I \pi b c + 2 b c \log(\operatorname{abs}(F)) \right)} + 2 I f e^{\left(-\frac{1}{2} I \pi b c x \operatorname{sgn}(F) + \frac{1}{2} I \pi b c x - \frac{1}{2} I \pi a c \operatorname{sgn}(F) + \frac{1}{2} I \pi a c \right) / \left(-I \pi b c \operatorname{sgn}(F) + I \pi b c + 2 b c \log(\operatorname{abs}(F)) \right)} \right) e^{(b c x \log(\operatorname{abs}(F)) + a c \log(\operatorname{abs}(F)))}$$

maple [A] time = 0.07, size = 186, normalized size = 1.90

$$\frac{f F^{c(bx+a)}}{bc \ln(F)} + \frac{fbc \ln(F) e^{c(bx+a) \ln(F)}}{\left(1 + \tan^2\left(\frac{d}{2} + \frac{ex}{2}\right)\right) \left(e^2 + b^2 c^2 \ln(F)^2\right)} + \frac{2fe e^{c(bx+a) \ln(F)} \tan\left(\frac{d}{2} + \frac{ex}{2}\right)}{\left(1 + \tan^2\left(\frac{d}{2} + \frac{ex}{2}\right)\right) \left(e^2 + b^2 c^2 \ln(F)^2\right)} - \frac{fbc \ln(F) e^{c(bx+a) \ln(F)}}{\left(1 + \tan^2\left(\frac{d}{2} + \frac{ex}{2}\right)\right) \left(e^2 + b^2 c^2 \ln(F)^2\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(F^(c*(b*x+a))*(f+f*cos(e*x+d)),x)

[Out] $f/b/c/\ln(F)*F^{c*(b*x+a)}+f/(1+\tan(1/2*d+1/2*e*x)^2)*b*c*\ln(F)/(e^2+b^2*c^2*\ln(F)^2)*\exp(c*(b*x+a)*\ln(F))+2*f/(1+\tan(1/2*d+1/2*e*x)^2)/(e^2+b^2*c^2*\ln(F)^2)*e*\exp(c*(b*x+a)*\ln(F))*\tan(1/2*d+1/2*e*x)-f/(1+\tan(1/2*d+1/2*e*x)^2)*b*c*\ln(F)/(e^2+b^2*c^2*\ln(F)^2)*\exp(c*(b*x+a)*\ln(F))*\tan(1/2*d+1/2*e*x)^2$

maxima [B] time = 0.35, size = 216, normalized size = 2.20

$$\frac{\left(F^{ac} bc \cos(d) \log(F) - F^{ac} e \sin(d) \right) F^{bcx} \cos(ex + 2d) + \left(F^{ac} bc \cos(d) \log(F) + F^{ac} e \sin(d) \right) F^{bcx} \cos(ex) + \left(F^{ac} bc \cos(d) \log(F) - F^{ac} e \sin(d) \right) F^{bcx} \cos(ex + 2d) + \left(F^{ac} bc \cos(d) \log(F) + F^{ac} e \sin(d) \right) F^{bcx} \cos(ex)}{2 \left(b^2 c^2 \cos(d)^2 \log(F)^2 + b^2 c^2 \log(F)^2 \sin(d)^2 \right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(F^(c*(b*x+a))*(f+f*cos(e*x+d)),x, algorithm="maxima")

[Out] $1/2*((F^{a*c}*b*c*\cos(d)*\log(F) - F^{a*c}*e*\sin(d))*F^{(b*c*x)*\cos(e*x + 2*d)} + (F^{a*c}*b*c*\cos(d)*\log(F) + F^{a*c}*e*\sin(d))*F^{(b*c*x)*\cos(e*x)} + (F^{a*c}*b*c*\log(F)*\sin(d) + F^{a*c}*e*\cos(d))*F^{(b*c*x)*\sin(e*x + 2*d)} - (F^{a*c}*b*c*\log(F)*\sin(d) - F^{a*c}*e*\cos(d))*F^{(b*c*x)*\sin(e*x)})*f/(b^2*c^2*\cos(d)^2*\log(F)^2 + b^2*c^2*\log(F)^2*\sin(d)^2 + (\cos(d)^2 + \sin(d)^2)*e^2) + F^{(b*c*x + a*c)}*f/(b*c*\log(F))$

mupad [B] time = 2.56, size = 83, normalized size = 0.85

$$\frac{F^{ac+bcx} f \left(e^2 + b^2 c^2 \ln(F)^2 + b^2 c^2 \cos(d + ex) \ln(F)^2 + b c e \sin(d + ex) \ln(F) \right)}{b c \ln(F) \left(b^2 c^2 \ln(F)^2 + e^2 \right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(F^(c*(a + b*x))*(f + f*cos(d + e*x)),x)

[Out] $(F^{a*c + b*c*x}*f*(e^2 + b^2*c^2*\log(F)^2 + b^2*c^2*\cos(d + e*x)*\log(F)^2 + b*c*e*\sin(d + e*x)*\log(F)))/(b*c*\log(F)*(e^2 + b^2*c^2*\log(F)^2))$

sympy [A] time = 7.32, size = 408, normalized size = 4.16

$$\left\{ \begin{array}{ll}
 fx + \frac{f \sin(d+ex)}{e} & \text{for } F = 1 \\
 \tilde{\omega} e^2 f \left(e^{-\frac{ie}{bc}} \right)^{ac} \left(e^{-\frac{ie}{bc}} \right)^{bcx} \sin(d+ex) + \tilde{\omega} e^2 f \left(e^{-\frac{ie}{bc}} \right)^{ac} \left(e^{-\frac{ie}{bc}} \right)^{bcx} \cos(d+ex) & \text{for } F = e^{-\frac{ie}{bc}} \\
 \tilde{\omega} e^2 f \left(e^{\frac{ie}{bc}} \right)^{ac} \left(e^{\frac{ie}{bc}} \right)^{bcx} \sin(d+ex) + \tilde{\omega} e^2 f \left(e^{\frac{ie}{bc}} \right)^{ac} \left(e^{\frac{ie}{bc}} \right)^{bcx} \cos(d+ex) & \text{for } F = e^{\frac{ie}{bc}} \\
 F^{ac} \left(fx + \frac{f \sin(d+ex)}{e} \right) & \text{for } b = 0 \\
 fx + \frac{f \sin(d+ex)}{e} & \text{for } c = 0 \\
 \frac{F^{ac} F^{bcx} b^2 c^2 f \log(F)^2 \cos(d+ex)}{b^3 c^3 \log(F)^3 + b c e^2 \log(F)} + \frac{F^{ac} F^{bcx} b^2 c^2 f \log(F)^2}{b^3 c^3 \log(F)^3 + b c e^2 \log(F)} + \frac{F^{ac} F^{bcx} b c e f \log(F) \sin(d+ex)}{b^3 c^3 \log(F)^3 + b c e^2 \log(F)} + \frac{F^{ac} F^{bcx} e^2 f}{b^3 c^3 \log(F)^3 + b c e^2 \log(F)} & \text{otherwise}
 \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(F**(c*(b*x+a))*(f+f*cos(e*x+d)),x)

[Out] Piecewise((f*x + f*sin(d + e*x)/e, Eq(F, 1)), (zoo*e**2*f*exp(-I*e/(b*c))**
(a*c)*exp(-I*e/(b*c))**
(b*c*x)*sin(d + e*x) + zoo*e**2*f*exp(-I*e/(b*c))**
(a*c)*exp(-I*e/(b*c))**
(b*c*x)*cos(d + e*x), Eq(F, exp(-I*e/(b*c)))), (zoo*e
2*f*exp(I*e/(b*c))
(a*c)*exp(I*e/(b*c))**
(b*c*x)*sin(d + e*x) + zoo*e**2
*f*exp(I*e/(b*c))**
(a*c)*exp(I*e/(b*c))**
(b*c*x)*cos(d + e*x), Eq(F, exp(I*
e/(b*c)))), (F**(a*c)*(f*x + f*sin(d + e*x)/e), Eq(b, 0)), (f*x + f*sin(d +
e*x)/e, Eq(c, 0)), (F**(a*c)*F**(b*c*x)*b**2*c**2*f*log(F)**2*cos(d + e*x)
/(b**3*c**3*log(F)**3 + b*c*e**2*log(F)) + F**(a*c)*F**(b*c*x)*b**2*c**2*f*
log(F)**2/(b**3*c**3*log(F)**3 + b*c*e**2*log(F)) + F**(a*c)*F**(b*c*x)*b*c
*e*f*log(F)*sin(d + e*x)/(b**3*c**3*log(F)**3 + b*c*e**2*log(F)) + F**(a*c)
*F**(b*c*x)*e**2*f/(b**3*c**3*log(F)**3 + b*c*e**2*log(F)), True))

$$3.141 \quad \int \frac{F^{c(a+bx)}}{f+f \cos(d+ex)} dx$$

Optimal. Leaf size=79

$$\frac{2e^{i(d+ex)}F^{c(a+bx)} {}_2F_1\left(2, 1 - \frac{ibc \log(F)}{e}; 2 - \frac{ibc \log(F)}{e}; -e^{i(d+ex)}\right)}{f(bc \log(F) + ie)}$$

[Out] 2*exp(I*(e*x+d))*F^(c*(b*x+a))*hypergeom([2, 1-I*b*c*ln(F)/e], [2-I*b*c*ln(F)/e], -exp(I*(e*x+d)))/f/(b*c*ln(F)+I*e)

Rubi [A] time = 0.06, antiderivative size = 79, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 22, $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$, Rules used = {4457, 4451}

$$\frac{2e^{i(d+ex)}F^{c(a+bx)} {}_2F_1\left(2, 1 - \frac{ibc \log(F)}{e}; 2 - \frac{ibc \log(F)}{e}; -e^{i(d+ex)}\right)}{f(bc \log(F) + ie)}$$

Antiderivative was successfully verified.

[In] Int[F^(c*(a + b*x))/(f + f*Cos[d + e*x]), x]

[Out] (2*E^(I*(d + e*x))*F^(c*(a + b*x))*Hypergeometric2F1[2, 1 - (I*b*c*Log[F])/e, 2 - (I*b*c*Log[F])/e, -E^(I*(d + e*x))]/(f*(I*e + b*c*Log[F]))

Rule 4451

Int[(F_)^((c_)*((a_) + (b_)*(x_)))*Sec[(d_) + (e_)*(x_)]^(n_), x_Symbol] := Simp[(2^n*E^(I*n*(d + e*x))*F^(c*(a + b*x))*Hypergeometric2F1[n, n/2 - (I*b*c*Log[F])/(2*e), 1 + n/2 - (I*b*c*Log[F])/(2*e), -E^(2*I*(d + e*x))]/(I*e*n + b*c*Log[F]), x] /; FreeQ[{F, a, b, c, d, e}, x] && IntegerQ[n]

Rule 4457

Int[(Cos[(d_) + (e_)*(x_)]*(g_) + (f_)]^(n_)*(F_)^((c_)*((a_) + (b_)*(x_))), x_Symbol] := Dist[2^n*f^n, Int[F^(c*(a + b*x))*Cos[d/2 + (e*x)/2]^(2*n), x], x] /; FreeQ[{F, a, b, c, d, e, f, g}, x] && EqQ[f - g, 0] && ILtQ[n, 0]

Rubi steps

$$\begin{aligned} \int \frac{F^{c(a+bx)}}{f+f \cos(d+ex)} dx &= \frac{\int F^{c(a+bx)} \sec^2\left(\frac{d}{2} + \frac{ex}{2}\right) dx}{2f} \\ &= \frac{2e^{i(d+ex)}F^{c(a+bx)} {}_2F_1\left(2, 1 - \frac{ibc \log(F)}{e}; 2 - \frac{ibc \log(F)}{e}; -e^{i(d+ex)}\right)}{f(ie + bc \log(F))} \end{aligned}$$

Mathematica [A] time = 0.05, size = 80, normalized size = 1.01

$$\frac{2ie^{i(d+ex)}F^{c(a+bx)} {}_2F_1\left(2, 1 - \frac{ibc \log(F)}{e}; 2 - \frac{ibc \log(F)}{e}; -e^{i(d+ex)}\right)}{f(e - ibc \log(F))}$$

Antiderivative was successfully verified.

[In] Integrate[F^(c*(a + b*x))/(f + f*Cos[d + e*x]), x]

[Out] $((-2*I)*E^{(I*(d + e*x))*F^{(c*(a + b*x))*Hypergeometric2F1[2, 1 - (I*b*c*Log[F])/e, 2 - (I*b*c*Log[F])/e, -E^{(I*(d + e*x))}]/(f*(e - I*b*c*Log[F]))}$

fricas [F] time = 0.56, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{F^{bcx+ac}}{f \cos(ex + d) + f}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(F^(c*(b*x+a))/(f+f*cos(e*x+d)),x, algorithm="fricas")`

[Out] `integral(F^(b*c*x + a*c)/(f*cos(e*x + d) + f), x)`

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{F^{(bx+a)c}}{f \cos(ex + d) + f} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(F^(c*(b*x+a))/(f+f*cos(e*x+d)),x, algorithm="giac")`

[Out] `integrate(F^((b*x + a)*c)/(f*cos(e*x + d) + f), x)`

maple [F] time = 0.15, size = 0, normalized size = 0.00

$$\int \frac{F^{c(bx+a)}}{f + f \cos(ex + d)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(F^(c*(b*x+a))/(f+f*cos(e*x+d)),x)`

[Out] `int(F^(c*(b*x+a))/(f+f*cos(e*x+d)),x)`

maxima [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(F^(c*(b*x+a))/(f+f*cos(e*x+d)),x, algorithm="maxima")`

[Out] Timed out

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{F^{c(a+bx)}}{f + f \cos(d + ex)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(F^(c*(a + b*x))/(f + f*cos(d + e*x)),x)`

[Out] `int(F^(c*(a + b*x))/(f + f*cos(d + e*x)), x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\frac{\int \frac{F^{ac} F^{bcx}}{\cos(d+ex)+1} dx}{f}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(F**(c*(b*x+a))/(f+f*cos(e*x+d)),x)`

[Out] `Integral(F**(a*c)*F**(b*c*x)/(cos(d + e*x) + 1), x)/f`

$$3.142 \quad \int \frac{F^{c(a+bx)}}{(f+f \cos(d+ex))^2} dx$$

Optimal. Leaf size=169

$$\frac{2e^{i(d+ex)}F^{c(a+bx)}(-bc \log(F) + ie) {}_2F_1\left(2, 1 - \frac{ibc \log(F)}{e}; 2 - \frac{ibc \log(F)}{e}; -e^{i(d+ex)}\right)}{3e^2 f^2} - \frac{bc \log(F) \sec^2\left(\frac{d}{2} + \frac{ex}{2}\right) F^{c(a+bx)} \tan\left(\frac{d}{2} + \frac{ex}{2}\right)}{6e^2 f^2} + \dots$$

[Out] $-2/3*\exp(I*(e*x+d))*F^{(c*(b*x+a))*\text{hypergeom}([2, 1-I*b*c*\ln(F)/e], [2-I*b*c*\ln(F)/e], -\exp(I*(e*x+d)))*(I*e-b*c*\ln(F))/e^2/f^2-1/6*b*c*F^{(c*(b*x+a))*\ln(F)}*\sec(1/2*e*x+1/2*d)^2/e^2/f^2+1/6*F^{(c*(b*x+a))*\sec(1/2*e*x+1/2*d)^2*\tan(1/2*e*x+1/2*d)/e/f^2}$

Rubi [A] time = 0.10, antiderivative size = 169, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 3, integrand size = 22, $\frac{\text{number of rules}}{\text{integrand size}} = 0.136$, Rules used = {4457, 4448, 4451}

$$\frac{2e^{i(d+ex)}F^{c(a+bx)}(-bc \log(F) + ie) {}_2F_1\left(2, 1 - \frac{ibc \log(F)}{e}; 2 - \frac{ibc \log(F)}{e}; -e^{i(d+ex)}\right)}{3e^2 f^2} - \frac{bc \log(F) \sec^2\left(\frac{d}{2} + \frac{ex}{2}\right) F^{c(a+bx)} \tan\left(\frac{d}{2} + \frac{ex}{2}\right)}{6e^2 f^2} + \dots$$

Antiderivative was successfully verified.

[In] Int[F^(c*(a + b*x))/(f + f*Cos[d + e*x])^2,x]

[Out] $(-2*E^{(I*(d + e*x))*F^{(c*(a + b*x))*\text{Hypergeometric2F1}[2, 1 - (I*b*c*\text{Log}[F])/e, 2 - (I*b*c*\text{Log}[F])/e, -E^{(I*(d + e*x))}*(I*e - b*c*\text{Log}[F])]/(3*e^2*f^2) - (b*c*F^{(c*(a + b*x))*\text{Log}[F]*\text{Sec}[d/2 + (e*x)/2]^2)/(6*e^2*f^2) + (F^{(c*(a + b*x))*\text{Sec}[d/2 + (e*x)/2]^2*\text{Tan}[d/2 + (e*x)/2]})/(6*e*f^2)$

Rule 4448

Int[(F_)^(c*(a + b*x))*Sec[(d + e*x)]^(n), x_Symbol] := -Simp[(b*c*Log[F]*F^(c*(a + b*x))*Sec[d + e*x]^(n - 2))/(e^2*(n - 1)*(n - 2)), x] + (Dist[(e^2*(n - 2)^2 + b^2*c^2*Log[F]^2)/(e^2*(n - 1)*(n - 2)), Int[F^(c*(a + b*x))*Sec[d + e*x]^(n - 2), x], x] + Simp[(F^(c*(a + b*x))*Sec[d + e*x]^(n - 1)*Sin[d + e*x]/(e*(n - 1)), x]) /; FreeQ[{F, a, b, c, d, e}, x] && NeQ[b^2*c^2*Log[F]^2 + e^2*(n - 2)^2, 0] && GtQ[n, 1] && NeQ[n, 2]

Rule 4451

Int[(F_)^(c*(a + b*x))*Sec[(d + e*x)]^(n), x_Symbol] := Simp[(2^n*E^(I*n*(d + e*x))*F^(c*(a + b*x))*Hypergeometric2F1[n, n/2 - (I*b*c*Log[F])/(2*e), 1 + n/2 - (I*b*c*Log[F])/(2*e), -E^(2*I*(d + e*x))]/(I*e*n + b*c*Log[F]), x] /; FreeQ[{F, a, b, c, d, e}, x] && IntegerQ[n]

Rule 4457

Int[(Cos[(d + e*x)]*(g + f))^n*(F_)^(c*(a + b*x)), x_Symbol] := Dist[2^n*f^n, Int[F^(c*(a + b*x))*Cos[d/2 + (e*x)/2]^(2*n), x], x] /; FreeQ[{F, a, b, c, d, e, f, g}, x] && EqQ[f - g, 0] && ILtQ[n, 0]

Rubi steps

$$\int \frac{F^{c(a+bx)}}{(f + f \cos(d + ex))^2} dx = \frac{\int F^{c(a+bx)} \sec^4\left(\frac{d}{2} + \frac{ex}{2}\right) dx}{4f^2}$$

$$= -\frac{bcF^{c(a+bx)} \log(F) \sec^2\left(\frac{d}{2} + \frac{ex}{2}\right)}{6e^2 f^2} + \frac{F^{c(a+bx)} \sec^2\left(\frac{d}{2} + \frac{ex}{2}\right) \tan\left(\frac{d}{2} + \frac{ex}{2}\right)}{6ef^2} + \frac{\left(1 + \frac{b^2 c^2}{e^2}\right)}{3e^2 f^2}$$

$$= -\frac{2e^{i(d+ex)} F^{c(a+bx)} {}_2F_1\left(2, 1 - \frac{ibc \log(F)}{e}; 2 - \frac{ibc \log(F)}{e}; -e^{i(d+ex)}\right) (ie - bc \log(F))}{3e^2 f^2} - \frac{bcF^{c(a+bx)}}{3e^2 f^2}$$

Mathematica [A] time = 0.39, size = 145, normalized size = 0.86

$$\frac{2 \cos\left(\frac{1}{2}(d + ex)\right) F^{c(a+bx)} \left(4e^{i(d+ex)} \cos^3\left(\frac{1}{2}(d + ex)\right) (bc \log(F) - ie) {}_2F_1\left(2, 1 - \frac{ibc \log(F)}{e}; 2 - \frac{ibc \log(F)}{e}; -e^{i(d+ex)}\right) - \frac{bcF^{c(a+bx)}}{3e^2 f^2} (\cos(d + ex) + 1)^2\right)}{3e^2 f^2 (\cos(d + ex) + 1)^2}$$

Antiderivative was successfully verified.

[In] Integrate[F^(c*(a + b*x))/(f + f*Cos[d + e*x])^2,x]

[Out] (2*F^(c*(a + b*x))*Cos[(d + e*x)/2]*(-(b*c*Cos[(d + e*x)/2]*Log[F])) + 4*E^(I*(d + e*x))*Cos[(d + e*x)/2]^3*Hypergeometric2F1[2, 1 - (I*b*c*Log[F])/e, 2 - (I*b*c*Log[F])/e, -E^(I*(d + e*x))]*((-I)*e + b*c*Log[F]) + e*Sin[(d + e*x)/2])/(3*e^2*f^2*(1 + Cos[d + e*x])^2)

fricas [F] time = 0.60, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{F^{bcx+ac}}{f^2 \cos(ex + d)^2 + 2f^2 \cos(ex + d) + f^2}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(F^(c*(b*x+a))/(f+f*cos(e*x+d))^2,x, algorithm="fricas")

[Out] integral(F^(b*c*x + a*c)/(f^2*cos(e*x + d)^2 + 2*f^2*cos(e*x + d) + f^2), x)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{F^{(bx+a)c}}{(f \cos(ex + d) + f)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(F^(c*(b*x+a))/(f+f*cos(e*x+d))^2,x, algorithm="giac")

[Out] integrate(F^((b*x + a)*c)/(f*cos(e*x + d) + f)^2, x)

maple [F] time = 0.38, size = 0, normalized size = 0.00

$$\int \frac{F^{c(bx+a)}}{(f + f \cos(ex + d))^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(F^(c*(b*x+a))/(f+f*cos(e*x+d))^2,x)

[Out] int(F^(c*(b*x+a))/(f+f*cos(e*x+d))^2,x)

maxima [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(F^(c*(b*x+a))/(f+f*cos(e*x+d))^2,x, algorithm="maxima")

[Out] Timed out

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{F^{c(a+bx)}}{(f + f \cos(d + ex))^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(F^(c*(a + b*x))/(f + f*cos(d + e*x))^2,x)

[Out] int(F^(c*(a + b*x))/(f + f*cos(d + e*x))^2, x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\frac{\int \frac{F^{ac} F^{bcx}}{\cos^2(d+ex)+2\cos(d+ex)+1} dx}{f^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(F**(c*(b*x+a))/(f+f*cos(e*x+d))**2,x)

[Out] Integral(F**(a*c)*F**(b*c*x)/(cos(d + e*x)**2 + 2*cos(d + e*x) + 1), x)/f**2

Chapter 4

Listing of Grading functions

The following are the current version of the grading functions used for grading the quality of the antiderivative with reference to the optimal antiderivative included in the test suite.

There is a version for Maple and for Mathematica/Rubi. There is a version for grading Sympy and version for use with Sagemath.

The following are links to the current source code.

The following are the listings of source code of the grading functions.

4.0.1 Mathematica and Rubi grading function

```
(* Original version thanks to Albert Rich emailed on 03/21/2017 *)
(* ::Package:: *)

(* ::Subsection:: *)
(*GradeAntiderivative[result,optimal]*)

(* ::Text:: *)
(*If result and optimal are mathematical expressions, *)
(*      GradeAntiderivative[result,optimal] returns*)
(* "F" if the result fails to integrate an expression that*)
(*   is integrable*)
(* "C" if result involves higher level functions than necessary*)
(* "B" if result is more than twice the size of the optimal*)
(*   antiderivative*)
(* "A" if result can be considered optimal*)

GradeAntiderivative[result_,optimal_] :=
  If[ExpnType[result]<=ExpnType[optimal],
    If[FreeQ[result,Complex] || Not[FreeQ[optimal,Complex]],
      If[LeafCount[result]<=2*LeafCount[optimal],
        "A",
        "B"],
      "C"],
    If[FreeQ[result,Integrate] && FreeQ[result,Int],
      "C",
      "F"]]

(* ::Text:: *)
(*The following summarizes the type number assigned an *)
(*expression based on the functions it involves*)
(*1 = rational function*)
(*2 = algebraic function*)
```

```

(*3 = elementary function*)
(*4 = special function*)
(*5 = hyperpergeometric function*)
(*6 = appell function*)
(*7 = rootsum function*)
(*8 = integrate function*)
(*9 = unknown function*)

ExpnType[expn_] :=
  If[AtomQ[expn],
    1,
  If[ListQ[expn],
    Max[Map[ExpnType, expn]],
  If[Head[expn]===Power,
    If[IntegerQ[expn[[2]]],
      ExpnType[expn[[1]]],
    If[Head[expn[[2]]]===Rational,
      If[IntegerQ[expn[[1]]] || Head[expn[[1]]]===Rational,
        1,
        Max[ExpnType[expn[[1]], 2]],
      Max[ExpnType[expn[[1]], ExpnType[expn[[2]], 3]],
    If[Head[expn]===Plus || Head[expn]===Times,
      Max[ExpnType[First[expn]], ExpnType[Rest[expn]]],
    If[ElementaryFunctionQ[Head[expn]],
      Max[3, ExpnType[expn[[1]]],
    If[SpecialFunctionQ[Head[expn]],
      Apply[Max, Append[Map[ExpnType, Apply[List, expn]], 4]],
    If[HypergeometricFunctionQ[Head[expn]],
      Apply[Max, Append[Map[ExpnType, Apply[List, expn]], 5]],
    If[AppellFunctionQ[Head[expn]],
      Apply[Max, Append[Map[ExpnType, Apply[List, expn]], 6]],
    If[Head[expn]===RootSum,
      Apply[Max, Append[Map[ExpnType, Apply[List, expn]], 7]],
    If[Head[expn]===Integrate || Head[expn]===Int,
      Apply[Max, Append[Map[ExpnType, Apply[List, expn]], 8]],
    9]]]]]]]]]]

ElementaryFunctionQ[func_] :=
  MemberQ[{
    Exp, Log,
    Sin, Cos, Tan, Cot, Sec, Csc,
    ArcSin, ArcCos, ArcTan, ArcCot, ArcSec, ArcCsc,
    Sinh, Cosh, Tanh, Coth, Sech, Csch,
    ArcSinh, ArcCosh, ArcTanh, ArcCoth, ArcSech, ArcCsch
  }, func]

SpecialFunctionQ[func_] :=
  MemberQ[{
    Erf, Erfc, Erfi,
    FresnelS, FresnelC,
    ExpIntegralE, ExpIntegralEi, LogIntegral,
    SinIntegral, CosIntegral, SinhIntegral, CoshIntegral,
    Gamma, LogGamma, PolyGamma,
    Zeta, PolyLog, ProductLog,
    EllipticF, EllipticE, EllipticPi
  }, func]

HypergeometricFunctionQ[func_] :=
  MemberQ[{Hypergeometric1F1, Hypergeometric2F1, HypergeometricPFQ}, func]

```

```
AppellFunctionQ[func_] :=
  MemberQ[{AppellF1},func]
```

4.0.2 Maple grading function

```
# File: GradeAntiderivative.mpl
# Original version thanks to Albert Rich emailed on 03/21/2017

#Nasser 03/22/2017 Use Maple leaf count instead since buildin
#Nasser 03/23/2017 missing 'ln' for ElementaryFunctionQ added
#Nasser 03/24/2017 corrected the check for complex result
#Nasser 10/27/2017 check for leafsize and do not call ExpnType()
#
# if leaf size is "too large". Set at 500,000
#Nasser 12/22/2019 Added debug flag, added 'dilog' to special functions
#
# see problem 156, file Apostol_Problems

GradeAntiderivative := proc(result,optimal)
local leaf_count_result, leaf_count_optimal,ExpnType_result,ExpnType_optimal,
  debug:=false;

  leaf_count_result:=leafcount(result);
  #do NOT call ExpnType() if leaf size is too large. Recursion problem
  if leaf_count_result > 500000 then
    return "B";
  fi;

  leaf_count_optimal:=leafcount(optimal);

  ExpnType_result:=ExpnType(result);
  ExpnType_optimal:=ExpnType(optimal);

  if debug then
    print("ExpnType_result",ExpnType_result," ExpnType_optimal=",
ExpnType_optimal);
  fi;

# If result and optimal are mathematical expressions,
# GradeAntiderivative[result,optimal] returns
# "F" if the result fails to integrate an expression that
# is integrable
# "C" if result involves higher level functions than necessary
# "B" if result is more than twice the size of the optimal
# antiderivative
# "A" if result can be considered optimal

#This check below actually is not needed, since I only
#call this grading only for passed integrals. i.e. I check
#for "F" before calling this. But no harm of keeping it here.
#just in case.

if not type(result,freeof('int')) then
  return "F";
end if;

if ExpnType_result<=ExpnType_optimal then
  if debug then
    print("ExpnType_result<=ExpnType_optimal");
  fi;

```

```

if is_contains_complex(result) then
  if is_contains_complex(optimal) then
    if debug then
      print("both result and optimal complex");
    fi;
    #both result and optimal complex
    if leaf_count_result<=2*leaf_count_optimal then
      return "A";
    else
      return "B";
    end if
  else #result contains complex but optimal is not
    if debug then
      print("result contains complex but optimal is not");
    fi;
    return "C";
  end if
else # result do not contain complex
  # this assumes optimal do not as well
  if debug then
    print("result do not contain complex, this assumes optimal do
not as well");
  fi;
  if leaf_count_result<=2*leaf_count_optimal then
    if debug then
      print("leaf_count_result<=2*leaf_count_optimal");
    fi;
    return "A";
  else
    if debug then
      print("leaf_count_result>2*leaf_count_optimal");
    fi;
    return "B";
  end if
end if
else #ExpnType(result) > ExpnType(optimal)
  if debug then
    print("ExpnType(result) > ExpnType(optimal)");
  fi;
  return "C";
end if

end proc:

#
# is_contains_complex(result)
# takes expressions and returns true if it contains "I" else false
#
#Nasser 032417
is_contains_complex:= proc(expression)
  return (has(expression,I));
end proc:

# The following summarizes the type number assigned an expression
# based on the functions it involves
# 1 = rational function
# 2 = algebraic function
# 3 = elementary function
# 4 = special function
# 5 = hyperpergeometric function
# 6 = appell function
# 7 = rootsum function
# 8 = integrate function

```

```

# 9 = unknown function

ExpnType := proc(expn)
  if type(expn,'atomic') then
    1
  elif type(expn,'list') then
    apply(max,map(ExpnType,expn))
  elif type(expn,'sqrt') then
    if type(op(1,expn),'rational') then
      1
    else
      max(2,ExpnType(op(1,expn)))
    end if
  elif type(expn,'^^') then
    if type(op(2,expn),'integer') then
      ExpnType(op(1,expn))
    elif type(op(2,expn),'rational') then
      if type(op(1,expn),'rational') then
        1
      else
        max(2,ExpnType(op(1,expn)))
      end if
    else
      max(3,ExpnType(op(1,expn)),ExpnType(op(2,expn)))
    end if
  elif type(expn,'+' or type(expn,'*') then
    max(ExpnType(op(1,expn)),max(ExpnType(rest(expn))))
  elif ElementaryFunctionQ(op(0,expn)) then
    max(3,ExpnType(op(1,expn)))
  elif SpecialFunctionQ(op(0,expn)) then
    max(4,apply(max,map(ExpnType,[op(expn)])))
  elif HypergeometricFunctionQ(op(0,expn)) then
    max(5,apply(max,map(ExpnType,[op(expn)])))
  elif AppellFunctionQ(op(0,expn)) then
    max(6,apply(max,map(ExpnType,[op(expn)])))
  elif op(0,expn)='int' then
    max(8,apply(max,map(ExpnType,[op(expn)]))) else
    9
  end if
end proc:

ElementaryFunctionQ := proc(func)
  member(func,[
    exp,log,ln,
    sin,cos,tan,cot,sec,csc,
    arcsin,arccos,arctan,arccot,arcsec,arccsc,
    sinh,cosh,tanh,coth,sech,csch,
    arcsinh,arccosh,arctanh,arccoth,arcsech,arccsch])
end proc:

SpecialFunctionQ := proc(func)
  member(func,[
    erf,erfc,erfi,
    FresnelS,FresnelC,
    Ei,Ei,Li,Si,Ci,Shi,Chi,
    GAMMA,lnGAMMA,Psi,Zeta,polylog,dilog,LambertW,
    EllipticF,EllipticE,EllipticPi])
end proc:

HypergeometricFunctionQ := proc(func)
  member(func,[Hypergeometric1F1,hypergeom,HypergeometricPFQ])
end proc:

```

```

AppellFunctionQ := proc(func)
  member(func,[AppellF1])
end proc:

# u is a sum or product. rest(u) returns all but the
# first term or factor of u.
rest := proc(u) local v;
  if nops(u)=2 then
    op(2,u)
  else
    apply(op(0,u),op(2..nops(u),u))
  end if
end proc:

#leafcount(u) returns the number of nodes in u.
#Nasser 3/23/17 Replaced by build-in leafCount from package in Maple
leafcount := proc(u)
  MmaTranslator[Mma][LeafCount](u);
end proc:

```

4.0.3 Sympy grading function

```

#Dec 24, 2019. Nasser M. Abbasi:
#           Port of original Maple grading function by
#           Albert Rich to use with Sympy/Python
#Dec 27, 2019 Nasser. Added `RootSum`. See problem 177, Timofeev file
#           added 'exp_polar'
from sympy import *

def leaf_count(expr):
  #sympy do not have leaf count function. This is approximation
  return round(1.7*count_ops(expr))

def is_sqrt(expr):
  if isinstance(expr,Pow):
    if expr.args[1] == Rational(1,2):
      return True
    else:
      return False
  else:
    return False

def is_elementary_function(func):
  return func in [exp,log,ln,sin,cos,tan,cot,sec,csc,
    asin,acos,atan,acot,asec,acsc,sinh,cosh,tanh,coth,sech,csch,
    asinh,acosh,atanh,acoth,asech,acsch
  ]

def is_special_function(func):
  return func in [ erf,erfc,erfi,
    fresnels,fresnelc,Ei,Ei,Li,Si,Ci,Shi,Chi,
    gamma,loggamma,digamma,zeta,polylog,LambertW,
    elliptic_f,elliptic_e,elliptic_pi,exp_polar
  ]

def is_hypergeometric_function(func):
  return func in [hyper]

def is_appell_function(func):
  return func in [appellf1]

```



```

def is_atom(expn):
    try:
        if expn.isAtom or isinstance(expn,int) or isinstance(expn,float):
            return True
        else:
            return False

    except AttributeError as error:
        return False

def expnType(expn):
    debug=False
    if debug:
        print("expn=",expn,"type(expn)=",type(expn))

    if is_atom(expn):
        return 1
    elif isinstance(expn,list):
        return max(map(expnType, expn)) #apply(max,map(ExpnType,expn))
    elif is_sqrt(expn):
        if isinstance(expn.args[0],Rational): #type(op(1,expn),'rational')
            return 1
        else:
            return max(2,expnType(expn.args[0])) #max(2,ExpnType(op(1,expn)))
    elif isinstance(expn,Pow): #type(expn,'^^')
        if isinstance(expn.args[1],Integer): #type(op(2,expn),'integer')
            return expnType(expn.args[0]) #ExpnType(op(1,expn))
        elif isinstance(expn.args[1],Rational): #type(op(2,expn),'rational')
            if isinstance(expn.args[0],Rational): #type(op(1,expn),'rational')
                return 1
            else:
                return max(2,expnType(expn.args[0])) #max(2,ExpnType(op(1,expn)))
    elif isinstance(expn,Add) or isinstance(expn,Mul): #type(expn,'+`' or
    type(expn,'*`)
        m1 = expnType(expn.args[0])
        m2 = expnType(list(expn.args[1:]))
        return max(m1,m2) #max(ExpnType(op(1,expn)),max(ExpnType(rest(expn))))
    elif is_elementary_function(expn.func): #ElementaryFunctionQ(op(0,expn))
        return max(3,expnType(expn.args[0])) #max(3,ExpnType(op(1,expn)))
    elif is_special_function(expn.func): #SpecialFunctionQ(op(0,expn))
        m1 = max(map(expnType, list(expn.args)))
        return max(4,m1) #max(4,apply(max,map(ExpnType,[op(expn)])))
    elif is_hypergeometric_function(expn.func): #HypergeometricFunctionQ(op(0,
    expn))
        m1 = max(map(expnType, list(expn.args)))
        return max(5,m1) #max(5,apply(max,map(ExpnType,[op(expn)])))
    elif is_appell_function(expn.func):
        m1 = max(map(expnType, list(expn.args)))
        return max(6,m1) #max(5,apply(max,map(ExpnType,[op(expn)])))
    elif isinstance(expn,RootSum):
        m1 = max(map(expnType, list(expn.args))) #Apply[Max,Append[Map[ExpnType
    ,Apply[List,expn]],7]],
        return max(7,m1)
    elif str(expn).find("Integral") != -1:
        m1 = max(map(expnType, list(expn.args)))
        return max(8,m1) #max(5,apply(max,map(ExpnType,[op(expn)])))
    else:
        return 9

```

```

#main function
def grade_antiderivative(result,optimal):

    leaf_count_result = leaf_count(result)
    leaf_count_optimal = leaf_count(optimal)

    expnType_result = expnType(result)
    expnType_optimal = expnType(optimal)

    if str(result).find("Integral") != -1:
        return "F"

    if expnType_result <= expnType_optimal:
        if result.has(I):
            if optimal.has(I): #both result and optimal complex
                if leaf_count_result <= 2*leaf_count_optimal:
                    return "A"
                else:
                    return "B"
            else: #result contains complex but optimal is not
                return "C"
        else: # result do not contain complex, this assumes optimal do not as
well
            if leaf_count_result <= 2*leaf_count_optimal:
                return "A"
            else:
                return "B"
    else:
        return "C"

```

4.0.4 SageMath grading function

```

#Dec 24, 2019. Nasser: Ported original Maple grading function by
#           Albert Rich to use with Sagemath. This is used to
#           grade Fricas, Giac and Maxima results.
#Dec 24, 2019. Nasser: Added 'exp_integral_e' and 'sng', 'sin_integral'
#           'arctan2','floor','abs','log_integral'

from sage.all import *
from sage.symbolic.operators import add_vararg, mul_vararg

debug=False;

def tree_size(expr):
    r"""
    Return the tree size of this expression.
    """
    if expr not in SR:
        # deal with lists, tuples, vectors
        return 1 + sum(tree_size(a) for a in expr)
    expr = SR(expr)
    x, aa = expr.operator(), expr.operands()
    if x is None:
        return 1
    else:
        return 1 + sum(tree_size(a) for a in aa)

def is_sqrt(expr):
    if expr.operator() == operator.pow: #isinstance(expr,Pow):
        if expr.operands()[1]==1/2: #expr.args[1] == Rational(1,2):
            if debug: print ("expr is sqrt")
            return True

```

```

        else:
            return False
    else:
        return False

def is_elementary_function(func):
    debug=False
    m = func.name() in ['exp','log','ln',
        'sin','cos','tan','cot','sec','csc',
        'arcsin','arccos','arctan','arccot','arcsec','arccsc',
        'sinh','cosh','tanh','coth','sech','csch',
        'arcsinh','arccosh','arctanh','arccoth','arcsech','arccsch','sgn',
        'arctan2','floor','abs'
    ]
    if debug:
        if m:
            print ("func ", func , " is elementary_function")
        else:
            print ("func ", func , " is NOT elementary_function")

    return m

def is_special_function(func):
    debug=False
    if debug: print ("type(func)=", type(func))

    m= func.name() in ['erf','erfc','erfi','fresnel_sin','fresnel_cos','Ei',
        'Ei','Li','Si','sin_integral','Ci','cos_integral','Shi','
sinh_integral'
        'Chi','cosh_integral','gamma','log_gamma','psi,zeta',
        'polylog','lambert_w','elliptic_f','elliptic_e',
        'elliptic_pi','exp_integral_e','log_integral']

    if debug:
        print ("m=",m)
        if m:
            print ("func ", func ," is special_function")
        else:
            print ("func ", func ," is NOT special_function")

    return m

def is_hypergeometric_function(func):
    return func.name() in ['hypergeometric','hypergeometric_M','
hypergeometric_U']

def is_appell_function(func):
    return func.name() in ['hypergeometric']    #[appellf1] can't find this in
sagemath

def is_atom(expn):

    debug=False
    if debug: print ("Enter is_atom")

    #thanks to answer at https://ask.sagemath.org/question/49179/what-is-
sagemath-equivalent-to-atomic-type-in-maple/
    try:
        if expn.parent() is SR:

```

```

        return expn.operator() is None
    if expn.parent() in (ZZ, QQ, AA, QQbar):
        return expn in expn.parent() # Should always return True
    if hasattr(expn.parent(),"base_ring") and hasattr(expn.parent(),"gens")
:
        return expn in expn.parent().base_ring() or expn in expn.parent().
gens()
    return False

except AttributeError as error:
    return False

def expnType(expn):

    if debug:
        print(">>>>Enter expnType, expn=", expn)
        print(">>>>is_atom(expn)=", is_atom(expn))

    if is_atom(expn):
        return 1
    elif type(expn)==list: #instance(expn,list):
        return max(map(expnType, expn)) #apply(max,map(ExpnType,expn))
    elif is_sqrt(expn):
        if type(expn.operands()[0])==Rational: #type(instance(expn.args[0],
Rational):
            return 1
        else:
            return max(2,expnType(expn.operands()[0])) #max(2,expnType(expn.
args[0]))
    elif expn.operator() == operator.pow: #instance(expn,Pow)
        if type(expn.operands()[1])==Integer: #instance(expn.args[1],Integer
)
            return expnType(expn.operands()[0]) #expnType(expn.args[0])
        elif type(expn.operands()[1])==Rational: #instance(expn.args[1],
Rational)
            if type(expn.operands()[0])==Rational: #instance(expn.args[0],
Rational)
                return 1
            else:
                return max(2,expnType(expn.operands()[0])) #max(2,expnType(
expn.args[0]))
        else:
            return max(3,expnType(expn.operands()[0]),expnType(expn.operands(
[1])) #max(3,expnType(expn.operands()[0]),expnType(expn.operands()[1]))
    elif expn.operator() == add_vararg or expn.operator() == mul_vararg: #
instance(expn,Add) or instance(expn,Mul)
        m1 = expnType(expn.operands()[0]) #expnType(expn.args[0])
        m2 = expnType(expn.operands()[1:]) #expnType(list(expn.args[1:]))
        return max(m1,m2) #max(ExpnType(op(1,expn)),max(ExpnType(rest(expn)))
    elif is_elementary_function(expn.operator()): #is_elementary_function(expn
.func)
        return max(3,expnType(expn.operands()[0]))
    elif is_special_function(expn.operator()): #is_special_function(expn.func)
        m1 = max(map(expnType, expn.operands())) #max(map(expnType, list(
expn.args)))
        return max(4,m1) #max(4,m1)
    elif is_hypergeometric_function(expn.operator()): #
is_hypergeometric_function(expn.func)
        m1 = max(map(expnType, expn.operands())) #max(map(expnType, list(
expn.args)))
        return max(5,m1) #max(5,m1)
    elif is_appell_function(expn.operator()):

```

```

        m1 = max(map(expnType, expn.operands()))      #max(map(expnType, list(
expn.args)))
        return max(6,m1)      #max(6,m1)
    elif str(expn).find("Integral") != -1: #this will never happen, since it
        #is checked before calling the grading function that is passed.
        #but kept it here.
        m1 = max(map(expnType, expn.operands()))      #max(map(expnType, list(
expn.args)))
        return max(8,m1)      #max(5,apply(max,map(ExpnType,[op(expn)])))
    else:
        return 9

#main function
def grade_antiderivative(result,optimal):

    if debug: print ("Enter grade_antiderivative for sagemath")

    leaf_count_result = tree_size(result) #leaf_count(result)
    leaf_count_optimal = tree_size(optimal) #leaf_count(optimal)

    if debug: print ("leaf_count_result=", leaf_count_result, "
leaf_count_optimal=",leaf_count_optimal)

    expnType_result = expnType(result)
    expnType_optimal = expnType(optimal)

    if debug: print ("expnType_result=", expnType_result, "expnType_optimal=",
expnType_optimal)

    if expnType_result <= expnType_optimal:
        if result.has(I):
            if optimal.has(I): #both result and optimal complex
                if leaf_count_result <= 2*leaf_count_optimal:
                    return "A"
                else:
                    return "B"
            else: #result contains complex but optimal is not
                return "C"
        else: # result do not contain complex, this assumes optimal do not as
well
            if leaf_count_result <= 2*leaf_count_optimal:
                return "A"
            else:
                return "B"
    else:
        return "C"

```